

Ultra-long range correlations of the dynamics of jammed soft matter

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We use photon correlation imaging, a recently introduced space-resolved dynamic light scattering method, to investigate the spatial correlation of the dynamics of a variety of jammed and glassy soft materials. Strikingly, we find that in deeply jammed soft materials spatial correlations of the dynamics are quite generally ultra-long ranged, extending up to the system size, orders of magnitude larger than any relevant structural length scale, such as the particle size, or the mesh size for colloidal gel systems. This has to be contrasted with the case of molecular, colloidal and granular “supercooled” fluids, where spatial correlations of the dynamics extend over a few particles at most. Our findings suggest that ultra long range spatial correlations in the dynamics of a system are directly related to the origin of elasticity. While solid-like systems with entropic elasticity exhibit very moderate correlations, systems with enthalpic elasticity exhibit ultra-long range correlations due to the effective transmission of strains throughout the contact network.

I. Introduction

Soft materials such as colloidal suspensions, emulsions and surfactant phases typically exhibit increasingly slow relaxation dynamics as a result of particle crowding or because of strong interactions, either attractive or repulsive.¹ Work in the past decade has shown that a feature shared by most of these systems is the heterogeneous character of their slow dynamics, which result from rearrangements that are localized in space and intermittent in time,^{1–10} in analogy with molecular glass formers^{11,12} and driven athermal grains and foams.^{13–17}

For colloidal hard spheres, probably the most studied soft matter model system exhibiting a glass transition,¹⁸ the size ξ of dynamical clusters undergoing correlated rearrangements has been shown to grow with volume fraction on approaching the glass transition.^{3,6,19,20} For supercooled samples whose dynamics are stationary, the growth is however modest, the largest reported values of ξ being of the order of a few particle sizes.^{3,6,19,20} Similar results have been reported for weakly attractive systems.^{7,8} This agrees with numerical and experimental findings for molecular glass formers^{11,12,21,22} and grains.^{13–16} Although the debate is still very active on whether or not the glass and the jamming transitions coincide in thermal hard spheres,^{23–28} and thus on how far the regime where ξ grows may extend, it is unlikely that significantly larger correlation lengths may be measured in the supercooled regime.

Recent experiments using time-resolved light scattering methods suggest that this scenario could be very different for a wide range of soft materials quenched in a nearly-arrested, out-of-equilibrium state, which we shall refer to (somewhat loosely) as jammed soft systems. In these experiments, very large

temporal fluctuations of the intensity autocorrelation function were observed,^{9,10,29} suggesting that the size of regions undergoing correlated rearrangements may be a sizeable fraction of the scattering volume, *i.e.* that they may extend over macroscopic distances. Indeed, direct measurements of ξ in a strongly attractive colloidal gel³⁰ and in concentrated soft particles³¹ have shown that in these systems the correlation length of the dynamics is limited essentially only by the system size.

In this paper, we present data on a variety of soft jammed systems, showing that extremely long ranged correlations of the dynamics in jammed systems are the rule rather than the exception. The systems investigated include hard and soft spheres, colloidal gels made of attractive particles, biomimetic protein films, a concentrated surfactant solution (“onion” phase) and Laponite suspensions: with the exception of the supercooled hard spheres, ξ always exceeds 1 millimetre, much larger than any structural length scale. We discuss the role of both the strength and the microscopic origin of the elasticity in shaping spatial correlations of the dynamics and compare our results to the behavior of jammed materials under shear.^{32–35}

II. Materials and methods

A. Time resolved correlation and photon correlation imaging

Although dynamic light scattering (DLS) is now a popular and well-established technique to probe the dynamics of soft materials,³⁶ its usefulness to measure dynamical heterogeneity has been limited until recently by the spatial and temporal averages usually involved in DLS measurements. In this section, we briefly recall the main features of a series of DLS time- and space-resolved methods that we have introduced in the past years. More details can be found in Refs 4, 29, 30, 37, 38.

Time resolved correlation (TRC). Valuable information on spatial correlations of the dynamics can be obtained in time-resolved measurements, even if they lack spatial resolution.

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Intuitively, this is due to the fact that temporal fluctuations of the dynamics are enhanced if the probed sample volume contains a limited number of statistically independent regions, as is the case when the dynamics are correlated over large distances.¹⁶ More formally, a dynamical susceptibility χ_4 can be introduced,³⁹ which quantifies temporal fluctuations of the dynamics, and which is proportional to the volume integral of the spatial correlation of the dynamics, G_4 .^{39,40} In our DLS experiments, we achieve temporal resolution by using a CCD camera as a detector and by averaging the intensity correlation function over pixels rather than over time. The CCD is placed in the far field, so that each pixel is illuminated by light issued from the whole scattering volume at a well defined scattering angle θ . The dynamics are probed on a length scale $\ell \sim 1/q$, where $q = 4\pi n\lambda^{-1}\sin(\theta/2)$ is the scattering vector and n and λ are the solvent refractive index and the in-vacuo wavelength of the laser that illuminates the sample, respectively. We measure a time-resolved intensity correlation function (proportional to the square of the dynamic structure factor), defined as

$$c_I(t, \tau) = \frac{\langle I_p(t)I_p(t + \tau) \rangle_p}{\langle I_p(t) \rangle_p \langle I_p(t + \tau) \rangle_p} - 1 \quad (1)$$

which we refer to as the degree of correlation. In eqn (1), I_p indicates the scattered intensity measured by the p -th pixel and the averages are taken over the whole CCD detector. The average dynamics and dynamical heterogeneity are quantified by

$$g_2(\tau) - 1 = \langle c_I(t, \tau) \rangle_t \quad (2)$$

$$\chi(\tau) = \text{var}[c_I(t, \tau)] = \langle c_I(t, \tau)^2 \rangle_t - \langle c_I(t, \tau) \rangle_t^2 \quad (3)$$

where averages are taken over time and where $g_2 - 1$ is the usual intensity correlation function measured in DLS, while χ is the equivalent for DLS of the dynamical susceptibility χ_4 used in numerical works. Note however that, contrary to χ_4 , χ is not normalized with respect to the number of particles in the scattering volume, a quantity not always easily accessible experimentally.

Photon correlation imaging (PCI). Spatial resolution may be achieved by modifying the collection optics so as to form an image of the scattering volume onto the CCD detector. This method, which we have termed photon correlation imaging (PCI), has been described for a low- q setup in Ref. 30. In Fig. 1 we show its implementation for $\theta = 90^\circ$ (a) and 180° (b), as in the experiments reported here. In both cases, an image of the illuminated sample is formed onto the CCD with magnification $M \sim 1$, using light scattered within a small solid angle centered around a well-defined scattering angle. The resulting image has a speckled appearance similar to that of conventional far-field scattering experiments. In practice, one adjusts the diaphragm aperture so as to roughly match the speckle size to the pixel size, which is typically of the order of 10 μm . Under these conditions, the speckle size is larger than the typical size of the scatterers ($\lesssim 1 \mu\text{m}$), which thus cannot be resolved individually. Information on the local dynamics, however, can still be obtained, because the relative motion of the scatterers results in fluctuations of the intensity of each speckle, as in regular DLS. In contrast to conventional DLS, here each speckle is illuminated by light issued from a well defined,

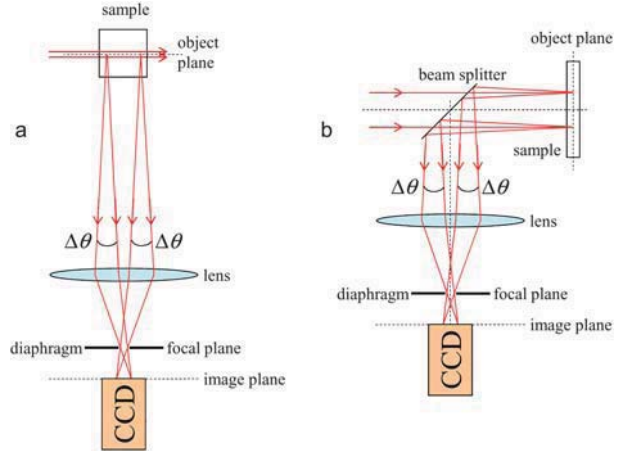


Fig. 1 A schematic of a PCI setup in two different configurations: (a) 90° scattering angle; (b) backscattering. From Ref. 30 with permission.

small region of the sample, so that spatially-resolved dynamics can be measured.

