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#### An approach for predicting the stability of vertical cuts in cohesionless soils above **Q2**1 the water table OK Samuel A. Stanier<sup>a</sup>, Alessandro Tarantino<sup>b,\*</sup> Q13 Centre for Offshore Foundation Systems, The University of Western Australia, Australia Department of Civil Engineering, University of Strathclyde, UK Change Department of Civil and Environmental Engineering ARTICLE INFO ABSTRACT 7 8 Article history: Temporary vertical excavations in cohesionless (granular) soils pose a problem for conventional 'two-phase' 23 Received 1 December 2011 soil mechanics theory since non-zero collapse height is not predicted using the classical 'dry/saturated' shear 24 10 Received in revised form 4 March 2013 strength criterion, given that cohesionless soils above the water table are assumed to be dry. An extension 25 11 Accepted 10 March 2013 of the classical shear strength equation to account for the effect of matric suction on the effective stress in 26 12 Available online xxxx partially saturated soil is presented here that is incorporated into the bound theorems of plasticity. A simple 27 18 validation experiment is reported to test the concept following which, a case study is presented that explores 28 Keywords: 16 the extent to which matric suction and its impact on shear strength can explain the large safe vertical cut 29 Excavation 17height that is often observed in cohesionless pozzolan deposits in the field. Lastly, the impact of rainfall 30 18 Laboratory tests events and subsequent ponded infiltration is investigated using a very simple analytical technique based 31 19 Limit analysis 20 Partial saturation on the classical Terzaghi consolidation solution. The research presented here gives practitioners with no 32 21 Shear strength particular expertise in the mechanics of unsaturated soil, techniques to assess the stability of geostructures 33 22Suction involving unsaturated cohesionless soils that are based on simple calculation techniques taught in under- 34 graduate courses. 35 © 2013 Published by Elsevier B.V. 36 4038 39 river-planform evolution 2004). These mechanisms should potentially be incorporated into 61 1. Introduction 41

The stability of vertical excavations in cohesionless (granular) 42soils is an important problem in geotechnical engineering and engi-43neering geology. Because excavations are typically carried out above 44 the water table cohesionless soils are unsaturated. In routine geotech-45nical engineering and engineering geology calculations cohesionless 46 47 soils (with no or little clay fraction) above the water table are generally assumed to be dry. Nonetheless this assumption is not accurate. 48 Soils above the water table, due to matric suction, are in fact par-49

tially saturated and also exhibit significantly higher shear strength 5051than dry soils. As a result, vertical cuts up to several metres in height may remain stable (Tsidzi, 1997; Whenham et al., 2007; De Vita et al., 522008) in cohesionless soils. The beneficial effect of partial saturation 5354is often exploited by contractors who typically cover the bank adjacent to the excavation with an impermeable membrane to divert sur-55 face runoff during heavy rainfall, thus preserving partial saturation. 5657The beneficial effect of partial saturation on the stability of vertical and near-vertical cuts is recognised by engineering geologists when 5859analysing and modelling bank retreat and delivery of bank sediments 60 to river (Rinaldi and Casagli, 1999; Simon et al., 2000; Rinaldi et al.,

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morphodynamic models of the evolution river planforms (Langendoen 62 Q3 et al., 2012; Nardi et al., 2012). Partial saturation plays an important 63 role in the stability of trenches (Vanapalli and Oh, 2012), which are 64 used in a variety of applications in assessing geologic hazards in engi- 65 neering geology, and tailing dams (Zandarín et al., 2009). The effect of 66 partial saturation is also well known to children when erecting sand 67 castles.

Classical 'dry/saturated' soil mechanics fails to predict a non-zero 69 safe vertical cut height in cohesionless soils above the water table, as 70 they are assumed to be dry. In theory a dry cohesionless soil exhibits a 71 zero collapse height, as is evidenced by the lower bound theorem of 72 plasticity (Chen, 2007) or experimentally by observation, since it is 73 impossible to fabricate a cylindrical sample of dry sand.

However, practitioners and academicians still find it convenient to 75 disregard the contribution of partial saturation to shear strength as 76 this leads to conservative design. This point of view can be questioned. 77 Significant costs might be saved if 'new' geostructures are designed to 78 account for the effects of partial saturation. Furthermore, geotechnical 79 engineers and engineering geologists are often confronted with 'existing' 80 stable yet potentially hazardous geostructures, e.g. steep slopes, for 81 which conventional soil mechanics theory offers no explanation of 82 the current state of equilibrium. In this case, a realistic analysis of the 83 current state of stress is required, including characterisation of the 84 partially saturated zone above the water table. This is essential when 85 assessing the likelihood of future instability and hence, is a key to 86

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ensuring the proposal of appropriate precautionary or remedialmeasures.

To quantify the effects of partial saturation on the stability of geostructures, methods should be developed to analyse collapse conditions in cohesionless partially saturated soils. So far, this problem has received little attention from researchers working on the mechanical behaviour of unsaturated soils.

This paper presents an approach based on the upper and lower bound theorems of plasticity. By assuming that the shear strength of partially saturated soils is controlled by the average skeleton stress, the classical approach developed for dry and saturated soils can easily be extended to cater for problems involving partially saturated soils.

Experimental evidence of the validity of this concept is provided 99 in the form of collapse tests performed on cylindrical samples of par-100 tially saturated sand. Because changes in suction and vertical stress 101 along the sample height are not negligible, this unconfined compres-102 sion test is regarded as a boundary value problem rather than an ele-103 ment test. The theoretical analysis of the column collapse load based 104 on the upper and lower bound theorems is thus essentially the same 105as the analysis that will be carried out to determine the collapse 106 height of a vertical cut. 107

The principal goal of the paper is to verify whether the upper and lower bound collapse loads determined theoretically, bracket closely the values observed in the model tests. This is aimed at validating an approach to predict the collapse height of unsaturated cohesionless soils based on the bound theorems of plasticity.

A case study concerning the safe unsupported vertical cut height potentially achievable in pyroclastic silty sand (Pozzolan deposits) is then presented. This illustrates the utility of the proposed extension of the bound theorems of plasticity when assessing geotechnical and engineering geology problems in the field involving unsaturated soils.

## 118 2. Extension of the bound theorems of plasticity to119 unsaturated soils

The upper and lower bound theorems of plastic collapse set limits to the collapse load of a structure and can be proven for the case of perfectly plastic materials with associated flow rule (Chen, 2007). In two-phase soils, the failure (yield) criterion under ultimate conditions can be defined by the following equation:

$$\tau = (\sigma - u) \tan \phi' \tag{1}$$

where  $\tau$  is the shear stress,  $\sigma$  is the normal stress, u is the pore pressure and  $\phi'$  is the effective angle of shearing resistance. Pore pressure equals the pore-water pressure  $u_w$  in saturated soils and the pore-air pressure  $u_a$  in ideally dry soils. Using the failure criterion given by Eq. (1), the ultimate conditions of soil structures such as retaining walls, foundations, vertical cuts, and slopes can be assessed for saturated and dry soil (Atkinson, 1981; Chen, 2007).

