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Research Article

Capacity of Magnetic-Induction MIMO Communication for Wireless Underground Sensor Networks

Song Li,^{1,2} Yanjing Sun,^{1,2} and Wenjuan Shi^{1,2}

¹China University of Mining and Technology, Xuzhou 221116, China ²Jiangsu Province Laboratory of Electrical and Automation Engineering for Coal Mining, Xuzhou 221116, China

Correspondence should be addressed to Yanjing Sun; yjsun@cumt.edu.cn

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In underground sensor networks, electronic magnetic waves undergo severe fading due to the challenging environment. Magneticinduction (MI) communication is a promising alternative physical layer technique for underground sensor networks. In this paper, we solve the intercoil crosstalk in magnetic-induction multiple-input multiple-output (MI MIMO) communication and investigate the channel capacity for underground MI MIMO wireless communication. Firstly, considering mutual induction between each two coils, we analyze the capacity of magnetic-induction channel. Secondly, the channel model of magnetic-induction multiple-input single-output (MISO) is introduced and a novel coil deployment method is proposed to reduce the crosstalk in MI MISO communication. Finally, the capacity of MI MISO communication and MI MIMO communication is deduced by the proposed coil deployment method. Simulation shows that the channel capacity would increase significantly in high SNR regime for underground MI MIMO communication.

1. Introduction

Underground sensor networks are in great demand in a wide variety of novel applications, such as intelligent irrigation, mine production monitoring, and earthquake forecast. In these underground sensor networks, sensors are buried underground to collect some environment information. The signal propagation medium is not air but soil [1–3]. The bottleneck in underground sensor networks is how to establish reliable communication link in the challenged environments.

In most existing wireless communication systems, such as cellular network, satellites, satellite communications, and wireless sensor network, the information transmission is accomplished using the electromagnetic (EM) waves. However, in some extreme environments, such as underground and underwater media, the electromagnetic waves undergo severe fading due to the hostile transmission medium. Also, the path loss is dependent on the properties of soils including soil makeup and density; thus, the path loss varies with space and time [4].

Magnetic-induction (MI) is a promising alternative physical layer technique for underground WUSNs. Since

the magnetic permeabilities of different materials are similar, the underground medium (such as soil) causes little variation in the attenuation rate of magnetic fields. This characteristic guarantees that the MI channel conditions remain constant when the composition of underground soil changes.

There are two differences between MI channel and EM channel: (1) unlike the EM channel, the MI channel condition is not time-varying, since there is no multipath effect; (2) the MI channel conditions remain constant in different transmission media, such as soil, water, and air, because the attenuation rate of magnetic fields does not change in nonmagnetic media. Instead, the path loss of EM channel is highly dependent on numerous soils properties, such as water content, soil makeup, and density. Thus the EM channel conditions can vary significantly with time and location [5, 6].

To enlarge the transmission range further, MI waveguide technique is introduced, by placing several relay coils between the transmitter and receiver in MI based communications. Different from the relay points in EM wave based communication system, the MI relay point is just a simple coil without any energy source or processing device. The channel



FIGURE 1: MI communication using mutual induction.

capacity of MI waveguide has been studied and the closed-form expression is given.

Despite the numerous advantages, the capacity and reliability of MI communication are the primary concerns. The bandwidth of MI based channel is much smaller than EM wave based wireless channel, since the MI coils have to work at the resonant frequency to keep path loss low. Also, the disability of one node would make the MI waveguide break off.

In electromagnetic (EM) waves based wireless communication system, multiple-input multiple-output (MIMO) makes use of the spatial dimension of the channel to provide considerable capacity, increased resilience to fading [7]. In magnetic-induction based communication system, when multiple coils are equipped at one node, cross talk exists because of the mutual induction between different coils at one node. In magnetic-induction multiple-input multiple-output (MI MIMO) system, it is critical to eliminate the cross talk while maintaining a better performance. To the best of our knowledge, these questions have not been addressed so far.

In this paper, the channel capacity of magnetic-induction multiple-input single-output (MI MISO) is introduced. We proposed a novel coil deployment method to solve the cross talk produced by mutual induction of coils in one node. Then, we propose a coil deployment method of magneticinduction multiple-input multiple-output (MI MIMO) system to increase the channel capacity, by deploying two orthogonal coils in each node, and power allocation method is studied to optimize the MI MIMO capacity.

2. Related Work

The magnetic-induction based communication is firstly introduced in [8] and the MI channel model is given in [9]. In MI based communication system, the MI transmitter and receiver are modeled as the primary coil and secondary coil of a transformer, as shown in Figure 1. Information is transmitted due to the mutual induction between the primary coil and secondary coil. The expression of received power and path loss of MI channel is presented in [9]. Comparing with EM based communication, the MI based communication has constant channel condition even in the soil with high water content.

