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**Flame-flow interaction during premixed and stratified swirl flame
flashback in an annular swirl combustor**

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Rakesh Ranjan

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Dedication

Dedicated to my parents who supported me in my endeavor despite all the odds

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Abstract

Flame-flow interaction during premixed and stratified flame flashback in an annular combustor

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The interaction between a propagating flame and the approach flow is critical to the understanding of boundary layer flashback of swirling flames. In this work, I investigated this interaction during flashback using high-speed luminosity imaging and simultaneous three-dimensional particle image velocimetry. The mean axial velocity through the mixing tube is kept at 2.5 m/s while the hydrogen enrichment of the fuel is varied up to 87%. These flashback experiments are conducted at pressures ranging from 1 to 5 atm.

To understand the flame-flow interaction physics, I developed a novel analysis methodology for low-turbulence fully-premixed methane-air swirl flame flashback, by stacking the planar flame profiles and three-dimensional velocity data. In the quasi-reconstructed velocity field, the motion of an approaching fluid parcel is analyzed in the frame-of-reference of the propagating flame. For the first time, the role of inertial forces in swirling flame-flow interaction is revealed.

Subsequently, I investigated the effect of fuel-air partial premixing on the flashback behavior at atmospheric and elevated pressures. A swirler-based fuel-injection system was used to create fuel-air stratification in the radial direction. For elevated pressure

measurements, an optically accessible elevated pressure chamber was designed and constructed to conduct flashback experiments up to 5 atm. The spatial distribution of the equivalence ratio under non-reacting conditions was investigated using planar laser-induced fluorescence with acetone as the fuel tracer. It was observed that fuel-air pockets were distributed across the mixing tube width, although in an average sense, the fuel-air mixture was radially stratified. The global behavior of upstream flame propagation is reported for different levels of hydrogen-enrichment. For stratified hydrogen-rich flashback, the propagation path of the flame changes from the inner wall to outer wall induced by the faster chemistry of stoichiometric mixtures that are frequently present near the outer wall. This behavior of hydrogen-rich flashback persists even at elevated pressures up to 5 atm, although the propagation of the flame occurs as a wide flame tongue as opposed to the acute-tipped flame structures present in the atmospheric cases.

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CHAPTER 1 : INTRODUCTION

Stringent emission restrictions on the power generation industry has led to a renewed focus on clean energy research. One of the attractive ways to reduce the carbon footprint of gas-turbine power plants is to blend hydrogen into the fuel [1]. However, combustors designed for natural gas are not necessarily suitable for hydrogen-rich fuel since the faster kinetics, lower density and higher diffusivity of hydrogen alter their performance. Thus, accommodation of hydrogen-rich fuel in gas turbine power plants necessitates combustor designs that can operate stably on fuels with variable composition. The fuel flexibility of combustors is a challenging task since the dynamic properties of the flame show significant variation with different percentages of hydrogen. The fuel flexibility can also lead to problems such as flashback and blow off [2].

During flashback, an erstwhile stable flame propagates upstream into the mixing tube, which may lead to the flame stabilizing inside the mixing tube; however, the mixing tube components are usually not designed for high-temperature conditions and so may become damaged by the presence of the flame. The resulting loss of mechanical integrity could alter the combustor's performance and efficiency. For high-hydrogen fuel air premixtures, this situation can lead to potentially catastrophic conditions. Figure 1-1 illustrates the thermal damage incurred on the center-body of a combustor due to flashback [3], [4].

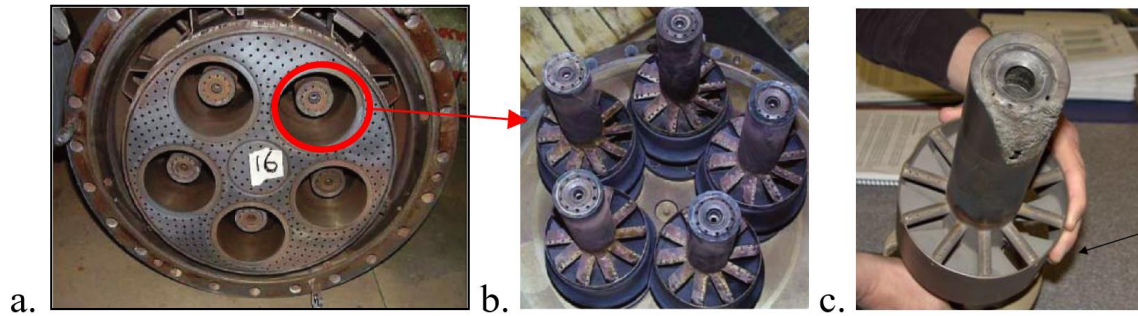


Figure 1-1 a. Section view of the gas turbine combustor assembly. b. Swirlers and the center-bodies in healthy condition c. Mechanical damage on the center-body due to flashback. [4]

1.1 Literature Review

Flashback has been an active area of research for decades [5][6]. Most of the work is relevant to industry needs and has focused on understanding flashback propensity and its dependence on physical factors such as the tip temperature, swirl strength, geometry, and hydrogen enrichment. In the last ten years, the focus of flashback research has shifted toward understanding flame propagation using high-speed imaging, laser diagnostics and numerical simulations. This thesis belongs to this line of research and hence we first review the flame propagation mechanisms.

1.1.1 FLAME PROPAGATION

When the fuel and the oxidizer streams are well-mixed in a proportion such that it would instantly ignite on providing some ignition source, the mixture is said to be flammable. On the other hand, if the fuel or air is in excess such that no flame propagation is achieved, the mixture is considered non-flammable. When the flame propagates through a flammable mixture, it propagates like a wave that processes the unburnt reactants into burnt products. Propagation behavior of such flames depend on several factors such as

combustion chemistry, strain rates, turbulence, ambient pressure, and temperature of the reactants. In the next two subsections, we will review premixed flame propagation in laminar and turbulent flows. We will also discuss how in certain flow configurations, such as vortex flows, there might be faster propagation of the flame that cannot be modelled as turbulent propagation.

1.1.1.1 Laminar premixed flame propagation

The laminar flame speed (S_L) of a flammable fuel-air mixture is the speed with which a flame would progress in a quiescent homogenous mixture under adiabatic conditions. Under laminar, homogeneous, and one-dimensional conditions, the laminar flame speed (S_{L0}) of a planar flame front is governed by its thermo-chemical properties and hence considered a function of the local equivalence ratio (ϕ). In general, flames are two- or three-dimensional and are affected by flame-stretch (κ) [7], [8]. Flame stretch is defined as the rate of change of surface area of a flame element per unit surface area, viz.,

$$\kappa = \frac{1}{A} \frac{dA}{dt}$$

Conventionally, a flame is considered positively stretched for a spherically expanding flame, and negatively stretched for Bunsen flames. The flame stretch may occur due to aerodynamic effects, when the tangential and normal components of velocity stretch the flame surface, or due to curvature of the flame sheet. For a stretched flame, imbalance in convective and diffusive fluxes occur near flame surface; hence, flame stretch can have a significant effect on the flame propagation speed when the fuel and air have different molecular and thermal diffusivities. To quantify the relative role of these two factors, we define Lewis number ($Le = \alpha/D$) as the ratio of thermal diffusivity (α) and mass diffusivity

(D). It has been found that for mixtures with $Le < 1$, the laminar flame speed increases with positive stretch and *vice versa*. The effect of weak stretch (κ) on laminar flame speed is quantified on the basis of the Markstein number (Ma) and unstretched flame thickness (δ_{L0}) as follows:

$$S_{L,\kappa} = S_{L,0} - \kappa Ma \delta_{L0},$$

where, $S_{L,\kappa}$ is the stretched flame speed while $S_{L,0}$ is the unstretched laminar flame speed.

[7]

1.1.1.2 Flame propagation along a vortex axis

Flame propagation along a vortex axis is relevant for swirling flames, especially for flashback studies. These vortices can range from small scales, such as in tubular combustors [9], to large scales, such as in weather cyclones [10]. It has been reported widely by various researchers that the flame propagation in a vortical flow of fuel-air premixture is faster along the axis, even under weak turbulence conditions [11]. This characteristic also manifests itself into flashback in swirl combustors without center-body [12], [13].

Flame propagation along a vortex exhibits higher flame speed along the axis than in the transverse direction. This behavior has been found to exist for straight vortices (two dimensional vortex structures) as well as for vortex rings (vortex structures whose axes are closed curves in space) [14], [15]. The axial flame propagation speed has been found to increase with the maximum azimuthal velocity in the vortex tube, and the density ratio across the flame [11]. In addition, flame propagation along the vortex axis has also found to sustain itself beyond the conventional flammability limits [16]. Figure 1-2 illustrates the

flame propagation along the axes of vortices with different strengths. In the first case, the flow inside a combustion chamber is kept still and a flame kernel was laser-ignited. The flame kernel developed in spherical fashion. This case is illustrated in Figure 1-2(a), where a flame kernel diameter grows to around 10 mm in 300 microseconds. In the other two cases, the flame kernel was ignited in a vortical flow. In Figure 1-2(b), the flame structure developing in a vortex flow, shows larger size in the axial direction of the vortex (y-axis in the figure, ~ 15 mm). For stronger vortex, this propagation along the vortex axis was faster. It should be noted that these vortices are two-dimensional in nature and the axial velocity component is negligible. Hence, in vertical direction the propagation behavior should not have changed. Though, it was noted that the flame propagates faster in vertical direction [17]. The stronger vortex exhibited faster propagation of flame along its axis.

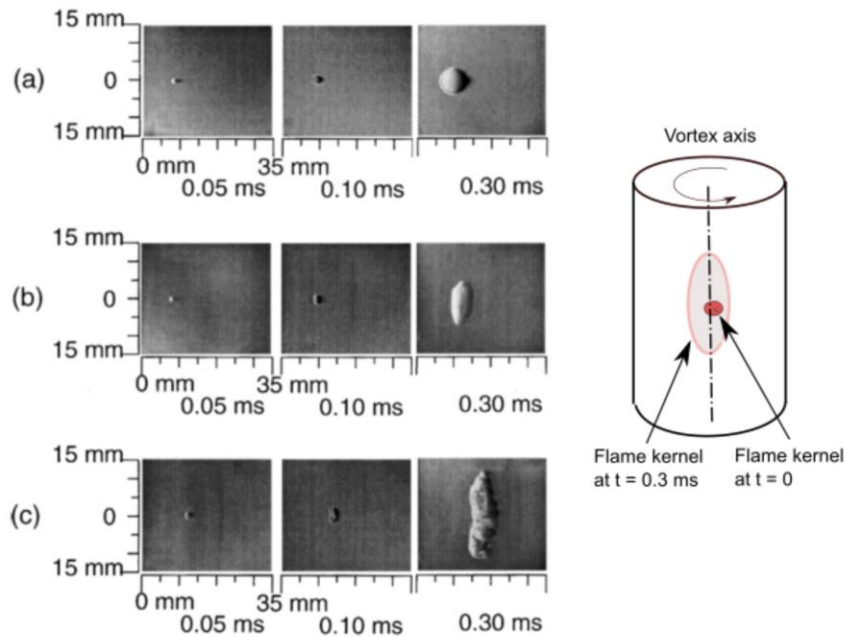


Figure 1-2 Schlieren images of hydrogen-nitrogen- mixture propagating in (a) non-swirling flow, (b) vertical vortex of intermediate strength, and (c) vertical vortex with large strength. The schematic shows the vortex axis and the growth of flame kernel in (c).

An explanation for this behavior is not feasible with one-dimensional picture as developed in the previous subsection. The canonical 1D picture of the flame surface predicts a pressure decrease across the flame due to the density decrease, whereas it has been observed experimentally that the pressure across the vortex flame is higher on the burnt gas side [16]. Researchers have postulated various models to explain the underlying physics for such behavior of the flame surface. Of these, the vortex breakdown model by Chomiak [18] and baroclinic vorticity generation mechanism proposed by Ashurst [19] have generated immense interest. The baroclinic vorticity have been shown to play an important role during the initial phase of propagation [16].

Swirling flame flashback, which occurs along a vortex core, is essentially a specific case of flame propagation along the vortex axis. [20] Even when the flame propagates along the boundary layer of the center-body in an annular combustor, it does so in a swirling environment and factors such as baroclinic vorticity generation have been proposed as an assisting factor for flame propagation [21]. It should be noted that turbulence plays little role in such propagation, whereas aerodynamic factors such as azimuthal velocity have been found to directly affect the flame propagation behavior [16].

1.1.1.3 Turbulent flame propagation

In most practical combustors the flame propagates in a turbulent flow environment. Turbulent premixed flame propagation is generally studied as the movement of a highly-wrinkled flame brush which propagates into the unburnt turbulent mixture [7]. Similar to premixed-laminar flame propagation, where the flame is treated as a wave moving with the laminar flame speed, turbulent-flame propagation is modeled as a wave that moves in space

with a characteristic velocity. To treat the flame brush as a wave, the motion of the mean flame brush is used as the characteristic flame speed, also called the turbulent displacement speed. The turbulent displacement speed of a flame brush is defined as follows,

$$S_{T,D} = (\mathbf{V}_f - \mathbf{V}_g) \cdot \vec{n},$$

where \mathbf{V}_f and \mathbf{V}_g are the average flame brush propagation speed and average unburnt gas speed upstream of the flame, respectively. $S_{T,D}$ refers to the turbulent displacement speed of the flame brush. \vec{n} refers to the mean flame brush normal unit vector. Both velocity vectors are measured in lab-frame. The turbulent displacement flame speed is difficult to measure experimentally; hence, in several applications, an easily measurable quantity, the fuel consumption speed is utilized. For turbulent flames, the global consumption speed ($S_{T,GC}$) is defined as follow:

$$S_{T,GC} = \frac{\dot{m}}{\rho A_{c=0.5}}$$

where \dot{m} is the mass flow rate, ρ is the density of the unburnt reactants, and $A_{c=0.5}$ is the flame brush area corresponding to the mean reacted state. For an unstretched laminar flame, the local fuel consumption speed is the same as the local flame displacement speed. It has been found in various studies that turbulence enhances the flame speed significantly [7], and this effect can be captured with the following relation,

$$\frac{S_T}{S_{Lo}} = f\left(\frac{u'}{S_{Lo}}\right),$$

where u' is the RMS of the velocity fluctuations. S_T and S_{Lo} is the turbulent flame speed and unstretched laminar flame speed respectively. This definition has been found to have substantial variation across different studies. It has been proposed that since the above

formulation doesn't take flame stretch effects into account, it cannot capture the correct physics of turbulent flame propagation [22].

Wrinkling of the flame surface can have dramatic effects on the flame propagation behavior of fuel-air mixtures, especially with Lewis numbers less than unity [7]. Wrinkling of the flame sheet modifies the thermal and diffusion processes, in ways that cannot be accounted for in one-dimensional flame models. For example, convex flame tips (or positively-stretched flames) have a larger supply of unburnt fuel species through diffusion, whereas concave flame surfaces (negatively-stretched flames) have limited access to the fuel. This difference results in higher flame speed at the flame tip and lower flame speed (and possible local extinction) at the flame troughs. This thermo-diffusive effect is generally stronger than the hydrodynamic instability and leads to cellular structure in lean flames.

For lean fuel-air mixtures with Lewis number that is greater than unity, we have the opposite behavior: flame tips with concave curved surfaces will have smaller flame speed, while the concave features on the flame will have higher flame speed. This behavior tends to stabilize the flame surface. For fuel-air mixtures with near unity Lewis numbers, thermo-diffusive effects have only a small effect on the flame structure.

A modified expression for the turbulent flame speed is proposed by Driscoll [23] where the geometry-dependent variation in turbulent speeds was taken into account by including the integral length scale in the streamwise direction (l):

$$\frac{S_T}{S_{Lo}} = f\left(\frac{u'}{S_{Lo}}, \frac{\delta_{Lo}}{l}, Ma\right),$$

where u' is the RMS of the velocity fluctuations. S_T and S_{Lo} is the turbulent flame speed and unstretched laminar flame speed respectively. δ_{Lo} is the flame thickness of unstretched laminar flame. Even after taking these factors in account, a strong quantitative scatter exists among the turbulent speed measurements by various researchers, which suggests that the geometry of the burner and the experimental set up might also have a role in turbulent flame speed measurements. [23]

Recently, it has been suggested by Venkateswaran et al. [24] that for lean hydrogen-air mixtures, the turbulent flame speed scales better with the maximum laminar stretched flame speed, instead of the laminar flame speed. In their justification, they propose that since the flame tip is generally richer than the rest of the flame sheet owing to the diffusion of fuel species, it propagates at the maximum flame speed. They further argue that such leading points dictate the global consumption speed of the turbulent flame brush.

1.1.1.4 Effect of hydrogen-enrichment on premixed flame propagation

Hydrogen enrichment of fuels is a well-established strategy to reduce the carbon footprint of industrial burners. The addition of hydrogen to methane has been studied extensively by previous researchers [25],[26]. These studies concluded that a linear increase in laminar burning velocity is experienced upon the addition of hydrogen, up to the point when the hydrogen content in the fuel is less than 0.7. For hydrogen content greater than 0.85, the rate of increase in flame speed is much steeper. The reasoning for this behavior was proposed that when hydrogen is the dominant fuel species, methane acts as an inhibitive factor for hydrogen chemistry. Later, Di Sarli and Di Benedetto [27] utilized numerical

calculations to quantify three regimes in methane-hydrogen-air mixtures which they described as methane-dominated combustion (H_2 content less than 0.5), transition (H_2 content from 0.5 to 0.9) and methane-inhibited combustion (H_2 content 0.9 and above). These regimes are illustrated in Figure 1-3. It should be noted that a linear interpolation of the laminar flame speeds is not applicable to assess the increase in the laminar flame speed in the transition regime.

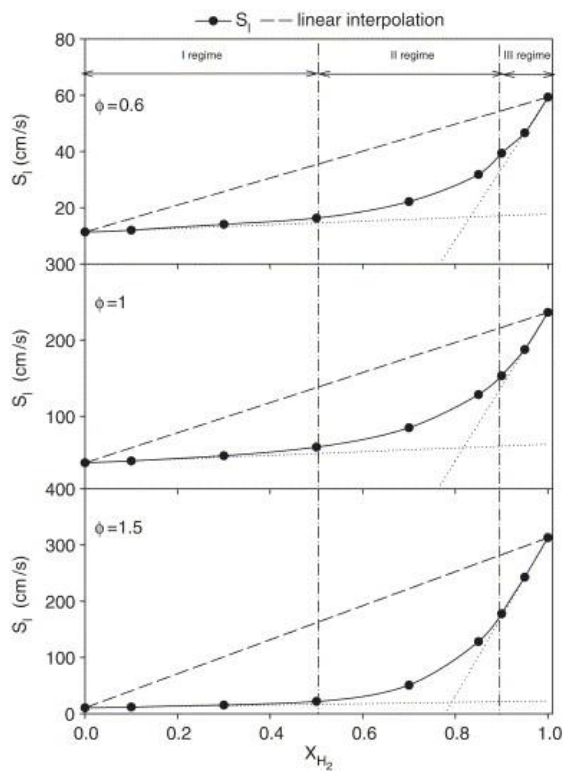


Figure 1-3 Laminar burning velocity of hydrogen–methane/air mixtures as a function of the hydrogen content at NTP conditions. Three regimes are defined for laminar flame speed estimation. ϕ represents the equivalence ratio of the fuel-air mixture.

Hu et al. [28] determined the laminar burning velocity based on spherical-reactor experiments for a range of hydrogen-percentages and equivalence ratios as shown in Figure 1-5. They concluded that for methane-inhibited flow regimes, the combustion is dominated

by H₂ and OH radicals in the reaction zone which show faster chemistry as compared to the methane-dominated regime. In their experiments, they also found the Markstein number (defined in section 1.1.1.1) for a range of hydrogen-content and equivalence ratio. It was shown that for the methane-inhibited regime, the Markstein number is either negative or very close to zero. Wang et al. [29] reported that the effect of hydrogen addition leads to less preference for aldehyde-dominated pathways, thereby reducing the aldehyde emissions in methane combustion. A recent study by Qingfang et al. [30] showed that for methane-rich fuel, CH₃ consumption significantly adds to the global heat release, whereas for hydrogen combustion, H and OH play the most important role.

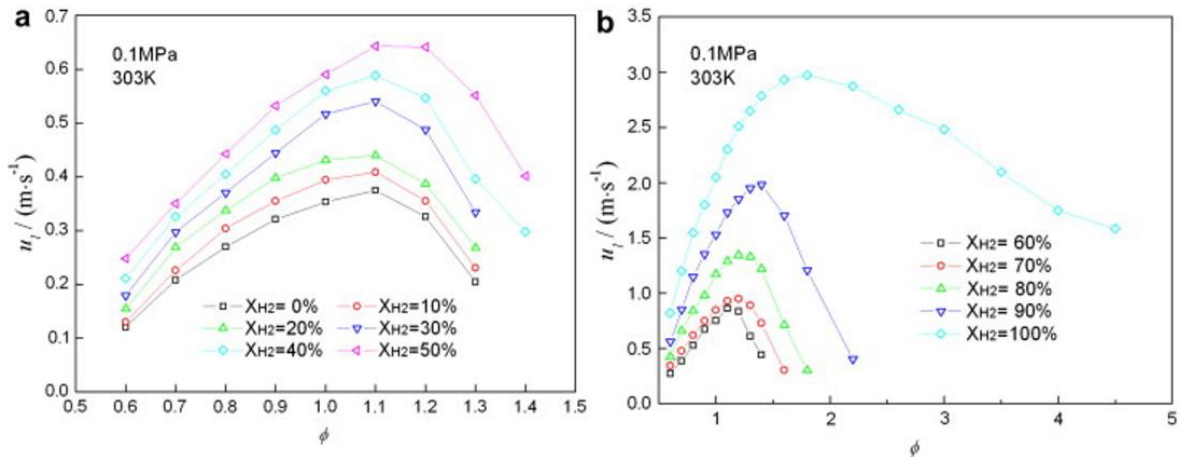


Figure 1-4 Laminar flame speed of methane-hydrogen-air premixtures for different levels of hydrogen enrichment: (a) 0-50%, and (b) 50-100%. X refers to the mole fraction. [31]

1.1.1.5 Effect of pressure on premixed flame propagation

Pressure influences flame propagation in different ways, but one of the most important is that it directly affects the combustion kinetics and hence the laminar flame speed.

Generally, increased pressure leads to reduced laminar flame speeds, and this effect is captured by the following empirical equation [32]:

$$\frac{S_{Lo,p1}}{S_{Lo,p0}} = \left(\frac{p_1}{p_0}\right)^\beta,$$

where $S_{Lo,p1}$ and $S_{Lo,p2}$ are the unstretched laminar flame speeds at pressures p_1 and p_0 , respectively, and β is an empirically-derived exponent. Halter et al.[33] and Gu et al. [34] estimate the value of β to be approximately -0.5 for stoichiometric methane-air mixtures. For richer hydrogen-enriched methane, this value has a lot of scatter in the experimental data. Recently, Moccia and D'Alessio [35] determined the value of β for different percentage of hydrogen up to 30% in hydrogen-methane fuel by conducting spherical flame experiments. They concluded that addition of hydrogen decreased the value of β from -0.45 to -0.40.

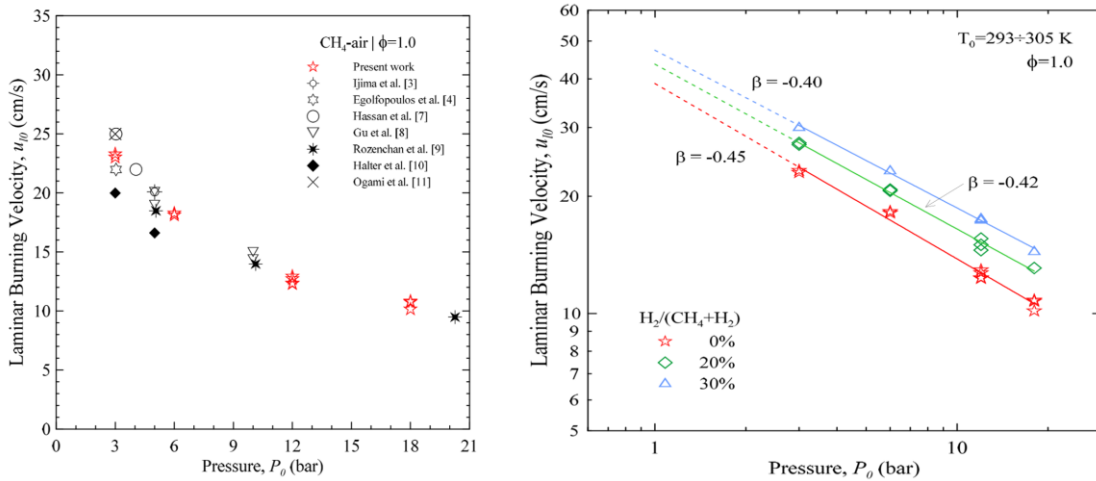


Figure 1-5 a. Variation in laminar burning velocity of methane air stoichiometric mixtures. b. Variation in laminar burning velocity of hydrogen-methane mixtures

Dahoe[36] conducted stoichiometric hydrogen-air flame speed measurements on the basis of pressure traces on the wall of a spherical bomb and determined the value of β to be

0.194, which was smaller than the value 0.43, as found by Iijima and Takeno [37]. Recently, Salzano et al. [38] conducted burning velocity measurements for pressures up to 6 bar and concluded that the exponent β changes its sign from negative to positive for pure hydrogen content..

Pressure also affects other flame characteristics. For example, the flame sheet thickness tends to decrease with increasing pressure due to a decrease in thermal diffusivity [7]. This thinning implies that there are sharper density gradients across the flame front at elevated pressures. Increased density gradients across the flame front can lead to the development of the Darrius-Landau instability, which is known to wrinkle the flame surface. According to its definition, any planar flame across which density changes, is intrinsically unstable, and with time, will develop positively and negatively curved surfaces over entire flame sheet. In this instability, streamline divergence due to the thermal expansion of unburnt gases upstream of the flame front causes a local deceleration of unburnt gases in the vicinity of the flame surface. Owing to this, the flame starts propagating faster in the lab frame of reference. On the other hand, if there is a streamline convergence in front of the flame surface, flame propagation in the lab frame of reference becomes smaller; thus, any initial perturbation grows with time, thereby wrinkling the flame surface.

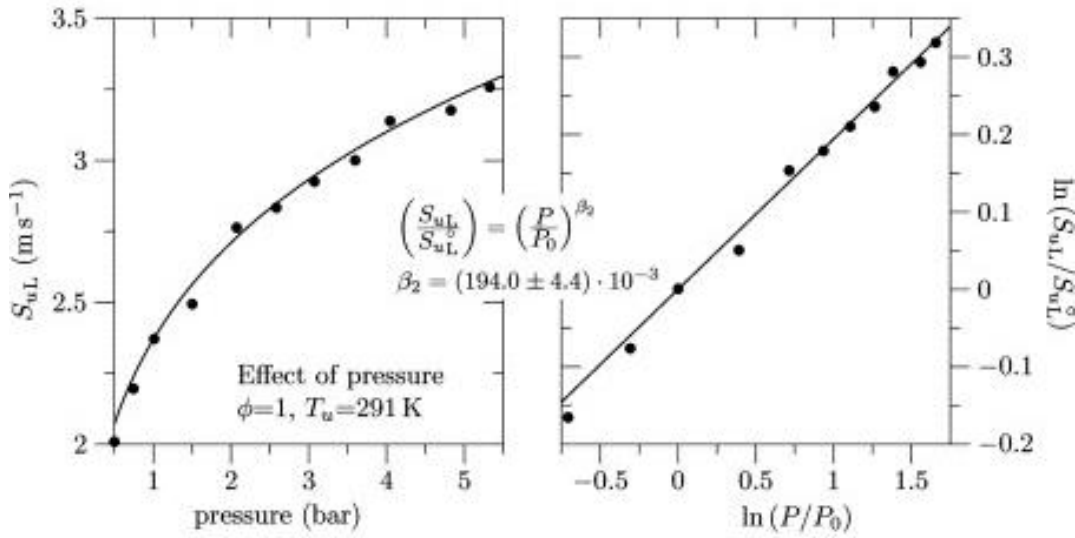


Figure 1-6 Effect of pressure on the laminar burning velocity of hydrogen-air stoichiometric mixtures [32]

1.1.2 PARTIALLY PREMIXED COMBUSTION

Combustion is categorized as ‘partially premixed’ when the fuel-oxidizer mixture is compositionally inhomogeneous. In partially premixed combustion, the flame can be locally diffusion-controlled while at another location on the same flame sheet, the flame might propagate into flammable fuel-air pockets. In order to differentiate between these two flames, Takeno introduced a flame index, which, depending on the local gradient orientation of fuel and oxidizers, differentiates between the premixed and non-premixed combustion [39]. The definition of the Takeno index γ is as follows:

$$\gamma = \frac{\vec{\nabla}Y_F \cdot \vec{\nabla}Y_O}{|\nabla Y_F \cdot \nabla Y_O|}$$

where Y_f and Y_o are the mass fractions of the fuel and oxidizer at the flame sheet, respectively. Takeno index assumes a value of +1 for premixed combustion and -1 for non-premixed combustion. Various improvements have been suggested to modify the Takeno

index to capture partially-premixed combustion characteristics. The measurement of flame index in a reacting flow field provides important insight into the spatial distribution of heat release and radical presence contributed by each type of combustion.

Da Cruz et al. [40] performed a numerical simulation of one-dimensional stratified flame propagation in methane-air mixtures and found that the flame propagates faster when it progresses from stoichiometric to lean premixtures. On the other hand, when the flame progressed from stoichiometric to rich premixtures, it propagated at a slower speed. It was argued that there is a memory effect and the flame propagation depends on the local gradient of equivalence ratio. An enhanced population of H₂ and CO radicals close to the flame surface were thought to be responsible.

Bilger, in his well-cited paper [22], defined stratified combustion as the flame propagation through inhomogeneous fuel air mixtures in which the stoichiometric fuel air mixture doesn't exist at any point in time and space. Lipatnikov follows the same definition in his text book [8]. However, in a recent review paper by Masri [41], stratified combustion has been defined as partially premixed combustion where the flame propagates in a flammable mixture. No distinction for stoichiometric quantities was made in his review paper. In our study, the definition by Masri [41] is followed.

Kang and Kyritsis [42] ran experiments with stratified methane-air mixtures and found the flame propagation speed to be almost twice the laminar flame speed. In addition, it was observed that the flame propagated in conventionally “non-flammable” fuel-air mixtures. These results showed that the flame propagation through a stratified mixture can't be assumed to be quasi-homogenous and there indeed is a memory effect playing a

role in flame propagation. It was suggested that local flame propagation is not just a function of local equivalence ratio (ϕ), but also the gradient of ϕ . In subsequent studies, to define stratification, the alignment angle between the flame progress variable gradient and the local equivalence ratio gradient is used to characterize stratified flames [41]. Stratified flames were differentiated as back-supported vs. front-supported depending on whether the flame is progressing from lean mixture towards the rich ones or the other way around. The flame is said to be back-supported when the fuel-rich burnt gas has an excess of combustion-critical radicals as compared to the unburnt gas. In this case, excess heat and radicals would diffuse across the flame to the preheat zone and would assist in its propagation. On the other hand, if the unburnt gas is richer than the burnt gas, there wouldn't be unidirectional movement of heat and excess radicals. In such a situation, flame propagation may or may not be assisted by the stratification. In general, back-supported flames have higher flame speeds, broader reaction zones and extended flammability limits. Pasquier et al. [43] investigated the flame propagation through stratified propane-air mixtures. In their work, the idea was to experimentally verify the memory effect proposed by Cruz et al. [40]. To generate a stratified fuel-air mixture, an anisole-seeded fuel jet was injected along the diameter of an optically accessible chamber. Jet and air flow rates were maintained at constant flow rates to attain a statistically-steady turbulent flow. Ignition was carried out at a fuel-rich location and the growth of the flame kernel was captured for a few milliseconds using simultaneous PLIF and PIV, as shown in Figure 1-8(b). Based on the flame propagation data conditioned on local equivalence ratio, it was found that when the flame propagated from rich to stoichiometric mixtures, the local flame speed was higher.

It was also noted that when the flame propagated from stoichiometric to lean mixtures, the flame speed was smaller. In the follow-up study in the same laboratory, Balusamy et. al [44] investigated the flame propagation in laminar stratified propane-air mixture. A thorough study on the local flame speed, curvature effects and memory effects were conducted using PLIF-PIV snapshots of the propagating flame, as shown in Figure 1-7(a). It was concluded that stratified propane-air flames propagated faster and are more robust to flame stretch as compared to fully premixed flames.

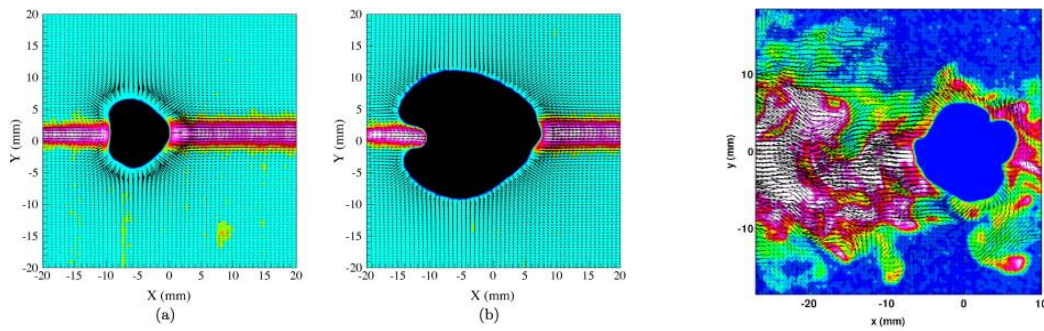


Figure 1-7 Instantaneous velocity and scalar field at two instants of laminar flame propagation at: (a) 1 ms, and (b) 4 ms after ignition. [44] (c) Turbulent stratified flame propagation in a similar experimental set up [43]

Another study was conducted by Galizzi and Escudie [45] to investigate the effect of stratification in a premixed flame brush stabilized on a flame holder. As illustrated in Figure 1-7(a), a V-shaped premixed laminar flame was stabilized in the wake of a flame-holder. A separate fuel nozzle was located asymmetrically upstream of the flame holder, such that the pure fuel flow through the nozzle would create a locally-rich flow on one of the sides of the V-flame. As shown in Figure 1-8(b), the locally-rich flow (blue arrow) led to a separate stagnation point in the flame brush. Also, the flame brush angle was found to be broadened due to the stratification. In a later paper they reported the stratified flame

brush in a turbulent flow [46]. It was observed that a turbulent stratified flame didn't form a separate stagnation point but increased the overall wrinkling in the flame surface. It was also observed that the flame-brush angle was much larger than the premixed branch. Since they did not conduct PLIF imaging in this study, they were not able to quantify the local equivalence ratio and hence no observations could be made regarding conditioned flame displacement speed. However, some of their observations, such as a more wrinkled surface and broader spread of flame brush, were confirmed by subsequent studies done by other researchers [21].