The application of bound theorems of plasticity to soil structures above the water table requires the definition of a suitable failure criterion for partially saturated soils. For compacted (aggregated) soils, shear strength under partially saturated states can be expressed by the following equation (Tarantino and Tombolato, 2005):

$$\tau = (\sigma - u_w S_{re}) \tan \phi' = (\sigma + s S_{re}) \tan \phi'$$
<sup>(2)</sup>

where  $u_w$  is the pore-water pressure, *s* is the suction ( $s = -u_w$ ), and *S<sub>re</sub>* is an effective degree of saturation (degree of saturation of the macro-pores), which is given by:

$$S_{re} = \frac{e_w - e_{wm}}{e - e_{wm}} \tag{3}$$

where *e* is the void ratio (volume of voids per volume of solids),  $e_w$ is the water ratio (volume of water per volume of solids), and  $e_{wm}$  is the 'microstructural' water ratio, which separates the region of 145 inter-aggregate porosity from the region of intra-aggregate porosity 146 (Romero and Vaunat, 2000). The parameter  $e_{wm}$  may conveniently 147 be determined by best fitting of shear strength data and the validity 148 of Eq. (2) in conjunction with Eq. (3) has been proven by Tarantino 149 (2007) and Tarantino and El Mountassir (in press) for a wide range 150 of clayey soils, including compacted, and natural soils.

On the other hand, reconstituted and non-clayey soils are generally 152 non-aggregated and the 'microstructural' water ratio  $e_{\rm wm}$  may there-153 fore be expected to be zero for these soils. Indeed, this has been demon-154 strated to be the case for a wide range of non-clayey soils by Tarantino 155 and El Mountassir (in press). 156

For non-aggregated soils, the failure criterion can therefore be 157 defined by the following equation (Öberg and Sällfors, 1997): 158

$$\tau = (\sigma - u_w S_r) \tan \phi' = (\sigma + sS_r) \tan \phi'.$$
(4)

If Eq. (2) or (4) is used in place of Eq. (1), collapse of geostructures 161 in partially saturated soils can be analysed in a very similar manner 162 by introducing a few simple modifications. To derive the upper bound 163 solution, the work done by the internal stresses  $W_i$  for the case of translational failure can be written as (assuming an effective cohesion c' = 0): 165

$$W_i = \delta \sin \phi' \int_l s S_{re} dl \tag{5}$$

where  $\delta$  is the magnitude of the block displacement,  $\phi'$  is the effective 166 (saturated) angle of shearing resistance, *s* is the suction,  $S_{re}$  is the effective 168 degree of saturation, and *l* is the length of the failure surface. It is worth 169 mentioning that the work done by the internal stresses  $W_i$  is written 170 here in terms of total stresses whereas the external work associated 171 with the gravitational load is calculated by considering the (total) soil 172 unit weight.

To derive the lower bound solution, the failure criterion must not 174 be exceeded at any point in the soil. This occurs if none of the Mohr's 175 circles cross the failure envelope in the  $\sigma + sS_{re}$ ,  $\tau$  plane (rather than 176 the  $\sigma'$ , $\tau$  plane as in the case of saturated or dry soils). 177

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## 3. Laboratory validation

Experimental verification of the proposed extension to the bound 180 theorems of plasticity was performed using a fine silica sand with grain 181 size range of 0.075–0.2 mm and specific gravity,  $G_s$ , of 2.73 (derived 182 experimentally). This material was expected to commence desaturation 183 under applied suctions of less than 5–10 kPa, allowing a simple nega-184 tive water column technique to be used to apply suctions to the base 185 of a sample. 186

3.2. Water retention behaviour 187

3.2.1. Apparatus

To derive the water retention characteristics of the fine sand a 189 simple negative water column method was employed. The apparatus 190 used is shown schematically in Fig. 1. A cylindrical cell was used to 191 house the sand sample and allow application of suction at the base. 192 Different magnitudes of suction were applied to the sand sample by 193 raising and lowering a water reservoir on a frame. A ThetaProbe 194 sensor (Delta-T Devices Ltd., 1999) was placed in the sample at the 195 surface to measure the volumetric water content at a known location. 196 A high air-entry filter (with an air entry value greater than the maxinum suction to be applied during the experimental procedure) was 198 specifically devised to provide an interface between the sand and the 199 hydraulic reservoir, thus maintaining suction. 200

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Fig. 1. Schematic of apparatus used to derive soil water retention behaviour of very fine uniform sand.

### 201 3.2.2. Sensor for water content measurement

The ThetaProbe sensor was used to measure the bulk dielectric permittivity of the soil, which is then correlated to the soil water content via calibration. The probe has a sensing length of 60 mm and the measurements taken in this investigation were assumed to be representative of the soil water content at the mid-depth of the probe (i.e. 30 mm from the surface of the sample).

The sensor outputs a voltage that is correlated to the soil bulk dielectric permittivity  $\varepsilon$  by the following relationship:

$$\sqrt{\varepsilon} = 1.07 + 6.4 \cdot V - 6.4 \cdot V^2 + 4.7 \cdot V^3 \tag{6}$$

where *V* is the output voltage of the probe (Gaskin and Miller, 1996;
Delta-T Devices Ltd., 1999). To convert the dielectric permittivity
measurement to the soil water content the following relationship is
suggested by the manufacturer:

$$\theta = \frac{\sqrt{\varepsilon} - a_0}{a_1} \tag{7}$$

216 where  $a_0$  and  $a_1$  are soil specific calibration parameters.

To confirm the accuracy of the relationship in Eq. (6), the dielectric constant of some common laboratory solvents (Acetone, Acetic Acid and Ethanol) was measured and checked against values quoted by Budevsky (1979), yielding an average percentage discrepancy of approximately  $\pm$  1.2%, which was deemed acceptable.