To prolong the communication range, the magneticinduction (MI) waveguide technique was developed [9, 10], deploying multiple coils between transmitter and receivers as relay node, as is shown in Figure 2. The sinusoidal current in the transmitter coil induces another sinusoidal current

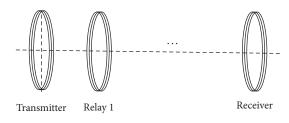


FIGURE 2: MI waveguide technology.

in the first relay and so on. The difference between EM based relay and MI based relay is that the MI relay node can be coil without battery and signal process component. Also the path loss of magnetic-induction waveguide is deduced. The closed-form expression of path loss of MI waveguide is analyzed in [9]. In magnetic-induction waveguide technique, only mutual induction between neighborhoods is considered to simplify the analysis. In other words, each relay has mutual induction with two neighbor coils. In ideal MI waveguide, several relay coils are placed along one axis between the MI transmitter coil and MI receiver coil.

The load impedance and noise model of MI waveguide are analysed in [11], considering the influence of conductivitybased losses in the soil and the frequency-selectivity feature of MI channel. Also the choice of the circuit elements at the relays, the deployment strategies, and the influence on the results are discussed. The channel capacity is maximized by optimizing system parameters, including the transmit power density, the number of coil windings, and the carrier frequency.

In [8–11], all the coils (transmitter, receiver, and relays) have the same parameters, as well as the same resonant frequency. The impedance of transmitter, relays, and receiver is dependent on the transmit frequency. If the transmit frequency is deviated from the resonant frequency, the capacity decreases dramatically. Consequently, the bandwidth is limited in MI communication. In order to solve the bandwidth bottleneck, a spread resonance strategy for MI communication is proposed in [12]. Different resonance frequencies are allocated on different MI relays to increase channel capacity. The spread resonance strategy utilizes tradeoff between larger bandwidth and lower path loss and finds optimal balance. Thus the system complexity is increased remarkably and the waveguide deployment also becomes more difficult.

Another strategy proposed to overcome the throughput bottleneck is to optimize the quality factor of transmitter coil and receiver coil [13]. In magnetic-induction based communication, the transmitter power is a function of quality factor, as well as bandwidth. Thus the capacity can be maximized under optimal value of quality factor.

Besides wireless underground sensor network, the magnetic-induction technology can also be used in other applications under challenging environments, such as underwater communication, body area network (BAN), and embedded medical communication systems [14–17]. Comparing with acoustic wave based communication, the communication range between transmitter and receiver can be increased to hundreds of meters in fresh water by

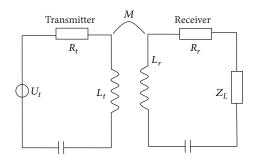


FIGURE 3: Equivalent circuit of MI communication.

magnetic-induction technique. 3D underwater magneticinduction wireless networking topologies are modeled for practical shallow and deep water in [15]. Because permeability of the air is the same as that of water, the magnetic-induction channel creates a homogeneous medium between underwater-underwater and underwater-surface areas.

The magnetic-induction waveguide method was studied as a method to increase the communication range in Near Field Magnetic-Induction Communication (NFMIC) in [17]. Unlike EM based wireless communication, the received power of MI based wireless communication does not degrade when the device is inside the human body.

3. MI Based Communication

3.1. MI Based Communication Model. In MI communications, the data transmission and reception are accomplished with the use of a coil of wire. We assume that each node contains one transmitter circuit with a voltage source U_t and one receiver circuit with a load impedance Z_L . Each node includes a magnetic antenna (which is assumed to be a multilayer air core coil), a capacitor C, and a resistor R (which models the copper resistance of coil). One coil can be modeled as a resistor and an inductor. The impedance of each coil increases with high operating frequency. Thus we add a capacitor Cto each coil to reduce the impedance and to guarantee that the transmitter and receiver operate in resonance frequency. By appropriately designing the capacitor value, resonant coils can be formed to effectively transmit the magnetic signals, such that the impedance of each coil can be reduced. Parasitic effects are not considered in this paper, including parasitic capacities, skin effect in windings, and proximity effect, which is nonnegligible in circuit elements at very high frequencies.

The equivalent model of the transmitter and receiver is presented in [2]. The transmitter and receiver circuit can be modeled as one resistor, one capacitor, and one inductor, as illustrated in Figure 3. The transmitted signal is carried by the voltage.

According to Kirchhoff's law and mutual induction theory, the current of transmitter and receiver matches the following equations:

$$I_r = -\frac{j\omega M I_t}{\left(Z_r + Z_L\right)},\tag{1}$$

$$U_t = I_t Z_t + j\omega M I_r,$$

where I_t , I_r denote the current in the transmitter and receiver, respectively, Z_t , Z_r denote the impedance of transmitter and receiver, respectively, M denote mutual induction of transmitter and receiver, and ω denote the angle frequency of transmit signal, $\omega = 2\pi f$.