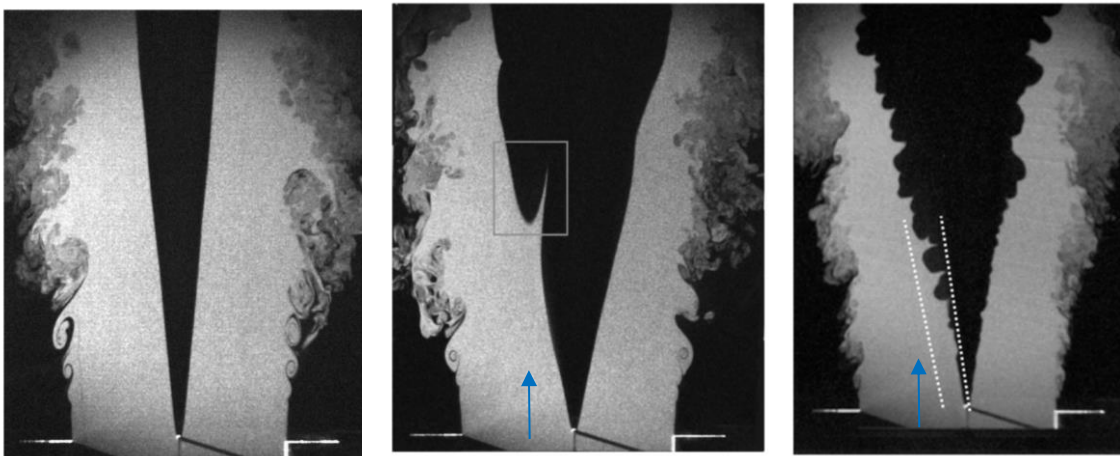


Figure 1-8: a. fully premixed laminar flame in the wake of a flameholder. [21] b. flame profile in stratified laminar conditions c. Flame profile in turbulent stratified conditions. [23] Blue arrow indicates the fuel-rich flow.

1.1.3 FLASHBACK

Flashback is defined as the event during which a stable premixed or stratified flame propagates upstream into the fuel-air mixing zone. Flashback is undesirable for multiple reasons, not only because the flame can stabilize on components that were not designed to withstand the thermal load. During flashback, the flame imposes a blockage effect on the

fuel-air flow, thereby changing the aerodynamics in the combustion chamber. This can lead to acoustic disturbances in the system that may trigger combustion instabilities. In addition, the flame-wall interaction not only reduces the availability of thermal energy for gas turbines but also increases the presence of unburnt radicals. The combustion research community has tried to understand the flashback physics and ways to avoid it, with limited success. In this subsection, we will first discuss the flashback in simple non-swirling flows. We will further consider how swirl affects flame propagation and then the effect of fuel-air stratification on flashback.

1.1.2.1 Flashback in non-swirling flows

Examples of flashback in non-swirling flows include flashback in a channel flow or a Bunsen burner. In both of these cases, flashback has been found to occur along the boundary layer at the wall of the pipe or channel. The classical model on flashback was proposed by Lewis and von Elbe [5].

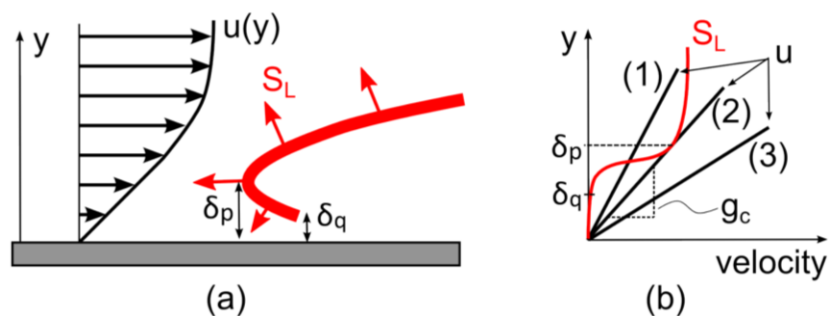


Figure 1-9: The classical model of boundary layer flashback (a) schematic of the flame front with respect to the boundary layer, and (b) illustration of the critical gradient model for three different velocity gradients.

Figure 1-9(a) shows a schematic that illustrates the critical gradient model. The flame (shown in red) propagates upstream through the low stream-wise momentum zone in the boundary layer. The flame tip is located at a location δ_p (penetration length) away from the wall. Owing to the heat loss to the wall, flame can exist only above δ_q (quenching distance) from the wall. Figure 1-9(b) shows three cases of velocity gradient close to the wall. The red line in this plot shows the component of flame propagation velocity in the stream-wise direction. When the velocity gradient is smaller than the critical velocity gradient g_c , the flame speed at the penetration length is larger than the approach flow speed, and hence the flame would propagate upstream. This classical model provides a standard metric for flashback to occur; however, the critical-gradient model is overly simplistic as it fails to describe the correct flame propagation speed [47]. The main problem is that the critical gradient model assumes that the incoming flow stays isothermal even in the vicinity of the flame; however, the flame substantially alters the incoming flow and leads to significant streamline divergence at the flame front [48]. Figure 1-10(a) shows the schematics for cases with and without flame flow interactions. The red and blue lines show the approach flow streamlines and flame surface respectively. When the flame and the flow do not interact, the streamlines stay straight while passing through the flame surface. This situation is easier to model and would be true for a situation when the density change across the flame surface is assumed to be negligible. On the other hand, when the volumetric flow generation across the flame surface is taken into account, the upstream approach flow streamlines diverge prior to entering the flame. This situation is illustrated in the Fig 1-10(b).

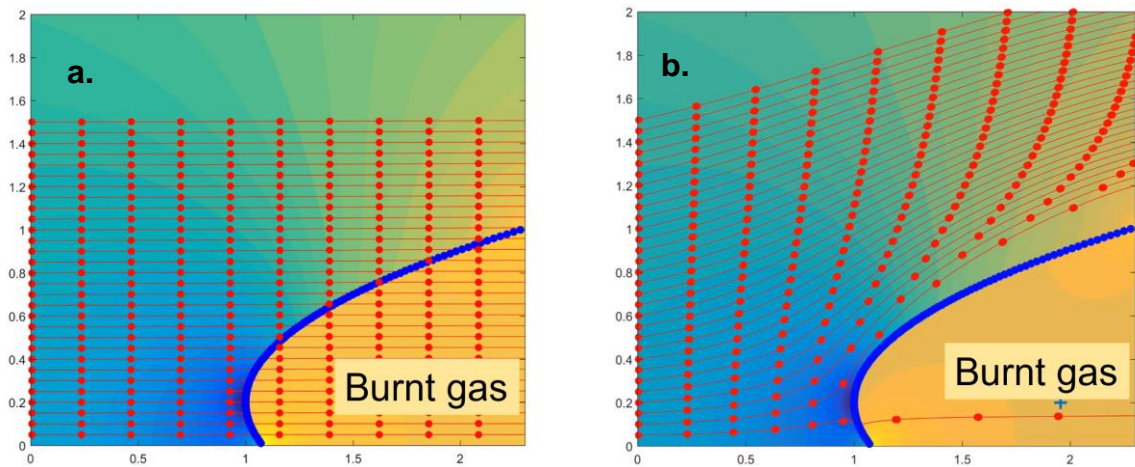


Figure 1-10 Schematic showing the streamlines during flashback with a. no flame-flow interaction b. strong flame flow interactions. Blue and red line represents the flame profile and the approach flow streamlines respectively.

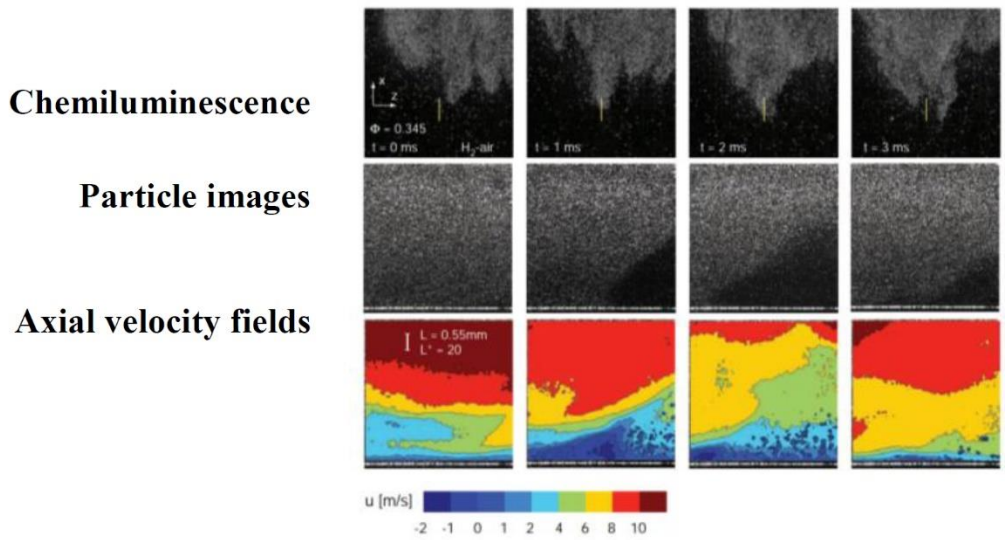


Figure 1-11: Simultaneous chemiluminescence images, particle images and velocity field at the flame tip during flashback [45]. The straight line in the chemiluminescence images show the location of laser sheet.

At TU Munich, Eichler et al. [49] and Baumgartner [50] investigated turbulent flame propagation along a flat wall. It was observed that the flame propagation was led by small “bulges” or “tips,” where the flow field upstream of it exhibited reversal of flow. This region is shown in blue in axial velocity maps in Figure 1-11. Baumgartner [50], in his thesis, proposed that the flame structures impose an adverse pressure gradient on the incoming flow, there inducing the separation of boundary layer. Hoferichter et al. [51] tried to model the flashback on the basis of the adverse pressure gradient imposed by the flame front.

1.1.2.2 Flashback in swirling flows

Flashback in gas turbine combustors may assume different modes of upstream propagation depending on the flow geometry. It might occur along the wall boundary layer [52], along the vortex core [12] or along the center-body boundary layer [53], as shown in Figure 1-11. Flame propagation along the vortex core happens even though the bulk flow velocity is much larger than the flame speed. Konle and Sattelmayer [54] proposed the role of combustion-induced-vortex-breakdown (CIVB) in assisting the flame propagation through core of swirling flows.

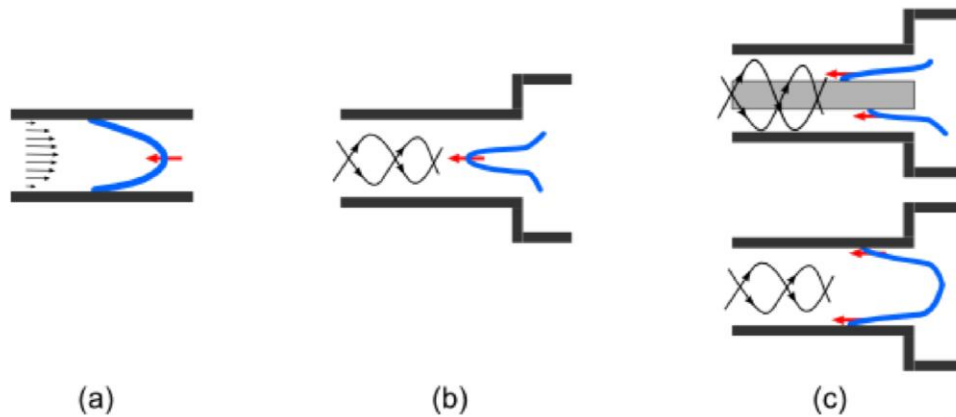


Figure 1-12: Different modes of flame flashback. (a) inside a channel or tube, (b) along the axis of a vortex, and (c) along the walls of different geometry swirl combustors. Blue line indicates the flame surface, while red arrow indicates the motion of the flame tip.

They suggested that since at the flame sheet, pressure gradient and the density gradients are misaligned, the resulting baroclinic torque supports the vortex breakdown at the tip of the flame. Negative azimuthal vorticity production at the tip leads to vortex breakdown which furthers the propagation of the flame. Numerical results obtained using unsteady RANS were found to support this proposition [20]; however, no experimental work has established the existence of a stagnation point upstream of the flame tip in a vortex core.

At TU Darmstadt, Heeger et al. [21] investigated lean-premixed swirl flame flashback and observed a negative axial velocity field upstream of the flame tip, which propagated along the center-body boundary layer. It was assumed then that these negative-axial velocity regions are akin to the one observed by Eichler et al. [49]. It was concluded that the flame tip separates the boundary layer upstream of it and thus its propagation gets assisted by the reversal of flow. However, in their study, there were no provisions to measure the out-of-

plane velocity component which, as shown later, might have important implications in swirl flows.

Ebi and Clemens [55] studied premixed flame flashback in a swirl-flame combustor with premix tube with center-body. They used time-resolved tomographic PIV measurements to examine the flow in proximity of the flame tip. They observed a negative axial velocity region, akin to the findings of Eichler et al. [49], was present on the side of the large flame tongue, which propagated along the center-body boundary layer. The global flame propagation behavior is illustrated in Figure 1-13. The flame tongue swirls around the center-body in the same fashion as the approach flow. The axially upstream motion of the flame is led by the flame tip. Behind the flame tip region is the trailing edge of the flame brush. This region is marked by the presence of the small flame bulges. The flame propagation was found to occur over a few milliseconds and the temperature of the center-body (less than 100°C in their case) was not found to affect this behavior.

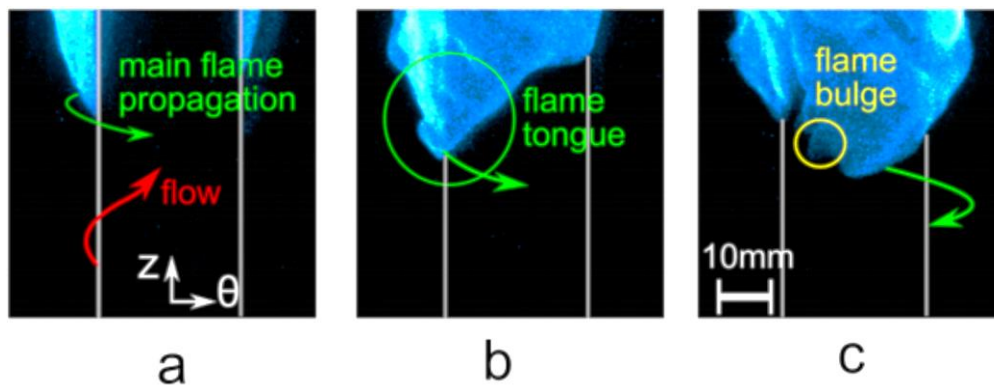


Figure 1-13 Global propagation behavior of the flame tongue during methane air flashback. a. Flame behind the center-body b. Flame tongue entering the front view c. Flame bulges on the trailing edge are visible. Each of these instants are separated by 10 milliseconds in time. Red arrow shows the direction of the approach flow. Green arrow indicates the motion of the flame tongue. [56]

However, their three-component PIV measurements showed that the negative axial velocity region was associated with flow deflection rather than flow reversal. This observation ruled out the leading role of boundary layer separation in flame propagation in lean-premixed swirl flame flashback. In Figure 1-14, instantaneous streamlines approaching the flame tongue from different locations, are shown. In the first case, the streamlines were found to reverse near the flame bulge. Near the leading edge of the flame, the flow was found to deflect in the direction of the swirl. These effects are illustrated in Figure 1-13. The streamlines approaching the flame and the pockets of flow upstream of the flame bulge are directed in opposite direction (actual reversal), as shown in Figure 1-13(a). The deflection of streamlines in Fig 1-13(b) can be observed as bending of streamlines (notice green streamlines in comparison with red streamlines).

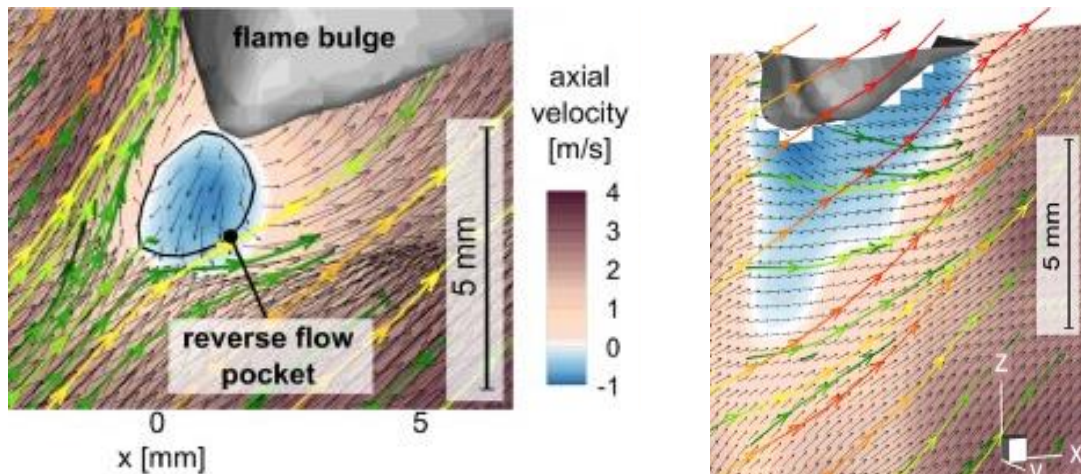


Figure 1-14: Streamlines in the unburnt gas region indicating the (a) reverse flow pockets, and (b) flow deflection upstream of the flame tip. Streamlines are colored by distance from the center-body. [53]

A recent DNS study by Gruber et. al [57] investigated premixed hydrogen-air flashback in a channel flow and observed the regions of negative stream-wise velocity form

at the tip of the leading points. It was suggested that Darrius-Landau instability and pressure fluctuations play a role in flame cusp formation and heat release at the flame tip reverses the flow upstream of these flame tips. [58] The pressure scaling of the flashback speed showed that at high pressure, higher flashback speed would be experienced. Kitano et al. [59] investigated the effect of pressure fluctuations on the flame propagation of hydrogen-air mixtures in channel flow flashback. They noted that the flame propagation was robust against the adverse pressure gradient and for an entire cycle of pressure fluctuations, the flame propagation proceeded in upstream direction.

The effect of hydrogen addition can have dramatic effects on flame flashback. In various studies, such as Dam et al. [60], Daniele et al. [61] and Beerer et al. [62], it was demonstrated that across all the burner geometries, flashback propensity was higher for hydrogen-rich fuels. It was reported that the turbulent displacement speed of pure hydrogen-rich flames was higher than the hydrogen-methane-air flames, for the same level of turbulent fluctuations. Sattelmayer et al. [52] investigated pure hydrogen-air flames in a swirl burner without a center-body, and found that hydrogen-swirl flames propagated initially along the vortex core, but immediately afterwards, the flame transitioned to propagation along the outer wall boundary layer. For a combustor geometry with a center-body, Ebi [53] observed that hydrogen-rich flames propagated along the center-body wall and the propagation behavior was grossly similar to that of methane-air flames, although with some differences. For example, it was noted that the flame surface of hydrogen-rich flames was significantly more wrinkled, which they explained on the basis of thermo-diffusive instability on hydrogen-air flame surface. They noted that the radial spread of the

propagating flame skirt was smaller than for the methane-air flames, as shown in Figure 1-15.

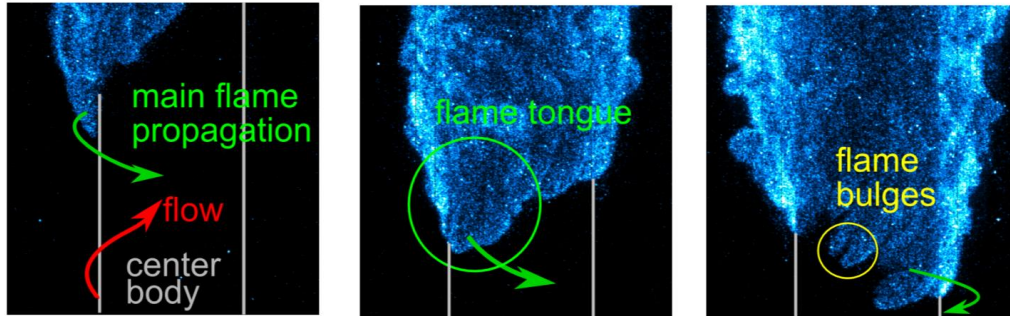


Figure 1-15 Chemiluminescence images of hydrogen-rich flame flashback as reported by Ebi. Flame surface is highly wrinkled for hydrogen-rich flames, however the global behavior of flame propagation remains the same as methane-air flashback [53].

Sayad et al. [13] observed that for preheated hydrogen-methane-air mixtures, flashback might occur by autoignition. Autoignition generally occurs when the residence time of the fuel-air mixtures is larger than the ignition delay of the fuel-air mixtures. Beerer and McDonnell [63] in their attempt to measure the ignition delay of hydrogen-air mixtures in gas turbines, found that the temperature at the premixing tube wall was high, even though auto-ignition had not occurred. It was supposed that the flow in the boundary layer has larger residence time, hence auto-ignition might have occurred along the wall. Another possibility was suggested to be the catalytic effects for the surface itself.

There have been few experimental studies that have focused on flashback under elevated pressure conditions [62],[64],[65],[66],[67]. Only one of these studies, by Mayer et al. [65], has observed the behavior of upstream propagation of hydrogen-air flames at

elevated pressure using time-resolved laser diagnostics. In their study, it was noted that for hydrogen-air flames, the flashback propensity increased with pressure and the critical gradient was found to be an order of magnitude higher than the atmospheric pressure cases. The critical gradients predicted by Fine [68] for sub-atmospheric pressure flashback were not found to be applicable. It was noted that the flashback prediction models for atmospheric pressure experiments may not be applicable at elevated pressure.

1.1.2.3 Flashback in partially-premixed fuel-air mixtures

Partial premixing of fuel-air mixtures has been a popular strategy to avoid flashback in industrial combustors. By partial premixing of fuel, regions prone to flashback such as vortex core or wall boundary layer can be kept too lean for flame propagation. However, depending on whether the flame is back-supported or front-supported, the flammability limits of the fuel-air mixture may be very different from conventional flammability limits [41]. This brings in the necessity to understand flame propagation in stratified mixtures. So far, there are two studies on flashback in a partially-premixed fuel-air mixtures. A joint experimental and numerical study by Sommerer et al. [69] involved studying the flashback in propane-air premixtures at atmospheric pressure. High-speed OH luminescence was captured at 10 kHz during flashback. It was noted that the flame flashed back along the vortex core of the swirl flames. For the analysis of numerical results, a modified flame index was utilized to predict the percentage of premixed and non-premixed flames in the flame brush. It was noted that upon flashback, the flame stabilized on the lip of the fuel injector and thus, the fraction of non-premixed flames increased by a factor of three.

Another study which reported flashback in a hydrogen-air partially premixed mixture was carried out at TU Munich. Utschick and Sattelmayer [70] investigated the possibility of sustained flashback that leads to flame-holding on the injection ports. Partial premixing of fuel was done by injecting the hydrogen-fuel through two types of injectors, one which injected the fuel normal to the flow, another which injected fuel iso-kinetically into the system. Ignition was triggered into the fuel-air mixing tube by laser ignition. A set of experimental conditions were mapped out for the flame-holding to occur. Based on flow conditions, a Damkohler number criteria was defined for which the flame-holding could not happen in the mixing tube. In another study by Utschick et al. [71], flame propagation behavior in the mixing tube was studied. By employing high-speed stereoscopic OH-luminescence imaging, it was noted that the flame moved along the outer wall on a helical path until it stabilized on the fuel ports.

1.2 Context of current work

As evident in the existing literature, flashback is a complex multi-physics process that requires further study, especially for swirling flows. In this study we aim to improve knowledge of flashback physics by investigating the flow near the leading side of the flame surface. The details of the flame-flow interaction are investigated using high-speed luminosity imaging and simultaneous particle image velocimetry. We have two main objectives in this study.

The first is to develop an improved understanding of the propagating swirl flame under fully-premixed conditions and to analyze its role in flashback assistance. For this purpose, a new analysis technique is applied that enables the three-dimensional structure of the flow to be reconstructed. The analysis from the flame frame-of-reference reveals the

role of inertial forces in the swirling-flame-flow interaction. A fundamental picture of azimuthal propagation of the flame is developed.

The second objective of this study is to understand the effect of fuel-air stratification on the flame propagation behavior. We induce stratification in the radial direction by placing the fuel injection ports on the radially outward section of the swirl vanes. The equivalence ratio field is analyzed to characterize the nature of the stratification in non-reacting flow. Further, we conduct reacting flow experiments and report different propagation behavior of flashback and the role of hydrogen-enrichment on flashback behavior. The global behavior of upstream propagation is studied for pressures up to 5 atm. However, laser diagnostic experiments are carried out up to 3 atm. Laser diagnostic experiments are used to reveal the role of equivalence ratio inhomogeneities on flame propagation behavior.

In the end, we discuss a general picture of flame-flow interactions on the upstream propagation of the flame inside the mixing tube. The limitations of the current study and possible research directions to further our understanding of flashback is explored.

CHAPTER 2 : EXPERIMENTAL SET UP

The flashback experiments were conducted with an annular swirl combustor which was mounted inside an elevated pressure chamber. A set of high-speed cameras and lasers were used to observe the flame propagation. In this section, we describe these experimental set ups in detail.

2.1 Swirl Combustor

The swirl combustor assembly used in these experiments is a lab-scale prototype of industrial combustors as shown in Figure 2-1. The section view of the combustor is illustrated below:

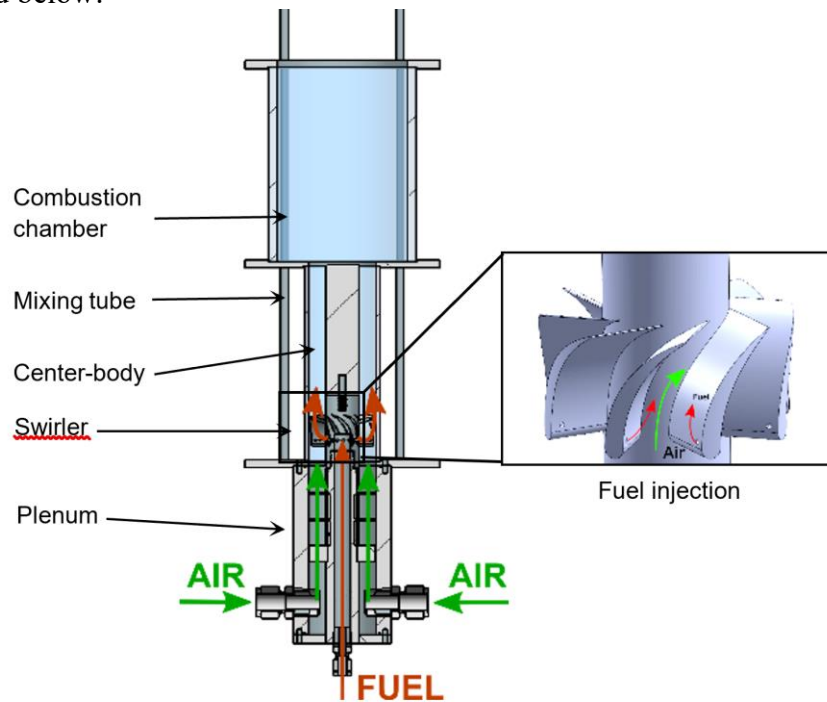


Figure 2-1 The optically accessible swirl combustor. Swirl vanes and the fuel path is illustrated in the inset.

It can be divided into three main sections: the plenum, the mixing tube, and the combustion chamber. The main air flow through the combustor enters the annular plenum

region through four inlet ports, positioned symmetrically around combustor center-line. Entry of air through these ports is depicted in Figure 2-1. Afterwards, this flow gets conditioned by passing through annular honeycomb straighteners and two stations of fine-wire mesh. The flow then passes through the swirl vane and into the mixing tube. The mixing tube consists of a center-body and an outer cylindrical wall. The axial swirler is a prototype of an industrial swirler with an inner and outer diameter of 25.4 and 50.8 mm respectively. The swirler body is made with cobalt-chrome and was three-dimensionally printed with an uncertainty of ± 60 microns. It was equipped with eight symmetric aerodynamically-curved vanes. Each swirler vane was angled at 60 degrees with respect to the combustor axis. These vanes were also equipped with fuel injection ports for use in partially-premixed flashback experiments. The fuel-entry paths through these ports are different than the main air flow and shall be discussed in a subsequent paragraph. The axial swirler imparts large azimuthal momentum to the approach flow. Numerical simulations of the flow at the exit of the mixing tube indicated that the swirl number is 0.9. The swirl number is the ratio of azimuthal to axial momentum flux of the swirling flow. The near-unity swirl number indicates that the flow in the mixing tube is of high swirl, according to conventional definitions (Swirl number > 0.6). The center-body of the mixing tube is attached coaxially to the downstream end of the axial swirler. The center-body is a lathe-machined stainless-steel cylinder with an outer diameter of 25.4 mm. Prior to installation, the near-polish-finished center-body surface was painted with an ultra-flat black spray paint (Krylon 5BIEP), which was desired to minimize the reflected light signal off the center-body. The outer wall of the mixing tube was made of optical grade fused silica (Heraeus Suprasil 310), which allowed optical accessibility into the flow field upstream of the combustion chamber. The inner diameter of the outer wall was 52 mm. The annular space of the mixing tube was bounded by the center-body and the inner wall of the fused

silica tube. To ensure that the fused silica tube could be mounted co-axially with the center-body, a specially-designed alignment apparatus and screw-tightening methodology was used. Downstream of the annular mixing tube, the flow opened up into the combustion chamber that had nearly twice the outer diameter of the mixing tube. The center-body end plane was flush with the mixing tube exit plane. The inner diameter of the combustion chamber was 100 mm and its axial length was 150 mm. The combustion chamber and mixing tube were held fixed by sandwiching these components between the holding plate at the top and the plenum plate, as shown in the Figure 2-1. The glass-metal components were sealed by using 1/8" thick ceramic paper gaskets (custom cut, in-house), which could withstand temperatures in up to 1200 °C. Additionally, the padding provided by these gaskets compensated for the thermal expansion mismatch between the steel and the glass.

The fuel streams through the swirl-vane injection ports follow a different flow-path prior to entering the mixing tube. The central space in the plenum was occupied by a hollow tube that was connected to the swirler and the center-body. The hollow tube was connected to a fuel line, independent of the main swirl flow lines. The inner regions of the swirler and the center-body were also designed to be hollow, thereby providing continuous access to the swirler vanes and the center-body. This access to the center-body was used to route thermocouples, which were used to measure the temperature of the center-body during flashback. Fuel was passed through internal passages in the swirl vanes and then injected into the main flow. The passages were cylindrical in shape and 3 mm in diameter. The fuel injection ports in the swirl vanes were 1 mm in diameter. Two ports were used on each vane. These fuel ports injected the fuel normal to the swirl vane surface, akin to a JICF (jets-in-crossflow) configuration. These ports were located at a radial position 3 mm away from the outer wall to introduce mean radial stratification in the mixing tube. It should be

noted that this inner-fuel-flow-design was optimized by doing several iterations of 3D printed plastic swirlers. Thin-channel designs are prone to be asymmetric due to large relative machining error (6-10%) and the possibility of partial choking of flow paths due to contaminants in the flow line. To minimize such problems, all of the flow paths were kept straight (easy-to-clean) and orthogonal at branching nodes (easy to ensure symmetry). As a qualitative way to ensure symmetric behavior across all flow passages, a laminar diffusion-flame test was developed, as shown in Figure 2-2(b).

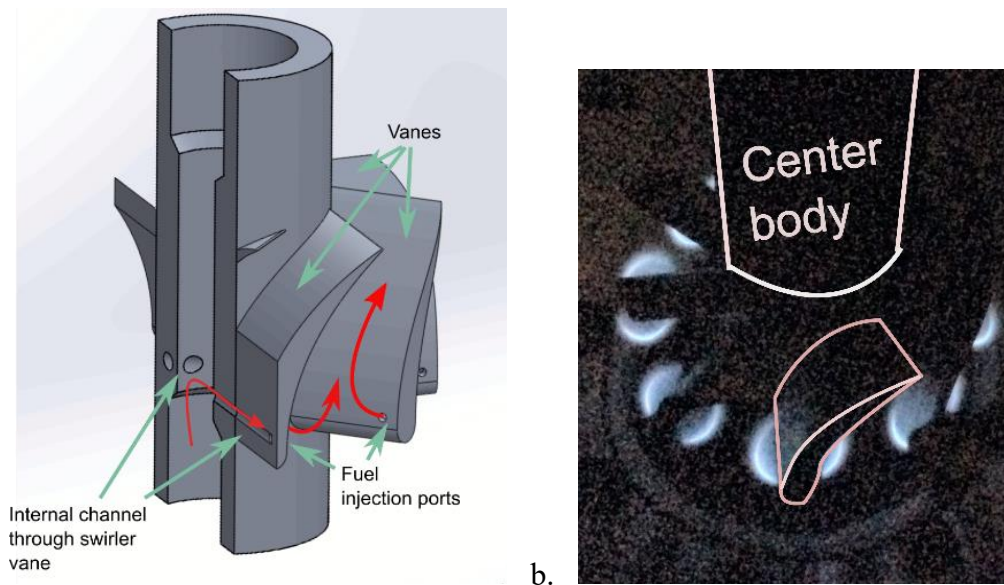


Figure 2-2 a. Cut out view of swirler showing the fuel path in red arrows b. Perspective view of the swirler during the laminar flame test. One swirler vane and the center-body is highlighted.

In this laminar-flame test procedure, a very small amount of fuel was continuously flown through the swirler vanes. Thereafter, diffusion flames were ignited in a fashion like a kitchen-stove burner. The resulting flame pattern indicated the symmetric nature (or the lack of it) of the flow through the injection ports. Any loss of symmetry indicated a possible

flow blockage problem, which was addressed by cleaning the fuel-ports. By repeating this procedure a few times, a reasonably symmetric appearance of the flames could be achieved. It should be noted that ensuring the symmetry of the flow is important to comment on the nature of flashback in partially-premixed flames.

Fuel flow to the combustor was supplied by industrial pressurized gas cylinders (Praxair or Airgas, 2500 psig when full, 99% purity) equipped with pressure regulators. The main air flow was supplied by a large pressure tank (maximum pressure: 150 psig) that was charged with air from the house compressor. These gas sources were connected to high-precision mass flow controllers (Alicat MCR series), which were given control input through an in-house written LabVIEW program (custom-edited Alicat software). The mass flow controllers had an accuracy of 0.2% of the full flow scale value. The gas-specific PID (proportional, integral, and differential) parameters of the mass-flow control were obtained by trial runs. These parameters were optimized to obtain a small response time, without overshooting the flow rates. Any overshoot beyond the fuel-flow set point may lead to undesired flame presence in the plenum or strong pressure fluctuations in the combustion chamber. A solenoid-driven shutoff valve was utilized to cut off the fuel-flow in such situations. Also, the flow control software was modified to ensure a quick and simultaneous control of multiple flow lines to avoid any untoward incident.

