

Notch effect on strength of components at elevated temperature under creep, fatigue and creep-fatigue loading conditions: phenomenon, and mechanism

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Abstract

Structural discontinuities (e.g. nozzle, hole, groove, etc) are widely existed in many high temperature components of nuclear and fossil power plants. In general, the notched component is employed for simplified tests and analyses due to the complexity of the introduction of a practical component. In previous works, the effects of the notch on failure life of the components have been reported experimentally, including the strengthening and weakening effects, but so far, the internal mechanisms have not been clearly demonstrated. Based on this, this work mainly reviews the notch effects on the structural strength of the notched components at elevated temperatures under creep, fatigue and creep-fatigue loading conditions. Experimental phenomenon about the notch effects (i.e. strengthening or weakening effects) for typical notched specimens subjected to the above three loading conditions are summarized, and related factors to notch effects on creep rupture life or cycle to failure of the components are discussed. The mechanisms for the strengthening or weakening effects induced by a notch are described. Evaluation procedures for notch effect analysis under complex loading conditions are also discussed. Main challenges about the notch effect analyses are provided for further investigations.

Keywords: notch effect, high temperature, creep, fatigue, creep-fatigue, review

1 Introduction

Structural discontinuities (e.g. nozzle, hole, groove, etc) are widely existed in many high temperature components of nuclear and fossil power plants. They are usually the main cause of the structural failure due to the complex stress and strain distributions around these local zones [1, 2]. In general, the notched component is employed for simplified tests and analyses due to the complexity of the introduction of a practical component. A notched component with various geometrical parameters can cause different multi-axial stress states around the notch root and then result in the change of the stress and strain behavior, as well as the failure life, of the component. Thus, it is crucial and necessary to investigate the effect of notch on structural behavior of high temperature components. Considering these components are usually exposed to a high temperature/pressure and cyclic loadings induced by the startup, steady operation and shutdown of the system, so creep, fatigue and creep-fatigue interaction are three potential failure modes, which will be included for analyses in this work.

In fact, the notch effects on structural responses of high temperature components originate from the multi-axial stress state induced by a notch. It should be noted that the multi-axial stress state induced by a notch for notched components (Type-A components, see Fig. 1a) is different from that of bi-axially loaded plates or tubes subjected to internal pressure and axial loadings (Type-B components, see Fig. 1b). Regarding notched components, the multi-axial stress state and the complex stress gradient across the notch section can be observed, while only the uniform multi-axial stress state exists and the stress gradient can be neglected or does not exist for Type-B components. When representing the effect of the stress state, the data of the Type-B component is compared with that of the smooth specimen with the same equivalent stress, while Type-A component is based on the smooth specimen under the same nominal stress across the notch section. Therefore, it can be expected that the structural behavior for components with a notch under creep, fatigue and creep-fatigue loading conditions could be different from that subjected to the uniform multi-axial stress

state.

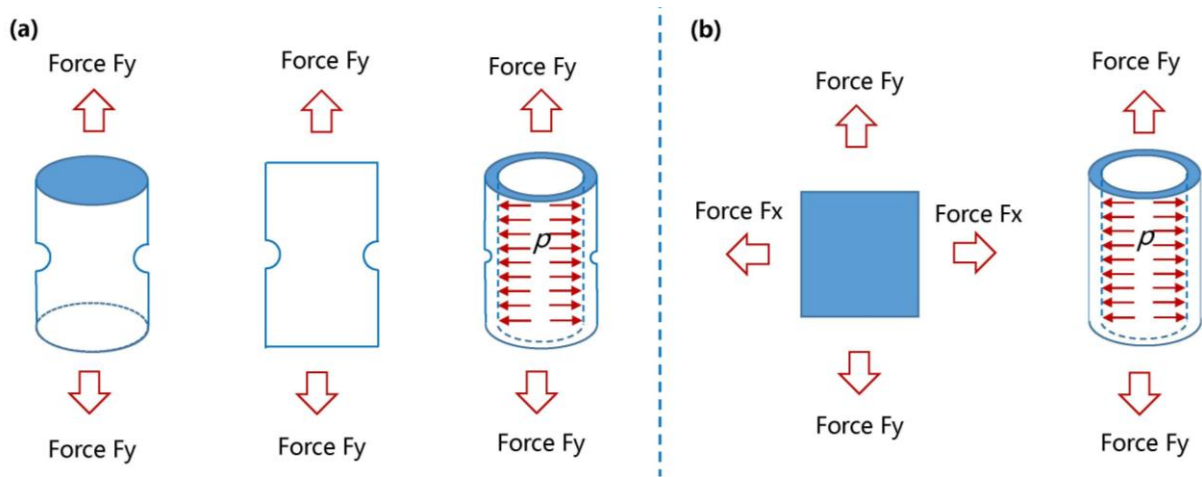


Fig. 1 The current creep, fatigue and creep-fatigue test specimens in published works: (a) Type-A components, (b) Type-B components

In general, the multi-axial stress effects can be analyzed from two aspects: one is on the stress and strain responses, and the other is on the failure life. These two aspects will be included in following.

Regarding the creep condition, the uniform multi-axial stress state of Type-B components can cause a smaller multi-axial creep fracture strain and a premature fracture of the component compared with the smooth specimen with the uni-axial stress state (see Fig. 2b). For Type-A components, as shown in Fig. 2a, a smaller multi-axial creep fracture strain can also be found due to the constraint effects around the notch region, but the creep failure life of notched components may be higher or lower than that of the smooth specimen, dependent on the geometry, material ductility, and so on. It should be noted that the average strain across the notch areas of the notched components (see Fig. 2a) is taken for comparisons, which is much smaller than that of the smooth specimen.

Regarding the fatigue loading, the uniform multi-axial stress state of Type-B components can induce the change of the stress and strain responses(see Fig. 3b), as well as the decrease of the fatigue failure cycle due to the larger energy loss per cycle. It should be stated that the hysteresis loop would be more complex when the non-proportional cyclic loadings are introduced. For Type-A components, displayed in Fig. 3a, the stress and strain

responses are based on the data across the notch region, which are smaller than that of the smooth specimens due to the smaller structural response adjacent to the notch root. However, the fatigue failure cycle of Type-A components is usually smaller than that of the smooth specimen due to the remarkable stress and strain concentration around the notch root of the component.

When the creep-fatigue loading condition is mentioned for analyses, the creep and fatigue actions interact with each other, and the combining actions determine the stress and strain behavior of components, as well as the structural strength of the components. The strengthening or the weakening effects are related to many factors, such as the loading parameters, geometrical parameters, and so on.

As a whole, in this work, the notch effect on failure life of the component is of the main concern, and the notched components (i.e. Type-A components) are chosen for analyses.

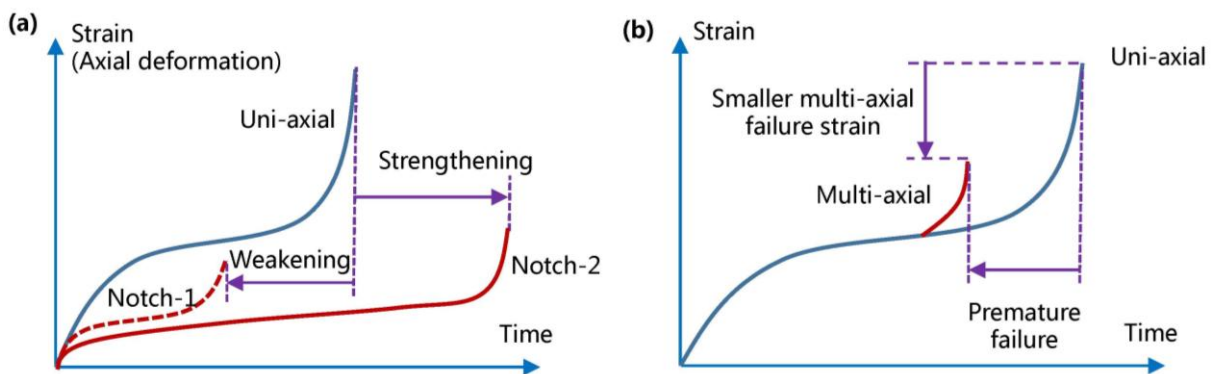


Fig. 2 Effect of stress state on creep deformation evolution behavior: (a) Type-A components, (b) Type-B components

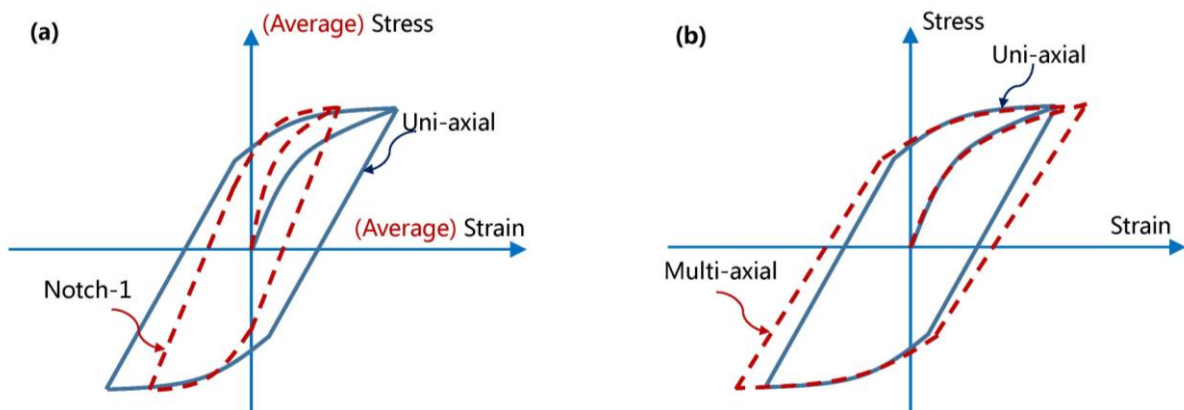


Fig. 3 Effect of stress state on fatigue stress-strain loop behavior: (a) Type-A components, (b)
Type-B components

So far, many experimental results about the notch effect of components under the complex loading conditions (i.e. creep, fatigue, and creep-fatigue) have been reported, including the strengthening and weakening effects. However, the internal mechanism of such notch effects on failure life of the components under various loading conditions is still not clearly described. Therefore, this work is to conduct a review over the notch effect on structural strength of the notched component under the complex loading conditions and then to discuss the mechanism for notch strengthening or weakening effects. Meanwhile, related analysis methods for notch effect evaluations of the notched components at elevated temperatures are included.