Soil specific calibration of parameters  $a_0$  and  $a_1$  was then conducted 222 223 on silica sands compacted into a mould of 150 mm height and 100 mm diameter. Compaction was achieved in three layers using a 250 g sliding 224hammer dropped from a height of 300 mm, with fifteen blows being 225 applied per layer. Four target soil water contents in the range of 0–0.35 226were tested to represent dry, damp, wet and saturated samples in both 227 fine sand and coarse sand with grain size ranges of 0.075-0.2 mm and 2280.4–0.6 mm respectively. After compaction of the sample the ThetaProbe 229was inserted and measurements taken for a period of 10 min, from 230which the time averaged root dielectric value was calculated using 231 232 Eq. (6). Following this the soil water content of each sample was derived experimentally. Fig. 2 shows a plot of the measured root 233 dielectric permittivity of the fine and coarse silica sand with respect 234 to the measured volumetric water content showing that soil dielectric 235 permittivity was not significantly grain size dependent. The calibration 236 parameters  $a_0$  and  $a_1$  were determined using the method of least 237 squares, yielding values of 1.492 and 9.743 respectively. The average 238 discrepancy of the calibration function from the measured soil water 239 content was  $\pm$  0.03, which is less than the capability of the device as 240 quoted by the manufacturer and thus deemed acceptable. 241

### 3.2.3. High air entry filter preparation

A simple high air entry filter was created using uniform silt with 243 an estimated air-entry suction of approximately 20–30 kPa. The filter 244 allows the transmission of water relatively rapidly at low applied suctions (0–15 kPa) but not air, thus allowing hydraulic suction to be 246 maintained at the base of the sample. 247

The silt filter has two critical advantages in comparison to com- 248 mercial high air-entry porous ceramics. It provides adequate air-entry 249 suction for sand whilst ensuring higher hydraulic conductivity and sub- 250 sequently shorter equalisation periods than for example, a commercial 251 100 kPa air-entry suction ceramic. Additionally, it ensures proper con- 252 tact with the sand and eliminates possible wall effects (large pores 253 at the interface between a flat surface and a granular material) that 254 could prevent suction being transmitted to the sample. 255

To construct the filter, first, a woven mesh was placed in the base 256 of the test chamber, which was covered by a paper filter. Liquefied silt 257 slurry was then poured on top of the filter paper and allowed to settle 258 under gravity, generating a targeted 10 mm depth of filter. Excess 259 water was then drained from the base, with clear water indicating a 260 successful filter and cloudy water indicating failure. Following suc- 261 cessful generation of the filter a test suction of 17 kPa was applied 262 (which was greater than the target maximum suction of 15 kPa), 263 whilst allowing complete drainage of the cylindrical cell and consoli- 264 dation of the filter without filter desaturation. This exposed the filter 265 to air, thus testing the ability of the filter to maintain hydraulic suc- 266 tion at the base of the sample. Before use each of the filters was tested 267 in this manner.

### 3.2.4. Experimental procedure

Following creation of a successful air entry filter oven dried fine 270 silica sand was rained into the cell, to attain a sample height of 271 150 mm with uniform density. The ThetaProbe was then placed into 272 the centre of the sample, with an accompanying latex cover being 273 used to isolate the sample from the atmosphere, thus minimising 274 evaporation of pore water from the sample to the atmosphere. The 275 cell was connected to the hydraulic reservoir using transparent plastic 276 tubing, with an air trap at the point of lowest pressure in the system. 277



**Fig. 2.** Calibration of parameters  $a_0$  and  $a_1$  for fine and coarse grained silica sands.

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Upon assembly of the apparatus, the water reservoir was raised above
the surface of the sand in the cylindrical cell to commence saturation,
which was achieved when the water table was observed to be above
the surface of the sand and the ThetaProbe was indicating a constant
measurement.

After saturation of the sample, the drying phase was initiated by lowering the water reservoir in increments followed by the wetting phase by raising the water reservoir. This allowed the investigation of the hysteretic hydro-mechanical properties of the soil.

### 287 3.2.5. Experimental results

Fig. 3 presents the change in soil volumetric water content ( $\theta$ ) 288with respect to time in hours, with the final measurement points used 289 to define the soil water retention drying and wetting curves indicated. 290 A change in sample porosity was evident between the start and the 291 end of the experiment. Fleuerau et al. (1993) observed in silty non-292 plastic soils that changes in void ratio were apparent during the drying 293 phase but only significantly before the air entry suction was reached. If 294the same behaviour is assumed to be apparent here it is reasonable to 295assume all volumetric changes occurred before the air entry suction 296of the sand was reached. The porosity at all suctions exceeding the 297air-entry value could thus be assumed to be equal to the final porosity, 298299 which was measured at the end of the experiment.

After correction of the initial soil water content measurement based upon this assumption, the van Genuchten (1980) relationship describing soil water retention characteristics was fitted using the least squares method for both the drying and wetting water retention curves as illustrated in Fig. 4. The following equations were used to model the main drying curve and the scanning wetting curve respectively:

 $S_r = \left(\frac{1}{1 + (\alpha_d s)^{n_d}}\right)^{m_d}$  (Main drying)

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$$S_r = S_{r0} + (1 - S_{r0}) \left(\frac{1}{1 + (\alpha_w s)^{n_w}}\right)^{m_w} \quad \text{(Scanning wetting)}. \tag{9}$$

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The scanning wetting curve was modelled by setting a 'residual' degree of saturation  $S_{r0}$  greater than 0. Table 1 summarises the Van-Genuchten parameters fitted for both the drying and wetting paths.

The difference in parameters used to fit the Van-Genuchten relationship is evidence of the hysteretic behaviour of the silica sand investigated. Thus for a given suction, two distinct degrees of saturation could exist dependent upon whether the soil is in a drying or







Fig. 4. Water retention curves for drying and wetting paths fitted using the Van-Genuchten relationship.

wetting cycle. Thus in relation to shear strength, if the shear strength 319 of the sand is assumed to be a function of suction multiplied by degree 320 of saturation, then the soil can exhibit two distinct shear strengths at the 321 same suction, depending on whether the degree of saturation lies on the 322 drying or wetting curve. This hypothesis was investigated by performing 323 simple column collapse tests on samples on both the drying and wetting paths. 325

A 100 mm diameter triaxial base and split-form was used in place 328 of the cylindrical cell to form the samples for the column collapse tests. 329 A high air entry filter was created in the base of the split-form following 330 the same method as previously described for the soil water retention 331 experiment (Figure 5). (Figure 5)

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### 3.3.2. Experimental procedure

Following testing of the air entry filter, oven-dried fine sand was 334 rained into the split-form to create a sample of uniform density, with 335 depth of 180 mm and diameter of 100 mm/Next the sample was satu- 336 rated by raising the water reservoir to provide a small positive head 337 potential at the surface of the sample. This was followed by either dry-338 ing to a target applied suction or drying to an applied suction of 8.2 kPa, 339 followed by wetting to a target applied suction at the base of the sam- 340 ple. Due to a ThetaProbe not being placed in-situ in the sample, to 341 facilitate collapse testing on a virgin sample, it was not possible to 342 observe constant soil-water content using the ThetaProbe in these ex- 343 periments. As a result, a period of 24 h was allowed for equalisation of 344 matric suction following the application of a suction increment either 345 in drying or wetting. This was seen as a conservative estimate of the 346 time required for equalisation of suctions within the sample according 347 to the response observed in the water retention test. 348

After the allowed equalisation period the split-form was removed, 349 revealing a cylindrical column of sand that could be loaded in com- 350 pression to failure. Loading was facilitated using a triaxial loading 351

Table 1         Van-Genuchten parameters fitted for drying and wetting hydro-mechanical behaviours				
Main drying		Scanning wetting		t1.3
$\alpha_d$	0.219	$\alpha_w$	0.384	t1.4
n <sub>d</sub>	5.81	n <sub>w</sub>	29.10	t1.5
$m_d$	0.32	$m_w$	0.046	t1.6
		$S_{r0}$	0.15	t1.7

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Fig. 5. Schematic of apparatus used to generate collapse in the sand sample.

cap and a plastic hopper, into which small ball bearings were placed
until failure. The mass of the loading cap and ball bearings at failure
allowed calculation of the failure boundary pressure for the sample.