We assume that all coils have the same material and size and thus have the same impedance. The impedance of each circuit is given by

$$Z = R + j\omega L + \frac{1}{j\omega C}.$$
 (2)

The resistance is determined by the material and the length of the coil:

$$R = N \cdot 2\pi a \cdot R_0, \tag{3}$$

where R_0 is the resistance of a unit length of the loop, N is the number of turns of each coil, and a is the radius of each coil. The induction of each coil can be calculated by

$$L = \frac{1}{2}\mu\pi N^2 a. \tag{4}$$

The capacitor of each node is chosen to make each circuit resonant at operating frequency, $j\omega L + (1/j\omega C) = 0$.

By solving (1), the current at transmitter and receivers can be expressed as

$$I_t = \frac{U_t}{Z_t + \omega^2 M^2 / (Z_r + Z_L)},$$

$$I_r = \frac{j\omega M_{tr} U_t / Z_t}{Z_r + Z_L + \omega^2 M^2 / Z_t}.$$
(5)

When the positions of transmitter and receiver are predetermined, the received power is dependent on the mutual induction between transmitter and receiver.

The mutual induction *M* can be deduced by the magnetic potential of the magnetic dipole:

$$M_{ij} = \mu \pi N^2 \frac{a^4}{4r^3} \left(2\sin\theta_i \sin\theta_j + \cos\theta_i \cos\theta_j \right) \cdot G, \quad (6)$$

where μ denotes the medium permeability; *r* is the distance between two coils; *N* is the number of turns of the coils; *a* is the coils radius; θ_i and θ_j are the angles between the coil radial directions and the line connecting the coil centers; *G* is an additional loss factor due to eddy current [6].

From (6), the mutual induction between two coils is dependent on the placed angles when the position of coils is determined. Mutual induction reaches its maximum, when the transmitter coil and the receiver coil are vertical to the line connecting the two coil centers, $\theta_t = \theta_r = \pi/2$. The maximum mutual induction can be calculated by

$$M_{\rm max} = \mu \pi N^2 \frac{a^4}{2r^3} \cdot G. \tag{7}$$

The transmitted power and received power can be expressed as

$$P_t = I_t U_t,$$

$$P_r = I_r^2 Z_L.$$
(8)

Substituting (5) into (8), we can get the transmit power and received power:

$$P_{t} = \frac{U_{t}^{2}}{Z_{t} + \omega^{2}M^{2}/(Z_{r} + Z_{L})},$$

$$P_{r} = \frac{\omega^{2}M^{2}U_{t}^{2}Z_{L}}{(Z_{r} + Z_{L} + \omega^{2}M^{2}/Z_{t})^{2}Z_{t}^{2}}.$$
(9)

The path loss in magnetic-induction communication is defined as the ratio of transmit power and received power, $L = P_t/P_r$:

$$L = \frac{\omega^2 M^2 Z_L \left(Z_t + \omega^2 M^2 / (Z_r + Z_L) \right)}{\left(Z_r + Z_L + \omega^2 M^2 / Z_t \right)^2 Z_t^2}.$$
 (10)

3.2. Capacity of MI Communication. Assuming all coils are identical and work in resonate frequency, for example, the transmitter coil and receiver coil have the same radius and turns and are made by the same material, they have the same impedance, $Z_r = Z_L = N \cdot 2\pi a \cdot R_0$.

Considering Shannon's information theory, the channel capacity can be expressed by

$$C = \int_{f_0 - B/2}^{f_0 + B/2} \log\left(1 + \frac{P(f)}{N_0 B}L(f)\right),\tag{11}$$

where *B* denotes bandwidth of the magnetic-induction system, f_0 denote the resonant frequency, N_0 denotes power spectral density of the noise, L(f) denotes the path loss of magnetic-induction system, and P(f) denotes power spectral density of transmit symbol:

$$L(f) = \frac{4\pi^2 f^2 M(f)^2 Z_L (Z_t + 4\pi^2 f^2 M(f)^2 / (Z_r + Z_L))}{(Z_r + Z_L + 4\pi^2 f^2 M(f)^2 / Z_t)^2 Z_t^2}.$$
 (12)

From (12), the path loss varies with operating frequency and reaches its minimum when transmitter works at the resonant frequency, $f_0 = 1/2\pi\sqrt{LC}$. When the operating frequency deviates from the resonant frequency, the coil selfimpedance Z contains both resistance and reactance, and the absolute value dramatically increases. Consequently, the path loss of magnetic-induction based communication also increases dramatically. In this paper, we consider the 3 dB bandwidth B as the channel bandwidth. The path loss at frequency $f_0 + 0.5B$ is two times the path loss at the resonant frequency f_0 .

