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Quantitative analysis of X-band weather radar attenuation correction accuracy

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Abstract. At short wavelengths, especially C-, X-, and Kband, weather radar signals are attenuated by the precipitation along their paths. This constitutes a major source of error for radar rainfall estimation, in particular for intense precipitation. A recently developed stochastic simulator of range profiles of raindrop size distributions (DSD) provides a controlled experiment framework to investigate the accuracy and robustness of attenuation correction algorithms. The work presented here focuses on the quantification of the influence of uncertainties concerning radar calibration, the parameterization of power law relations between the integral variables (radar reflectivity Z and specific attenuation k), and total path integrated attenuation (PIA) estimates at X-band. The analysis concerns single frequency, incoherent and nonpolarimetric radar systems. Two attenuation correction algorithms, based on a forward and a backward implementation respectively, are studied. From DSD range profiles, the corresponding profiles of integral radar variables are derived. Using a Monte Carlo approach, the accuracy and robustness of the two algorithms are quantified for the different sources of error previously mentioned. This framework of realistic DSD variability provides a robust way to confirm that, under realistic assumptions concerning the PIA estimation uncertainty, the forward algorithm outperforms the backward algorithm for PIA values below 10 dB.

1 Introduction

The space-time variability of rainfall is an important issue in a number of areas, e.g., hydrology, meteorology, and natural hazards. Weather radar is in principle able to provide quantitative estimates of rainfall fields with a high spatial and temporal resolution. Recently, there has been an increased

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interest in radars operating at short wavelengths, roughly from 1 to 5 cm. Examples are X-band radar networks (e.g., CASA, [http://www.casa.umass.edu\)](http://www.casa.umass.edu) and K-band radars operating from spaceborne platforms (e.g., the TRMM and GPM satellites). Even many operational radar networks across Europe operate at relatively short wavelengths (C-band). At such wavelengths, the attenuation of the radar signal by the precipitation along its path is a critical issue for quantitative radar rainfall estimates that has been recognized for a long time (e.g., [Atlas and Banks,](#page-5-0) [1951\)](#page-5-0). A recently developed stochastic simulator of range profiles of raindrop size distributions (DSD) provides a controlled experiment framework to investigate the accuracy and robustness of attenuation correction algorithms [\(Berne and Uijlenhoet,](#page-5-1) [2005\)](#page-5-1).

This paper focuses on the quantification of the influence of uncertainties concerning the radar calibration, the parameterization of a power-law relation between the radar reflectivity Z and the specific attenuation k , and total path integrated attenuation (PIA) estimates. The analysis concerns single frequency, incoherent and non-polarimetric radar systems. Two attenuation correction algorithms are studied: a forward algorithm based on the analytical solution proposed by [Hitschfeld and Bordan](#page-6-0) [\(1954\)](#page-6-0) and a backward algorithm based on the solution proposed by [Marzoug and Amayenc](#page-6-1) [\(1994\)](#page-6-1). From DSD range profiles, the corresponding profiles of bulk rainfall variables are derived. Using a Monte Carlo approach, the accuracy of the two algorithms is quantified for the different sources of error previously mentioned. The results presented in this paper complement previous work on the sources of uncertainty in attenuation correction (e.g., [Del](#page-6-2)[rieu et al.,](#page-6-2) [1999a\)](#page-6-2), by emphasizing on the variability of the DSD along a range profile in a stochastic framework.

Table 1. Mean, standard deviation and characteristic spatial scale of $N' = \ln N_t$ (with N_t in m⁻³) and $\lambda' = \ln \lambda$ (with λ in mm⁻¹) deduced from HIRE'98 data at a 2 s time step.

	Mean	Std	θ (km)
N'	8.11	0.41	4.4
λ'	0.93	0.31	4.4

2 DSD simulator

The DSD simulator used in the following has been proposed by [Berne and Uijlenhoet](#page-5-1) [\(2005\)](#page-5-1). It enables to generate realistic DSD range profiles. It is based on the exponential DSD, which two parameters N_t and λ are considered to be random variables

$$
N(D|N_t, \lambda) = N_t \lambda e^{-\lambda D}, \qquad (1)
$$

where $N(D|N_t, \lambda)$ dD denotes the drop concentration in the diameter interval [D, $D + dD$] given N_t (total drop concentration) and λ . The latter are assumed to be jointly lognormally distributed. In order to be able to simulate spatial correlation within the range profiles, $N' = \ln N_t$ and $\lambda' = \ln \lambda$ are assumed to follow a first order discrete vector auto-regressive process:

$$
\mathbf{X}[j+1] = \mathbf{C_1}\mathbf{C_0}^{-1}\mathbf{X}[j] + \mathbf{E}[j+1],\tag{2}
$$

where

$$
\mathbf{X}[j] = \begin{bmatrix} N'(j) - \mu_{N'} \\ \lambda'(j) - \mu_{\lambda'} \end{bmatrix},
$$

$$
\mathbf{C_0} = \begin{bmatrix} \sigma_{N'}^2 & \sigma_{N'} \sigma_{\lambda'} \rho_{N'\lambda'} \\ \sigma_{N'} \sigma_{\lambda'} \rho_{N'\lambda'} & \sigma_{\lambda'}^2 \end{bmatrix},
$$

$$
\mathbf{C_1} = \begin{bmatrix} \sigma_{N'}^2 \rho_{N'}(1) & \sigma_{N'} \sigma_{\lambda'} \rho_{N'\lambda'}(1) \\ \sigma_{N'} \sigma_{\lambda'} \rho_{\lambda' N'}(1) & \sigma_{\lambda'}^2 \rho_{\lambda'}(1) \end{bmatrix},
$$

$$
\mathbf{E}[j+1] = \begin{bmatrix} \epsilon_{N'}(j+1) \\ \epsilon_{\lambda'}(j+1) \end{bmatrix},
$$

j is the distance index, $\rho_{N'}(1)$ represents the autocorrelation at ag 1 (idem for λ'), $\rho_{N'\lambda'}(1)$ represents the cross-correlation at lag 1, and $\epsilon_{N'}$ represents a Gaussian white noise process (idem for λ'). Therefore C_0 and C_1 are the covariance matrices at lags 0 and 1. The variances of the white noise processes $\epsilon_{N'}$ and $\epsilon_{\lambda'}$ are fixed such that **X** is a second order stationary process. For such a first order vector auto-regressive process, the auto-correlation function takes an exponential form according to:

$$
\rho(r) = e^{-2r/\theta} \tag{3}
$$

where r represents the distance lag and θ the characteristic spatial scale, also known as the scale of fluctuation [\(Vanmar](#page-6-3)[cke,](#page-6-3) [1983\)](#page-6-3):

$$
\theta = 2 \int_{0}^{\infty} \rho(r) dr . \tag{4}
$$

Using this stochastic model, we are able to generate range profiles of DSDs of equivolumetric spherical drops. DSD time series measurements from an optical spectropluviometer, collected during the HIRE'98 experiment [\(Uijlenhoet](#page-6-4) [et al.,](#page-6-4) [1999\)](#page-6-4) in Marseille, France, are used to parameterize the model. We focus on a period of 45 min of intense rainfall during the 7 September 1998 rain event in order to simulate high rainfall intensities. To convert the measured DSD time series to DSD range profiles, we assume Taylor's hypothesis with a constant velocity of 12.5 m s^{-1} , consistent with the wind speed estimate of [Berne et al.](#page-5-2) [\(2004\)](#page-5-2). The zerolag cross-correlation between the fitted N' and λ' values is found to be negligible. The characteristic scale θ is found to be very similar for N' and λ' , and is therefore assumed to be equal. Note that this is not a prerequisite of the model. As a consequence, the number of model parameters reduces to five: the mean and standard deviation of N' and λ' , and the characteristic scale θ . Their values are given in Table 1.

The generated DSD profiles have a total length of 30 km, with a spatial resolution of 25 m (corresponding to a 2 s time step). From these DSD profiles, the corresponding profiles of bulk rain variables (radar reflectivity Z and specific one-way attenuation k) are easily derived, using the Mie theory [\(van](#page-6-5) [de Hulst,](#page-6-5) [1981\)](#page-6-5) for the scattering cross-sections and Beard's velocity model for the drop terminal fall velocities [\(Beard,](#page-5-3) [1976\)](#page-5-3). The radar reflectivity Z $\text{[mm}^6 \text{ m}^{-3} \text{]}$ is defined as

$$
Z = \frac{10^{6}l^4}{\pi^5|K|^2} \int_{0}^{\infty} \sigma_B(D)N(D|N_t, \lambda) \, dD \tag{5}
$$

