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Research Article

Parallel-Machine Scheduling Problems with Past-Sequence-Dependent Delivery Times and Aging Maintenance

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We consider parallel-machine scheduling problems with past-sequence-dependent (psd) delivery times and aging maintenance. The delivery time is proportional to the waiting time in the system. Each machine has an aging maintenance activity. We develop polynomial algorithms to three versions of the problem to minimize the total absolute deviation of job completion times, the total load, and the total completion time.

1. Introduction

A common assumption in classical scheduling theory is that the machines are available at all times. However, there are many situations where machines need to be maintained and become unavailable during certain periods. Cheng et al. [1] study single-machine scheduling with deteriorating job processing times. Lee and Leon [2] investigated single machine scheduling with a rate-modifying activity. Kubzin and Strusevich [3] presented a setting where the maintenance activity was deteriorating; that is, delaying the maintenance activity increased the time required to perform it. Lee and Lin [4] considered single machine scheduling with maintenance and repair rate-modifying activity. Lee and Chen [5] discussed parallel-machine scheduling where each machine must be maintained once during the planning horizon. Cheng et al. [1, 6] considered the unrelated parallel-machine scheduling with aging maintenance activities. Cheng et al. [7] studied a single machine problem of common due-window assignment and scheduling of aging jobs and a maintenance activity simultaneously.

Browne and Yechiali [8] claimed that the time and effort required to put out a fire increase if there was a delay in the start of the fire-fighting effort. Scheduling in this setting is known as scheduling with aging jobs, which was first independently introduced by J. N. D. Gupta and S. K. Gupta [9] and Browne and Yechiali [8]. Since then, models of scheduling with deteriorating or aging jobs have been extensively studied from a variety of perspectives. More recent papers which have considered deterioration include Zhao and Tang [10], Cheng et al. [1], Wang et al. [11], Lai and Lee [12], Cheng et al. [13], Huang and Wang [14], Yin et al. [15], Lee et al. [16], Zhao and Tang [17], Wang and Liu [18], Zhao and Tang [19], Wu and Lee [20], Wang [21], Miao et al. [22], Wu and Lee [23], Yin et al. [24], Oron [25], Sicilia et al. [26], Wang et al. [27], Yin et al. [28], J.-B. Wang and J.-J. Wang [29], Xu et al. [30], Yin et al. [31], Bai et al. [32], and Ji et al. [33].

In modern industrial production, the manufacturing environment has an increasing influence on the processing times of jobs. A growing evidence displays that waiting time or manufacturing environment may have a disadvantageous effect on the total processing time of a job before delivery to the customer. For example, an electronic component may be exposed to certain electromagnetic or radioactive fields while waiting in the machines preprocessing area and regulatory authorities require the component to be treated for an amount of time proportional to the jobs' exposure time

to these fields. This treatment can be performed after the component has been processed by the machine but before it is delivered to the customer so it can be delivered with a guarantee. Such an extra time for eliminating adverse effects between the main processing and the delivery of a job is viewed as a past-sequence-dependent (psd) delivery time [34]. As usual, we suppose the treatment of the adverse effect for a job does not occupy any machine and has no relation to the schedule of the jobs main processing. In addition, we also assume that the psd delivery time of a job is proportional to the job's waiting time.

Koulamas and Kyparisis [34] assumed that the psd delivery time of a job is proportional to the job's waiting time, that is, the start time of processing. They proved some problems could be polynomially solvable. Liu et al. [35] studied the problem of single-machine scheduling with past-sequence-dependent delivery times, which was introduced in Koulamas and Kyparisis [34]. Liu [36] considered identical parallel-machine scheduling problem with past-sequence-dependent delivery times and learning effect. Shen and Wu [37] introduced the single machine past-sequence-dependent delivery times scheduling with general learning effects. Yin et al. [22] studied a single machine batch scheduling with an unavailability interval. Yin et al. [38] introduced a single-machine scheduling with past-sequence-dependent delivery times and a linear deterioration.

