1 Amplified mid-latitude planetary waves favour

2 particular regional weather extremes

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10 There has been an ostensibly large number of extreme weather events in 11 the northern hemisphere mid-latitudes during the last decade¹. An open question that is critically important for scientists and policy makers is 12 13 whether any such increase in weather extremes is natural or 14 anthropogenic in origin²⁻¹⁴. One mechanism proposed to explain the 15 increased frequency of extreme weather events is the amplification of midlatitude atmospheric planetary waves¹⁵⁻¹⁷. Disproportionately large 16 17 warming in the northern polar regions compared to mid-latitudes - and 18 associated weakening of the north-south temperature gradient - may 19 favour larger amplitude planetary waves^{15,17}, although observational 20 evidence for this remains inconclusive¹⁸⁻²⁰. A better understanding of the 21 role of planetary waves in causing mid-latitude weather extremes is 22 essential for assessing the potential environmental and socio-economic 23 impacts of future planetary wave changes. Here we show that months of 24 extreme weather over mid-latitudes are commonly accompanied by

25 significantly amplified quasi-stationary mid-tropospheric planetary waves, with zonal wave numbers of 3-8. Conversely, months of near-average 26 weather over mid-latitudes are often accompanied by significantly 27 28 attenuated wave numbers 3-8. Depending on geographical region, certain 29 types of extreme weather (e.g., hot, cold, wet, dry) are more strongly 30 related to wave amplitude changes than others. The findings suggest that 31 amplification of quasi-stationary wave numbers 3-8 preferentially increases the probabilities of heat waves in western North America and 32 33 central Asia, cold outbreaks in eastern North America, droughts in central 34 North America, Europe and central Asia, and wet spells in western Asia.

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36 A series of weather extremes have hit the Northern Hemisphere mid-latitudes in 37 the recent years¹, such as the European heat wave in summer 2003⁸, cold and 38 snowy winters in 2009/10, 2010/11 and 2013/14 in northeast United States¹⁶, 39 the Russian heat wave in summer 2010²⁻⁵, Texas drought of 2011⁶, and the 40 summer 2012 and winter 2013/14 floods in United Kingdom⁷; all have had 41 significant socio-economic impacts. There is increasing scientific evidence¹⁻¹⁴ and a growing public perception²¹ that extreme weather events are occurring 42 43 more frequently. However, the mechanisms that drive weather extremes and 44 through which climate change may influence climate variability are poorly 45 understood. A potential cause of increased weather extremes is the amplification of atmospheric planetary waves¹⁵⁻¹⁷. Empirical^{15,16} , dynamical¹⁷ and 46 modelling^{16,22} evidence suggest a weakening north-south temperature gradient – 47 a key characteristic of anthropogenic climate change^{23,24} – causes larger 48 49 amplitude planetary waves, and it is hypothesised that high-amplitude planetary

waves favour the occurrence of extreme weather. It is this hypothesis that weexamine here.

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53 First, it is necessary to define precisely "extreme weather" for this application. 54 We are concerned with persistent anomalies in land surface temperature (T_L) 55 and land precipitation (P_L), such as heat waves, cold spells, droughts and 56 prolonged wet periods, which are evident on monthly timescales and large spatial scales (see Methods). Initially we focus on absolute (i.e., irrespective of 57 58 their sign) T_L and P_L anomalies (denoted $|T_L'|$ and $|P_L'|$). This is appropriate 59 because planetary waves tend to induce positive T_L (and perhaps P_L) anomalies 60 at some longitudes and negative anomalies at other longitudes.