3.3. Modulation Scheme in MI Communication. Although the magnetic-induction based communication has been studied for a few years, the modulation in magnetic-induction is still an open issue.

The path loss would vary when operation frequency changes, since the impedance of each coil varies with the operation frequency. Different symbol should be sent with

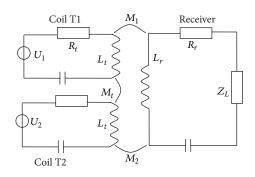


FIGURE 4: Multiple-input single-output magnetic-induction system.

the same frequency (resonant frequency) to keep path loss low, such as in MASK and MPSK modulation. Otherwise if the signals were sent by different operating frequency, such as in FSK and GMSK system, different symbol will experience different path loss. The received amplitude of different symbol would be different.

Here, we consider MASK in MI system. Let s(t) denote the information that will be transmitted by the transmitter in time slot *t*. The information bearing voltage signal is

$$u_t(t) = s(t)\sin 2\pi f t, \tag{13}$$

where $u_t(t)$ denote the voltage represented in time domain, s(t) is transmitted symbol, determined by the signal to be transmitted in time slot t, and f denotes the resonant frequency.

4. Capacity of MI MIMO Communication

4.1. MI MISO Communication. When MI transmitter and receiver are equipped with one coil, the communication is referred to as MI SISO communication. In MI SISO communication, the path loss is dependent on the placed angle of each coil and the location of receiver. In this section, the communication model of MI MISO and MI MIMO is proposed, and the channel capacity is analyzed.

4.1.1. MI MISO Communication Model. We consider a magnetic-induction based communication system with two nodes: transmitter (source node) and receiver (destination node). The transmitter is equipped with two coils (T1 and T2), while the receiver is equipped with one coil. The equivalent circuit is shown in Figure 4. Different from MI SISO, mutual induction exists between each two coils. In this case, the receiver can be stimulated by both transmitter coils (T1 and T2). Also there is mutual induction between two transmitter coils (T1 and T2), represented by M_t . Therefore crosstalk exits between two transmit coils. The situation is much more complicated than a communication system with one transmitter coil. Assume U_1 and U_2 denote the voltage of the coil TI's battery and coil T2's battery, respectively. The currents and voltages of each coil match the following equations:

$$I_{r} = -\frac{(j\omega M_{1}I_{1} + j\omega M_{2}I_{2})}{(Z_{r} + Z_{L})},$$

$$U_{1} = I_{1}Z_{1} + j\omega M_{t}I_{2} + j\omega M_{1}I_{r},$$

$$U_{2} = I_{2}Z_{2} + j\omega M_{t}I_{1} + j\omega M_{2}I_{r},$$
(14)

where I_1 , I_2 , and I_r denote the current in the transmitter coil T1, coil T2, and receiver, respectively, Z_1 , Z_2 , and Z_r denote the impedance of transmitter coil T1, coil T2, and receiver, respectively, M_i denotes mutual induction of coil *i* and receiver coil, i = 1, 2, and M_t denotes mutual induction of coil T1 and coil T2.

By solving (14), the current in each coil can be deduced as

$$I_{1} = \frac{\begin{vmatrix} U_{1}(Z_{r}+Z_{L}) & j\omega M_{t}(Z_{r}+Z_{L}) + \omega^{2}M_{1}M_{2} \\ U_{2}(Z_{r}+Z_{L}) & Z_{2}(Z_{r}+Z_{L}) + \omega^{2}M_{2}^{2} \end{vmatrix}}{\Delta},$$
(15)

$$I_{2} = \frac{\begin{vmatrix} Z_{1}(Z_{r}+Z_{L}) + \omega^{2}M_{1}^{2} & U_{1}(Z_{r}+Z_{L}) \\ j\omega M_{t}(Z_{r}+Z_{L}) + \omega^{2}M_{1}M_{2} & U_{2}(Z_{r}+Z_{L}) \end{vmatrix}}{\Delta},$$
(16)

$$I_{r} = \frac{\omega \left| \begin{array}{c} U_{1} & \omega M_{12}M_{1}(Z_{r}+Z_{L}) + jZ_{1}(Z_{r}+Z_{L})M_{2} \\ U_{2} & -\omega M_{1}M_{2}(Z_{r}+Z_{L}) - jZ_{2}(Z_{r}+Z_{L})M_{1} \\ \end{array} \right|}{\Delta},$$
(17)

where

$$= \begin{vmatrix} Z_1 (Z_r + Z_L) + \omega^2 M_1^2 & j \omega M_t (Z_r + Z_L) + \omega^2 M_1 M_2 \\ j \omega M_t (Z_r + Z_L) + \omega^2 M_1 M_2 & Z_2 (Z_r + Z_L) + \omega^2 M_2^2 \end{vmatrix}.$$
 (18)

After calculating the current in the transmitter's coil and receiver's coil, we can get the transmitted power and the received power, respectively. Thus, the transmit and received power are

$$P_t = I_1 U_1 + I_2 U_2,$$

$$P_t = I_r^2 Z_L.$$
(19)

The path loss in MI MISO system can be calculated considering (19), $L(f) = P_r/P_t$.