To the best of our knowledge, the aging maintenance scheduling problems with psd delivery time have not been investigated. In this paper, we introduce parallelmachines scheduling model with aging maintenance and psd delivery time. We will present that these scheduling problems are polynomially solvable. The remaining part of this paper is organized as follows. In Section 2, a precise formulation of the problem is given. We consider problems of minimizing the total absolute deviation of job completion times, the total load on all machines, and the total completion time in Section 3. The last section contains some conclusions of our model.

2. Problem Formulation

There are n independent and nonpreemptive jobs simultaneously available for processing and m identical parallel machines. Each machine can handle one job at a time and preemption is not allowed. If $m \ge n$, the problem is trivial. Therefore, we assume that m < n throughout the paper.

Let a_{ij} (p_{ij}) be the normal (actual) processing time of job J_{ij} ; let $a_{i[k]}$ ($p_{i[k]}$) be the normal (actual) processing time of the job $J_{i[k]}$ if it is scheduled in the kth position on machine M_i in a sequence. Due to the effects of aging, maintenance may be performed on the machine to improve its production efficiency. We suppose that at most one maintenance operation is allowed on one machine throughout the scheduling horizon. However, the starting time of the maintenance operation in the sequence is not known in advance. It can be scheduled immediately after completing the processing of any job. We further assume the following: (1) after maintenance, the machine will revert to its initial condition and the aging effects will start anew and (2)

the machine maintenance duration is a linear function of its starting time and is represented by $f(t) = \mu + \sigma t$, where $\mu > 0$ is the basic maintenance time, $\sigma > 0$ is a maintenance factor, and t is the starting time of the maintenance operation.

Suppose the position of maintenance operation is k_i on machine M_i . Hence, the machine maintenance duration is $f(t) = \mu + \sigma t = \mu + \sigma(\sum_{l=1}^{k_i} p_{i[l]})$. As in Liu et al. [39], we consider that the actual processing time of job $J_{i[j]}$ which is scheduled on machine M_i in position j $(j = 1, 2, ..., n_i)$ is given by

$$p_{i[j]} = \begin{cases} a_{i[j]} + bt = a_{i[j]} + b \sum_{l=1}^{j-1} p_{i[l]}, & \text{if } j \leq k_i, \\ a_{i[j]} + bt = a_{i[j]} + b \sum_{l=k_i}^{j-1} p_{i[l]}, & \text{if } j > k_i. \end{cases}$$

$$(1)$$

As in Koulamas and Kyparisis [34], the processing of job $J_{i[r]}$ must be followed by the psd delivery time $q_{i[r]}$, which can be computed as

$$q_{i[1]} = 0,$$
 $q_{i[r]} = \gamma W_{i[r]} = \gamma \sum_{l=1}^{r-1} p_{i[l]},$ $r = 2, 3, ..., n_i.$ (2)

 $\gamma \geq 0$ is a normalizing constant and $W_{i[r]}$ denotes the waiting time of job $J_{i[r]}$. In addition, it is supposed that the postprocessing operation of any job $J_{i[l]}$ modeled by its delivery time $q_{i[l]}$ is performed off-line; consequently, it is not affected by the availability of the machine and it can commence immediately upon completion of the main operation resulting in

$$C_{i[j]} = W_{i[j]} + p_{i[j]} + q_{i[j]}$$

$$= (1 + \gamma) \sum_{l=1}^{j-1} p_{i[l]} + p_{i[j]} \quad \text{if } j \le k_i,$$

$$C_{i[j]} = (1 + \gamma) \left(\mu + (1 + \sigma) \sum_{l=1}^{k_i} p_{i[l]} + \sum_{l=k_i+1}^{j-1} p_{i[l]} \right) + p_{i[j]} \quad \text{if } j > k_i,$$
(3)

where $C_{i[j]}$ denotes the completion time of job $J_{i[j]}$.