2.2 Elevated pressure chamber

An important purpose of this research is to understand how flashback occurs in an industrial gas turbine. Thus, to simulate the turbine conditions, a continuous-flow, backpressure-controlled elevated pressure chamber was designed and built. Although an actual gas turbine power plant reaches pressures up to 30-40 atm, the current chamber is

designed to operate only up to 10 atm. Since the hot regions of the pressure chamber may reach high temperatures (up to 500 °C), the pressure chamber was made of stainless steel, which exhibits excellent yield strength even at elevated temperatures [72] The chamber is designed for thermal heating powers up to 300 kW.

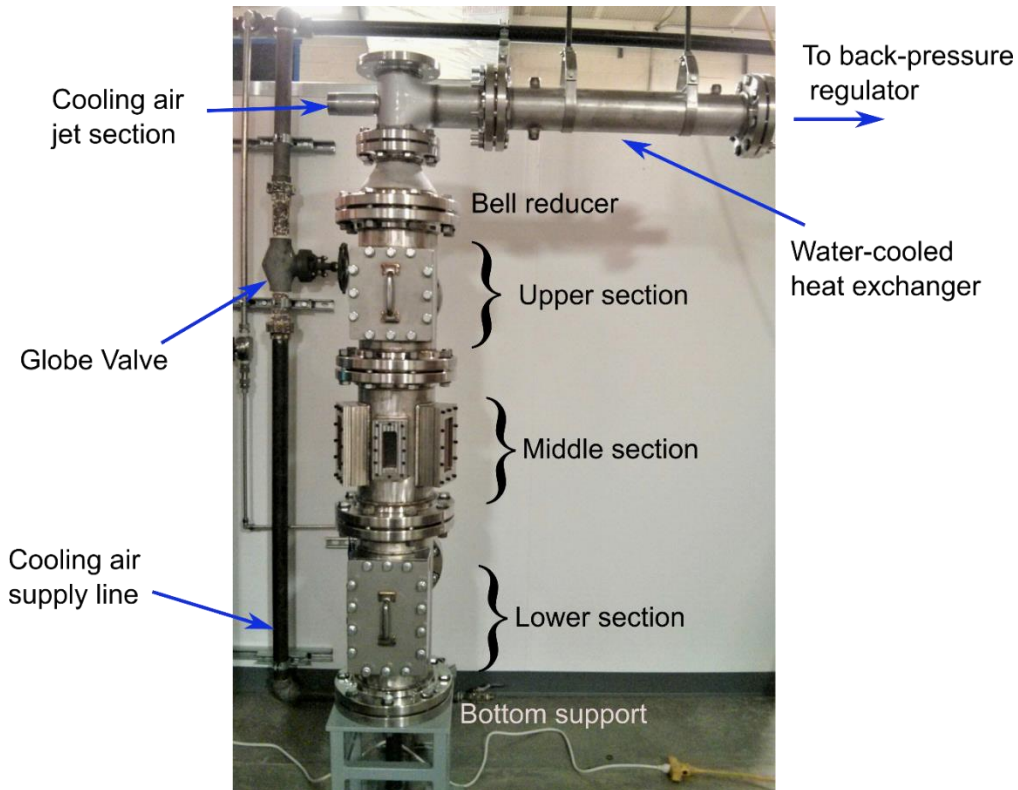


Figure 2-3 Photograph of the elevated pressure chamber

The pressure chamber is shown in Figure 2-3. This chamber is provided with two rectangular access ports that allow for manual access to the internal assembly. Four different fused silica windows were incorporated into the pressure chamber so that high-pressure laser diagnostic experiments could be carried out. The lower section provides the platform for the experimental set up installed inside the chamber. It has a blind-flanged connection on the side that offers a flat surface for fuel entry ports. It also has an access

door on opposite side that is useful for the installation and adjustment of the internal assembly. The inlet for the cooling air co-flow is provided at the center of the bottom face. The inlet of cool air co-flow is shown in the cut-out image of the pressure chamber in Figure 2-4.

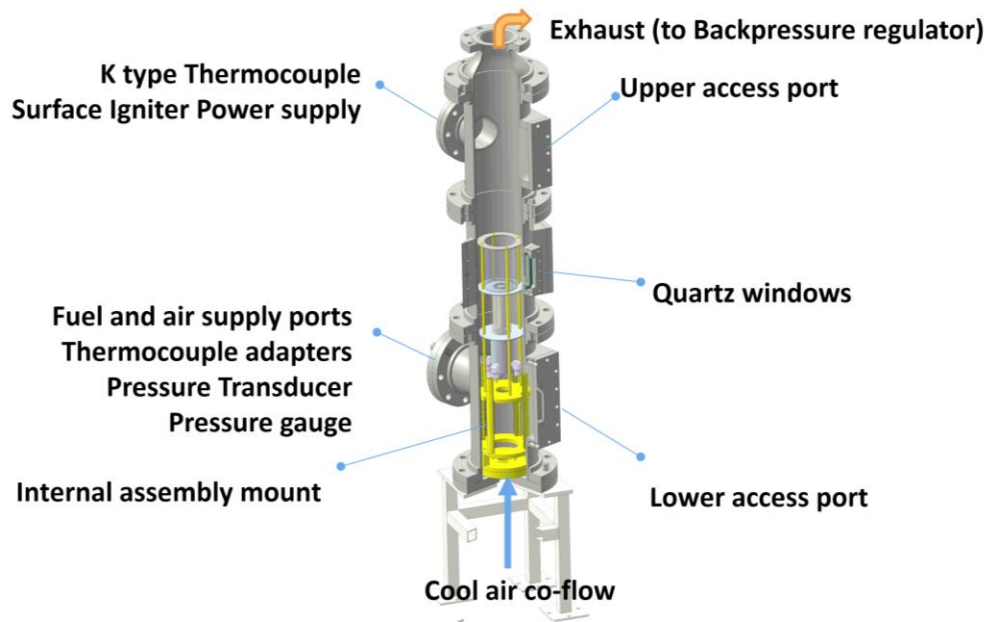


Figure 2-4 Section view of the pressure chamber showing the internal assembly

The middle section consists of three rectangular windows, two large ones (6" × 2.4") and a smaller one (4" × 1.5"), to allow optical access to the test section. The axes of the larger windows are at an angle of 70 deg with respect to the smaller window in the horizontal plane. The orientation of the large windows allows for stereoscopic PIV to be conducted. The windows are made of S1UV fused silica glass (supplied by Esco Optics), which have high transmission for UV light.

The upper section features another access port, which was primarily used to install the calibration target for stereo PIV. Attached to the upper section is a bell reducer, which acts as a passage for the hot exhaust gases. The smooth transition from 8-inch diameter to 4-inch diameter piping allows for streamlined flow of the cooling air. This geometry maintains low acoustic noise in the chamber, which is necessary for safe operation. At the top of the chamber, another window is provided to allow for a laser sheet to enter the chamber. To shield this window from hot gases, additional cooling air is supplied from the side that reroutes the exhaust and decreases the sudden rise in temperature at the glass surface. A thin sacrificial glass plate is provided in the window assembly to protect the main window from the hot gases. The high-pressure chamber is versatile in the sense that it can host various combustor geometries. Air mass flow rates to the combustor of up to 0.1 kg/sec are possible, which corresponds to a Reynolds number of 200,000 at 150 psi based on the tube diameter of 50 mm. The chamber is designed for thermal heating powers up to 300 kW. The vertical pipe assembly offers great adaptability for different visualization methods. Depending on optical access requirements, the middle section can be replaced to allow alternate window locations. The top window is ideal to observe the flashback process in a transverse plane.

Safety has been given utmost importance in designing of this pressure chamber. The glass windows have been designed with a high safety factor (~ 10). A pressure safety valve is provided in the bottom section of chamber. The cooling air supply tank is kept at the maximum of 150 psi which is also the maximum design pressure of the chamber. Thus, during operation, the pressure chamber is inherently safe against any unintended rise in airflow.

2.2.1 FLOW THROUGH THE PRESSURE CHAMBER

Fig 2-5 shows a simplified process and instrumentation diagram for the pressure chamber. The cooling air is supplied to the pressure chamber from a medium pressure gas tank (maximum pressure 150 psi) located at the Wind tunnel lab, Pickle Research Campus. The flow through the supply line is controlled using a control valve that is normally-closed and is provided a diaphragm actuator pressure of 40 psi. A set of ball valves are included in the air supply line to isolate different sections of the process flow during start up. Fuel is supplied to the set up through industrial gas cylinders equipped with standard gas pressure regulators. A bank of high-precision mass flow controllers (Alicat scientific, $\pm 0.2\%$ full scale accuracy) are used to supply the air and fuel flow through the combustor. The cooling air co-flow is regulated using the globe valve (typical opening of a quarter turn) and the control valve. The cooling air supply line (diameter 2 inch) opens at the bottom flange of the pressure chamber. The cooling air jet spreads out in the pressure chamber (inner diameter of 8 inches) and flows around the internal assembly of the combustor. Upon crossing the combustor's location, the cooling air shrouds the inner walls of the pressure chamber and gradually mixes with the combustion products of the swirling flame.

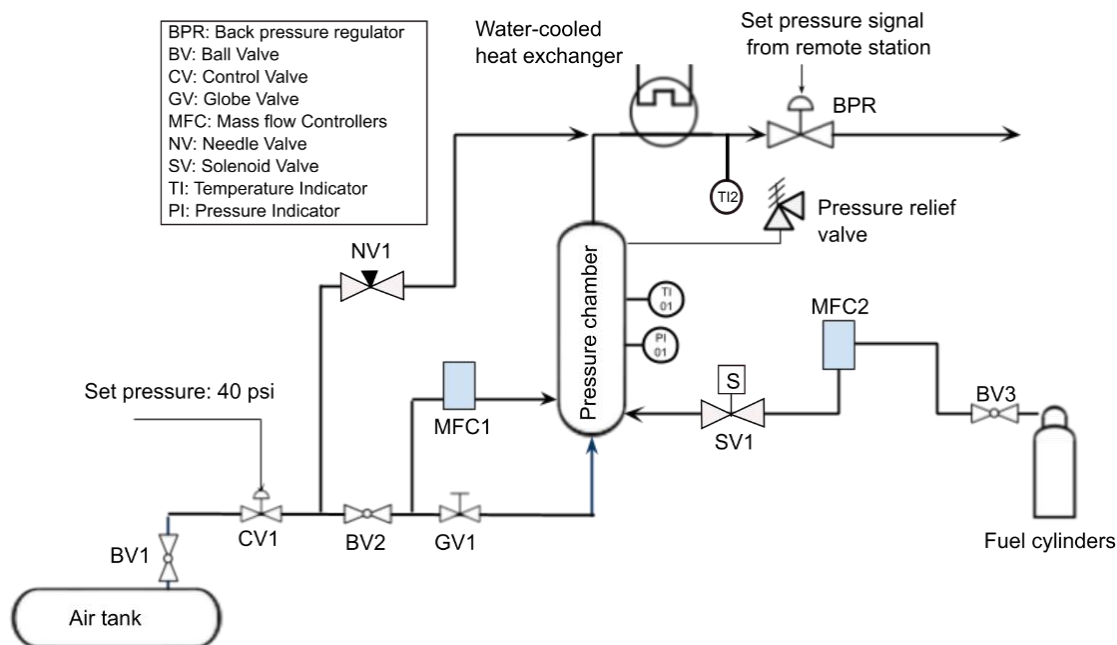


Figure 2-5 Simplified Process and instrumentation diagram for the pressure chamber

The entire pressure chamber facility was operated remotely from a control station equipped with four different computer systems. These computer systems were remotely connected on the internal network to the master computers for processes such as image capturing and pressure chamber monitoring. In addition to the cameras for optical diagnostics, a set of security cameras were installed to monitor the experimental facility area during the experiments.

2.3 Optical diagnostics

2.3.1 CHEMILUMINESCENCE IMAGING

High-speed chemiluminescence imaging was used extensively to investigate flashback. For this purpose, a high-speed imaging camera (Photron APX) with a mounted external intensifier (HiCatt, Lambert Instruments) is used to capture the flame propagation.

Depending on the experimental requirements, a 105mm Nikon lens (narrow view) or 70-250 Tokina lens (wider view) is used. Typically, luminosity images are captured at 4 kHz with an exposure of 250 microseconds. The intensifier gate is kept at 50 and 100 microseconds for methane-air and hydrogen-rich flames, respectively. For corresponding cases, the intensifier gain is kept at 750 and 850. During simultaneous laser diagnostics, a digital delay generator was used to sync the intensifier with the lasers such that the intensifier gate is closed during the laser pulse. In general, care was taken to avoid any reflection towards the intensifier. The center-body was painted black and any possible reflected light towards the intensifier was blocked. For further protection of the camera and the intensifier, the monitor current trip limit was set at 6%.

Interpretation of chemiluminescence images depend on the global shape and propagation behavior of the flame that enters the mixing tube. If the flame surface topography remains consistent over length-scales and timescales of the observation, it can be assigned an identity. A simple example would be a spherical flame [7] or a flame tongue as was identified by Ebi and Clemens [55] for swirling flashback flames. Although the geometry of a flame tongue may or may not be geometrically consistent, the convex shape of the flame surface allows us to define a flame tip. The flame tip is the most upstream point of the flame tongue. When considering axial flame propagation, the axially-upstream point can be identified and defined easily. This point leads the upstream propagation of the flame surface and tracking it allows us to identify the axial motion of the flame tongue.

Luminosity signal is line-of-sight integrated in nature, which prohibits us from determining the three-dimensional position of the flame tip from a single projection of luminosity. However, previous studies in this facility of flashback for premixed reactants showed that the flame tip tends to stay close to the center-body as it flashes back [47], [21].

Thus, even with a single luminosity image, the location of the flame tip can be easily tracked.

Figure 2-6(a) shows the top view of the visible region in the mixing tube. The region behind the center-body is occluded for the luminosity imaging camera. The region on the left and right of the camera can be distinguished on the basis of the angle subtended at the center. The left region extends from $(-\pi/3 < \theta < 2\pi/3)$, and thus any tracking of the flame structure could be done only in the non-occluded region. Given the line-of-sight integrated nature of luminosity signal, the depth of any flame feature detected in the left and right section would be difficult to comment upon.

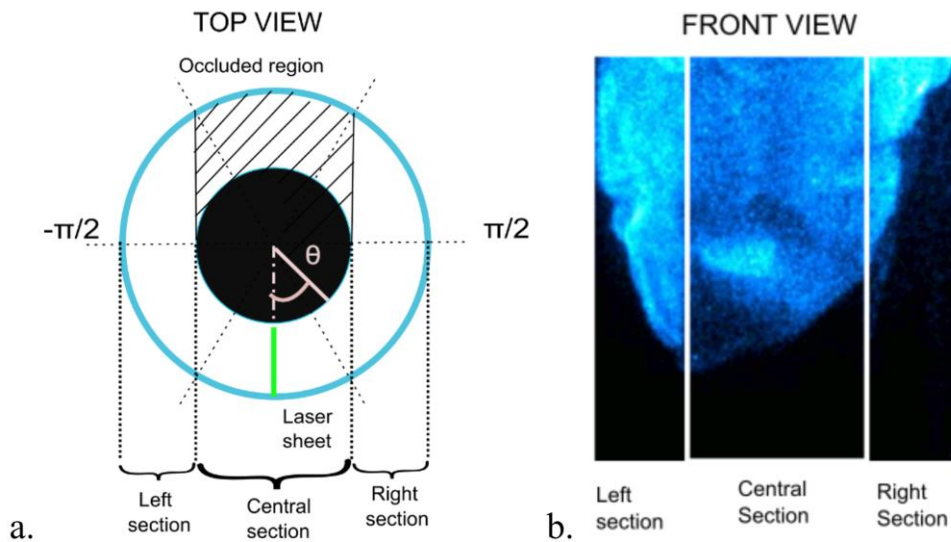


Figure 2-6 a. Top view of the mixing tube showing the region occluded for luminosity imaging. The position of the laser sheet and different regions of the field of view are shown. b. Front view of the flame structure.

2.3.2 PLANAR LASER INDUCED FLUORESCENCE (PLIF)

Fuel-air mixing upstream of the combustor exit plane is quantified using acetone PLIF. Acetone has been widely used as a fuel-tracer, mainly due to its excellent

fluorescence quantum yield, low toxicity and low cost. Acetone has an absorption spectrum which extends from 225 nm to 325 nm (ground level to first excited singlet transition). The fluorescence is emitted over the range of 350 nm to 650 nm. When excited with an ultraviolet beam the acetone fluorescence appears as blue-violet.

2.3.2.1 Acetone bubbler

To conduct the laser-induced fluorescence experiments, the fuel flow is seeded with acetone vapor. To achieve this the fuel line is passed through an acetone bubbler prior to entering the mixing tube. The bubbler is a cylindrical copper vessel filled with liquid acetone. The internal diameter of the bubbler is approximately 3.5 in. The copper vessel has a brazed brass top with a three-inch diameter female thread. This section is capped with a brass plug. To prevent continuous cooling of liquid acetone due to evaporation, water is passed through copper coils that are immersed in the liquid acetone. This system enables us to produce a high level of acetone enrichment without condensation in the fuel stream. The fuel flow enters the bubbler through a vertical half-inch tube that extends into the bottom of the bubbler. This tube is plugged at the end but is perforated to enable the gas to be injected into the liquid acetone like a shower head. As the gas rises it becomes more enriched with acetone vapor. The enrichment level depends on the residence time of the gas in the acetone bath, but typically saturated conditions could be achieved. The acetone level can be easily tracked using the Teflon tube level indicator attached to the side of the bubbler.

During flashback experiments, it was realized that the acetone tended to condense in the tube, which clogged the fuel tube over time. Thus, in order to prevent the excess acetone condensation in the tube, another cylindrical copper vessel was connected

downstream of the bubbler. This vessel served as a condensate-accumulator and prevented liquid acetone build up in the fuel supply tube or the combustor.

2.3.2.2 Lasers and Imaging set up

In order to excite the acetone fluorescence, a laser sheet at 266 nm is passed into the mixing tube from the side, as depicted in Figure 2-5. A scientific CCD camera (PCO 1400) is used to image the fluorescence from the acetone. This camera is placed normal to the laser sheet. Maximizing the fluorescence signal collection is important to get a good signal-to-noise ratio. Hence, the camera-mounted 50 mm Nikon lens is kept at its lowest f-number ($f/1.2$). A 12 mm extension tube is used to enable focusing of the camera lens for the short working distances used. The camera was turned by 90 degrees to help match the aspect ratio of the field of view. The pixels were binned 2x2 to improve the SNR (Signal to Noise ratio). To minimize the background noise, an ultra-flat black painted surface is kept in the background. For high-pressure PLIF measurement, the inner wall of the pressure chamber on the opposite side of the laser sheet is painted black.

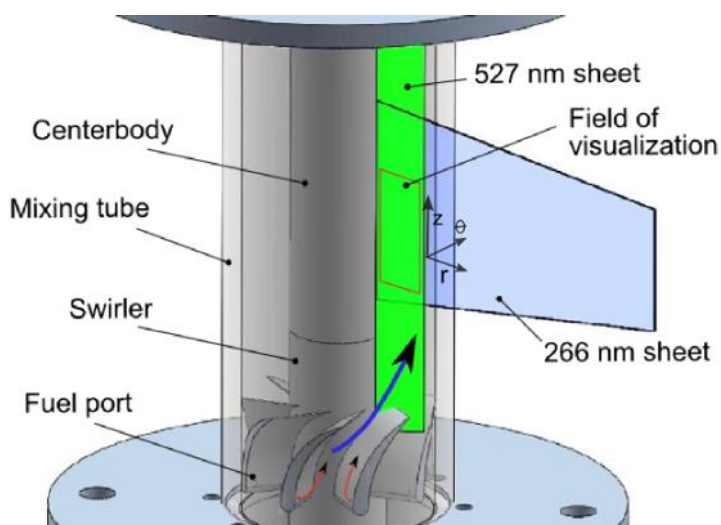


Figure 2-7 Schematic diagram of the field of view inside the mixing tube. A 266 nm sheet is brought from the side of the mixing tube.

A colored blue filter is placed in front of the camera lens to reduce any extraneous signal. The 266 nm laser sheet is formed using a 532 nm pulse from Nd YAG laser (Continuum Powerlite DLS 9010). The one-joule 532 nm pulse is passed through a frequency-doubling KD*P crystal (Spectra Physics). Frequency-doubling is a highly non-linear process whose efficiency is dependent on factors such as crystal temperature, incident angle of the beam on the crystal and polarization of the laser beam. Thus, prior to running the PLIF experiments, the frequency doubling is maximized by tuning the crystal inclination and temperature. The output beam from the crystal consists primarily of 532 nm and 266 nm beams. The residual green laser is filtered by passing the beam through three 255 nm dichroic mirrors. The frequency doubling is continuously tracked using a power meter (Coherent FieldMax II-TO), while tuning the crystal. Once tuned, the crystal is not disturbed until the experimental campaign is over. It was noted that the shot-to-shot variation could be as high as 50% during experiments, even though the crystal inclination and temperature settings was kept the same. This issue might be because of the local variation in the crystal temperature, although the exact reason could not be ascertained. Thus, to correct for this temporal variation in the pulse energy, the sheet energy and profile were measured on a shot-to-shot basis.

After the 266 nm beam is passed through the sheet forming optics, a fused silica flat is used to reflect a fraction of beam (~4%) towards a cuvette (CV10Q3500F-E, ThorLabs) filled with a mixture of fluorescent dye and water. The rest of the beam is directed towards the mixing tube. The cuboidal cuvette (10 mm 10 mm x 50 mm) allows the beam to enter through its flat surface and is then absorbed by the fluid. The fluorescence is captured by another scientific-grade CCD camera (PCO Pixelfly). This camera is synced with the operation of PLIF imaging camera to enable simultaneous capture of the PLIF data and the fluorescence from the dye in the cuvette. The cuvette fluorescence provides a

measure of the pulse-to-pulse variation in the laser energy and the sheet profile. The location of the cuvette and the field of view are positioned symmetrically with respect to the fused silica plate, which enabled the laser sheet profile to be of same dimensions as that of the PLIF imaging field. However, the optical path lengths of the beams are not completely symmetric since the laser sheet passes through the mixing tube wall. Owing to its curvature, it can cause some lensing effect on the beam, however since the laser sheet as well as the cylinder is vertical, it should have minimal effect on the vertical profile. In order to register the laser sheet profile correspondence between the cuvette image and the field of visualization, an optically opaque object such as an Allen key was placed in the path of the laser beam. Figure 4-7(a) shows an image of the mixing tube filled with acetone vapor. The blockage of the laser beam is visible in the image. Figure 4-7(b) shows the fluorescence from the cuvette, which also shows the shadowed region.

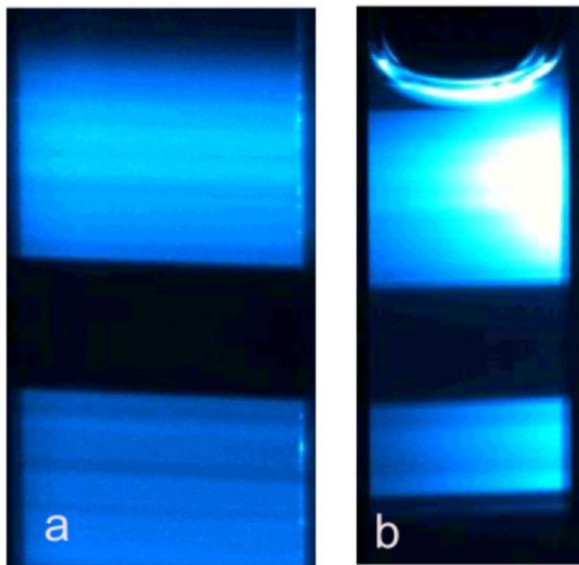


Figure 2-8 (a) PLIF signal from the laser sheet after partially blocking the beam, and (b) simultaneous laser sheet profile in the cuvette

Using this method, we could correct the laser sheet profile on a shot-to-shot basis. The sheet-profile apparatus also provided us with an improved means of controlling the 266 nm beam energy fluctuations. During experimental runs, the PLIF images were monitored using the live view mode of the PCO camera. Depending on the PLIF signal intensity, the crystal phase-matching angle was varied such that the frequency doubling was maximized. In this way, the SNR could be improved by as much as 200%. A typical variation in shot-to-shot pulse energy is plotted in Figure 2-9.

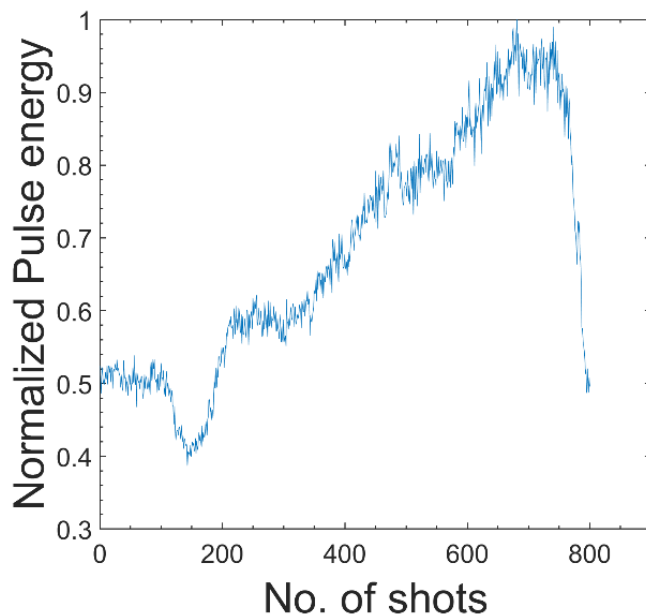


Figure 2-9 Typical shot-to-shot variation in 266 nm beam as measured from the cuvette signal

Another issue with PLIF imaging in a confined flow arises from the scattering from the neighboring surfaces. In the atmospheric pressure set up, reflections could be minimized by tracking the source of the reflections and blocking them or judiciously painting components black. On the other hand, in the elevated pressure chamber, the process is more challenging. There are two primary reasons for this. The first is that the

laser sheet correction method could not take into account any possible change in the laser sheet profile due to dust at the flat windows. In particular, we observed that the laser sheet profile in the cuvette and the mixing tube were not the same. The second is that the scattering from the windows and the inner walls of the pressure chamber could induce additional background in the PLIF images, which could not be accounted for by the sheet correction. In order to reduce this background interference, the pressure chamber windows were almost entirely blocked except for a slit that allowed the laser sheet to enter the pressure chamber. A sample background-corrected PLIF image is shown in Figure 2-8. The colorbar indicates the pixel value. The vertical straight lines in the region $6 \text{ mm} < r < 8 \text{ mm}$ are due to the scattering that cannot be corrected even by shot-to-shot correction.

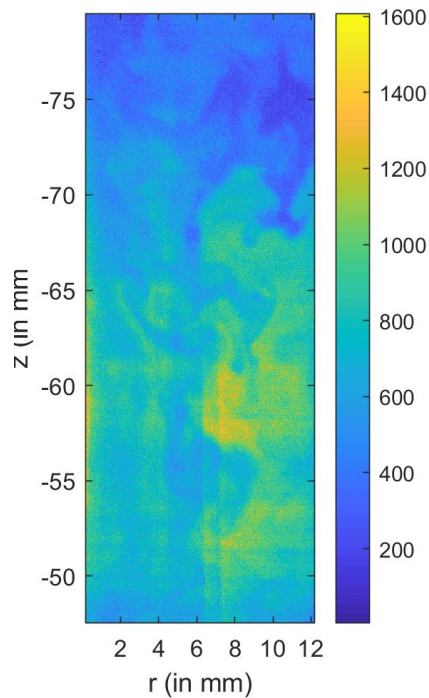


Figure 2-10 Background-corrected PLIF image for methane-air mixing at 3 atm, $Re_h = 18600$.

2.3.2.3 Fuel air ratio determination

The acetone fluorescence signal $F(x,y)$ is directly proportional to the local laser fluence and concentration of acetone. In general, the acetone fluorescence depends on the local temperature, but in the current study this method is primarily used under isothermal conditions. The pixel intensity $I(x,y)$ in a PLIF image is the sum of background, intrinsic camera noise and the fluorescence. The background noise is usually related to scattering from surfaces and windows, or fluorescence from unintended sources such as windows or paints. The intrinsic noise in the camera is mainly due to readout noise [73]. To separate the fluorescence signal, the background signal is subtracted from the PLIF image. The background image $B(x,y)$ is obtained by capturing the image without any acetone present in the flow field. The background signal is shot-dependent and any shot-to-shot variation in laser energy causes it to fluctuate. It is not an issue when the fluorescence is an order of magnitude higher than the background, however in fuel-air mixing for very lean patches, it can lead to significant error. Thus, accounting for shot-to-shot variation helps in reducing the background noise. The shot-adjusted background signal has been used in this study. Once this image is subtracted from the shot-adjusted PLIF images, the resulting signal is an outcome of the fluorescence from the acetone. To obtain ‘pure-fuel’ fluorescence, the mixing tube is filled with acetone-saturated air. The mixing tube is plugged with an annular Teflon plug and “pure-fuel” is added to the mixing tube. This pure-fuel signal $P(x,y)$ is then corrected for the shot-to-shot variation in the laser pulse. The shot-adjusted background signal is then subtracted from the shot-adjusted pure-fuel signal. The resulting image provides the fluorescence from the maximum concentration of acetone. The fuel-air ratio at a point can be calculated by dividing the shot-adjusted background-corrected PLIF signal of fuel-air mixture with the corresponding pure-fuel pixel value. The final image provides the spatial distribution of fuel-air ratio in the mixing tube.

For these experiments, the SNR is found to be in the range of 24-30 in fuel-rich regions, while in fuel-lean regions the signal could be as low as the background. The fluorescence data is affected by the laser sheet absorption as it passes through the field of view. In addition, the scattering off the inner-wall of the mixing tube and hence the background signal may vary from shot-to-shot because of fluorescence itself. These factors are relatively low in magnitude (<10%) and difficult to correct for. Hence, the image processing does not account for these errors.

2.3.3 PARTICLE IMAGE VELOCIMETRY

High speed stereoscopic PIV measurements were taken during the flashback runs. A pair of Nd:YLF lasers (Coherent Evo 90) were used to get a pair of laser pulses which were combined and expanded into a laser sheet entering the swirl combustor from the top. This arrangement of laser sheet allowed the illumination of the boundary layer on the center-body without much scattering off the wall. By bringing the laser sheet from the top, the forward scattering of laser sheet was captured by high speed cameras (Photron APX). These high-speed cameras were tilted with respect to the laser sheet. Hence, to keep the particles in focus, scheimpflug adapters were mounted on the camera. These adapters were adjusted to satisfy the scheimpflug criterion. This arrangement of the laser sheet and the cameras are illustrated in the schematic as shown in Fig 2-11. A set of digital delay generators (SRS DG535) were used to sync the lasers such that there is a delay of 80 microseconds between laser pulses. At the same time, camera trigger and the frame rates were adjusted such that both cameras capture simultaneous particle images. These cameras were operated in “End” trigger mode which allowed the data to be captured with a manual trigger. Camera operations were controlled using Photron software (PFV 0.63).

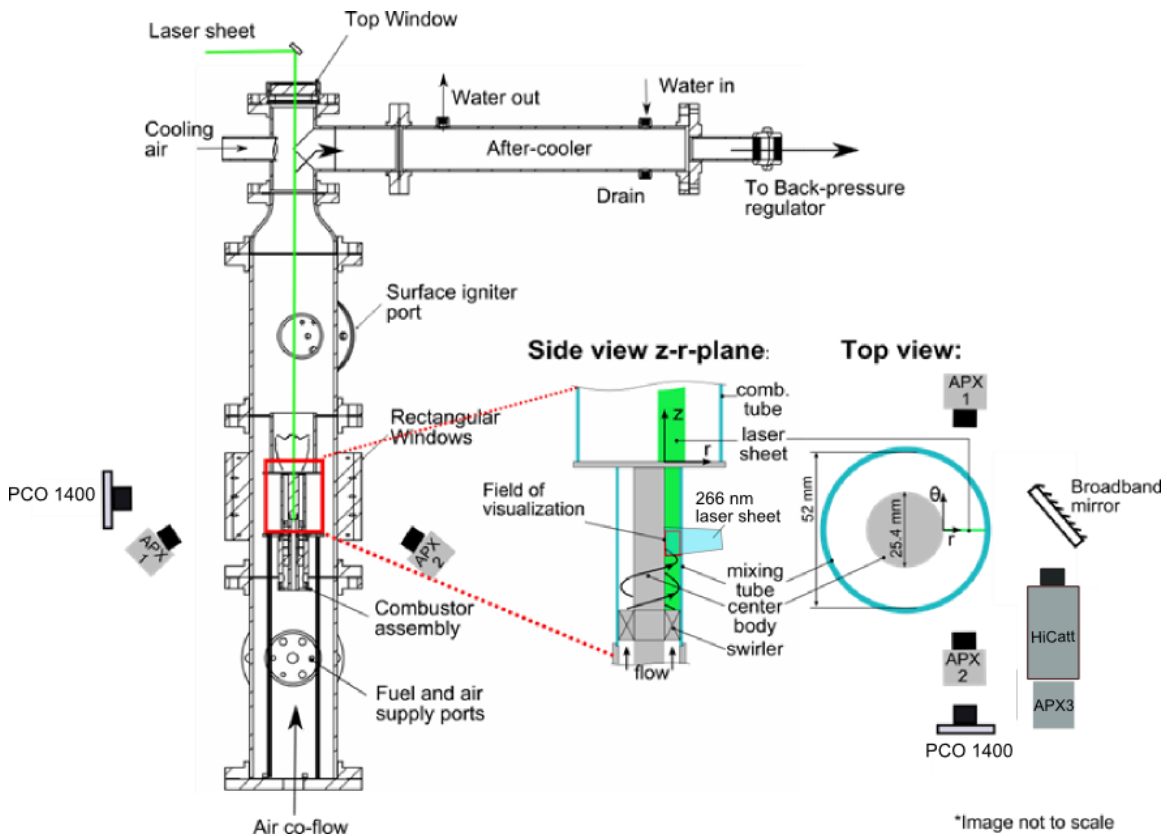


Figure 2-11 Optical diagnostic set up for elevated pressure experiments

A digital delay generator (SRS DG535) was used to provide a delay of $80 \mu\text{s}$ between laser pulses. The laser sheet thickness was kept at 1mm FWHM. The field of visualization extended from $z = -80\text{mm}$ to $z = -55\text{mm}$ where the z -coordinate is measured relative to the exit of the mixing tube. A calibration target of size 10 mm x 40 mm with dot spacing of 1 mm was translated normal to the measurement plane in the steps of 0.5 mm. Solid and liquid seeding particles were used to Mie-scatter the laser on to the particle imaging cameras. For liquid particle seeding, air flow is seeded with olive oil droplets of nominal diameter size of 1 micron. These olive particles are generated by flowing a fraction of air flow through the six-jet atomizer (TSI). For solid particle seeding, titanium oxide particles with nominal diameter of 1 micron were used. For this purpose, a copper fluidized bed

seeder was used to generate a uniformly seeded air flow. During experimental runs with solid seeding particles, the mixing tube inner wall would get covered with a fine layer of particles. So, after 2-3 runs, the combustor was disassembled to clear the mixing tube walls. For this inconvenience, the elevated pressure chamber experiments were carried out using liquid seeding particles.

