

Research Article

Initial Systematic Investigations of the Landscape of Low-Layer NAHE Variation Extensions

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The discovery that the number of physically consistent string vacua is on the order of 10^{500} has prompted several statistical studies of string phenomenology. Focusing on the Weakly Coupled Free Fermionic String formalism, we present systematic extensions of a variation on the NAHE (Nanopoulos, Antoniadis, Hagelin, Ellis) set of basis vectors. This variation is more conducive to the production of “mirrored” models, in which the observable and hidden sector gauge groups (and possibly matter content) are identical. This study is parallel to the extensions of the NAHE set itself and presents statistics related to similar model properties. Statistical coupling between specific gauge groups and spacetime supersymmetry is also examined. Finally, a model with completely mirrored gauge groups is discussed. It is found that the region of the landscape explored generates no physically realistic models due to a lack of three net chiral generations.

1. Introduction

The large number of string vacua [1, 2] has prompted both computational and analytical examinations of the landscape, for example, [3–11]. The Weakly Coupled Free Fermionic Heterotic String (WCFHFS) [12–15] approach to string model construction has produced some of the most phenomenologically realistic string models to date [16–57]. The present study focuses on the systematic extension of an NAHE Variation [50] thereby scanning a region the WCFHFS parameter space yet to be explored. The NAHE Variation is of particular interest because it is conducive to the generation of mirror models. Additionally, it was hoped that this regime would produce models with three net chiral generations which turns out not to be the case. Traditionally, the number of fermion families is linked to the topological structure of the compactification; however, in the language of the WCFHFS this connection is difficult to explore analytically because many such models do not have a well-defined geometric interpretation. This work parallels that presented in [58] regarding NAHE extension.

1.1. The NAHE Variation. While there have been many quasirealistic models constructed from the NAHE basis, other bases can be used to create different classes of realistic and

quasirealistic heterotic string models. Like the NAHE set, the NAHE variation is a collection of five order-2 basis vectors. However, the sets of matching boundary conditions are larger than those of the NAHE set. This allows for a new class of models with “mirrored” groups, that is, with gauge groups that occur in even factors. Some also have mirrored matter representations that do not interact with one another. This means that hidden sector content matches the observable sector, making the dark matter and observable matter gauge charges identical. Several scenarios with mirrored dark matter have been presented as viable phenomenological descriptions of the universe [59–62].

The NAHE set does not have a tendency to produce mirrored models because the boundary conditions making up the $SU(4)^3$ gauge groups break the mirroring between the elements $\bar{\psi}$, $\bar{\eta}$, and $\bar{\phi}$. We can remedy this by ensuring that the worldsheet fermions $\bar{\psi}^{1,\dots,5}$ and $\bar{w}^{1,\dots,6}$ have the same boundary conditions as $\bar{\phi}^{1,\dots,8}$. In doing so, the NAHE variation basis vectors generate a model with gauge group $SO(22) \otimes E_6 \otimes U(1)^5$. The basis vectors making up this set are presented in Table 1 with the resulting particle content of the NAHE variation model presented in Table 2.

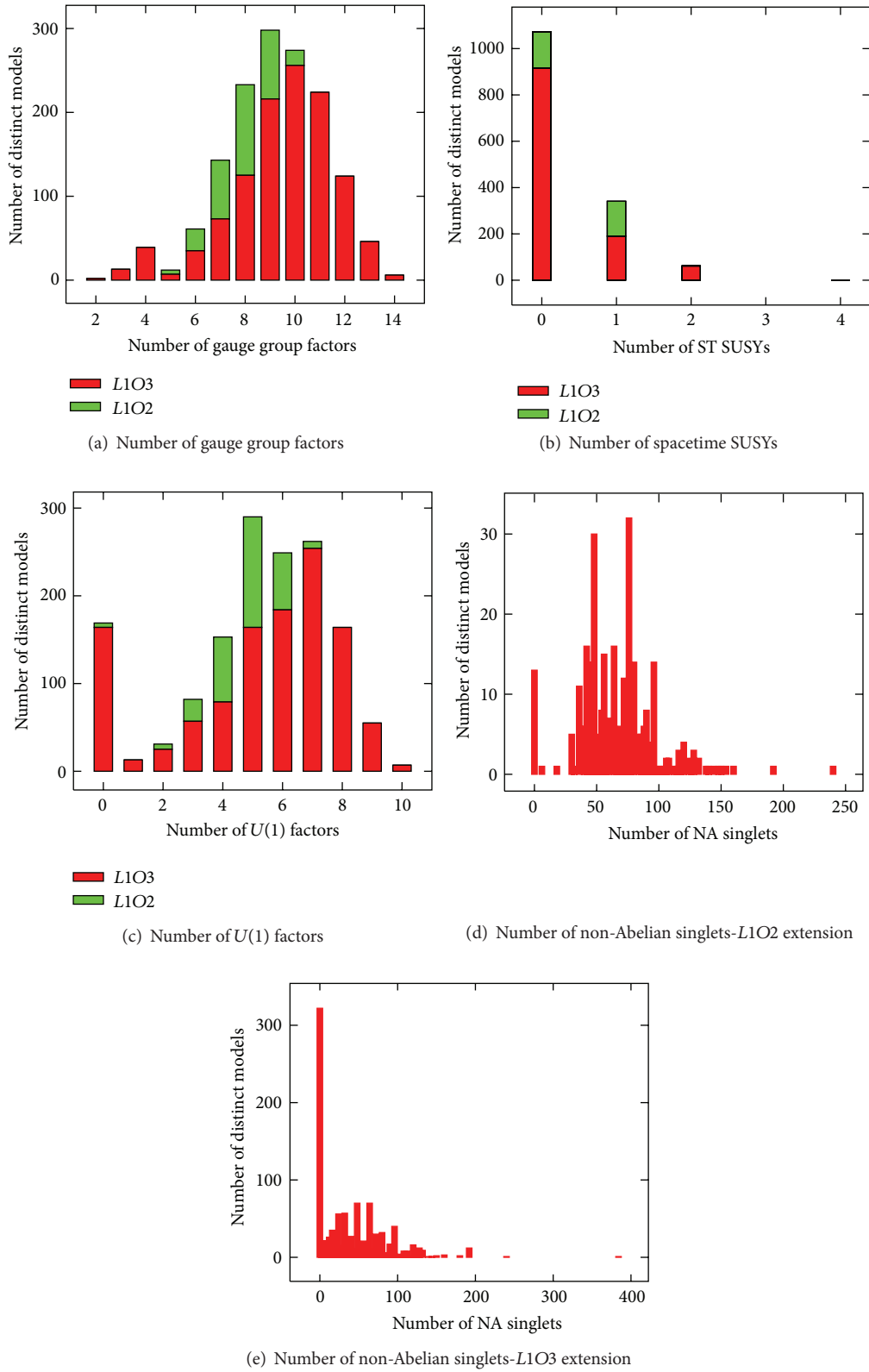


FIGURE 1: Statistics for the full NAHE variation extension data set.