For convenience, we denote the psd delivery times given in (2) by $q_{\rm psd}$. Let TADC_i denote the total absolute deviation of jobs' completion times on machine M_i ; that is, $\sum {\rm TADC}_i = \sum_{l=1}^{n_i} \sum_{k=l}^{n_i} |C_{i[l]} - C_{i[k]}|$. Let L_i indicate the load of machine M_i ; that is, $L_i = \max\{C_{i[r]}\}, \ r = 1, 2, \ldots, n_i$. We, respectively, consider the minimization of the following objective functions: the sum of the total absolute deviation of jobs' completion times on each machine $\sum_{i=1}^m {\rm TADC}_i$, the total loads on all machines $\sum_{i=1}^m L_i$, and the total completion time $\sum_{i=1}^m \sum_{j=1}^{n_i} C_{ij}$. Using the three-field notation introduced

by Graham et al. for scheduling problems, we denote our problems as

$$P_{m} | q_{psd}, p_{i[j]} = a_{i[j]} + bt, ma | f,$$

$$f \in \left\{ \sum \sum C_{ij}, \sum L_{i}, \sum TADC_{i} \right\}.$$
(4)

Before presenting the main results, we first present several Lemmas and some notations that will be used in the proofs in sequel. If the number of jobs n_i and the position of the job preceding the maintenance operation k_i on machine M_i are known in advance, the actual processing times and the completion times of jobs on machine M_i are as follows:

$$p_{i[1]} = a_{i[1]}$$

$$C_{i[1]} = p_{i[1]} = a_{i[1]}$$

$$p_{i[2]} = a_{i[2]} + bp_{i[1]} = a_{i[2]} + ba_{i[1]}$$

$$C_{i[2]} = a_{i[2]} + (1 + \gamma + b) a_{i[1]}$$

$$\vdots$$

$$p_{i[k_i]} = a_{i[k_i]} + ba_{i[k_{i-1}]} + b (1 + b) a_{i[k_{i-2}]}$$

$$+ \dots + b(1 + b)^{k_{i-2}} a_{i[1]}$$

$$C_{i[k_i]} = a_{i[k_i]} + (1 + \gamma + b) a_{i[k_{i-1}]}$$

$$+ \dots + (1 + \gamma + b) (1 + b)^{k_{i-2}} a_{i[1]}$$

$$f(t) = \mu + \sigma \left(p_{i[1]} + p_{i[2]} + \dots + p_{i[k_i]} \right)$$

$$= \mu + \sigma \sum_{j=1}^{k_i} (1 + b)^{k_{i-j}} a_{i[j]}$$

$$p_{i[k_i+1]} = a_{i[k_i+1]}$$

$$(5)$$

$$C_{i[k_{i}+1]} = (1+\gamma)\mu + (1+\gamma)(1+\sigma)\sum_{j=1}^{k_{i}} (1+b)^{k_{i}-j}a_{i[j]} + a_{i[k_{i}+1]}$$

$$\vdots$$

$$p_{i[n_i]} = a_{i[n_i]} + ba_{i[n_i-1]} + \dots + b(1+b)^{n_i-k_i-2}a_{i[k_i+1]}$$

$$C_{i[n_i]} = (1+\gamma)\mu + (1+\gamma)(1+\sigma)\sum_{j=1}^{k_i} (1+b)^{k_i-j}a_{i[j]}$$

$$+ \sum_{j=k_i+1}^{n_i-1} (1+\gamma+b)(1+b)^{n_i-j-1}a_{i[j]} + a_{i[n_i]}.$$

Let $P(n, m, k) = (n_1, n_2, ..., n_m; k_1, k_2, ..., k_m)$ denote the allocation vector. We derive a lemma to bound P(n, m, k).

Lemma 1. The number of P(n, m, k) vector is bounded from above by $(n + 1)^{2m-1}/m!$.

Proof. For machine M_1 , n_1 is chosen from $\{0,1,\ldots,n\}$ and there are n+1 options for n_1 . When n_1 is determined, k_1 has at most n+1 options. After n_1 is determined, n_2 is chosen from $\{0,1,\ldots,n-n_1\}\subseteq\{0,1,\ldots,n\}$ at most n+1 times. Subsequently, k_2 has at most n+1 options, too. For machines M_3,\ldots,M_{m-1} , we similarly select n_3,\ldots,n_{m-1} and k_3,\ldots,k_{m-1} . Note that, for the last machine M_m , n_m is determined after choosing n_1,\ldots,n_{m-1} , because $\sum_{i=1}^m n_i = n$, and k_m has at most n+1 options. Considering that m machines are identical, there are $(n+1)^{2m-1}/m!$ possibilities for P(n,m,k) vector. This completes the proof. □

Lemma 2 (see [40]). Let there be two sequences of numbers x_i and y_i . The sum $\sum_i x_i y_i$ of products of the corresponding elements is the least (largest) if the sequences are monotonic in the opposite (same) sense.