The Mie scattering from the particles was captured as images of size 256 x 512 pixels at 8 kHz. Since the Mie scattering was imaged through a curved surface, the resulting distortion was corrected by applying a 3rd order polynomial mapping function obtained by the calibration.

2.3.3.1. Particle Image Processing

The three-component planar velocity field was calculated on the basis of two subsequent Mie scattering images taken at 8 kHz using the LaVision DaVis software package. The interrogation window size was 16x16 pixels corresponding to 0.8 x 0.8 mm² in physical space. A 75% overlap was chosen to get a larger number of vectors in the vicinity of the flame front (based on vaporized droplets). The distance between the wall and the first velocity vector in the radial direction was about 0.5 mm. The calibration process included correcting the images for geometrical distortion induced by the curvature of the mixing tube walls. For the current experiment, a fused-silica tube with high optical homogeneity (i.e., no lengthwise striations) was used to minimize optical defects.

Entry of the PIV laser sheet from the top of the mixing tube ensured that PIV measurements could be made near the center-body surface with a minimum of scattering. Reducing the scattering is more important with PIV than with PLIF since the laser light and scattered light are at the same frequency and so cannot be distinguished. This orientation of the laser sheet worked well at atmospheric pressure, but at higher pressure,

striations in intensity appeared in the particle scattering images. These intensity striations were random in nature and were caused by the sheet passing through the swirl flame and exhaust gases. This effect increased at higher pressures owing to the larger gradients associated with the higher Reynolds numbers. Example striations in the particle scattering images are shown in Fig 3(a). The resulting striated particle fields are problematic for PIV since they cause the cross-correlation peaks to have a two-dimensional character. Figure 3(a) shows a sample cross correlation map calculated at a location with striations and exemplifies the elongated cross-correlation function. To mitigate this effect, the intensity profile was corrected by first filtering the vertical sliding background of size 16 pixels and then applying min-max normalization filter. The resulting image had a relatively uniform particle image. A sample correlation maps for a sheet-corrected image is shown in Figure 3. The corrected image shows axisymmetric correlation peaks, as is expected for round particle images. This operation greatly improves the quality of the resulting PIV data, as shown in Fig 8(b).

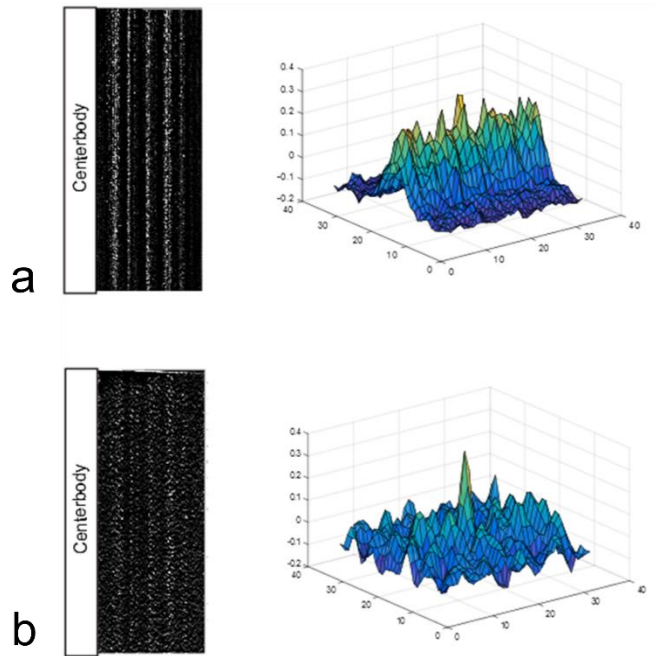


Figure 2-12 Striated Mie scattering image captured at 3 atm and corresponding correlation map (a) before sheet correction (b) after sheet correction

The uncertainty bias in the velocity calculation for atmospheric pressure experiments is measured to be less than 0.1 m/s, whereas the stereo-reconstruction error is found to be less than 0.3 pixel at all points in the field-of-view. For elevated pressure measurements, the maximum uncertainty bias and the stereo-reconstruction error was found to be 0.2 m/s and 0.6 pixel respectively.

2.3.3.2 Detection of the flame front

The flame front is detected in the particle images by detecting the low scattering signal region. Since the burnt gases occupy a larger volume for a given mass, the particle density experiences a sudden dip in its value across the flame surface. This drop in particle density could be detected in particle images captured by high-speed cameras. A MATLAB code was used to extract the flame front on the basis of threshold intensity in 8x8 px

windows with 75% overlap. For the particle images captured at 3 atm, striations were filtered out as described earlier. Then, a smoothing spatial filter was applied to get rid of high-frequency signals due to the discrete nature of the particle images. Afterwards, the image was binarized on the basis of a cut off intensity. Any morphological opening in the binarized image was corrected by taking the binarized version of the inverted image and then remove any gaps in the detected flame front. Then, an edge detection routine was applied to get the flame front location. It should be noted that the filtering also averages out the sub-millimeter flame structures which might exist in highly turbulent flames. Fig 2-13 shows the flame surface detection for hydrogen-rich flame flashback. The gamma correction of image is carried out to reveal the particles in burnt gases. The flame edge detection routine is successful in detecting wrinkled flame profiles.

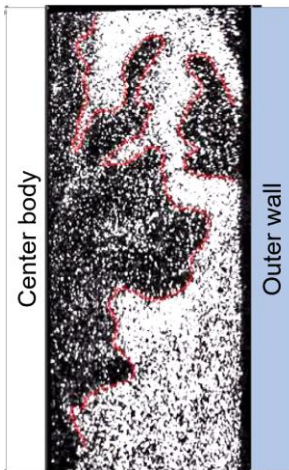


Figure 2-13 Flame edge detection on the basis of seeding particle density

Determination of flame front at elevated pressure remained challenging, particularly due to the presence of striations in the flow field. These striations were dynamic in nature and would cause the local fluence of the laser to low in certain parts of

the particle images A sample particle image of elevated pressure flame is shown in Figure 2-14. In the regions marked with red ellipse it is difficult to mark the flame surface profile.

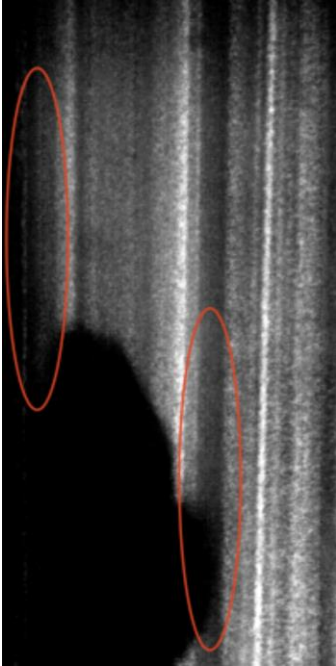


Figure 2-14 Striated particle image during the elevated pressure flashback of methane-air swirl flames

Thus, the striations in the particle images affect not only the PIV as discussed in the previous subsection, but they also affect the determination of the flame front. This issue becomes even severe with hydrogen-rich flames at elevated pressure since the flame wrinkling is very strong in the hydrogen-air flames.

CHAPTER 3 : PREMIXED FLAME FLASHBACK

This chapter is dedicated towards developing a three-dimensional understanding of the flame-flow interaction during swirl flame flashback. The swirling flame tongue during the flashback is unique in the sense that different regions of the flame tongue interact with the approach flow in different ways. This aspect of flame-flow interaction is analyzed by constructing a quasi-three-dimensional flame surface and the flow field around it. Later, in this chapter, we discuss the interaction from the flame's frame of reference.

3.1 Swirl flame flashback: A unique scenario

3.1.1 ASYMMETRICAL SITUATION IN AZIMUTHAL DIRECTION

Typically, flashback is conceptualized for the case where the oncoming flow opposes the direction of propagation of the flame [6], [58], [51], [74]. However, in swirl-flame flashback, which can be led by a three-dimensional flame tongue, the nature of the flame-flow interaction differs for different parts of the flame tongue. Figure 3-1 shows a schematic of a propagating flame tongue in front and top view. The motion of the flame tongue is marked with red arrow while the motion of the upstream fluid is marked with black arrows. The leading or the front side of the flame tongue is defined as the side which leads the propagation. It is marked with a green rectangle in Fig 3-1. The aft end or the trailing edge of the flame tongue is marked with a pink rectangle. On this end, the flame surface normal and upstream flow oppose each other. On the contrary, the leading side of the flame tongue has the flame surface normal and the upstream flow aligned in the same direction.

Results in this chapter has been published in the following article:
Rakesh Ranjan, Dominik F Ebi, Noel T Clemens, Role of inertial forces in flame-flow interaction during premixed swirl flame flashback, Proceedings of the Combustion Institute, 2018,ISSN 1540-7489, <https://doi.org/10.1016/j.proci.2018.09.010>.
Dr. Ebi conducted the flashback experiments, while the post-processing of data, development of frozen-flame assumption and the analysis of velocity fields were done by Rakesh Ranjan.

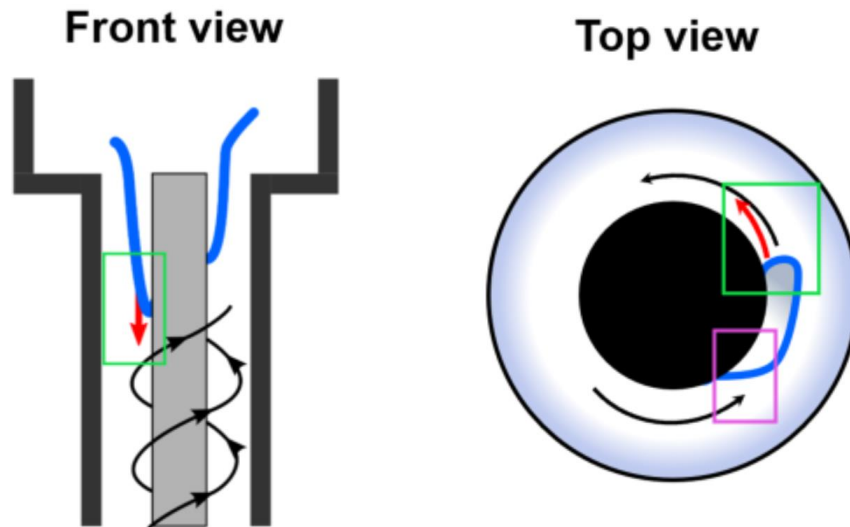


Figure 3-1 Schematic of the flame tongue propagation as viewed from the front and the top. The blue line indicates the flame surface and the black arrows show the approach flow pattern. The red arrow indicates the motion of the flame surface. The green and pink rectangles show leading and trailing sides of the flame tongue.

Thus, the flame propagation is led by the front side, since the flame ‘rides’ on the upstream flow, as opposed to the aft end where flame ‘resists’ the approach flow. From a kinematic perspective, the flame tongue gets advected in the same direction as that of the swirl.

3.1.2 FLAME SURFACE AS AN IMMATERIAL PISTON

In any type of boundary layer flashback, the flame surface deflects the low-momentum streamlines in the boundary layer, and hence modifies the velocity profile of the approaching boundary layer. As discussed in the literature review, this nature of flame-flow interaction plays a major role in the lab-frame propagation speed of the flame front. DNS of channel flow flashback shows that the leading edge of the flame front is modulated by the fluctuations in the approach flow. However, as noted by Ebi and Clemens [55] the swirling flame retains its flame tongue topography during its entire period of propagation. A possible reason for this may lie in the back-pressure support that the flame surface receives while propagating. Any back-pressure support to a flame supports the deflection

of the approach flow thereby creating favorable conditions for flame surface to move in the lab-frame. Thus, a continuously back-supported flame surface would have a preferred shape towards the approach flow owing to the continuous deflection of the streamlines in the approach flow. Experiments by Dreizler's group have shown the existence of elevated back-pressure during swirling flame flashback [75]. The existence of back-pressure has also been found to be true in flames which propagate along the vortex axis [16].

The deflection of the oncoming flow streamlines by the flame means that unlike the pure kinematic picture of flame as envisaged by the classical Lewis and von Elbe model, the flame deflects the streamlines, and this helps in the flame propagation. This deflection or the push from the flame surface acts not only towards opposing the approach flow but also towards adding to the momentum of the upstream flow, especially in the case of swirling flame flashback. For example, in the top view of Fig 3-1, the flame would push the upstream flow in azimuthal direction because the flame tongue and the upstream flow is moving in the same direction. This action of flame on the upstream flow is akin to 'sweeping' (dynamic interaction) in addition to the 'riding' (kinematic effect). The sweeping type interaction would not be apparent in the front view of Figure 3-1, since the flame normal and the flow do not point in the same direction. The discussion in the existing research literature, so far, is based on the picture presented in the front view.

To investigate the flame-flow interaction, we make certain assumptions which allow us to reconstruct the three-dimensional flow field from planar three-component PIV data. This method is described in the next subsection.

3.2 Flame-flow interaction: the three-dimensional picture

3.2.1 FLAME SURFACE TOPOLOGY

Previous studies have shown that the upstream propagation of the flame during swirl flame flashback is characterized by a unique three-dimensional shape of the flame surface [76]. We call it a flame tongue due to its convex aerodynamic shape which has a well-defined leading point i.e. the flame tip. While studying flame-flow interaction, it becomes necessary to define different regions of the flame surface since the interaction is location-specific. It also becomes necessary to define how the flow approaches the flame surface. Thus, the entire neighborhood space of the flame tongue needs to be defined.

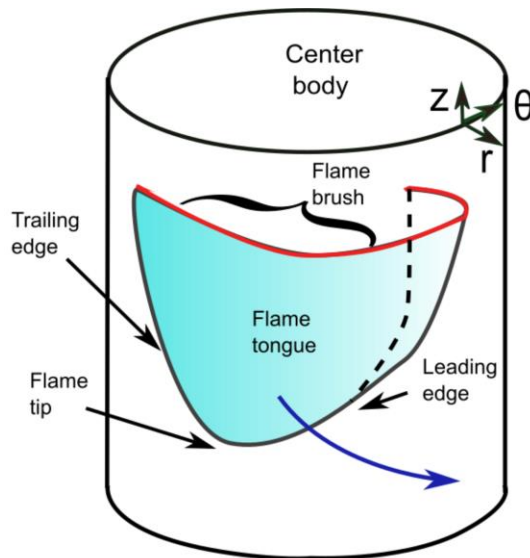


Figure 3-2 Schematic of the flame topology

Different regions on the flame surface are named on the basis of the flame movement in lab-frame. This nomenclature is illustrated in Figure 3-2. The motion of the flame tongue is marked with a blue arrow. The flame tongue is the entire flame surface in turquoise color. The leading edge of the flame is the forward side of the flame surface

which interacts with the flow upstream of it, while progressing along its spiral path (blue arrow). The flame tip is the three-dimensionally curved point of the flame tongue. This point is the most axially-upstream point. In any kind of luminosity image, this point could be identified conveniently as the ‘tip’. The trailing edge is shown in the wake side. In this region, there are small-scale flame structures, which are not shown in the schematic. This region on the flame surface does not interact with the approach flow in the same way as the leading edge of the flame. The leading edge leads the motion of the flame structure, while the trailing edge just follows up the path decided by the leading edge motion. The flame-flow interaction at the trailing edge of the flame tongue is from the sideways streamlines. The small-scale structures resist this flow, as in anchoring the flame from getting blown away, however its role is limited in deciding the global motion of the flame surface. More details on this structure could be found in Ebi et al. [53]. The flame brush is defined as the flame surface away from the center-body wall. This region usually interacts with the outer wall, not shown in this picture.

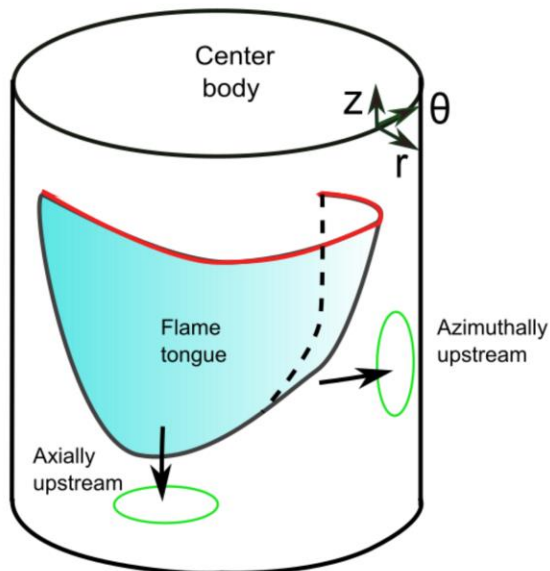


Figure 3-3 Definition of upstream locations

To specify the neighborhood of the flame tongue, we use terms such as axially upstream to mark the region upstream in z-direction, and azimuthally upstream to show the region of unburnt gases in the azimuthal direction. Otherwise, any reference to upstream in this work refers to the direction of the flame normal. It implies that a region upstream of the leading edge would be between the green ellipses in Fig 3-3, since the leading edge as defined in previous figure is inclined with respect to the z and θ -axis. If the term is “downstream of the flame surface”, it would mean normal to the flame surface and not the flow.

When the discussion is in reference to the streamlines or pathlines, the term downstream refers to the direction along the streamline or pathline. Thus, if the fluid is moving on a spiral streamline and it is commented that it burns at a downstream location it means that the fluid parcel moves along its path and gets burnt. This statement has no reference to where on the flame surface it burns.

3.2.2 FLAME SURFACE RECONSTRUCTION

Over multiple flashback experiments, the global behavior of the upstream propagation during flashback is identified as a flame tongue swirling around the center-body in the annular space of the mixing tube. This propagating flame tongue tends to maintain its shape and size as it moves around the center-body [47]; thus, we hypothesize that the flame can be modeled as “frozen”. This assumption would not be valid if the flame shape changed quickly over the timescales of observation.

The first benefit of the frozen-flame assumption is the ability to track the flame structure as a whole, by tracking a single point on the flame surface. The three-dimensional surface of the flame tongue allows us to uniquely define its flame tip in the luminosity images. Hence, the flame tongue tip can be easily tracked in the luminosity images. The

determination of the position of the flame tongue in three-dimensions is carried out as explained in Sec 2.3.1. Thus, by tracking the flame tip, the speed of the flame tongue, in axial and azimuthal directions, can be determined. Figure 3-4 shows the axial position of the flame tip for a stoichiometric methane-air flashback event. The axial velocity of the flame tip ($v_{z\text{tip}}$) is nearly constant during the observation time of about 50 ms, during which it propagated about 50 mm in the axial direction. Similarly, the angular position of the flame tip is also tracked and the angular velocity of the flame tip (Ω_{tip}) is also found to be nearly constant [47].

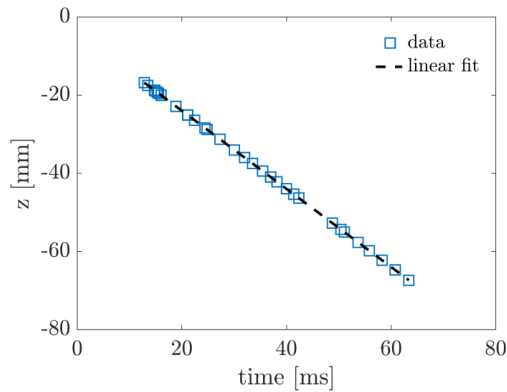


Figure 3-4 Axial position of the flame tip during upstream propagation for a single flashback event

It should be noted that for an aerodynamically-shaped flame tongue, the flame speed may vary from point-to-point depending on the local flame stretch and the approach flow speed, however for low-turbulence methane-air flashback, this effect should be minimal.

A significant benefit of the frozen-flame assumption is that it opens up the possibility of employing the principle of space-time equivalence. Space-time equivalence, which is the cornerstone of Taylor's hypothesis, means that we can map a time series to a

spatial profile by considering a frozen flow to be simply advected by the mean flow. In the case where we are conducting planar imaging, such as with PIV data, the space-time equivalence can be applied at each point in the plane. The utility of this implication is illustrated in Fig 3-5.

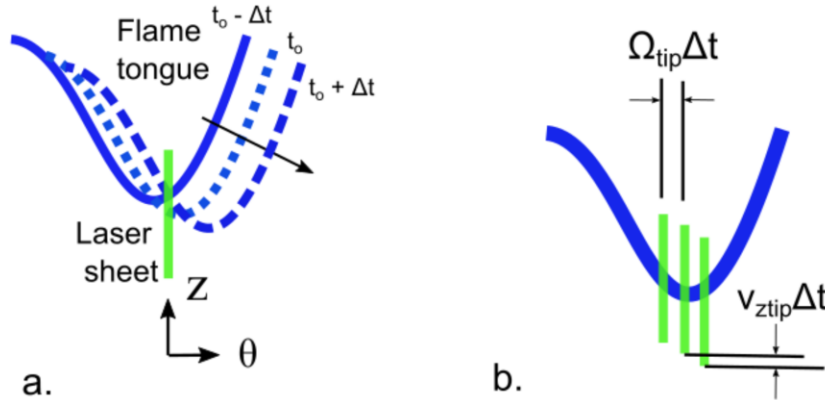


Figure 3-5 a. Three instances of a flame tongue crossing the laser sheet b. Stacking of planar flame profile to construct the flame surface

In Figure 3-5(a), the blue line in the figure marks the flame surface. The green straight line shows the location of the laser sheet. The flame surface at three different instances are marked with different dashes. The flame surface profile that crosses the laser sheet at instants $t_0 - \Delta t$, t_0 and $t_0 + \Delta t$ could be stacked in space by shifting the flame profile by $v_{ztip} \Delta t$ and $\Omega_{tip} \Delta t$ in axial and azimuthal directions, respectively. It should be noted that in this case, the PIV repetition rate must be smaller than the time-scales over which flame surface changes. In the current set of data, the flame profiles were extracted from particle images of size 256 x 512 pixels. The decrease in particle density across the flame front served as the marker for the flame surface. Particle images were captured every 250 microseconds, while the leading-edge topography was found to sustain over 20-30 milliseconds. The flame structures at the trailing edge of the flame tongue are usually of smaller size and time scales, and hence difficult to reconstruct. For propagating flames, the

flame-flow interaction at the leading edge of the flame tongue is important, and so this is the primary focus of this study.

Figure 3-6 shows the reconstructed flame surface for a methane-air flashback tongue. In this case, the flame tongue has axial and angular velocities of 0.14 m/s and 306 rad/sec (~ 4 m/s on the center-body), respectively. A corresponding luminosity image is shown for comparison. Interestingly, wrinkles on the flame surface are seen in the reconstructions, which are otherwise not very clear from the chemiluminescence signal.

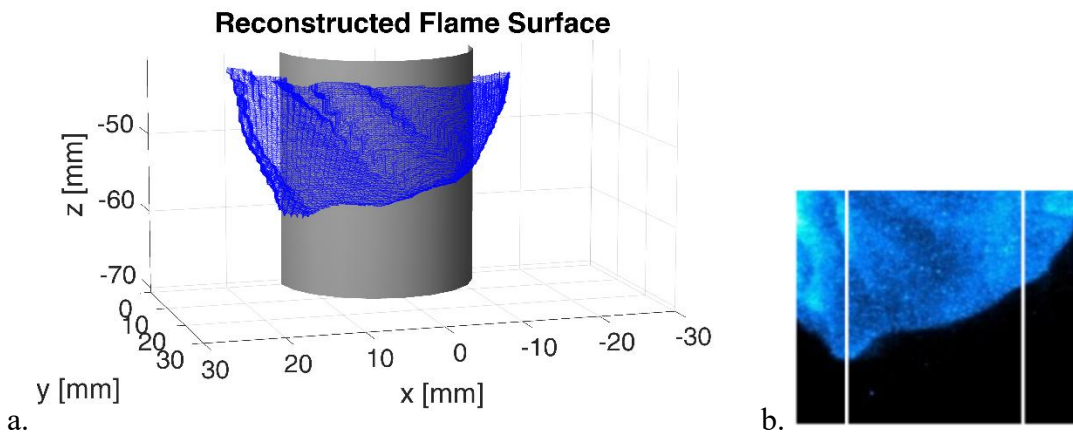


Figure 3-6 a. Flame surface reconstruction b. Luminosity image for a methane-air swirling flame flashback $Re_h = 6600$

The visual similarity between the recreated surface and the luminosity images is striking even though the reconstruction is a three-dimensional object and the luminosity image is line-of-sight integrated and thus effectively planar. One way to qualitatively assess the reconstruction of the flame surface is by projecting the reconstructed flame surface onto a plane and compare it with the luminosity images. However, since the flame is moving in space while the lab-reference observer is not, the projection taken from a single point would

provide only a single frame for comparison. For example, in Figure 3-6, the projected view of the reconstructed flame surface is chosen such that it appears similar to the luminosity image. The visual similarity would not be apparent for a different view of the reconstructed surface.

A way to circumvent this issue is by taking the projection of the reconstructed flame surface from different vantage points. Since we already know the lab-frame velocity of the flame structure ($v_{z\text{tip}}$ in axial direction, Ω_{tip} in azimuthal direction), if the vantage point moves with the $-v_{z\text{tip}}$ and $-\Omega_{\text{tip}}$ then the projections comparable to that of the instantaneous luminosity images could be obtained.

To obtain these projections, a view transformation matrix corresponding to a vantage point is calculated in MATLAB and applied to the three-dimensional flame surface. This routine is repeated for vantage points that are shifted by $-\Omega_{\text{tip}}\Delta t$ in the azimuthal direction. The camera elevation is set at 5 degrees for all projections. The resulting projection obtained gives a recreated line-integrated signal of the reconstructed flame surface. It should be noted that this method is only approximate since the local luminosity of a flame surface is dependent on more factors than just geometry, but the luminosity signal is sufficient to mark the presence of the flame along a line-of-sight. Thus, it can be used to mark the leading flame edge as seen from a given vantage point, which enables us to compare the flame tongue leading edge in the experimentally observed luminosity images and projections of the reconstructed surface. The fitting of the leading edges was found to match within ± 1 mm in the vicinity of the laser sheet location. Figure 3-7 shows a comparison of the luminosity images and the projections from reconstructions at the instants when the flame swirls towards the front of the center-body.

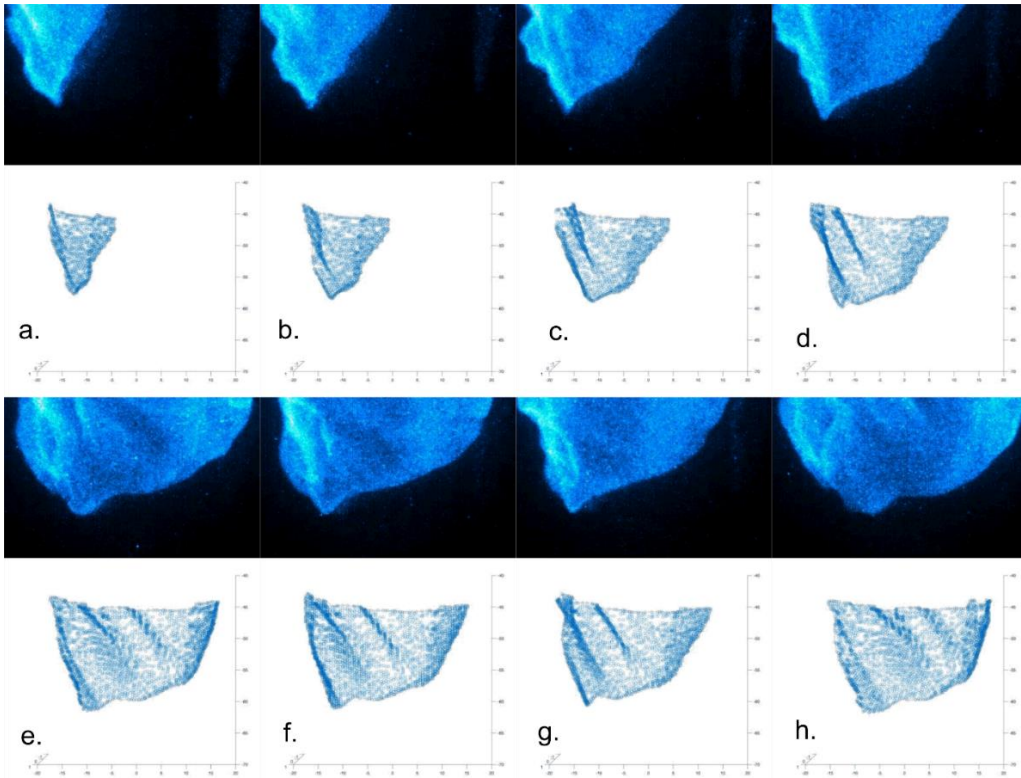


Figure 3-7 Comparison of the luminosity images and the projections from reconstructed flame surface. Each frame is taken 1 millisecond apart. The trailing edge of the flame tongue is not reconstructed.

From Figure 3-7(a) – (c) we see the flame tongue has not even crossed the laser sheet location (midline of the image) and yet, the flame surface projection created by the frozen flame assumption recreates the leading edge with remarkable similarity. This observation affirms that the flame moves as a single structure and maintains a nearly constant axial and angular velocity.

3.2.3 FLOW FIELD RECONSTRUCTION

Premixed flames respond to the local flow environment, an example of which is the wrinkling associated with a flame that propagates in a turbulent flow. Hence, the premixed flame surface is inherently coupled to the flow upstream of it. Therefore, a frozen flame

that does not change in shape over time, implies the relative flow upstream of the flame feature is also frozen in the immediate vicinity of the flame surface.

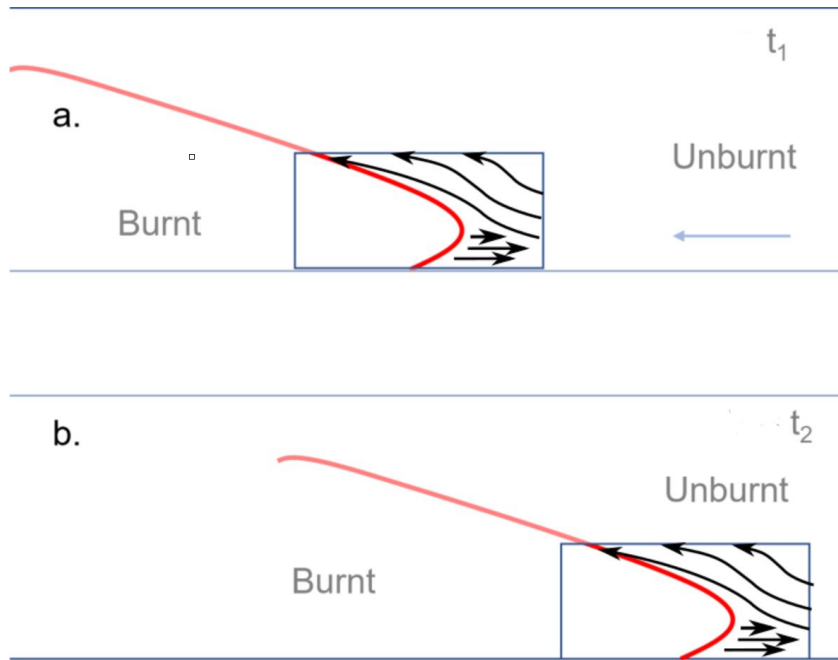


Figure 3-8 The propagating flame tongue in a channel at two different instances. The red line shows the flame and the arrow shows the direction of the streamlines.

This situation is described in Figure 3-8 where two instants in time, t_1 and t_2 of flame propagation, are shown. As the flame propagates it retains its shape and size. The frozen flame assumption imposes the condition that the flame surface at these two instants are the same. Subsequently, due to aerodynamic considerations, it can be inferred that the flow immediately upstream or downstream of the flame does not change in time. Thus, the region inside the marked rectangles in Figure 3-8 at two different instants are the same. This two-dimensional picture can be extended to all dimensions, if the flame surface retains its three-dimensional topography.

For the assessment of the validity of this assumption, we check the value of divergence in the reconstructed flow field. If the flow were incompressible, then the

divergence value should be zero everywhere; however, at the flame surface, the dilatation should cause the divergence to be non-zero. In Figure 3-9 (a), we show the distribution of the normalized divergence values in the reconstructed flow field in the incoming unburnt gases only.

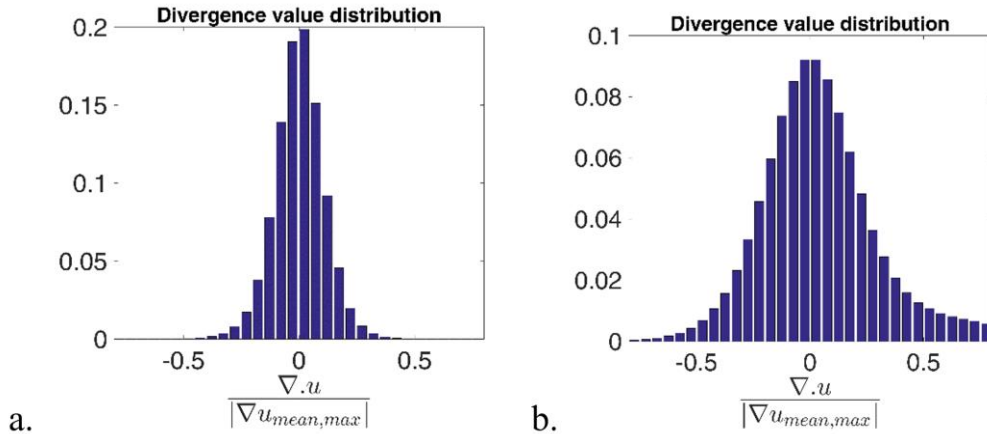


Figure 3-9 Divergence value distribution in the reconstructed flow field with a. only unburnt gases b. unburnt, burnt and flame surface

The divergence is normalized by the maximum gradient in the mean velocity profile. The resulting distribution is normal and has a standard deviation of 0.1. In Figure 3-9(b), the divergence distribution is shown for all regions irrespective if they are unburnt or burnt. As is clear, the distribution is not symmetric and the tail on the positive side extends farther with the skewness value of 0.75. This observation is expected since the divergence near the flame front is expected to be positive owing to dilatation effects.