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62 Fig. 1a,b show normalized time-series for monthly $|T_L'|$ and $|P_L'|$, respectively, 63 area-averaged over northern mid-latitudes (35-60°N; ML). The 40 months with 64 largest values (approx. 10% of cases) are highlighted by circles and labelled on 65 the lower x-axis. The months of extreme T_L and P_L lie relatively evenly through 66 the 34-year period, and there is no long-term trend. A full discussion of 34-year 67 trends in $|T_L'|$ and $|P_L'|$ is provided in the Supplementary Discussion S1. Fig. 1c 68 shows planetary-wave amplitude anomalies (normalized by removing the mean 69 amplitude and dividing by the standard deviation, σ , for each wave number) for 70 wave numbers 3-8 during months of T_L extremes (i.e., the months shown by 71 circles in Fig. 1a). The overwhelming majority of the statistically significant 72 amplitude anomalies are positive. The number of significant positive anomalies 73 (32) is appreciably larger than would be expected by chance alone (12). On half 74 of the extreme months considered there is at least one significant positive

75 amplitude anomaly for wave numbers 3-8. The three months with significant 76 negative amplitude anomalies also have at least one significant positive 77 amplitude anomaly. Thus, it would appear that some wave numbers are 78 amplified at the expense of other wave numbers. Although significantly amplified 79 planetary-waves are common during months of T_L extremes, it is not always the 80 same wave number(s) that is/are amplified. The greatest number of significant 81 positive amplitude anomalies are found for wave numbers 5, 6 and 7. Positive 82 monthly-mean amplitude anomalies imply, in physical terms, highly meridional 83 and persistent (slow-moving) circulation regimes (see Supplementary 84 Discussion S2).

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86 The statistically significant planetary-wave amplitude anomalies during months 87 of P_L extremes (i.e., the months shown by circles in Fig. 1b) are also 88 predominantly positive (Fig. 1d). Significantly amplified waves, in at least one 89 wave number 3-8, are identified in 40% of the months with extreme P_L. This 90 percentage increases to 50% for the 20 months with most extreme P_L . In 91 contrast, only one of these 20 months displays a significant negative amplitude 92 anomaly and further, this is accompanied by positive anomalies in two other 93 wave numbers. As for T_L , this suggests a link between extreme P_L and 94 significantly amplified planetary waves. However, clearly not all months with $T_{\rm L}$ 95 or P_L extremes are associated with significantly amplified, or attenuated, 96 planetary-wave amplitudes.

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Fig. 2a shows the probability density function (PDF) of amplitude anomalies for
each of wave numbers 3-8 in each of the 40 months of T_L extremes. Months of T_L

100 extremes over ML are associated with significantly amplified planetary waves, in 101 the sense that positive amplitude anomalies occur relatively more often during months of T_L extremes than they do climatologically. The difference in mean 102 103 amplitude anomalies, between extreme months and climatology, is very highly 104 statistically significant (p < 0.001). The difference in amplitude variance is also 105 highly significant (p < 0.01), with greater variance in months of T_L extremes than 106 climatologically. This increase in variance is primarily due to larger frequencies 107 at the positive tail of the distribution. This suggests that not only are T_L extremes 108 associated with amplified waves on average, but also that there is an particularly 109 strong association between the most highly amplified planetary waves and 110 extreme T_L.

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112 On the basis of daily reanalysis data, it can be seen that planetary-wave 113 amplitude and $|T_L'|$ co-vary almost simultaneously, but with the temperature 114 anomalies lagging the amplitude anomalies by 1-2 days (Supplementary Figure 115 3). This time lag implies that surface temperatures are responding to the 116 atmospheric circulation anomalies and not the other way round. Furthermore, 117 whilst surface temperatures respond very rapidly to circulation changes (hours 118 to days), the timescale for the mid-tropospheric circulation (wave amplitude is 119 defined at 500 hPa; see Methods) to respond to surface temperature anomalies is 120 much slower (tens of days to months). Thus irrespective of the small time lag, the 121 timescale of the response is strongly suggestive of a causal link between 122 planetary-wave amplitude and temperature extremes (see Supplementary 123 Discussion S3).

Fig. 2b-h show PDFs for the planetary-wave amplitude anomalies during months with T_L extremes over seven geographical regions (shown in Fig. 3). Over wNAm, cNAm and Euro, T_L extremes are associated with significantly larger mean amplitude and greater amplitude variance, consistent with the results for ML. T_L extremes over eNAm are linked to increased amplitude variance, but not significantly different mean amplitude. Over eAsia, significantly attenuated planetary-wave amplitudes accompany T_L extremes.

