

1                    **Individual repeatability and heritability of divorce in a wild population**

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23

24 **ABSTRACT**

25 Understanding micro-evolutionary responses of mating systems to contemporary selection  
26 requires estimating sex-specific additive genetic variances and cross-sex genetic covariances in  
27 key reproductive strategy traits. One key trait comprises the occurrence of divorce versus mate-  
28 fidelity across sequential reproductive attempts. If divorce represents an evolving behavioural  
29 strategy that responds to selection it must have non-zero individual repeatability and heritability,  
30 but quantitative estimates from wild populations are scarce. We used 39 years of individual  
31 breeding records and pedigree data from free-living song sparrows (*Melospiza melodia*) to  
32 quantify sex-specific permanent individual and additive genetic variances, and hence estimate  
33 repeatability and heritability, in liability for divorce. We estimated moderate repeatability among  
34 females, but little repeatability among males. Estimates of additive genetic variance were small  
35 in both sexes, and the cross-sex genetic covariance was close to zero. Consequently, the total  
36 heritability was small but likely non-zero, indicating low potential for micro-evolutionary  
37 response to selection. Rapid micro-evolutionary change of divorce rate therefore appears  
38 unlikely, even if there were substantial fitness benefits of divorce and resulting selection.

## 39 INTRODUCTION

40 Pair-bond resilience, resulting from mate-fidelity (i.e. maintaining pair-bonds over multiple  
41 breeding attempts) versus divorce (i.e. dissolving pair-bonds to re-pair with a new mate), is a key  
42 feature of animal mating systems and outcome of sexual selection [1,2]. Such resilience can  
43 fundamentally influence the distribution of offspring across parents and resulting population-  
44 wide variance in fitness.

45 Divorce occurs in numerous socially-monogamous taxa and may increase individual  
46 fitness by counter-acting constraints on initial mate choice, and hence be adaptive [2,3].  
47 However, for there to be ongoing micro-evolution of divorce rate in response to selection [2,4–  
48 6], liability for divorce must have non-zero heritability and hence vary consistently among  
49 individuals (i.e. have non-zero repeatability).

50 In general, repeatable expression of mating and reproductive traits implies that selection  
51 could act consistently on individuals, and typically defines the maximum possible heritability  
52 [7,8]. Decomposing total phenotypic variance into permanent (i.e., repeatable) individual  
53 variance ( $V_I$ ), additive genetic variance ( $V_A$ ) and environmental variance allows estimation of  
54 heritability and indicates the potential for micro-evolutionary responses to contemporary  
55 selection [9]. However, divorce represents an interesting jointly-expressed (i.e. ‘emergent’) trait  
56 that results from female-male interactions and can be simultaneously influenced by genetic and  
57 non-genetic effects of both pair members. Further, correlated effects of genotypes, when  
58 expressed in females versus males, create non-zero cross-sex genetic covariance ( $COV_{A\text{♀♂}}$ ) and  
59 can generate evolutionary sexual conflict over divorce [10]. Such non-zero  $COV_{A\text{♀♂}}$  alters the  
60 contributions of sex-specific genetic effects to the phenotypic and total additive genetic variances  
61 in divorce rate, and alters the potential for evolutionary responses to sex-specific selection

62 resulting from the fitness consequences of divorce [11]. Understanding the evolutionary  
63 dynamics of divorce, and the implications for other co-evolving reproductive behaviours  
64 contributing to mating systems, therefore requires explicit estimation of sex-specific  $V_I$  ( $V_{I♀}$  and  
65  $V_{I♂}$ ),  $V_A$  ( $V_{A♀}$  and  $V_{A♂}$ ), and  $COV_{A♀♂}$ , in divorce in populations experiencing un-manipulated  
66 natural and sexual selection environments.

67 Advances in quantitative genetic methods mean that  $V_{A♀}$ ,  $V_{A♂}$ , and  $COV_{A♀♂}$  underlying  
68 emergent traits can be estimated given complex relatedness structures arising in wild populations  
69 [9]. Since divorce versus mate-fidelity represent alternative phenotypic outcomes of pairing  
70 decisions across consecutive breeding attempts, divorce is appropriately modelled as a ‘threshold  
71 trait’, where breeding pairs’ underlying continuous joint liabilities for divorce translate into  
72 expression at some threshold (e.g. [12]). Such models also permit estimation of ‘total  
73 heritability’ of divorce, resulting from the combination of  $V_{A♀}$ ,  $V_{A♂}$ , and  $COV_{A♀♂}$  [13], which  
74 represents the overall potential for micro-evolutionary responses to selection on the population-  
75 wide distribution of liabilities [11]. Such analyses require phenotypic observations of divorce  
76 versus mate-fidelity, conditional on survival between consecutive breeding attempts, from  
77 diverse relatives [14]. We use 39 years of comprehensive observations of free-living song  
78 sparrows (*Melospiza melodia*) to estimate (i) population-level divorce rate, (ii)  $V_{I♀}$ ,  $V_{I♂}$ ,  $V_{A♀}$ ,  
79  $V_{A♂}$  and  $COV_{A♀♂}$  in divorce, and (iii) individual repeatability and the sex-specific and total  
80 heritability, thereby assessing the potential for ongoing evolution of divorce as a key  
81 reproductive strategy.

82

## 83 MATERIAL AND METHODS

84 A resident population of individually colour-ringed song sparrows on Mandarte Island, Canada  
85 has been intensively studied since 1975. Each year, all individuals alive in late April (typical  
86 start of breeding [15]) are recorded in a comprehensive census to determine over-winter survival  
87 and pairing status (re-sighting probability  $>0.99$  [16]), and all breeding attempts are closely  
88 monitored (ESMS1). Females and males form socially persistent pairings and jointly rear  
89 offspring (1–4 broods per year), but can form new pairings within and between breeding seasons  
90 following divorce or mate-death.

91 To identify cases of divorce versus mate-fidelity, we extracted each female’s lifetime  
92 sequence of breeding events ( $\geq 1$  egg laid) where re-pairing could have occurred (i.e. she initiated  
93 a subsequent breeding event) and categorized these events as divorce (i.e. paired with a different  
94 mate for her subsequent breeding event when mate-death did not occur), mate-fidelity, or mate-  
95 death according to the pair-bond’s fate (ESMS1). Instances of mate-death were identified from  
96 daily field observations and April censuses, and excluded from our dataset.

97 We fitted two generalized linear mixed models to decompose total variance in pair liability  
98 for divorce. Model 1 estimated variances attributable to  $V_{I\text{♀}}$ ,  $V_{I\text{♂}}$ , and of unique female-male  
99 social pairings ( $V_S$ ), and the year when a focal breeding event occurred ( $V_Y$ ). Model 2  
100 additionally estimated  $V_{A\text{♀}}$ ,  $V_{A\text{♂}}$ , and  $\text{COV}_{A\text{♀♂}}$  in pair liability for divorce, using comprehensive  
101 pedigree data to quantify relatedness (i.e. an ‘animal model’ [9]; ESMS2).  $\text{COV}_{A\text{♀♂}}$  is the  
102 covariance between additive genetic effects of alleles expressed in all females versus all males,  
103 not the genetic covariance between a female and her socially-paired mate (e.g. [15,17]; ESMS3).  
104 Thus, both models treat divorce as an emergent trait of the breeding pair, and do not specify sex-  
105 specific effects as ‘direct’ or ‘indirect’ (ESMS3). Our current aim was to partition the total  
106 naturally-occurring variation in liability for divorce and thereby appropriately estimate

107 heritability, not to explain variation in the occurrence of divorce. Fixed effects were  
108 consequently restricted to a two-level factor that defined whether an observation of divorce  
109 versus mate-fidelity spanned breeding events separated by the non-breeding season ('between-  
110 season') versus consecutive events within the same season ('within-season', ESMS1) and  
111 separate regressions on female and male individual coefficients of inbreeding ( $f$ , Model 2 only),  
112 thereby estimating inbreeding depression in liability for divorce and minimising any associated  
113 bias in estimated  $V_A$  [18].