The structure of the paper is arranged as follows: Firstly, the representation of the notch effect on failure life of components is given in Section 2. Then, notch effects on failure life of the components under creep conditions and fatigue loadings are provided in Sections 3 and 4, respectively. Later, Section 5 reports the notch effect on structural strength of components at elevated temperature under creep-fatigue loading conditions. Finally, concluding remarks are provided in Section 6.

2 Representation of notch effect on failure life of components

To describe the notch effect on the failure life of components quantitatively, the previous notch effect descriptions for creep, fatigue and creep-fatigue loading conditions are firstly reviewed.

Regarding creep conditions, several representations of the notch effect on structural strength of components have been proposed. For example, Hayhurst et al. [3] defined the normalized representative rupture stress when investigating the notch effect under creep conditions, shown as Eq. (1).

$$\alpha_r = \frac{\sigma_r}{\sigma_n} \quad (1)$$

where, α_r is the normalized representative rupture stress; σ_r is the creep stress for smooth specimen which has the same life as the notched specimen; σ_n is the average stress at the net section. If the equivalent un-axial stress σ_r is lower than the average stress σ_n , the notch presents a strengthening effect. Otherwise, the notch has a weakening effect. Later, Nix et al. [4] proposed a more intuitive quantity, called notch effect factor (NEF), expressed as Eq. (2), i.e. the inverse of Eq. (1).

$$\alpha = \frac{\sigma_n}{\sigma_r} \quad (2)$$

where, α is notch effect factor. The notch has a strengthening effect if the coefficient α is larger than 1, while a weakening effect is observed for the coefficient α smaller than 1. Then, some researchers define the ratio of creep rupture life of notched specimen to plain specimen as notch effect factor [5], shown as Eq. (3).

$$\alpha = \frac{t_{\text{notch}}}{t_{\text{smooth}}} \quad (3)$$

where, t_{notch} and t_{smooth} are the creep rupture lives for notched and smooth specimens. Similarly, the strengthening effect can be concluded if the creep rupture life of the notched component is higher than that of the smooth specimen.

Regarding fatigue loadings, the cycles to failure for notched specimens are always compared with that of the smooth specimen, implying that the notch effect factor can be represented by the equation like Eq. (3) and the creep rupture life should be replaced by the cycle to failure. Similarly, when the creep-fatigue loading conditions are considered, the cycle to failure is usually adopted to define the notch effect factor. Therefore, for notch effect factor under fatigue or creep-fatigue conditions, the cycle to failure can be employed to define the notch effect on structural strength of the notched components.

As mentioned above, the notch effect factor can be represented by stress-based

variables or creep rupture life for creep conditions, or by the cycle to failure for fatigue/creep-fatigue loadings. Considering that the creep rupture life for creep conditions and the cycle to failure for fatigue/creep-fatigue loadings are the structural strength of components under a specific loading, so the notch effect coefficient η between the strength of the notched component (N_{notch}) and that of the smooth specimen (N_{smooth}) is introduced to indicate the notch effect on structural strength of the component, shown as Eq. (4).

$$\eta = \frac{N_{\text{notch}}}{N_{\text{smooth}}} \quad (4)$$

where, η is the notch effect coefficient, defined as the strength ratio of the notched component to smooth specimen. It should be noted that the strength herein means cycles to failure for fatigue/creep-fatigue loadings and creep rupture life for creep conditions. A strengthening effect is observed for notch effect coefficient η larger than 1.0, while it means a weakening effect for the coefficient η smaller than 1.0.

3 Notch effect of components under creep conditions

3.1 Notch effect and related factors

Notch effects of the components under creep conditions have been reported in many published works [5-20], where the strengthening and weakening effects are both mentioned. Among these works, they are all based on the assumption that the net stress at the notch plane of the notched component is the same as that of the smooth specimen. Experimental results demonstrate that the notch effect on creep rupture life of the notched component is related to notch shape, notch acuity ratio, material ductility, stress level and so on.

3.1.1 Notch shape and notch acuity ratio

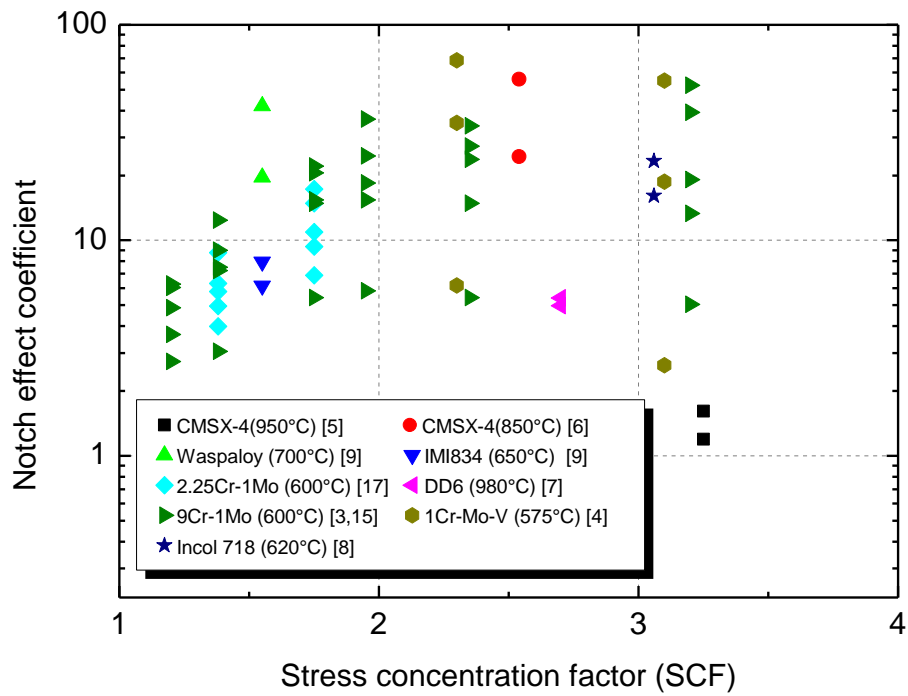
Notch shape determines the multi-axial stress state around the notch root and directly affects the creep rupture life of the notched components. Many experimental studies have stated that the notch presents a strengthening effect for C/U/V-shape notched bars and double-edge notched plates for many creep ductile materials (e.g. 9Cr-1Mo [5, 17],

2.25Cr-1Mo[19], 1CrMoV[6], CMSX-4[7, 8], DD6[9], Inconel 718[10], IMI834[11], 316[12], 316LN[13], 12CrWCoB[14]). In other words, the notched components have a longer creep rupture life than the smooth specimens when the same nominal stress or average stress is applied. Moreover, the creep rupture life of the notched component remarkably increases with the notch acuity ratio. However, it displays a weakening effect for plate/bar specimens with a circular hole or a slot [12], as shown in Fig. 4.

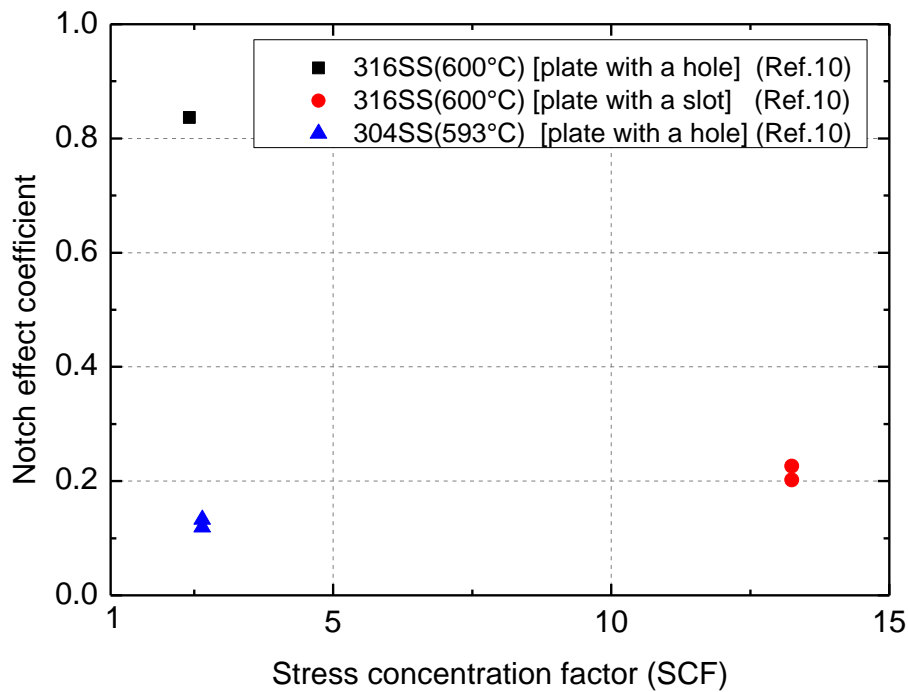
The damage evolution behaviors of notched bars under creep conditions have been discussed based on continuum damage mechanics (CDM). As concluded in Ref. [20], the creep damage evolution behavior can be ascribed to the combining action of the equivalent stress and the stress tri-axiality of the components. The results present that the notched component has a lower equivalent stress than the nominal stress for the smooth specimen, which plays a more remarkable role on creep rupture life than the stress tri-axiality. This is why the notched component presents a longer creep rupture life than the smooth one, indicating a notch strengthening effect. In addition, numerical results revealed that the location with the maximum creep damage shifts from the notch root to the interior regions during the creep process for creep ductile materials. This is verified by the experimental investigations that inner cracks are initiated at several hundred micro-meters from the notch root (see Fig. 5), demonstrating that the creep rupture behavior of the notched specimens are not only controlled by the equivalent stress, but also the stress tri-axiality of the components.