#### 355 **3.3.3.** *Experimental results*

Collapse boundary pressures are plotted against the suction applied
 at the base of the sample in Fig. 6. The results clearly show that there is a
 hysteretic effect and it will later be demonstrated that this is associated
 with the hysteresis of the water retention curve.



Fig. 6. Collapse boundary stresses measured on samples subjected to drying and wetting hydraulic paths.

3.4. Prediction of the upper and lower bounds of collapse pressure 360

#### 3.4.1. Failure criterion

The following failure criterion was adopted for the sand according 362 to Öberg and Sällfors (1997): 363

$$\mathbf{r} = (\sigma + sS_r)\tan\phi'. \tag{10}$$

The internal angle of friction  $\phi'$  of the fine sand was estimated in a 366 very simple manner using a tilting slide mechanism. Sand was placed 367 in a Perspex slide formed from three pieces of Perspex to make a slide 368 1 m long and 0.15 m wide with sides to contain the sand and a rough 369 surface along the base. The sand was placed in a uniform thickness of 370 approximately 30 mm depth. The slide was then tilted until move- 371 ment of the sand was observed; indicating the angle of the slope of 372 the slide had exceeded the angle of friction of the sand material. 373 The slide was then tilted back toward horizontal until the movement 374 of the sand subsided. At which point the angle of the slide was calcu- 375 lated using simple trigonometry; thus giving an estimate of  $\phi' = 32^{\circ}$  376 for the critical angle of friction for the sand material. This simple method 377 was preferred to the more conventional direct shear or triaxial tests 378 as the low stresses were more representative of those apparent in 379 the experiments presented in the previous section. 380

#### 3.4.2. Estimating degree of saturation

To model shear strength by Eq. (10), the degree of saturation  $S_r$  <sup>382</sup> needs to be estimated as a function of suction. For the case where tests <sup>383</sup> were performed along the draining path, the main drying curve given <sup>384</sup> by Eq. (9) was used because points at any elevation in the sample all <sup>385</sup> desaturated from a saturated state (State 0 in Fig. 7: <sup>386</sup>

For the case where the sample was wetted after being partially  $_{387}$  dried by lowering the reservoir to  $H_w^*$  (see Figure 7), the scanning  $_{388}$  curve given by Eq. (10) was used. As points at different elevations  $_{389}$  in the sample had previously been dried to different degrees of satu-  $_{390}$  ration, they followed different scanning paths as illustrated in Fig. 7  $_{391}$  (hydraulic paths 1–2). The scanning wetting curve was modelled by  $_{392}$  scaling the wetting curve using the parameter  $S_{r0}$ . It can be demon-  $_{393}$  strated that this parameter can be derived as follows:  $_{394}$ 

$$S_{r0}(z) = \frac{\left(\frac{1}{1+[\alpha_d \cdot s^*(z)]^{n_d}}\right)^{m_d} - \left(\frac{1}{1+[\alpha_w \cdot s^*(z)]^{n_w}}\right)^{m_w}}{1 - \left(\frac{1}{1+[\alpha_w \cdot s^*(z)]^{n_w}}\right)^{m_w}}$$
(11)

where  $s^*(z)$  is the suction at the end of the drying process generated 396 by the water level  $H_w^*$  as shown in Fig. 7. 397

3.4.3. Lower bound solution of collapse boundary pressure

To derive the lower bound solution, we assume the axial and radial 399 directions to be principal stress directions. The axial and radial stress,  $\sigma_a$  400 and  $\sigma_r$  respectively, are therefore given by 401

$$\sigma_r = 0$$
  

$$\sigma_a = q + \left[\int_0^z \gamma(z) dz\right] \cdot z$$
(12)

where q is the applied pressure at the top of the sample, z is the depth 402 from the sample top surface, and q is the unit weight. The latter is in 404 turn a function of the degree of saturation: 405

$$\gamma = \gamma_s (1 - n) + \gamma_w Sn \tag{13}$$

where  $\gamma_s$  and  $\gamma_w$  are the specific weights of the solids and water respec- 400 tively  $\gamma_s = 26.7 \text{ kN/m}^3$  and  $\gamma_w = 9.81 \text{ kN/m}^3$ ) and *n* is the porosity 408 (n = 0.31).

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Fig. 7. Hydraulics paths followed at different elevations (e.g. A and B) in the samples during the drying path (0–1) and wetting path (1–2).

410 The lower bound solution for the collapse pressure q is obtained 411 by imposing that the Mohr circle at the base of the sample is a tangent 412 to the failure envelope in  $\sigma''-\tau$  space as illustrated in Fig. 8:

$$q_l = \left(k_p - 1\right)[s(H)S_r(H)] - \int_0^H \gamma(z)dz$$
(14)

413 where  $k_p$  is the passive earth coefficient.

### 415 3.4.4. Upper bound solution of collapse boundary pressure

The upper bound solution was derived by considering a single block mechanism with a planar failure surface formed at an angle  $\beta$ to the vertical as illustrated in Fig. 9. It was found that the minimum upper bound value of the collapse pressure is obtained for the angle generating a failure surface that cuts the cylinder in two halves as shown in Fig. 9.

