

Research Article Model and Frequency Control for Three-Phase Wireless Power Transfer System

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In order to the eliminate the "dead spot" in the traditional three-phase wireless power transfer (WPT) system, a three-phase WPT system with an asymmetric magnetic circuit is presented in this paper. Additionally, mathematical model of the system is established and the system parameters are optimized. Based on the fact that the resonant frequency and efficiency are greatly varied with the load, a method based on impedance conversion is further proposed to improve the frequency stability and system efficiency. Finally, simulation and experimental results show that the proposed method is reliable and feasible to eliminate the "dead spot."

1. Introduction

Wireless power transfer (WPT) can transmit electric energy from the power sources to the loads without any wire between the two sides, which offers advantages in terms of flexibility, reliability, and safety [1–4]. Therefore, it has been widely used in some special fields, including wireless power desktop supply platform, two-way power supply for tram [5], and mining application [6].

Most of the previous research is limited in single-phase WPT system. With rapid development of electrical equipment, the three-phase WPT system has been further developed [7-9]. A new three-phase and bidirection WPT system that is suitable for rapid charging of EVs is presented [10]. A new three-phase bipolar inductive power transfer system can provide power across the entire width of a roadway [11]. However, a three-phase WPT system usually suffers the "dead spot" problem in pick-up side. Some researchists present a solution about the pick-up "dead spot" in a three-phase WPT system [12–14]. It is suitable for desk wireless power supply system. There will be a tiny pick-up voltage when the load is exactly in the pick-up "dead spot." Besides, the system will automatically switch one-phase to another to avoid "dead spot" problem. However, it suffers low efficiency, complicated operation, and extra detection circuit. Furthermore, the impacts of the load variation on system stability and efficiency are not considered in this system. Some papers did some research on the efficiency of the three-phase WPT system from magnetic structure and system modeling [15]. Therefore, further studies on the three-phase WPT system, especially the dead spot elimination, frequency stabilization, and efficiency improvement are strongly required. A lot of papers study the method of impedance conversion [16, 17]. However, this method is rarely studied to control frequency stability in three-phase WPT system.

In this paper, to eliminate the "dead spot" in the traditional three-phase WPT system with symmetric circuit, a new asymmetric magnetic circuit is studied. Mathematical model of the system is established to optimize the system parameters. In addition, an impedance conversion based method is proposed to improve the frequency stability and system efficiency as both the resonant frequency and efficiency are heavily affected by the load variation. An experimental prototype is established to verify the validity of the proposed method. Simulation and experimental results indicate that the "dead spot" can be always eliminated regardless of the load position.

2. Typical Three-Phase WPT System Analysis

2.1. Overview of Three-Phase Wireless Power Transfer System. A typical three-phase WPT system with a symmetrical



FIGURE 1: Typical symmetrical magnetic three-phase WPT system.

magnetic circuit is shown in Figure 1. This system consists of DC power supply (U_d) , high frequency inverter $(S_1 \sim S_6)$, primary side $(L_A, L_B, L_C \text{ and } C_A, C_B, C_C)$, and pick-up side $(L_s \text{ and } C_s)$ as well as load (R_{eq}) . Meanwhile, * is dotted terminal of the three-phase primary coils. The mutual inductances between primary side and pick-up side are denoted by M_1 , M_2 , and M_3 . Primary-side power converter generates a three-phase symmetrical high frequency sinusoidal current in the primary coils. Then the pick-up side, which is magnetically coupled to primary side, obtains power from the primary side to supply load through power conversion.

It has been confirmed that such a system in Figure 1 suffers from "dead spot" problem in the pick-up side. And a new three-phase WPT system with asymmetrical magnetic circuit which can effectively eliminate the "dead spot" is presented [18]. However, system parameters optimization and the influence of load variation on system stability were both ignored in this paper.

2.2. Characteristic Analysis of "Dead Spot". By the analysis of three-phase full-bridge inverter, currents in the three primary coils, with the same value of amplitude I_0 , can be written as

$$\begin{split} i_A &= I_0 e^{j\omega t}, \\ i_B &= I_0 e^{j\omega t + j\pi 2/3}, \\ i_C &= I_0 e^{j\omega t + j\pi 4/3}. \end{split} \tag{1}$$

The pick-up voltage of secondary coil is

$$\begin{split} u_{\rm OC} &= u_{AS} + u_{BS} + u_{CS} \\ &= j\omega M_1 i_A + j\omega M_2 i_B + j\omega M_3 i_C \\ &= j\omega I_0 e^{j\omega t} \left(M_1 + e^{j\pi 2/3} M_2 + e^{j\pi 4/3} M_3 \right), \end{split}$$
(2)

where u_{AS} , u_{BS} , and u_{CS} are the pick-up voltages of the secondary coil induced from three primary coils.