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Analogous PDFs for months of P_L extremes are shown in Fig. 2i-p. As for T_L extremes, we find that P_L extremes over ML are associated with significantly larger mean amplitude and significantly larger variance (again, the latter is primarily due to greater frequencies at the positive tail of the PDF). Regional P_L extremes over wNAm, Euro and wAsia are also linked to significantly amplified waves.

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140 The association between planetary-wave amplitude and mid-latitude- mean $|T_L'|$ 141 exists over a wide range of timescales from daily to sub-seasonal. The strength of 142 this relationship is relatively insensitive to timescale, although is it marginally 143 strongest on 5-14 day timescales (Supplementary Discussion S5). In contrast, the 144 amplitude-precipitation relationship weakens for timescales less than 12 days. 145 This implies that planetary waves are more important for longer-duration 146 precipitation extremes, such as those that contribute to drought, than they are 147 for short-lived precipitation extremes. We speculate that precipitation variability 148 is closely related to synoptic- or local-scale drivers on short timescales whereas 149 longer-lived events are more closely tied to the large-scale atmospheric150 circulation.

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152 If extreme weather is linked to amplified waves, is near-average weather 153 accompanied by attenuated planetary waves? Months of near-average (see 154 Methods for definition) T_L over ML and wNAm are associated with, on average, 155 significantly attenuated planetary-wave amplitudes, whereas months of near-156 average T_L over eAsia are accompanied by significantly amplified waves (Fig. 3). 157 All these relationships are opposite to those found for months with extreme T_{l} . 158 In Euro and wAsia, amplitude variance is significantly lower in months of 159 extreme T_L than climatologically. From the PDFs, it can be seen that this 160 primarily reflects fewer cases of large positive amplitude anomalies during the 161 months of near-average T_L than climatologically. Whilst months with T_L extremes 162 are often accompanied by highly amplified waves, these rarely accompany 163 months with near-average T_L. Turning to precipitation, none of the geographical 164 regions show a significant difference in mean amplitude anomaly between 165 months of near-average P_L and climatology (Fig. 3i-p). However, amplitude 166 variance is significantly lower over ML and wNAm, as a consequence of fewer (in 167 percentage terms) large positive amplitude anomalies during months of near-168 average P_L than in all months taken together.

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170 It is reasonable to expect that any particular planetary wave will induce positive
171 T_L (and perhaps P_L) anomalies at some longitudes and negative anomalies at
172 other longitudes. If wave phase was highly variable in time (i.e., the waves were
173 "free"), amplified waves might favour extremes of both sign (hot or cold, wet or

dry) at any specific longitude. However in reality, the waves have preferred 174 phases (i.e., they are quasi-stationary), related to orography and climatological-175 mean thermal gradients^{15,25}. This is especially the case for the smaller wave 176 177 numbers. Further, at any particular location, T_L and P_L may be more sensitive to 178 amplitude anomalies of one sign than the other, or to some wave numbers and 179 phases than others. Therefore, amplified waves may in fact favour one type of 180 extreme weather more than another, in any specific location. Table 1 compares 181 the mean amplitude and variance in regionally hot, cold, wet and dry months to climatological mean amplitude and variance (the full PDFs are shown in 182 183 Supplementary Discussion S5). Consistent with the rationale above, it appears 184 that in most regions there are stronger links between planetary-wave amplitude 185 and weather extremes of one sign than extremes of the other. Significantly 186 amplified waves are found during hot extremes over wNAm and cAsia, cold 187 extremes over eNAm, dry extremes over Euro and cAsia, and wet extremes over 188 wAsia. In each case, extremes of opposite sign in the same region are not accompanied by significantly amplified, or attenuated, planetary waves. 189 190 Precipitation extremes over cNAm are an interesting case: amplified waves tend 191 to accompany dry extremes whereas attenuated waves preferentially occur 192 during wet extremes.