Regarding plate specimens with a hole, preliminary results [21] have demonstrated that the maximum creep damage is located at the corner angle perpendicular to the applied loadings and the critical damage value (e.g. 0.99) is firstly reached at this location. This is quite different from that for notched bars under creep conditions. There is a remarkable stress relaxation for notched bars during the whole creep process, while this does not occur for plate specimens with a hole, remaining a relatively high stress level during the creep stage. Therefore, the notch bar is prone to indicate a strengthening effect due to a smaller

equivalent stress even with a relatively high stress tri-axiality, while, for plate specimens with a hole, the weakening effect happens due to a remarkable local stress concentration, which is much higher than the net section stress at the minimum section.

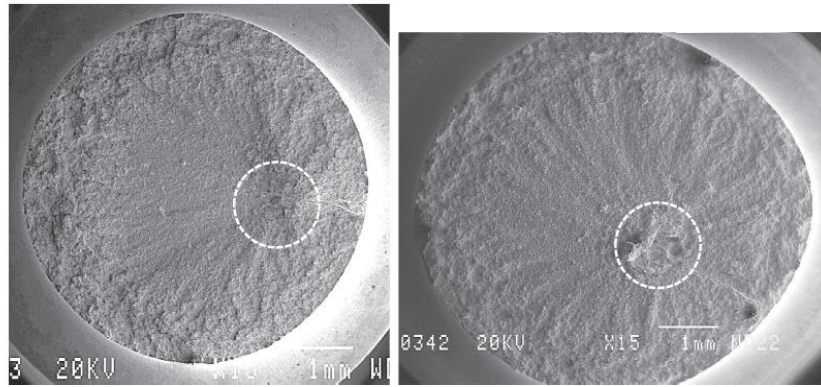


(a) Cases for strengthening behavior



(b) Cases for weakening behavior

Fig. 4 Notch effect of high temperature components under creep conditions



(a) Case A

(b) Case B

Fig. 5 Failure of notch rupture specimens tested at 793 MPa resulted from internal initiations similar to cyclic max dwell notch low cycle fatigue specimens [22]

3.1.2 Material ductility

The notch effect on creep rupture life of the component is also dependent on the material ductility. As reported in Ref. [5], the notch is more likely to present a strengthening effect for creep ductile materials, while it is prone to manifest a weakening effect for creep brittle materials due to the failure caused by the local accumulated strain exceeding a limit value before attaining the stationary state across the notch throat section. Meanwhile, the effect of creep ductility on creep rupture behavior of the notched bars is discussed based on CDM in Ref. [20], where the strengthening and weakening effects under different creep ductility are both reported. It is found that the strengthening effect is more likely to occur for materials with high creep ductility, while the weakening effect is expected to happen for materials with small creep ductility. The strengthening or weakening mechanisms can be explained as follows. Compared with the smooth component, at the beginning of the creep process, the maximum creep damage is located at the notch root due to a high equivalent stress and a relatively high stress triaxility, and the creep ductility exhausted within the same time is higher for a notched component than that for a smooth specimen. However, with the increasing creep time, the maximum damage point shifts from the notch root to the interior regions and the creep damage is not as large as that for a smooth specimen. Therefore, if the creep

ductility of the material is high enough, then the strengthening effect caused by the notch is expected to present. Otherwise, the notch is likely to display a weakening effect for materials with small creep ductility. It should be noted that the above conclusion is mainly limited to notched bars with a hoop notch (e.g. C/U/V-shape).

When plate specimens with a hole are taken for analysis, the notch effect does not present similar creep behavior as that of the notched bars. Based on the analyses given in Section 3.1.1, it can be predicted that the weakening effect is more likely to happen due to the remarkable stress/strain concentration around the hole, independent on the material types (i.e. creep ductile or brittle materials).

3.1.3 Stress level

Stress level is another factor affecting the notch effect of the components under creep conditions. Many tests of the notched bar specimens, reported in Section 3.1.1, also present that the strengthening effect can be detected for a wide stress level, ranging from the stress lower than the yield stress to that higher than the yield stress. It should be noted that the above conclusion is mainly limited to the bar specimens with a hoop notch or double-edge notched plates. In addition, creep material ductility is always the stress-related, so the strengthening effect at a high stress level (with a high creep material ductility) may change to a weakening effect for a relatively small stress (with a small creep material ductility). Numerical studies are conducted in Ref. [20], where the stress-related creep ductility of the material is adopted.

For plate specimens with a hole, the hole has a weakening effect for the stress level involved. Moreover, different from the conclusion obtained for notched bars, the change from a weakening effect to a strengthening effect probably does not occur. The main cause for the weakening effect is due to the local stress/strain concentration around the hole of the plate, and the steady stress cannot be lower than the average stress around the hole. Thus, the weakening effect should be dominant for a wide stress level.

3.2 Related models for notch effect on creep strength of components

As described above, the notch presents strengthening or weakening effects, dependent on the creep ductility, notch shape, applied stress, temperature and so on. Based on the understanding of the phenomenon about the notch effect under creep conditions, the mechanism behavior behind the phenomenon should be established.

As a whole, there are three typical analysis strategies on evaluations of the notch strengthening or weakening effects. Firstly, we can extract the representative stress at the skeletal point and combines the material parameters, and the representative stress of the notched component can be determined. Based on this, the strengthening or weakening effects caused by the notch can be evaluated. Secondly, the continuum damage mechanics has been adopted for assessing the creep rupture life of the notched components, including the classical K-R creep damage equations, the strain exhaustion concept and so on. Later, the strengthening or weakening effects can be found. Finally, there are some analytical methods describing the effective stress of the notched component, and then the creep rupture life of the component can be identified. Based on the creep rupture life determined, the notch effect on creep rupture life of the notched component can be found. In following, the above three analysis strategies about the mechanism of the notch effect will be discussed in detail.

3.2.1 Representative stress and skeletal point concept

In this section, the evolution behavior of the representative stress is firstly reviewed. Then, the strengthening or weakening effects of the notched components will be discussed.

In general, multi-axial creep rupture is mainly governed by several stress variables: maximum principal stress, hydrostatic stress and von Mises stress. Many studies have pointed out that the creep deformation and creep cavity nucleation processes are mainly controlled by von Mises stress, while the maximum principal and hydrostatic stress have a significant effect on the continuum cavity growth. Meanwhile, the maximum principal stress

is also responsible for the intergranular cavity growth [4]. To reflect the effect of multi-axial stress, many representative stress models have been introduced, which includes the relative contribution of above stress components [23].

The early study about the multi-axial stress state under creep conditions and the corresponding representative stress model can be tracked to 1950s, where the creep test of pure copper under bi-axial loadings was reported by Johnson et al. [24]. In their work, the representative stress is mainly based on the maximum principle stress and the material constant A in Norton equation is a function of three stress invariants, expressed as Eq. (5).

$$t = f(J_1, J_2, J_3) \sigma_1^{-\chi} \quad (5)$$

where, t is creep rupture life, J_1 , J_2 and J_3 are the first, second and third stress invariants, σ_1 is the maximum principle stress, χ is the stress exponent. Later, in 1958, Sdobyrev [25] used thin-walled tubular sections to produce the biaxial deformation and rupture life, and he proposed a revised model for representative stress description, shown as Eq. (6):

$$\sigma_r = \lambda \sigma_1 + (1 - \lambda) J_2^{1/2} \quad (6)$$

where, J_2 is the second deviatoric stress invariant, λ is contribution coefficient. It can be found that the representative stress is a combination of the maximum principle stress and the second deviatoric stress invariant with different contribution factors. Hayhurst and his-coworkers [26] developed a new model of the representative stress based on the creep rupture life of the cruciform bi-axial plate specimen, which covers the contribution of the maximum principle stress, the first stress invariant and the second deviatoric stress invariant, displayed as Eq. (7).

$$\sigma_r = \alpha \sigma_1 + \beta J_1 + \gamma J_2^{1/2} \quad (7)$$

where, α , β and γ are the contribution coefficients for the maximum principle stress, the first stress invariant and the second deviatoric stress invariant, respectively. It can be observed that Eq. (7) is derived from Eq. (6) with the inclusion of the first stress invariant and can be simplified as Eq. (6) when the contribution factor β equals to zero. Then, Hayhurst and Leckie

[27] found that the maximum principal stress and the effective stress are much more important than the hydrostatic stress in determining multi-axial creep rupture. Thus, the contribution coefficient β in Eq. (7) is assumed as zero and the second deviatoric stress invariant is transformed as equivalent stress. Then, the above representative stress (Eq. (7)) is modified as Eq. (8):

$$\sigma_r = \alpha\sigma_1 + (1-\alpha)\sigma_e \quad (8)$$

where, σ_e is the equivalent stress. Later, Cane [28] discussed the mechanism of the formation and growth of cavities and it was found that the controlling factors are mainly attributed to the maximum principle stress, and the ratio between the maximum principle stress and the equivalent stress. Then, a model for representative stress was provided, shown as Eq. (9).

$$\sigma_r = \sigma_1^p \sigma_e^{(1-p)} \quad (9)$$

where, p is the contribution coefficient for maximum principle stress. Also, Huddleston [29] provided an improved multi-axial creep strength criterion based on the further development of the work of Cane [28], which incorporates three independent stress parameters, shown as Eq. (10).

$$\sigma_r = \frac{3}{2} S_1 \left(\frac{2\sigma_e}{3S_1} \right)^a \exp \left[b \left(\frac{J_1}{S_s} \right) - 1 \right] \quad (10)$$

where, S_1 is the maximum deviatoric stress, J_1 is the sum of three principle stresses, S_s is an invariant stress parameter, a and b are material constants. The bi-axial creep data of 304SS at 593°C are taken for the validation of the proposed criteria. It should be noted that this model has been adopted by the ASME III-NH standard for creep damage evaluations based on the inelastic analysis with a slight modification (suppose parameter $a=1.0$). As a whole, the above models are mainly limited to creep rupture life of the specimens under bi-axial stress states (e.g. cruciform biaxial plates or thin-walled tubes with torsion loadings), while the complex tri-axial stress state around the notch root of the bars are not included. The main differences of two stress states (e.g. bi-axial plates and tri-axial notched bars) are as

follows: For notched bars, the stress state around the notch root or across the notch plane is not uniformly distributed, which is quite different from that of the cruciform bi-axial plates, which have the same stress state for any node at the specimens. Therefore, the representative stress model reported for specimens subjected to bi-axial stress state is likely not adequate to describe the tri-axial stress state (e.g. the stress state around the root of notched bars).