In practice, we divide the CCD images in regions of interest (ROIs), each corresponding to a small volume in the sample, and apply the TRC method separately to each ROI. We compute a space- and time-resolved degree of correlation, defined as

$$c_I(t, \tau, \mathbf{r}) = \frac{\langle I_p(t)I_p(t + \tau) \rangle_{\mathbf{r}}}{\langle I_p(t) \rangle_{\mathbf{r}} \langle I_p(t + \tau) \rangle_{\mathbf{r}}} - 1 \quad (4)$$

where the average is now over all pixels within a ROI corresponding to a small volume centered around \mathbf{r} . The ROIs must contain at least about 100 speckles for the statistical noise on the local degree of correlation to be acceptable: this limits the resolution of the method, which should be regarded as a coarse-grained technique. The main advantage of PCI is to decouple the size of the field of view (dictated by the magnification M) from the length scale ℓ over which the dynamics are probed (dictated by q and thus the scattering angle). Thus, very restrained motion can be measured with a large field of view. This is not the case for conventional imaging methods, where ℓ is a fixed fraction of the field of view.

The spatial correlation of the dynamics may be quantified by comparing the temporal evolution of the local degree of correlation calculated, for a given lag, for different locations. Traces corresponding to pairs of regions with correlated dynamics will exhibit similar fluctuations, while uncorrelated ROIs yield independent fluctuations of c_I . An example that will be discussed towards the end of this paper is given in Fig. 6. We define

$$\tilde{G}_4(\tau, \Delta\mathbf{r}) = \left\langle \frac{\langle \delta c_I(t, \tau, \mathbf{r}) \delta c_I(t, \tau, \mathbf{r} + \Delta\mathbf{r}) \rangle_t}{\sqrt{\text{var}[c_I(t, \tau, \mathbf{r})] \text{var}[c_I(t, \tau, \mathbf{r} + \Delta\mathbf{r})]}} \right\rangle_{\mathbf{r}} \quad (5)$$

where $\delta c_I = c_I - \langle c_I \rangle_t$ are the temporal fluctuations of the local dynamics. This is the analogous, albeit at a coarse grained level, of the spatial correlation of the dynamics calculated in numerical and experimental work where particle trajectories are accessible.^{13,19,32,40} In most cases, the dynamics are isotropic and we average \tilde{G}_4 over all orientations of $\Delta\mathbf{r}$.

An important point concerns the normalization of eqn (5): we recall that c_I contains a noise contribution due to the statistical

noise associated with the finite number of pixels processed for each ROI.³⁸ In PCI experiments, this contribution may be quite large, since one typically tries to reduce the size of the ROIs as much as possible in order to achieve a better spatial resolution. Distinct ROIs have uncorrelated noise; as a result, the numerator of the right hand side of eqn (5) is noise-free (except for $\Delta r = 0$), while the noise contributes to the denominator by increasing its value. Thus, at spatial lags > 0 \tilde{G}_4 is depressed because of the noise contribution, an effect that depends on the size of the ROIs used for the analysis. For systems that exhibit a finite spatial correlation of the dynamics at $\Delta r > 0$, we introduce a normalized spatial correlation of the dynamics defined as

$$G_4(\tau, \Delta \mathbf{r}) = b(\tau) \tilde{G}_4(\tau, \Delta \mathbf{r}) \quad (6)$$

where b is a time-lag dependent coefficient chosen so that $G_4 \rightarrow 1$ for $\Delta \mathbf{r} \rightarrow 0$.

B. Experimental systems

We report below PCI measurements of heterogeneous slow dynamics on a variety of systems: “artificial skin” (Vitro-corneum® by IMS Inc.), concentrated colloidal hard spheres, an “onion” gel, and a Laponite suspension. For the sake of comparison, we recall also results obtained from concentrated soft spheres and a colloidal gel, taken from Refs 31 and 30, respectively. For all systems, data are taken under single scattering conditions. The experiments on the “artificial skin” will be discussed somewhat more in depth, because (i) its behavior is representative of the main features observed for the other systems; (ii) unlike most colloidal systems where the control parameters for the slow dynamics are volume fraction and interparticle potential, in “artificial skin” the slow dynamics is controlled by the relative humidity (RH). In this respect, “artificial skin” is representative of a class of materials of biological relevance whose slow dynamics are still poorly characterized and whose visco-elastic properties change dramatically with changes in hydration, as in *stratum corneum*, the uppermost part of the epidermis of mammalian skin.^{41–43} This behavior is due to the fact that, for these materials, water acts as a plasticizer, lowering their glass transition temperature below room temperature at high RH.

The “artificial skin” is a protein-based thin film (thickness: 20–25 μm) that mimics the properties of human *stratum corneum*. We mount a piece of the film on a circular frame of 10 mm diameter to keep it flat and place it in a sealed custom-made cell that allows the relative humidity (RH) to be controlled during the PCI measurements. The desired value of the RH is imposed by placing a saturated solution of a suitable salt in a reservoir contained in the cell. We present here results for two saturated salt solutions (prepared by adding 20% more in weight fraction than the solubility limit at 20 °C), yielding a humid (RH = 62%, using KI) and a dry (RH = 12%, using LiCl) atmosphere, respectively. The measurements are performed in the backscattering geometry depicted schematically in Fig. 1b (where the RH-controlling cell is not shown for simplicity), with $\theta = 180^\circ$, corresponding to a typical probed length scale $\ell \sim 30$ nm. The imaged portion of the sample has a size of 4.288×4.288 mm² (3.752×3.752 mm²) for the dry (humid) sample; in both cases,

square ROIs of size 268×268 μm^2 were used for the PCI analysis. More details on the lags used and the duration of the experiment are given in the discussion below.

The colloidal hard sphere samples are suspensions of poly-(methyl methacrylate) spheres of radius ~ 100 nm⁴⁵ in an index matching mixture of *cis/trans*-decalin and tetralin. Their average dynamics have been reported in Refs 20 and 44. For the space-resolved measurements discussed here, we use the PCI geometry shown in Fig. 1a, where $q = 25$ μm^{-1} , and where the size of the field of view and ROIs are 2.5×0.6 mm² and 55×55 μm^2 , respectively. We present data for two volume fractions, $\phi = 0.5468$ (delay time $\tau = 20$ ms, relaxation time of the dynamic structure factor $\tau_\alpha = 0.147$ s) and $\phi = 0.5957$ ($\tau = 14$ s, $\tau_\alpha = 2350$ s). All data are taken in a regime where the dynamics are stationary.