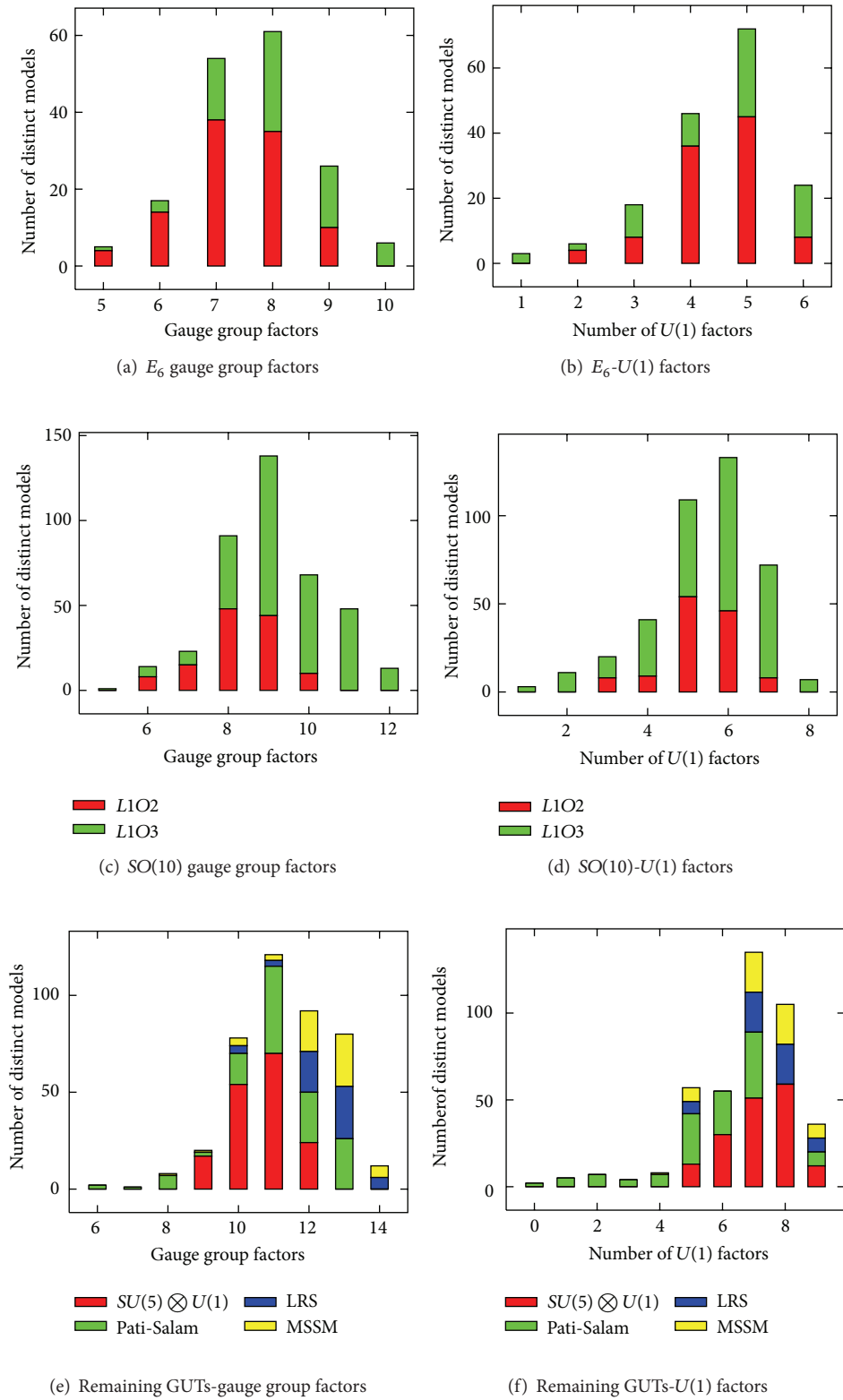


FIGURE 2: Gauge and $U(1)$ statistics for various GUT models in the NAHE variation extensions data set.

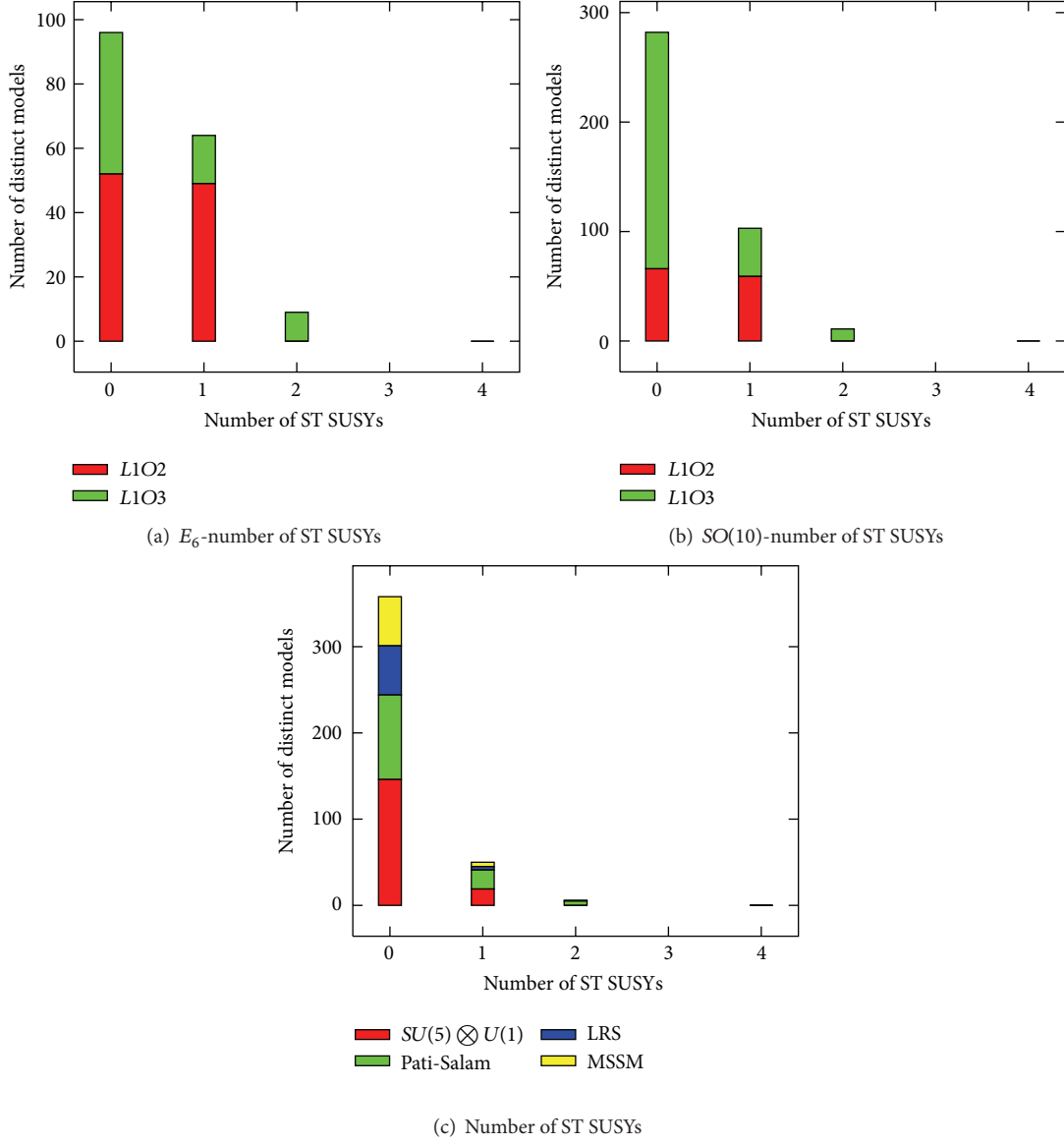


FIGURE 3: ST SUSY statistics for various GUT models. Note that only the E_6 and $SO(10)$ occur from $L1O2$ extensions.