3. Parallel-Machine Scheduling Problems

3.1. The Total Completion Time. In this section, we consider the problem of minimizing the total completion time; that is, $P_m|q_{psd}, p_{i[j]} = a_{i[j]} + bt, ma|\sum\sum C_{ij}$. For machine M_i , from the above analyse, we derive the total completion time on this machine:

$$\sum_{j=1}^{n_{i}} C_{ij} = (n_{i} - k_{i}) (1 + \gamma) \mu$$

$$+ \sum_{j=1}^{k_{i}} \left(1 + (1 + \gamma + b) \frac{(1 + b)^{k_{i} - j} - 1}{b} + (n_{i} - k_{i}) (1 + \gamma) (1 + \sigma) (1 + b)^{k_{i} - j} \right) a_{i[j]}$$

$$+ \sum_{j=k_{i}+1}^{n_{i}} \left(1 + (1 + \gamma + b) \frac{(1 + b)^{n_{i} - j} - 1}{b} \right) a_{i[j]}.$$
(6)

Therefore, the total completion time is

$$\begin{split} \sum_{i=1}^{m} \sum_{j=1}^{n_i} C_{ij} \\ &= \sum_{i=1}^{m} \left(n_i - k_i \right) \left(1 + \gamma \right) \mu \\ &+ \sum_{i=1}^{m} \sum_{j=1}^{k_i} \left(1 + \left(1 + \gamma + b \right) \frac{(1+b)^{k_i - j} - 1}{b} \right. \\ &+ \left. \left(n_i - k_i \right) \left(1 + \gamma \right) (1+\sigma) \left(1 + b \right)^{k_i - j} \right) a_{i[j]} \\ &+ \sum_{i=1}^{m} \sum_{j=k_i+1}^{n_i} \left(1 + \left(1 + \gamma + b \right) \frac{(1+b)^{n_i - j} - 1}{b} \right) a_{i[j]} \\ &= \sum_{i=1}^{m} \left(n_i - k_i \right) \left(1 + \gamma \right) \mu + \sum_{i=1}^{m} \sum_{j=1}^{n_i} w_{ij} a_{i[j]}, \end{split}$$

(7)

where

$$w_{ij} = \begin{cases} 1 + (1 + \gamma + b) \frac{(1+b)^{k_i - j} - 1}{b} + (n_i - k_i) (1 + \gamma) \\ \times (1 + \sigma) (1 + b)^{k_i - j}, \\ i = 1, 2, \dots, m, \quad j = 1, 2, \dots, k_i, \\ 1 + (1 + \gamma + b) \frac{(1+b)^{n_i - j} - 1}{b}, \\ i = 1, 2, \dots, m, \quad j = k_i + 1, k_i + 2, \dots, n_i. \end{cases}$$
(8)

When n_i and k_i are given, $\sum_{i=1}^m (n_i - k_i)(1 + \gamma)\mu$ is a constant. And $\sum_{i=1}^m \sum_{j=1}^{n_i} w_{ij} a_{i[j]}$ can be viewed as the scalar product of the w_{ij} vector and $a_{i[j]}$ vector. Therefore, on machine M_i , if the number n_i of jobs and the maintenance position k_i are known, by Lemma 2, all jobs are sorted in nondecreasing order of their normal processing times first. Then the largest job is assigned to the position with the smallest value of w_{ij} , the second largest job to the position with the second smallest value of w_{ij} , and so on. The time complexity of sorting algorithm on machine M_i is $O(n_i \log n_i)$. Together with Lemma 1, we derive the following theorem.

Theorem 3. The problem $P_m|q_{psd}, p_{i[j]} = a_{i[j]} + bt, ma| \sum \sum C_{ij}$ can be solved in $O(n^{2m-1}n \log n)$ time.