The upper bound collapse load is obtained by equating the external work associated with the pressure q and the self-weight W with the internal work done by shear and normal stresses along the failure surface:

$$\left(W + q\frac{\pi d^2}{4}\right)\delta\cos(\beta + \varphi') = \delta\sin\varphi'\int_L sS_r dL$$
(15)

where  $\delta$  is the displacement of the block, d is the sample diameter, q is 426 the pressure applied at the boundary, and W is the self-weight of the 427 sliding bock. By rearranging this equation we obtain: 428

$$q_u = \frac{4}{\pi d^2} \left[ \frac{\sin\varphi'}{\cos(\beta + \varphi')} \int_L sS_r dL - W \right]$$
(16)

with the failure stress  $q_u$ , the self-weight *W* and the integral  $\int sS_r dL$  cal- 420 culated numerically by subdividing the problem vertically into 100 dis- 431 crete parts. Therefore when calculating the degree of saturation along a 432 scanning wetting path, 100 different scanning curves were used which 433 were described by the scaling parameter defined by Eq. (11). 434

3.5. Discussion 435

The lower and upper bound envelopes for the drying and wetting 436 paths are shown in Fig. 10 together with the experimental results. The 437 lower and upper bound solutions appear to bracket the experimental 438 data showing that the theorems of bound plasticity can adequately 439 capture the collapse behaviour even for partially saturated soils. Al- 440 though simplistic, this, to the authors' knowledge, represents the first 441 validation of limit analysis for partially saturated soils. 442

The lower and upper bound solutions were derived under two assumptions that might seem to be questionable at first glance: (i) an 444

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Fig. 8. State of stress to determine a lower bound collapse pressure using the lower bound theorem of plasticity.

associative flow, i.e. a dilatancy angle,  $\psi = 32^{\circ}$ ; and (ii) a friction 445 angle equal to the critical (ultimate) friction angle,  $\phi'_{crit}$ . The first as-446 sumption, although unrealistic, leads to an upper bound solution that 447 coincides with the solution obtained by the limit equilibrium method, 448 which is the simplest approach to understand and apply in geotech-449 nical design. On the other hand, the adoption of the critical friction 450angle allows for a conservative estimate of the collapse load that 451 452tends to compensate for the overestimation associated with the asso-453 ciative flow.



Fig. 9. Kinematic mechanism to determine an upper bound collapse pressure using the upper bound theorem of plasticity.



Fig. 10. Collapse boundary stresses predicted using the bound theorems of plasticity and comparison with experimental results.

This is demonstrated by a simple calculation of the upper bound 454 collapse load using a non-associated flow rule. Bolton (1986) has 455 demonstrated that sands tend to dilate even at relatively low relative 456 densities and relatively high mean stresses. A non-zero dilatancy 457 leads, in turn, to a peak friction angle that is greater than the critical 458 state angle. Bolton proposed a widely used relationship between the 459 peak friction angle,  $\phi'_{\perp peak}$ , the critical friction angle  $\phi'_{\perp crit}$ , and the 460 dilatancy,  $\psi$ :

$$\phi_{peak} - \phi_{crit} = 0.8\psi. \tag{17}$$

As an example, for the sand tested in this programme ( $\phi'_{crit} = 32^\circ$ ), 464  $\psi = 5^\circ$  generates peak friction angle  $\phi'_{peak} = 36^\circ$  and  $\psi = 10^\circ$  gener- 465 ates peak friction angle  $\phi'_{peak} = 40^\circ$ .

To estimate the upper bound load for soils with non-associated 467 flow rules, Drescher and Detournay (1993) suggested using rigid 468 block mechanisms with reduced discontinuity strength. This reduced 469 strength is a function of the friction and dilatancy angle,  $\phi_{\perp}^{\prime*}$  and fol-470 lows the formula derived by Davis (1968): 471

$$\tan\phi^{'*} = \frac{\cos\psi \cdot \sin\phi'}{1 - \sin\psi \cdot \sin\phi'} \tag{18}$$

where  $\phi'$  and  $\psi$  are the friction and dilation angles respectively. 472

To appreciate the role of dilatancy, the upper bound collapse load 474 was calculated using Eq. (18) for two values of dilatancy angles,  $\psi = 5^{\circ}$  475 and  $\psi = 10^{\circ}$ , and corresponding values of peak friction angle  $\phi'_{peak} = 476$  36° and  $\phi'_{peak} = 40^{\circ}$  respectively. The results from this analysis are 477 shown in Fig. 10 where it can be seen that the non-associative solution 478 for a small value of the dilatancy angle ( $\psi = 5^{\circ}$ ) is very similar to the 479 one obtained by assuming associative flow using the critical friction 480 angle ( $\phi'_{crit} = 32^{\circ}$  and  $\psi = 32^{\circ}$ ) and the solution obtained for higher 481 dilatancy angle ( $\phi'_{peak} = 40^{\circ}$  and  $\psi = 10^{\circ}$  in Figure 10) leads to a sig-482 nificant overestimation of the collapse load.

This demonstrates that the classical upper bound solution based 484 on associative flow and friction angle equal to the critical one, widely 485 used in geotechnical design even if disguised in the form of the limit 486 equilibrium method, is acceptable for engineering purposes. 487

### 4. Case study: Pozzolan Quarry

A demonstration of the application of this approach is to consider 489 the maximum unsupported vertical cut height in a cohesionless soil 490 in the field. De Vita et al. (2008) described vertical cuts up to 15 m 491

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492 high in a pyroclastic Pozzolan deposit in a quarry in the Campi Flegrei 493 area near Naples in Italy with a water table depth of a few tens of metres. The authors were successful in capturing the correct order 494 495of magnitude of the critical height but they used a rather simplistic approach that would be problematic to use in engineering practice. 496 They estimated the contribution of suction to shear strength using a 497 linear relationship (Fredlund et al., 1978), which is conceptually and 498 experimentally incorrect since the failure envelope with respect to 499500suction has been demonstrated to be markedly non-linear (Escario and Sáez, 1986). They also assumed a constant suction throughout 501 the excavation, which is inadmissible since the suction varies with 502depth in a profile that depends on the groundwater table level and 503the hydraulic boundary condition at the ground surface. 504

505 By using the approach proposed and validated in the previous 506 section, a more accurate estimate can be attained, which accounts for 507 the depth of the water table and incorporates a more realistic shear 508 strength criterion.

### 509 4.1. Mechanical and hydraulic characteristics of pozzolan deposit

The Pozzolan soil relevant to this case study was investigated by 510511 De Vita et al. (2008) by means of 7 samples labelled C1 to C7. The material is characterised by a field porosity *n* in the range 0.54–0.68 and 512a specific unit weight of the solids  $\gamma_s$  in the range of 23.6–25.2 kN/m<sup>3</sup> 513(average values of *n* of 0.63 and  $\gamma_s$  of 24.4 kN/m<sup>3</sup> are used in these 514calculations). The grain size distribution is characterised by a silt frac-515516tion in the range 0.32–0.50, a sand fraction in the range 0.45–0.52 and the absence of any clay fraction. 517

518 Water retention characteristics of the soil were investigated using 519 a conventional tensiometer by De Vita et al. (2008). Water retention 520 data is shown in Fig. 11a together with the van Genuchten function 521 (Eq. (8)) which was optimised to fit the experimental data.



**Fig. 11.** Water retention curve (a) and shear strength criterion (b) for the pozzolanic soil in Campi Flegrei near Naples.