114 Sex-specific repeatabilities in liability for divorce were estimated from Model 1 as:

$$115 \quad \text{Repeatability}_{\varphi} = \frac{V_{I\varphi}}{V_{P\_Model1}} \quad \text{and} \quad \text{Repeatability}_{\sigma} = \frac{V_{I\sigma}}{V_{P\_Model1}}$$

116

117 Sex-specific heritabilities ( $h^2$ ) were estimated from Model 2 as:

$$118 \quad h^2_{\varphi} = \frac{V_{A\varphi}}{V_{P\_Model2}} \quad \text{and} \quad h^2_{\sigma} = \frac{V_{A\sigma}}{V_{P\_Model2}}$$

119

120 The 'total heritability' ( $T^2$ ) was calculated from Model 2 as:

$$121 \quad T^2 = \frac{V_{A\varphi} + V_{A\sigma} + 2(COV_{A\varphi\sigma})}{V_{P\_Model2}}$$

122 The total variance in liability ( $V_{P\_Model1}$ ,  $V_{P\_Model2}$ ) was calculated separately for each model  
123 (ESMS3). Models were fitted using Bayesian inference in R [19] with relatively uninformative  
124 priors (ESMS5). Posterior distributions of repeatabilities, heritabilities, and  $T^2$  were calculated  
125 from marginal posterior distributions of underlying variance components. We report liability-

126 scale posterior modes, means and 95% credible intervals (95%CI) from 5000 posterior samples,  
127 and present prior distributions alongside posteriors to facilitate inference. Estimates and  
128 conclusions were robust to alternative model specifications (ESMS5).

129

## 130 **RESULTS**

131 There were 1,419 breeding events where divorce could have occurred, involving 566 unique  
132 social pairings among 358 females and 341 males. Divorce occurred on 166 (11.7%) occasions  
133 (details in ESMS1).

134 Model 1 revealed that the largest component of variance in overall liability for divorce  
135 was  $V_{I♀}$ , while  $V_{I♂}$  was comparatively small (table 1, ESMS4). Because  $V_S$  and  $V_Y$  were also  
136 small, female repeatability for divorce was moderate (~16%; table 1). The lower 95%CI limit  
137 converged towards zero, but 98% of posterior samples exceeded 0.01, departing from the prior  
138 distribution (figure 1a), and indicating that female repeatability is most likely greater than zero.  
139 In contrast, male repeatability was smaller (table 1); only 76% of posterior samples exceeded  
140 0.01 (figure 1b). Divorce was less likely to occur within a breeding season than between seasons  
141 (table 1).

142 Model 2 showed that  $V_{A♀}$  and  $V_{A♂}$  in liability for divorce were both small, and  
143  $COV_{A♀♂}$  was estimated as close to zero (table 1, ESMS4). Sex-specific heritabilities were  
144 therefore small for both females and males. However, posterior distributions departed from the  
145 priors, with higher density at higher values (e.g. at the posterior means, figure 2a,b) implying  
146 that heritabilities, and underlying  $V_{A♀}$  and  $V_{A♂}$ , exceed zero. Indeed,  $V_{A♀}$ ,  $V_{A♂}$ , and  $COV_{A♀♂}$   
147 combined to generate a small but likely non-zero total heritability ( $T^2$ ) for divorce (table 1); 92%

148 of posterior samples exceeded 0.01. This again deviates from the prior distribution (figure 2c),  
149 and from the posterior distribution that would have resulted given zero  $V_{A♀}$ ,  $V_{A♂}$  and hence  $T^2$   
150 (ESMS5). Liability for divorce tended to increase with increasing individual coefficient of  
151 inbreeding ( $f$ ), especially in females, but the 95% CIs overlapped zero (table 1).

152

## 153 **DISCUSSION**

154 The ~12% divorce rate observed in song sparrows is relatively low compared to other temperate-  
155 breeding passerine birds (~20–50%; [14,20,21]). However, there was evidence of moderate  $V_{I♀}$   
156 and hence female repeatability, but lower  $V_{I♂}$  and male repeatability, in liability for divorce  
157 (figure 1a,b, ESMS4). These estimates imply that sex-specific  $h^2$  is not *a priori* zero (i.e. given  
158 zero repeatability). However in practice,  $h^2$  was estimated to be small in both sexes.

159           Most previous quantitative genetic analyses of divorce come from human twin-studies,  
160 and show relatively high heritabilities with divorce defined as a sex-specific trait (e.g. 0.3–0.6  
161 [22,23]). However, such estimates may be inflated by shared environmental and cultural effects  
162 [9], and often only consider whether individuals ever divorced over their lifetime. Our focus on  
163 sequential breeding events, considering among-individual variances across repeat observations,  
164 allows estimation of individual repeatability as well as pair and year variances, which encompass  
165 variances stemming from ecological and/or social environmental effects that could influence the  
166 occurrence of divorce. The only previous quantitative genetic analysis of divorce in a wild (non-  
167 human) population also estimated low female heritability in savannah sparrows (*Passerculus*  
168 *sandwichensis*) [14]. Because [14]’s estimate of male repeatability for divorce was not  
169 distinguishable from zero, heritability estimates were restricted to females and did not consider



170 potential contributions of  $V_{A\delta}$  or  $COV_{A\delta\delta}$ . Our results suggest that sex-specific genetic effects  
171 expressed in both sexes contribute to the total additive genetic variance, and hence to the total  
172 heritability for divorce ( $T^2$ ) in song sparrows. Indeed small, potentially undetectable, effects in  
173 each sex can combine to generate detectable total  $T^2$  [13]. Thus the overall apparent potential for  
174 micro-evolutionary responses to selection on divorce is greater when considering the interactive  
175 effects of the sexes jointly (i.e. considering divorce as an emergent trait) than when considering  
176 either sex alone.

177           Many studies have investigated the potential costs and benefits of divorce in wild  
178 populations, particularly in socially-monogamous birds (reviews: [2,3,5]). Divorce is generally  
179 considered to be adaptive, and increases an individual's subsequent breeding success and hence  
180 fitness under certain conditions [2,3]. However, ongoing micro-evolutionary responses to such  
181 contemporary selection require  $V_A$ . Our results indicate that such  $V_A$ , and consequent potential  
182 for evolutionary response to selection, while probably non-zero, is smaller than is often  
183 implicitly assumed [2,4–6]. Further, relatively low divorce rates, such as observed in song  
184 sparrows, will intrinsically limit the intensity of selection [12]. Overall, rapid and marked micro-  
185 evolutionary changes in the frequency of divorce appear unlikely, even if divorce were beneficial  
186 for one or both sexes. Consequently, there is also limited potential for genetic covariance  
187 between liability for divorce and other key reproductive strategy traits, such as female extra-pair  
188 reproduction (EPR), negating the suggestion that divorce and EPR both represent manifestations  
189 of an underlying 'weak-pair' syndrome [24] and limiting the potential for indirect selection.

190

191 **Ethics**

192 All field procedures approved by the University of British Columbia Animal Care Committee  
193 ethical review (certificates UBCACC A12-0229 and A14-0336).

194

### 195 **Data accessibility**

196 Data and code are available as electronic supporting information.

197

### 198 **Authors' contributions**

199 RRG and MEW designed the study and conducted analyses with input from JMR. All authors  
200 contributed to writing, agree to be held accountable for all aspects of the work, and approve the  
201 final version of the manuscript.