TABLE 1: The basis vectors and GSO coefficients of the NAHE variation arranged into sets of matching boundary conditions. The worldsheet fermions ψ , x^i , $\bar{\psi}^i$, $\bar{\eta}^i$, and $\bar{\phi}^i$ are expressed in a complex basis, while y^i , w^i , \bar{y}^i , and \bar{w}^i are expressed in a real basis.

Sec	O	ψ	x^{12}	x^{34}	x^{56}	$\bar{\psi}^{1,\dots,5}$	$\bar{\eta}^1$	$\bar{\eta}^2$	$\bar{\eta}^3$	$\bar{\phi}^{1,\dots,8}$	$y^{12} \bar{y}^{12}$	$y^{34} \bar{y}^{34}$	$y^{56} \bar{y}^{56}$	$w^{1,\dots,6} \bar{w}^{1,\dots,6}$
$\vec{1}$	2	1	1	1	1	1, ..., 1	1	1	1	1, ..., 1	1 1	1 1	1 1	1, ..., 1 1, ..., 1
\vec{S}	2	1	1	1	1	0, ..., 0	0	0	0	0, ..., 0	0 0	0 0	0 0	0, ..., 0 0, ..., 0
\vec{b}_1	2	1	1	0	0	1, ..., 1	1	0	0	0, ..., 0	0 0	1 1	1 1	0, ..., 0 0, ..., 0
\vec{b}_2	2	1	0	1	0	1, ..., 1	0	1	0	0, ..., 0	1 1	0 0	1 1	0, ..., 0 0, ..., 0
\vec{b}_3	2	1	0	0	1	1, ..., 1	0	0	1	0, ..., 0	1 1	1 1	0 0	0, ..., 0 0, ..., 0

$$k_{ij} = \begin{pmatrix} & \vec{1} & \vec{S} & \vec{b}_1 & \vec{b}_2 & \vec{b}_3 \\ \vec{1} & 1 & 0 & 1 & 1 & 1 \\ \vec{S} & 0 & 0 & 0 & 0 & 0 \\ \vec{b}_1 & 1 & 1 & 1 & 1 & 1 \\ \vec{b}_2 & 1 & 1 & 1 & 1 & 1 \\ \vec{b}_3 & 1 & 1 & 1 & 1 & 1 \end{pmatrix}$$

TABLE 2: The particle content for the NAHE variation model. The model also has five $U(1)$ groups and $N = 1$ ST SUSY.

QTY	$SO(22)$	E_6
30	22	1
15	1	27
90	1	1
15	1	$\overline{27}$

TABLE 3: A summary of the GUT group study with regard to the number of chiral fermion generations in the NAHE variation investigation.

GUT	Net chiral generations	Three generations
$L1O2 E_6$	Yes	No
$L1O2 SO(10)$	Yes	No
$L1O3 E_6$	No	No
$L1O3 SO(10)$	No	No
$L1O3 SU(5) \otimes U(1)$	No	No
$L1O3$ Pati-Salam	No	No
$L1O3$ L-R symmetric	No	No
$L1O3$ MSSM	No	No

The observable sector is generally regarded as being the E_6 ; however, contributions to the observable sector may come from the breaking of the $SO(22)$. As compared to the NAHE set, the large number of $U(1)$ s and non-Abelian singlets is less phenomenologically favorable; however, the quantities of both can be reduced drastically which are shown in the statistics for single-layer extensions.

In Section 2, layer 1, order 2 ($L1O2$) extensions of the NAHE variation are investigated, with a focus on statistics. In Section 3, $L1O3$ extensions are similarly examined. In Section 4, the statistics of GUT and of spacetime supersymmetries of both orders are determined. Section 5 offers an example of a near mirrored model, and Section 6 reviews the findings of the prior sections.

2. Layer 1, Order 2 Extensions

There were 309 quasi-unique models out of 1,315,328 total consistent models built given the input parameters. A redundancy related to the rotation of the gauge groups, discussed in detail in [58], is also present. Duplicate models within the set of 309 were removed by hand. Approximately 2% of the models in the data set without rank cuts were duplicates, while none of the models with rank cuts had duplicates. The gauge group content of those models is presented in Table 5(a).

The most common gauge group in this data set is $U(1)$, while the most common non-Abelian gauge group is $SU(2)$, though less than half of the models contain it. The other pertinent feature of these models is the presence of nonsimply laced gauge groups with high rank. The $SO(2n + 1)$ groups range from rank 2 up to rank 10. Finally, about one third of the models retain their E_6 symmetry. The stability of the E_6 is in contrast to the more common breaking of $SO(10)$, the observable sector, in NAHE-based models [58]. These models will be revisited later with the E_6 treated as an

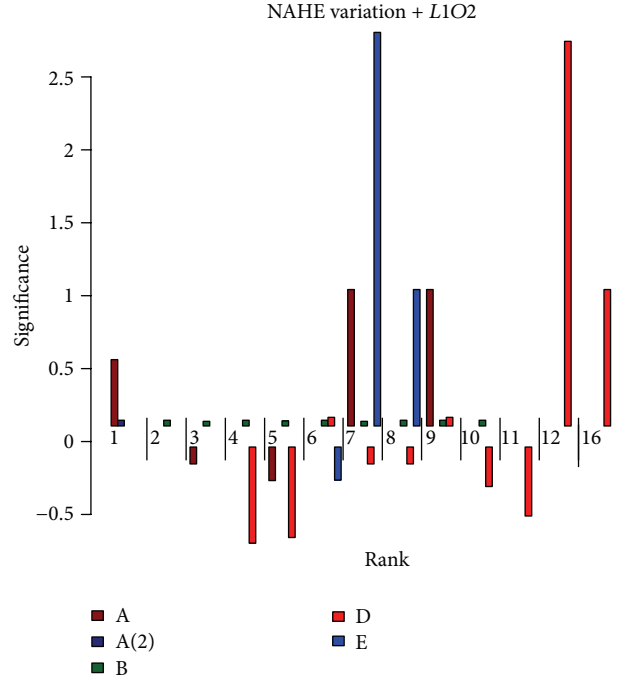


FIGURE 4: The significance values for models in the NAHE variation $L1O2$ extensions with regard to ST SUSY. Any (absolute) significance values greater than three indicate a strong statistical significance.