where l [cm] denotes the wavelength of the radar signal, K [-] is a constant related to the refractive index of the hydrometeors, and σ_B [cm²] is the backscattering cross-section. Similarly, the specific one-way attenuation k [dB km⁻¹] is defined as

$$
k = \frac{1}{\ln 10} \int_{0}^{\infty} \sigma_E(D) N(D|N_t, \lambda) dD \tag{6}
$$

where σ_E [cm²] is the extinction cross-section. Figure [1](#page-2-0) presents an example of generated N_t and λ profiles, as well as the corresponding attenuated and non-attenuated Z profiles at X-band. This controlled experiment framework allows to apply a Monte Carlo technique to quantify the respective influence of the different sources of uncertainty in attenuation correction.

3 Attenuation correction algorithms

As mentioned in the introduction, we consider incoherent, single frequency and non-polarimetric radar systems. Two different types of algorithms will be studied in the following. The measured attenuated reflectivity Z_a reads

$$
Z_a(r) = \delta_c A(r) Z(r) , \qquad (7)
$$

where δ_c is the calibration error factor and $A(r)$ is the twoway attenuation factor at the range r ($0 \le A \le 1$). Assuming the Z-k relation reads

$$
Z = \delta_{\alpha} \alpha \, k^{\delta_{\beta} \beta} \tag{8}
$$

where δ_{α} (δ_{β} respectively) is the error factor in α (β). Therefore, A can be written as

$$
A(r) = \exp\left[-0.2\ln(10)\int_0^r \left(\frac{Z(s)}{\delta_\alpha\alpha}\right)^{1/(\delta_\beta\beta)} ds\right].
$$
 (9)

[Hitschfeld and Bordan](#page-6-0) [\(1954\)](#page-6-0) (HB hereafter) proposed an analytical solution to express Z as a function of Z_a :

$$
Z(r) = Z_a(r) / \left[\delta_c^{1/(\delta_\beta \beta)} - \frac{0.2 \ln(10)}{\delta_\beta \beta} \int_0^r \left(\frac{Z_a(s)}{\delta_\alpha \alpha} \right)^{1/(\delta_\beta \beta)} ds \right]^{\delta_\beta \beta} . \quad (10)
$$

The HB algorithm is a forward algorithm because the integral is between 0 and r . However, the difference in its denominator can be close to 0 and this makes the algorithm potentially highly unstable [\(Hitschfeld and Bordan,](#page-6-0) [1954\)](#page-6-0).

To avoid instability problems, another family of attenuation correction algorithms has been developed. It is based on the knowledge of an estimate A_0 of the PIA at a given range r_0 . For ground based radar, ground echoes may be used to derive PIA estimates by comparing their reflectivity values during dry and rainy periods, as proposed by [Delrieu et al.](#page-6-6) [\(1997\)](#page-6-6). The estimate A_0 can be uncertain, that is

$$
A(r_0) = \delta_A A_0 , \qquad (11)
$$

where δ_A is the error factor in A_0 . The reformulation of Eq.[\(10\)](#page-2-1) starting from r_0 and going backward to the radar guarantees the stability of the algorithm. As an example, we use the solution proposed by [Marzoug and Amayenc](#page-6-1) [\(1994\)](#page-6-1) (MA hereafter):

$$
Z(r) = Z_a(r) / \left[\left(\delta_c \delta_A A_0 \right)^{1/(\delta_\beta \beta)} + \frac{0.2 \ln(10)}{\delta_\beta \beta} \int_r^{r_0} \left(\frac{Z_a(s)}{\delta_\alpha \alpha} \right)^{1/(\delta_\beta \beta)} ds \right]^{\delta_\beta \beta} . \quad (12)
$$

The main drawback of such a backward algorithm is that it requires a reliable estimation of the PIA at a given range.

Fig. 1. Top panel: example of generated N_t and λ profiles. Bottom panel: corresponding non-attenuated Z (solid) and attenuated Z_a (dashed) profiles at X-band frequency.