With the further development of the representative stress model, the tri-axial creep rupture data (e.g. notched bars) are mentioned to formulate a more general description. For example, Nix et al [4] proposed a modified formulation of the representative stress, shown as Eq. (11), which is based on the stress redistribution associated with grain boundary sliding and is expected to be valid for alloys that exhibit grain boundary sliding and fail by cavitation of grain boundaries perpendicular to the maximum principal stress.

$$\sigma_r = 2.24\sigma_1 - 0.62(\sigma_2 + \sigma_3) \quad (11)$$

where, σ_2 and σ_3 are the second and third principle stresses, respectively. This model has been validated by the creep data of cruciform biaxial plates and notched bars reported by Hayhurst et al. [3], Cane [30], Stanzl et al. [31], Dyson and Mclean [32], and so on. It should be noted that the stress adopted for evaluations for are mainly based on the node at the center of the notch plane. Further investigations by Kraus [33] presented that for symmetric shapes and simple loading conditions (e.g. constant tension, pressure or bending), a point exists in the cross-section of the notch plane where the stress remains unchanged during the creep process. Al-Faddagh et al. [34] conducted some numerical studies on the creep behavior of the notched bars and also reported that there is a region with approximately constant effective stress, which is also independent of the stress index n . Moreover, an approximate method was established for estimating the maximum equivalent steady-state stress across the notch throat. Similar works are also made by Hayhurst and his co-workers [35]. With the further development of the skeletal point stress, the skeletal point stress for a

variety of notch geometries have been analyzed and a code of practice for notched bar testing was formulated initially in 1991 [36] and updated in 2004 [23]. Based on the standard established, many experimental results are conducted to demonstrate the applicability of the representative stress at the skeletal point and good consistency is also observed. For example, Goyal et al. [5, 17, 19] conducted the creep tests of the notched bars made of 9Cr-1Mo steel and 2.25Cr-1Mo steel at high temperatures. The observed creep rupture data are employed to characterize the multi-axial creep life based on the skeletal point concept (see Fig. 8) and three representative stress models are included for analyses, such as the model of Hayhurst et al. [26], Cane [30] and Nix et al. [4], all indicating an adequate solution.

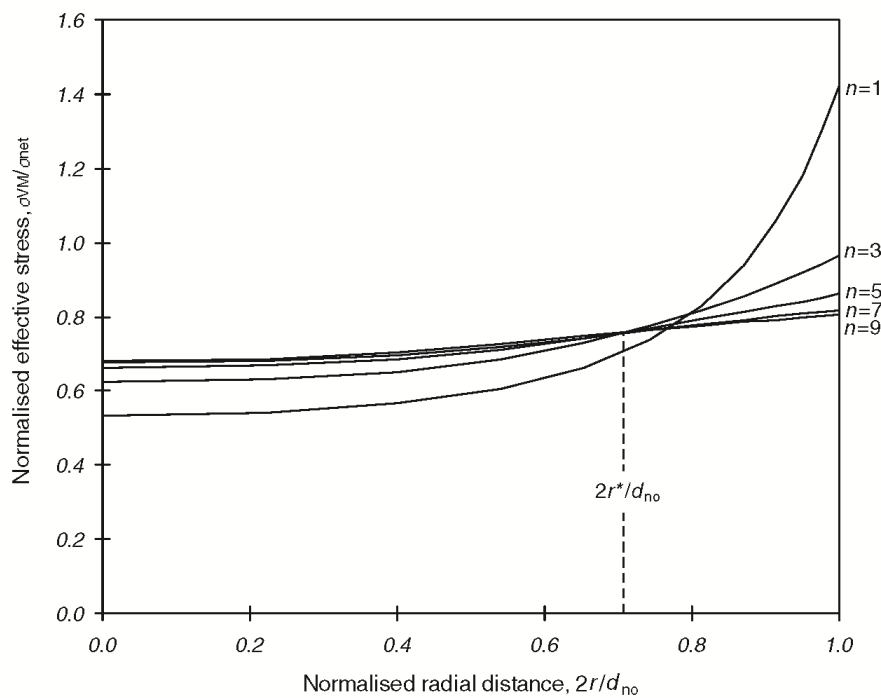


Fig. 6 Normalized effective stress distribution at steady state across the throat of a semi-circular notch [23]

The above description mainly includes the evolution behavior of the representative stress, and the skeletal point concept is also mentioned for analyses. Based on the above equation describing the representative stress, the characteristic equivalent stress of the notched component can be found. Then, the creep rupture life of the notched component can be calculated and the notch effect on creep rupture life of the component can be

evaluated. Taking the equation by Hayhurst et al as an example, the maximum principle stress and the equivalent stress at the skeletal point can be determined. Then, the representative stress of the component can be gained using the material parameter. At this time, if the representative stress is higher than the average stress for the smooth specimen, then the weakening effect is prone to happen. Otherwise, the strengthening effect can occur if the representative stress is smaller than the average stress for the smooth specimen.

3.2.2 Methods based on continuum damage mechanics (CDM)

Yao et al. [37] reviewed the creep analysis and design methods for components under multi-axial stress states. Meanwhile, they divided the existing theories and creep design approaches into three categories, including the classical plastic theory (CPT) based approach, the cavity growth mechanism (CGM) based approach and the continuum damage mechanics (CDM) based approach. For CDM-based damage models, in general, these models mainly originate from the work of Kachnaov [38], Rabotnov [39], Lemaitre [40] and so on. It should be noted that the representative stress concept mentioned in Section 3.2.1 can also be coupled with CDM analysis, such as the work of Hayhurst et al. [3], Hyde et al. [10, 11], Liu and Murakami [41], Jiang et al. [42, 43], Goyal et al. [5, 17, 19], Zhang et al. [44], and so on. Numerical results presented that the critical creep damage of the notched component is highly related to the notch shapes, stress levels, et al. Exactly speaking, for a relatively shallow notch, the critical creep damage is located at the zone inside the notch tip, while it is nearly around the notch root for a relatively sharp notch. Moreover, the predicted creep rupture lives of the notched components are also consistent with the experimental results, but the specific solution accuracy is dependent on the material studied. For example, the error band of the predicted creep rupture life of the notched component is within a factor of 1.1 for GH3536 [44] and it is 3.0 for 9Cr-1Mo steel [5, 17].

The above mentioned damage constitutive equations are mainly limited to stress-based damage models. The main disadvantage of these models is that many material equations

are introduced in these damage models, and great efforts should be made to the determination of these parameters, causing a big barrier for engineering applications of the above models. Based on this, the strain-based damage model (e.g. ductility exhaustion concept) has been included for creep damage evolution analysis of the components at elevated temperatures due to the simplicity of the model with fewer material parameters, which was adopted since the work of Yatomi et al. [45, 46]. Recently, similar work about the notch effect on creep rupture life of the component was also conducted by Xu et al. [20], where the Cock-Ashby model was also employed to describe the relationship between the uniaxial creep fracture strain and multi-axial creep fracture strain. It was concluded that for creep ductile materials, the creep rupture life of the notched component is determined by the combining action of the equivalent stress and stress tri-axiality. At the beginning of the creep process, the equivalent stress presents a remarkable stress relaxation, and the corresponding stress tri-axiality is higher than that of the smooth specimen. Meanwhile, with the further increase of creep process, the equivalent stress remains a low stress level and the equivalent stress plays an important role on creep strain rate or creep damage rate of the notched component. This is why the creep strain rate (i.e. creep damage rate) is smaller than that for the smooth specimen. Numerical results may present strengthening and weakening effects for various geometrical, material types, loading conditions, and so on. Meanwhile, the critical creep damage is mainly located at the zone inside the notch root for creep ductile material, which is consistent with the experimental results provided in Fig. 5.

3.2.3 Analytical methods

Some analytical equations between the effective stress and the geometrical parameters, as well as the correlation of the creep rupture life and the notch parameter, are mentioned. For example, Dyson and Loveday [47] conducted notched specimens of Nimonic 80A with a Bridgman geometry at 750°C using a wide stress range (154-600MPa). The strengthening behavior was clearly observed and the Bridgman effective stress [48] was taken as the

representative stress, shown as Eq. (12). This method was also considered for a qualitative comparison in Ref. [22].

$$\sigma_{\text{eff}} = \sigma_{\text{net}} \left[\left(1 + \frac{2R}{a} \right) \ln \left(1 + \frac{a}{2R} \right) \right]^{-1} = \sigma_{\text{net}} f \left(\frac{a}{2R} \right) \quad (12)$$

where, σ_{eff} is the effective stress, σ_{net} is the net section stress, a is the distance from the center of the specimen to the notch root and R is defined as the radius of the notch. It should be stated that this analytical equation can only be adopted to analyze the strengthening effects and this is because the factor $f \left(\frac{a}{2R} \right)$ in Eq. (12) has a value smaller than 1.0, shown as Fig. 7. When the weakening effects of the notched components are reported, the above analytical strategy is no longer available.