3.2. The Sum of Load on All Machines. In this section, we investigate the problem of minimizing the sum of load on all machines; that is, $P_m|q_{psd}, p_{i[j]} = a_{i[j]} + bt, ma|\sum L_i$. For machine M_i , from the above analysis, we calculate the sum of load on this machine:

$$L_{i} = (1 + \gamma) \mu$$

$$+ (1 + \gamma) (1 + \sigma) \sum_{j=1}^{k_{i}} (1 + b)^{k_{i} - j} a_{i[j]}$$

$$+ \sum_{j=k_{i}+1}^{n_{i}-1} (1 + \gamma + b) (1 + b)^{n_{i}-j-1} a_{i[j]} + a_{i[n_{i}]}.$$
(9)

Hence, the sum of load on all machines is

$$\sum_{i=1}^{m} L_{i} = m (1 + \gamma) \mu$$

$$+ \sum_{i=1}^{m} \sum_{j=1}^{k_{i}} (1 + \gamma) (1 + \sigma) (1 + b)^{k_{i} - j} a_{i[j]}$$

$$+ \sum_{i=1}^{m} \sum_{j=k_{i}+1}^{n_{i}-1} (1 + \gamma + b) (1 + b)^{n_{i} - j - 1} a_{i[j]}$$

$$+ \sum_{i=1}^{m} a_{i[n_{i}]} = m (1 + \gamma) \mu + \sum_{i=1}^{m} \sum_{j=k_{i}}^{n_{i}} w_{ij} a_{i[j]},$$
(10)

where

$$w_{ij} = \begin{cases} (1+\gamma)(1+\sigma)(1+b)^{k_i-j}, \\ i = 1, 2, \dots, m, & j = 1, 2, \dots, k_i, \\ (1+\gamma+b)(1+b)^{n_i-j-1}, \\ i = 1, 2, \dots, m, & j = k_i+1, k_i+2, \dots, n_i-1, \\ 1, & i = 1, 2, \dots, m, & j = n_i. \end{cases}$$
(11)

Since $m(1 + \gamma)\mu$ is a constant, if n_i and k_i are given, $\sum_{i=1}^{m} \sum_{j=1}^{n_i} w_{ij} a_{i[j]}$ can be viewed as the scalar product of the w_{ij} vector and $a_{i[j]}$ vector. Similar to the above analysis, on machine M_i , the time complexity of sorting algorithm is $O(n_i \log n_i)$. Together with Lemma 1, we conclude the following theorem.

Theorem 4. The problem $P_m|q_{psd}, p_{i[j]} = a_{i[j]} + bt, ma|\sum L_i$ can be solved in $O(n^{2m-1}n\log n)$ time.

3.3. The Sum of TADC on All Machines. In this section, we present the problem of minimizing the sum of TADC on all machines; that is, $P_m|q_{psd}$, $p_{i[j]}=a_{i[j]}+bt$, $ma|\sum TADC_i$. For machine M_i , from the above analysis, we express the sum of TADC on this machine:

TADC,

$$= \sum_{j=k_{i}+1}^{n_{i}} (2j-1-n_{i}) (1+\gamma) \mu$$

$$+ \sum_{j=1}^{k_{i}} \left((2j-1-n_{i}) + \sum_{h=j+1}^{k_{i}} (2h-1-n_{i}) (1+\gamma+b) \right)$$

$$\times (1+b)^{h-j-1}$$

$$+ \sum_{h=k_{i}+1}^{n_{i}} (2h-1-n_{i}) (1+\gamma)$$

$$\times (1+\sigma) (1+b)^{k_{i}-j} a_{i[j]}$$

$$+ \sum_{j=k_{i}+1}^{n_{i}-1} \left((2j-1-n_{i}) + \sum_{h=j+1}^{n_{i}} (2h-1-n_{i}) (1+\gamma+b) \right)$$

$$\times (1+b)^{h-j-1} a_{i[j]}$$

$$+ (n_{i}-1) a_{i[n_{i}]}. \qquad (12)$$

Thus, the sum of TADC on all machines is

$$\sum_{i=1}^{m} \text{TADC}_{i}$$

$$= \sum_{i=1}^{m} \sum_{j=k_{i}+1}^{n_{i}} (2j - 1 - n_{i}) (1 + \gamma) \mu$$

$$+ \sum_{i=1}^{m} \sum_{j=1}^{n_{i}} \left((2j - 1 - n_{i}) + \sum_{k=j+1}^{k_{i}} (2k - 1 - n_{i}) (1 + \gamma + b) (1 + b)^{k-j-1} + \sum_{k=k_{i}+1}^{n_{i}} (2k - 1 - n_{i}) (1 + \gamma) (1 + \sigma)$$