From (15) and (16), there is crosstalk between coils T1 and T2 caused by the mutual induction; for example, the voltage of T2 will interfere with the current in T1. The performance can be deteriorated when the transmitter is equipped with two coils because of the crosstalk between two transmitter coils.

4.1.2. Cross Talk Cancellation. From the analysis above, cross talk exists when multiple coils are deployed in one node (transmitter or receiver). Interestingly, the cross talk can be cancelled by deploying two transmit coils in a special way. We consider one special coil deployment of MI MISO channel model, where the transmitter coil T1 and the receiver coil are vertical to the line connecting the two coil centers, and

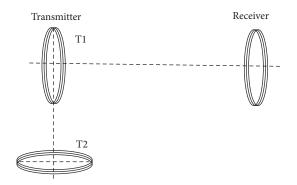


FIGURE 5: MI MISO system model when two transmit coils are placed vertically.

the line connecting the transmitter coils T1 and T2 is vertical to the line connecting the transmitter and receiver, as is shown in Figure 5.

We assume that the distance between two transmitter coils is much smaller than that between transmitter and receiver. In this case, the received power is dependent on the placed angle of coil T1.

When coil T2 is placed vertical to coil T1, the mutual induction of two transmitter coils decreases to zero according to (6), $M_t = 0$. Also, the mutual induction between coil T2 and receiver coil decreases almost to zero, $M_2 \approx 0$, because the distance between transmitter and receivers is much larger than the distance between two transmitter coils. Then the system is equivalent to single-input single-output magnetic-induction system:

$$I_{1} = \frac{U_{t}}{Z_{t} + \omega^{2} M^{2} / (Z_{r} + Z_{L})},$$

$$I_{2} = \frac{U_{2}}{Z_{2}},$$

$$I_{r} = \frac{j \omega M_{tr} U_{t} / Z_{t}}{Z_{r} + Z_{L} + \omega^{2} M^{2} / Z_{t}}.$$
(20)

From the analysis above, the transmit cross talk can be cancelled by deploying two transmit coils vertically. The induction on coil T1 caused by coil T2 is reduced to 0. If two receiver coils are deployed in the same way, two parallel links are established.

4.2. *MI MIMO Communication*. In this subsection, the capacity of MI MIMO is considered, when both transmitter and receiver are equipped with more than one coil. Also, the cross talk is cancelled by the coil deployment method proposed in Section 4.1.2.

4.2.1. MI MIMO Capacity Analysis. Although the coil deployment in MI MISO system in Figure 5 succeeds in canceling the cross talk between two transmit coils, the receiver coil can only receive the signal transmitted by coil T1. To receive the signal transmitted by T2, one horizontal coil R2 would be deployed on receiver. Hence, the MI MISO becomes MI MIMO by adding one horizontal coil, as shown in Figure 6.

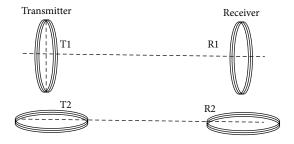


FIGURE 6: Magnetic-induction multiple-input multiple-output communication.

When one coil is placed vertically (T1 in Figure 6) and one coil horizontally (T2 in Figure 6) in transmitter, the mutual induction between two transmit coils becomes 0. Also, the coils are placed in the same way in receiver. When the distance between two coils at one single node (T1 and T2, e.g.) is much shorter than that between transmitter and receiver, the mutual induction between T2 and R1 can be neglected. The current induced in each received coil can be denoted as

$$I_{r1} = \frac{-j\omega U_1 Z_2 \left(Z_r + Z_L\right) M_1}{\Delta},$$

$$I_{r2} = \frac{-j\omega U_2 Z_1 \left(Z_r + Z_L\right) M_2}{\Delta},$$
(21)

where M_i represents mutual induction between Ti and Ri, i = 1, 2.