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These findings reinforce suggestions that amplified planetary waves favour extreme weather in mid-latitudes^{15-17,26}. However, previous studies have not determined which types of extreme weather are caused by amplified waves, or where these extremes are likely to occur. Clearly these details are critically important for decision makers in assessing the risk of, and planning for the 199 impacts of, extreme weather events in the future. If quasi-stationary wave 200 numbers 3-8 are amplified in response to anthropogenic climate change, as has 201 been proposed^{15,17}, our results suggest that this would preferentially increase the 202 probabilities of heat waves in western North America and central Asia, cold 203 waves in eastern North America, droughts in central North America, Europe and central Asia, and wet extremes in western Asia. However, robust observational 204 205 evidence for long-term trends in planetary-wave amplitude is lacking¹⁸⁻²⁰ and 206 further work is required to understand better the physical mechanisms through 207 which human-induced climate change may impact upon mid-latitude planetary 208 waves.

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210 Methods

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212 **Observations.** Monthly-mean T_L and P_L from January 1979 to December 2012 213 were taken from the CRUTEM4 and GPCP v2.2 data sets, respectively. CRUTEM4 data²⁷ are derived from in situ observations at meteorological stations. GPCP 214 215 data²⁸ are derived from a combination of in situ measurements and satellite 216 estimates. For this study, GPCP data were re-gridded to the CRUTEM4 grid (5° by 217 5° longitude-latitude). The global-mean T_L and P_L have been subtracted from the 218 grid-box values. This procedure removed global-mean variability and trends, but 219 retained regional signatures such as those associated with planetary wave 220 changes.

Extremes. We derived T_L and P_L anomalies (denoted T_L' and P_L') by removing the relevant climatological monthly mean at each grid-box. Absolute values (i.e., the modulus) of T_L' and P_L' (denoted $|T_L'|$ and $|P_L'|$) are used to describe the

magnitude of the anomalies irrespective of their sign. This is appropriate 224 225 because planetary waves tend to induce positive T_L (and perhaps P_L) anomalies 226 at some longitudes and negative anomalies at other longitudes. Grid-point 227 anomalies were area-averaged over eight geographical regions: mid-latitudes 228 (ML; 35-60°N, 180°E-180°W), western North America (wNAm; 35-60°N, 115-229 150°W), central North America (cNAm; 35-60°N, 80-115°W), eastern North 230 America (eNAm; 35-60°N, 45-80°W), Europe (Euro; 35-60°N, 25°E-15°W), 231 western Asia (wAsia; 35-60°N, 25-65°E), central Asia (cAsia; 35-60°N, 65-105°E) and eastern Asia (eAsia; 35-60°N, 105-145°E). These regions (shown in Fig. 3) 232 233 were chosen *a priori* based on conventional (sub-) continental boundaries and 234 are approximately equal in area and together they cover all the mid-latitude 235 landmasses. The area-averaged monthly time-series were normalised by 236 removing the climatological mean and dividing by the standard deviation for 237 each calendar month. For each region, we then defined "extreme months" as the 238 40 cases (approximately 10%) with largest $|T_L'|$ or $|P_L'|$; and "near-average" 239 months as the 40 cases with smallest $|T_L'|$ or $|P_L'|$. "Hot", "cold", "wet" and "dry" months are defined based on the 40 months with largest T_L', smallest T_L', largest 240 P_L' and smallest P_L' , respectively. The selected years are provided in 241 242 Supplementary Discussion S6.

Wave amplitude. We analyse amplitudes of planetary waves in the monthlymean mid-tropospheric mid-latitude circulation, with zonal wave numbers 3-8.
Amplitudes were defined based upon Fourier analysis of 500 hPa geopotential
heights (Z₅₀₀), meridionally averaged over mid-latitudes (35-60°N), as a function
of longitude. Monthly-mean Z₅₀₀ were taken from the ERA-Interim reanalysis²⁹.
This approach is consistent with the "zonal amplitude" metric used in ref. 18,

except here we use monthly-mean Z₅₀₀ averaged over latitudes 35-60°N rather than daily values at 45°N. Whilst multi-decadal trends in planetary-wave amplitude are sensitive to how amplitude is defined^{18,20}, month-to-month variability of amplitude is highly consistent using the two frameworks outlined in ref. 18. In this manuscript we exclusively consider amplitude variability (not trends) and thus, use only one definition of planetary-wave amplitude.