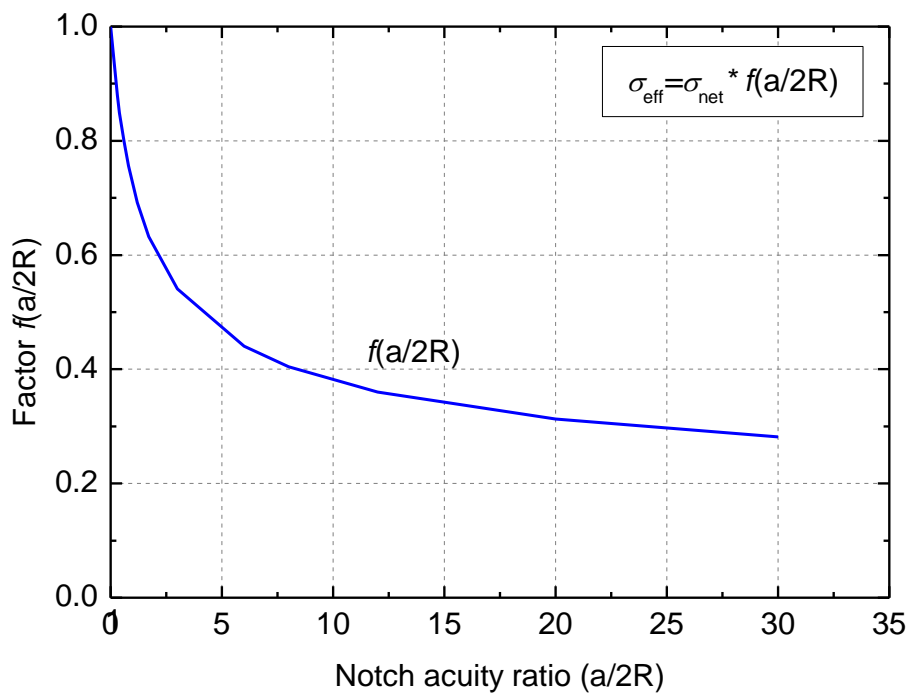


Fig. 7 Relationship between the factor $f(a/2R)$ for Bridgman effective stress and notch acuity ratio of notched components

4 Notch effect of components under fatigue loadings

4.1 Notch effect and related factors

In general, the experimental studies on the notched components under fatigue loadings

are mainly divided into two controlled modes: stress-controlled and strain-controlled modes. In following, the notch effect of the components under these two controlled modes will be provided.

4.1.1 Stress-controlled mode

For stress-controlled mode, notch effects of the components under low cycle fatigue loadings at elevated temperatures have been discussed [49-62]. Among these cases studies, many kinds of specimens are taken for analyses, such as notched bar specimens, single-edge or double-edge notched plates, plate component with a hole, and so on. It is always assumed that the net section stress of the notched component is the same as that of a smooth specimen. Through experimental investigations reported, in general, the notched component has a shorter cycle to failure than a smooth component, meaning that the notch has a weakening effect (see Fig. 8). Meanwhile, it is found that the weakening effect is much more remarkable for specimens with a high stress concentration factor (SCF) than that with a small SCF. The main reason for the weakening effect is that the surface crack is easily initiated at the notch root of the notched components due to a high local stress/strain at the notch root. With the development of the optical technology, it makes in situ viewing of the fatigue crack initiation possible by taking a telephoto lens microscope combined with a video camera [49, 51, 63]. Experimental results demonstrate that fatigue crack is initiated around the notch root for the notched plates and bars, or at the edge of the hole for plates with a hole, further supporting the above understandings.

The effect of the stress level on notch effect on cycle to failure of the component is also shown in Fig. 8. It should be noted that the detailed stress levels are not marked in the figure, but they are all based on a certain specimen (corresponding to a stress concentration factor), implying they have the same horizontal axis for a given specimen made of a certain material in Fig. 8. It can be found that the extent of the notch weakening effect is closely related to the stress level applied. Similar conclusion about the effect of the temperature on notch effect

can be obtained based on the experimental results in Ref. [52]. It should be noted that these two factors usually do not alter the notch effect on cycle to failure of the component from weakening effect to strengthening effect.

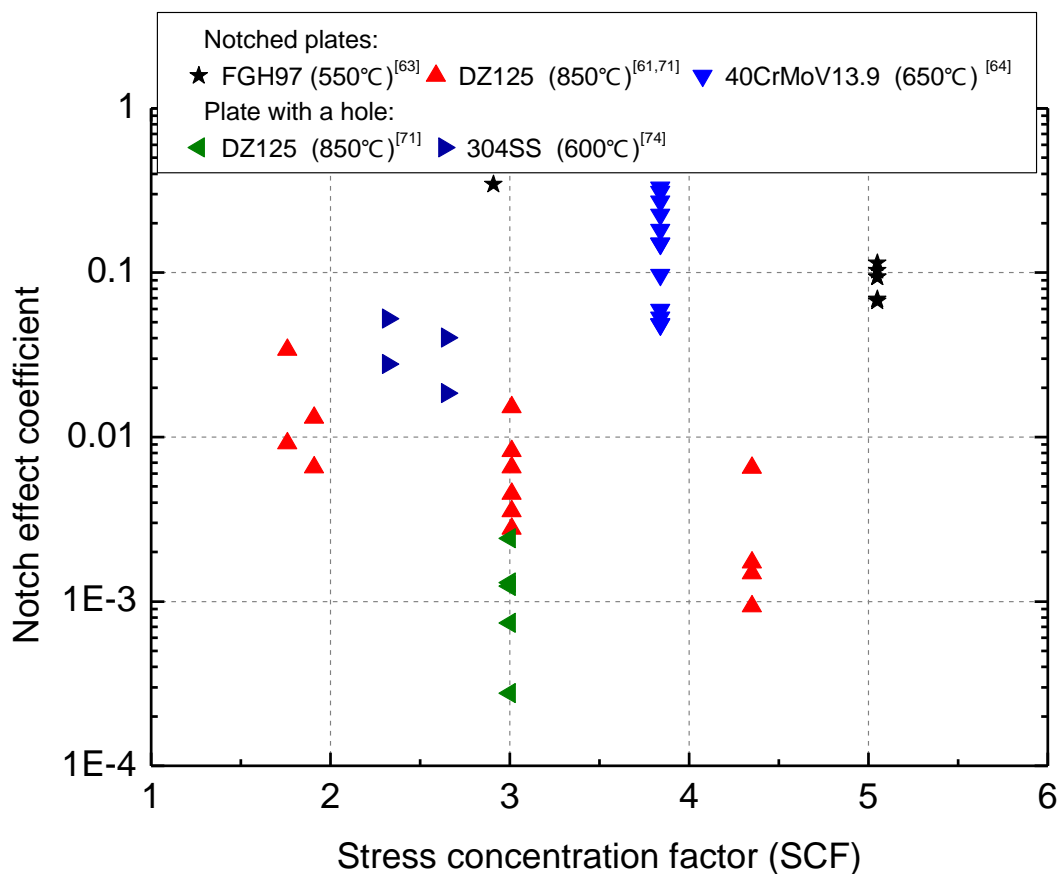


Fig. 8 Notch effect of high temperature components under stress-controlled fatigue loadings

In addition, the effect of the stress ratio on notch effect may be different from that of the stress level and temperature, which may alter the notch effect from weakening effect to the strengthening effect with the increasing stress ratio. This is mainly because with the increase of the stress ratio, a relatively large average stress may induce an evident creep contribution during the cyclic process according to the numerical results obtained in Ref. [1]. Thus, the strengthening effect caused by the notch can probably be detected for fatigue loadings with a high stress ratio. It should be noted that the above description is only limited to notched bars (with a hoop notch) or single-edge/double-edge notched plates, while the plates with a hole do not present such behavior. This is mainly because the hole causes a weakening effect even under pure creep conditions and the stress ratio does not cause the change from

notch weakening effect to notch strengthening effect.

4.1.2 Strain-controlled mode

For strain-controlled mode, notch effects of the components under low cycle fatigue loadings at elevated temperatures have been discussed [63, 64]. It is always assumed that the applied strain imposed to a notched specimen is the same as that to a smooth component for strain controlled mode, which is different from the assumption for stress-controlled mode. Under this circumstance, it can be expected that the local stress and strain around the notch root is much higher than the applied strain (equals to that for smooth specimens). Experimental investigations also indicate that the notched component has a shorter cycle to failure than a smooth component, implying a weakening effect (see Fig. 9). Moreover, components with a higher SCF can induce a more remarkable reduction of fatigue strength. Similar to that under stress-controlled mode, the main cause for the weakening effect is that the surface crack is easily initiated at the notch root due to a high local stress/strain at these zones. For plate specimens with a hole, the experimental results under strain controlled mode are relatively rarely reported. Even so, it can be expected that the hole present a weakening effect due to the prominent stress and strain concentration around the edge of the hole.

As reported in Section 4.1.1, it is stated that for a relatively high stress ratio, the notch may indicate a strengthening effect under fatigue loadings. However, this phenomenon is difficult to occur for component under strain-controlled mode. The current experimental study about the strain-controlled mode is mainly based on the assumption that the applied strain for smooth and notched specimens is the same, equivalent to the same external loadings. With the increase of the stress ratio, the creep contribution caused by the average stress gets remarkable. However, the notched and smooth components still sustain the same external loadings and the weakening effect can be gained even under pure creep conditions, which is quite different from the conclusion for stress-controlled mode in Section 4.1.1.