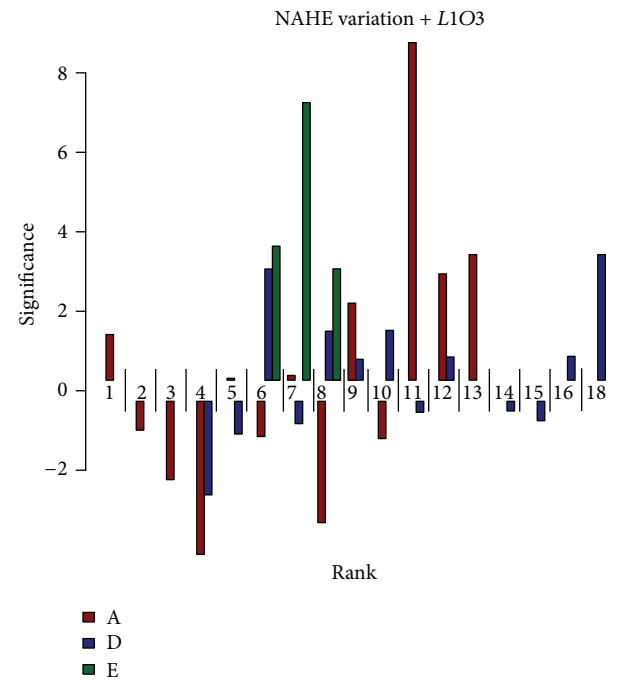


FIGURE 5: The significance values for models in the NAHE variation $L1O3$ extensions. Any (absolute) significance values greater than three indicate a strong statistical significance.

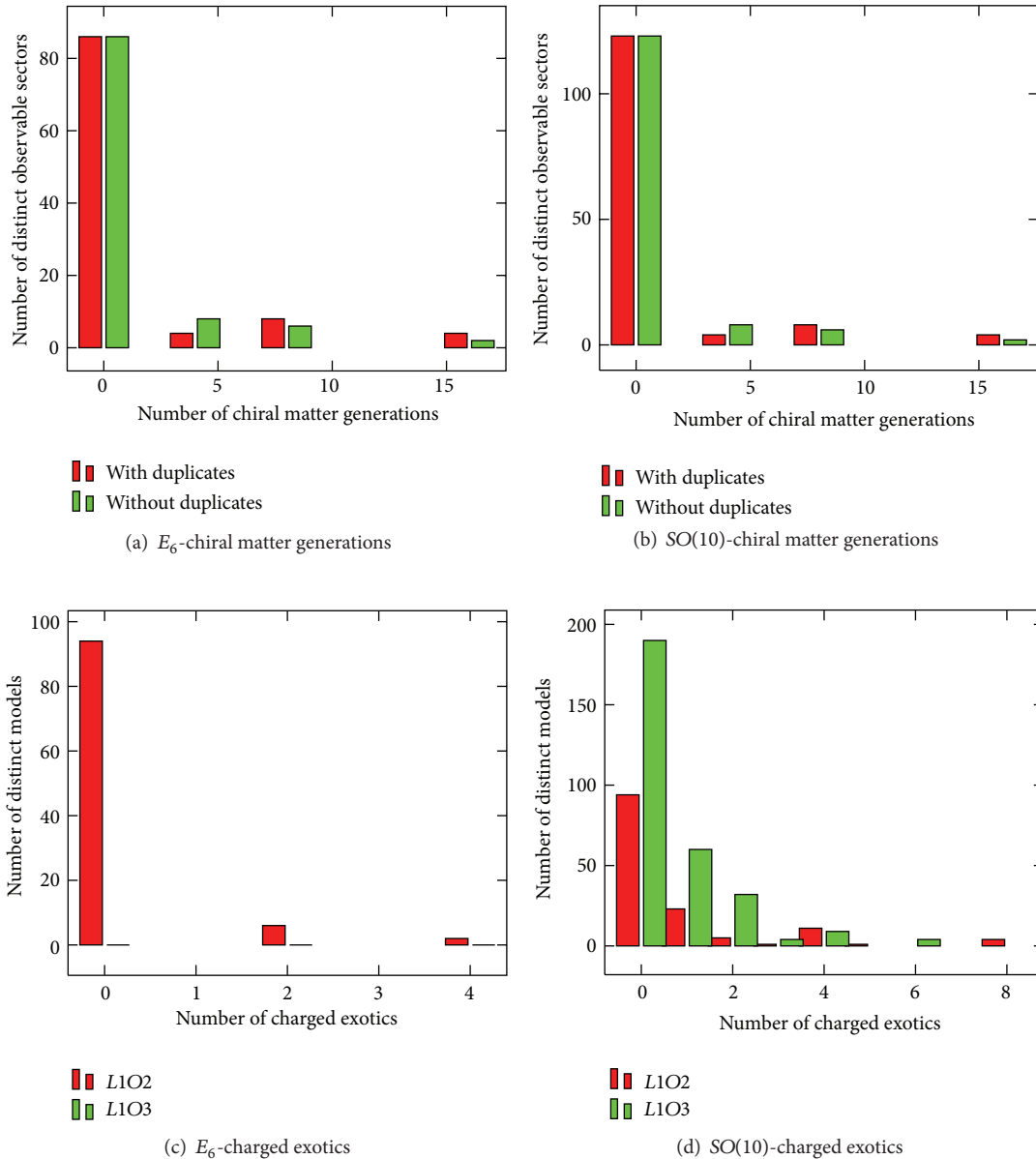


FIGURE 6: The number of chiral matter generations and charged exotics for E_6 and $SO(10)$ models in the NAHE variation extensions.

observable sector gauge group, and the number of chiral matter generations they have will be statistically examined.

Also of interest regarding the gauge group content of this data set is the number of gauge group factors present in each model; see Figure 1(a). The distribution of the number of gauge group factors across the unique models peaks around 8, suggesting that, roughly, the most common effect of $L1O2$ extension is the breaking of only one group factor. In a few models, some of the factors have enhancements, typically the $U(1)$ groups. Additional adjoint content distributions are provided in Figure 1(c), with GUT model distributions presented in Table 4, but will not be discussed in detail here.