The MIMO channel becomes two separate SISO channels. The capacity of MIMO magnetic-induction channel can be deduced as

$$C = \sum_{i=1,2} \int_{f_0 - B/2}^{f_0 + B/2} \log\left(1 + \frac{P_i(f)}{2N_0 B} L_i(f)\right), \qquad (22)$$

where $L_i(f)$ denote the path loss of link Ti \rightarrow Ri, i = 1, 2:

$$L_{i}(f) = \frac{4\pi^{2} f^{2} M_{i}(f)^{2} Z_{L} \left(Z_{t} + 4\pi^{2} f^{2} M_{i}(f)^{2} / (Z_{r} + Z_{L})\right)}{\left(Z_{r} + Z_{L} + 4\pi^{2} f^{2} M_{i}(f)^{2} / Z_{t}\right)^{2} Z_{t}^{2}}.$$
(23)

Here, MI MIMO equals two parallel MI channels; therefore, the robustness is improved by providing one more channel. Each coil transmits signals with the power spectral density $P_i(f)$, when transmit power is allocated equally. So transmit power of each coil would be half of that in MI system with one coil. When the transmit power is allocated on one coil only, the MI MIMO is degraded to MI SISO system.

The transmit node and receiver node can be equipped with three coils on each node, comprising three pairs, as is shown in Figure 7. Two coils are parallel with each other in each pair, for example, T1 and R1. Each pair is vertical with another two pairs, for example, T1-R1 and T2-R2. In this case, there are three parallel MI channels between transmit node and receiver node.

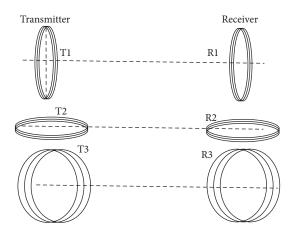


FIGURE 7: Magnetic-induction multiple-input multiple-output system.

Different from MIMO in wireless communication system, MI MIMO can only provide multiplex gain when multiple coils are deployed as Figures 6 and 7. Diversity gain cannot be provided because each receiver coil can only receive signal transmitted by one transmit coil. For example, R1 can only be stimulated by the sinusoidal current in T1. Also, R2 can only be stimulated by T2.

The MI MIMO channel between magnetic-induction transmitter and magnetic-induction receiver is equal to multiple parallel channels.

4.2.2. MI MIMO Capacity Optimization. In this subsection, the power allocation on multiple transmit coils is investigated to optimize the capacity of MI MIMO communication. In MI MIMO system, the transmit power is allocated on multiple transmit coils according to water-filling algorithm. The transmit power allocated on each coil can be expressed as

$$P_i(f) = \max\left\{A - \frac{N_0 B_0}{L_i(f)}, 0\right\}.$$
 (24)

The value of *A* can be obtained by substituting all the $P_i(f)$ into the power constraint equation:

$$\sum_{i} \int_{f_{0}-B/2}^{f_{0}+B/2} \log\left(1 + \frac{P_{i}(f)}{2N_{0}B}L_{i}(f)\right) P_{i}(f) \le P_{\max}.$$
 (25)

The magnetic-induction (MI) waveguide technique was developed to prolong the communication range, by deploying multiple coils between transmitter and receiver as relay node. In order to reduce the computational complexity, we assume that one relay node is stimulated by two neighbor coils in MI based waveguide model; for example, relay *i* is stimulated by relay i - 1 and relay i + 1. In this case the signal could be transmitted from one relay to the next relay. When one relay becomes invalid, the signal transmission will break off. By increasing the density of relays, the network robustness can be improved. But each relay will be stimulated by other nodes beside two neighbor nodes. In this case, the computational complexity will be increased. Also, some existing conclusion may not be applicable. Thus there is tradeoff between network

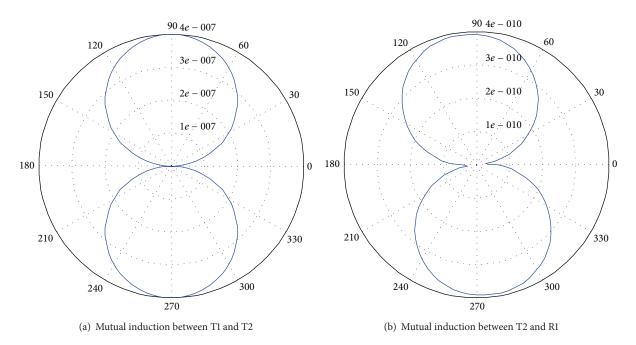


FIGURE 8: Mutual induction between two coils.

robustness and computational complexity. The MI MIMO can also be introduced into MI waveguide technology. Multiple coils are equipped in relay nodes, transmitter and receiver, respectively.

5. Simulation Results

In the simulation section, the parameters are chosen as follows: the resistance of unit length R_0 is set as 0.01 Ω/m . The number of turns of each coil is 10. The radius of coil equals 0.15 m. The distance between transmitter and receiver is 5 m. The permeability of soil medium is the same as that in the air, which is $4\pi \times 10^{-7}$ H/m. The operating frequency is 10 MHz.

In Figure 8(a), the mutual induction of two coils at transmitter is given when the coil T2 is placed with the same location but different angle. The transmit coil is placed according to the proposed coil deployment method. The location of receiver coil is illustrated in Figure 5, but the angle varies. From Figure 8, the mutual induction M_{ti} decreases to zero when coil T2 is placed vertically to coil T1, $\theta_i = 0$. In this case there is no intercoil interference at the transmitter. The mutual induction between coils T1 and T2 reaches a maximum when two coils are parallel.