$$\times (1 + b)^{k_{i}-j} a_{i[j]}$$

$$+ \sum_{i=1}^{m} \sum_{j=k_{i}+1}^{n_{i}-1} \left((2j - 1 - n_{i}) + \sum_{k=j+1}^{n_{i}} (2k - 1 - n_{i}) (1 + \gamma + b) + \sum_{k=j+1}^{m} (n_{i} - 1) a_{i[n_{i}]} + \sum_{k=1}^{m} \sum_{j=k_{i}+1}^{n_{i}} (2j - 1 - n_{i}) (1 + \gamma) \mu$$

$$+ \sum_{i=1}^{m} \sum_{j=1}^{n_{i}} w_{ij} a_{i[j]}, \qquad (13)$$

where

$$w_{ij} = \begin{cases} (2j-1-n_i) + \sum_{h=j+1}^{k_i} (2h-1-n_i) (1+\gamma+b) (1+b)^{h-j-1} \\ + \sum_{h=k_i+1}^{n_i} (2h-1-n_i) (1+\gamma) (1+\sigma) (1+b)^{k_i-j}, \\ i = 1, 2, \dots, m, \quad j = 1, 2, \dots, k_i, \\ (2j-1-n_i) + \sum_{h=j+1}^{n_i} (2h-1-n_i) (1+\gamma+b) (1+b)^{h-j-1}, \\ i = 1, 2, \dots, m, \quad j = k_i + 1, k_i + 2, \dots, n_i - 1, \\ n_i - 1, \\ i = 1, 2, \dots, m, j = n_i. \end{cases}$$

$$(14)$$

Since $\sum_{i=1}^{m} \sum_{j=k_i+1}^{n_i} (2j-1-n_i)(1+\gamma)\mu$ is a constant, when n_i and k_i are given, $\sum_{i=1}^{m} \sum_{j=1}^{n_i} w_{ij}a_{i[j]}$ can be viewed as the scalar product of the w_{ij} vector and $a_{i[j]}$ vector. Similar to the above analysis, the time complexity of scheduling algorithm on machine M_i is $O(n_i \log n_i)$. Together with Lemma 1, we obtain the following theorem.

Theorem 5. The problem $P_m|q_{psd}, p_{i[j]} = a_{i[j]} + bt, ma|\sum TADC_i$ can be solved in $O(n^{2m-1}n \log n)$ time.

4. Conclusions

In this paper we study parallel-machine scheduling problems with past-sequence-dependent (psd) delivery times and aging maintenance. The delivery time of a job is proportional to its waiting time. Each machine has an aging maintenance activity. Polynomially solvable problems have been explored for parallel-machine scheduling. The research extends the existed models of parallel machine scheduling with delivery times. For future research, it will be worth extending the problem to multiple maintenances or flow-shop environment.

Conflict of Interests

The authors declare that there is no conflict of interests regarding the publication of this paper.

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References

- [1] T. C. Cheng, W. C. Lee, and C. C. Wu, "Single-machine scheduling with deteriorating functions for job processing times," *Applied Mathematical Modelling. Simulation and Computation for Engineering and Environmental Systems*, vol. 34, no. 12, pp. 4171–4178, 2010.
- [2] C.-Y. Lee and V. J. Leon, "Machine scheduling with a rate-modifying activity," *European Journal of Operational Research*, vol. 128, no. 1, pp. 119–128, 2001.
- [3] M. A. Kubzin and V. A. Strusevich, "Planning machine maintenance in two-machine shop scheduling," *Operations Research*, vol. 54, no. 4, pp. 789–800, 2006.
- [4] C.-Y. Lee and C.-S. Lin, "Single-machine scheduling with maintenance and repair rate-modifying activities," *European Journal of Operational Research*, vol. 135, no. 3, pp. 493–513, 2001.
- [5] C.-Y. Lee and Z.-L. Chen, "Scheduling jobs and maintenance activities on parallel machines," *Naval Research Logistics*, vol. 47, no. 2, pp. 145–165, 2000.
- [6] T. C. E. Cheng, C.-J. Hsu, and D.-L. Yang, "Unrelated parallel-machine scheduling with deteriorating maintenance activities,"