The onion gels are concentrated surfactant solutions forming a dense packing of polydisperse, deformable spheres of average size of the order of a few μm .⁴⁶ Each sphere is constituted by a stacking of surfactant bilayers that roll up to form a multilamellar vesicle, or onion. The average dynamics and the rheological properties of the onions have been described in Refs 47 and 48; an optical microscopy investigation^{49,50} suggests that their dynamics is correlated at least up to length scales comparable to the field of view accessible in those experiments, about 1 mm. In the PCI measurements reported here, we use the 90° scattering angle geometry of Fig. 1a, with a field of view of 1.9×0.39 mm² and ROIs of size 130×130 μm^2 . The delay time is $\tau = 1000$ s, about 20 times smaller than the relaxation time of $g_2 - 1$. The dynamics slow down with time: we analyze data for $20\,000 < t < 60\,000$ s ($t = 0$ being the time at which the surfactant solution is quenched in the gel phase by a temperature jump⁴⁷).

Laponite RD (Rockwood, US) is a synthetic clay consisting of discoid charged particles. By dispersing 3.5 wt% of Laponite powder into pure water, we obtain a colloidal glassy suspension that keeps aging for several days.^{51,52} To properly weight the Laponite content, we dry the powder for 12 h in an oven at 130 °C. In order to prevent chemical corrosion, the Laponite powder is then dispersed in a pH 10 solution constituted of pure Millipore water and a proper amount of sodium hydroxide. The white dispersion is held in a magnetic stirrer for 25 min until it becomes almost transparent, and it is then injected into the scattering cell through a 1 μm filter in order to eliminate particle clusters. The sample is prepared in an inert argon atmosphere in order to prevent contact with CO₂. The scattering cell is then sealed in order to preserve this pure condition. The final step before measurements consists of a 3 min centrifugation at 3000 rpm, to eliminate small gas bubbles that may have formed during the process. This sets the age zero of the sample ($t = 0$) with an uncertainty of a few minutes. The data shown here refer to 2.0×10^5 s $< t < 2.5 \times 10^5$ s; they were taken using a special cell, as described at the end of the next section.

III. Results

As a representative example of dynamical heterogeneity in jammed systems, we first describe in some detail the behavior of “artificial skin” films. We show in Fig. 2 both the average dynamics and the dynamical susceptibility for a film in humid (RH = 62%, a) and dry (RH = 12%, b) atmospheres. The data shown here are obtained by processing the full images and by

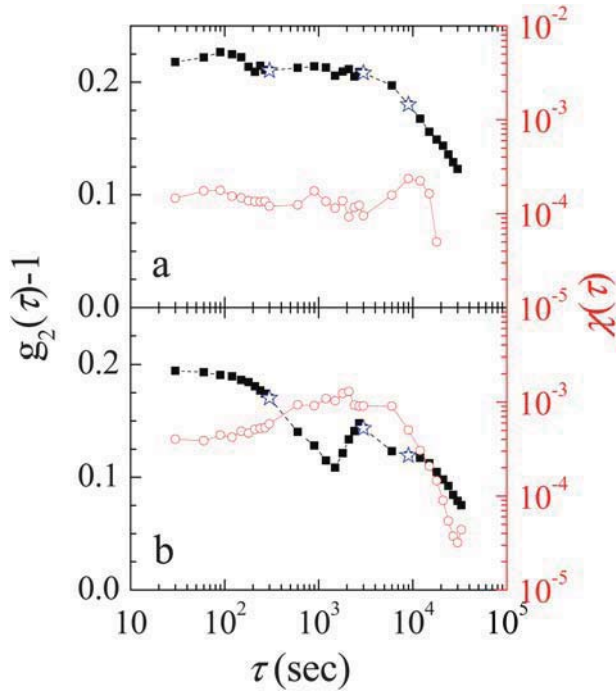


Fig. 2 The intensity–time autocorrelation function, $g_2 - 1$ (left axis, filled squares), and dynamical susceptibility, χ (right axis, open circles), for the “artificial skin” sample, as measured in the backscattering configuration schematized in Fig. 1b. (a) relative humidity = 62%; (b) relative humidity = 12%. Note the enhanced dynamical heterogeneity in the dry atmosphere, as shown by the higher values of χ . The three lags indicated by open stars are those for which the spatial correlation of the dynamics is shown in Fig. 4.

averaging over several tens of thousands of seconds (36 000 s for the sample at RH = 12% and 22 500 s for RH = 62%). The temporal intensity correlation functions (filled squares, left axis) exhibit a decay on a very long time scale, of the order of 10^4 s. For the dry sample, $g_2 - 1$ appears to be more noisy than the humid one, with an additional decay at earlier times, $\tau \approx 400$ s. This “noisiness” is due to enhanced dynamical heterogeneity, as compared to the humid sample: as discussed below, the dynamics of the dry sample are intermittent in time and correlated in space over very large distances: as a result, the temporal and spatial averages performed in calculating $g_2 - 1$ are poorer than for the humid sample. In both panels, we show also the dynamical susceptibility $\chi(\tau)$ (open circles, right axis). For the humid sample, χ depends weakly on τ , barely exhibiting a peak on the time scale of the decay of $g_2 - 1$. A peak in χ is a distinctive feature of dynamical heterogeneity,^{13,22,38,40} while the noise contribution to the dynamical susceptibility is essentially flat for time delays smaller than the decay time of the intensity correlation function.^{37,38} Thus, the data in Fig. 2a suggest that the dynamics for the humid sample are mildly heterogeneous and that the noise contribution dominates the measured χ , with the exception of the small peak around $\tau = 10^4$ s. By contrast, the dynamical susceptibility of the dry sample presents a well-developed peak, about a factor of three higher than the short- τ value of the dynamical susceptibility and more than a decade higher than χ at large delay times. This suggests that the dynamics of the dry sample are highly heterogeneous.

In order to gain further insight on the nature of the dynamical heterogeneity of “artificial skin”, we plot in Fig. 3 the temporal evolution of the degree of correlation, c_I , calculated for a time delay much smaller than the relaxation time of g_2 ($\tau = 150$ and 90 s for the humid and dry sample, respectively). We focus on small delays because this allows us to capture better the impact of individual rearrangement events, since, at larger τ , several events may occur in between two images. The signals shown here have been calculated for an individual ROI, but are representative of the general behavior of all ROIs. For the humid sample, c_I exhibits modest fluctuations symmetrically distributed around its mean value (panel a). Moreover, the probability distribution function (PDF) of c_I , shown in panel b, is close to Gaussian. We have shown in previous work^{29,37,38} that this is typical of a signal dominated by the measurement noise, which is particularly high when the degree of correlation is calculated over the limited number of pixels of a small portion of the image, as required by a space-resolved analysis. Panels c and d show c_I and its PDF, respectively, for the dry sample. In contrast to the humid film, sudden drops of the degree of correlation can be easily observed, corresponding to sudden rearrangement events in the sample. As a result, the PDF of the degree of correlation is skewed, with a tail associated with the intermittent drops of c_I . In other systems, the shape of the PDF has been shown to be well fitted by a Gumbel distribution,³⁸ often observed in the statistics of rare events in systems with extended spatial and temporal correlations.⁵³ Here, the dynamics were too slow to allow us to accumulate enough statistics to make any quantitative statement on the shape of the PDF. We note however that the analysis of the temporal evolution of c_I and its PDF confirms the differences between the two samples discussed in relation to Fig. 2: the dynamics of the dry sample are much more heterogeneous than those of the humid one.