Regarding the matter content, the number of ST SUSYs is plotted in Figure 1(b), and the number of non-Abelian singlets is plotted in Figure 1(d). It is clear from the latter that

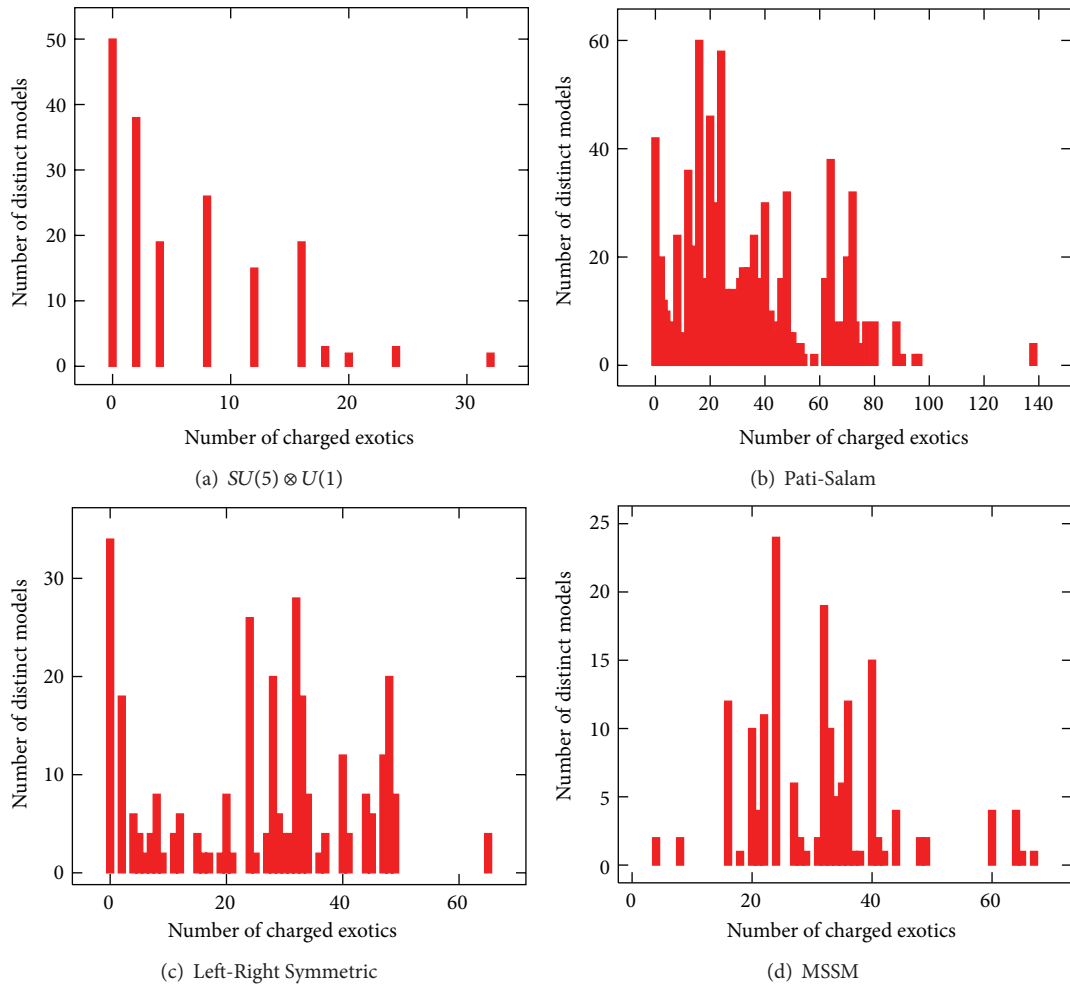
the number of non-Abelian singlets can get quite high. While most models have between 50 and 80, there can be up to 250 non-Abelian singlets in a model. This implies that many models in this data set cannot be viable candidates for quasi-realistic or realistic models.

3. Layer 1, Order 3 Extensions

As was the case with the NAHE extensions, there are more distinct NAHE variation $L1O3$ extensions than $L1O2$ extensions. Out of 442,272 models built, 1,166 of them were unique. Based on the order-2 redundancies, the systematic uncertainty for this data set is estimated to be 2%. Their gauge group content is tabulated in Table 5(b).

TABLE 4: The GUT group content of the NAHE variation extensions data set.

GUT group	<i>L1O2</i>		<i>L1O3</i>	
	Number of unique models	Percentage of unique models	Number of unique models	Percentage of unique models
E_6	101	32.69%	68	5.832%
$SO(10)$	125	40.45%	271	23.24%
$SU(5) \otimes U(1)$	0	0%	165	14.15%
$SU(4) \otimes SU(2) \otimes SU(2)$	0	0%	125	10.72%
$SU(3) \otimes SU(2) \otimes SU(2)$	0	0%	61	5.232%
$SU(3) \otimes SU(2) \otimes U(1)$	0	0%	63	5.403%


 FIGURE 7: The number of charged exotics for $SU(5) \otimes U(1)$, Pati-Salam, Left-Right Symmetric, and MSSM-like models in the NAHE variation extensions.

As was the case with the *L1O2* data set, $U(1)$ is the most common gauge group. However, the percentage is significantly lower here, about 86% as opposed to 98%. This suggests that some of the added basis vectors are unifying the five $U(1)$ s in the NAHE variation into larger gauge groups. Also of note is the number of models with gauge groups of rank higher than 11. In the *L1O2* data set, there were only three models of this type, about 1%. In the *L1O3* data set, there were 28 models with this property, about 2.4%.

While it may seem from Table 5(b) that the order-3 models are more prone to enhancements, Figure 1(a) makes it clear that is not the case. The distribution of the number of gauge group factors for a model peaks between 9 and 11 factors, as opposed to the peak at 8 factors for the order-2 models. However, there are several models with enhancements, even some models with as few as 2 distinct gauge group factors in them, something not seen with the order-2 models. This implies there is a class of order-3 basis vectors