4.2 Related models for notch effect on fatigue strength of components

4.2.1 Methods for applications at room temperature

In current studies, the notch effect has been included when conducting the multi-axial fatigue strength evaluation of the notched component, especially at room temperature. Many methods have been proposed for multi-axial fatigue strength representation by researchers. In general, the current methods can be divided into several classes: (1) One is the classical method aiming to establish the description of the effective stress of the notched component. The typical approaches are listed below: local stress/strain approach (LSSA), stress gradient approach (SGA), normal stress approach (NSA), stress field intensity approach (SFIA) [65], critical distance approach (CDA) [66, 67], critical plane approach (CPA) [68], critical volume approach (CVA) [69], and so on. (2) The second is to evaluate the fatigue life of the notched component by the strain-based variables, such as the equivalent strain range, maximum principle strain, maximum shear strain, and so on. (3) The third is based on energy approach (EA) [70]. Among these methods, some have been successfully adopted for the fatigue life evaluation of the notched component, and even engineering structures, indicating a reasonable prediction solution.

4.2.2 Methods for applications at high temperature

For notched components at elevated temperature, the notch effect representation has been discussed by some researchers when investigating the notch effect made of various materials. As a whole, many experimental results have demonstrated that multiply cracks initiate at the surface of the notch. Meanwhile, the process of the fatigue crack initiation and propagation can be real-time recorded. Researchers come to conclude that the location of the fatigue crack initiation is some distance away from the notch root. For example, Moore et al. [61, 71] discussed the notch fatigue behavior of the directionally solidified (DS) superalloy CM247LC at 750°C and 950°C. It was concluded that the crack initiation is not located at the notch root, which is consistent with the maximum Hill's stress. Later, Shi et al. [49] discussed

the effect of notch types and stress concentration factor on low cycle fatigue life and cracking of DS superalloy DZ125. It was also found that the cracking does not occur at the notch apex but at the location where the maximum principal stress or Hill's stress is the highest. Similar results are also reported in Refs. [51, 53, 63], and isotropic materials (e.g. 304SS in Ref. [63]) are also mentioned. In addition, for the thermomechanical fatigue behavior, it was also reported that the fatigue crack offsets from the notch root [72, 73]. It should be noted that for the fatigue crack propagation, in general, the fatigue crack turned to the plane perpendicular to the loading direction. Meanwhile, as reported in Ref. [49], the fatigue crack path is dependent on the stress concentration factor: it presents a zigzag line for components with a small SCF, while the straight crack propagation can be detected for a high stress concentration factor.

To accurately predict the fatigue life of the notched component, several models have been proposed. For instance, Domas and Antolovich [74] provided an approach to predict the fatigue life of the notched component based on hysteresis loop energy. Many fatigue data were adopted to validate the proposed model, but results presented that limited data can be correlated correctly. Leidermark et al. [75] discussed the fatigue life of the components in presence of notches using a critical plane approach combined with a critical distance concept and it seemed that the simulated results are consistent with the experimental results. Berto et al. [52] studied the stress-controlled fatigue tests on smooth and notched specimens made of 40CrMoV13.9 steel. Meanwhile, fatigue data from un-notched and notched specimens are re-analyzed by means of the mean value of the strain energy density (SED), presenting a reasonable solution. Also, stress relaxation locus (SRL) method is taken for the prediction of the strain range and the cycle number, and it is concluded that the SRL method with a coefficient of 1.6 can provide a reasonable prediction [63, 64]. Based on the stress-strain behavior of the material in the notch, Filippini [53] proposed a fatigue damage parameter (the maximum range of resolved shear stress on the

crystallographic planes), which allows the transferability of tests results from plain specimen data to notched specimen data. Later, Huang et al. [59] developed a simple unified critical plane damage parameter (i.e., the modified resolved shear strain range) based on a slip mechanism-related critical plane concept, where the critical plane is determined as the slip plane on which the damage parameter is the maximum during the cycle. The predicted results also demonstrated that the proposed critical plane damage parameter can provide a reasonable solution, where the material orientation, temperature, loading ratio and notch shapes are also included. In addition, Karolczuk and Macha [76] reviewed the multiaxial fatigue failure criteria based on the critical plane concept, which are divided into three groups (i.e. (i) stress, (ii) strain and (iii) strain energy density criteria), according to the fatigue damage parameter used in the criterion. As a whole, the above models have been successfully employed for the life prediction of the notched components (at least for cases studied), but the applicability of these models to other cases or materials still needs more investigations. Therefore, a generalized life prediction model under multi-axial fatigue loadings is necessary and crucial. Moreover, the solution of the model is another challenge for a reasonable description of the notched components under cyclic loadings.

5 Notch effect of components under creep-fatigue loadings

Considering that the notch effects on notched components under creep-fatigue loading conditions with stress and strain controlled modes are different from each other, so in following, the stress and strain-controlled modes are discussed separately.

5.1 Stress-controlled mode

In previous studies, creep-fatigue tests of notched components under stress-controlled creep-fatigue loading conditions have been reported [22, 60, 77-80], where the strengthening and weakening effects are both mentioned. As a whole, the notch effect is closely related to material ductility (ductile or brittle materials), loading parameters, and so on.

5.1.1 Ductile materials

For ductile materials, as described in Sections 3 and 4, some consistent conclusions about notch effect have been drawn for components under creep conditions or fatigue loadings only. Taking the notched bar specimens with a circumferential C/U/V-shape notch for example, the notch usually presents a strengthening effect under creep conditions only, but it indicates a weakening effect for notched structures under fatigue loadings only. For notch effect under creep-fatigue loading conditions, however, the notch strengthening and weakening effects are both reported, such as the work of Sakane et al. [77], where they analyzed the frequency and hold-time effects on stress-controlled low cycle fatigue for notched bar specimens made of SS304. Further investigations about their experimental results (see Fig. 9) demonstrate that the notch effect is closely related to holding time. The weakening effect is observed for a small holding time (e.g. 0.0056h), while it changes to strengthening effect when the holding time is long enough (e.g. 0.27h and 2.77h). The above phenomenon can also be explained by Fig. 10. When the holding time is zero, the creep-fatigue loading is just fatigue loading and the notch presents a weakening effect, while it changes to the creep spectrum with an infinite long holding time, and the notch strengthening effect is observed. For creep-fatigue conditions, however, the notch effect is dependent on the holding time and it is concluded that the difference could be ascribed to the creep damage contribution in the holding stage [1]. Meanwhile, the stress concentration factor (SCF), stress ratio, and the maximum stress are all included in Ref. [1] and the results indicated that the influences of the above factors are strongly dependent on the competition of creep and fatigue mechanism.

As described in Section 3, it is found that the critical creep damage is located at the place inside the notch tip for components with a relatively shallow notch, while the fatigue crack can be more easily formed at the notch root. Thus, for the creep-fatigue loadings, the maximum damage should be located at the zone between the two above critical locations. Recently,

experimental investigations in Ref. [22] displayed that the primary initiation site is internal at a substantial distance away from the notch root for the air and vacuum tested cyclic max dwell fatigue tests, as shown in Fig. 11. The location of the primary failure origin away from the notch root is attributed to visco-plastic stress redistribution controlling the damage evolution process. Meanwhile, a single small secondary surface initiation region was also found for cases mentioned (see Fig. 11). Similar experimental results are also observed in Ref. [6], where the experimental studies on the notched bar specimens of a low alloy steel are conducted. In their work, the SEM results of the notched bar specimens after fracture manifested that micro damages (e.g. small creep cracks) are mainly observed around several hundred micro-meters below the surface.

It should be noted that the above conclusions are mainly limited to notched components with a hoop notch, and may be applied to single-edge or double-edge plates. For plate specimens with a hole, limited experimental studies under stress-controlled creep-fatigue loading conditions are reported [60]. In general, as concluded in Sections 3 and 4, the hole indicates a weakening effect for creep conditions for ductile materials, and also presents a weakening effect when fatigue loading conditions are considered. Thus, it can be expected that the hole always presents a weakening effect for creep-fatigue loading conditions (see Fig. 10). The experimental results in Ref. [60] also support this point, where the plate with a hole made of DZ125 superalloy at 850 °C under creep-fatigue loading conditions is tested.

5.1.2 Brittle materials

For notched components made of brittle materials, related works are rarely published. When creep conditions (one extreme condition of creep-fatigue loadings) are considered only, the notch usually presents a weakening effect. This is because the stress re-distribution of the notched component is relatively slow and the local accumulated strain exceeds the limit required for fracture before attaining the stationary state across the notch throat plane [5, 17, 19]. The numerical results of Ref. [20] also support that the weakening effect can be detected

for material with relatively small creep ductility. For the other extreme condition, fatigue loadings, the crack initiation is easier at the notch root and the crack propagation rate is faster, and then a notch weakening effect is expected. For cases under creep-fatigue loadings, considering that the creep conditions and fatigue loadings are two extreme cases of creep-fatigue loadings, it can be expected that a notch still presents a weakening effect by analogy to ductile materials shown in Fig. 10. Surely, further experimental validation for the notch effect evaluation is also needed for an intuitive demonstration.