Figure 3-10 shows the isosurface plots of the normalized divergence value of 0.4 and 0.6 in the reconstructed flow field. It is evident that large divergence values exist very close to the flame surface. This observation gives us confidence that the reconstruction of the flow field satisfies the physics associated with the flow.

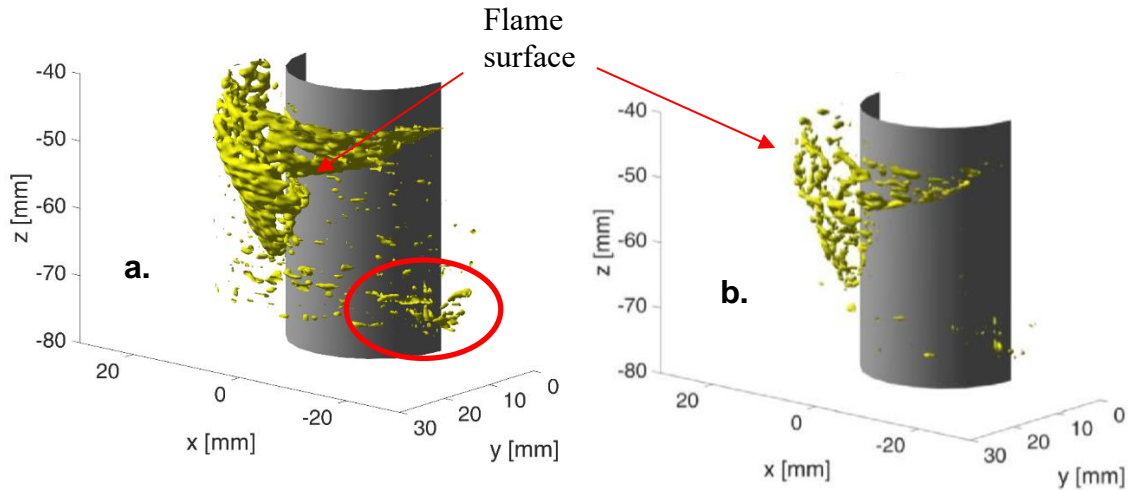


Figure 3-10 Isosurface plot of normalized divergence value of a. 0.4 and b. 0.6. Pockets of high divergence are marked with a red circle

There are scattered pockets of large-divergence in the flow field (red circled in Figure 3-10(a)), however they lie close to the outer wall, away from the leading edge of the flame. These large-divergence values at large radial locations are a result of stacking the velocity data in given azimuthal steps, which at large radial locations increases the grid spacing. At smaller radial locations, this error is smaller. Thus, under the frozen flow assumption, the reconstructed flow field is - at best - “quasi-instantaneous” in nature. In regions away from the flame surface, or at large radial locations, the three-dimensional stitching of the velocity field would not be valid. In highly turbulent conditions, the flow field reconstruction in the azimuthal direction would require highly-resolved data to enable any kind of out-of-plane reconstruction.

The reconstructed flame surface and the quasi-instantaneous flow provides us the complete three-dimensional flame surface and flow field during flashback, albeit under the frozen flame-flow assumption. In subsequent subsections, we use these data to discuss the nature of flame-flow interaction for these low-turbulence cases. We mention the pathlines and streamlines constructed using the quasi-instantaneous flow as quasi-pathlines and quasi-streamlines respectively.

3.2.3 THE QUASI-INSTANTANEOUS FLAME-FLOW INTERACTION

Instantaneous streamlines in a swirling flow are three-dimensional in nature, as shown in Figure 3-11. These streamlines originate from $z = -65$ mm (upstream of the mixing tube exit) at a radial location of $r = 2$ mm (away from the center-body surface). In an undisturbed swirling flow, these quasi-streamlines would show little sign of deflection, as is marked by the black ellipse in the Figure 3-11. However, quasi-streamlines which exist closer to the flame tongue are deflected by the approach flow. In the regions marked by the yellow ellipse, the deflection is apparent as an increase in the azimuthal component of the velocity and a decrease in the axial component (z -direction), identifiable as the near-horizontal tilt of the quasi-streamlines. Interestingly, further along the z -axis ($-55 < z < -45$ mm) the quasi-streamlines exhibit the “push effect” from the flame in the radial direction as well. This “push-effect” region is marked with a green ellipse, which when compared with the undisturbed flow (black ellipse) shows how the flame surface acts as a piston in pushing the flow out of the way. These quasi-streamlines seem to wrap around the flame surface, instead of ending on it, which indicates that the push effect from the flame surface acts in all three-directions, thereby shaping the quasi-streamlines.

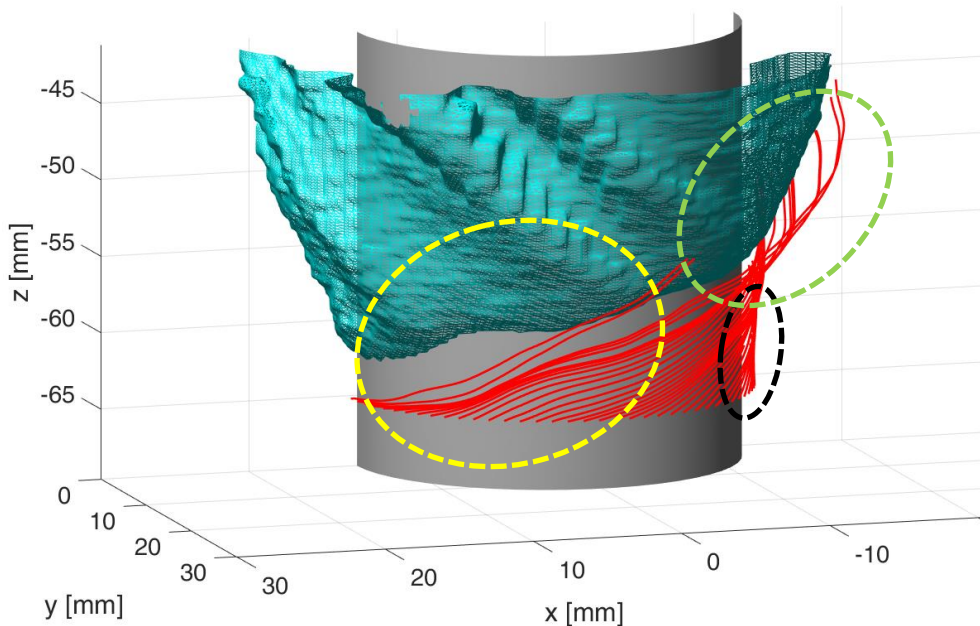


Figure 3-11 Instantaneous quasi-streamlines in front of the flame surface. These streamlines emanate in the boundary layer along the center-body

3.2.4 QUASI-PATHLINES

A logical way to understand the flame-flow interaction is to investigate it from the perspective of streamlines that get disturbed due to the approach flow, as discussed above. An even better way to understand it is to track a fluid parcel starting in the oncoming flow and see how it gets affected by the flame surface. For an unsteady flow, the instantaneous streamlines are not the same as the pathlines [77]. For example, if in the previous subsection (Figure 3-9), one treats the quasi-streamlines as the quasi-pathlines, the fluid parcels approaching the flame surface would appear to escape the fate of getting burnt since the quasi-streamlines wrap around the flame surface. This picture plainly ignores the fact that the flame surface is also moving. If one tracks the fluid parcel's movement in space, a simultaneous estimation of flame surface motion would also be needed to understand how the fluid-parcel and the flame interact. In other words, it is necessary to know how the fluid parcel moves with respect to the flame surface.

Owing to these considerations, it is useful to view the flow from the frame-of-reference of the flame. While defining the flame's frame of reference itself can be a challenging task, it is well-defined for a propagating swirl flame tongue. We have already obtained the velocity of the flame tongue, and therefore to analyze the flow from the flame's frame of reference, we must subtract the flame's velocity from the fluid velocity field. In the flame's frame of reference, the flow is steady (ignoring turbulence), and so quasi-pathlines and quasi-streamlines are the same. Thus, the fluid particle movement can be tracked in space.

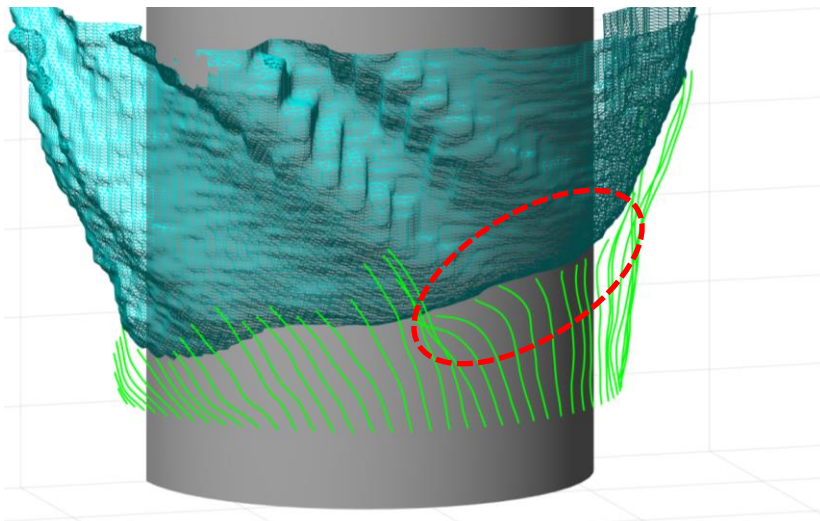


Figure 3-12 Quasi-streamlines in flame's frame of reference

In the flame's frame of reference, quasi-streamlines are the same as quasi-pathlines. Thus, in the following discussion these pathlines shall be referred to as streamlines, unless specified otherwise. Figure 3-12 shows the quasi-streamlines in the approach flow as seen from the flame's frame of reference. The radial and axial points of streamline initiation is the same as that in Figure 3-11. However, unlike the quasi-streamlines in the lab-frame

which move away from the flame surface, the quasi-streamlines in the flame-frame approach the flame surface. This picture tells us that the flame moves faster than the flow upstream of it. It is also seen that as the quasi-streamlines approach the leading edge of the flame, they diverge (shown in red ellipse). This divergence indicates that the oncoming flow decelerates upstream of the flame tongue, in the axial as well as the azimuthal direction. On the other hand, in the *lab-frame*, the flame is found to cause an *acceleration* of the approach flow in the azimuthal direction while it slows down the flow in the axial direction, as illustrated in Figure 3-11. As discussed at the start of this chapter, the lab frame can be misleading when considering the flame-flow interaction. Evidence for this is that in the flame's frame of reference the flame causes deceleration of the approach flow in both the axial and azimuthal directions.

3.2.5 NON-INERTIAL FRAME OF REFERENCE

In the previous subsection, we noted that the quasi-streamlines diverge as they approach the flame tongue's leading edge. To further analyze this kind of interaction, we investigate the motion of any fluid parcel approaching the flame tongue. We apply the fundamentals of Newtonian mechanics to understand the dynamics of the interaction.

According to Newtonian mechanics, if the observer's frame of reference is accelerating, to satisfy the force-acceleration relation, there should be fictitious forces applied to the mass whose motion is described in the observer's frame. For rectilinear motions, these forces appear only when the speed of the frame is changing in time, such as the apparent force experienced during sudden braking of vehicles. For rotating frames of reference, even if the angular velocity is constant, the velocity vector changes its direction and thus the frames are accelerating in nature. In such a case, there would be a fictitious force acting on the mass.

A swirling flame feature rotates in the lab-frame, and so any frame associated with a swirling flame feature is accelerating in nature, which introduces fictitious forces such as centrifugal and Coriolis forces. The centrifugal force acts radially outward, whereas the Coriolis force acts perpendicular to the frame-relative velocity of the particle. These forces are dependent on the frames of choice such that the Newtonian laws of motion are satisfied. Centrifugal forces are often used in swirling flows to define the radial pressure gradient. However, the Coriolis force is usually not discussed in the context of swirling flows. In the next paragraph, we discuss its importance and its role in the flame-flow interaction.

Forces acting on a moving particle can be frame-independent, such as pressure and viscous forces, or frame-dependent, such as centrifugal and Coriolis forces. Our choice of frame is usually to simplify the dynamic force balance. For example, if we consider a point mass (m) tied with a string used to rotate it around its axis with angular velocity (Ω_0), we choose to work with either from the lab-frame (inertial) or mass-frame (non-inertial). In the lab-frame, we have centripetal acceleration ($\Omega_0^2 r$) which acts radially inward; thus, tension in the string is $T = m\Omega_0^2 r$. In point mass frame of reference, the particle does not move, but the observer's frame is accelerating. The centrifugal force which acts radially outward is equal to the tension T , which results in $T = m\Omega_0^2 r$. The Coriolis force would be zero by definition, since the relative velocity of the particle is zero. Tension in the string is frame-independent in nature, which means that in any observer's frame, whether moving or not, T should be measured to be $m\Omega_0^2 r$. The above two frames are frames of choice since they result in direct measurement of the tension in the string.

This problem can be analyzed from a frame of reference other than the that of the lab or the point mass. For example, let us say that the observer moves with an angular velocity Ω_f , which is different from than that of the point mass. In such a case, the centrifugal force would be $m\Omega_f^2 r$. In this frame, the particle is not static since it moves with

a relative velocity of $(\Omega_f - \Omega_0)r$ in the direction opposite of the frame. It means that the Coriolis force is $2m\Omega_f(\Omega_f - \Omega_0)$, which acts in radially inward. Since, in this frame, the particle velocity is also changing continuously, there would be a centripetal acceleration given by $(\Omega_f - \Omega_0)^2r$, which acts radially inward. Again, using the force balance equation, the tension in the string is $T = m\Omega_f^2r - 2m\Omega_f(\Omega_f - \Omega_0) + m(\Omega_f - \Omega_0)^2r = m\Omega_0^2r$, and is the same as in the other frames. This analysis illustrates the fact that the force balance on a point mass could be worked out in any frame of reference. However, our choice of frame (in this case, lab-frame and mass-frame) is made in order to simplify the calculations. In the most general case, the centrifugal force, Coriolis force and centripetal acceleration, all three factors associated with curvilinear motion play a role in determining the dynamics of the point mass. It should also be noted that all the forces in this example point along the radial direction; hence, identifying these terms would simply not be possible until one correctly knows the three-dimensional velocity field and the angular velocity of the observer's frame. Typically, these two factors are not known, but fortunately they are in the current space-time reconstructions; hence, we are able to determine the fundamentals of the dynamic balance on the point mass, which we shall later use to analyze the motion of a fluid parcel approaching the flame tongue.

3.2.6 Regions with the maximum blockage from the flame surface

Understanding the interaction between a three-dimensionally curved flame tongue and the swirling flow requires the assessment of the characteristic streamlines which represent the interaction in a true manner. One needs to identify these streamlines such that the strength of interaction could be evaluated.

Figure 3-13 illustrates the flame-flow interaction behavior at the tip and the leading side of the flame tongue during swirl flame flashback. The red arrow indicates the direction

of the mean flow field in the absence of a flame. The blue arrow indicates the motion of the flame tongue in the lab-frame.

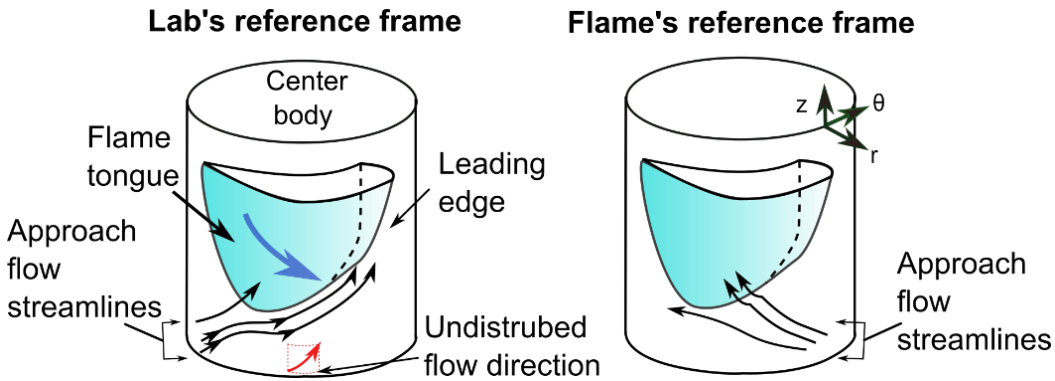


Figure 3-13 Isometric views of flame-flow interaction at the leading side of the flame tongue in the lab and flame's frame of reference

The flame tongue has a highly three-dimensional topography, which means that in the flame-frame, when the flow approaches the flame tongue and the streamlines diverge, every fluid parcel associated with a streamline interacts with the flame surface differently. The strong three-dimensional curvature of the flame surface leads to three-dimensional relieving of the blockage effect on the approach flow. As shown in Figure 3-11, the streamline that is closer to the flame tip has a stronger three-dimensional relieving effect as compared to the flame leading edge.

This leads us to the question regarding which streamline (or set of streamlines) reveal the strength of the blockage effect. In a two-dimensional case, it would have been convenient to consider the streamlines very close to the wall (but beyond the quenching distance), since the flame-flow interaction is the strongest in the low-approach flow momentum regions.

In the current case, we are studying the interaction from the flame frame of reference. In this frame, any object which is not moving in the lab-frame would have a velocity opposite to that of the flame in the lab-frame. Hence, the center-body, which is static in the lab-frame, moves with an axial velocity of $v_{z\text{tip}}$ in the positive z-direction (upwards) and turns with an angular velocity $-\Omega_{\text{tip}}$ (clockwise, since the flame moves anti-clockwise in lab-frame). Owing to viscous effects near the wall, the approach flow is provided momentum by the rotating wall, which implies that the natural choice for the set of streamlines to be studied in a channel-flow flashback is not the same as in swirl-flame flashback. Instead, the nature of the interaction between the flame-tongue and the approach flow is very similar to that of the flow at the nose of curved surface such as sphere. In those cases, the maximum blockage effect is marked by the minimum velocity, i.e., at the stagnation point.

Hence, analogously, we approach the assessment of the blockage effect by tracking the velocity of the fluid parcels. For this purpose, the regions with minimum velocity are found and the behavior of the fluid parcels passing through those regions are analyzed.

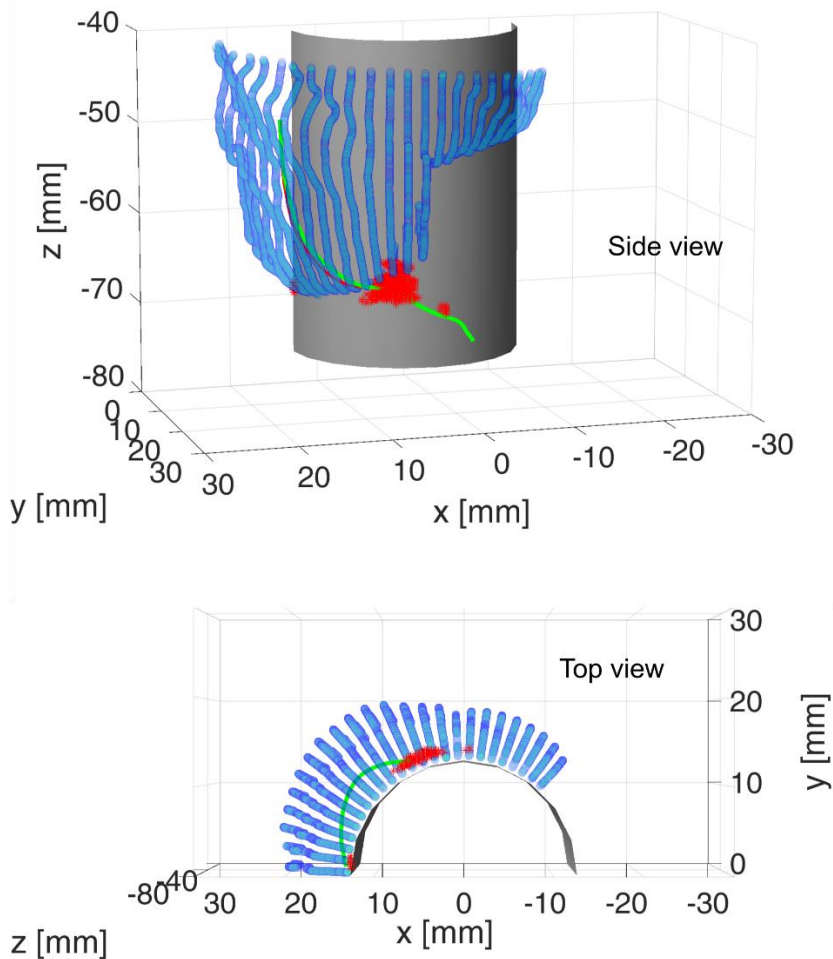


Figure 3-14 Wireframe representation of the flame surface(blue) and points of maximum blockage effect (red dots) and a representative streamline

Figure 3-14 shows the top and side view of the wireframe flame surface as constructed from the planar information of a stoichiometric methane-air flame flashback. The green line shows a quasi-streamline in the flame frame of reference. The region with maximum blockage is marked with red dots. These points indicate the regions of minimum velocity (slowest fluid parcels) in the entire reconstructed fluid flow. Unsurprisingly, most of these points are in the proximity of the flame tongue's leading edge. This region of maximum blockage is approximately 2 mm x 6 mm x 6 mm in the radial, azimuthal and

axial directions, respectively. A typical path of a fluid parcel after passing through this volume is marked by the radially outward deflection that would not occur if not for the blockage effect. Any such deflection also assists in the propagation of the flame since it reduces the flame-normal approach flow velocity. In a subsequent subsection, we shall study the kinematics of the fluid parcel that passes through the maximum blockage volume.

3.2.7 KINEMATICS OF THE FLUID PARCEL

In section 3.2.5, we discussed the role of fictitious forces arising in an accelerating frame. While analyzing the kinematics of a fluid parcel which approaches the flame tongue, it becomes necessary to evaluate these fictitious forces. These forces can play an important role in determining the fluid particle path, which could be missed by an observer in the lab frame.

Figure 3-15 shows a schematic of a quasi-pathline approaching the leading edge of the flame tongue.

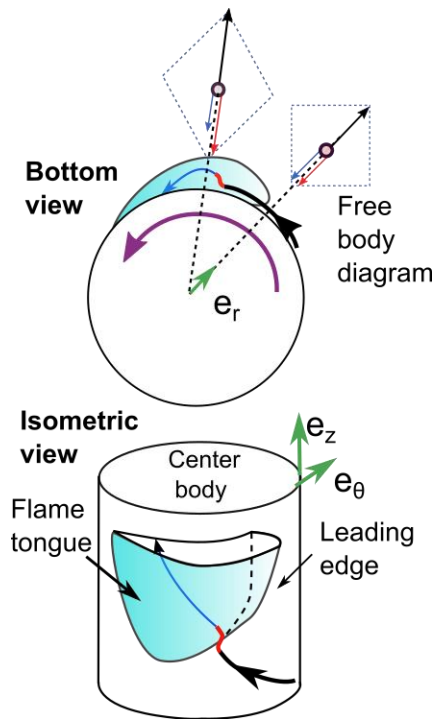


Figure 3-15 Representative quasi-streamline in flame's frame of reference. Free body diagram illustrates the radial balance of forces, centrifugal (black) pressure gradient (blue) and coriolis force (red)

The black portion of the line shows the path that is unaffected by the flame surface. This pathline is spiral in nature, as would be typical of swirling flows. The red portion of the pathline shows the radial deflection prior to reaching the flame surface. The blue portion of the pathline shows the path of the fluid parcel after crossing the flame surface. This behavior of the pathline within the burnt gases does not seem to be present in 2D channel-flow flashback. For example, in the channel flow flashback DNS carried out by Gruber et al. [57], the streamlines were found to straighten out along the channel length. Figure 3-16 shows the quantitative evaluation of the kinematics at the point of maximum blockage. The region A marks the deceleration of the particle as it approaches the flame surface (black line in Fig 3-15). In the flame frame of reference, the relative speed of the fluid parcel reaches its minimum value. In the lab frame, this situation would correspond

to the fluid parcel being pushed by the flame to nearly the same speed as that of the flame tongue. It should be noted that towards the end of the deceleration stage, the fluid parcel is deflected radially outward, as shown by the increase in the radial component. In stage B, or the acceleration stage, the fluid parcel crosses the flame. The flame crossing is shown as the red vertical line, which corresponds to the maximum divergence along the quasi-pathline. In stage C, corresponding to the burnt gases section, the velocity components increase, although the radial component moves to negative values, which signifies the bending of fluid parcel paths. It should be noted that since the flame has a lab-frame velocity in the azimuthal and axial directions only, the radial component of velocity is unchanged for an observer in both the lab and flame frames of reference. An explanation of this behavior of a fluid parcel would require an analysis from a Lagrangian perspective. In next subsection, we discuss the forces acting on the fluid parcel.

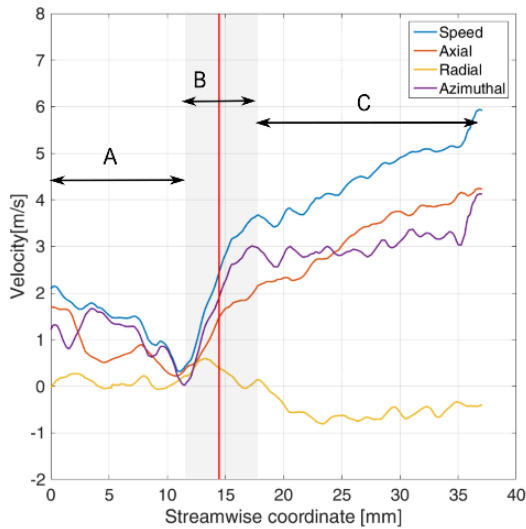


Figure 3-16 Velocity components along the quasi-pathline. Red line indicates the location of maximum divergence.

3.2.8 DYNAMICS OF THE FLUID PARCEL

We saw in Figure 3-16 that the speed, axial velocity and azimuthal velocity increase in magnitude along a pathline as a fluid parcel crosses the flame front, while the radial velocity turns negative. To analyze this behavior, we use the force balance equation for the approaching particle in a rotating frame of reference: [10]

$$\frac{D\mathbf{u}_p}{Dt} = \underbrace{-\frac{\nabla p}{\rho}}_{\text{Pressure gradient}} - \underbrace{2\boldsymbol{\Omega}_f \times \mathbf{u}_p}_{\text{Coriolis}} - \underbrace{\boldsymbol{\Omega}_f \times (\boldsymbol{\Omega}_f \times \mathbf{r})}_{\text{Centrifugal}} + \mathbf{F}_{viscous},$$

where $\boldsymbol{\Omega}_f = \Omega_{tip} \hat{\mathbf{e}}_z$, $\mathbf{r} = r \hat{\mathbf{e}}_r + \theta \hat{\mathbf{e}}_\theta + z \hat{\mathbf{e}}_z$ and $\mathbf{u}_p = u_z \hat{\mathbf{e}}_z + u_\theta \hat{\mathbf{e}}_\theta + u_r \hat{\mathbf{e}}_r$, the quantities $\hat{\mathbf{e}}_r$, $\hat{\mathbf{e}}_\theta$ and $\hat{\mathbf{e}}_z$ represent the unit vectors in radial, azimuthal and axial directions as represented in Fig 3-13. The centrifugal term is calculated as $\Omega_{tip}^2 r \hat{\mathbf{e}}_r$ and the Coriolis term is evaluated as $-2\Omega_{tip} u_\theta \hat{\mathbf{e}}_r - 2\Omega_{tip} u_r \hat{\mathbf{e}}_\theta$. The material acceleration is controlled by these four forces acting on the particle. It should be noted that the pressure gradient and viscous forces are frame-invariant, whereas the Coriolis and centrifugal forces are frame-dependent fictitious forces.

For the axial motion of the particle, centrifugal and Coriolis forces play no role in the current flow configuration since these forces act in the r - θ plane. Thus, the pressure gradient and the viscous forces are responsible for the deceleration and acceleration of the particle upstream and downstream of the flame, respectively. This behavior is in accordance with previous studies on channel-flow flashback where the flow accelerates after burning. The r - θ motion however is different from the 2D channel-flow picture since the Coriolis and centrifugal forces come into play. Considering the particle momentum equation, we can analyze the dynamics of the flame-flow interaction. In Figure 3-16, during the deceleration stage of the flame-flow interaction, the particle approaching the flame

along the representative pathline slows down due to the dilatation. The dilatation induces a pressure gradient in the axial-azimuthal direction due to volumetric expansion at the flame surface.

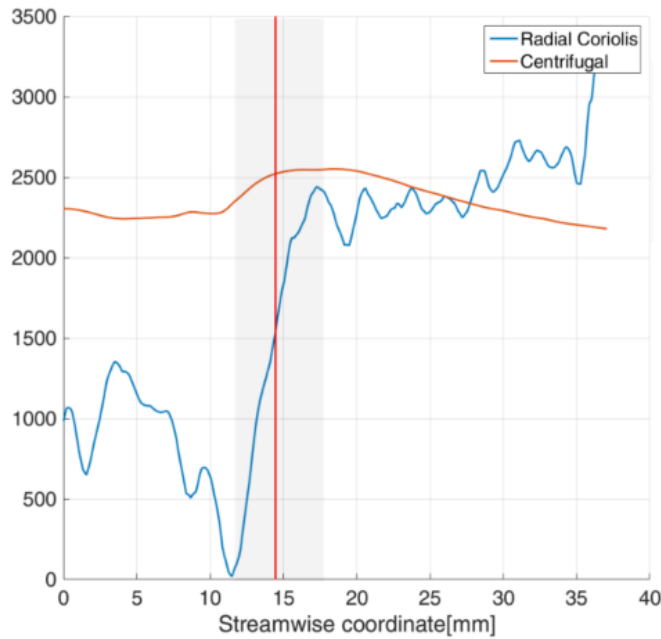


Figure 3-17 Fictitious forces acting on the fluid parcel through representative pathline

The corresponding fictitious forces are plotted in Figure 3-17. Considering the dynamic balance as depicted in Figure 3-17, the decrease in u_θ leads to the loss of the radial component of the Coriolis force ($-2\Omega_{tip}u_\theta$), which results in the dominance of the centrifugal force ($\Omega_{tip}^2 r$). Subsequently, the second stage of the flame-flow interaction initiates and u_r starts to increase due to centrifugal action. An increase in u_r leads to the rise of the azimuthal component of the Coriolis force ($-2\Omega_{tip}u_r$), which starts countering the blockage effect and bends the pathline in the azimuthal direction, and thus, the particle is brought onto the flame surface. In the burnt gases, the particle experiences a gradual acceleration as shown in Figure 3-14. The gradual rise in u_θ leads to an increase in the radial

Coriolis force. The competing centrifugal force experiences no change upon burning since it depends on the radial location and the angular velocity of the frame. Thus, the larger magnitude Coriolis force assists in bending of particle paths towards the center-body. The particle moves to smaller radial location, which further reduces the centrifugal action. At this stage, the particle continues moving in the negative radial direction. It should be noted that the pressure gradient and viscous forces also play a role here. However, an estimation of these terms from the available measurements would have large uncertainty.

Qualitatively, the behavior of the quasi-pathlines (Figure 3-14) is found to be consistent across multiple experimental runs; however, the flame shape varies across these runs. Any attempt to get the mean flame shape and the average upstream velocity field leads to the loss of information due to the instantaneous variations in the flame-flow interaction.

3.2.9 DYNAMIC TERMS FOR MULTIPLE QUASI-PATHLINES

Our discussion of fluid parcel kinematics and dynamics has been based on the representative streamline. However, the dilatation-induced blockage effect of the flame is imposed on the volume near the tip of the flame tongue, as discussed in section 3.2.6. In this subsection, we show the Coriolis and centrifugal forces for 100 quasi-pathlines going through the volume experiencing the flame blockage. Figure 3-18 shows the variation in the centrifugal acceleration experienced for each of these pathlines. It is clear that most pathlines exhibit similar behavior. Since the centrifugal acceleration is proportional to the radial coordinate value (given the constant angular velocity of the reference frame), the radial motion of the fluid parcel could also be inferred from this picture. It should be noted that relative change in centrifugal force is not large (~10%). It also shows that the radial

deflection in the particle paths is small compared to the radial location of the particle (approximately equal to radius of the center-body).

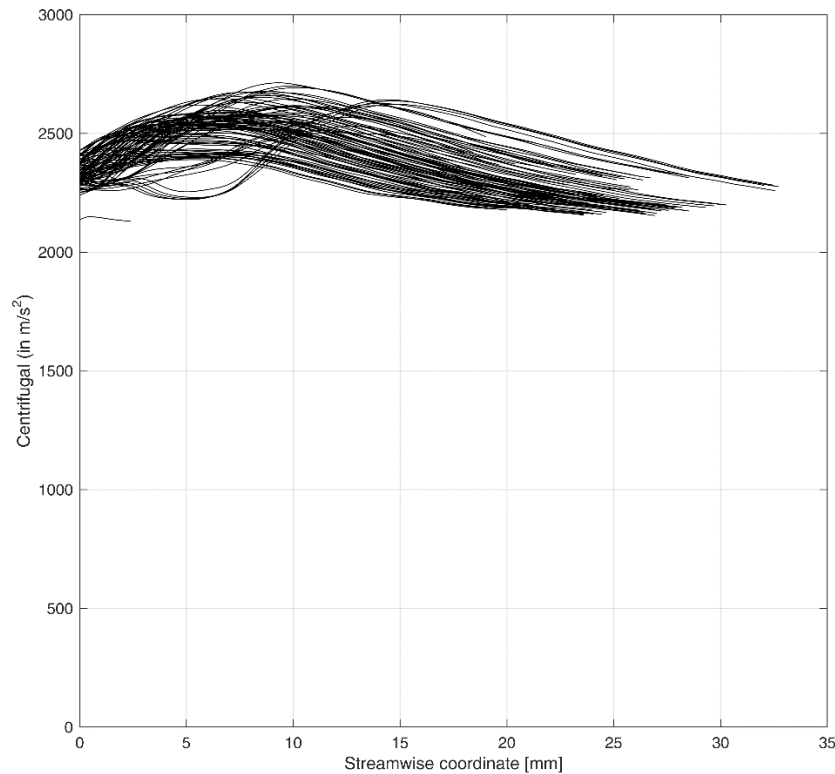


Figure 3-18 Variation of centrifugal term acting on the 100 different fluid particles after the point of maximum blockage.

Figure 3-19 shows the variation in the radial component of the Coriolis force as it crosses the point of maximum blockage. In comparison to the centrifugal force, the relative change in the Coriolis acceleration is very large (~500%). This increase in the Coriolis term directly corresponds to the increase in azimuthal velocity, since the reference frame has a constant angular velocity. Interestingly, the Coriolis term has no dependence on the radial location of the fluid parcel. It does, however, have a strong dependence on the dilatation since it is the dilatation that induces the large relative change in velocity.