De Vita et al. (2008) did not carry out suction-controlled or suction- 522 monitored tests on the pozzolan pyroclastic soils. However, shear 523 strength of a very similar pyroclastic soil was investigated by Papa 524 Q5 et al. (2008), whose water retention curve (Nicotera et al., 2010) is com- 525 pared with the one obtained by De Vita et al. (2008) in Fig. 11a. Papa et 526 Q6 al. (2008) observed that Eq. (4) models the experimental data in the 527 range of suction 0–20 kPa very well with a friction angle  $\phi' = 36.9^{\circ}$ . 528

When the shear strength criterion given by Eq. (4) is extrapolated at 529 high suctions, it is found that the contribution of suction to shear strength, 530  $\Delta \tau = s \cdot S_r \cdot \tan \phi'$ , indefinitely increases with suction (Figure 11b), 531 which is not intuitively acceptable. Eq. (4) is physically based on the 532 effects of bulk water on the soil skeleton and can be anticipated to 533 fail when pore-water is predominantly present in the form of menisci or adsorbed water as occurs at high suctions. As a first approximation, 535 the residual suction shown in Fig. 11a may be assumed to delimit the 536 range of menisci/bulk water and, hence, to limit the validity of Eq. (4). 537 This assumption seems to be corroborated by Cattoni et al. (2007), dem-538 Q7 onstrating that Eq. (4) holds in the range of suctions bounded by the 539

Accordingly, the contribution of suction to shear strength was 541 assumed to become constant as the residual suction is exceeded as 542 illustrated in Fig. 11b. 543

### 4.2. Stability of a vertical cut in pozzolan deposit

To derive an upper bound of the critical height *H*, the simplest 545 kinematic mechanism was considered, which consisted of a single block 546 with a planar slip surface inclined by the angle  $\alpha$  as shown in shown in 547 Fig. 12a. Considering that the unit weight  $\gamma$  of the soil is given by: 548

$$\boldsymbol{\gamma} = (1 - n)\boldsymbol{\gamma}_s + n \cdot \boldsymbol{S}_r \boldsymbol{\gamma}_w \tag{19}$$

where *n* is the porosity,  $\gamma_s$  and  $\gamma_w$  are the specific unit weights of the solid 540 particles and water respectively and  $S_r$  is the degree of saturation. The 551 weight *W* of the block can be calculated as follows: 552

$$W = \gamma_s(1-n)\tan\alpha \frac{H^2}{2} + n\gamma_w \tan\alpha \int_H S_r(z)(H-z)dz$$
(20)

hence, the work done by the external forces  $W_e$  is equal to:

$$W_e = \left[\gamma_s(1-n)\tan\alpha\frac{H^2}{2} + n\gamma_w\tan\alpha\int_H S_r(z)(H-z)dz\right]\delta\cos(\alpha+\phi').$$
(21)

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**Fig. 12.** (a) State of stress adopted to derive a lower bound solution and (b) kinematic mechanism to derive an upper bound solution for the critical height of a cut slope.

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An upper bound solution for the critical height can then be obtained by equating  $W_e$  with  $W_i$ . It can then be demonstrated (see for example Stanier and Tarantino, 2010) that the minimum 'upper bound' value is obtained for:

$$\alpha = \frac{\pi}{4} - \frac{\phi'}{2}.$$
(23)

564

To derive a lower bound value for the critical height, we assume the vertical and horizontal directions to be principal directions of stress. Accordingly, the equilibrium stress state is given by:

$$\begin{cases} \sigma_z = \gamma z \\ \sigma_x = 0 \end{cases}$$
(24)

569 where  $\sigma_z$  and  $\sigma_x$  are the vertical and horizontal stresses. Based on the 571 shear strength criterion given by Eq. (4) a lower bound can be obtained 572 by imposing that the Mohr stress circle in the " $\sigma + sS_r$ ,  $\tau$ " plane relative 573 to a point at the base of the excavation (Figure 12b) is a tangent to the 574 failure envelope:

$$s(H) \cdot S_r(H) = k_a \{ [(1-n)\gamma_s + n \cdot S_r(H) \cdot \gamma_w] H + s(H)S_r(H) \}$$
(25)

where  $k_a$  is the active earth coefficient, s is the suction that is a function of H, and  $S_r$  is the degree of saturation that is in turn a function of suction s.

The lower and upper bound solutions obtained by assuming a 579hydrostatic suction profile are plotted in Fig. 13 as a function of the 580depth  $H_w$  of the water table. As expected, the critical height increases 581 with the depth of the groundwater table, although the effect becomes 582 less and less important at large values of the groundwater table 583depth. Fig. 13 shows that the calculated critical height is significant 584in this cohesionless material and this is in general agreement with 585586 field observations (see De Vita et al., 2008).



**Fig. 13.** Upper and lower bound solutions of critical height in pozzolan pyroclastic soil as a function of groundwater table depth assuming an hydrostatic suction profile and suction profiles generated by ponded infiltration.

#### 4.3. Effect of rainfall on suction profile

Stability of vertical cuts in cohesionless soils has been demonstrated 588 to rely on matric suction. However, its effect could partially or totally 589 vanish when rainwater infiltrates at the ground surface. For engineering 590 purposes, it becomes crucial to assess the potential impact of rainfall 591 on matric suction and, hence, on vertical cut stability. A very simple 592 method that allows preliminary assessment of this risk of vertical cut 593 collapse is proposed here that is based upon solutions available in classical geotechnical textbooks focusing on saturated soils. The principal 595 advantage of the method is that it can be used by practitioners lacking 596 the water table. 598

As a simplification the water flow equation may be linearised by 599 assuming that hydraulic conductivity is constant and the water retention curve is linear. For conservatism the hydraulic conductivity is 601 assumed to be equal to the saturated value ensuring a maximal infiltration rate and, hence, the highest reduction in suction and shear 603 strength. Under these circumstances the water flow equation becomes (Tarantino et al., 2010): 605

$$\left(\frac{k_{sat}}{\gamma_w\frac{\Delta\theta}{\Delta u_w}}\right)\frac{\partial^2 u_w}{\partial x^2} = \frac{\partial u_w}{\partial t}$$
(26)

where  $u_w$  is the pore-water pressure, t is the time, z is the vertical 60% coordinate,  $k_{sat}$  is the saturated hydraulic conductivity,  $\gamma_w$  is the unit 608 weight of water, and  $\Delta\theta/\Delta u_w$  is the slope of the linearised water reten-609 tion curve. The water retention curve is highly non-linear and we sug-610 gest two possible linearisations in Fig. 14. It will be demonstrated later 611 that these linearisations are essentially equivalent for the purpose of 612 estimating suction profiles following rainfall.