Statistics. Differences in sample means were assessed using an unequal variance t-test. This is an adaptation of the Student's t-test that accounts for the two samples having different sizes and possibly unequal variances³⁰. Differences in sample variance were assessed using a Fisher f-test. We tested against the null hypothesis that the two sample means or variances are equal. The null hypothesis was rejected if the probability of equal means or variances is less than 10% (p < 0.1).

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- and wrote the paper. I. S. discussed the results and commented on the
- 347 manuscript.

- 348 Tables
- 349

350 Table 1: Differences in planetary-wave amplitude anomalies between
351 months of extreme weather and climatology.

	Hot		Cold		Wet		Dry	
	t	f	t	f	t	f	t	f
wNAm	2.31	1.22	-0.05	1.13	0.71	1.07	1.05	1.05
cNAm	1.11	1.19	1.48	1.21	-1.80	-1.09	2.52	1.25
eNAm	-1.18	-1.02	3.54	1.37	1.08	1.18	0.25	1.03
Euro	0.78	1.00	1.15	1.01	0.08	1.02	2.54	1.10
wAsia	-0.45	-1.12	0.70	-1.03	2.45	1.03	-0.86	-1.01
cAsia	3.11	1.02	0.28	1.11	0.25	-1.01	2.94	1.11
eAsia	-1.24	-1.12	0.12	1.14	-0.04	1.21	-0.05	-1.07

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The t and f statistics corresponding to, respectively, differences in mean planetary-wave amplitude and differences in amplitude variance between composites of months with extreme weather and climatology. Statistics are provided separately for four types of weather extreme (hot, cold, wet and dry) and for eight geographical regions. Differences in mean amplitude or variance that are significant at the 90% confidence level are shown in bold italic type. Regions and their abbreviations are shown in Fig. 3.

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Figure 1: Planetary-wave amplitude anomalies during months of extreme 363 364 weather. Normalised monthly time-series of mid-latitude- (35-60°N) mean land-365 based absolute temperature anomalies (a) and absolute precipitation anomalies 366 (**b**), 1979-2012. In **a** and **b**, the 40 months with largest values are identified by 367 circles and labelled on the lower x-axis, and the green line shows the threshold 368 value for extremes. Normalised wave amplitude anomalies, for wave numbers 3-369 8, during 40 months of mid-latitude- mean temperature extremes (c) and 370 precipitation extremes (d). In c and d, the months are labelled on the abscissa in 371 order of decreasing extremity from left to right. Grey shading masks anomalies 372 that are not statistically significant at the 90% confidence level; specifically, 373 anomalies with magnitude smaller than 1.64σ , the critical value of a Gaussian 374 (normal) distribution for a two-tailed probability p = 0.1. Red shading indicates 375 wave numbers that are significantly amplified compared to average and blue 376 shading indicates wave numbers that are significantly attenuated compared to 377 average.



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379 Figure 2: Frequency distributions of planetary-wave amplitude anomalies 380 during months of extreme weather. Probability density functions (PDFs) for 381 normalised wave amplitude anomalies (wave numbers 3-8) during 40 months of 382 extreme temperature over eight geographical regions: ML (**a**), wNAm (**b**), cNAm 383 (c), eNAm (d), Euro (e), wAsia (f), cAsia (g) and eAsia (h); and during 40 months 384 of extreme precipitation over the same 8 regions (**i-p**), respectively. The 385 coloured bars show the relative frequency (expressed as a percentage of the total 386 number of anomalies) of amplitude anomalies in bins of 0.5σ . The black lines 387 show the climatological frequencies. The t and f statistics and their associated p 388 values are provided, with bold green text highlighting values that are statistically 389 significant at the 90% confidence level. The regions and their abbreviations are 390 shown in Fig. 3.





393 **Figure 3: The geographical regions used in this study**. Black boxes show the

394 regions and are labelled with their abbreviations.

395



- **397** Figure 4: Frequency distributions of planetary-wave amplitude anomalies
- 398 during months of near-average weather. As Fig. 2, but for months of near-
- 399 average temperature (**a**-**h**) and precipitation (**i**-**p**).