Then the mutual induction of coil T2 and receiver was simulated in Figure 8(b). From the simulation result, the minimum of M_{ir} cannot decrease to 0.

The equivalent mutual induction between transmitter and receiver in MISO communication is simulated in Figure 9; when two transmitter coils are placed as in Figure 5, the receiver coil is located in different direction with the same distance as transmitter; the placed angle of receiver coil is the same as transmitter coil T1. From Figure 9, the directional property is much better than MI SISO. In other words, the receiver would have better performance regardless

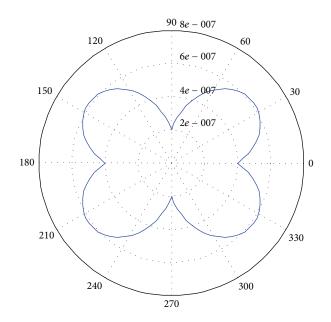


FIGURE 9: Equivalent mutual induction between transmitter and receiver.

of its direction. Conversely, the performance of MI SISO is dependent on the receiver's direction.

From Figure 10 the path loss in magnetic-induction based communication system is simulated with different transmit frequency. The resonant frequency is assumed to be 10 MHz. The path loss reaches its minimum value at the resonant frequency. When the operating frequency slightly deviates from resonant frequency, the path loss increases dramatically.

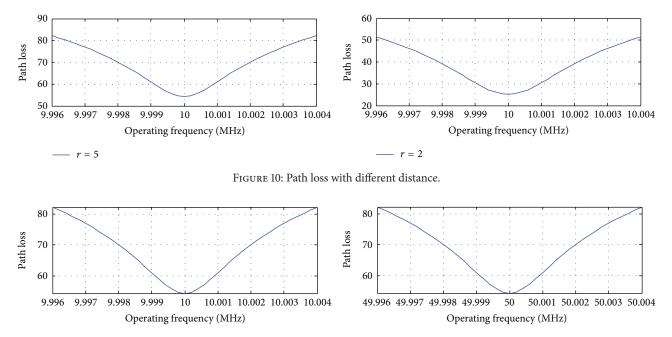


FIGURE 11: Path loss with different operating frequency.

Also we can observe that the path loss increases with the distance between transmitter and receiver increasing.

From Figure 11 the path loss in magnetic-induction based communication system is simulated with the resonant frequencies $f_0 = 10$ MHz and $f_0 = 50$ MHz. The path loss is decreased with the resonant frequency $f_0 = 50$ MHz, which means that the magnetic-induction based communication system has a better performance. When the size and material of coil remain the same, the value of capacitor can be decreased to improve the resonant frequency. According to the definition of mutual induction, increasing operating frequency results in increasing the mutual induction, meanwhile, reducing the path loss. From the simulation result, the bandwidth remains constant with operating frequency changes. The bandwidth of magnetic-induction communication system is about 1.5 kHz.

The capacity of single-input single-output magneticinduction system and multiple-input multiple-output magnetic-induction system is simulated in Figure 12. In MI SISO system, the transmitted power is allocated on one coil, while in MI MIMO system the transmitted power is allocated on multiple transmitted coils equally. The performance of MI MIMO system outperforms MI SISO system significantly, when the transmit SNR is larger than 27 dB. Thus the MI MIMO is more suitable for high rate applications. In low SNR regime, the MI SISO performs better. When using MI MIMO in low SNR, the power should be allocated on one coil only.

When the power is allocated on each coil optimally, the capacity of MI SISO and MI MIMO system is simulated in Figure 13. In low SNR regime, the MI MIMO system with optimal power allocation (OPA) among multiple transmit coils has the same capacity as magnetic-induction system with one coil. In other words, the power is allocated on one

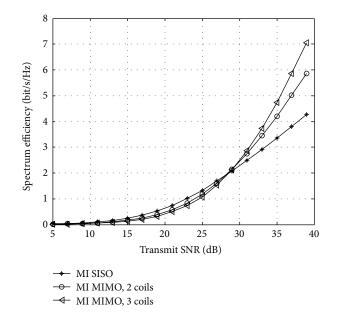


FIGURE 12: The capacity of magnetic-induction based communication system.

coil only in magnetic system with multiple coils; the other two coils do not transmit data. However, in high SNR regime, the MI MIMO system would outperform magnetic-induction system with one coil.