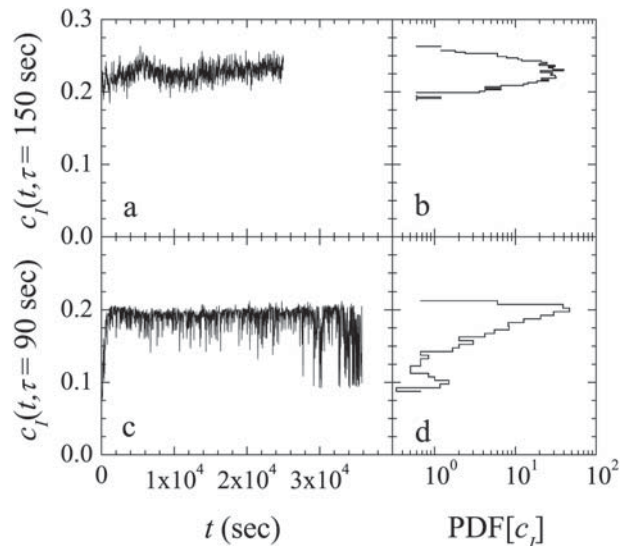


Fig. 3 For a representative ROI, degree of correlation c_I at a fixed delay τ as a function of time and its PDF for the “artificial skin” in humid (RH = 62%, $\tau = 150$ s, panels a and b) and dry (RH = 12%, $\tau = 90$ s, panels c and d) atmosphere. Note that the dry sample exhibits large temporal fluctuations.

Since the dynamics measured on the full field of view (Fig. 2) exhibit significant fluctuations, we expect them to be spatially correlated over macroscopic distances. The spatial correlation of the dynamics calculated according to eqns (5) and (6) is shown in Fig. 4, for the two samples, and for the three time lags indicated by open stars in Fig. 2. Quite generally, G_4 is significantly larger than zero up to distances of the order of 1 mm (for the humid sample) or even several mm (for the dry sample). This is remarkable, since all relevant structural length scales are much smaller. Furthermore, the range of the spatial correlations of the dynamics is much longer for the dry sample than for the humid one; together with the enhanced intermittency under dry conditions seen in Fig. 3, this explains why the dynamical susceptibility of the dry sample is higher than that of the wet one, as shown in Fig. 2. Interestingly, the time lag dependence of G_4 is different for the two values of RH. At high RH, the range of G_4 is maximum at intermediate time delays and decreases at small and large τ . This is similar to what is reported in numerical work on supercooled molecular glass formers⁴⁰ and experiments on grains,¹⁴ suggesting that dynamical heterogeneity progressively builds up with time, starting from individual events that are relatively limited in size. Eventually, at very large time lags, one expects G_4 to decay on short length scales, since many uncorrelated events will have occurred everywhere in the sample. The shorter range of G_4 at $\tau = 9000$ s observed in Fig. 4a probably corresponds to the onset of this large τ regime. For the dry sample in panel b, G_4 is highly correlated over a very long range for essentially all probed lags, indicating that individual events extend over several millimetres. We don't currently have an explanation for the somehow faster decay of G_4 at intermediate lags; the long range

of G_4 at the largest probed lag ($\tau = 9000$ s) indicates that on this time scale the regime where many uncorrelated events have occurred throughout the sample is not yet attained. Longer lags could not be reliably analyzed due to the limited duration of the experiment.

Summarizing, the dynamics of the “artificial skin” are markedly heterogeneous under dry conditions, associated with intermittent rearrangement events. These events imply the motion of the scatterers over just a few nanometres (we recall that the full decay of $g_2 - 1$ corresponds to displacements of the order of 30 nm); however, whenever they occur, they impact essentially the whole sample, since the spatial correlation of the dynamics extends over several mm. For the humid sample, dynamical heterogeneities are less pronounced; the range of spatial correlations, although reduced in comparison to that of the dry sample, is still of the order of 1–2 mm, much larger than any structural length scale in the sample. The change in dynamical behavior under different RH conditions observed here for the “artificial skin” is related to the loss of rigidity upon hydration and is reminiscent of the sensitivity to humidity of biological tissues. Indeed, humidity plays a key role in controlling biomechanical properties of *stratum corneum*,⁵⁴ whose elastic modulus, e.g., increases by several orders of magnitude with decreasing RH.^{42,43}

One may wonder whether similar dynamical features are observed also in other glassy or jammed soft matter systems that, similarly to the “artificial skin”, are characterized by ultraslow dynamics and a viscoelastic behavior where the solid-like response dominates. To address this question, we plot in Fig. 5 the spatial correlation function of the dynamics of a series of systems: concentrated hard spheres at the onset of the supercooled regime and in the deep supercooled regime, soft spheres below and above random close packing (data taken from Ref. 31), an onion gel, a colloidal gel (data taken from Ref. 30), and the dry “artificial skin” film already shown in Fig. 2. With

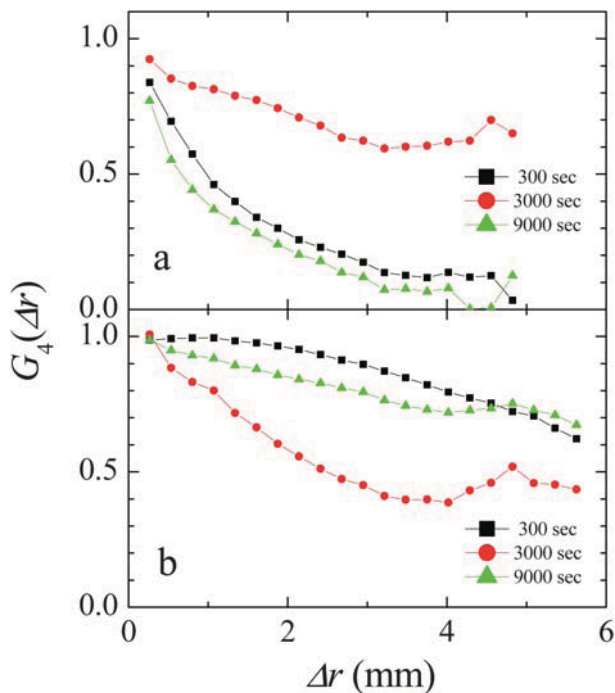


Fig. 4 Spatial correlation of the dynamics, $G_4(\Delta r)$, for the “artificial skin” samples in humid (RH = 62%, a) and dry (RH = 12%, b) atmosphere. The curves are labeled by the temporal lag at which the dynamics were probed.