According to (2), the vector graph of pick-up voltage u_{OC} is shown in Figure 2.

From (2) and Figure 2, it can be assured that pick-up u_{OC} equals zero when three mutual inductances M_1-M_3 have the same value. That is, "dead spot" exists when secondary coil is located in the center of three primary coils.



FIGURE 2: Vector graph of pick-up voltage u_{OC} in symmetric threephase WPT system.

3. New Type of Three-Phase WPT System with Asymmetric Magnetic Circuit

3.1. Analysis of Eliminating "Dead Spot". In order to solve the problem of "dead spot" in three-phase WPT system, a three-phase WPT system with an asymmetric magnetic circuit is proposed in Figure 3. The dotted terminal of *C* phase (the third phase of three phase coils) is reversed so that the magnetic circuit becomes asymmetric.

Figure 4 shows the equivalent model of the pick-up side. In this case, the pick-up voltage V_{OC} of the pick-up side can be written as

$$u'_{OC} = u_{AS} + u_{BS} - u_{CS}$$

= $j\omega M_1 i_A + j\omega M_2 i_B - j\omega M_3 i_C$ (3)
= $j\omega I_P e^{j\omega t} \left(M_1 + e^{j\pi 2/3} M_2 - e^{j\pi 4/3} M_3 \right),$

where I_p is the current amplitude and ω is the work frequency of the system.

It can be seen from (3) that, regardless of the value of three mutual inductances M_1 , M_2 , and M_3 , "dead spot" never exists compared to the traditional symmetrical magnetic circuit, ensuring that the load on any position can achieve efficient power transmission.



FIGURE 3: Three-phase WPT system with asymmetric magnetic circuit.

3.2. Design and Optimization of Parameters. As shown in Figure 3, the instantaneous value of current flowing in the three primary coils can be represented by

$$i_A = I_P \sin(\omega t) = I_P \angle 0^\circ,$$

$$i_B = I_P \sin(\omega t + 120^\circ) = I_P \angle 120^\circ,$$
 (4)

$$i_C = I_P \sin(\omega t + 240^\circ) = I_P \angle 240^\circ,$$

where i_A , i_B , and i_C are all the current instantaneous value.

In Figure 4, L_S is self-inductance of secondary windings. C_S is the pick-up resonant capacitor. C_S can be expressed as

$$C_{\rm S} = \frac{1}{\omega^2 L_{\rm S}}.$$
 (5)

The pick-up current $C_{\rm S}$ is

$$I_{S} = \frac{\omega M_{1} I_{P} \angle 0^{\circ} + \omega M_{2} I_{P} \angle 120^{\circ} - \omega M_{3} I_{P} \angle 240^{\circ}}{R_{\text{eq}}}.$$
 (6)

According to Ohm's law, a phase of primary coils can be represented by

$$I_P Z_A = \omega M_1 I_S,\tag{7}$$

where Z_A is the reflected impedance. By (6) and (7), Z_A can be expressed as

$$Z_{A} = \frac{\omega^{2} M_{1}}{R_{eq}} \left(M_{1} + M_{2} \angle 120^{\circ} - M_{3} \angle 240^{\circ} \right)$$
$$= \frac{\omega^{2} M_{1}}{R_{eq}} \left[M_{1} - \frac{1}{2} M_{2} + \frac{1}{2} M_{3} + \left(\frac{\sqrt{3}}{2} M_{2} + \frac{\sqrt{3}}{2} M_{3} \right) j \right].$$
(8)



FIGURE 4: Equivalent model of the secondary circuit.



FIGURE 5: Primary equivalent inductance coupling model of asymmetric circuit.