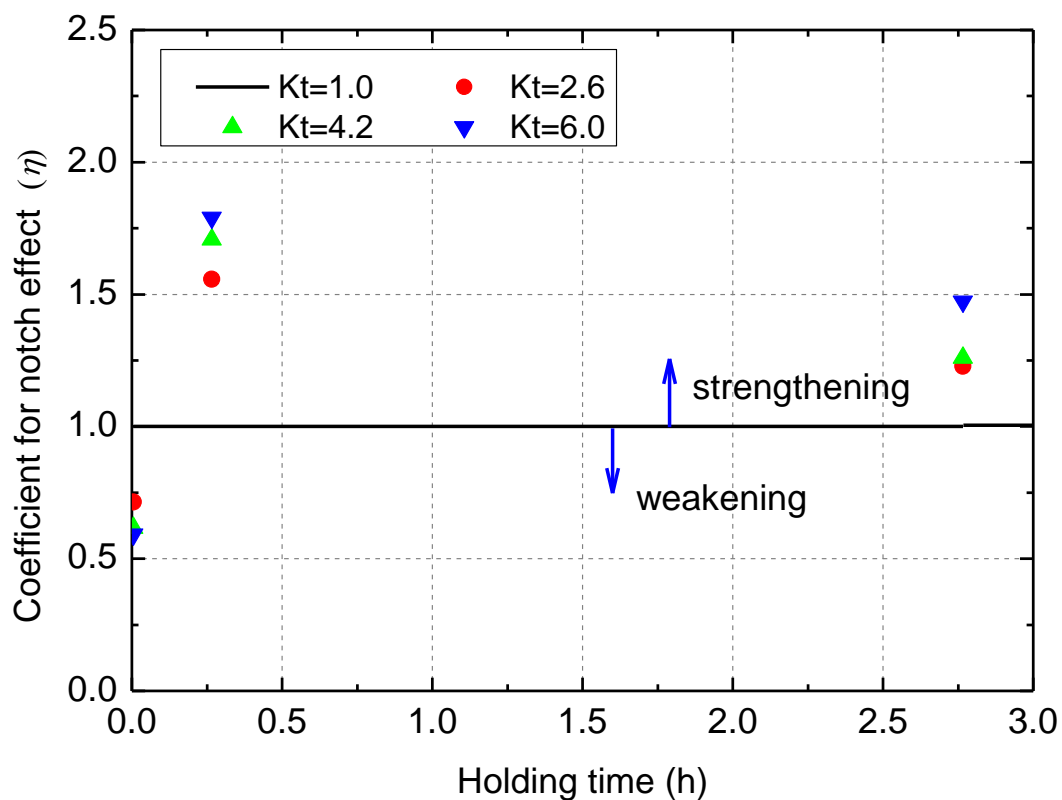


Fig. 9 Weakening and strengthening behavior of notches under the creep-fatigue condition in terms of the of Ref. [77] ([1])

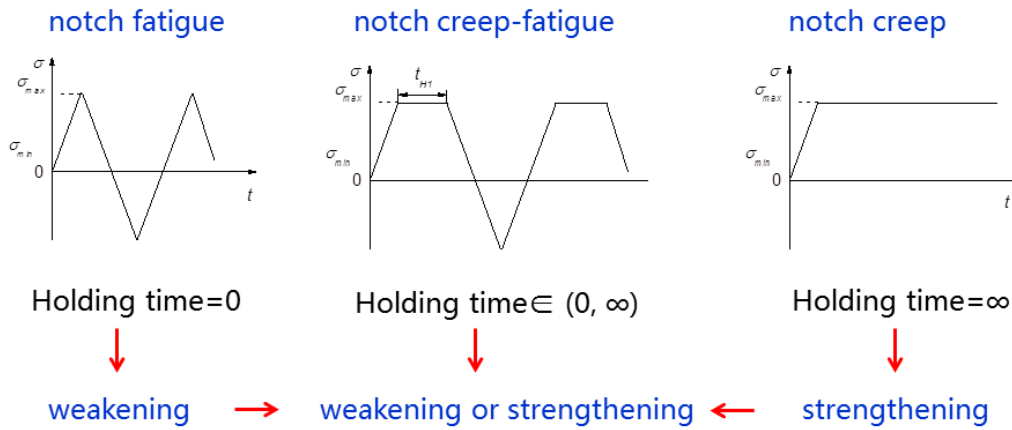


Fig. 10 Schematic diagram of notch effect under creep/fatigue/creep-fatigue conditions [1]

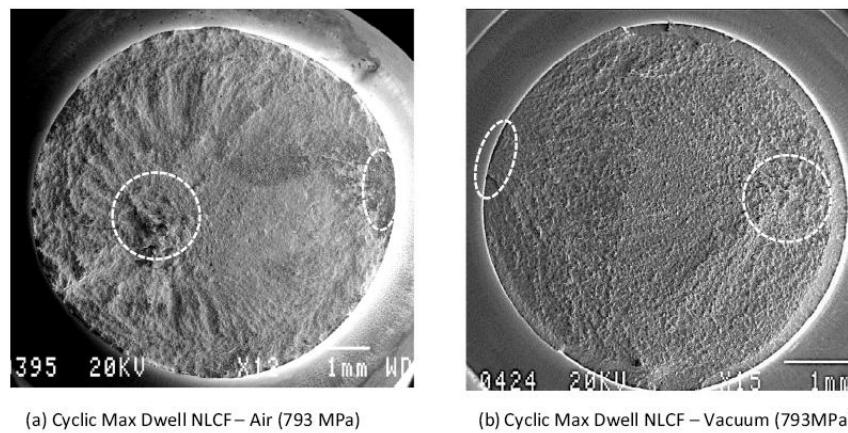


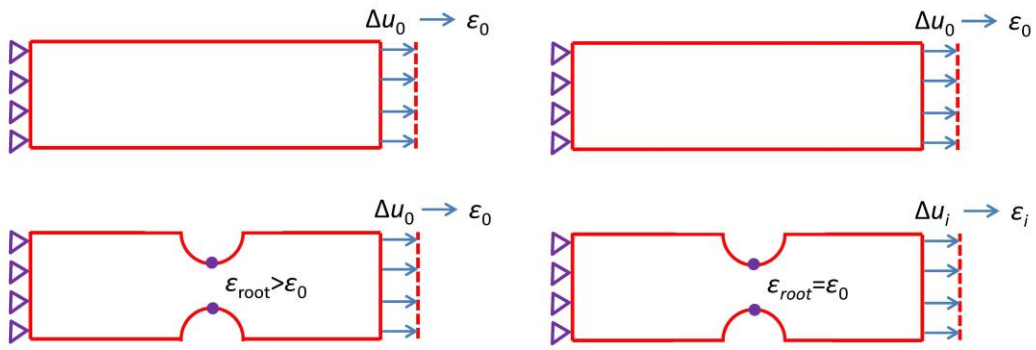
Fig. 11 Comparison of failure modes and dwell fatigue lives for air and vacuum tested cyclic max dwell notch low cycle fatigue specimens tested at 793 MPa [22]

It should be noted that the current work about the notch effect under stress-controlled mode is mainly limited to tensile holding time only, while the compressive holding time is rarely considered. Some experimental studies have focused on the creep-fatigue behavior of the notched components. For example, Telesman et al. conducted the study about the effect of notches on creep-fatigue behavior of a P/M nickel-based superalloy, and the results presented that the compressive holding time can cause an even more detrimental effect on creep-fatigue strength of components than that with a tensile holding time. In general, it is thought that the compressive holding time can induce a closure effect of the crack and then prevent the rate of the crack propagation. The conclusion obtained is quite different from the general understanding of the effect caused by the compressive holding time. The mechanism

of the above phenomenon is ascribed to the remarkable oxidation behavior during the compressive holding stage. Considering that the link between the oxidation behavior and mechanics-based variables is quite complex and is not clearly established, it is not easy to discuss the representation of notch effect currently and much work is still needed for future studies.

5.2 Strain-controlled mode

For notched bar specimens, strain-controlled creep-fatigue experimental studies on the notched bar components are reported [71, 81-86]. For stress-controlled mode mentioned above, the uniform stress at the notch plane is kept as the same as that of the smooth specimens. Different from that for stress-controlled mode, the application of the strain can be divided into two methods (see Fig. 12): The first method is to directly apply the same strain for a notched component as that for a smooth specimen (see Fig. 12a). At this moment, the strain at the notch root for a notched component is higher than that for a smooth specimen. References [81, 82] have demonstrated that the notch weakening effect is clearly observed for the cases mentioned. Moreover, in general, the notch weakening effect is more remarkable for a large stress concentration factor than that for a small stress concentration factor (see Fig. 13). The opposite behavior is also found by Nozaki et al. (see Fig. 13), but the possible reason may be due to the limited specimens conducted in their experimental studies. The second method is to keep the maximum strain around the notch root as a constant for components with various elastic stress concentration factors (see Fig. 12b), and the applied strain can be determined by detailed finite element analysis. Experimental results of Refs. [83-85] have displayed that the notch presents a strengthening effect and the strengthening effect is more remarkable with the increasing elastic stress concentration factor (see Fig. 13).



(a) Notch effect for the same loadings (b) Notch effect for the same strain

Fig. 12 Two possible conditions for notch effect of notched components under creep-fatigue loading conditions