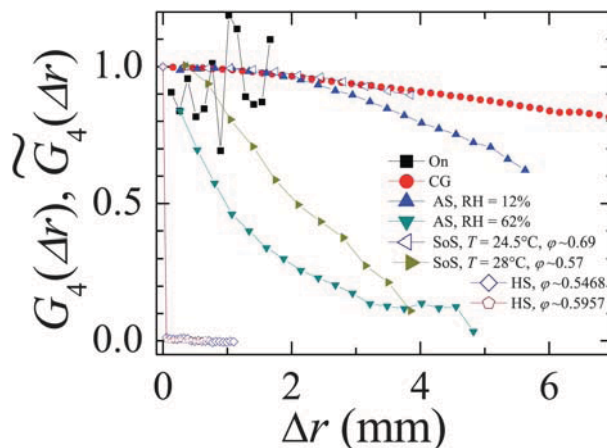


Fig. 5 Spatial correlation of the dynamics for all systems that we have studied except for Laponite, as indicated by the label (On: onion gel; CG: colloidal gel, from Ref. 30; AS: “artificial skin”, $\tau = 300$ s; SoS: soft spheres, from Ref. 31; HS: hard spheres). Data for Laponite are shown in Fig. 6 below. All spatial correlation functions have been normalized according to eqn (6), except for the hard spheres, for which \tilde{G}_4 is shown (see eqn (5)), rather than G_4 .

the exception of the soft spheres and the colloidal gel, for which data were taken in a low-angle configuration ($q \sim 1 \mu\text{m}^{-1}$), all data are collected either at $\theta = 90^\circ$ or 180° . For all samples, we calculate the spatial correlation of the dynamics at a time lag τ much shorter than the relaxation time of the corresponding $g_2 - 1$, in order to capture as much as possible the characteristics of single events. Quite generally, very long range correlations of the dynamics are observed for all samples, up to several mm, once again much larger than any structural length scale and comparable to the system size. In particular, data for the onions, albeit somewhat noisy due to the relatively small number of available pixels and the limited duration of the experiment (about twice the relaxation time of $g_2 - 1$), confirm and extend the long-range correlation of the dynamics observed, for a smaller field of view, by microscopy.^{49,50} Even for the “artificial skin” under humid conditions and the less compressed soft sphere system ($T = 28^\circ\text{C}$), where G_4 decreases more rapidly than for the other systems, spatial correlations still extend over macroscopic length scales. The only exceptions are the hard spheres samples. For these systems, \tilde{G}_4 drops to zero as soon as $\Delta r > 0$; although we show here data at τ much smaller than the relaxation time of $g_2 - 1$, we point out that a similar behavior is found at all τ . Since the normalization method described in Sec. 2.1 can not be applied, we represent \tilde{G}_4 rather than G_4 as for the other samples. For the less concentrated hard sphere suspension, such a sharp drop of \tilde{G}_4 is not surprising, since no spatial correlation of the dynamics are to be expected at the onset of the supercooled regime. Indeed, at $\phi = 0.5468$ the dynamics is slower than in the $\phi \rightarrow 0$ limit by a relatively modest factor of 100, and the shape of the dynamic structure factor differs only marginally from that in the diluted case.²⁰ For the most concentrated hard sphere sample, by contrast, the system relaxation is already slowed down by a factor of about 10^7 compared to the $\phi \approx 0$ limit and a fully developed plateau is observed in the dynamic structure factor, revealing caging and glassy dynamics.^{20,44} It has been proposed that such a dramatic slow down of the dynamics is associated with the growth of spatial correlations of the dynamics. Previous experiments, both by confocal microscopy¹⁹ and dynamic light scattering,^{6,20} indicate that the range, ξ , of such correlations does not exceed a few particles sizes, *i.e.* a few μm in our case. Therefore, the absence of any measurable correlation in our PCI experiment, where the smallest accessible spatial lag is $55 \mu\text{m}$, is fully consistent with previous results. On the one hand, this negative result illustrates the limitations intrinsic to PCI, a coarse grained method. On the other hand, it highlights the dramatic difference between the dynamics of supercooled, stationary hard spheres and those of the other jammed, out-of-equilibrium samples, for which macroscopic spatial correlations of the dynamics are observed.

The results shown here suggest that system-size correlations of the dynamics are ubiquitous in fully jammed systems, where the solid-like behavior of the sample dominates over its viscous response. Indeed, in a material that is essentially solid-like, any deformation due to a local rearrangement will propagate very far before being substantially damped, leading to extended spatial correlations of the dynamics. Another (less attractive) explanation of the dynamical fluctuations reported here could be that they are due to some kind of artifact. In fact, one should be aware that measuring fluctuations in a reliable fashion is much more difficult than just probing the average dynamics, and many

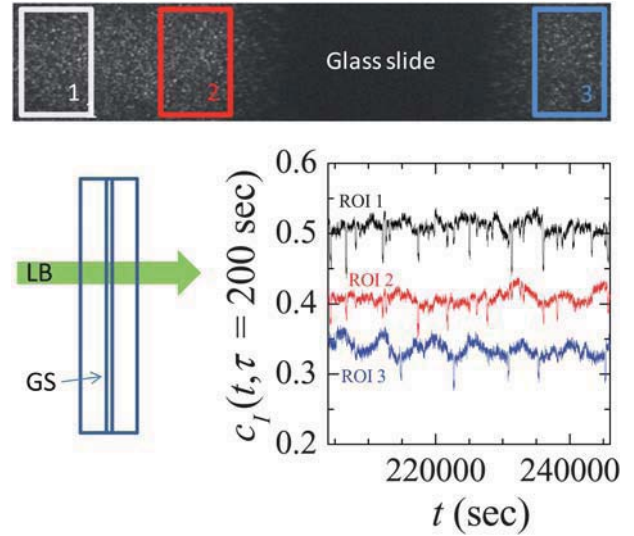


Fig. 6 Bottom left: a schematic side view of the cell used for the experiment on Laponite. LB: laser beam, GS: glass slide. Top: a typical CCD image of the scattering volume. The dark region corresponds to the thickness of the glass slide, view from the side. The three ROIs for which the degree of correlation is shown in the bottom right plot are highlighted. The size of the imaged region is $2.62 \times 0.52 \text{ mm}^2$. Bottom right: the time dependence of c_l , for a delay time $\tau = 200 \text{ s}$, for the three ROIs shown above. For the sake of clarity, the curves of ROIs 1 and 2 have been offset vertically by 0.2 and 0.1, respectively. Note that the signals measured on the same side of the glass slide (ROIs 1 and 2) are correlated, while signals from opposite sides are uncorrelated.

spurious effects have to be controlled and ruled out (for a discussion of some possible sources of artifacts, such as temperature fluctuations and laser beam pointing instabilities, see also Ref. 38). In order to address the role of the elastic propagation of a strain field and to demonstrate the genuine nature of the spatial correlations observed here, we discuss briefly an experiment performed on a Laponite sample using a specially devised cell.