Let us assume that the initial condition for pore-water pressure is hydrostatic and controlled by the groundwater table located at the depth  $H_w$  from the ground surface. This is a conservative assumption as evapotranspiration at the ground surface would generate suctions higher than those associated with hydrostatic conditions. To simulate infiltrating rainwater, the hydraulic boundary condition at the ground surface should be represented by an inward flux. For conservatism it is assumed that a pond immediately forms at the ground surface and that the hydraulic boundary condition is represented by zero pore-water pressure at the ground surface (i.e. ponded infiltration). This is the most conservative assumption as it returns the maximum possible infiltration and, hence, the highest reduction in suction. Therefore, the groundwater table and the ponded surface infiltration represent the hydraulic boundary conditions at the bottom and top of the flow domain.



Fig. 14. Linearisation of the water retention curve for the pozzolan pyroclastic soil.

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628 With these initial and boundary conditions, the problem reduces 629 to the classical Terzaghi consolidation problem with triangular excess pore-water pressure and double-drainage. The solution of this problem 630 631 is widely found in classical geotechnical textbooks, often in graphical form (e.g. Lambe and Whitman, 1969), and can therefore be exploited 632 by engineers with no specific background in unsaturated soil mechanics. 633 The solution is given by: 634

$$u(z,t) = \sum_{n=1}^{\infty} \frac{2u_0}{n\pi} \left\{ 1 - \left(\frac{2H}{n\pi}\right) \sin(n\pi) \right\} \sin\frac{n\pi z}{2H} \exp\left(-\frac{n^2 \pi^2 T}{4}\right)$$
(27)

where  $u_0$  is the initial excess pore-water pressure at the ground surface 636 and *T* is the time factor given by: 637

$$T = \left(\frac{k_{\text{sat}}}{\gamma_w \frac{\Delta \theta}{\Delta u_w}}\right) \frac{1}{H^2} \cdot t \tag{28}$$

where *H* is the drainage length. By assuming  $k_{sat} = 7 \cdot 10^{-7}$  m/s 639 640 (Nicotera et al., 2010),  $\Delta\theta/\Delta u_w$  is equal to 0.005 or 0.009 (see Figure 14), and a rainfall duration of 2 days, we can derive the pore-water pressure 641 642 profiles as shown in Fig. 15 for different water table depths  $H_{w}$ . It appears 643 that rainfall only affects a shallow portion of the ground and its effects become less and less important as the depth of the groundwater table 644 increases. If the lower and upper bound solutions are calculated by con-645 sidering the pore-water pressure profiles after two days (ponded) infil-646 tration, the values shown in Fig. 13 are obtained. 647

648 It appears that there is not a significant difference between the values derived under the assumption of hydrostatic pore-water pressure 649 profile and either of the ponded surface infiltration solutions. Hence, the 650 choice regarding the slope of the 'linearised' water retention curve is not 651 652 overly critical. In conclusion therefore, rainfall does not seem to jeopar-653 dise slope stability, which compliments field observations (De Vita et al., 2008). It should be stressed again that the analysis of the effect of rain-654water is definitively conservative since saturated hydraulic conductivity 655 and ponded infiltration was considered. 656

#### 5. Conclusions 657

An extension to the classical limit analysis has been proposed to 658 allow assessment of the stability of excavations above the water table 659 660 in cohesionless (granular) soils, which accounts for the beneficial effect



Fig. 15. Suction profiles after two days of ponded infiltration for water table depths of 10, 20, and 30 m.

of suction and partial saturation on shear strength. A modified shear 661 strength criterion has been incorporated into the traditional bound 662 theorems of plasticity approach using a relationship relating shear 663 strength to the product of suction, s, and saturation ratio, S<sub>r</sub>. This has 664 facilitated analysis of the stability of vertical cuts in cohesionless soils 665 above the water table. 666

To assess the validity of this extension, simple small-scale column 667 collapse tests were performed using fine silica sand for which the 668 water retention characteristics were derived using a negative-water 669 column approach. The column collapse tests allowed assessment of the 670 failure boundary pressure of the column for a given boundary suction 671 applied to the base of the sample. Upper and lower bound solutions 672 were derived for this boundary value problem, generating failure 673 bounds that bracketed the experimental results reasonably well. To 674 the authors' knowledge, this represents the first experimentally vali- 675 dated appraisal of the application of the bound theorems of plasticity 676 to problems involving cohesionless soil above the water table. 677

The impact on practice of the findings of the laboratory validation 678 tests was then explored using a case study, focussing on the vertical 679 cut height observed in pyroclastic Pozzolan deposits near Naples, 680 Italy. This problem has previously been addressed by De Vita et al. 681 (2008) by introducing, however, several oversimplifications (constant 682 matric suction within the excavation and linear 'unsaturated' failure 683 envelope) that were removed in this paper. The upper and lower bounds 684 for the safe vertical cut height were calculated accounting for varying 685 suction, s, and saturation ratio,  $S_r$ , within the deposit and a non-linear 686 failure envelope. These were solved using numerical integration and 687 the calculated failure heights indicated good agreement with field 688 observations of stable vertical cuts in pyroclastic Pozzolan deposits. 689

The impact of rainfall on infiltration and vertical cut stability was 690 then explored. Simplifying the scenario of rainfall to a case with ponded 691 infiltration and maximum (saturated) hydraulic conductivity, a conser- 692 vative appraisal of vertical cut stability was generated using the classical 693 Terzaghi consolidation solution for double drainage and a triangular 694 excess pore pressure distribution. The impact of 2 days of constant 695 rainfall causing ponded infiltration has been demonstrated to minimally 696 impact upon the vertical cut stability in Pozzolan soil. This would ex- 697 plain the long-term stability of the large vertical cuts (tens of metres) 698 observed in Pozzolan deposits in the field (De Vita et al., 2008). 699

The findings of this paper present and validate an approach to 700 assessing the stability of vertical cuts in cohesionless soils that are 701 based principally upon methods taught in most undergraduate Civil 702 Engineering courses and that require little specialist knowledge. Hence, 703 it is envisaged that these techniques may be used in the future by prac-704 tising engineers, to rationalise the often unexplained non-zero vertical 705 cut height observed in cohesionless soils above the water table, for 706 which classical soil mechanics theory offers no rational explanation. 707