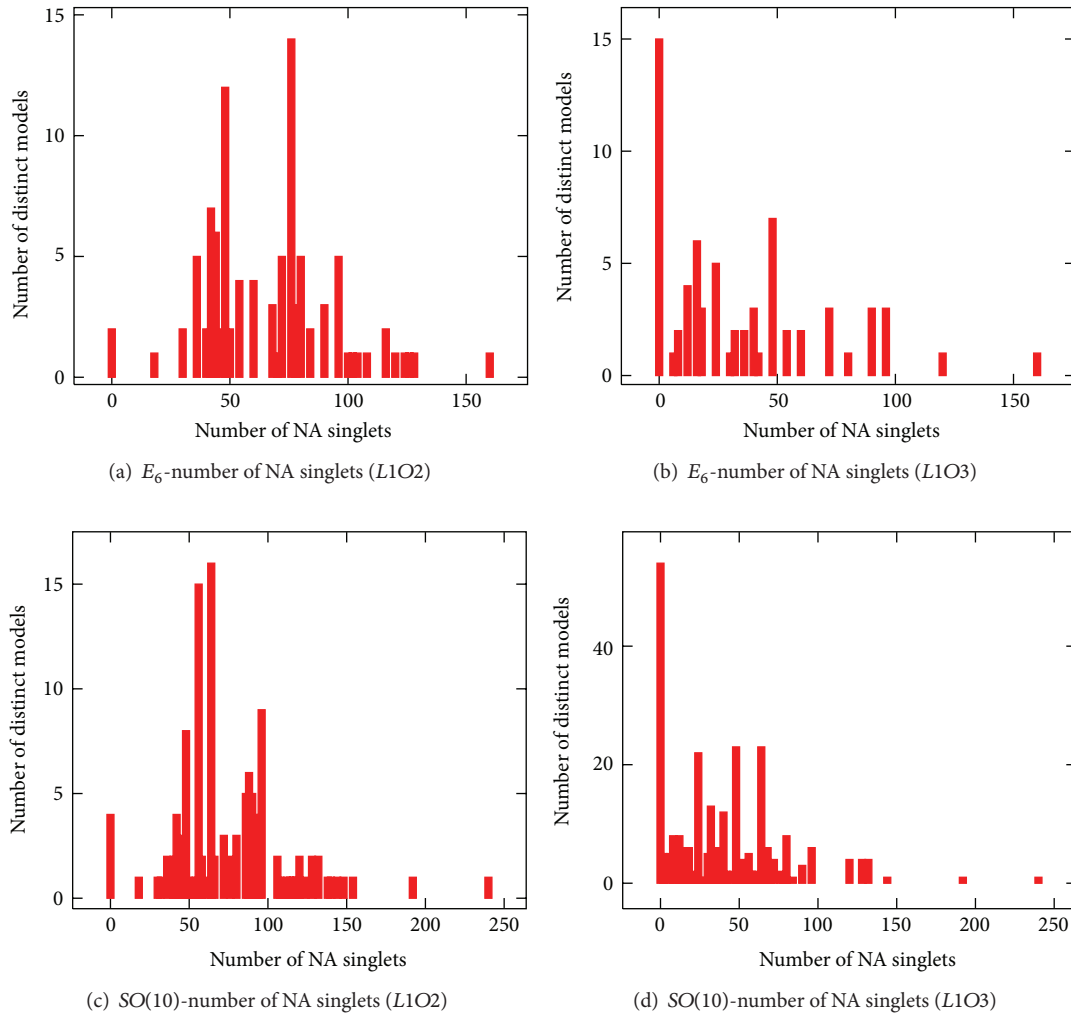


FIGURE 8: NA singlet statistics for the E_6 and $SO(10)$ models in the NAHE variation extensions data set.

that greatly enhances the gauge group symmetries, while most order-3 models break them.

The number of $U(1)$ gauge groups per model is plotted in Figure 1(c). The distribution of $U(1)$ peaks between 5 and 7. More interestingly, a nontrivial number of models do not have $U(1)$ symmetries at all. This implies, when combined with Figure 1(a), that in some models the $U(1)$ s are enhancing larger (but still small relative to $SO(22)$ and E_6) gauge groups. The mechanism producing this effect warrants further study, as it could be used to reduce the number of $U(1)$ factors for order-layer combinations that tend to produce too many $U(1)$ s. The frequency of the GUT groups is presented in Table 4.

The number of ST SUSYs is presented in Figure 1(b). While there are a statistically significant number of enhanced ST SUSYs (expected from models with odd-ordered right movers), the majority of these models has $N = 0$ ST SUSY.

The number of non-Abelian singlets is plotted in Figure 1(e). The distribution of non-Abelian singlets indicates that a large number of models do not have any non-Abelian

singlets. It is possible that this is related to the number of models with no $U(1)$ factors.

4. Models with GUT Groups

As a parallel to the NAHE extension study, the subsets of models containing the GUT groups E_6 , $SO(10)$, $SU(5) \otimes U(1)$, $SU(4) \otimes SU(2) \otimes SU(2)$ (Pati-Salam), $SU(3) \otimes SU(2) \otimes SU(2)$ (Left-Right Symmetric), and $SU(3) \otimes SU(2) \otimes U(1)$ (MSSM) are examined (see Figure 2). Like the NAHE study, the usual statistics will be reported along with the number of net chiral generations for models containing the GUT groups in question. If there is more than one way to configure an observable sector, each configuration will be counted when tallying the charged exotics and net chiral generations. For example, a model may have two E_6 groups with different matter representations. Each one would be counted individually when examining the number of charged exotics and net chiral generations.

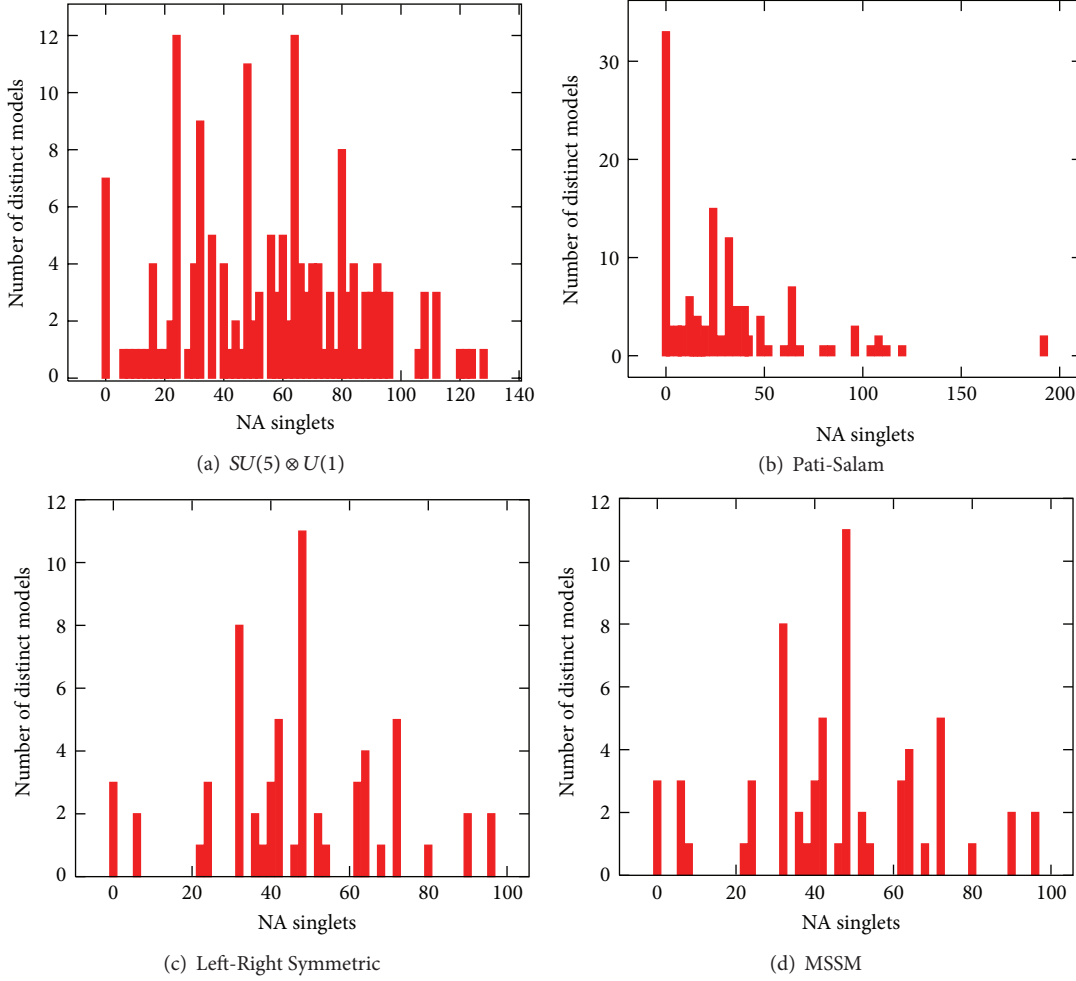


FIGURE 9: NA singlet statistics for the $SU(5) \otimes U(1)$, Pati-Salam, Left-Right Symmetric, and MSSM-like models. Note that these only arise as $L1O3$ extensions.