The cell is a cylindrical tube of inner diameter $\approx 10 \text{ mm}$ (see Fig. 6), with a microscope glass slide glued in the interior with epoxy, so as to separate the cell into two chambers. Because the glass slide is cut unevenly and does not perfectly fit the cell walls, the two chambers are in contact through openings of size $\approx 1 \text{ mm}$, so that the sample contained in the two chambers is fully equilibrated and experiences exactly the same conditions. The laser beam impinges perpendicularly to the glass slide, thereby illuminating both chambers, and the scattering volume is imaged at an angle $\theta = 90^\circ$, as in the geometry shown in Fig. 1a. We calculate the local c_l for larger-than-usual ROIs, in order to reduce the noise contribution (see Fig. 6). From the plot in Fig. 6, it is clear that the time evolution of the degree of correlation measured on the same side of the glass slide is highly correlated (ROIs 1 and 2, separated by $\Delta r = 0.57 \text{ mm}$), since most of the downward spikes corresponding to sudden rearrangement events are co-occurrent. Indeed, \tilde{G}_4 calculated from the signals for ROIs 1 and 2 is as high as 0.394 (we recall that \tilde{G}_4 is affected by the noise contribution, so that an even higher value would be observed in the absence of noise). By contrast, the events recorded in ROI 3, on the opposite side of the glass slide, appear

Table 1 The rheological parameters of most of the system shown in Fig. 5 and 6. The sample names are as in the caption of Fig. 5

	ν/Hz	$G'(\nu)/\text{Pa}$	$G'(\nu)/G''(\nu)$	Ref.
On	1	600	15	48
CG	1	$\sim 0.9 \times 10^{-3}$	10	59
SoS, $\varphi = 0.57$	1.6	0.6	0.3	31
SoS, $\varphi = 0.69$	1.6	20	8	31
HS, $\varphi = 0.5468$	1	40	1.1	60,61
HS, $\varphi = 0.5957$	1	>80	>1.4	60,61
Laponite	0.7	≥ 300	20	55,56

to be uncorrelated with respect of those of ROIs 1 and 2, as confirmed by low values of the correlation (e.g., $\tilde{G}_4 = -0.015$ when correlating the signals from ROIs 2 and 3).

This experiment demonstrates that the downward spikes observed in c_I cannot be due to some mechanical, temperature or laser beam instability, since they occur independently on either side of the glass slide. On the other hand, the data of Fig. 6 support the idea that the propagation of a strain field in a predominantly elastic medium is responsible for long range spatial correlations. Indeed, such a strain field cannot propagate through the rigid glass slide, so that the dynamical activity in the two chambers is uncorrelated, while the one in a given chamber is correlated.

IV. Discussion

To better understand the relationship between the viscoelastic properties and spatial correlations of the dynamics, we examine published rheological data for most of the systems investigated here and summarize the relevant rheological parameters in Table 1, where we choose, somehow arbitrarily, $\nu \sim 1$ Hz as a reference frequency for comparing different systems. Oscillatory rheology experiments for the onion gels⁴⁸ show that both the storage, $G'(\nu)$, and loss, $G''(\nu)$, moduli are essentially frequency-independent in the range $4 \times 10^{-3} \text{ Hz} < \nu < 10 \text{ Hz}$, and that $G' \sim 600$ Pa dominates over G'' by a factor of ~ 15 . Similar results are obtained for the Laponite suspension⁵⁵ and for the colloidal gels⁵⁷. Note that the magnitude of the elastic modulus of the colloidal gel ($G' \sim 4.4 \times 10^{-4} - 1.5 \times 10^{-3} \text{ Pa}$ ⁵⁷⁻⁵⁹) is lower than that of the onion gel and of the Laponite suspension by at least 5 orders of magnitude, implying that the absolute value of G' is not a relevant parameter in determining the range of spatial correlations of the dynamics. A systematic investigation of the shear moduli of the soft particles is presented in Ref. 31. For the most concentrated sample reported in Fig. 5 above, one finds that G' and G'' are nearly frequency-independent and that the former is larger than the latter by almost a factor of 10. By contrast, for the less concentrated sample both moduli are comparable (see panels (a) and (b) of Fig. 3 of Ref. 31), revealing a complex viscoelastic behavior where neither the solid-like nor the fluid-like character prevail. Since spatial correlations of the dynamics are shorter-ranged in the less concentrated sample, these observations are consistent with the notion that a fully developed elastic behavior is a necessary condition for long-range spatial correlations of the dynamics. The same trend is likely to hold for the “artificial skin”. Indeed, we find that the range of the spatial correlation of the dynamics increases as the RH decreases. Although no rheology data are available for the “artificial skin”, it is worth noting that in *stratum corneum*,^{42,43} a material whose

properties the Vitro-corneum® film is designed to mimic, the elastic modulus grows by almost 3 orders of magnitude when the RH decreases from 100% to 30%.

Collectively, these results indicate that systems with long-ranged spatial correlations of the dynamics have a solid-like behavior. A close inspection of rheology data for hard sphere suspensions, for which we recall that ξ is limited to a few particle sizes at most, show that the reverse is not true. Mason and Weitz have measured the shear moduli of supercooled hard spheres.⁶⁰ Care must be taken in applying their results to our hard sphere samples, due to the unavoidable uncertainties in the determination of the absolute volume fraction.^{44,62} A generally accepted approach consists in considering the separation, $\varepsilon = (\varphi_c - \varphi)/\varphi_c$, with respect to the location φ_c of the (apparent) divergence of the relaxation time as obtained from a mode coupling theory fit of $\tau_\alpha(\varphi)$ (in our work, $\varphi_c \approx 0.59$,²⁰ while $\varphi_c \approx 0.575$ in Ref. 60). For our most dilute sample, $\varphi = 0.5468$ and $\varepsilon \approx 0.07$, corresponding roughly to the data for $\varphi = 0.53$ in Ref. 60. At that volume fraction, G' and G'' have approximately equal magnitude in all the accessible frequency range, similar to the case of our soft spheres at $\varphi = 0.57$. However, no spatial correlation of the dynamics is observed in the hard spheres at $\varphi = 0.5468$, while $\xi \sim 2$ mm for the soft spheres at $\varphi = 0.57$. This difference is even more striking if we consider our most concentrated hard sphere sample, for which ξ is limited to a few particle sizes,²⁰ although the sample is solid-like (G' dominates over G'') and the magnitude of its elastic modulus⁶¹ is comparable to that of the Laponite suspension, which exhibits systems-size dynamical correlations.

Our measurements thus indicate that, while elasticity is a necessary condition for observing extended spatial correlations of the dynamics, it is not a sufficient one. The microscopic origin of the elasticity must also play a crucial role: the differences discussed above suggest that ξ is modest in systems where the elasticity has an entropic origin, as for the hard spheres, and no long-lived network of contacts exists. By contrast, ξ is very large in systems where elasticity has an enthalpic origin, be it due to the bending rigidity of the protein filament network in “artificial skin” and the backbone in diluted gels made of strongly attractive particles, or to the bulk elasticity of squeezed particles, as in the soft spheres and the onions. Note that the Laponite suspension also falls into the latter category: while the platelets are not in direct contact, they interact *via* a screened Coulombic repulsive potential and can thus be effectively regarded as squeezed soft particles. Interestingly, recent work⁶³ has identified a structural length scale that controls the mechanical properties of attractive colloidal systems: this length scale is of the order of the particle size for hard spheres, while it grows as short-ranged attractive interactions become increasingly important, as in colloidal gels. Our data suggest that this behavior may be mirrored by a similar growth of ξ . In repulsive, squeezed systems, the same role is presumably played by a persistent network of interparticle forces, such as that visualized by confocal microscopy in compressed emulsions.⁶⁴

In view of the above discussion, it is natural to compare our results to numerical and experimental work on driven jammed systems. In these works, the sample is sheared by imposing either a continuous deformation or a sinusoidal one. The dynamics are quantified by the particle displacements perpendicular to the shear direction or after subtracting the affine component (for

a continuous shear), or by comparing successive configurations at zero deformation (for oscillatory shear). For a 2D granular medium sheared at a finite shear rate, Lechenault *et al.*³² find that a spatial correlation function analogous to our G_4 decays on a length scale ξ_4 of the order of ten particle sizes at the jamming transition, and that this length decreases upon further compression, although only a restrained range of densities above jamming could be probed, due to the particle stiffness. Simulations of sheared soft disks³³ indicate that above the jamming transition and at finite shear stress, σ , ξ remains moderate, but a scaling analysis suggests that ξ diverges in the limit $\sigma \rightarrow 0$ for all densities above jamming. This is confirmed by quasi-static shear simulations of jammed soft particles,^{34,35} where it is shown that spatial correlations of the dynamics above jamming are limited only by the system size.