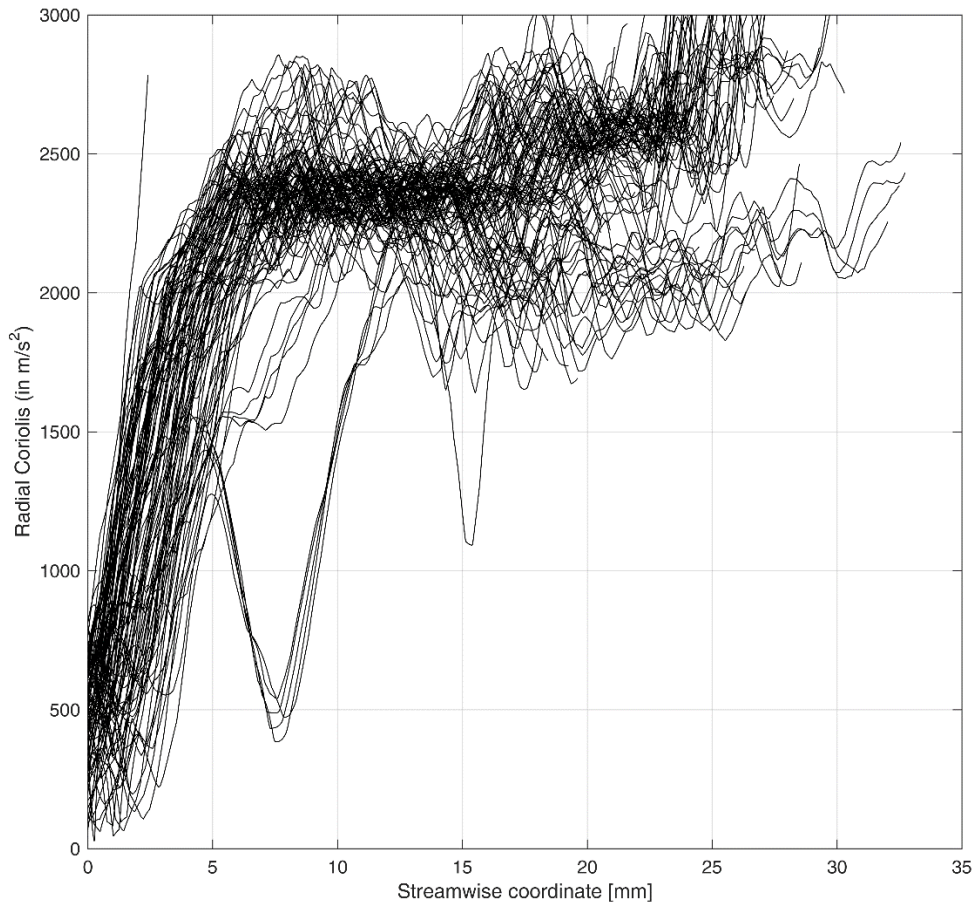


Figure 3-19 Variation in Coriolis force along 100 quasi-pathlines after the point of maximum blockage

A tempting thought to further understand the flame-flow interaction is to estimate the rest of the terms in the governing equation. Theoretically, barring viscous forces, the remaining terms of the governing kinematic equation could be measured. However, the accuracy of the gradient terms remains in question for a quasi-reconstructed velocity field. In this analysis, neither the Coriolis, nor the centrifugal term depend on any derivative term of velocity. However, the radial acceleration term in the governing equation requires that derivatives be computed from the data. Figure 3-18 shows the radial acceleration term for

the same quasi-pathlines as shown in the previous two figures. It can be seen that the radial acceleration fluctuates from -1000 to 1000 m/sec^2 , which is of the same order as that of the Coriolis and centrifugal terms. Given the lack of precision of this methodology, such an approach is not used in this study.

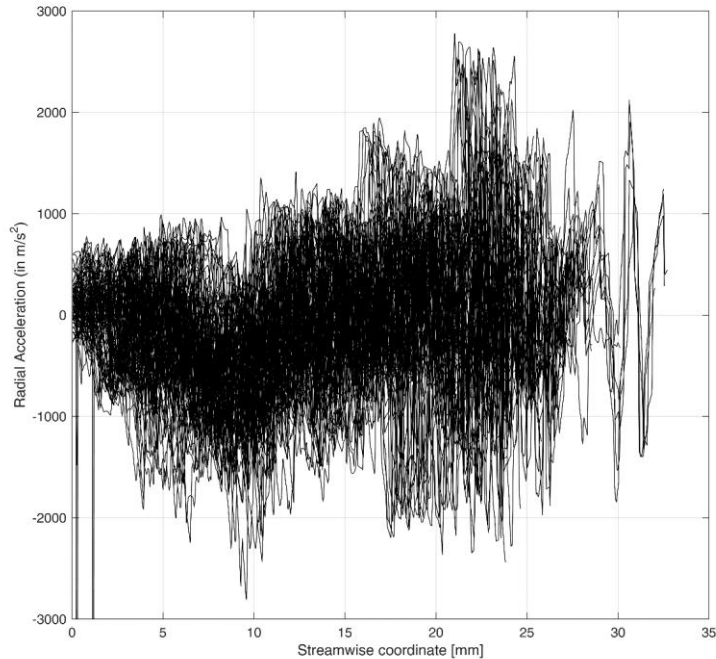


Figure 3-20 Radial acceleration along 100 different quasi-pathlines after point of maximum blockage

3.3 Conclusions

This chapter dealt with the detailed understanding of how flame-flow interaction takes place in an annular swirling environment. Flashback of methane-air flames under low-turbulence ($Re_h = 6600$) conditions was investigated under the assumption that the flame tongue maintains its shape as it swirls around the center-body. The leading edge of the flame tongue was reconstructed from time-resolved PIV data using space-time construction. The projections of the reconstructed flame surface were found to be in good

match with the corresponding luminosity images. The flow field reconstruction was assessed by computing the divergence upstream and downstream of the flame. It was noted that the pockets of large divergence values occurred near the flame surface or at large radial locations. Thus, it was concluded that the regions of interest in this study, i.e. the regions close to the flame tongue leading edge were constructed well enough to construct the fluid streamlines in the reconstructed flow field. Further, the three-dimensional quasi-streamlines were constructed to demonstrate the blockage effect from the flame surface. It was noted for the first time that it acts not only in radial but all three directions.

Further analysis of the flame-flow interaction was carried out from the flame frame of reference. A fluid parcel was tracked by using the quasi-reconstructed flow field. It was noted that the balance between the Coriolis and centrifugal terms is disturbed during the flame-flow interaction. The change in these two fictitious forces were concomitant with the radial bending of the representative quasi-pathline. The radial bending of the pathlines may have some role in the generation of backpressure at the flame surface, however the limitation in finding the gradient terms correctly did not allow us to estimate the pressure gradient.

This understanding of the physics underlying the fluid and flame interaction also helps us to assess how a “rich fuel-air pocket” would interact with a flame surface. This idea is extended to the next chapter to understand how stratified flows interact with the flame surface.

CHAPTER 4 : STRATIFIED FLAME FLASHBACK

In this chapter, we discuss the global propagation behavior of stratified swirl flames and the flame-flow interaction during flashback. The flashback experiments have been conducted at pressures up to 5 atm and the range of Reynolds number (based on the hydraulic diameter) is within the range 2×10^3 to 3.3×10^5 . The level of stratification in the mixing tube is kept at its maximum, which means that for all flashback runs fuel is injected through the ports on the swirler vanes. It was noted that the stratification in the fuel-flow mixture delays the flashback, hence the global equivalence ratios are kept at values higher than that of the premixed flame flashback runs.

4.1 GLOBAL BEHAVIOR OF STRATIFIED FLAME FLASHBACK

4.1.1 Flame stabilization behavior

In fully premixed flashback the flame starts from a stable swirl position, propagates upstream, and stabilizes in the wake of swirler vanes. For stratified flame flashback, the flame can also stabilize on the swirler vanes, but can also stabilize aerodynamically further up in the mixing tube. These different stabilization modes are illustrated in Figure 4-1. Images shown in this figure were captured with a point and shoot camera (Samsung WB350F) which was mounted outside the pressure chamber to capture the real-time video of flashback. In Figure 4-1(a), a stable stratified swirl flame is shown, which stabilizes in the combustion chamber as expected for normal operation of the combustor. The appearance of this flame is similar to the premixed swirl flames [53] in which the swirling flame stabilizes in the inner shear layer. Figure 4-1(b) shows the flashback stage when the flame enters the mixing tube and stabilizes at an intermediate location, downstream of the swirler vanes. At this stage the flame is noticeably louder to the ear, and the appearance of

the flame is brighter as it sits inside the mixing tube. In this case, the flame stabilizes neither on the fuel ports nor on the swirler vanes. Thus, the stabilization of the flame is akin to a lifted flame, albeit in a swirling environment. We call this mode as intermediate stabilization, since the flame stops at an intermediate location in the mixing tube.

Figure 4-1(c) shows the flame feature which propagates farther upstream and stabilizes on the fuel injection ports. These flames are anchored robustly, and far upstream inside the mixing tube which may be catastrophic to the upstream components of the combustor. We call this mode of flame anchoring as “flameholding”. The appearance of the flame is not as bright since this stage occurs only when the fuel is hydrogen-rich. The lack of CH^* radicals, which emit blue luminescence, can be noted by comparing to the methane-rich case in Figure 4-1(b).

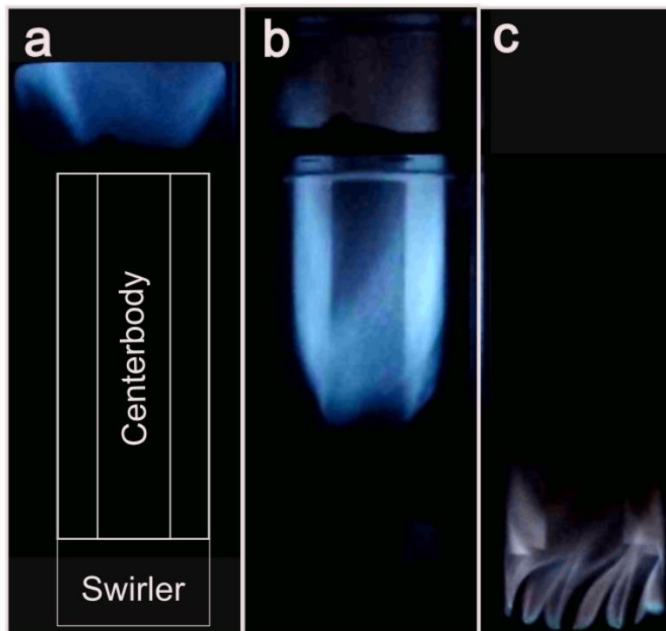


Figure 4-1 Different stages of stratified flames a. Stable in the combustor b. Stabilized in mixing tube after flashback c. Flameholding

4.1.2 Experimental regimes

The stratified flame flashback experiments have been conducted for cases where the mean axial velocity through the mixing tube is in the range 1.1 to 4.5 m/s. Some of the experiments were conducted in a high-pressure facility, in which case the pressure was varied from 1 to 5 atm. The variation in pressure allowed us to vary the Reynolds number from 2×10^3 to 3.3×10^5 , while maintaining similar volumetric flow rates and hence strain rates and residence times. These experiments were conducted primarily to identify the flashback regime which was described in the previous subsection.

Figure 4-2 shows the regime diagram of final stabilization modes after flashback has occurred. The dotted curve in the plot is an approximate separation line between these two flame stabilization modes in the mixing tube. For fuel-air mixtures with >90% hydrogen content (by mol) always propagate all the way to the fuel ports on the swirler vane and the flameholding takes place. At lower Reynolds numbers, the level of enrichment required for a given equivalence ratio is lower. Similar behavior has been reported by researchers at TU Munich, who investigated hydrogen-rich flashback in a different geometrical configuration. [71] In their case, the fuel injection was carried out on the outer wall and the flame stabilized itself on the fuel ports.

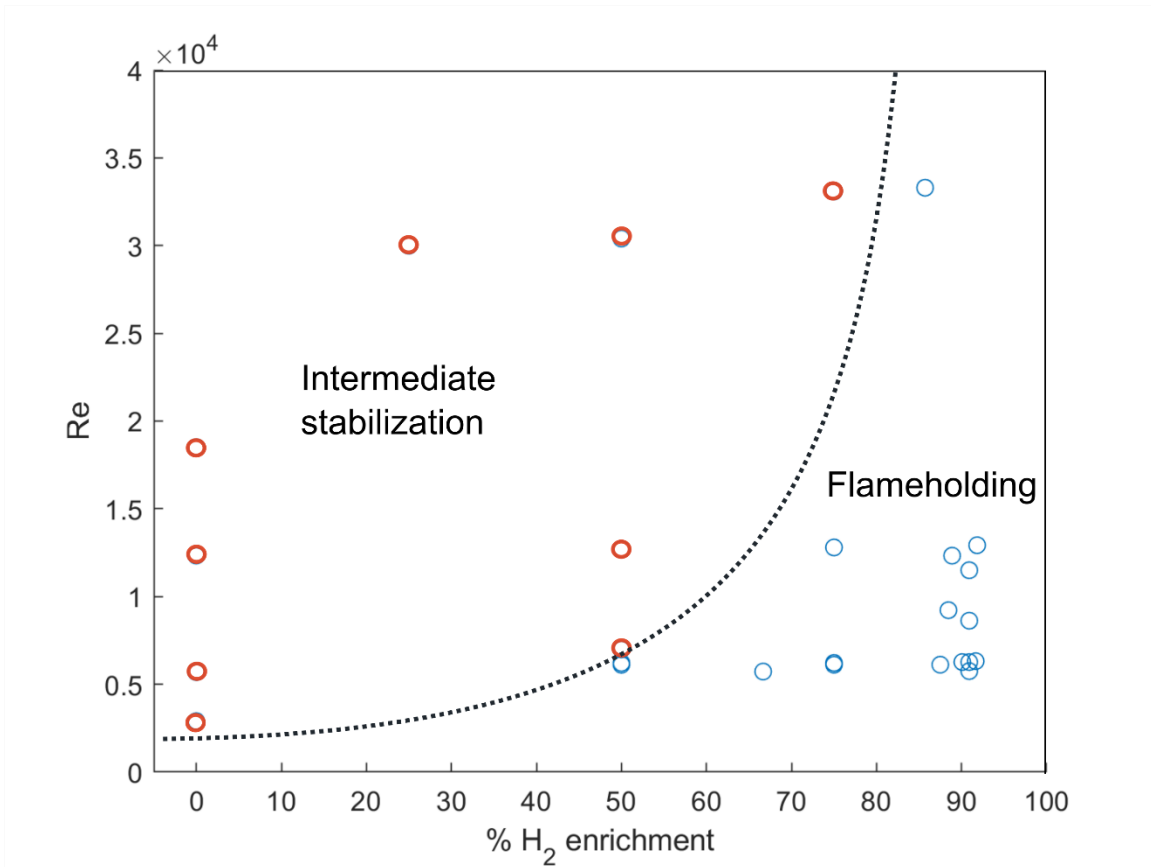


Figure 4-2 Regime diagram marking the mode of upstream propagation. Red circle refers to intermediate stabilization while the blue circle indicates flameholding.

In this study we are focusing on the flame-flow interaction during flashback, rather than characterizing the conditions for which the different stabilization modes occur. Determining the global conditions is no doubt of significance to industrial applications, but is beyond the scope of this study. In this study, we focus on the flame-flow interaction and conduct detailed laser diagnostic experiments for conditions which are comparable to the premixed flashback cases described in the previous chapter.

The next subsection of this chapter is devoted to describing luminosity imaging of flashback in stratified swirl flames. We discuss the global and local behavior of the flame

surface and why it is difficult to reconstruct a three-dimensional picture of the flame tongue, as we could do in fully premixed conditions.

4.1.3 Time-resolved luminosity imaging of the propagating flame

4.1.3.1 Intermediate stabilization

High-speed luminosity imaging of stratified flame flashback shows that flashback is initiated in a way that is very similar to that of the premixed case. The reason for this is that the fuel and air become progressively better mixed as they travel down the mixing tube, until they reach a nearly premixed state at the entrance to the combustor. The typical process for the initiation of flashback is that a large flame tongue swirls around the center-body, sometimes dipping down and then returning, but at some point, it continues to propagate downward along the center-body. However, after this point, the behavior of the flame for fully premixed and stratified cases is very different. For example, for the stratified case, as the flame moves upstream, at some point it reaches relatively unmixed fluid and the flame surface starts to wrinkle as has been shown in previous partially-premixed flame studies [41]. Two instances of the flame tongue swirling around the center-body are shown in Figure 4-3. These luminosity images correspond to methane-air stratified flame flashback at $Re_h = 6600$. In Figure 4-3 (a), the flame tongue is an easily identifiable structure (marked as white dashed line). The flame surface is more wrinkled but the leading edge of the flame tongue can be identified and tracked. After 5 milliseconds, the flame tongue moves to the central section of the view. In premixed cases, the flame tongue retains its topology while moving in space. Furthermore, the line-of-sight integrated luminosity signal at the leading edge shows a step increase across the flame surface, which makes it possible identify the flame tip. This, however, is not the case with the flame tongue in the stratified mixture. The flame surface is more non-uniform in brightness exhibiting very

bright pockets, while the leading edge might be very faint, as is the case shown in Figure 4-3(b). In such a case, not only does the flame tip not retain its shape but it is difficult to identify the flame surface.

This situation leads us to the conclusion that not only is a stratified flame tongue different in its flame-flow interaction physics, but some basic features of the flame topology remain difficult to define. The upstream propagation of the flame stops at an intermediate location in the mixing tube, as can be noticed in Figure 4-3. Although the mean upstream propagation of the flame is arrested, the flame tongue still swirls around the center-body and the global features of the flame brush seem to be moving around the center-body. The flame surface fills the entire width of the mixing tube; however, this situation is not axisymmetric at any instant. The flame tongue still revolves around the center-body, even though its leading edge or the flame tip is not distinct. We did notice a distinct sound emanating from the mixing tube during flashback that may be of interest for future studies.

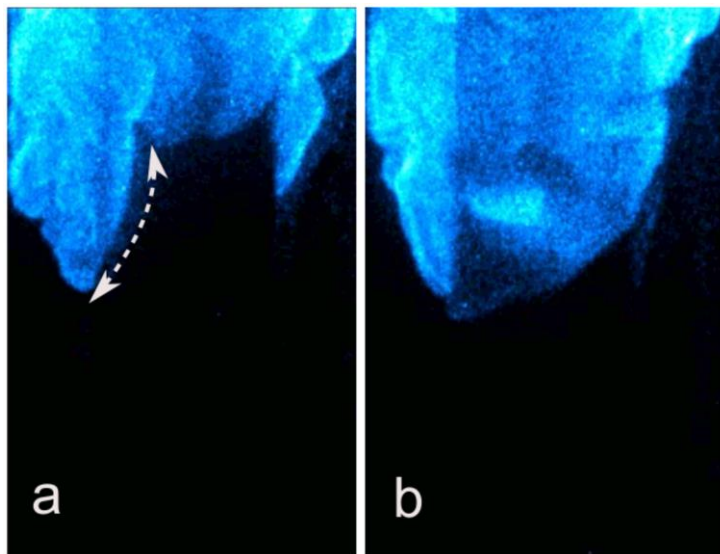


Figure 4-3 Two luminosity images captured 5 ms apart during the stratified flame flashback of methane-air mixture. $Re_h = 6600$.

4.1.3.2 Flameholding

Hydrogen-rich fuel shows a higher propensity for flameholding on the fuel-ports. In the current set up, stratification is achieved by injecting the fuel through ports that are close to the outer wall, as described in section 2.1 of this thesis. Prior to the occurrence of flashback, the swirl flame is stabilized in the inner shear layer of the recirculation zone in the combustor. The upstream propagation of the flame starts like the case of premixed flashback. A large flame tongue propagates down the center-body as it swirls around it in the same direction as the swirl flow. It has been reported that the hydrogen-rich flames have smaller radial spread than the methane-air flames for fully premixed case [47]. This, however, is not the case with stratified flames since the flame brush fills the entire radial extent of the mixing tube. Thus, the flame brush interacts with richer fuel-air pockets in the proximity of the outer wall. The flame propagation along the center-body occurs up to an intermediate location in the mixing tube. So far, the global propagation behavior is similar to that of the intermediate stabilization mode. However, the interaction of the flame brush with the outer-wall fuel-air pockets continues. The flame brush tries to propagate into the flammable mixtures along the outer wall and seems to succeed when the flame encounters streaks of near-stoichiometric fuel-air pockets. Once it reaches the outer wall the flame starts propagating along the outer wall led by acute-tipped bright flame structures.

Figure 4-4 shows a sequence of luminosity images that are captured 5 milliseconds apart. The formation of a flame structure along the outer wall is marked with a yellow ellipse. In Figure 4-4(a), a locally bright flame structure that moves in the approach flow direction (red arrow) spreads out quickly and leaves behind acute flame structures, which anchor themselves in the outer wall boundary layer. These flame structures are pointed in the negative streamwise direction, and are similar to the small scale structures that form in

the trailing side of the flame tongue during premixed flame flashback [76]. It is interesting to notice that these structures do not get convected in the direction of the swirl. Once anchored in the outer wall boundary layer, these structure show resistance to the approach flow. During this phase, the flame structure does not seem to move. At times, these structures are washed away by the approach flow, however once a structure starts propagating upstream and anchors on one of the fuel ports, the flame anchors itself on all the fuel injection ports. This step towards flame anchoring is very fast as compared to any of the previous stages.

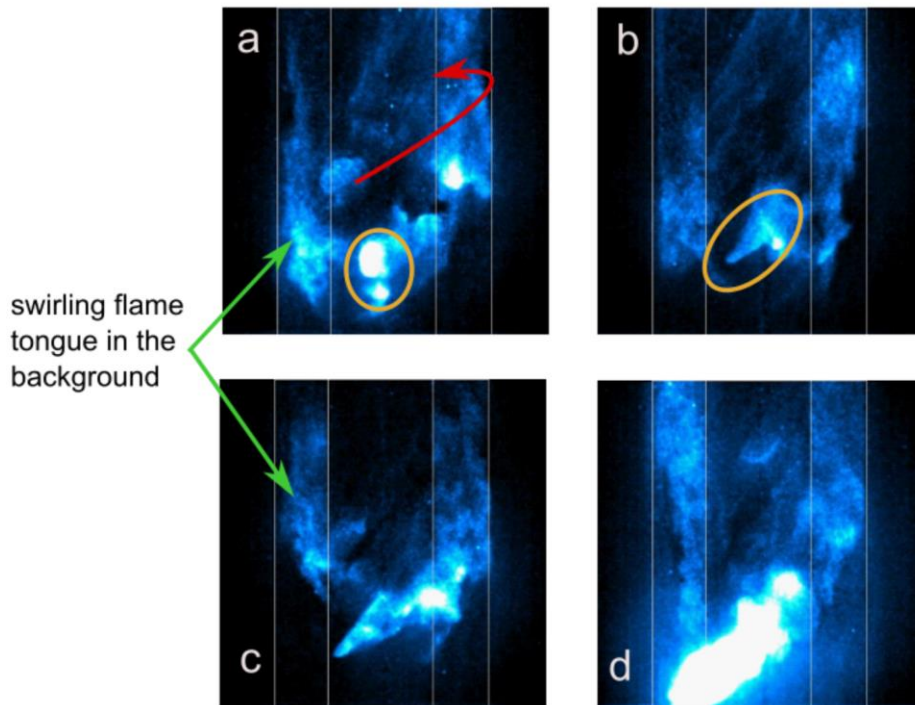


Figure 4-4 Propagation of flame structure on the outer wall a. bright flame structure appearance b. acute flame structure formation c. acute flame anchoring d. upstream propagation towards flameholding. Red arrow shows the direction of the approach flow.

When the flame structure does not form in the central section of the luminosity image (defined in Figure 2.5), it is very difficult to identify the flame structure. Also, the

formation of these acute structures is random. It requires multiple flashback runs until one gets to capture the propagating flame structure in the central section (center-body in the background).

Another interesting feature of stratified propagation is the simultaneous presence of the swirling flame tongue on the center-body. It is usually difficult to decipher because of its lower level of luminescence, but dim flame tongues on the center-body can be noted in Figure 4-4. The flame tongues are circled with an orange ellipse in Figure 4-4. The swirling flame tongue is on the left side of the luminosity images, although it is easier to see in the videos than these still images. It should be noted that the initial formation of the bright flame structure in Figure 4-4(a) occurs on the flame brush of the swirling flame. In other words, the intermediate-stabilized swirling flame in the mixing tube acts as the initiator of the propagation along the outer boundary wall.

4.2 LASER DIAGNOSTIC EVALUATION OF STRATIFIED FLAME FLASHBACK

Based on our observations from luminosity images, we already know that the fuel-air distribution in the approach flow affects the characteristics of the flame surface. Hence, in this work, we first assess the fuel-air mixing in the mixing tube and then report time-resolved PIV data.

We employ planar laser-induced fluorescence imaging (PLIF) with acetone as the fuel tracer. For methane-air mixing, we inject acetone-seeded air with the same flow rate as that of methane during flashback. The mixing characteristics of the methane are assumed to be similar to that of acetone-air due to their comparable density and diffusivity characteristics. The PLIF images are captured at 10 Hz, and thus insights provided by these images are not time-resolved in nature. However, these images can provide important statistics for methane-air mixing in the annular swirling flow. The distribution of

equivalence ratio in the mixing tube was determined by first calibrating the signal at the exit of the mixing tubes as representing the “pure” fuel state (note that it is actually composed of a mixture of acetone and air). This signal was then used to normalize the PLIF signal at all imaging locations, and from this normalized signal the equivalence ratio could be computed.

4.2.1 Stratified Methane-air swirl flame flashback

4.2.1.1 Fuel-air mixing

In this subsection, we report the fuel-air mixing characteristics as assessed using acetone PLIF images. The hydraulic-diameter Reynolds number (calculated using streamwise velocity) is kept at 6600, while the global equivalence ratio is kept at 0.63. The field of visualization extends from $z = -50$ mm to $z = -80$ mm (negative signifies the upstream location). At these flow conditions, during the reacting-flow experiments, the flame propagates into the mixing tube and attains intermediate stabilization within the field of view. We assume that the flame’s presence in the mixing tube does not affect the fuel-air mixing upstream of the flame. This is reasonable since the intermediate stabilization occurs at about 60 to 65 mm upstream of the mixing tube, whereas the fuel is injected about 120 mm upstream of the fuel injection ports. The distance between the fuel ports and the flame brush is thus about 70 nozzle diameters downstream as measured from the fuel-injection ports. It should be noted that fuel-air mixing is affected by multiple other factors such as jet-jet interactions, jet-wall interactions, jet-vane interaction and the swirling action of the swirler. In such a case, it is not feasible to compare the mixing with any canonical studies. Phenomenologically, one can say that as the fuel-air pockets move along the flow, they mix primarily due to molecular and turbulent diffusion. Schmidt number, the ratio of kinematic viscosity and the molecular diffusivity for methane-air and acetone-air is 0.99

and 1.5, respectively. Thus, by keeping the same Re and similar Schmidt numbers, one can argue that the mixing characteristics can be assessed reliably.

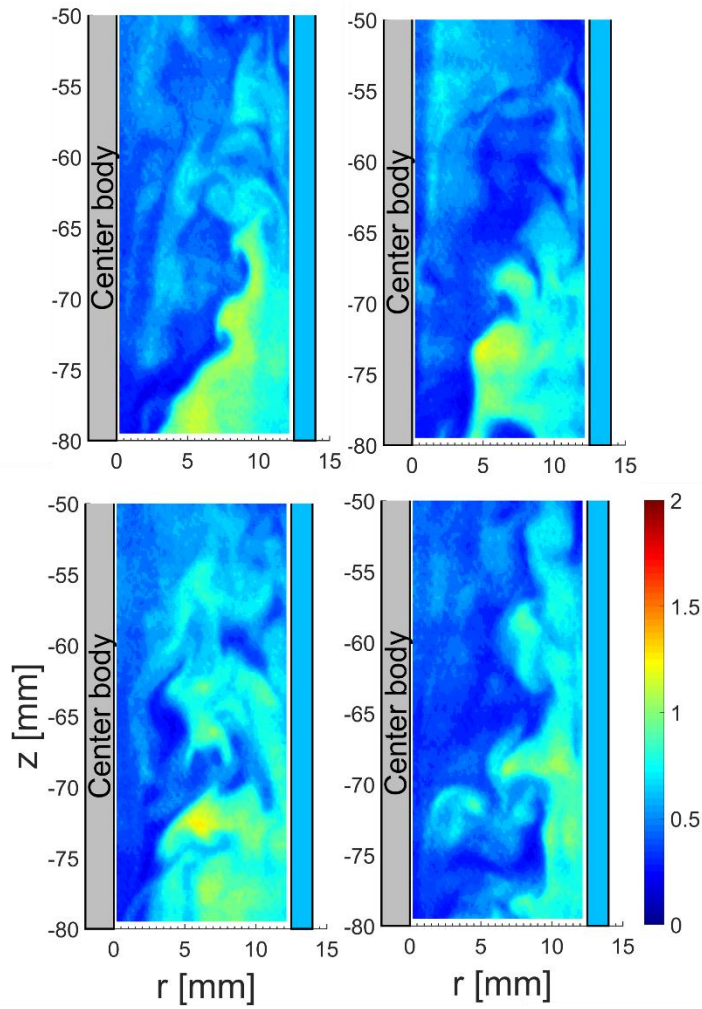


Figure 4-5 Instantaneous PLIF snapshots showing the distribution of equivalence ratio at flashback-equivalent conditions. $Re_h = 6600$

Figure 4-5 shows instantaneous statistically-uncorrelated PLIF images of fuel-air mixing. The flow close to the center-body is predominantly fuel-lean. Stoichiometric and fuel-rich pockets can be noticed in the flow close to the outer wall. This confirms that the

fuel-injection strategy of positioning the fuel-injection ports away from the center-body leads to an inhomogeneous equivalence ratio distribution. The intermittent presence of fuel-air pockets close to the center-body can be attributed to the swirl and turbulence in the mixing tube flow.

Figure 4-6 shows the mean distribution of the equivalence ratio in the mixing tube. At $z = -80$ mm, the equivalence ratio at the center-body is very lean ($\phi \sim 0.3$) while the flow at the outer wall is richer ($\phi \sim 0.9$). The lean and rich flammability limits for methane-air mixtures are 0.5 and 1.7 respectively, and near these limits the flame speed becomes small. Thus, in a mean equivalence ratio field, the propagating flame would not be able to reach $z = -80$ mm. At $z = -68$ mm there is a sudden change in the mean fuel-richness of the flow, which can also be noted in the instantaneous PLIF images in Figure 4-5. The reason behind it may be the orientation of the streamlines, which move out of the plane of the laser sheet; thus, any fuel-rich pocket would move out of the measurement plane. The three-dimensionality of the flow also makes it difficult to comment on the length-scales of the fuel-air pockets.

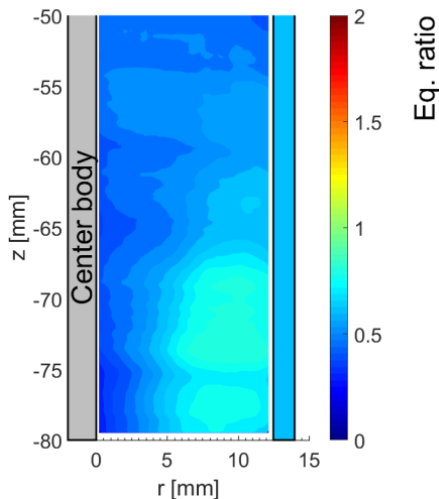


Figure 4-6: Mean distribution of equivalence ratio during methane-air mixing at $Re_h = 6600$, Global equivalence ratio = 0.63.

4.2.1.2 Flame-flow interaction during the methane-air flashback

As discussed in the previous subsection, as the flame propagates upstream along the center-body it encounters a lean premixture embedded with intermittent fuel-rich pockets. Near the lean flammability limit, the flame luminosity becomes very low, which makes the identification of the flame surface challenging. In left and right sections of the field of view, the line-of-sight integrated signal is affected by the flame curvature. To explain this issue, we show two luminosity images captured during stratified flame flashback in Figure 4-7. The images Figure 4-7(a) and (b) show the same luminosity image, except a gamma correction has been applied to Figure 4-7(b).

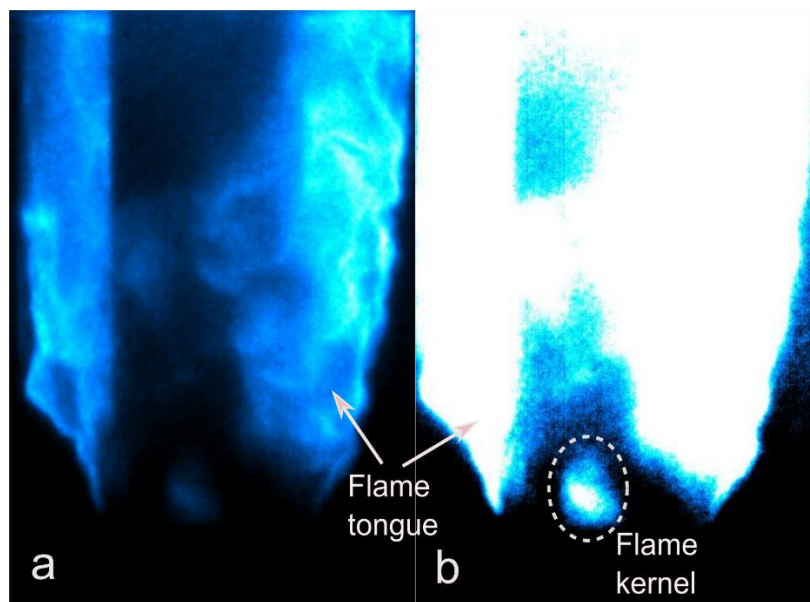


Figure 4-7 Luminosity image captured during methane-air stratified flame flashback a. Gamma = 1 b. Gamma = 0.3

In Figure 4-7(a) the luminosity from the flame surface is captured while the region close to the leading edge of the flame tongue is not visible. The brightness on the flame brush is due to the fuel-rich pockets burning at regions away from the center-body. In such a case, any interesting feature at the leading edge is easy to miss. On the other hand, once

gamma is corrected to observe the leading line of the flame surface, we notice a flame kernel near the flame front. It appears to be disconnected from the flame surface, but it cannot be so, since the ignition of this kernel, which is at room temperature before burning, is not possible without an ignition source. Any possibility of auto-ignition does not exist since the fuel-air premixture is not preheated. This argument suggests that even though there is nearly zero luminosity around the flame kernel, there should be a flame surface in its vicinity that ignites it, as it moves downstream in the mixing tube. This raises the question whether we can detect an ultra-lean flame that lies close to the center-body.