202

### 203 **Competing interests**

204 We declare no competing interests.

205

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215

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273 **Table 1:** Marginal posterior modes, means and 95% CIs from models decomposing total variance  
274 in liability for divorce.  $V_I$  and  $V_A$  represent permanent individual and additive genetic variances  
275 for females ( $\ominus$ ) and males ( $\omin�$ ).  $COV_{A\ominus\omin�}$  is the cross-sex genetic covariance.  $V_S$  and  $V_Y$  are the  
276 social pair and year variances, respectively. Posterior statistics for sex-specific repeatabilities and  
277 heritabilities ( $h^2$ ), ‘total heritability’ ( $T^2$ ), fixed effects of within-season versus between-season  
278 (intercept) and regressions on individual female or male coefficient of inbreeding ( $f$ ) are also  
279 shown.

	Model 1		Model 2	
	mode, mean	95%CI	mode, mean	95%CI
<b>variance components</b>				
$V_{I♀}$	0.24, 0.28	$4 \times 10^{-6}$ , 0.53	0.003, 0.22	$6 \times 10^{-7}$ , 0.48
$V_{I♂}$	0.001, 0.09	$5 \times 10^{-8}$ , 0.26	0.002, 0.08	$4 \times 10^{-8}$ , 0.25
$V_S$	0.001, 0.14	$2 \times 10^{-9}$ , 0.46	0.003, 0.15	$4 \times 10^{-8}$ , 0.48
$V_Y$	0.001, 0.07	$4 \times 10^{-7}$ , 0.19	0.001, 0.07	$8 \times 10^{-9}$ , 0.19
$V_{A♀}$			0.001, 0.07	$5 \times 10^{-9}$ , 0.25
$V_{A♂}$			0.001, 0.08	$4 \times 10^{-8}$ , 0.21
$COV_{A♀♂}$			-0.0002, -0.003	-0.08, 0.06
<b>variance ratios</b>				
repeatability $_{♀}$	0.16, 0.17	$3 \times 10^{-6}$ , 0.30		
repeatability $_{♂}$	0.001, 0.05	$3 \times 10^{-8}$ , 0.15		
$h^2_{♀}$			0.001, 0.04	$2 \times 10^{-9}$ , 0.14
$h^2_{♂}$			0.001, 0.04	$3 \times 10^{-8}$ , 0.12
$T^2$			0.02, 0.08	$1 \times 10^{-4}$ , 0.20
<b>fixed effects</b>				
intercept	-0.64, -0.66	-0.89, -0.44	-0.81, -0.90	-1.28, -0.59
within-season	-1.08, -1.10	-1.34, -0.85	-1.11, -1.12	-1.37, -0.87
$f_{♀}$			1.92, 1.98	-0.66, 4.45
$f_{♂}$			0.59, 0.94	-1.72, 3.61

282 **Figure 1.** Marginal posterior samples (bars), density (solid black line), mean (red dotted line)  
283 and 95%CI limits (dashed lines) of sex-specific repeatabilities for divorce in (a) female and (b)  
284 male song sparrows. Blue lines illustrate prior distributions (ESMS5). Areas where the posterior  
285 density exceeds the prior density highlight parameter values that are likely supported by the data.

286

287 **Figure 2.** Marginal posterior distributions for (a) female and (b) male heritabilities ( $h^2$ ), and (c)  
288 the total heritability ( $T^2$ ) for divorce in song sparrows. See figure 1 for plot description.



**Electronic Supplemental Materials for:**  
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**Electronic Supplemental Material S1 – Descriptive details of re-pairing dataset**

*S1.1 Classifying re-pairing due to divorce and mate-death*

Divorce rates are often highest in relatively short-lived species where re-pairing due to mate-death is also common [1]. However, because most study systems lack comprehensive observations of individual survival and/or records of the lifetime number of reproductive attempts, many investigations of divorce are severely limited in their ability to accurately ascribe instances of re-pairing due to divorce versus mate-death [2,3]. In contrast, the small size of Mandarte Island (~6ha) and intensity of field monitoring (below), mean that the causes of re-pairing among song sparrows can be accurately ascribed, presenting a valuable opportunity to dissect the quantitative genetic basis of divorce independent of mate-death.

In the Mandarte Island study population, males and females can begin breeding in their first adult season (aged one year) and rear 1–4 broods per year over a median lifespan of approximately 2 years [4]. Following a complete annual census in late April designed to document over-winter survival and identify new immigrant breeders, all individuals on Mandarte are closely monitored through the end of breeding in late July-early August [4]. All offspring surviving ~6 days post-hatch and immigrants (0.92<sup>-year</sup> on average) are colour-ringed. During monitoring, the territories of each breeding pair, and of unpaired males (typically ~10–40% of males annually), are visited every 3–5 days to record nesting and

territorial behaviour. Any instances of territorial take-overs or within-season re-pairing are thus observed soon after they occur [5].

Each breeding event (social pairing where  $\geq 1$  egg was laid) constitutes an observation after which a social pair could potentially express divorce or mate-fidelity (conditional on both individuals surviving to a subsequent breeding event). To extract these observations, we tabulated each female's lifetime sequence of breeding events, except her last (where expression of mate-fidelity or re-pairing is not possible), and recorded whether the identity of her social mate changed between the focal and subsequent event. Instances where social male identity did not change were classified as 'mate-fidelity'. For instances where the female's social mate did change, we determined whether her mate from the focal event was observed in the population (breeding or otherwise) later that season during daily monitoring and/or survived to the following April census (i.e. within-season vs between-season re-pairing). In instances where the male survived to the next breeding event of his former mate, re-pairing was classified as 'divorce', whereas if the male did not survive re-pairing was classified as 'mate-death'. Breeding events ending in mate-death were excluded from the 'divorce dataset' (See ESMS 1.2), but subsequent breeding events by the focal female which could have ended in divorce or mate-fidelity were retained. All observations in the dataset therefore describe whether a pair divorced or not after a given breeding event, and thus the focal trait describes a change in state between two consecutive breeding events. We attributed observations of divorce or mate-fidelity to characteristics of the initial breeding event of each social pair. Thus, independent variables associated with the trait (e.g. within- versus between-season, and observation year) are attributed to the initial event. The same phenotypic dataset would have been obtained had we instead focused on sequences of male rather than female breeding events [6,7].

Due to reduced field effort in 1980, information on social pairing throughout the breeding season and thus within-season divorce or mate-death was not available. However, information on the survival of all individuals alive at the beginning of the 1980 season was still collected via the April census. Consequently, two breeding events at the end of 1979 (i.e. each female's last breeding event for that year) could be accurately classified as 'between-season mate-death', whereas all other breeding events that could have ended in re-pairing at the end of 1979 ( $n = 5$ ) were excluded due to uncertainty in whether females maintained mate-fidelity or re-paired in 1980.

### SI.2 Descriptive statistics of re-pairing dataset

Of the 1,595 total breeding events which could have resulted in re-pairing from 1979–2015, there were 176 instances of re-pairing due to mate-death (11%). Of these, 120 mate-deaths occurred 'between-seasons', while 56 mate-deaths occurred 'within-season'. Of the 166 instances of divorce (see *Results*), 91 occurred 'between-seasons', while 75 occurred 'within-season'.

The 358 females included in our 'divorce dataset' (i.e. 1,419 breeding events where divorce could have occurred, *Results*) formed a mean of 1.58 ( $\pm 0.90$  SD, range 1–6) unique social pairings, and 220 females formed only one social pair. The 341 males formed a mean of 1.66 ( $\pm 0.97$  SD, range 1–7) unique social pairings, and 204 males formed only one social pair. Further, there were 72 exclusive pairings where a females only ever paired with a single male that did not pair with any other female. These characteristics of the data were sufficient to separate female and male individual effects on divorce in Models 1 and 2, as well as to separate social pair identity effects from the individual effects of each female and male (see ESMS5.3). Over the 36 observation years included in our study (1979–2015; excluding 1980,

above), there was a mean of 39.4 ( $\pm 21.9$  SD, range 1–81) breeding events per year that could have ended in divorce. Of these, there was a mean of 4.6 ( $\pm 3.1$  SD, range 0–11) divorces per year.