4 Monte Carlo approach

To study the accuracy of the algorithms, we use a Monte Carlo technique. The analysis focuses on attenuation correction at X-band (3.2 cm wavelength) using Eqs. [\(10\)](#page-2-1) and [\(12\)](#page-2-2). One thousand profiles of N_t and λ (hence of Z, k and Z_a) are generated. To be consistent with operational radar sampling resolutions, the high spatial resolution (25 m) profiles are averaged at a lower spatial resolution of 250 m. On each profile a Z-k power-law relation is fitted by means of a non-linear regression technique. It must be noted that they constitute the best possible power-law relations. Figure [2](#page-3-0) presents the distributions of prefactor and exponent values for the 1000 profiles. The exact PIA value is calculated as the difference between the non-attenuated and the attenuated Z profiles. Then the two algorithms are applied using the fitted relations on the 1000 profiles. Using these reference values enables to independently analyze the influence of the different sources of error on the two attenuation correction algorithms.

The top pannel of Fig. [3](#page-3-1) shows the median, as well as the 10% and 90% quantiles, of the distribution of the root mean square error (RMSE) calculated between the exact Z profiles and the Z_c profiles obtained by applying the two attenuation correction algorithms without any uncertainty (i.e. $\delta_c=\delta_{\alpha}=\delta_{\beta}=\delta_A=1$). To illustrate the effect of attenuation, the RMSE between the Z and the uncorrected Z_a profiles has also been plotted, and appears to be much larger than the

Fig. 2. Distribution of the values of the prefactor α (top panel) and **Exponent β** (bottom panel) of the Z-k relation for the 1000 profiles at X-band frequency.

RMSE for the Z_c profiles. The significant dispersion of the distribution (top panel of Fig. [3](#page-3-1) is in log scale) is explained distribution (top panel of Fig. 3 is in log scale) is explained $\frac{1}{2}$ by the fact that the use of a deterministic power law between Z and k is not consistent with the stochastic nature of these z and k is not consistent with the stochastic nature of thes variables.

[1994\)](#page-6-1), the MA algorithm $(0.1 < \text{median} < 0.3 \text{ dBZ})$ **is** more stated and accorate that are red any superium theories in the entry-about 1 in [3](#page-3-1) cases in total. The bottom panel of Fig. 3 shows the percentage of divergent cases as a function of the PIA the percentage of arrespect called as a ranceroff of the rank
value. This confirms previous work on the instability of the HB algorithm (e.g, [Delrieu et al.,](#page-6-2) [1999a\)](#page-6-2), showing that the HB algorithm becomes significantly unstable when the PIA is above 15 dB: 20% (40%) of divergence for a PIA of about 20 dB ([3](#page-3-1)0 dB). The RMSE values in the top panel of Fig. 3 will constitute the reference values for the quantification of the influence of the different sources of uncertainty, as detailed in the following sections. As a well-known result (e.g., [Marzoug and Amayenc,](#page-6-1) more stable and accurate than the HB algorithm

5 Influence of the uncertainty in calibration

Radar systems can be affected by calibration errors. In this section, the influence of the uncertainty in calibration on the accuracy of the attenuation correction algorithms is quantified. For better visual inspection, the calibration error is

Fig. 3. Top panel: median (solid line) of the distribution of the RMSE calculated between the exact Z profiles and the attenuated reflectivity Z_a ("No correction"), and the Z_c profiles obtained by applying the two attenuation correction algorithms ("HB" and "MA"), for 1000 profiles at a 250 m resolution. The dotted and/or dashed lines represent the 10% and 90% quantiles. "div" indicates the percentage of diverging HB corrections. We arbitrarily limit the maximum PIA at 60 dB for clarity, although 10% of the profiles have a PIA above 60 dB. The percentage of divergent cases corresponds to all 1000 profiles. The convention is the same for the responds to all 1000 profiles. The convention is the same for the subsequent figures. Bottom panel: percentage of profiles for which subsequent figures. Bottom panel: percentage of profiles for which the HB algorithm diverges as a function of the PIA value. the HB algorithm diverges as a function of the PIA value.

expressed in dB as ϵ_c =10 log(δ_c) and varies in the interval [−5,+5]. The additional error due to uncertain calibration is calculated as the ratio between the RMSE values for a given calibration error and the reference RMSE values. Figure [4](#page-4-0) presents the median, as well as the 10% and 90% quantiles, of the distribution of the RMSE ratio as a function of the calibration error. The other error factors (δ_{α} , δ_{β} and δ_{A}) are fixed to 1.