In this subsection, our discussion focuses on how the apparent flame kernels affect the flame surface and the flow upstream of it. The leading regions of the flame surface – in the absence of the fuel-rich pockets -- should play little role in blocking the approach flow since the flame resides in barely-flammable lean regions. Hence, in the subsequent paragraph, we discuss the interaction of the bright flame structures and approach flow.

Figure 4-8 shows the simultaneous luminosity and velocity fields upstream of the flame surface. Figure 4-8(a) and Figure 4-8(b) are spaced by 3 ms while rest of the images are captured 1 ms apart. Figure 4-8(b) – (d) tracks a bright flame structure, circled in yellow, which crosses the laser sheet. The white region in the velocity contour plot indicates the presence of flame products that vaporize the PIV seed particles. The effect of the bright flame structure on the velocity field is evident as it crosses the laser sheet. Regions of negative axial velocity are found upstream of the flame front during the time that the structure crosses the laser sheet. Out-of-plane velocity (measured simultaneously but not shown) is positive, which shows that these flame structures deflect the incoming flow rather than causing flow reversal.

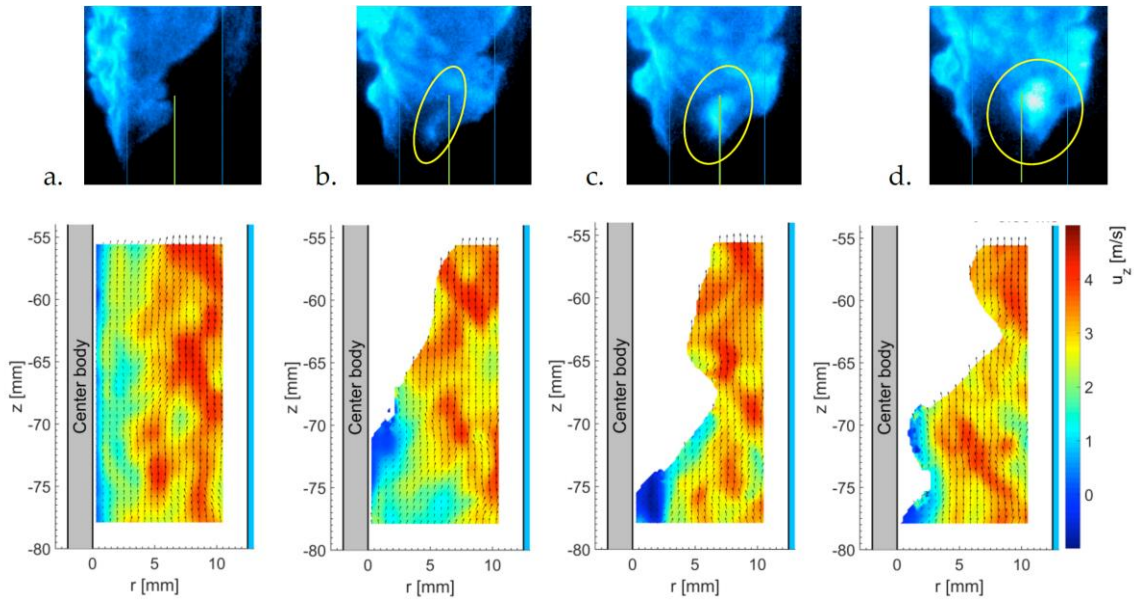


Figure 4-8 Chemiluminescence and the axial velocity fields at time instants: a. t_0 , b. $t_0 + 3$, c. $t_0 + 4$ and d. $t_0 + 5$ ms. Green line in the chemiluminescence images shows the position of laser sheet. Evolution of a flame structure is marked by yellow circle.

Prior to the flame structure crossing the laser sheet, the planar profile of the flame was not wrinkled. However, as noted in Figure 4-8(c) and (d), the flame kernel wrinkles the flame surface and at the same time applies a strong blockage effect on the approach flow. This structure imposes negative axial velocity on the approach flow. A similar mechanism was found to assist the upstream propagation of the flame tongue in premixed flame flashback [74],[57] However, for the case of stratified flame flashback, there is little effect on the approach flow by the flame surface a bright flame structure appears. It should also be noted that despite imposing very strong blockage effect on the approach flow, the bright flame structure does not change its motion. Instead it keeps moving along its spiral path towards the mixing tube exit. The apparent lack of deflection of the bright flame structures' path tells us that in global upstream motion of the flame brush during flashback, a single flame kernel does not contribute to the propagation dynamically. Instead, it moves

along the spiral path around the center-body. Along its way out, the flame structure burns out depending on its length scale. The burning out of this flame structure is identified by the decrease in luminosity of the flame structure.

The chemiluminescence signal captured in these images are line-of-sight integrated and have a strong dependence on local ϕ . A local variation in ϕ imposes variation in local flame speed, stretches the flame surface and increases the flame curvature. The presence of bright flame structures seems to result from the presence of locally fuel-rich pockets in the flow, which is consistent with the non-reacting PLIF measurements. To confirm this hypothesis, acetone PLIF measurements were taken for reacting flows as well. However, seeding of fuel flow with acetone affected the flashback limits for a given bulk velocity and required smaller fuel flow rates to trigger the flashback.

Figure 4-9 shows two normalized PLIF snapshots capturing the flame brush during a stratified-flame flashback event. The flame front can be identified as the region of sharp decrease in PLIF signal, which occurs owing to the pyrolysis of acetone in the preheat zone of the flame. The regions of large curvature, such as the cusps (in red ellipse, Figure 4-9(a)), are associated with a sharp change in the spatial distribution of ϕ . This observation confirms the role of mixture variation in wrinkling of the flame brush of the flashing back stratified flame; however, we are not able to map the PLIF signal to equivalence ratio owing to pyrolysis and temperature variations that affect the acetone PLIF signal. Instead, the pixel intensity was normalized with the maximum pixel value in the visualized region. After normalization, the region with maximum PLIF signal should correspond to fuel-rich regions. If we correspond these fuel-rich regions with those in the non-reacting flow, the local equivalence ratio in these pockets should correspond to $\phi \sim 1.1-1.6$ for the methane-air mixture. As we discussed in the literature review, this range of equivalence ratio corresponds to the unstretched laminar flame speed of 0.2 to 0.3 m/s. Thus the flame

wrinkling will occur depending on the local equivalence ratio gradient. If the pocket is near-stoichiometric, it would induce positive curvature on the flame surface. On the other hand, if the fuel-air pocket is near the flammability limits then the flame surface would have little propagation in those regions. The resulting variation in local flame speed thus modulates the flame surface. There should also be additional effects that come into play, such as in a back-supported or front-supported flame environment, but these details are difficult to comment upon.

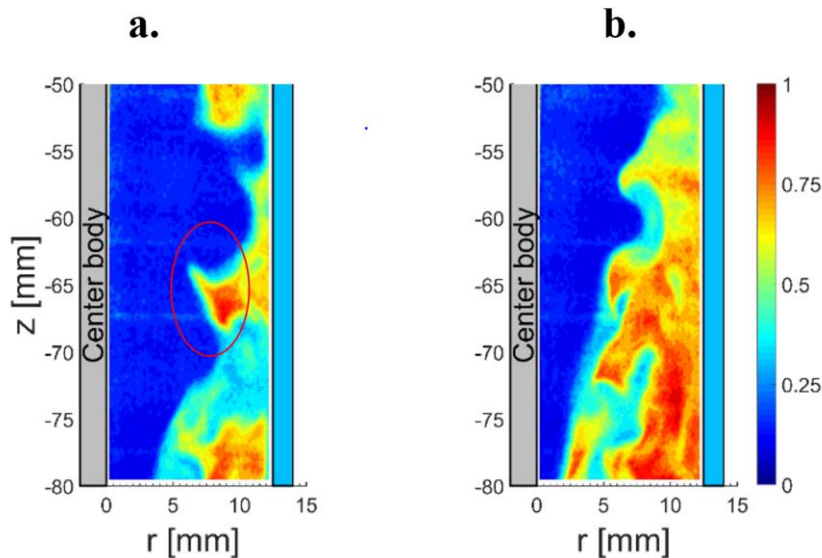


Figure 4-9 Normalized acetone PLIF signal captured during the flashback

4.2.2 Stratified hydrogen-rich swirl flame flashback

Hydrogen-enrichment of fuel leads to new pathways for flames to propagate, as we have discussed in section 4.1.3.2. In this section, we analyze hydrogen flashback behavior for the case with the same mean axial velocity of 2.5 m/s and with hydrogen enrichment of 87% by mole. The global equivalence ratio is maintained at 0.4. First, we assess the mixing behavior of the fuel and air.

4.2.2.1 Mixing behavior

Acetone PLIF was also used to investigate the mixing characteristics for the case of stratified flashback with enriched-hydrogen fuel. However, in contrast to the work above, the acetone was seeded into helium to create a non-reacting surrogate that had a density that is closer to that of the enriched hydrogen fuel. Helium is seeded with acetone by passing through the acetone bubbler. Instantaneous PLIF images for these runs is shown in Figure 4-10.

A comparison of Figs. 4-5 and 4-10 indicates that the mixing behavior is qualitatively similar to that of the methane-fuel case. There are fuel-lean yet locally-richer fuel-air pockets spread across the mixing tube. The concentration and relative size of these pockets are large close to the outer wall; however, there is an intermittent presence of fuel-air pockets close to the center-body boundary layer.

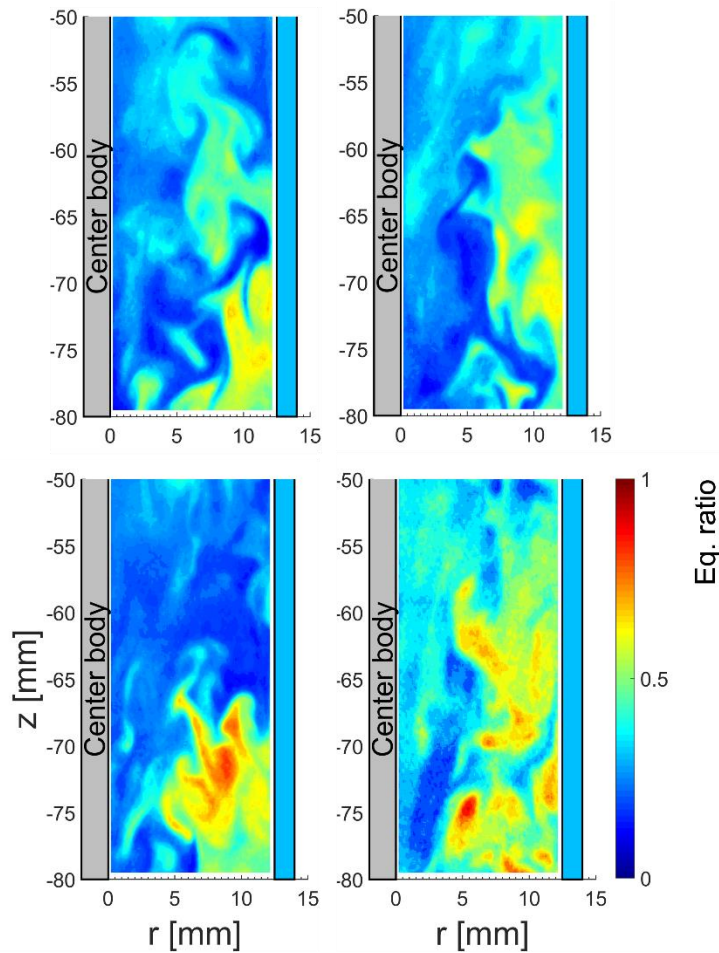


Figure 4-10 Instantaneous equivalence ratio distribution during helium-air mixing $Re_h = 6300$

The mean of 900 instantaneous images is shown in Figure 4-11. The mixing behavior of the mean is also similar to that of methane-air mixing, except that the equivalence ratio values are different. For the case of hydrogen-rich fuel, the equivalence ratio does not reach stoichiometric in the mean, which simply reflects the lower global equivalence ratio used. Also, instantaneously, there are pockets of near-stoichiometric mixtures in the flow.

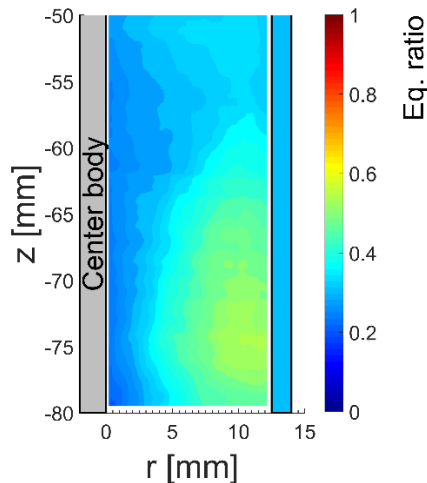


Figure 4-11 Mean equivalence ratio distribution in the mixing tube. $Re_h = 6300$

The hydrogen-air mixture, even though fuel-lean in terms of equivalence ratio, is still very reactive as compared to stoichiometric methane-air mixtures. The lean flammability limit equivalence ratio for 87% hydrogen-methane mixture has a lower flammability limit of 0.11. These limits encompass almost the entire visualized region in the mixing tube. In flammable regions, the unstretched laminar flame speed of hydrogen-air is as high as 3 m/s for near-stoichiometric fuel-air pockets. These fuel-air pockets occur frequently in the regions close to the outer wall as shown in Figure 4-10, thereby increasing the likelihood of flame propagation along the outer wall.

4.2.2.2 *Time-resolved luminosity images and simultaneous PIV*

We observe that hydrogen-rich flashback occurs in two steps. The first step is the propagation along the center-body boundary layer in a way similar to that of the fully premixed flame. The flame starts from a stable condition where it is anchored in the inner shear layer of the combustor. Upon triggering the flashback, it propagates upstream through the boundary layer of the center body. In a manner similar to the intermediate stabilization, the flame tongue rotates around the center-body. The flame brush is broad

enough to maintain interaction with the outer wall. During this interaction, the flame surface propagates to the outer wall and begins to propagate down it. It should be noted that the flame's existence along the outer wall is not favored by the swirling action since it leads to the low-density fluid along the outer wall. The centrifugal force acts radially outward and so the low-density gases on the outer wall is inherently unstable. Still, the propagation of the flame surface along the outer wall occurs, primarily due to the fast chemistry associated with the richer mixtures at the outer wall. In Figure 4-12 we show the first definitive evidence of flame propagation along the outer wall using simultaneous time-resolved PIV and luminosity. The framing rate for these measurements is 4 kHz.

Figure 4-12(a) shows an instant when the flame along the center-body and the outer wall are on the either side of laser sheet (green). In 4.25 ms the flame on the center-body revolves around the center-body and crosses the laser sheet. At the same time, the flame structure on the outer wall also crosses the laser sheet in the opposite direction. At this instant, the outer wall and the center-body flame structures share the same azimuthal location. The propagation of the outer wall structure occurs as an acute flame tip shedding the burnt gases as bright flame structures. The burnt gases, which are low in density, cannot sustain themselves in the vicinity of the outer wall. Thus, immediately after getting burnt, these gases form a puffy tail-like structure in the wake of the leading point of the propagating flame surface. In Figure 4-12(c), the flame on the center-body has crossed the laser sheet and is on the other side of the annulus. At this stage, the acute flame tip which is anchored in the outer wall boundary layer, starts propagating upstream. During this process, the single flame structure bifurcates into 2-3 flame structures approaching the fuel-injection ports.

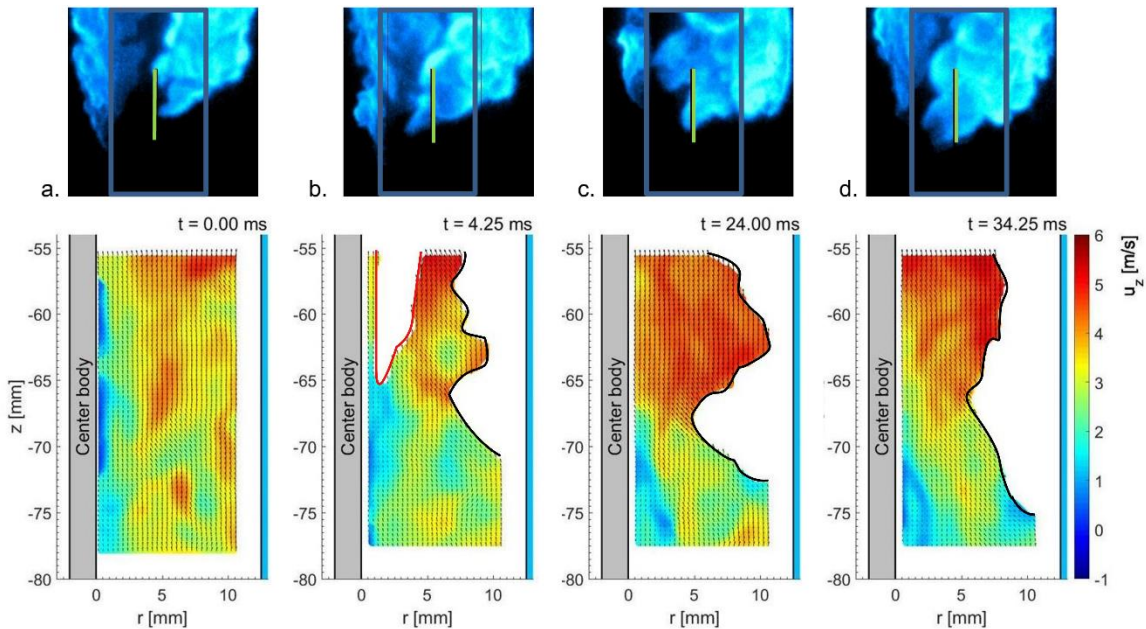


Figure 4-12 Chemiluminescence images and simultaneous axial velocity fields at different time instances during flame propagation along the outer wall boundary layer. White region in the velocity shows the burnt gas region.

While propagating, we expect the outer flame structure to apply blockage to the approach flow. These flame structures, which push the approach flow in the negative streamwise direction, can apply blockage to reverse the flow at the flame tip. To capture this effect, the laser sheet needs to be imaged very close to the outer wall of the mixing tube. The curvature of the mixing tube makes it difficult to capture this detail. In the results reported here, we could get PIV data up to 2 mm away from the outer wall. Thus, any portion of the flame and the flow within 2 mm of the wall could not be captured. However, the blockage from the flame structure is apparent in Figure 4-12(d). Just upstream of the flame tongue ($z = -77$ mm, $r = 10.5$ mm), the blockage effect from the flame reduces the axial velocity to ~ 1 m/s, as marked by local light blue background.

Another interesting aspect of this propagation is the flame-flow interaction. The flame structure on the center-body keeps swirling while anchored at an intermediate location. This swirling flame can cause a sweeping effect in the azimuthal direction, similar

to the one discussed in previous chapter. On the other hand, the outer flame structure, which is primarily controlled by the equivalence ratio distribution upstream of it, also interacts with the flow by pushing in the opposite direction. Now, inside the mixing tube, these two flames move in opposite swirling directions. The flow that is affected by the flame on the center-body can also interact with the flame on the outer wall, which can cause a three-way interaction. To ascertain this would require simultaneous multi-plane measurements which was not possible with our current experimental setup.

To further understand the propagation along the outer wall, we describe the flame propagation in two stages: (1) flame anchoring on the wall, and (2) flame advancement along the wall. Flame anchoring on the wall can be defined by attachment of acute flame tips on the outer wall. In this process, the flame does not move but resists getting convected with the approach flow. At times, acute flame structures anchor themselves and thus resist being convected by the upstream flow. The flame advancement stage starts when the flame structure starts propagating upstream. In this phase, either the flame structure bifurcates into two similar structures or it remains on the streaks of stoichiometric mixture (most reactive mass fraction) and advances till the flameholding occurs.

PIV runs were conducted in an atmospheric-pressure burner with alumina seeding particles. Alumina particles do not get consumed in the flame and so it is possible to obtain velocity measurements in the burnt gas regions. In previous work, the 2D dilatation has been found to agree well with the flame surface. [76],[78]. Theoretically, the three-dimensional divergence value should be zero everywhere except for the flame surface. Also, the larger the volume generation per unit volume, the larger would be the divergence. Thus, it is also an indirect indicator of heat release, assuming that the entire heat release acts to generate volume. With this idea, we use the 2D divergence value as the marker of

heat release. Another marker of heat release in stratified flows is luminosity, however deriving any quantitative measurement is beyond the scope of current work.

Figure 4-13 shows two instants during the flame anchoring phase. At first there is no acute structure on the wall, however a bright flame structure crosses the laser sheet (shown with light green). In Figure 4-13(a), in the velocity field, the flame surface is marked with a white line. Determination of the flame surface was accomplished by looking for large changes in the local particle density [76],[79]. It can be noted that the flame surface agrees well with the 2D dilatation, but only in the upstream portions of the flame surface.

Previously reported work on fully premixed flame found these peaks of large 2D dilatation all along the flame surface [53]. In Figure 4-13(b), even though the flame surface exists in the laser sheet plane, there were no distinguishable peaks in the 2D dilatation map. One can correlate the absence of bright flame structure in the laser sheet plane with the absence of peaks in the 2D dilatation map. This observation agrees well with the idea that the bright flame structures are associated with large heat release – and hence with large three-dimensional dilatation which reflects in the 2D dilatation maps. With this argument, the large 2D dilatation values at the upstream locations of the flame structure indicates that the heat release on the flame structure is not the same all along the surface. The axially-upstream side of the flame structures have larger dilatation than the axially-downstream side of the flame tongue. This observation may be an outcome of the environment around the propagating flame structure. These acute flame structures move through the stratified fuel-air mixture, propagating along the regions of the most reacting mixture fraction. This structure should have a relatively richer and a relatively leaner fuel air mixture on either side of it. Hence, the sides of these structures – visualized as the axially upstream and downstream side in Figure 4-13 should have different levels of dilatation. This should also

be reflected in the luminosity imaging; rich and lean sides of the flame structures should have different levels of luminosity. However, no such evidence was found in the luminosity images. Since, there is another dim flame structure in the background (revolving around the center-body), any comment on the variation of luminosity across a flame structure is difficult to make.

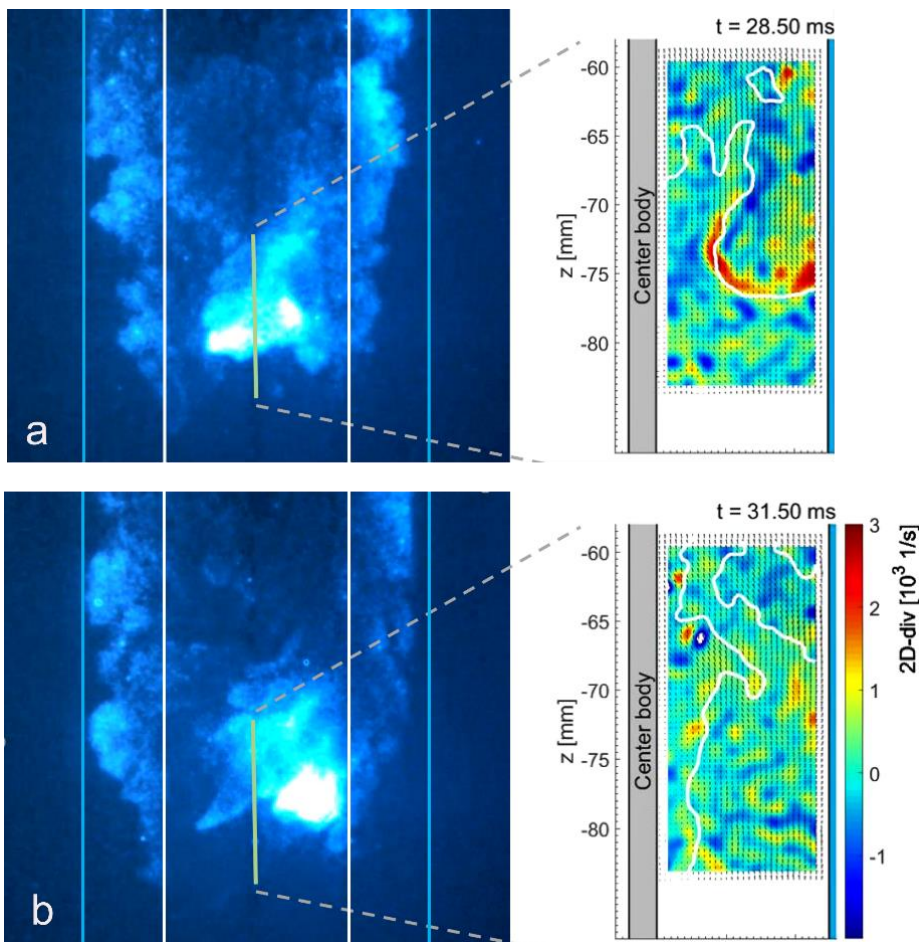


Figure 4-13 (a) Bright flame feature crossing the laser sheet and simultaneous 2D divergence field, (b) Formation of acute tipped flame structure on the outer wall

In Figure 4-13(a), the bright flame structure in the luminosity image corresponds to the region of high 2D dilatation in the PIV data. In Figure 4-13(b), the bright structure

moves downstream, while the acute-tipped flame structures stay as it is. In the PIV image there is no sign of large dilatation in the vicinity of the flame surface.

For the flame advancement stage, we show three instantaneous PIV images along with the luminosity (Figure 4-14). In these images, the flame surface exists along the center-body boundary layer as well as along the outer wall. In Figure 4-14, the regions of large divergence are associated with the flame on the center-body and not on the outer wall. However, at subsequent times, this large divergence shifts toward the outer wall. Simultaneously, the bright flame structure now interacts with the outer wall and assists in making progress in the upstream direction.

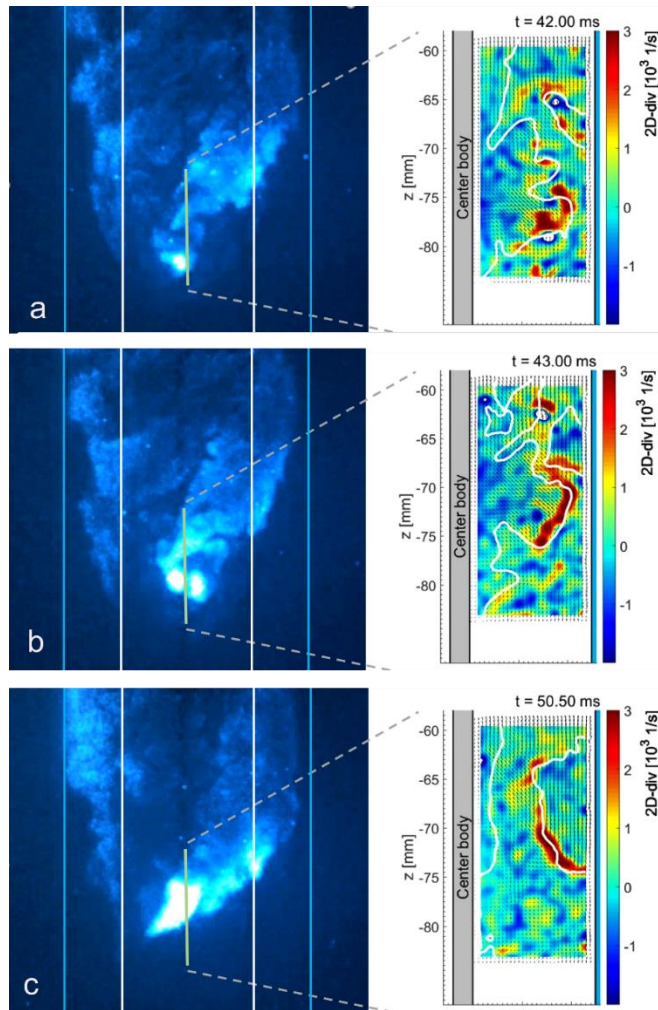


Figure 4-14 Simultaneous luminosity images and 2D divergence maps. Regions of large divergence correspond to the bright flame structures crossing the laser sheet.

If we associate the luminosity and the dilatation value with the heat release, these bright flame structures are essentially sources of large heat release. Thus, when these structures interact with the boundary layer, they allow the flame to anchor on the outer wall. If they occur in tandem, or in the vicinity of the stoichiometric mixtures, they can assist in upstream propagation of the flame.

4.2.3 Effect of elevated pressure

In the current study, elevated pressure flashback runs were conducted at the same mean axial velocity as that of the atmospheric pressure runs. Thus, an increase in pressure results in a proportional increase in the Reynolds number. In this work, we report flashback behavior for methane-air stratified flames at 3 atm and $Re_h = 18,400$. As in the atmospheric-pressure cases, acetone PLIF was used to assess the fuel-air mixing behavior in the mixing tube under non-reacting conditions. For example, Figure 4-15 shows instantaneous images of equivalence ratio that were derived from the acetone PLIF data.

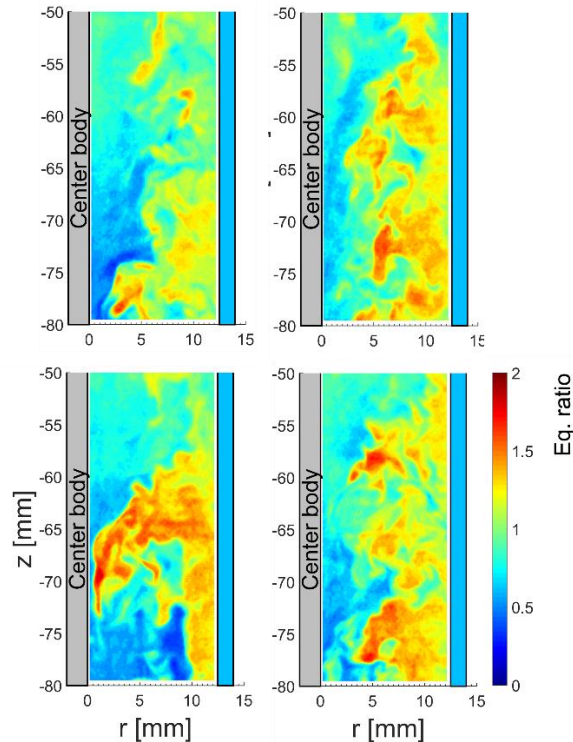


Figure 4-15. Instantaneous PLIF images showing the small-scale fuel-rich structures in the flow. These images correspond to methane-air flashback at 3 atm. $Re_h = 18600$ $\phi_g = 0.85$

Pressure can affect flame propagation characteristics by affecting the reaction chemistry and by increasing the turbulence through the higher Reynolds number. In our discussion on stratified flame-flow interaction, pressure is likely to be important owing to

both effects. The effect of turbulence in the flow is apparent in the instantaneous PLIF images as captured at 3 atm. There are multiple small-scale (sub-millimeter) structures that were not present in atmospheric pressure runs. For methane-air mixtures, the laminar flame speed decreases with an increase in the pressure [7]. This reduction in the flame speed is consistent with our observation that the flashback limit increased at elevated pressure. At 3 atm, flashback was triggered at $\phi_g = 0.85$, as compared to 0.63 at 1 atm. At 3 atm, once flashback occurred, the flame would always stabilize on the swirl vanes. Furthermore, the flame brush was wrinkled, bright and filled the mixing tube. The flame front was found to be marked by small-scale flame structures.

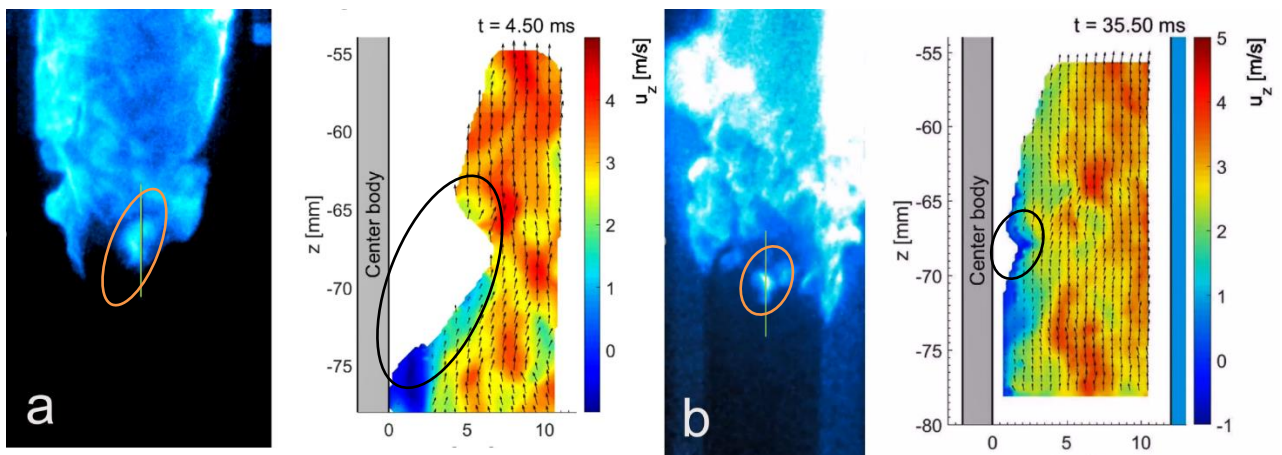


Figure 4-16 Interaction of the flame surface and fuel-rich pockets in the approach flow. (a) 1 atm, and (b) 3 atm. The orange ellipse mark the luminosity signal from bright flame structures. The black ellipse shows corresponding effect on the flame surface

Figure 4-16 shows two instants from methane-air flashback events at 1 atm and 3 atm. Luminosity is shown on the left and PIV on the right. These two instances are comparable since in both the cases the fuel-air pocket interacts with the flame surface. At atmospheric pressure, the fuel-air mixtures are usually not fine-scale, thus the interaction between the flame tongue and the fuel-air pockets alters the topology of the flame surface

significantly. It can be seen that these pockets can have a strong effect on the approach flow as well. On the contrary, at 3 atm, the fuel-air pockets are smaller scale (red ellipse in Figure 4-16(b)) and seem to have lower impact on the approach flow. Figure 4-16(b) shows an instant at 3 atm when the rich fuel-air interacts with the flame surface. It is noted that there was very little change to the flame surface (marked with black ellipse).

Elevated-pressure hydrogen rich flashback still follows the flashback behavior as described for the atmospheric pressure case. Flashback experiments were conducted at 3 atm, with global equivalence ratio of 0.3. Hydrogen enrichment was kept at 86%. Similar to the 1 atm case, the flame propagated along the center-body and then the flame switched to the outer wall.

The propagation along the outer wall occurred in a similar way as that of at atmospheric pressure; however, the flame along the outer wall was characterized as a wider flame tongue, which is similar to observations of channel-flow flashback.