In order to calculate the net number of chiral fermion generations, we utilize the following expressions:

$$\begin{array}{ll}
 E_6 & |N_{27} - N_{\bar{27}}| \\
 SO(10) & |N_{16} - N_{\bar{16}}| \\
 SU(5) \otimes U(1) & |\min(N_{10}, N_{\bar{5}}) - \min(N_{\bar{10}}, N_5)| \\
 \text{Pati-Salam} & |N_{(4,2,1)} - N_{(\bar{4},2,1)}| \\
 \text{Left-Right Symmetric} & |N_{(3,2,1)} - N_{(\bar{3},2,1)}| \\
 \text{MSSM} & |N_{(3,2)} - N_{(\bar{3},2)}|, |N_{(3,1)} - N_{(\bar{3},1)}|.
 \end{array}$$

Upon analysis, it is found that the $L1O2$ extensions yield E_6 and $SO(10)$ observable sectors with net chiral generations while no models with $SU(5) \otimes U(1)$, $SO(6) \otimes SO(4)$, $SU(3) \otimes SU(2) \otimes SU(2)$, nor $SU(3) \otimes SU(2) \otimes U(1)$ have this property. This is a consequence of the fact that the latter groups only arise from $L1O3$ extensions which are not conducive to production of net chiral generations. The distribution of net chiral generations, as well as charged exotic matter, by gauge group is provided in Figures 6 and 7. The distributions of number of non-Abelian singlets, by gauge group, can be found in Figures 8 and 9.

In addition to matter content, the hidden sector gauge content is tabulated for each of the aforementioned gauge groups: Tables 6, 7, and 8. We can see from Table 4 that the NAHE variation extensions favor E_6 and $SO(10)$ over the other groups. This is easily understood as E_6 is already present and the breaking E_6 to $SO(10)$ is rather straight forward. However, in order to produce the low-rank $SU(n+1)$ groups, either the $U(1)$ s must be enhanced or there must be significant breaking of either the E_6 or $SO(22)$. However, neither of these readily occur with a single layer or at low order.

4.1. ST SUSYs. The distributions of ST SUSYs for the entire data set can be found in Figure 1(b) with a breakdown by gauge group in Figure 3.

The $L1O2$ models all have the same distributions regardless of which GUT is chosen. In these models, the gauge content does not statistically couple with the ST SUSY. For the $L1O3$ models, however, some of the GUT groups do appear to have such a coupling. In particular, the occurrence of E_6

TABLE 5: The gauge group content of the NAHE variation data set.

(a) Layer 1, order 2		
Gauge group	Number of unique models	Percentage of unique models
$SU(2)$	131	42.39%
$SU(2)^{(2)}$	18	5.825%
$SU(4)$	33	10.68%
$SU(6)$	99	32.04%
$SU(8)$	1	0.3236%
$SU(10)$	1	0.3236%
$SO(5)$	18	5.825%
$SO(7)$	12	3.883%
$SO(9)$	18	5.825%
$SO(11)$	14	4.531%
$SO(13)$	18	5.825%
$SO(15)$	12	3.883%
$SO(17)$	18	5.825%
$SO(19)$	18	5.825%
$SO(21)$	18	5.825%
$SO(8)$	30	9.709%
$SO(10)$	125	40.45%
$SO(12)$	38	12.3%
$SO(14)$	33	10.68%
$SO(16)$	33	10.68%
$SO(18)$	38	12.3%
$SO(20)$	36	11.65%
$SO(22)$	31	10.03%
$SO(24)$	2	0.6472%
$SO(32)$	1	0.3236%
E_6	101	32.69%
E_7	3	0.9709%
E_8	1	0.3236%
$U(1)$	304	98.38%

(b) Layer 1, order 3

Gauge group	Number of unique models	Percentage of unique models
$SU(2)$	731	62.69%
$SU(3)$	128	10.98%
$SU(4)$	355	30.45%
$SU(5)$	165	14.15%
$SU(6)$	167	14.32%
$SU(7)$	75	6.432%
$SU(8)$	143	12.26%
$SU(9)$	164	14.07%
$SU(10)$	169	14.49%
$SU(11)$	137	11.75%
$SU(12)$	56	4.803%
$SU(13)$	4	0.3431%

(b) Continued.

Gauge group	Number of unique models	Percentage of unique models
$SU(14)$	1	0.08576%
$SO(8)$	376	32.25%
$SO(10)$	271	23.24%
$SO(12)$	151	12.95%
$SO(14)$	81	6.947%
$SO(16)$	106	9.091%
$SO(18)$	28	2.401%
$SO(20)$	69	5.918%
$SO(22)$	5	0.4288%
$SO(24)$	11	0.9434%
$SO(28)$	13	1.115%
$SO(30)$	1	0.08576%
$SO(32)$	2	0.1715%
$SO(36)$	1	0.08576%
E_6	68	5.832%
E_7	24	2.058%
E_8	9	0.7719%
$U(1)$	1002	85.93%

models $N = 2$ ST SUSY is disproportionately high while $SU(5) \otimes U(1)$, Left-Right Symmetric, and MSSM models with $N = 1$ ST SUSY have a reduced occurrence. As all of the models containing these GUTs have at least a single $U(1)$, there could be a correlation between the number of $U(1)$ s and the number of ST SUSYs. Further investigations of these findings show several statistical couplings for higher ST SUSY models containing certain gauge group factors. The methodology used to analyze these couplings was detailed in [58]. The observed significances are plotted in Figures 4 and 5 for the $L1O2$ and $L1O3$ NAHE variation extensions, respectively.

While there are no significant gauge groups in the $L1O2$ extensions, several groups are significant with regard to enhanced ST SUSYs in the NAHE $L1O3$ extensions. In particular, the three exceptional groups, as well as $SO(12)$, $SU(12)$, $SU(13)$, $SU(14)$, and $SO(36)$, all have a significant statistical correlation with the average number of ST SUSYs. This is likely due to the additional basis vector adding a gravitino generating sector, which is common with odd-order extensions, and additional roots for the gauge groups. Further analysis will be needed to confirm the cause of this significance. It is also worth noting that one group, $SU(5)$, has a negative impact on ST SUSYs. If this trend occurs for more odd-ordered extensions of the NAHE variation, it may affect the viability of realistic flipped- $SU(5)$ models derived from this variation.

5. Models with Mirroring

The larger sets of matching boundary conditions, seen in Table 1, are expected to lead to models with mirrored gauge

TABLE 6: The hidden sector gauge group content for the NAHE variation extension models with E_6 observable.