## **Electronic Supplemental Material S2 – Summary of pedigree construction**

We compiled a complete social pedigree, wherein detailed field observations from 1975–2015 were used to assign all ringed chicks to their social parents. All chicks ringed since 1993 and their potential parents, plus an additional sample of chicks ringed between 1986–1992, were genotyped at 160 polymorphic microsatellite loci, allowing genetic paternity assignment with extremely high confidence [8]. We used all available genetic parentage data to correct the social pedigree for ~28% extra-pair paternity so far as feasible (details of pedigree reconstruction [6]). The resulting pedigree for 1975–2015 was pruned to all phenotyped individuals and their known ancestors, and then used to construct the inverse of the numerator relatedness matrix and to calculate individual coefficients of inbreeding ( $f$ ) (e.g. [9–11]). The pruned pedigree comprised 959 individuals. Across the phenotyped individuals, mean female  $f$  was  $0.054 \pm 0.053$  SD, and mean male  $f$  was  $0.054 \pm 0.056$  SD.

## Electronic Supplemental Material S3 – Model details, implementation and interpretation

### S3.1 Model details

The occurrence of divorce was modelled as a threshold trait using generalized linear mixed models, where each observation (i.e. mate-fidelity or divorce after a focal breeding event) is assigned a value for the normally distributed liability of divorce [12–14]. Such threshold models are a well-established method for treating dichotomous traits in quantitative genetics [12]. Conceptually, they consider an underlying continuously distributed (Gaussian) variable – the ‘liability’ – that translates into expression of a discrete phenotype at some threshold value. Such models ensure that the key quantitative genetic assumption of multivariate normality of additive genetic effects is fulfilled irrespective of the observed frequency of occurrence of the focal phenotype(s).

In our model, liability values below the threshold result in expression of mate-fidelity, whereas values above the threshold result in divorce. Liability is an emergent trait of each focal social pair and is modelled by a linear function of factors unique to each female, male and social pair [8–10,14]. We fitted two nested models that decomposed the vector containing each pair's liability for divorce across observations ( $\mathbf{l}$ ):

$$\mathbf{l} = \mathbf{X}\boldsymbol{\beta} + \mathbf{Z}_i\mathbf{i} + \mathbf{Z}_s\mathbf{s} + \mathbf{Z}_y\mathbf{y} \quad (\text{Model 1})$$

$$\mathbf{l} = \mathbf{X}\boldsymbol{\beta} + (\mathbf{Z}_a\mathbf{a} + \mathbf{Z}_i\mathbf{i}) + \mathbf{Z}_s\mathbf{s} + \mathbf{Z}_y\mathbf{y} \quad (\text{Model 2})$$

into vectors of fixed effects ( $\boldsymbol{\beta}$ ) and random permanent individual ( $\mathbf{i}=[\mathbf{i}_\varnothing', \mathbf{i}_\sigma']$ ), social pair identity ( $\mathbf{s}$ ), year of initial breeding event ( $\mathbf{y}$ ), and additive genetic ( $\mathbf{a}=[\mathbf{a}_\varnothing', \mathbf{a}_\sigma']$ ) effects.

Parentheses in Model 2 are not mathematically necessary, but visually group sources of repeatable individual effects. Random effects  $\mathbf{s}$  and  $\mathbf{y}$  follow univariate normal distributions, defined by means of zero and variances to be estimated. Residual effects are not explicitly

included in the liability of the threshold model (eqn. 4 of [14]). Female and male permanent individual and additive genetic effects are assumed to follow bivariate normal distributions, defined by means of zero and covariance matrices:

$$\mathbf{G}_I = \begin{bmatrix} V_{I\text{♀}} & 0 \\ 0 & V_{I\text{♂}} \end{bmatrix} \quad \mathbf{G}_A = \begin{bmatrix} V_{A\text{♀}} & \text{COV}_{A\text{♀♂}} \\ \text{COV}_{A\text{♀♂}} & V_{A\text{♂}} \end{bmatrix}$$

where  $V_{I\text{♀}}$  and  $V_{I\text{♂}}$  are the variances among female and male permanent individual effects,  $V_{A\text{♀}}$  and  $V_{A\text{♂}}$  are the variances among female and male additive genetic effects, respectively, and  $\text{COV}_{A\text{♀♂}}$  is the cross-sex covariance in additive genetic effects. Because related females and males, each socially paired to other individuals, share some alleles,  $\text{COV}_{A\text{♀♂}}$  represents the covariance in additive genetic effects among opposite sex relatives, weighted by the probability of sharing alleles identical by descent. Note that  $\text{COV}_{A\text{♀♂}}$  is not the covariance in additive genetic effects between a female and her socially paired mate [9,11]. However, no such cross-sex covariance among permanent individual effects ( $\mathbf{i}$ ) is defined. To estimate  $\mathbf{G}_A$ , individual female and male identities in Model 2 were each linked to the inverse of the numerator relatedness matrix [12,16] constructed from the pedigree (ESMS2, [8–11]). The threshold on the liability scale is set to zero by using a probit link function and fixing the residual variance to one [14]. Accordingly, this model simultaneously estimates female and male additive genetic effects on liability for divorce, and estimates the cross-sex covariance. It consequently does not *a priori* define divorce as primarily a trait of one sex or the other, or hence specify the sex-specific genetic effects as ‘direct’ or ‘indirect’ (*sensu* [17]). These estimated variance components partition the total variance in liability for divorce. They thereby encompass effects of ecology and the social environment on that liability such as could stem, for example, from variation in the presence of other potential mates.

Because our aim was to estimate repeatability and heritability for the observed variation in liability for divorce, not to explain population-wide variation in divorce rate or

partition variance in divorce conditioned on all possible environmental influences, we fitted minimal fixed effects. Specifically, we modelled between-season versus within-season effects and regressions on individual  $f$  (see *Methods*), but did not explicitly model effects of other variables, for example including age or pair relatedness (for which see [7]). To minimize under-estimation of  $f$ , phenotypic observations were restricted to individuals with known grandparents, hence truncated to 1979–2015, and excluded immigrants.

### S3.2 Model implementation

Models were fitted using Bayesian inference to obtain 5,000 samples of the posterior distribution of parameters using the R [18] packages *MCMCglmm* [13] and *nadiv* [19], following a burn-in of 10,000 iterations and implementing a thinning interval of 5,000 iterations for a total of 25,010,000 model iterations. We used diffuse normal prior distributions (mean=0 and variance= $10^{10}$ ) for all fixed effects and parameter expanded priors for variance components, which gave relatively uninformative priors with scaled non-central  $F$ -distributions of numerator and denominator degrees of freedom equal to one [20] and scale parameter of 1,000.

Since liability for divorce was modelled as an emergent (‘joint’) trait stemming from the individual (Models 1 and 2) and additive genetic (Model 2) effects of both females and males, as well as the additive genetic covariance (Model 2), total phenotypic variance ( $V_P$ ) for divorce in each model, conditioned on the fitted fixed effects, is approximated on the liability scale as:

$$V_{P\_Model\ 1} = V_{I\text{♀}} + V_{I\text{♂}} + V_S + V_Y + 1 \quad (\text{Model 1})$$

$$V_{P\_Model\ 2} = V_{A\text{♀}} + V_{A\text{♂}} + 2(\text{COV}_{A\text{♀}\text{♂}} \times \bar{r}) + V_{I\text{♀}} + V_{I\text{♂}} + V_S + V_Y + 1 \quad (\text{Model 2})$$



Here,  $\bar{r}$  is the mean female-male relatedness across all observed breeding pairs, where relatedness  $r$  for each observed pairing is calculated as twice the coefficient of kinship between paired individuals, as obtained from the numerator relatedness matrix constructed from the pedigree [21–23]. Across the 566 pairings that contributed phenotypic data,  $\bar{r} = 0.146$ . The addition of a one on the right hand side of each equation for  $V_P$  is the link scale variance for a probit link function and additive overdispersion model. Unlike in a binomial model with logit link, no residual variance is included in the calculation of  $V_P$  for a threshold model with probit link, because the residual effect is incorporated as part of the threshold parameter (see the description of Model 2 above and eqn. 4 of [14]).