- Computers and Industrial Engineering, vol. 60, no. 4, pp. 602–605, 2011.
- [7] T. C. E. Cheng, S. J. Yang, and D. L. Yang, "Common duewindow assignment and scheduling of linear time-dependent deteriorating jobs and a deteriorating maintenance activity," *International Journal of Production Economics*, vol. 135, no. 1, pp. 154–161, 2012.
- [8] S. Browne and U. Yechiali, "Scheduling deteriorating jobs on a single processor," *Operations Research*, vol. 38, no. 3, pp. 495– 498, 1990.
- [9] J. N. D. Gupta and S. K. Gupta, "Single facility scheduling with nonlinear processing times," *Computers and Industrial Engineering*, vol. 14, no. 4, pp. 387–393, 1988.
- [10] C.-L. Zhao and H.-Y. Tang, "Single machine scheduling problems with deteriorating jobs," *Applied Mathematics and Computation*, vol. 161, no. 3, pp. 865–874, 2005.
- [11] X.-R. Wang, X. Huang, and J.-B. Wang, "Single-machine scheduling with linear decreasing deterioration to minimize earliness penalties," *Applied Mathematical Modelling*, vol. 35, no. 7, pp. 3509–3515, 2011.
- [12] P.-J. Lai and W.-C. Lee, "Single-machine scheduling with a non-linear deterioration function," *Information Processing Letters*, vol. 110, no. 11, pp. 455–459, 2010.
- [13] T. C. Cheng, W.-C. Lee, and C.-C. Wu, "Single-machine scheduling with deteriorating jobs and past-sequence-dependent setup times," *Applied Mathematical Modelling*, vol. 35, no. 4, pp. 1861–1867, 2011.
- [14] X. Huang and M.-Z. Wang, "Parallel identical machines scheduling with deteriorating jobs and total absolute differences penalties," *Applied Mathematical Modelling*, vol. 35, no. 3, pp. 1349–1353, 2011.
- [15] Y. Q. Yin, W.-H. Wu, T. C. E. Cheng, and C.-C. Wu, "Single-machine scheduling with time-dependent and position-dependent deteriorating jobs," *International Journal of Computer Integrated Manufacturing*, 2014.
- [16] W.-C. Lee, J.-B. Lin, and Y.-R. Shiau, "Deteriorating job scheduling to minimize the number of late jobs with setup times," *Computers and Industrial Engineering*, vol. 61, no. 3, pp. 782–787, 2011.
- [17] C. Zhao and H. Y. Tang, "A note to due-window assignment and single machine scheduling with deteriorating jobs and a rate-modifying activity," *Computers & Operations Research*, vol. 39, no. 6, pp. 1300–1303, 2012.
- [18] J.-B. Wang and L.-L. Liu, "Two-machine flow shop scheduling with linear decreasing job deterioration," *Computers and Industrial Engineering*, vol. 56, no. 4, pp. 1487–1493, 2009.
- [19] C. Zhao and H. Tang, "Single machine scheduling with past-sequence-dependent setup times and deteriorating jobs," Computers and Industrial Engineering, vol. 59, no. 4, pp. 663–666, 2010
- [20] C.-C. Wu and W.-C. Lee, "Single-machine scheduling problems with a learning effect," *Applied Mathematical Modelling*, vol. 32, no. 7, pp. 1191–1197, 2008.
- [21] J.-B. Wang, "Single-machine scheduling problems with the effects of learning and deterioration," *Omega*, vol. 35, no. 4, pp. 397–402, 2007.
- [22] C. Miao, Y. Zhang, and Z. Cao, "Bounded parallel-batch scheduling on single and multi machines for deteriorating jobs," *Information Processing Letters*, vol. 111, no. 16, pp. 798–803, 2011.
- [23] C.-C. Wu and W.-C. Lee, "Two-machine flowshop scheduling to minimize mean flow time under linear deterioration," *International Journal of Production Economics*, vol. 103, no. 2, pp. 572– 584, 2006.