Therefore, the dynamical behavior reported here appears to be due to the connected nature of the materials investigated, where a strain field can propagate over very large distances, as in fully jammed systems sheared at a vanishingly small rate. A related issue, still open, concerns the microscopic origin of the dynamics. The systems studied in Refs 32–35 are athermal, with no dynamics in the absence of an external driving. Although the systems presented here are thermal and no external drive is applied to them, it is unlikely that thermal motion alone is responsible for their dynamics in the jammed state. This is illustrated, *e.g.*, by the volume fraction dependence of the dynamics reported for the soft spheres of Ref. 31. In the supercooled regime, the relaxation time, τ_c , grows sharply with ϕ , as in hard sphere systems. Above random close packing, a different regime sets in, where τ_c grows very slowly with ϕ . Thus, above jamming, the relaxation time is orders of magnitude smaller than what is expected by extrapolating the behavior in the supercooled regime, strongly suggesting that an additional relaxation mechanism has set in. We propose that, quite generally, the relaxation of internal stress may be such a mechanism in jammed soft matter. This is an appealing explanation, since it would be consistent with the observed ultra-long range correlations of the dynamics. However, this conjecture still awaits for a direct experimental proof.

V. Conclusions

We have presented direct measurements of the correlation length of the slow dynamics of a variety of glassy and jammed soft systems, obtained using the recently introduced PCI method. This technique allows one to measure coarse grained maps of the dynamical activity of a sample. Its main advantage consists in the possibility of probing motion on a very small length scale, yet for a very large field of view. This is an attractive feature for jammed systems, where motion is very restrained, but highly spatially correlated. Additionally, the technique does not require individual particles to be imaged; accordingly, it can be applied to systems for which direct visualization by optical or confocal microscopy is not possible, including turbid samples as, *e.g.*, foams.⁶⁵

We find that in deeply jammed systems ξ is quite generally very large, typically of the order of the system size. This is in striking contrast with the modest correlation lengths measured in glass formers, including colloidal hard spheres. An analysis of the

viscoelastic properties of the various systems investigated here shows that a well-developed elasticity ($G' > G''$) always accompanies the presence of long-ranged spatial correlations of the dynamics, regardless of the absolute magnitude of the elastic modulus. The reverse, however, is not true, as exemplified by concentrated hard sphere suspensions, whose macroscopic rheological response is predominantly solid-like, whereas the correlation length of the dynamics is limited to a few particle sizes. These results highlight the crucial role of the microscopic origin of elasticity (entropic vs. enthalpic) in determining the range of spatial correlations of the dynamics. Further work will be needed to thoroughly test these ideas, for example by continuously varying the strength of attractions in dense colloidal suspensions, so as to progressively change the nature of the elasticity⁶³ and, presumably, the correlation length ξ .

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References

- 1 L. Cipelletti and L. Ramos, *J. Phys.: Condens. Matter*, 2005, **17**, R253–R285.
- 2 W. K. Kegel and A. van Blaaderen, *Science*, 2000, **287**, 290–293.
- 3 E. R. Weeks, J. C. Crocker, A. C. Levitt, A. Schofield and D. A. Weitz, *Science*, 2000, **287**, 627–631.
- 4 L. Cipelletti, H. Bissig, V. Trappe, P. Ballesta and S. Mazoyer, *J. Phys.: Condens. Matter*, 2003, **15**, S257–S262.
- 5 R. Sarcia and P. Hebraud, *Phys. Rev. E: Stat., Nonlinear, Soft Matter Phys.*, 2005, **72**, 011402–011405.
- 6 L. Berthier, G. Biroli, J. P. Bouchaud, L. Cipelletti, D. El Masri, D. L’Hôte, F. Ladieu and M. Pierno, *Science*, 2005, **310**, 1797–1800.
- 7 Y. Gao and M. L. Kilfoil, *Phys. Rev. Lett.*, 2007, **99**, 078301.
- 8 C. J. Dibble, M. Kogan and M. J. Solomon, *Phys. Rev. E: Stat., Nonlinear, Soft Matter Phys.*, 2008, **77**, 050401.
- 9 P. Ballesta, A. Duri and L. Cipelletti, *Nat. Phys.*, 2008, **4**, 550–554.
- 10 A. Duri and L. Cipelletti, *Europhys. Lett.*, 2006, **76**, 972–978.
- 11 S. C. Glotzer, *J. Non-Cryst. Solids*, 2000, **274**, 342–355.
- 12 M. D. Ediger, *Annu. Rev. Phys. Chem.*, 2000, **51**, 99–128.
- 13 O. Dauchot, G. Marty and G. Biroli, *Phys. Rev. Lett.*, 2005, **95**, 265701.
- 14 R. Candellier, O. Dauchot and G. Biroli, *Phys. Rev. Lett.*, 2009, **102**, 088001.
- 15 A. S. Keys, A. R. Abate, S. C. Glotzer and D. J. Durian, *Nat. Phys.*, 2007, **3**, 260–264.
- 16 A. R. Abate and D. J. Durian, *Phys. Rev. E: Stat., Nonlinear, Soft Matter Phys.*, 2007, **76**, 021306.
- 17 P. Mayer, H. Bissig, L. Berthier, L. Cipelletti, J. P. Garrahan, P. Sollich and V. Trappe, *Phys. Rev. Lett.*, 2004, **93**, 115701.
- 18 P. N. Pusey and W. Vanmegen, *Nature*, 1986, **320**, 340–342.
- 19 E. R. Weeks, J. C. Crocker and D. A. Weitz, *J. Phys.: Condens. Matter*, 2007, **19**, 205131.
- 20 G. Brambilla, D. El Masri, M. Pierno, L. Berthier, L. Cipelletti, G. Petekidis and A. B. Schofield, *Phys. Rev. Lett.*, 2009, **102**, 085703–085704.
- 21 C. Dalle-Ferrier, C. Thibierge, C. Alba-Simionesco, L. Berthier, G. Biroli, J. P. Bouchaud, F. Ladieu, D. L’Hôte and G. Tarjus, *Phys. Rev. E: Stat., Nonlinear, Soft Matter Phys.*, 2007, **76**, 041510.
- 22 S. Karmakar, C. Dasgupta and S. Sastry, *Proc. Natl. Acad. Sci. U. S. A.*, 2009, **106**, 3675.