### References

Atkinson, J.H., 1981. Foundations and Slopes: An Introduction to Applications of Critical	709
State Soil Mechanics. McGraw-Hill, London.	710
Bolton, M.D., 1986. The strength and dilatancy of sands. Geotechnique 36 (1), p65-p78.	711
Budevsky, O., 1979. Foundations of chemical analysis. British Library Cataloguing in	712
Publication Data. Ellis Horwood Ltd. Publishers0-85312-113-3.	713
Chen, W.F., 2007. Limit Analysis and Soil Plasticity. J. Ross Publishing 638.	714
Davis, E.H., 1968. Theories of plasticity and failure of soil masses. In: Lee, I.K. (Ed.), Soil	715
<ul> <li>Mechanics Selected Topics. Elsevier, New York (USA), pp. 341–354.</li> </ul>	716
De Vita, P., Angrisani, A.C., Di Clemente, E., 2008. Engineering geological properties of	717
the phlegraean pozzolan soil (Campania region, Italy) and effect of the suction on	718
the stability of cut slopes. Italian Journal of Engineering Geology and Environment	719
2, 5–22.	720
Delta-T Devices Ltd., 1999. ThetaProbe user manual. Available at http://www.delta-t.	721
co.uk.	722
Drescher, A., Detournay, E., 1993. Limit load in translational mechanisms for associative	723
and non-associative materials. Geotechnique 43 (3), 443–456.	724
Escario, V., Sáez, J., 1986. The shear strength of partly saturated soils. Geotechnique 36	725
(3) 453–456	726

Fleuerau, J.M., Kheirbek-Saoud, S., Soemitro, R., Taibi, S., 1993. Behavior of clayey soils 727 on drying-wetting paths. Canadian Geotechnical Journal 30, 287-296. 728

708

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S.A. Stanier, A. Tarantino / Engineering Geology xxx (2013) xxx-xxx

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Change

- Fredlund, D.G., Morgestern, N.R., Widger, R.A., 1978. The shear strength of unsaturated soils. Canadian Geotechnical Journal 13 (3), 313–321.
   Gaskin, G.J., Miller, J.D., 1996. Measurement of soil water content using a simplified impedance measuring technique Journal of Agricultural Engineering 63, 153–160.
  - impedance measuring technique. Journal of Agricultural Engineering 63, 153–160. Lambe, T.W., Whitman, R.V., 1969. Soil Mechanics. John Wiley & Sons.
  - Langendoen, E.J., Simon, A., Klimetz, L., Bankhead, N., Ursic, M.E., 2012. Quantifying sediment loadings from streambank erosion in selected agricultural watersheds draining to Lake Champlain. US Department of Agriculture Agricultural Research Service, Technical Report No. 72.

Nardi, L., Rinaldi, M., Solari, L., 2012. An experimental investigation on mass failures occurring in a riverbank composed of sandy gravel. Geomorphology 163–164, 56–69.

- Nicotera, M.V., Papa, R., Urciuoli, G., 2010. An experimental technique for determining the hydraulic properties of unsaturated pyroclastic soils. Geotechnical Testing Journal 33 (4). http://dx.doi.org/10.1520/GTJ102769.
- Öberg, A.L., Sällfors, G., 1997. Determination of shear strength parameters of unsaturated silts and sands based on the water retention curve. Geotechnical Testing Journal 20 (1), 40–48 (March 1997).
- Rinaldi, M., Casagli, N., 1999. Stability of streambanks formed in partially saturated soils and effects of negative pore water pressures: the Sieve River (Italy). Geomorphology 26, 253–277.
- Rinaldi, M., Casagli, N., Dapporto, S., Gargini, A., 2004. Monitoring and modelling of pore water pressure changes and riverbank stability during flow events. Earth Surface Processes and Landforms 29, 237–254.
- Romero, E., Vaunat, J., 2000. Retention curves in deformable clays. In: Tarantino, A., Mancuso, C. (Eds.), Experimental Evidence and Theoretical Approaches in Unsaturated Soils. A.A. Balkema, Rotterdam, pp. 91–106.

Simon, A., Curini, A., Darby, S.E., Langendoen, E.J., 2000. Bank and near-bank processes in an incised channel. Geomorphology 35, 193–217.

- Stanier, S., Tarantino, A., 2010. Active earth force in 'cohesionless' unsaturated soils 757 Q8 using bound theorems of plasticity. In: Alonso, E.E., Gens, A. (Eds.), Proc. 5th Int. 758 Conf. on Unsaturated soils: vol. 2, vol. 2, pp. 1081–1086 (Barcelona, Spain, 6-8 759 September 2010). 760
   Tarantino, A., 2007. A possible critical state framework for unsaturated compacted roll soils. Geotechnique 57 (4), 385–389. 762
- Tarantino, A., El Mountassir, G., in press. Making unsaturated soil mechanics accessible for engineers: preliminary hydraulic-mechanical characterisation & stability assessment.
   764 Engineering Geology.
   765
- Tarantino, A., Tombolato, S., 2005. Coupling of hydraulic and mechanical behaviour in unsaturated compacted clay. Geotechnique 55 (4), 307–317. 767
- Tarantino, A., Sacchet, A., Dal Maschio, R., Francescon, F., 2010. A hydro-mechanical 768 approach to model shrinkage of air-dried green bodies. Journal of the American 769 Ceramic Society 93 (3), 662–670. 770
- Tsidzi, K.E.N., 1997. An engineering geological approach to road cutting slope design in 771 Ghana. Geotechnical and Geological Engineering 15 (1), 31–45. 772
- van Genuchten, M.T., 1980. A closed form equation for predicting the hydraulic con-773 ductivity of unsaturated soils. Soil Science Society of America Journal 44, 892–898. 774
- Vanapalli, S.K., Oh, W.T., 2012. Stability analysis of unsupported vertical trenches in 775 unsaturated soils. GeoCongress 2012 State of the Art and Practice in Geotechnical 776 Engineering Geotechnical Special Publication No. 225 Oakland, California, USA 777 25-29 March 2012 Stability, 4, pp. 2502–2511.
- Whenham, V., De Vos, M., Legrand, C., Charlier, R., Maertens, J., Verbrugge, J.C., 2007. Influence
   of soil suction on trench stability. In: Schanz, T. (Ed.), Experimental unsaturated soil mechanics. Proceedings in Physics, vol. 112, Part VII. Springer, pp. 495–501.
- Zandarín, María T., Oldecop, L.A., Rodríguez, R., Zabala, F., 2009. The role of capillary 782 water in the stability of tailing dams. Engineering Geology 105, 108–118. 783
  - 784

Papa R., Urciuoli G., Evangelista A. and Nicotera M.V. (2008). Mechanical properties of unsaturated pyroclastic soils affected by fast landslide phenomena. In Unsaturated Soils, Advances in Geo-Engineering, Proceedings of the 1st European Conference, E-UNSAT 2008, Durham, United Kingdom, D.G. Toll, C.E. Augarde, D. Gallipoli, and S.J. Wheeler (eds), Taylor & Francis, pages 917–923.

Cattoni, E., Cecconi, M. and Pane, V. (2007). "Geotechnical properties of an unsaturated pyroclastic soil from Roma". Bull Eng Geol Environ, vol. 66: 403–414.

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