- [24] Y. Yin, W.-H. Wu, T. C. E. Cheng, and C.-C. Wu, "Due-date assignment and single-machine scheduling with generalised position-dependent deteriorating jobs and deteriorating multimaintenance activities," *International Journal of Production Research*, vol. 52, no. 8, pp. 2311–2326, 2014.
- [25] D. Oron, "Single machine scheduling with simple linear deterioration to minimize total absolute deviation of completion times," *Computers & Operations Research*, vol. 35, no. 6, pp. 2071–2078, 2008.
- [26] J. Sicilia, M. González-De-la-Rosa, J. Febles-Acosta, and D. Alcaide-López-de-Pablo, "An inventory model for deteriorating items with shortages and time-varying demand," *International Journal of Production Economics*, vol. 155, pp. 155–162, 2014.
- [27] D. Wang, Y. Huo, and P. Ji, "Single-machine group scheduling with deteriorating jobs and allotted resource," *Optimization Letters*, vol. 8, no. 2, pp. 591–605, 2014.
- [28] N. Yin, L. Kang, and X. Y. Wang, "Single-machine group scheduling with processing times dependent on position, starting time and allotted resource," *Applied Mathematical Mod*elling, vol. 38, no. 19-20, pp. 4602–4613, 2014.
- [29] J.-B. Wang and J.-J. Wang, "Single machine group scheduling with time dependent processing times and ready times," *Information Sciences*, vol. 275, pp. 226–231, 2014.
- [30] Y.-T. Xu, Y. Zhang, and X. Huang, "Single-machine ready times scheduling with group technology and proportional linear deterioration," *Applied Mathematical Modelling*, vol. 38, no. 1, pp. 384–391, 2014.
- [31] N. Yin, L. Kang, T.-C. Sun, C. Yue, and X.-R. Wang, "Unrelated parallel machines scheduling with deteriorating jobs and resource dependent processing times," *Applied Mathematical Modelling*, vol. 38, no. 19–20, pp. 4747–4755, 2014.
- [32] J. Bai, Z.-R. Li, J.-J. Wang, and X. Huang, "Single machine common flow allowance scheduling with deteriorating jobs and a rate-modifying activity," *Applied Mathematical Modelling*, 2014.
- [33] P. Ji, G. Li, Y. Z. Huo, and J.-B. Wang, "Single-machine common flow allowance scheduling with job-dependent aging effects and a deteriorating maintenance activity," *Optimization Letters*, vol. 8, no. 4, pp. 1389–1400, 2014.
- [34] C. Koulamas and G. J. Kyparisis, "Single-machine scheduling problems with past-sequence-dependent delivery times," *International Journal of Production Economics*, vol. 126, no. 2, pp. 264–266, 2010.
- [35] M. Liu, F. Zheng, C. Chu, and Y. Xu, "New results on single-machine scheduling with past-sequence-dependent delivery times," *Theoretical Computer Science*, vol. 438, pp. 55–61, 2012.
- [36] M. Liu, "Parallel-machine scheduling with past-sequencedependent delivery times and learning effect," Applied Mathematical Modelling, vol. 37, no. 23, pp. 9630–9633, 2013.
- [37] L. Shen and Y.-B. Wu, "Single machine past-sequencedependent delivery times scheduling with general positiondependent and time-dependent learning effects," *Applied Mathematical Modelling*, vol. 37, no. 7, pp. 5444–5451, 2013.
- [38] Y. Q. Yin, T. C. E. Cheng, J. Y. Xu, S.-R. Cheng, and C.-C. Wu, "Single-machine scheduling with past-sequencedependent delivery times and a linear deterioration," *Journal of Industrial and Management Optimization*, vol. 9, no. 2, pp. 323– 339, 2013.
- [39] M. Liu, S. Wang, and C. Chu, "Scheduling deteriorating jobs with past-sequence-dependent delivery times," *International Journal of Production Economics*, vol. 144, no. 2, pp. 418–421, 2013
- [40] G. H. Hardy, J. E. Littlewood, and G. Polya, *Inequalities*, Cambridge University Press, London, UK, 1967.

















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