- 23 R. D. Kamien and A. J. Liu, *Phys. Rev. Lett.*, 2007, **99**, 155501.
- 24 L. Berthier and T. A. Witten, *Europhys. Lett.*, 2009, **86**, 10001.
- 25 L. Berthier and T. A. Witten, *Phys. Rev. E: Stat., Nonlinear, Soft Matter Phys.*, 2009, **80**, 021502.
- 26 N. Xu, T. K. Haxton, A. J. Liu and S. R. Nagel, *Phys. Rev. Lett.*, 2009, **103**, 245701.
- 27 Z. Zhang, N. Xu, D. T. N. Chen, P. Yunker, A. M. Alsayed, K. B. Aptowicz, P. Habdas, A. J. Liu, S. R. Nagel and A. G. Yodh, *Nature*, 2009, **459**, 230.
- 28 H. Jacquin and L. Berthier, *Soft Matter*, 2010, **6**, 2970.
- 29 H. Bissig, S. Romer, L. Cipelletti, V. Trappe and P. Schurtenberger, *PhysChemComm*, 2003, **6**, 21–23.
- 30 A. Duri, D. A. Sessoms, V. Trappe and L. Cipelletti, *Phys. Rev. Lett.*, 2009, **102**, 085702–085704.
- 31 D. A. Sessoms, I. Bischofberger, L. Cipelletti and V. Trappe, *Philos. Trans. R. Soc. London, Ser. A*, 2009, **367**, 5013–5032.
- 32 F. Lechenault, O. Dauchot, G. Biroli and J. P. Bouchaud, *Europhys. Lett.*, 2008, **83**, 46003.
- 33 P. Olsson and S. Teitel, *Phys. Rev. Lett.*, 2007, **99**, 178001.
- 34 C. Heussinger and J.-L. Barrat, *Phys. Rev. Lett.*, 2009, **102**, 218303.
- 35 C. Heussinger, L. Berthier and J.-L. Barrat, *Europhys. Lett.*, 2010, **90**, 20005.
- 36 B. J. Berne and R. Pecora, *Dynamic Light Scattering*, Wiley, New York, 1976.
- 37 A. Duri, P. Ballesta, L. Cipelletti, H. Bissig and V. Trappe, *Fluctuation Noise Lett.*, 2005, **5**, L1–L15.
- 38 A. Duri, H. Bissig, V. Trappe and L. Cipelletti, *Phys. Rev. E: Stat., Nonlinear, Soft Matter Phys.*, 2005, **72**, 051401–051417.
- 39 S. Franz *et al.*, *Philos. Mag. B*, 1999, **79**, 1827; S. Franz and G. Parisi, *J. Phys.: Condens. Matter*, 2000, **12**, 6335.
- 40 N. Lacevic, F. W. Starr, T. B. Schroder, V. N. Novikov and S. C. Glotzer, *Phys. Rev. E: Stat., Nonlinear, Soft Matter Phys.*, 2002, **66**, 030101.
- 41 A. V. Rawlings, *Exog. Dermatol.*, 2004, **3**, 57–71.
- 42 A. C. Park and C. B. Baddiel, *J. Soc. Cosmet. Chem*, 1972, **23**, 3–12.
- 43 A. C. Park and C. B. Baddiel, *J. Soc. Cosmet. Chem*, 1972, **23**, 13–21.
- 44 D. El Masri, G. Brambilla, M. Pierno, G. Petekidis, A. Schofield, L. Berthier and L. Cipelletti, *J. Stat. Mech.: Theory Exp.*, 2009, **2009**, P07015.
- 45 G. Brambilla, D. El Masri, M. Pierno, L. Berthier, L. Cipelletti, G. Petekidis and A. Schofield, *Phys. Rev. Lett.*, 2010, **104**, 169602.
- 46 L. Ramos, D. Roux, P. D. Olmsted and M. E. Cates, *Europhys. Lett.*, 2004, **66**, 888–894.
- 47 L. Ramos and L. Cipelletti, *Phys. Rev. Lett.*, 2001, **87**, 245503.
- 48 L. Ramos and L. Cipelletti, *Phys. Rev. Lett.*, 2005, **94**, 158301.
- 49 S. Mazoyer, L. Cipelletti and L. Ramos, *Phys. Rev. Lett.*, 2006, **97**, 238301.
- 50 S. Mazoyer, L. Cipelletti and L. Ramos, *Phys. Rev. E: Stat., Nonlinear, Soft Matter Phys.*, 2009, **79**, 011501–011510.
- 51 A. Mourchid, A. Delville, J. Lambard, E. Lecolier and P. Levitz, *Langmuir*, 1995, **11**, 1942–1950.
- 52 A. Knaebel, M. Bellor, J.-P. Munch, V. Viasnoff, F. Lequeux and J. L. Harden, *Europhys. Lett.*, 2000, **52**, 73–79.
- 53 S. T. Bramwell, K. Christensen, J.-Y. Fortin, P. C. W. Holdsworth, H. J. Jensen, S. Lise, J. M. Lopez, M. Nicodemi, J.-F. Pinton and M. Sellitto, *Phys. Rev. Lett.*, 2000, **84**, 3744–3747.
- 54 A. V. Rawlings, J. J. Leyden, *Skin Moisturization*, Marcel Dekker Inc., New York, 2002.
- 55 S. Jabbari-Farouji, M. Atakhorrami, D. Mizuno, E. Eiser, G. H. Wegdam, F. C. MacKintosh, D. Bonn and C. F. Schmidt, *Phys. Rev. E: Stat., Nonlinear, Soft Matter Phys.*, 2008, **78**, 061402.
- 56 The data $G' = 300$ Pa and $G'/G'' = 20$ taken from Ref. 55 are for a suspension at 3.2 wt%, instead of 3.5 wt% as in our experiments. From Ref. 55, we estimate that the elastic modulus increases by a factor ~ 1.5 when the concentration increases from 3.2 wt% to 3.5 wt%.
- 57 T. Gisler and D. A. Weitz, *Phys. Rev. Lett.*, 1999, **82**, 1064.
- 58 A. H. Krall and D. A. Weitz, *Phys. Rev. Lett.*, 1998, **80**, 778.
- 59 The moduli of the very diluted colloidal gel studied here ($\phi = 6 \times 10^{-4}$) are too weak to be measured by mechanical rheology. Estimates of the elastic modulus vary between 4.4×10^{-4} Pa and 1.5×10^{-3} Pa depending on whether they are obtained from DLS measurements⁵⁸ or by extrapolating mechanical rheology data⁵⁷ taken at larger ϕ . In Table 1, we use data at $\phi = 8.9 \times 10^{-3}$ from Ref. 57 to estimate G'/G'' .
- 60 T. G. Mason and D. A. Weitz, *Phys. Rev. Lett.*, 1995, **75**, 2770.
- 61 In order to account for the difference in particle size ($a = 105$ and 210 nm in Refs 20 and 60, respectively), in Table 1 we multiply the G' data of Ref. 60 by a factor $(210/105)^3$, due to the scaling $G' \sim K_B T / a^3$. Note that the density of our most concentrated hard sphere sample is higher than that of the densest suspension studied in Ref. 60, even when considering the difference in ϕ_c . Accordingly, the values of G' and G'/G'' reported in Table 1 should be regarded as lower bounds.
- 62 P. N. Segre, S. P. Meeker, P. N. Pusey and W. C. K. Poon, *Phys. Rev. Lett.*, 1996, **77**, 585–585.
- 63 A. Zaccone, H. Wu and E. Del Gado, *Phys. Rev. Lett.*, 2009, **103**, 208301.
- 64 J. Brujic, S. F. Edwards, D. V. Grinev, I. Hopkinson, D. Brujic and H. A. Makse, *Faraday Discuss.*, 2003, **123**, 207–220.
- 65 D. Sessoms, H. Bissig, A. Duri, L. Cipelletti and V. Trappe, *Soft Matter*, 2010, **6**, 3030.