So, Z_B and Z_C can be expressed as

$$Z_{B} = \frac{\omega^{2} M_{2}}{R_{eq}} \left[M_{2} - \frac{1}{2} M_{1} + \frac{1}{2} M_{3} - \left(\frac{\sqrt{3}}{2} M_{1} + \frac{\sqrt{3}}{2} M_{3} \right) j \right],$$

$$Z_{C} = \frac{\omega^{2} M_{3}}{R_{eq}} \left[M_{3} + \frac{1}{2} M_{1} + \frac{1}{2} M_{2} + \left(\frac{\sqrt{3}}{2} M_{2} - \frac{\sqrt{3}}{2} M_{1} \right) j \right].$$
(9)

Based on mutual inductance coupling principle, the pickup side can be reflected into primary side. The equivalent model is shown in Figure 5. According to the actual demand of the system, the real part of Z_A , Z_B , and Z_C should be more than zero to ensure the system resonance; then

$$\operatorname{Re}(Z_{A}) = M_{1} - \frac{1}{2}M_{2} + \frac{1}{2}M_{3} > 0,$$

$$\operatorname{Re}(Z_{B}) = M_{2} + \frac{1}{2}M_{3} - \frac{1}{2}M_{1} > 0,$$
 (10)

$$\operatorname{Re}(Z_{C}) = M_{3} + \frac{1}{2}M_{1} + \frac{1}{2}M_{2} > 0.$$

The sums between imaginary parts of Z_A , Z_B , Z_C , and ωL should be more than zero.

$$\operatorname{Im}\left(Z_{A}+\omega L_{A}\right) = \frac{\omega^{2}M_{1}}{R_{\mathrm{eq}}}\left(\frac{\sqrt{3}}{2}M_{2}+\frac{\sqrt{3}}{2}M_{3}\right)+\omega L_{A}$$

$$>0,$$

$$\operatorname{Im}\left(Z_{B}+\omega L_{B}\right) = \frac{\omega^{2}M_{2}}{R_{\mathrm{eq}}}\left(-\frac{\sqrt{3}}{2}M_{1}-\frac{\sqrt{3}}{2}M_{3}\right)$$

$$+\omega L_{B}>0,$$

$$\operatorname{Im}\left(Z_{C}+\omega L_{C}\right) = \frac{\omega^{2}M_{3}}{R_{\mathrm{eq}}}\left(\frac{\sqrt{3}}{2}M_{2}-\frac{\sqrt{3}}{2}M_{1}\right)+\omega L_{C}$$

$$>0.$$

From (10), when mutual inductance $M_2/2 < M_1 < 2M_2$, (11) can be simplified as

$$L_{B} > \frac{\sqrt{3}}{2} \frac{\omega M_{2}}{R_{eq}} (M_{1} + M_{3}),$$

$$L_{C} > \frac{\sqrt{3}}{2} \frac{\omega M_{3}}{R_{eq}} (M_{1} - M_{2}).$$
(12)

Assuming that $L_A = L_B = L_C = L$, the self-inductance of the primary windings meets (13) only.

$$L > \frac{\sqrt{3}}{2} \frac{\omega M_2}{R_{\rm eq}} \left(M_1 + M_3 \right).$$
 (13)

In summary, the mutual inductance and self-inductance of three-phase WPT system with an asymmetric magnetic circuit should meet the following equation:

$$\frac{M_2}{2} < M_1 < 2M_2,
L > \frac{\sqrt{3}}{2} \frac{\omega M_2}{R_{eq}} (M_1 + M_3).$$
(14)

When the primary side is at resonance, (15) should meet

$$\operatorname{Im}\left(Z_{A} + j\omega L_{A} + \frac{1}{j\omega C_{A}}\right) = 0,$$

$$\operatorname{Im}\left(Z_{B} + j\omega L_{B} + \frac{1}{j\omega C_{B}}\right) = 0,$$
 (15)

$$\operatorname{Im}\left(Z_{C} + j\omega L_{C} + \frac{1}{j\omega C_{C}}\right) = 0.$$



FIGURE 6: Impedance conversion circuit.