accuracy of the two algorithms. For instance, the median RMSE ratio value is about 2 when $\epsilon_c = \pm 1$ for the MA algorithm. It is about 3 when ϵ_c = +1 for the HB algorithm. When ϵ_c <0, the distribution remains similar for the MA algorithm. For the HB algorithm, Eq. [\(10\)](#page-2-1) shows that $\delta_c < 1$ (or $\epsilon_c < 0$) results in more diverging profiles because the denominator can ϵ_c >0, the median values are similar for the two algorithms but the dispersion is larger for the HB algorithm. When As expected, the RMSE ratio rapidly increases when $\epsilon_c \neq 0$, that is the calibration error significantly decreases the

Fig. 4. Median, 10% and 90% quantiles of the distribution of the RMSE ratio as a function of the calibration error ϵ_c expressed in dB, for the two attenuation correction algorithms.

approach zero already for smaller Z_a values, as illustrated in Fig. [4](#page-4-0) by the almost systematic divergence and therefore near complete failure of the HB algorithm when $\epsilon_c < 0$ (absence of points and larger percentage of divergences).

6 Influence of the uncertainty in the parameterization of the *Z***-***k* **relation**

The two studied algorithms are based on the assumption of a power-law relation between Z and k . To analyze the influence of the uncertainty in the parameters of the Z-k power law on the accuracy of the two attenuation correction algorithms, an error factor between 0.7 and 1.3 is applied to the prefactor (the exponent respectively). The additional error due to uncertain parameterization of the Z-k relation is calculated as the ratio between the RMSE values for a given prefactor (exponent) error and the reference RMSE values. Figure [5](#page-4-1) presents the median, as well as the 10% and 90% quantiles, of the distribution of the RMSE ratio as a function of the relative deviation of the prefactor and exponent, with respect to the reference Z-k relation. The other error factors $(\delta_c \text{ and } \delta_A)$ are fixed to 1.

For the prefactor (top panel of Fig. [5\)](#page-4-1), the distribution of the RMSE ratio is roughly similar for the two algorithms. The distribution of the RMSE ratio for δ_{α} < 1 remains similar for the MA algorithm, while the HB algorithm is more sensitive to an underestimation of the prefactor (δ_{α} <1), with a larger dispersion of the quantiles. When the underestimation of δ_{α} becomes large, the HB algorithm diverges (see Eq[.10\)](#page-2-1). The median RMSE ratio is about 3 when the error is about $\pm 15\%$ in the prefactor for the MA algorithm. It is also about 3 when the error is about +15% for the HB algorithm.

The influence of the exponent appears to be similar to that of the prefactor for the HB algorithm, while it is stronger for the MA algorithm. For instance, the median RMSE ratio is about 10 when the error in the exponent is about $\pm 15\%$ for

Fig. 5. Median, 10% and 90% quantiles of the distribution of the **Fig. 5.** Median, 10% and 90% quantiles of the distribution of the RMSE ratio as a function of the relative deviation of the prefactor RMSE ratio as a function of the relative deviation of the prefactor (top panel) and exponent (bottom panel) of the Z-k power law, for (top panel) and exponent (bottom panel) of the Z-k power law, for the two attenuation correction algorithms. the two attenuation correction algorithms.

the MA algorithm. It is about 2 when the error is about $15%$ for the HB algorithm.

6 Influence of the uncertainty in the PIA estimate

HB algorithm, but it requires an additional parameter which is the estimate of the PIA at a given range. This section is devoted to the quantification of the influence of the uncertainty in this PIA estimate on the accuracy of the MA algorithm. Similarly to ϵ_c , we define $\epsilon_A=10 \log(\delta_A)$. The error in the PIA estimate ϵ_A is generated as a Gaussian white noise with a standard deviation of 2.5 dB [\(Delrieu et al.,](#page-6-7) 1999b). The additional error due to an uncertain PIA estimate ϵ_A is calculated as the ratio between the RMSE values for the uncertain PIA estimate and the reference RMSE values. The top panel of Fig. [6](#page-5-4) presents the median, as well as the 10% and 90% quantiles, of the distribution of the RSME ratio as a function of ϵ_A for the MA algorithm. The other error factors (δ_c , δ_α and δ_{β}) are fixed to 1. The MA algorithm is more accurate and more robust than the

For the prefactor of Fig. 5 and Fig. $\frac{4}{3}$, should in theory be identical as far as the MA algorithm is concerned, because δ_A and δ_c can be interchanged. In **The distribution of the RMSE ratio for a given reference** Z_a profile, the error in the plactice, for a given ference \mathbb{Z}_q prome, the efform in the polynomial polynomial property different calibration and in the PIA estimate are generally different According to Eq. [\(12\)](#page-2-2), the top panels of Fig. [6](#page-5-4) and Fig. [4](#page-4-0)