### S3.3 Evolutionary interpretation

When emergent traits are jointly expressed by a pair of opposite sex individuals, each paired individual expresses sex-specific genetic effects that influence the emergent trait. Each individual also carries sex-specific genetic effects that would be expressed if in the opposite sex. The correlation between these within-individual male- and female-specific additive genetic effects on liability for divorce, emerging across all population members, is measured by the cross-sex additive genetic covariance ( $COV_{A\text{♀♂}}$ , [24]).

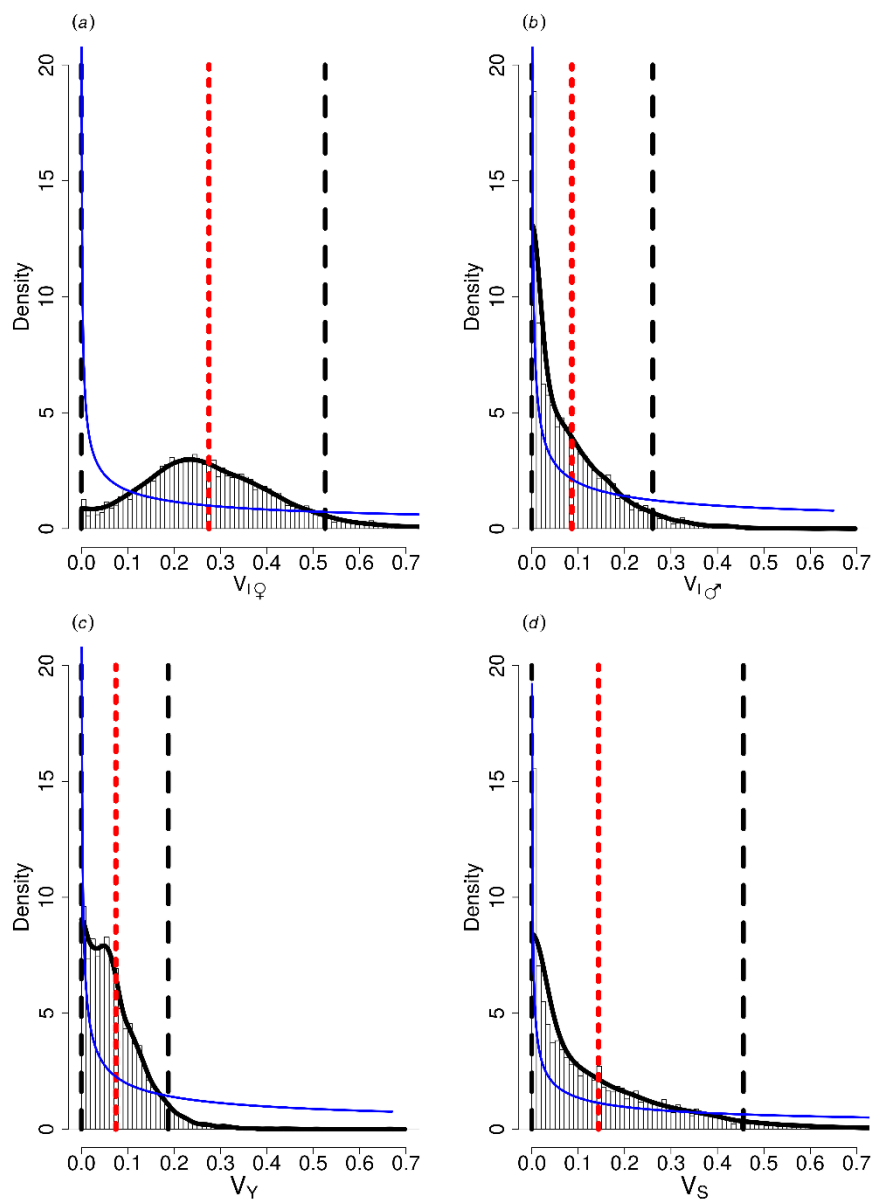
Sex-specific selection on emergent trait phenotypes is described by the covariance between fitness in the focal sex and phenotypes expressed by pairs of opposite sex individuals. Selection acting on one sex can therefore alter the distributions of both female and male sex-specific genetic effects on liability for divorce that are carried by all members of the sex under selection [24]. Hence an evolutionary response to selection on mean liability for divorce can occur via sex-specific selection, altering the additive genetic effects of both sexes in the next generation. Consequently, the total additive genetic variance measures the

standing genetic variation available for an evolutionary response to selection in the population's liability for divorce. Because all individuals carry both sex-specific genetic effects on the emergent trait, the sex-specific additive genetic variances alone are not sufficient to quantify the potential evolutionary response to selection.

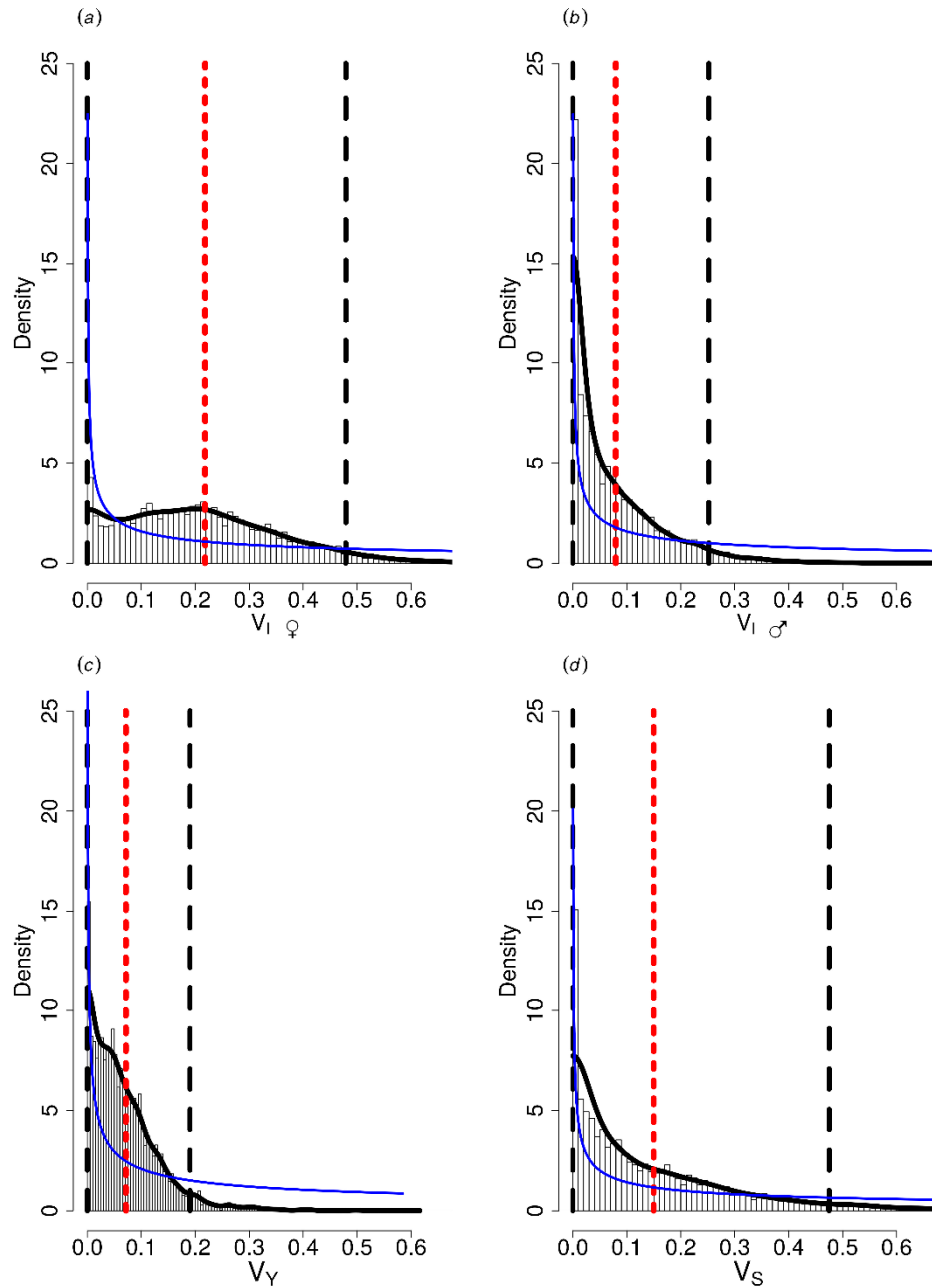
Broadly analogous to a standard heritability, the total additive genetic variance can be expressed relative to the phenotypic variance in the population before selection. In contrast to the total additive genetic variance, the phenotypic variance does not measure the variance in both sex-specific effects on the emergent trait contained within individuals. Instead, it measures the net impact of all effects that are expressed by individuals engaged in emergent traits, and ignores effects that are carried but not expressed. Consequently, the phenotypic variance can potentially be less than the total additive genetic variance [24].