So the resonant capacitor of the three-phase primary winding can be written as

$$C_{A} = \frac{2R_{eq}}{\sqrt{3}\omega^{3}M_{1}(M_{2} + M_{3}) + 2R_{eq}\omega^{2}L},$$

$$C_{B} = \frac{2R_{eq}}{-\sqrt{3}\omega^{3}M_{2}(M_{1} + M_{3}) + 2R_{eq}\omega^{2}L},$$

$$C_{C} = \frac{2R_{eq}}{\sqrt{3}\omega^{3}M_{3}(M_{2} - M_{1}) + 2R_{eq}\omega^{2}L}.$$
(16)

Obviously, actual operation frequency is affected by load R_{eq} . That is, there is a one-to-one correspondence between corresponding direct parameters (inductances and capacitances) and a load value. However, the value of load is usually variational due to heat and temperature variation. So, common platform is more meaningful for three-phase WPT system.

3.3. The Analysis of Frequency Stability. From (16), the values of the primary resonance capacitor are associated with M, R_{eq} , and ω . Fixed and variable frequency control are two main control strategies. It is obvious that fixed frequency control is more suitable for this system. If the load is placed in the center of three-phase primary coils, the mutual inductance M is fixed. Therefore, the values of the primary resonance capacitor are only associated with R_{eq} . In practical three-phase WPT system, power transfer and efficiency are greatly affected by the change in resonant frequency due to the load variance. To solve the problem mentioned above, a fixed frequency control strategy based on impedance conversion was presented in next section.

4. Frequency Stability Method Based on Impedance Conversion

4.1. Basic Principle of Impedance Conversion. In the pickup side, for the sake of achieving the frequency stability of system, a rectifier-filter circuit and DC/DC converter are introduced to achieve the fixed frequency of system, which can maintain the equivalent impedance of load through regulating the duty cycle of DC chopper.

The schematic circuit of impedance conversion based on the Buck-Boost converter is shown in Figure 6, where R_1 is the equivalent impedance after rectifier-filter circuit regulation and R_{eq} is the equivalent impedance across the pick-up power compensation part.

As shown in Figure 6, pick-up coil generates a direct voltage U_1 after resonance compensation and rectifier-filter circuit. Then, this voltage (U_1) can provide power for load (R_L) across the Buck-Boost converter, so that the output voltage of load becomes U_o .

4.2. Theoretical Derivation. Assume that Buck-Boost circuits work in the soft-switching mode and the switching loss is ignored. To simplify the system, the load R_L is a resistant load; then

$$\frac{U_1^2}{R_1} = \frac{U_0^2}{R_L}.$$
 (17)

When the Buck-Boost circuit works under the continuous current mode, the relationship between U_0 and U_1 can be expressed as

$$U_0 = \frac{\delta}{1 - \delta} U_1,\tag{18}$$

where δ is the duty cycle of switch.

From (17) and (18), the relationship between R_1 and R_L can be given by

$$R_1 = \frac{(1-\delta)^2}{\delta^2} R_L.$$
 (19)

The equivalent ac resistance R_{eq} for the rectifier with capacitive filter [19] is given by

$$R_{\rm eq} = \frac{8}{\pi^2} R_1.$$
 (20)

The relation between the duty ratio of switch δ and the load R_L can be calculated from (19) and (20).

$$\delta = \frac{2\sqrt{2}}{2\sqrt{2} + \pi\sqrt{R_{\rm eg}/R_L}},\tag{21}$$

where δ is in the range 0~1. The relationship between duty cycle δ and variable load R_L is shown in Figure 7 when equivalent load R_{eq} is held constant.

From Figure 7, for a given R_L , there will be δ to hold R_{eq} constant.

5. Simulation and Experimental Results

The viability of the proposed system is verified by simulation and experiments. The prototype system is shown in Figure 8. For the following confirmatory experiments, 10Ω load will be powered by a 500 V DC voltage source. The system resonant frequency is 20 kHz. The three primary coils inductors L_A , L_B , and L_C are 91.78 mH. The pick-up coil L_S is 67 mH. The mutual inductances of M_1 , M_2 , and M_3 are 30 mH. According to (5), the capacitances of secondary



FIGURE 7: One-to-one correspondence between duty cycle δ and variable load R_L for constant equivalent load R_{eq} .



FIGURE 8: Experimental platform.

side can be calculated as $0.94 \,\mu\text{F}$. Furthermore, from (16), the capacitances of primary side C_A , C_B , and C_C are $0.565 \,\mu\text{F}$, $0.906 \,\mu\text{F}$, and $0.686 \,\mu\text{F}$, respectively.

In Figures 9–14, (a) is the waveform of simulation and (b) is the waveform of experiment.