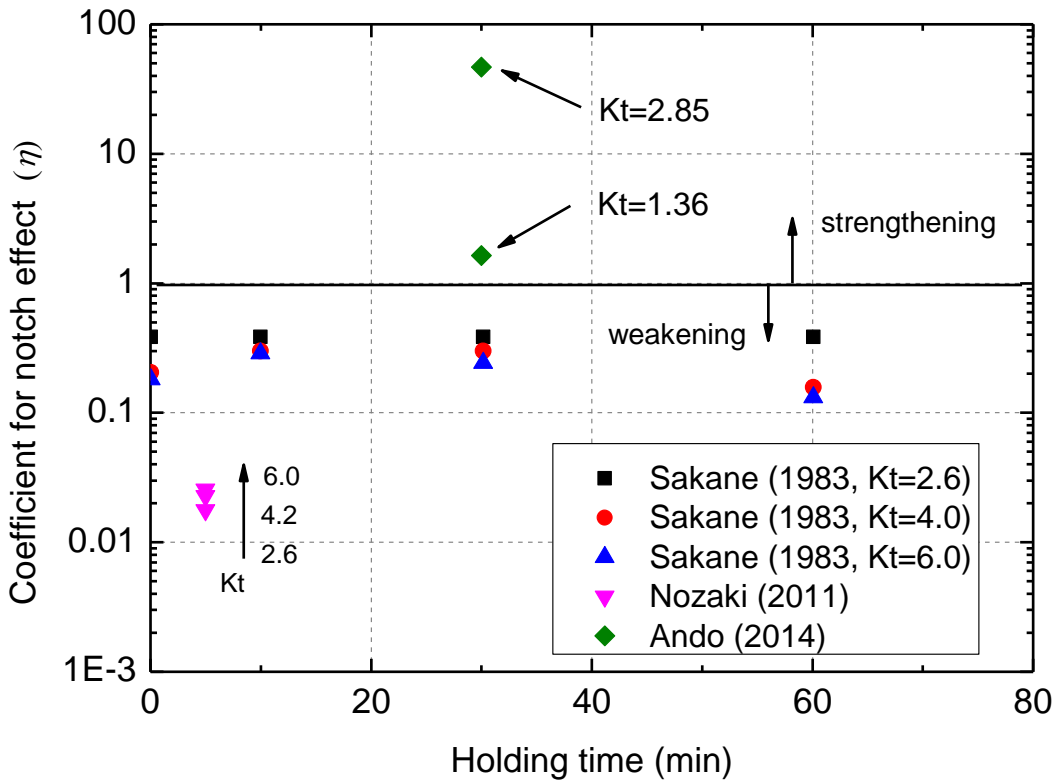


Fig. 13 Weakening and strengthening behavior of notches under the strain-controlled creep-fatigue condition in terms of Refs. [81-83]

For plate specimens with a hole, the experimental tests are usually based on the loading condition of Fig. 12a. As mentioned in Section 5.1, the hole usually indicates a weakening effect for ductile or brittle materials due to the remarkable stress/strain concentration around the hole. This rule is also applicable to specimens with a hole under strain controlled creep-fatigue loading conditions. This is because the stress around the hole

can approach to the uniform stress state for a smooth specimen due to the remarkable stress relaxation around the hole during the holding stage, but it is still higher than that for a smooth specimen. Therefore, it can be expected that the weakening effect can be observed for specimens with a hole subjected to creep-fatigue loading conditions. In addition, there are other experimental studies over the creep-fatigue behavior of the notched component under strain controlled creep-fatigue loading conditions [64, 87-89]. However, the experimental results of the notched components are only provided and that of the smooth specimens are not reported, so it is difficult to conduct a notch effect evaluation.

5.3 Notch effect evaluation under creep-fatigue loading conditions

To evaluate the notch effect of the notched components under creep-fatigue loading conditions, the allowable cycles to failure for smooth and notched specimens should be identified, meaning that the evaluation procedure for creep and fatigue damage should be chosen firstly. There are several methods for notch effect study of the components under creep-fatigue loadings, such as the procedures in some international standards (e.g. ASME III-NH [90], R5 [91]), the revised procedure based on ASME III-NH [1], and so on.

5.3.1 Main evaluation procedures

Some international standards have provided the creep and fatigue damage evaluation procedures for components under creep-fatigue loadings, such as ASME III-NH, R5, and so on. These standards are based on the time fraction model, but the creep damage evaluation procedures recommended in these standards have some remarkable differences. Exactly speaking, in ASME III-NH, the creep damage is defined as the ratio of the holding time to the allowable creep rupture life, which is evaluated by the effective stress for inelastic analysis (see Eq. (13)). In addition, fatigue damage is evaluated by the maximum equivalent strain range (see Eq. (14)).

$$\sigma_{\text{eff}} = \sigma_{\text{vm}} \exp \left[C \left(\frac{\sigma_1 + \sigma_2 + \sigma_3}{[\sigma_1^2 + \sigma_2^2 + \sigma_3^2]^{1/2}} - 1 \right) \right] \quad (13)$$

$$\Delta \varepsilon_{\text{equiv},i} = \frac{\sqrt{2}}{2(1+\nu^*)} \left[(\Delta \varepsilon_{xi} - \Delta \varepsilon_{yi})^2 + (\Delta \varepsilon_{yi} - \Delta \varepsilon_{zi})^2 + (\Delta \varepsilon_{zi} - \Delta \varepsilon_{xi})^2 + \frac{3}{2} (\Delta \gamma_{xyi}^2 + \Delta \gamma_{yzi}^2 + \Delta \gamma_{zxi}^2) \right]^{1/2} \quad (14)$$

where, σ_{eff} is the effective stress; σ_{vm} is the equivalent von Mises stress; C is a material constant; $\Delta \varepsilon_{\text{equiv},i}$ is the equivalent von Mises strain range for time point i ; $\Delta \varepsilon_{xi}$, $\Delta \varepsilon_{yi}$, $\Delta \varepsilon_{zi}$, $\Delta \gamma_{xyi}$, $\Delta \gamma_{yzi}$, $\Delta \gamma_{zxi}$ are the corresponding differences of the six strain variables for each point in time i ; ν^* is the Poisson's ratio and equals to 0.5 for inelastic analysis. However, in R5 standard, the creep damage is based on the ductility exhaustion concept, shown as Eq. (15)

$$D_c = \int_0^{t_0} \frac{\dot{\varepsilon}}{\varepsilon_f} dt \quad (15)$$

where, $\dot{\varepsilon}$ is the strain rate for a certain moment; ε_f is the creep ductility for a certain stress state, which can be identified by Cock-Ashby, or other models, transforming the multi-axial creep ductility to uniaxial ones. Based on the creep and fatigue damage per cycle, as well as the damage evaluation criteria, one can determine the allowable cycles to failure (N_{notch} and N_{smooth}) of the notched and smooth components, marked as the life of the notched and smooth specimens. Then, the notch effect can be identified using the ratio of the two.

Besides, Gong and Xuan [1] proposed another damage evaluation procedure when conducting the notch effect analysis of the notched bar specimens based on the procedure of ASME III-NH, where the creep damage is evaluated by the representative stress at the skeletal point but the fatigue damage is still based on the maximum equivalent strain range.

5.3.2 Applications for notch effect evaluation

For notched components with a circumferential notch, the procedure in ASME III-NH has been adopted for notch effect analysis [1]. Numerical results demonstrated that the current creep damage evaluation cannot describe the strengthening effect for notched component under creep conditions. Based on the existing problem, Gong and Xuan [1] proposed a revised method for creep damage evaluation based on the Hayhurst's representative stress of skeletal point instead of the effective stress in ASME III-NH, and the fatigue damage is still

based on the equivalent strain described in ASME III-NH. Results presented that the revised method is adequate to discuss the notch effect for components under creep-fatigue conditions. The notch presents a weakening effect for a small holding time, while it displays a strengthening effect for a long holding time. These conclusions are consistent with the experimental results in Ref. [77]. It should be noted that the above description is mainly focused on the bar specimens with a hoop notch. When the single-edge or double-edge plate specimens are mentioned, it is expected that they present a similar notch effect behavior to bar specimens with a hoop notch.

For components with a hole, the damage behavior is quite different from that of the notched components with a hoop notch. Therefore, how to discuss the creep and fatigue damage is a main challenge. For creep damage, continuum damage mechanics (CDM) method has been adopted to identify the damage behavior during the whole creep process [21]. Results presented that the maximum creep damage is always located at the corner angle perpendicular to the loading axis, which is also higher than the damage for the smooth specimen. This indicates that the notch or the hole has a weakening effect on the structural strength of the component. For fatigue damage, it is also based on the maximum equivalent strain range in ASME III-NH and the weakening effect is observed, consistent with general conclusions in Section 3. As a whole, the weakening effect can be expected for specimens with a hole under creep-fatigue conditions.

It should be stated that although the above methods could provide a basic notch effect analysis, the notch effect factor calculated is not very consistent with the experimental results. Thus, further analyses on notch effect evaluation are still needed, including the creep and fatigue damage evaluation procedures. Moreover, the creep-fatigue interaction may introduce difficulties for exact evaluation and should be mentioned in future investigations.

6 Concluding remarks

This work mainly reviews the experimental and numerical studies on notch effect of high temperature components under creep, fatigue and creep-fatigue loading conditions. Some progresses have been achieved over the notch effect analysis and evaluation for notched components under the above loading conditions. The strengthening and weakening effects are both observed for components under creep conditions, which are related to the notch shape, material ductility, stress level, and so on. For specimens subjected to fatigue loadings, the weakening effect is mainly found due to the remarkable stress/strain concentration around the notch root or the hole. When the creep-fatigue loading conditions are mentioned, the notch effect is dependent on the controlling mode, material ductility, notch shape, and so on. As a whole, the complex mechanisms of the notch effect have been stated for components under creep, fatigue and creep-fatigue loading conditions, which are also consistent with experimental results. It should be noted that there are still some questions needing further investigations, which are listed below:

(1) The notched component is a basic structural component for further investigating the engineering components under complex loading conditions. The current notch strengthening and weakening effects have been reported and analyzed, but only some of these conclusions can be applicable to engineering components. This is because it is difficult to define the similar reference cross-section to the notched component, and accordingly the methods developed by notched components could not be employed directly for engineering cases. In the future, a general method is still needed for the accurate description of the failure life of the practical components. Surely, the importance of the notched component could not be replaced due to its simple geometry and they are important structural cases for experimental validations.

(2) Although the procedure for notch effect analysis has been established for notched component under creep, fatigue and creep-fatigue loading conditions, the notch effect

coefficient is still not very consistent with the experimental results. This means that the current creep/fatigue damage evaluation procedures may not evaluate the corresponding damage exactly. Thus, much attention should be paid to the improvement and development of the current life evaluations of the notched components.

(3) For creep-fatigue loading conditions, notch effect is closely related to material ductility, loadings parameters, geometrical parameters, etc. Among these factors, various materials and geometrical parameters are included, but the creep-fatigue loading parameters are mainly limited to tensile holding time only. Further investigations on notched components under creep-fatigue conditions are still needed to discover the notch effect with compressive holding stage included.

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