## Electronic Supplemental Material S4 – Full posterior variance component distributions

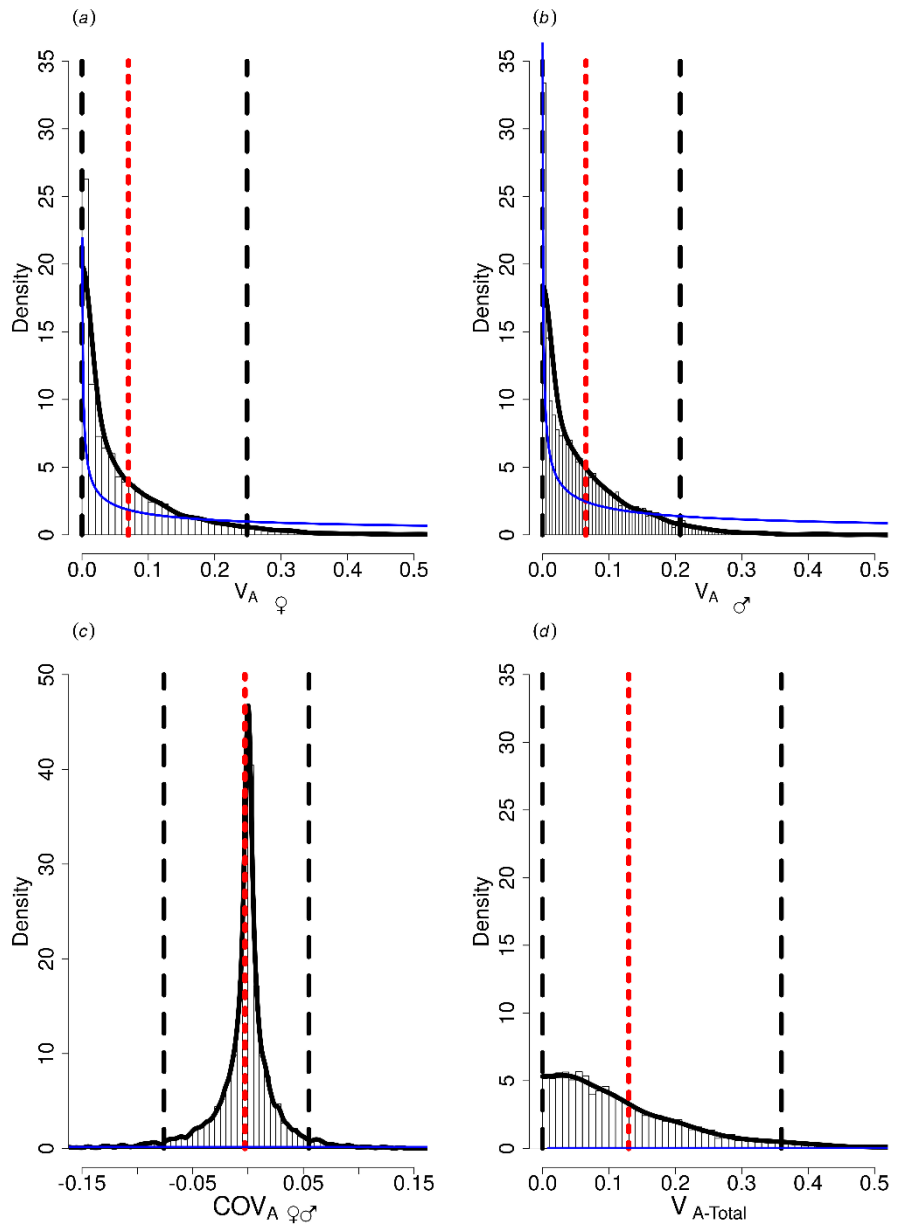
**Figure S1.** Marginal posterior samples (bars), density (solid black line), mean (red dotted line), and 95%CI limits (dashed lines) of variance component estimates from Model 1, consisting of (a) female permanent individual variance ( $V_{I\varphi}$ ), (b) male permanent individual variance ( $V_{I\sigma}$ ), (c) year variance ( $V_Y$ ), and (d), variance due to unique social pairings ( $V_S$ ). Blue lines illustrate the marginal prior density (see ESMS5.1).



**Figure S2.** Marginal posterior distributions of variance component estimates from Model 2 (see figure S3 for additive genetic components), consisting of (a) female permanent individual variance ( $V_{I\text{♀}}$ ), (b) male permanent individual variance ( $V_{I\text{♂}}$ ), (c) year variance ( $V_Y$ ), and (d), variance due to unique social pairings ( $V_S$ ). See figure S1 for plot description.



**Figure S3.** Marginal posterior distributions of all additive genetic component estimates from Model 2, consisting of (a) female additive genetic variance ( $V_{A\text{♀}}$ ), (b) male additive genetic variance ( $V_{A\text{♂}}$ ), (c) the cross-sex additive genetic covariance ( $\text{COV}_{A\text{♀♂}}$ ), and (d) total additive genetic variance ( $V_{A\text{-Total}}$ ). See figure S1 for plot description and ESMS5.3 for notes about the shape of  $V_{A\text{-Total}}$ . Note different scale of x and y-axes for (c).



## Electronic Supplemental Material S5 - Alternative model results

### S5.1 Prior influence on posterior distributions

Since we had no strong *a priori* prediction regarding the magnitudes of effects on liability for divorce, we specified relatively uninformative priors. To visually inspect the influence of prior specifications on posteriors we plotted an approximate prior density on top of each plot of posterior samples. For all independent variance components, prior densities were derived by evaluating the probability density function for the *F*-distribution (section 3.6 of [13]) at each of the posterior histogram mid-points. These densities were then scaled to approximate a total area of one under the prior density curve.

For all covariances and associated variances, approximate prior densities were obtained from 10,000 random draws from the prior distribution. For the repeatabilities and heritabilities, approximate prior distributions were obtained by performing the same calculations as for the posterior with each sample of the simulated prior. A constant of one was added to the denominators for repeatability and heritability to account for the constant probit link variance that was introduced into the calculations of these values on the liability scale (see ESMS3.2). Kernel density estimation was then applied to the samples from the prior. Plot areas where posterior samples have a different shape from the prior distribution (e.g. more/less density in a tail, or less density under the mode) indicate that the posterior distribution is likely influenced by the data rather than solely by the prior.