5.1. Elimination of "Dead Spot". Pick-up voltage with a symmetric magnetic circuit is illustrated in Figure 9. From Figure 9, it is evident that the primary-to-pick-up mutual inductances are approximately equal; therefore, the induced voltage, u_{OC} , will become zero if the pick-up coils are placed in the center of three-phase primary coils. Figure 10 shows the pick-up voltage u'_{OC} with an asymmetric magnetic circuit. Even if the load is placed in the center of three-phase primary coils, the induced voltage u'_{OC} is not zero. Comparing Figure 9 with Figure 10, the proposed three-phase WPT system with an asymmetric magnetic circuit can effectively eliminate the pick-up voltage "dead spots."

5.2. Parameter Verification. Figure 11 shows the voltage and current waveforms of capacitor C_S in asymmetric system (Figure 3). As evident from the illustration, the waveform of the voltage and current is not distorted. And its frequency and amplitude are very stable so that the parameters of the system are designed properly.



FIGURE 9: Pick-up voltage of secondary coil with symmetric magnetic circuit.



FIGURE 10: Pick-up voltage of secondary coil with asymmetric magnetic circuit.



FIGURE 11: Voltage and current of capacitor $C_{\rm S}$ in asymmetric system.

5.3. Impedance Conversion. From (16), when the value of load R_{eq} is 100 Ω , the system in Figure 3 will be in the nonresonant state for existing values of inductors and capacitors if any impedance conversion circuit is not added to the system. Then, the voltage waveform of pick-up coil is shown in Figure 12.

Obviously, the waveform of current has apparent distortion and high harmonic percentages. In this case, the transmission efficiency is low.

In order to achieve the frequency stability of asymmetric three-phase WPT system, impedance conversion is adopted in secondary side which is shown in Figure 6, and the



FIGURE 12: Voltage of pick-up coil when R_{eq} equals 100 Ω .



FIGURE 13: Input voltage before impedance conversion circuit.

topology of primary side remains the same. In addition, R_L is 100 Ω , C_1 is 220 μ F, L_b is 3.9 mH, and C_b is 10 μ F.

Figure 13 shows the voltage waveform U_1 which is before impedance conversion circuit. From Figure 13, the load changes from 100Ω to 50Ω at 0.05 s. Meanwhile, according to (21), duty cycle δ of switch S_7 is changed from 0.741 to 0.649 for maintaining constant equivalent load R_{eq} in Figure 6. The DC voltage U_1 remains stable after dynamic change in a period of time, which means reflected impedances from secondary side to primary side maintain being constant. U_1 rises to 54 V after load change. However, the error is about 1.48%, which indicates that the pick-up voltage holds stable basically after adding the impedance conversion circuit.

In conclusion, the input voltage U_1 and impedance R_1 of impedance conversion circuit in Figure 6 can be unchanged by adjusting duty cycle δ at the time of load change. So, the output power of load R_L will be stable according to (17) whether R_L is changed or not.

Figure 14 shows the voltage waveform of load R_L . Comparing Figure 14(a) with Figure 14(b), the output voltage lowers in actual system because of the existence of parasitic resistances which are ignored in calculation and simulation.

From Figure 14(b), the output power is 201.64 W while it reduces to 200 W after load change. However, the error is only 0.8%, which indicates that the output power of system can maintain being constant.

According to the above analysis, the proposed system improves frequency stability and efficiency by applying impedance conversion circuit into three-phase WPT system.

6. Conclusion

Aimed at the problem of "dead spot" in symmetric threephase WPT system, a three-phase WPT system with an asymmetric magnetic circuit has been presented. The parameters of the system are designed and optimized. However, there is a one-to-one correspondence between corresponding direct parameters (inductances and capacitances) and a load value. It means the system will be in nonresonant state if the load is changed, which causes low efficiency and high total harmonic distortion. But, in fact, the value of load is usually variational due to heat and temperature variation. So, common platform is more meaningful for three-phase WPT system. As transfer power and efficiency are greatly affected



FIGURE 14: Output voltage of load R_L .

by load change, a fixed frequency design method based on impedance conversion is proposed and correlation theory is derived in detail. So far, a three-phase WPT system has been designed which has advantages of stable operating frequency, high efficiency, and no "dead spot."

Competing Interests

The authors declare that there are no competing interests regarding the publication of this paper.

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