6. Conclusions

In this paper, the closed-form expression of path loss and capacity of MI based channel are derived. The system model of MI MISO channel is introduced. In order to solve the

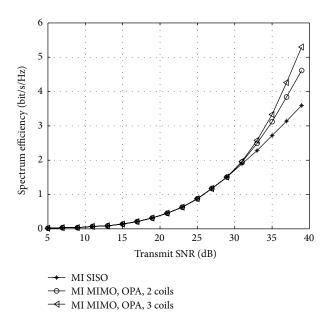


FIGURE 13: The capacity of magnetic-induction based communication system.

cross talk when multiple coils are equipped at one node, we introduced a coil deployment method in which each two coils are placed perpendicularly. The channel capacity of MI MISO and MI MIMO communication is derived. Also the capacity can be maximized by power allocation of different coils. The deployment method could also be used in MI waveguide technology to improve the channel capacity and network robustness.

Conflict of Interests

The authors declare that there is no conflict of interests regarding the publication of this paper.

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References

- J. Ma, X. Zhang, and Q. Huang, "Near-field magnetic induction communication device for underground wireless communication networks," *Science China Information Sciences*, vol. 57, no. 12, pp. 1–11, 2014.
- [2] B. V. Hieu, Y. Park, and T. Jeong, "Improving output gain of wireless sensor network hardware design for underground applications," *KSCE Journal of Civil Engineering*, vol. 17, no. 4, pp. 729–735, 2013.
- [3] S. Kahrobaee and M. C. Vuran, "Vibration energy harvesting for wireless underground sensor networks," in *Proceedings of the IEEE International Conference on Communications (ICC '13)*, pp. 1543–1548, IEEE, Budapest, Hungary, June 2013.

- [4] A. E. Forooshani, S. Bashir, D. G. Michelson, and S. Noghanian, "A survey of wireless communications and propagation modeling in underground mines," *IEEE Communications Surveys and Tutorials*, vol. 15, no. 4, pp. 1524–1545, 2013.
- [5] X. Dong and M. C. Vuran, "A channel model for wireless underground sensor networks using lateral waves," in *Proceedings of* the 54th Annual IEEE Global Telecommunications Conference (GLOBECOM '11), pp. 1–6, Houston, Tex, USA, December 2011.
- [6] J. I. Agbinya, "Performance of magnetic induction communication systems using induction factors," *Wireless Personal Communications*, vol. 70, no. 2, pp. 945–968, 2013.
- [7] A. Goldsmith, S. A. Jafar, N. Jindal, and S. Vishwanath, "Capacity limits of MIMO channels," *IEEE Journal on Selected Areas in Communications*, vol. 21, no. 5, pp. 684–702, 2003.
- [8] R. Bansal, "Near-field magnetic communication," *IEEE Antennas and Propagation Magazine*, vol. 46, no. 2, pp. 114–115, 2004.
- [9] Z. Sun and I. F. Akyildiz, "On capacity of magnetic inductionbased wireless underground sensor networks," in *Proceedings of the INFOCOM*, pp. 370–378, IEEE, 2012.
- [10] E. Shamonina, V. A. Kalinin, K. H. Ringhofer, and L. Solymar, "Magneto-inductive waveguide," *Electronics Letters*, vol. 38, no. 8, pp. 371–373, 2002.
- [11] S. Kisseleff, W. Gerstacker, R. Schober, Z. Sun, and I. F. Akyildiz, "Channel capacity of magnetic induction based wireless underground sensor networks under practical constraints," in *Proceedings of the IEEE Wireless Communications and Networking Conference (WCNC '13)*, pp. 2603–2608, April 2013.
- [12] Z. Sun, I. F. Akyildiz, S. Kisseleff, and W. Gerstacker, "Increasing the capacity of magnetic induction communications in RFchallenged environments," *IEEE Transactions on Communications*, vol. 61, no. 9, pp. 3943–3952, 2013.
- [13] K. Lee and D.-H. Cho, "Maximizing the capacity of magnetic induction communication for embedded sensor networks in strongly and loosely coupled regions," *IEEE Transactions on Magnetics*, vol. 49, no. 9, pp. 5055–5062, 2013.
- [14] M. C. Domingo, "Magnetic induction for underwater wireless communication networks," *IEEE Transactions on Antennas and Propagation*, vol. 60, no. 6, pp. 2929–2939, 2012.
- [15] B. Gulbahar and O. B. Akan, "A communication theoretical modeling and analysis of underwater magneto-inductive wireless channels," *IEEE Transactions on Wireless Communications*, vol. 11, no. 9, pp. 3326–3334, 2012.
- [16] N. Thilak and R. Braun, "Near field magnetic induction communication in body area network," in *Proceedings of the International Conference on Devices, Circuits and Systems (ICDCS '12)*, pp. 124–125, March 2012.
- [17] M. Masihpour and J. I. Agbinya, "Cooperative relay in near field magnetic induction: a new technology for embedded medical communication systems," in *Proceedings of the 5th International Conference on Broadband and Biomedical Communications* (*IB2Com* '10), December 2010.