### S5.2 Pre-1993 pedigree error due to extra-pair paternity

While extra-pair paternity before 1993 presumably introduces error into the 1975–1992 pedigree, approximately 90% of all pedigree links are likely to be correct [6,10,11]. Such error likely causes little bias in estimates of  $V_A$  [25], even if paternity error is non-random [26]. To verify this expectation, we additionally fitted Model 2 to a data subset comprising phenotypic and pedigree data starting from individuals hatched from 1993 onwards to ensure all phenotyped individuals had genetically verified parents. The restricted phenotypic data comprised 661 breeding events where divorce could have occurred during 1994–2015, containing 305 unique social pairings involving 192 females and 189 males. Divorce occurred on 92 (13.9%) occasions.

We altered the pedigree by removing all individuals with parents that were not genetically assigned, and pruned this pedigree to the restricted set of phenotyped individuals. Thus, individuals with genetically un-assigned parents, but that were the genetically assigned parents of a subsequent generation, became the founder individuals. Note that because total variance on the liability scale depends on the observed phenotypic mean (i.e., divorce rate), results are not quantitatively comparable between the full and restricted datasets. However, the pattern of variance partitioning among the different components is similar between the two models (table S1). This supports the view that pre-1993 pedigree error does not substantively bias estimates of additive genetic (co)variances. Model 1, and resulting estimates of repeatabilities, do not rely on a pedigree and so will not be affected by pedigree errors.

**Table S1:** Marginal posterior modes, means and 95% CIs of variance components from models decomposing the liability for divorce in the full dataset (main text Model 2) or data since 1993.  $V_I$  and  $V_A$  represent permanent individual and additive genetic variances for females ( $\text{♀}$ ) and males ( $\text{♂}$ ), and  $\text{COV}_{A\text{♀♂}}$  is the cross-sex genetic covariance.  $V_S$  and  $V_Y$  are the social pair and year variances, respectively.

	<b>Main text Model 2</b>		<b>Post-1993 data and pedigree Model 2</b>	
	<b>mode, mean</b>	<b>95%CI</b>	<b>mode, mean</b>	<b>95%CI</b>
<b>variance components</b>				
$V_{I\text{♀}}$	0.003, 0.22	$7 \times 10^{-7}$ , 0.48	0.003, 0.29	$2 \times 10^{-8}$ , 0.86
$V_{I\text{♂}}$	0.002, 0.08	$4 \times 10^{-8}$ , 0.25	0.002, 0.18	$1 \times 10^{-8}$ , 0.61
$V_S$	0.003, 0.15	$4 \times 10^{-8}$ , 0.48	0.004, 0.42	$2 \times 10^{-7}$ , 1.28
$V_Y$	0.001, 0.07	$8 \times 10^{-9}$ , 0.19	0.05, 0.18	$1 \times 10^{-7}$ , 0.49
$V_{A\text{♀}}$	0.001, 0.07	$5 \times 10^{-9}$ , 0.25	0.001, 0.10	$5 \times 10^{-9}$ , 0.38
$V_{A\text{♂}}$	0.001, 0.08	$4 \times 10^{-8}$ , 0.21	0.003, 0.16	$1 \times 10^{-8}$ , 0.54
$\text{COV}_{A\text{♀♂}}$	-0.0002, -0.003	-0.08, 0.06	-0.0007, -0.006	-0.14, 0.11



### S5.3 Alternative versions of Model 2: separation of sex-specific individual variances

The total number of unique social pairings, pairings per individual, number of exclusive pairings (ESMS1.2), and previous analyses of song sparrow data [9–11], support the ability of our dataset to produce unbiased estimates of female and male  $V_I$ ,  $V_A$ , and  $COV_{AS}$  in shared or emergent trait models.

In the current manuscript, the sampling correlation between  $V_{A♀}$  and  $V_{A♂}$  from Model 2 is 0.04, indicating that estimates of these two *variance components* are essentially independent of one another (the sampling covariance is a relationship between different quantities than  $COV_{A♀♂}$ ; the latter measures the covariance between random additive genetic *effects* as expressed in a female versus a male). Because variances are bounded to be greater than zero, the small sampling correlation between  $V_{A♀}$  and  $V_{A♂}$  explains why the shape of the  $T^2$  posterior differs noticeably from the shape of each of the  $V_{A♀}$  and  $V_{A♂}$  posterior distributions (figure 2, figure S3). In this circumstance, when  $V_{A♀}$  is almost zero the sampling correlation implies that  $V_{A♂}$  is likely to be relatively large, and vice versa, because  $V_{A♂}$  is bounded at zero and so can only be uncorrelated with a small value of  $V_{A♀}$  if  $V_{A♂}$  is large. As  $T^2$  is a function of the sum of  $V_{A♀}$  and  $V_{A♂}$ , posterior samples where both  $V_{A♀}$  and  $V_{A♂}$  are close to zero will be infrequent. This explains why the high density at zero for  $V_{A♀}$  and  $V_{A♂}$  does not also occur for  $T^2$  and why calculation of  $T^2$  using posterior modes/means (i.e., summary statistics of the marginal posterior distributions) does not equate to the posterior mode/mean of the calculated  $T^2$  for each sample of the posterior distributions.

The sampling correlation between  $V_{I♀}$  and  $V_{I♂}$  from Model 2 is -0.02 (Model 1 correlation: 0.0004), also indicating that estimates of these two variance components are independent from one another. Consequently, re-running Model 2 with divorce as either a female or male trait (i.e., removing  $V_A$  and  $V_I$  of the opposite sex mate in each pair) produced quantitatively similar posterior modes and means of the variance components (table S2).

Similarly, the sampling correlations between individual variances within each sex (i.e.,  $V_A$  and  $V_I$ ) is -0.23 for females and -0.14 for males. Low correlations such as these indicate that reported variance component estimates for sex-specific effects on the liability for divorce are not confounded with each other, and hence not biased by other components in the model.

**Table S2:** Marginal posterior modes, means and 95% CIs of variance components from models decomposing the liability for divorce as either a female or male trait.  $V_I$  and  $V_A$  represent permanent individual and additive genetic variances for females ( $\text{♀}$ ) and males ( $\text{♂}$ ), and  $\text{COV}_{A\text{♀}\text{♂}}$  is the cross-sex genetic covariance.  $V_S$  and  $V_Y$  are the social pair and year variances, respectively.

variance components	Model 1				Model 2			
	Female		Male		Female		Male	
	mode, mean	95%CI	mode, mean	95%CI	mode, mean	95%CI	mode, mean	95%CI
$V_{I\text{♀}}$	0.27, 0.28	$5 \times 10^{-6}$ , 0.51			0.002, 0.22	$1 \times 10^{-10}$ , 0.47		
$V_{I\text{♂}}$			0.001, 0.11	$9 \times 10^{-7}$ , 0.30			0.002, 0.10	$2 \times 10^{-6}$ , 0.30
$V_S$	0.003, 0.17	$1 \times 10^{-9}$ , 0.50	0.38, 0.37	$4 \times 10^{-7}$ , 0.74	0.004, 0.18	$4 \times 10^{-9}$ , 0.51	0.21, 0.36	$1 \times 10^{-5}$ , 0.78
$V_Y$	0.0008, 0.07	$1 \times 10^{-7}$ , 0.19	0.05, 0.09	$2 \times 10^{-6}$ , 0.22	0.001, 0.06	$2 \times 10^{-7}$ , 0.17	0.06, 0.09	$4 \times 10^{-8}$ , 0.23
$V_{A\text{♀}}$					0.001, 0.06	$3 \times 10^{-9}$ , 0.22		
$V_{A\text{♂}}$							0.001, 0.08	$8 \times 10^{-9}$ , 0.24

Similarly, we demonstrate that estimates of variance among individual repeatable effects ( $V_I$ ) are not confounded with variance among pair-level repeatable effects ( $V_S$ ) in Model 1. The sampling correlation between  $V_S$  and  $V_{I\text{♀}}$  is -0.22 and between  $V_S$  and  $V_{I\text{♂}}$  is -0.11. Results from a version of Model 1 without the social pair term ( $V_S$ ) show no appreciable change in either  $V_{I\text{♀}}$  or  $V_{I\text{♂}}$  (table S3). In this model, the marginal posterior distribution of  $V_{I\text{♀}}$  no longer converges towards zero, suggesting the slightly higher sampling correlation of  $V_{I\text{♀}}$  with  $V_S$ , compared to  $V_{I\text{♂}}$  and  $V_S$ , has a small effect on the precision of  $V_{I\text{♀}}$ . However, the posterior modes and means remained similar, implying that our estimates of female and male permanent individual effects, and hence repeatability, are robust.