Fig. 6. Top panel: median, 10% and 90% quantiles of the distribu-**Fig. 6.** Top panel: median, 10% and 90% quantiles of the distribu-Fig. 0. Top panel. Including to π and σ θ dualities of the unstructiontion of the RMSE ratio as a function of the PIA error ϵ_A expressed in dB for the MA algorithm. Bottom panel: similar to top panel of Fig. [3,](#page-3-1) to compare HB and MA with uncertain PIA estimates.

and therefore the deduced distribution of the RMSE ratio is and therefore the detailed distribution of the KNDE fails κ slightly different. Nevertheless, the influence of δ_A is similar to that of s to that of δ_c .

Finally, it must be noted that an under- or over-estimation I haddy, it mass be noted that an ander of over estimation of about 2 dB in the estimated PIA leads to a multiplication of about 2 dB in the estimated 113 relats to a manippication of the error by a factor of about 4. In case of relatively small PIA values (below 10 dB), the bottom panel of Fig. [6](#page-5-4) shows for the HB algorithm. that the MA algorithm is less accurate than the HB algorithm. **7 Influence of the uncertainty in the PIA estimate** [zoug and Amayenc,](#page-6-1) [1994;](#page-6-1) [Delrieu et al.,](#page-6-6) [1997\)](#page-6-6). This also small PIA (below 10 dB) and the MA algorithm for larger PIA (above 10 dB). This behaviour is consistent with previous work (e.g., [Mar](#page-6-1)suggests that at X-band, one should use the HB algorithm for

\overline{v} at the influence of the influence of the uncertainty of the σ conclusions **8 Conclusions**

Attenuation correction is an important step for quantitative rain estimation using C_1 , X-, or K-band weather radar. In this a standard delight $\frac{1}{2}$, $\frac{1}{2}$, $\frac{1}{2}$, $\frac{1}{2}$, $\frac{1}{2}$, $\frac{1}{2}$ and incoherent, single frequency and paper, we root on Tr can uncertain, onget requestly and non-polarimetric radar systems. We investigate the influence non polarimetric ratal systems. We investigate the innactive of uncertainties in the radar calibration, in the parameterizaof ancertainties in the redain canonialism, in the parameterization of a power-law relation between the radar reflectivity Z and the specific attenuation k, and in the total path integrated and the specific distribution *n*, and *m* are four pain integrated
attenuation (PIA) estimates on the accuracy of two attenuaditerminism (1 π 1) estimates on the accuracy of two attendant tion correction algorithms. The first (HB algorithm) is based aon correction argorit
on a forward impleme on a forward implementation and is known for its instability. The second (MA algorithm) is based on a backward implementation and is stable, but requires an additional piece of information, which is the PIA at a given range from the radar. A stochastic model of DSD range profiles provides a controlled experiment framework, with fully consistent Z and k profiles, to quantify the influence of the different sources of uncertainty. An uncertainty of 1 dBZ in the measured Z (or of 1 dB in the PIA estimate) leads to a multiplication of the RMSE by at least a factor 2 with respect to attenuation correction errors resulting from the stochastic nature of the DSD alone. An uncertainty of about 15% in the prefactor of

the Z-k relation leads to a multiplication of the RMSE by at least a factor 3 for both algorithms. The MA algorithm is more sensitive to uncertainties in the exponent (a multiplication by a factor of about 10 for 15% uncertainty), while the HB algorithm diverges more often.

For practical applications, a combination of the two algorithms appears as a good compromise: in case of small PIA (below 10 dB), the HB algorithm should be used, while the MA algorithm should be used when the PIA is larger than 10 dB. Such an hybrid algorithm has been implemented in the context of intense Mediterranean precipitation and has provided reliable results [\(Delrieu et al.,](#page-6-6) [1997;](#page-6-6) [Berne et al.,](#page-6-8) [2005\)](#page-6-8).

Finally, the framework described in this paper offers a suitable test-bed for other hybrid (e.g., [Iguchi and Meneghini,](#page-6-9) [1994\)](#page-6-9) or polarimetric (e.g., [Testud et al.,](#page-6-10) [2000\)](#page-6-10) attenuation correction algorithms.

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