(a) Layer 1, order 2

Gauge group	Number of unique models	Percentage of unique models
$SU(2)$	14	13.86%
$SU(2)^{(2)}$	8	7.921%
$SU(4)$	10	9.901%
$SO(5)$	6	5.941%
$SO(7)$	2	1.98%
$SO(9)$	6	5.941%
$SO(11)$	6	5.941%
$SO(13)$	6	5.941%
$SO(15)$	2	1.98%
$SO(17)$	6	5.941%
$SO(19)$	8	7.921%
$SO(21)$	6	5.941%
$SO(8)$	8	7.921%
$SO(10)$	14	13.86%
$SO(12)$	14	13.86%
$SO(14)$	9	8.911%
$SO(16)$	9	8.911%
$SO(18)$	14	13.86%
$SO(20)$	12	11.88%
$SO(22)$	8	7.921%
E_8	1	0.9901%
$U(1)$	101	100%

(b) Layer 1, order 3

Gauge group	Number of unique models	Percentage of unique models
$SU(2)$	31	45.59%
$SU(3)$	1	1.471%
$SU(4)$	12	17.65%
$SU(6)$	4	5.882%
$SU(8)$	6	8.824%
$SU(9)$	10	14.71%
$SU(10)$	8	11.76%
$SU(11)$	5	7.353%
$SU(12)$	4	5.882%
$SU(13)$	1	1.471%
$SO(8)$	9	13.24%
$SO(10)$	15	22.06%
$SO(12)$	12	17.65%
$SO(14)$	5	7.353%
$SO(16)$	3	4.412%
$SO(18)$	4	5.882%
$SO(20)$	2	2.941%
$SO(22)$	2	2.941%
E_8	2	2.941%
$U(1)$	68	100%

TABLE 7: The hidden sector gauge group content for the NAHE variation extension models with $SO(10)$ observable.

(a) Layer 1, order 2

Gauge group	Number of unique models	Percentage of unique models
$SU(2)$	23	18.4%
$SU(2)^{(2)}$	8	6.4%
$SU(4)$	10	8%
$SU(6)$	10	8%
$SO(5)$	6	4.8%
$SO(7)$	2	1.6%
$SO(9)$	6	4.8%
$SO(11)$	6	4.8%
$SO(13)$	6	4.8%
$SO(15)$	2	1.6%
$SO(17)$	6	4.8%
$SO(19)$	8	6.4%
$SO(21)$	6	4.8%
$SO(8)$	8	6.4%
$SO(12)$	35	28%
$SO(14)$	10	8%
$SO(16)$	10	8%
$SO(18)$	14	11.2%
$SO(20)$	12	9.6%
$SO(22)$	9	7.2%
E_6	14	11.2%
E_7	1	0.8%
$U(1)$	125	100%

(b) Layer 1, order 3

Gauge group	Number of unique models	Percentage of unique models
$SU(2)$	155	57.2%
$SU(3)$	27	9.963%
$SU(4)$	59	21.77%
$SU(5)$	14	5.166%
$SU(6)$	59	21.77%
$SU(7)$	22	8.118%
$SU(8)$	24	8.856%
$SU(9)$	36	13.28%
$SU(10)$	26	9.594%
$SU(11)$	19	7.011%
$SU(12)$	11	4.059%
$SU(13)$	1	0.369%
$SU(14)$	1	0.369%
$SO(8)$	48	17.71%
$SO(12)$	35	12.92%
$SO(14)$	22	8.118%
$SO(16)$	10	3.69%
$SO(18)$	7	2.583%
$SO(20)$	2	0.738%
$SO(22)$	3	1.107%
E_6	15	5.535%

(b) Continued.

Gauge group	Number of unique models	Percentage of unique models
E_7	4	1.476%
E_8	2	0.738%
$U(1)$	271	100%

TABLE 8: The hidden sector gauge group content for the NAHE variation extension $L1O3$ models with GUT observable.

(a) Left-Right Symmetric

Gauge group	Number of unique models	Percentage of unique models
$SU(4)$	12	19.67%
$SU(7)$	14	22.95%
$SU(8)$	7	11.48%
$SU(9)$	9	14.75%
$SU(10)$	12	19.67%
$SU(11)$	17	27.87%
$SU(12)$	2	3.279%
$SO(8)$	8	13.11%
$SO(10)$	6	9.836%
$U(1)$	61	100%

(b) MSSM

Gauge group	Number of unique models	Percentage of unique models
$SU(4)$	13	20.63%
$SU(6)$	1	1.587%
$SU(7)$	14	22.22%
$SU(8)$	7	11.11%
$SU(9)$	9	14.29%
$SU(10)$	12	19.05%
$SU(11)$	18	28.57%
$SU(12)$	3	4.762%
$SO(8)$	8	12.7%
$SO(10)$	6	9.524%

(c) $SU(5) \otimes U(1)$

Gauge group	Number of unique models	Percentage of unique models
$SU(2)$	87	52.73%
$SU(3)$	19	11.52%
$SU(4)$	28	16.97%
$SU(6)$	8	4.848%
$SU(7)$	20	12.12%
$SU(8)$	23	13.94%
$SU(9)$	34	20.61%
$SU(10)$	35	21.21%
$SU(11)$	32	19.39%
$SU(12)$	1	0.6061%
$SO(8)$	22	13.33%
$SO(10)$	14	8.485%
$SO(12)$	7	4.242%
$SO(14)$	5	3.03%

(d) Pati-Salam

Gauge group	Number of unique models	Percentage of unique models
$SU(3)$	12	9.6%
$SU(5)$	8	6.4%
$SU(6)$	25	20%
$SU(8)$	29	23.2%
$SU(9)$	24	19.2%
$SU(10)$	15	12%
$SU(11)$	3	2.4%
$SU(12)$	7	5.6%
$SO(8)$	9	7.2%
$SO(10)$	11	8.8%
$SO(12)$	22	17.6%
$SO(14)$	19	15.2%
$SO(16)$	4	3.2%
$SO(20)$	2	1.6%
E_6	1	0.8%
$U(1)$	123	98.4%

groups and matter states. Only one model, generated by Table 9(a), in those discussed thus far exhibits full-gauge mirroring. However, the matter states are not mirrored. The particle content of that model is presented in Table 9(b).

The gauge groups are completely mirrored, and the matter representations are almost mirrored between one another. There is a state charged as a **16** under both $SO(16)$ groups and one charged as a **128** under one of the $SO(16)$ groups, but not the other. Thus, the matter is not mirrored. The potential for mirroring is clear from the basis vectors: $\bar{\psi}^{1,\dots,5}$ and $\bar{\eta}^{1,2,3}$ are mirrored with $\bar{\phi}^{1,\dots,8}$. There are also many models in which the observable and some of the hidden matter are mirrored, but include a shadow sector gauge group for which matter representations are not coupled.

These have been presented and discussed in [50].

6. Conclusions

Though there were many models containing GUTs in the data sets explored in this study, a vast majority of them do not contain any net chiral fermion generations. No three-generation models were found. These conclusions are summarized in Table 3.

While there were more models with GUT gauge groups in the NAHE variation $L1O3$ extensions, none of them had any net chiral matter generations, implying that the added basis vector produces the barred and unbarred generations in even pairs, if at all. More complicated basis vector sets will need to be studied to determine if any NAHE variation-based quasi-realistic models can be constructed.

The distribution of ST SUSYs across the subsets of GUT models was also examined. It was concluded that, as was the

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