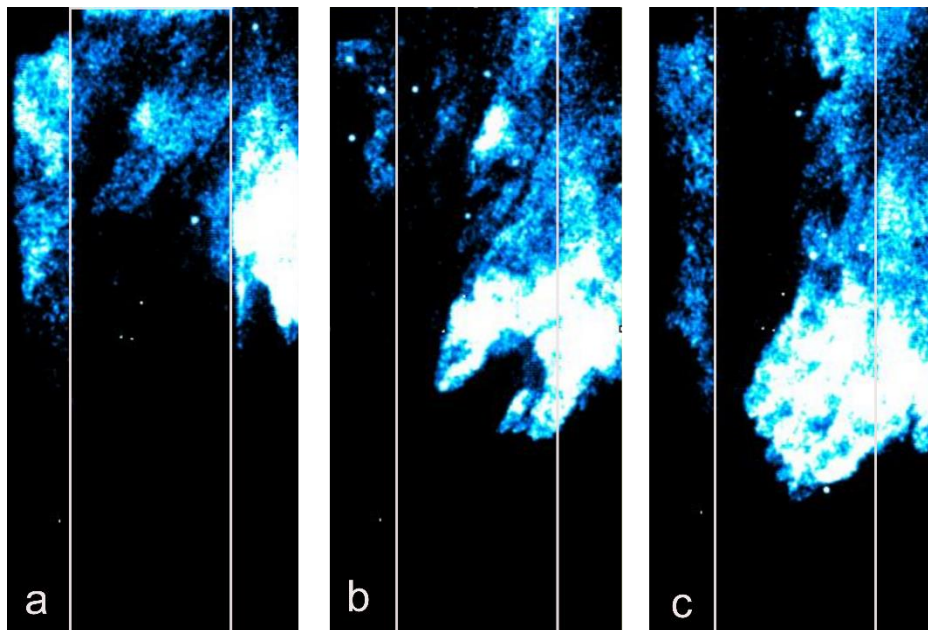


Figure 4-17 Luminosity images captured during hydrogen-rich flashback at 3 atm a. t_0 b. $t_0 + 12$ ms c. $t_0 + 14$ ms; $Re_h = 18600$ $\phi_g = 0.3$

Figure 4-17 shows three instants during a hydrogen-rich flashback event. In Figure 4-17(a) the flame brush clings to the outer wall of the mixing tube. Flame anchoring occurs in a similar way as that of the 1 atm case. Two acute flame tips were found to propagate along the outer wall in Figure 4-17(b). These acute tips are also a bit wider (by a few millimeters). Interestingly the advancement towards the fuel injection ports occurs as a wide band ($\approx 10\text{mm}$) instead of the acute-tipped flame feature. This suggests that the acute-tip structures primarily anchor the flame in the outer wall boundary layer and act to spread the flame in the approach flow such that a wide flame tongue could be formed. Simultaneous PIV measurements could not be taken for elevated pressure measurements due to limited number of experiments which could not capture the flame tongue propagation within the field of visualization.

4.4 CONCLUSIONS

In this chapter, we analyzed the flame propagation behavior during stratified flame flashback. The mean sense of stratification was kept in radial direction such that the regions close to the center-body were fuel-lean, while the flow on the outer wall was fuel-rich. The global equivalence ratio was kept at 0.63 and 0.85 for atmospheric and 3 atm methane-air experiments respectively. For hydrogen-rich mixtures, the hydrogen-enrichment level was kept at approximately 87% for atmospheric and elevated pressure experiments.

Multiple flashback runs were carried out to identify the flashback regime diagram distinguishing the two modes of flame stabilization in the mixing tube, namely intermediate stabilization and flame-holding. During intermediate stabilization of the flame, the upstream propagating flame stops at an intermediate location in the mixing tube and keeps swirling around the center body as a flame tongue with relatively-dim leading edge and bright flame brush. It was noted that intermittently bright flame structures would appear at

the upstream edge of the flame and these structures would impose strong blockage on the approach flow. However, these bright flame structure, which are rich fuel-air pockets in the swirling, would merge with the flame brush without assisting towards the sustained upstream movement of the flame along the center-body boundary layer. The flame leading edge was dim in luminosity and did not seem to affect the upstream flow as strongly as a fully premixed surface. The flame brush almost entirely filled the mixing tube during intermediate stabilization of the flame.

The other mode of flame propagation, flameholding occurs when the flame propagates along the outer wall boundary layer and anchors itself on the fuel ports. This behavior was found prevalent in hydrogen-rich fuel. It was noted that the upstream propagation of the flame initiates along the boundary layer of the center-body. As the flame propagates upstream, it attains intermediate stabilization. Meanwhile, the flame brush interacts with the fuel-rich pockets along the outer wall boundary layer. The bright flame structures appear in the mixing tube, which upon interaction with the outer wall, anchor as acute flame structures. These structures resist the approach flow and move slowly as seen in lab-frame. However, these flame tip structures upon interacting with rich fuel-air pockets start propagating along the outer wall and keep progressing until the flame-holding happens. The bright flame structures which assist in upstream propagation are found to concur with strong 2D dilatation in the velocity field. This suggests that these flame structure impose strong blockage on the approach flow, thereby assisting in the acute-tip flame anchoring.

These two modes of flame propagation were found to occur at elevated pressures as well. Although flashback experiments were conducted up to 5 atm ($Re_h \sim 33000$) for flashback regime determination, elevated pressure high-speed laser diagnostic was carried out only up to 3 atm ($Re_h \sim 18300$). It was noted that the nature of flame-flow interaction

for methane-air flames stayed the same. The flame surface stabilized itself at an intermediate location in the mixing tube. The finer scale fuel-air pockets were found to appear at the region immediately upstream of the flame tongue. These fuel-air pockets did not affect the flow field at elevated pressure as strongly as during the atmospheric pressure flashback experiments.

For hydrogen-rich fuel at elevated pressure, the flame-holding started with interaction of bright flame structures with the outer wall. Acute flame structures were found to anchor in the turbulent boundary layer on the outer wall. After flame anchoring, a wide flame tongue was found to form during the flame advancement stage. The appearance and propagation behavior of the flashback was similar to that of channel flashback.

CHAPTER 5 : SUMMARY AND FUTURE WORK

The research work in this thesis is aimed towards improving the current understanding of boundary layer flashback with the use of high-speed imaging and laser diagnostics. The focus of this study was on the upstream flame propagation mechanisms under fully premixed and stratified conditions. The experiments were conducted in an optically accessible annular swirl combustor, which allowed for flow imaging inside the mixing tube. For the elevated-pressure flashback experiments, a back-pressure-controlled combustion facility was designed *ab-initio* and installed at the J.J. Pickle Research Campus at UT Austin. For the stratified flame experiments, a swirl-nozzle design was used that was inspired by fuel-injection methods used in some industrial gas-turbine combustors. In this design the fuel is injected into the main swirling flow through fuel ports in the swirler vanes. These fuel ports were located close to the outer wall such that stratification is achieved in the radial direction. Flashback experiments were conducted at pressures up to 5 atm. Hydrogen-enrichment level in the methane-hydrogen fuel was varied from 0% to 87% by volume. The mean axial velocity was kept at 1.0 – 4.0 m/s for flashback runs; however, the laser diagnostic experiments were carried out at the mean axial velocity of 2.5 m/s. By varying the chamber pressure, the hydraulic-diameter-based Reynolds number was varied from 2×10^3 to 3.3×10^4 . A kHz-frame-rate imaging system equipped with a high-speed image-intensifier was used to capture time-resolved chemiluminescence images and simultaneous three-component particle image velocimetry (PIV) data. The assessment of fuel-air mixing was carried out by seeding acetone vapor into the fuel stream and imaging its distribution using planar laser induced fluorescence.

The main objective of this work was to understand the flame-flow interaction during swirl flame flashback. For this, we first investigated fully-premixed flashback and analyzed the effect of three-dimensionality of the flame-flow interaction on the flame

propagation behavior. Upon developing the three-dimensional picture of the propagating flame, further work was focused on flashback that occurs in stratified pre-mixtures. Global flame propagation and stabilization behavior for a stratified swirl flame is reported in this work. High-speed diagnostics were used to investigate the flame propagation behavior, and two different modes of flame propagation were identified. In the following paragraphs, I summarize the findings of this thesis work and propose future work.

5.1 Three-dimensional picture of premixed swirl flame flashback

This work extended the data analysis performed in [76][55], to reveal new physics of flame-flow interaction during flashback in premixed reactants. In this new method for swirling flows, planar 3-component time-resolved PIV data were used to create space-time reconstructions of the 3D flow-field. Focus was kept on low-turbulence stoichiometric methane-air flames since the appearance of this flame is smooth and the global propagation behavior is stable. The most upstream point of the flame, the flame tip, was tracked using the time-resolved luminosity images. It was demonstrated that the flame tip moves with a nearly-constant angular and axial velocity during upstream propagation in the mixing tube. [47]. It was also noted that the flame surface topological features such as the leading edge and the flame tip retain their shapes and sizes during upstream propagation. Based on this observation, a hypothesis of frozen-flame surface was made. This hypothesis imposes the constancy of flame surface in strict sense. The simultaneity of luminosity images and planar information in the laser sheet plane, allowed us to employ space-time equivalence. Under this assumption, the planar images captured in a time-resolved manner were stacked in space such that a three-dimensional flow-field was created. This method also enabled the reconstruction of the 3D flame surface. The reconstructed flame surface and the luminosity images of methane-air flashback were found to be in excellent agreement,

which offers some level of validation of the methodology. The flame surface reconstruction revealed the details on the surface such as the curved flame leading edge or the wrinkles on the flame surface; however, a detailed characterization of the flame surface was not the focus of this work.

The reconstruction of the velocity field provided the flow field in an annulus sector volume, which is a challenging view to obtain with alternative experimental techniques such as tomographic PIV. The three-dimensional quasi-instantaneous flame surface and flow field provided a detailed picture of swirling flame and flow interaction. Quasi-streamlines in the upstream flow were drawn and it was revealed that the flame surface deflects the approach flow in all three directions. In earlier research, attention had been paid to the flame surface blocking the approach flow in the z-direction (along the axis of the center-body). For the first time, the blockage effect of the flame surface was shown to disturb the velocity field in all three directions. This demonstrated blockage effect indicates the presence of a substantial pressure gradient in the vicinity of the flame front. The pressure gradient is often cited as the reason for baroclinic vorticity generation at the flame surface.

Further analysis of the flame-flow interaction was carried out by shifting the reference frame to that of the moving flame surface. This change in observer's frame allowed the flame surface to be steady in time. This approach conveniently allowed us to recreate a steady-flow picture of flame-flow interaction. Once the steady flow-field and flame surface was obtained, the kinematics of a fluid particle could be analyzed before and after burning. In the unburnt section the fluid particle is shown to deflect radially outward upon approaching the flame surface. In the burnt gases, the fluid particle was found to deflect radially inward towards the center-body surface. This observation is not in

agreement with the current understanding of flashback in 2D channels, hence an analysis of fluid parcel movement was carried out with fundamental Newtonian mechanics.

Application of Newtonian mechanics is valid only for inertial frames, i.e., frames which are non-accelerating in nature. The flame structure moves with a constant axial and angular velocity; hence the rotation of the flame structure makes it an accelerating frame of reference. To apply Newtonian mechanics in an accelerating frame of reference, inertial forces or fictitious forces need to be considered. This brings in the role of centrifugal and Coriolis forces in flame-flow interaction. It was assumed that viscous forces have limited role in the kinematics of the fluid parcel. Hence, the motion of the particle can be explained from the balance of three forces, pressure-gradient, centrifugal and Coriolis. By definition, the Coriolis force on a fluid particle depends on the relative velocity of the approaching fluid parcel. On the other hand, for any kind of flashback, it has been shown that the approach flow speed changes due to the blockage effect from the flame surface. Thus, in a rotating frame, the blockage from the flame affects the Coriolis force acting on the fluid particle. The radial component of the Coriolis force is particularly affected by the swirling flame thereby disturbing the force-acceleration balance in the radial direction. It is shown that the Coriolis force experiences a quick increase when the particle crosses the flame surface and accelerates. The resulting force in the radially inward direction concurs with the radial deflection of the fluid particle. However, this motion can not be entirely ascribed to the Coriolis action since the pressure field remains unknown. We further show that the pressure field estimation can not be carried out from a quasi-reconstructed velocity field, owing to the lack of precision.

5.1.1 FUTURE WORK ON PREMIXED-FLAME FLASHBACK

There are several aspects from this work which could be studied further in future. The frozen flame assumption has allowed us to recreate the flame surface of a propagating flame feature. This could be used to obtain detailed information of the flame surface curvature of propagating flames, which could be helpful in assessing fundamental quantities such as flame stretch. Another direction for future studies would be to understand the flashback from the flame's frame of reference. The prevalent approach of predicting the flashback propensity is by identifying the low-momentum approach flow regions, such as in the boundary layer. The closer the flame is to the wall, the more likely it is to flashback. However, while looking at the approach flow from swirl flames' reference frame, the low momentum zone does not exist near the wall but at a certain length away from the wall. The presence of a low momentum zone away from the wall implies that the possibility of flame quenching would be low in such a case. Any investigation in this research direction could also explain the larger flashback propensity of swirling flames relative to non-swirling ones.

5.2 Stratified flame flashback

In next part of this thesis, stratified flame experiments were conducted for a wide range of Reynolds numbers. The level of hydrogen enrichment was varied up to 87%. The global propagation behavior of the flame tongue was studied and two modes of flame stabilization in the mixing tube. The first mode, intermediate stabilization, corresponded to the case when the propagating flame stops at an intermediate location in the mixing tube, and keeps swirling without making a continuous upstream movement. The overall appearance of the flame surface was characterized with a bright flame brush and a relatively dim upstream flame surface. At the leading side of the flame tongue, intermittent bright

structures were noted. The second mode of flame stabilization is characterized by the anchoring of the flame on the fuel ports. In this mode, the flame propagation occurs along the outer wall and it continues until the flame is stabilized on the fuel ports.

The assessment of the degree of stratification was carried out in non-reacting flows with planar laser-induced fluorescence (PLIF) of acetone seeded into the “fuel” stream. The instantaneous PLIF images revealed the distribution of equivalence ratio in the flow field. It was noted that the fuel-rich pockets are frequent near the outer wall, but there is an intermittent presence of these pockets near the center-body. In the mean sense, the flow near the outer wall is richer ($\phi \sim 1.0$ - 1.5 for methane, $\phi \sim 0.5 - 0.6$ for hydrogen) than near the center-body. These equivalence ratios correspond to unstretched laminar flame speeds as high as 0.30 m/s and 1.5 m/s for methane and hydrogen, respectively. In an instantaneous sense, the maximum equivalence ratios were higher for both methane and hydrogen, which corresponded to maximum unstretched laminar flame speeds of 0.30 m/s and 3.0 m/s. Thus, in an instantaneous sense, a hydrogen-air flame has faster propagation speed by an order of magnitude.

Simultaneous high-speed luminosity imaging and stereoscopic PIV measurements were captured at 4 kHz. In the intermediate stabilization mode, it was observed that there are bright flame structures near the leading edge of the flame, which grow in time until they merge with the flame brush. These flame structures seem to follow the path of the swirling flow, which indicates that the effect of flame tongue’s blockage is not a dominant factor in flame-flow interaction. Instead, it is noted that the bright flame structures impose strong blockage on the approach flow. However this blockage is not sustained in time, thus any assistance in upstream propagation of flame is not available. The case of hydrogen-rich flame is different though.

The flame profile captured in the laser sheet plane confirmed the presence of flame structure on the outer wall during hydrogen-rich flashback. The simultaneous luminosity imaging revealed the presence of acute-tipped flame structures on the outer wall. The outer wall propagation of the flame occurred in two distinct phases. In the first phase, the formation of the acute-tipped flame structure initiates upon interaction of bright flame structures with the outer wall. In this phase, the flame structure resists the approach flow without moving in the axial or azimuthal direction. The next phase is marked with the flame advancement towards the fuel ports. In this phase, the flame tip catches on to near stoichiometric mixtures along the outer wall. The flame structure gets brighter as it approaches the fuel ports.

The elevated pressure experiments revealed the role of turbulence in breaking the fuel-parcels into smaller fuel rich pockets. These fuel rich pockets appear as bright flame structures at the leading edge of the flame tongue, however the sizes of bright flame structure are millimeter scale. This flame structure does not affect the flow as much as its atmospheric pressure counterpart. For elevated-pressure hydrogen-rich flashback, the mechanism of acute flame anchoring was the same as that of atmospheric pressure flashback. However, at the flame advancement stage, the flame propagated as a wide flame brush along the outer wall.

5.2.1 FUTURE WORK ON STRATIFIED-FLAME FLASHBACK

Future studies in understanding the stratified flame flashback should be directed towards getting the instantaneous three-dimensional distribution of equivalence ratio. With the current know-how, it would be a challenging experiment in the confined space of the mixing tube. An achievable target would be to get the time-resolved PLIF data inside the

mixing tube, which would allow us to understand the three-dimensional correlated features in the fuel-air pockets. By doing so, one could predict how the fuel-rich pockets would burn. A simultaneous tomographic PIV data could further help us in elucidating the role of back-supported/front-supported mechanism on the flame propagation during flashback.

Appendices

APPENDIX A: FLASHBACK LIMITS FOR SWIRLING FLAMES

Table A-1 Flashback-critical equivalence ratios for premixed and stratified methane-hydrogen swirl flames for different levels of hydrogen enrichment

Flashback limits			
	Re	Premixed	Stratified
0% H₂	5600	0.74	0.84
	8400	0.79	no flashback
25% H₂	5600	0.61	0.71
	8400	0.64	0.71
50% H₂	5600	0.46	0.5
	8400	0.46	0.5
75% H₂	6400	0.33	0.36
	8400	0.33	0.36

APPENDIX B: MATHEMATICAL FORMULATION OF FROZEN FLAME ASSUMPTION

A parametric expression for a three-dimensionally curved surface can be written as

$$S(t) = x(t)\hat{i} + y(t)\hat{j} + z(t)\hat{k}$$

where, x, y and z refer to the cartesian coordinates. While $\hat{i}, \hat{j}, \hat{k}$ refer to the unit vectors. t represents time variable. Since the surface is moving in space, the coordinates are time-dependent.

In cylindrical coordinates, this expression can be written as

$$S(t) = r(t)\hat{e}_r + \theta(t)\hat{e}_\theta + z(t)\hat{k}$$

where r, θ and z represent the radial, azimuthal and axial coordinates

Initially, at $t = t_0$, let us say that the surface is represented as S_0 .

Then, at time, $t = t_0 + \Delta t$

$$S(t_0 + \Delta t) = r(t_0 + \Delta t)\hat{e}_r + \theta(t_0 + \Delta t)\hat{e}_\theta + z(t_0 + \Delta t)\hat{k}$$

Under frozen flame assumption, the back-pressure supported flame surface moves like a solid surface for a small Δt . For current analysis, there is only swirling and axial motion of the flame surface. Thus,

$$\begin{aligned}r(t_0 + \Delta t) &= r(t_0) \\ \theta(t_0 + \Delta t) &= \theta(t_0) + \Omega_f \Delta t \\ z(t_0 + \Delta t) &= z(t_0) + v_{z,f} \Delta t\end{aligned}$$

where, Ω_f and $v_{z,f}$ represent the velocity of the flame tip (or tongue). It should be noted that these expressions can be extended to higher-order terms of a Taylor series expansion, however for the current set of measurements and experiments, it is not done.

$$S(t_0 + \Delta t) = S_0 + \Omega_f \Delta t \hat{e}_\theta + v_{z,f} \Delta t \hat{k}$$

Relative to any observer moving in the lab-frame with a velocity $\vec{v}_{obs} = v_{obs,r} \hat{e}_r + \Omega_{obs} \hat{e}_\theta + v_{obs,z} \hat{k}$, the equation for the surface is expressed by

$$S(t_0 + \Delta t) = S_0 + (\Omega_f - \Omega_{obs}) \Delta t \hat{e}_\theta + (v_{z,f} - v_{obs,z}) \Delta t \hat{k}$$

Thus, for an observer co-rotating with the flame, surface coordinates become independent of time

$$S(t_0 + \Delta t) = S_0 + (\Omega_f - \Omega_{obs})\Delta t \hat{e}_\theta + (v_{z,f} - v_{obs,z})\Delta t \hat{k}$$

Let us define the laser sheet plane

$$L = r(t)\hat{e}_r + \theta(t)\hat{e}_\theta + z(t)\hat{k}$$

Since the laser sheet is aligned along the radial-axial plane, azimuthal position of the laser sheet is fixed in lab-frame. Hence, the laser sheet can be expressed as

$$L = r\hat{e}_r + \theta_0\hat{e}_\theta + z\hat{k}$$

It should be noted that the expression for L represents the set of points in the laser sheet plane. Thus, the vectorial components do not represent the surface normal but the position vectors of points in the plane. There is no temporal dependence in the laser sheet location in lab-frame. However, for an observer co-moving with the flame, the relative position of the laser sheet changes.

$$L_{sheet,f} = r\hat{e}_r + (\theta_0 - \Omega_f\Delta t)\hat{e}_\theta + (z - v_{z,f}\Delta t)\hat{k}$$

For an observer in lab-frame when the flame surface crosses the laser sheet, the flame profile as captured in the laser sheet is an intersection of the flame surface and the laser sheet. Thus, the flame profile (P_{fl}) can be expressed as

$$P_{fl} = S \cap L$$

Since, at least one of the two surfaces is moving, irrespective of the observers frame, the plane profile changes with time and space. It can be expressed as

$$P_{fl} = \underbrace{S(t) \cap L}_{\text{In lab-frame}} = \underbrace{S \cap L(t)}_{\text{In flame-frame}}$$

This equation marks an important implication of the frozen flame. The flame profiles obtained in the laser sheet by a lab-frame observer, are the same as the flame profiles captured by moving the laser sheet, as is seen by a flame-frame observer. Thus, if we know the relative position of the laser sheet in the flame-frame, we can reconstruct the three-dimensional flame surface, as one would do with a scanning-laser sheet.

APPENDIX C: ASSEMBLY DRAWINGS OF THE PRESSURE CHAMBER

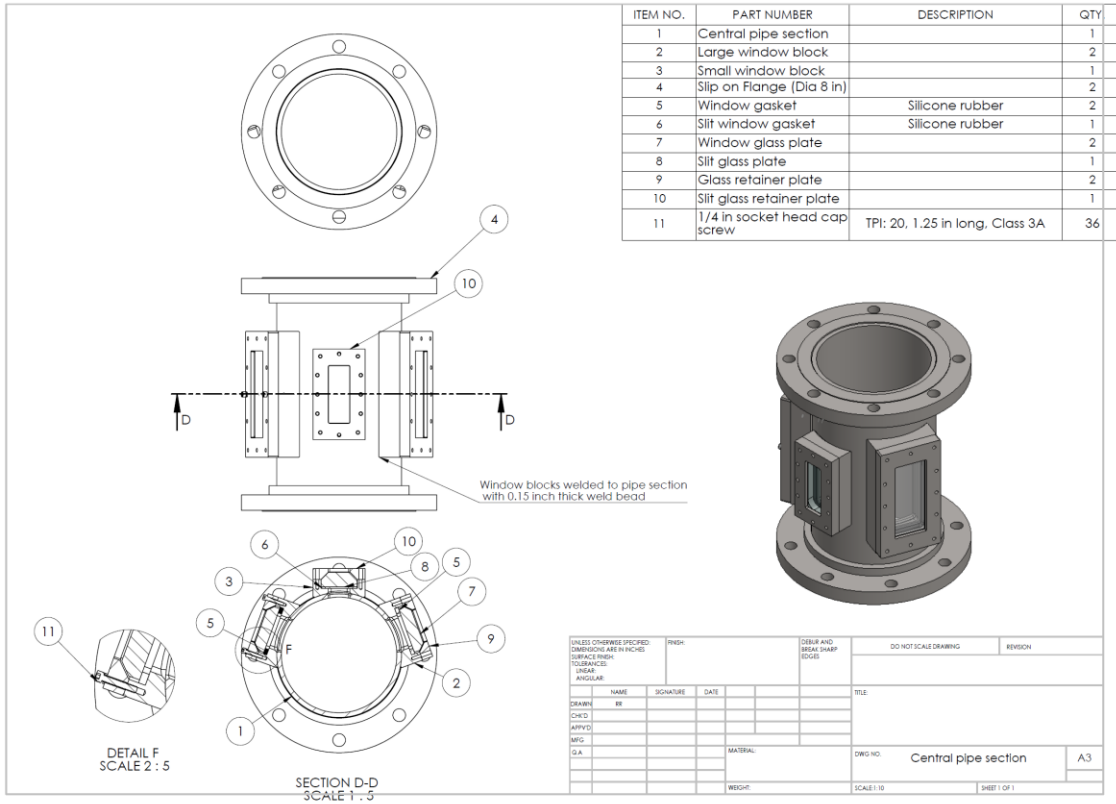


Figure C-1 Assembly of the central section of the pressure chamber

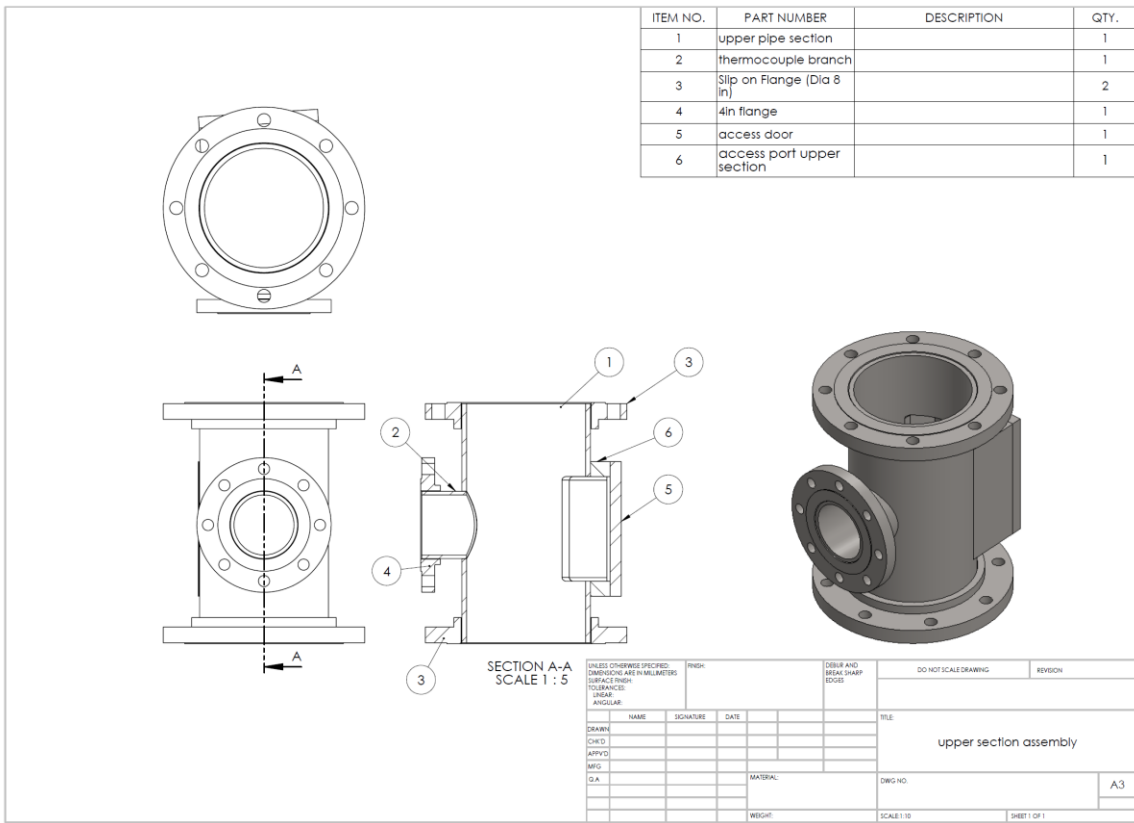


Figure C-2 Assembly of the upper section of the pressure chamber

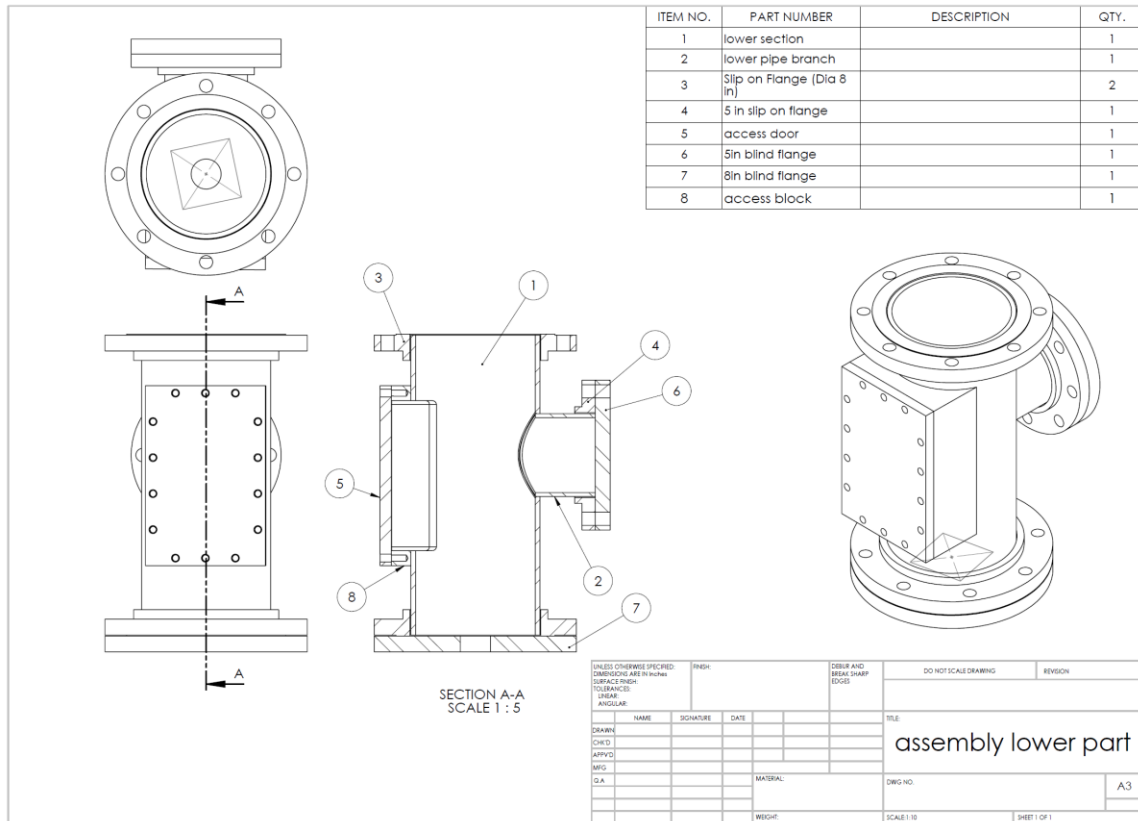


Figure C-3 Assembly of the lower section of the pressure chamber

APPENDIX D: HYDROTESTING OF THE PRESSURE CHAMBER

In order to ensure safe operation of any high-pressure set up, it is essential to conduct a hydro-test. Following pictures illustrate the process in pictures.

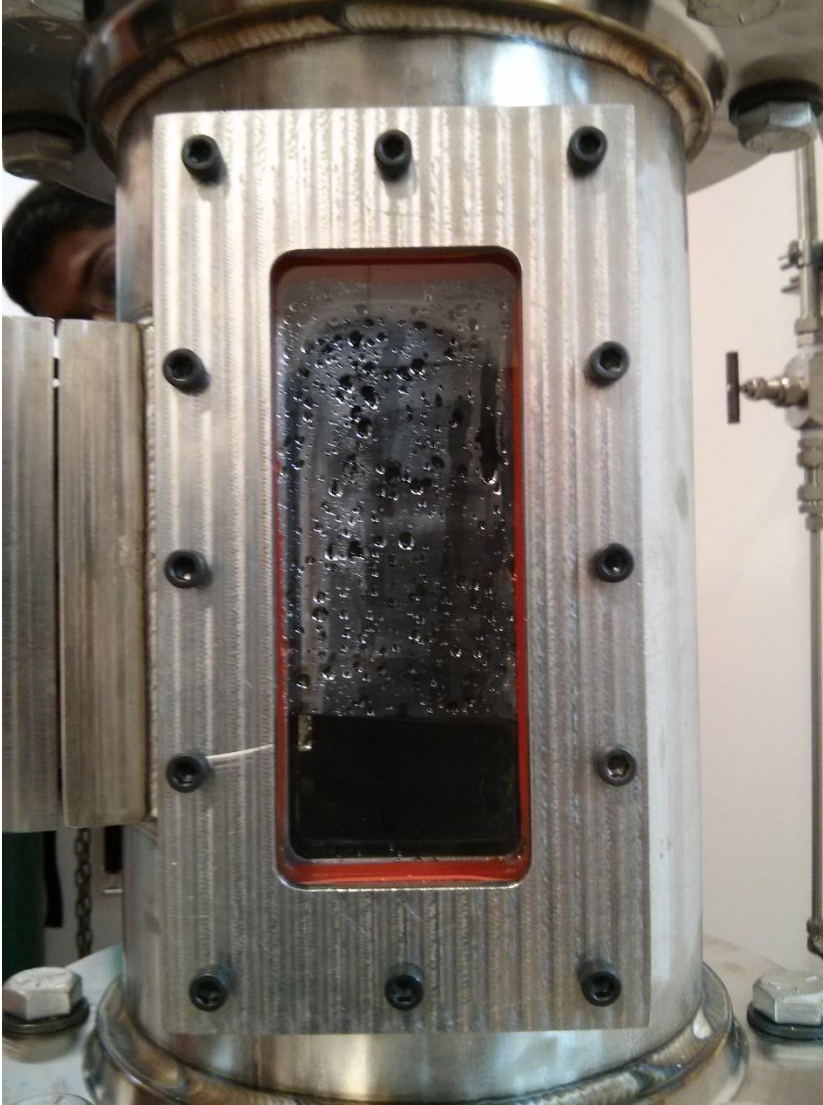


Figure D-1 Water-filling process of the pressure chamber.

First, the pressure chamber was isolated from the upstream and downstream piping. Thereafter, tap-water was supplied to the chamber using a rubber hose which was connected to the top-flange of the chamber. The water level was continuously gauged during the filling process, as illustrated in Fig. D-1. Once the water filling was done, the top flange nuts were also tightened. A quarter-inch Swagelok connection was provided at the top in order to supply high-pressure air. A pressure gauge was mounted on the top flange, as shown in Fig D-2. Once the desired pressure (100 psig) was reached the air supply to the chamber was discontinued.



Figure D-2 Air supply and pressure monitoring at the top flange of the chamber

The pressure reading was continuously monitored. During pressurized condition, any possible leaks were tended to. After confirming that the air pressure stayed the same for over an hour, the hydro-test of the pressure chamber was deemed successful.



Figure D-3 General arrangement of the set up during pressurized condition

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