**Table S3:** Marginal posterior modes, means and 95% CIs of variance components from models decomposing the liability for divorce with the full Model 1 or from a model with social pair variance ( $V_S$ ).  $V_I$  represents permanent individual variances for females ( $\text{♀}$ ) and males ( $\text{♂}$ ) and  $V_Y$  is the year variance.

variance components	Model 1		Model 1 Without $V_S$	
	mode, mean	95%CI	mode, mean	95%CI
$V_{I\text{♀}}$	0.24, 0.28	$4 \times 10^{-6}$ , 0.53	0.25, 0.30	0.065, 0.56
$V_{I\text{♂}}$	0.001, 0.09	$5 \times 10^{-8}$ , 0.26	0.001, 0.10	$2.23 \times 10^{-8}$ , 0.29
$V_S$	0.001, 0.14	$2 \times 10^{-9}$ , 0.46		
$V_Y$	0.001, 0.07	$4 \times 10^{-7}$ , 0.19	0.001, 0.06	$7 \times 10^{-11}$ , 0.16

#### S5.4 Null Simulations of Model 2

To further support our inference from Model 2 that liability for divorce exhibits small but likely non-zero sex-specific and total heritability, we conducted a Monte Carlo simulation to estimate key parameters from data where  $V_{A\text{♀}}$  and  $V_{A\text{♂}}$  in liability for divorce are zero.

For each of 50 replicates, we randomly sampled the observed incidences of divorce versus mate-fidelity without replacement, and replaced each observed value in our dataset with the randomised values. We thereby retained the observed divorce rate, and did not change the total variance to be partitioned.

We then fitted the Model 2 structure to each of the 50 resampled datasets exactly as for the real dataset, retaining the same random and fixed effects structures. The posterior mean sex-specific additive genetic variances and heritabilities, and the total heritability ( $T^2$ ), were computed for each replicate, and the grand mean and standard deviation of these posterior means was calculated across the 50 replicates.

Across the simulated null datasets, the grand mean posterior mean sex-specific  $V_A$  and  $h^2$ , and the total heritability ( $T^2$ ), in liability for divorce were all smaller than the posterior mean values estimated given the real data (Table S4). The difference frequently exceeded two standard deviations, providing strong evidence that the estimates from the real data differ from those generated by the null simulations (even though, as expected given the intrinsically zero-bounded and right-skewed posterior distributions, the null posterior means were not zero). Consequently, we conclude that the posterior means estimated from the real data indicate that the sex-specific  $V_A$  and  $h^2$ , and  $T^2$ , in liability for divorce are small but most likely greater than zero.

**Table S4:** Marginal posterior means from Model 2 fitted to the real data and the mean (and one standard deviation, SD) of the posterior means across 50 null simulations in which the occurrence of divorce was randomly sampled.  $V_A$  represents additive genetic variances for females ( $\text{♀}$ ) and males ( $\text{♂}$ ).  $\text{COV}_{A\text{♀♂}}$  is the cross-sex genetic covariance. Results for sex-specific heritabilities ( $h^2$ ) and ‘total heritability’ ( $T^2$ ) are also shown.

	<b>Real data mean</b>	<b>‘Null simulation’ mean (SD)</b>
<b>variance components</b>		
$V_{A\text{♀}}$	0.07	0.023 (0.013)
$V_{A\text{♂}}$	0.08	0.020 (0.009)
$\text{COV}_{A\text{♀♂}}$	-0.003	$4 \times 10^{-5}$ (0.001)
<b>variance ratios</b>		
$h^2_{\text{♀}}$	0.04	0.020 (0.010)
$h^2_{\text{♂}}$	0.04	0.017 (0.007)
$T^2$	0.08	0.036 (0.013)

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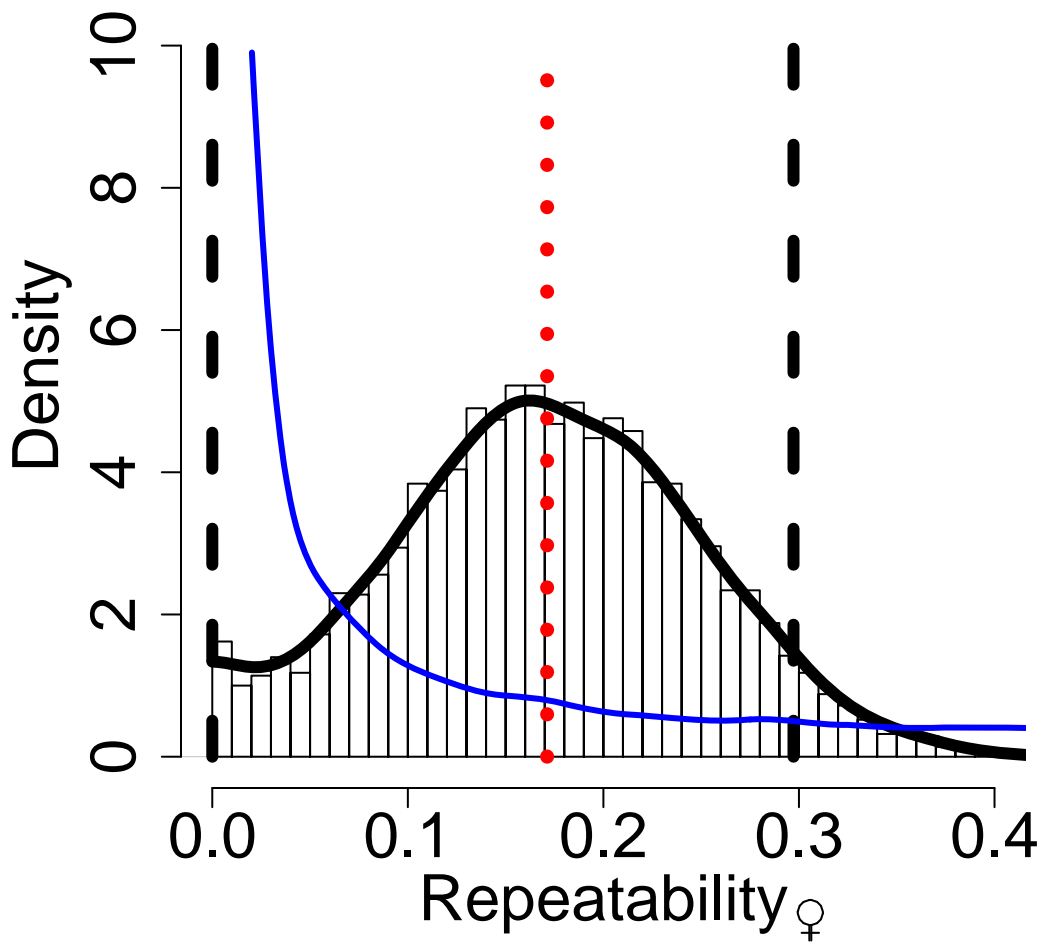
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(a)



(b)

