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# Unique Characteristics of Vertical Carbon Nanotube Field-effect Transistors on Silicon

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Abstract: A vertical carbon nanotube field-effect transistor (CNTFET) based on silicon (Si) substrate has been proposed and simulated using a semi-classical theory. A single-walled carbon nanotube (SWNT) and an n-type Si nanowire in series construct the channel of the transistor. The CNTFET presents ambipolar characteristics at positive drain voltage  $(V_d)$  and n-type characteristics at negative  $V_d$ . The current is significantly influenced by the doping level of n-Si and the SWNT band gap. The n-branch current of the ambipolar characteristics increases with increasing doping level of the n-Si while the p-branch current decreases. The SWNT band gap has the same influence on the p-branch current at a positive  $V_d$  and n-type characteristics at negative  $V_d$ . The lower the SWNT band gap, the higher the current. However, it has no impact on the n-branch current in the ambipolar characteristics. Thick oxide is found to significantly degrade the current and the subthreshold slope of the CNTFETs.

Keywords: Carbon Nanotube; Field-effect Transistors; Semi-classical Simulation

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## Introduction

The rapid development of information technology requires a smaller MOSFET (Metal-Oxide-Semiconductor Field-Effect Transistor), the main building block in microelectronics. The shrinkage of the MOSFET must follow the Dennard's scaling theory [1], i. e., the vertical dimensions must be scaled down with the lateral dimensions to avoid the so-called short channel effect. This means the channel thickness must be scaled down together with the channel length. However, this shrinkage will stop when it meets the physics limit. It has been reported that the bulk silicon MOS-FET will not perform reliably at sub-10 nm gate length [2]. New material or new transistor structure must be developed at the end of scaling road map. Single-walled carbon nanotubes (SWNTs) have been considered to be one of the most promising materials for silicon due to their excellent electrical properties and ultrathin body [3, 4]. The sub-2 nm diameter of the SWCNT makes it easier to satisfy the body thickness requirement for a 5 nm node FET while it is impossible for Si technology [2, 5]. Recently-developed CNTFETs with single SWCNT and sub-10 nm channel length have shown much better performance than the best competing silicon devices [6] in switching behavior and the normalized current density at a low operating voltage of 0.5V. More importantly, the output characteristics have shown clear device saturation behavior at a drain voltage less than 0.4 V, much lower than the 0.64 V predicted by the ITRS Roadmap for 5 nm node transistors [7], showing the power benefit of CNTFETs compared to silicon transistors.

Despite the promising progress in the performance of the CNTFETs, the fabrication of short channel CNT-

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FETs still rely on some high cost and low throughput techniques, for example, electron beam lithography. To solve this problem, we have developed vertical carbon nanotube field-effect transistors (CNTFETs) recently [8, 9]. The unique feature of this kind of CNT-FETs is that the source and drain of the transistors are vertically stacked with a dielectric sandwiched in between. This configuration makes it easier to fabricate short channel CNTFETs because the channel length is precisely the thickness of the dielectric layer between the source and drain. Short channel length in the range from several nanometers to sub-micrometers can be fabricated without using those complicated techniques. Another advantage of this structure is that it can improve the integration density since the vertical transistors occupy less space than their planar counterpart [10]. Furthermore, it offers an approach to integrate carbon nanotubes to silicon if the vertical CNTFETs are fabricated on silicon. This fabrication does not need to change the silicon technology. By using  $SiN_x$  to isolate the Si source and metal drain contact, we have successfully fabricated vertical CNT-FETs on Si [9], as schematically shown in Fig. 1(a). The channel length and channel width are 600 nm and 2 μm, respectively. The mobility of our CNTFETs is better than other group's results which are extracted from planar CNTFETs fabricated using similar CNT solution [11, 12]. Interestingly, the vertical CNTFETs have shown some characteristics significantly different from those CNTFETs fabricated with metal source and drain. The transfer characteristics of the vertical CNT-FETs on Si can be either ambipolar or unipolar (n-type or p-type) depending on the sign of the drain voltages [9]. The n-type/p-type characteristics are defined by the Si doping type. We have simulated these phenomena using a semi-classical model in our former paper [9]. The calculation results are well consistent with the experimental observations. However, the variations of Si doping level and carbon nanotube band gap have not been taken into consideration. In this paper, we will present the influence of different alignment of Si Fermi level and different carbon nanotube band gap, and the impact of the oxide thickness on the performance of the CNTFETs in detail. It is very useful for designing a perfect vertical CNTFET on Si.

### 1 Methods

The performances of the vertical CNTFETs on Si are simulated using a semi-classical method [13-17]. The configuration of the CNTFET is schematically illustrated in Fig. 1(b). Source and drain are vertically stacked, isolated by  $SiN_x$ . Since the gate overlapped with part of the silicon contact in experiment, as shown in Fig. 1(a), the conductance of this part is also modified by the gate voltage. We therefore propose that the channel is composed of a SWNT and a Si nanowire in the calculation. Two metal contacts are used as source and drain of the CNTFET. A grounded right gate electrode (not shown here) is used for the calculations. It is 190 nm away from the  $HfO_2$  gate dielectric layer.



Fig. 1 a) 3D structure of the vertical CNTFET on silicon. b) Schematic configuration of the CNTFET for calculation. The vertical channel is composed of a SWNT and a Si nanowire.

As we know, CNTFETs work as Schottky barrier (SB) transistors [18]. The current is controlled by thermal assisted tunneling through the SBs at the contact. It has been reported that the contact resistance is larger than the channel resistance for ultra-scaled CNTFETs [5]. This means that the contact plays a more important role than scattering in the channel for the CNT-FETs with a short channel. Therefore, we suppose the carrier transport in SWNT and the Si channel is ballistic for the simplicity of calculation. This assumption may cause that the calculation result is somewhat higher than that of the actual transistors. The current is given by the Landauer-Büttiker formula.

$$I = \frac{4e}{h} \int [F(E) - F(E + eV_d)]T(E)dE, \qquad (1)$$

where  $V_d$  is the drain voltage, F(E) is the Fermi function and T(E) is the energy-dependent transmission through the SB between the SWNT/Si and electrodes. T(E) can be estimated using the Wentzel-KramersBrillouin (WKB) approximation

$$T(E) = \exp\left[-2\int_{z_1}^{z_2} k(z)dz\right],\tag{2}$$

with the wave number

$$k(z) = \frac{2}{3aV_0} \left\{ \left(\frac{E_g}{2}\right)^2 - [E + eV(z)]^2 \right\}^{1/2}, \quad (3)$$

where a = 0.144 nm,  $E_g = 0.4 \sim 0.8$  eV, and  $V_0 = 2.5$  eV are the C-C bond length, the SWNT band gap and the tight-binding parameter, respectively. V(z) is the electrostatic potential along the channel and is obtained by numerically solving the Laplace equation. The integration is performed between the two classical turning points,  $z_1$  and  $z_2$  [13]. The temperature considered here is 300 K. The Fermi level,  $E_F$ , of the source and drain contacts is assumed at the middle of the SWNT band gap. It locates  $0.1 \sim 0.3$  eV below the conduction band of n-Si for a Si band gap of 1.1 eV.

## 2 Results and Discussion

We first consider the influence of Si Fermi level (or doping level) on the transfer characteristics of the CNT-FETs. For the Si Fermi level locating 0.2 eV below the conduction band ( $\Delta E_{cf} = E_c - E_f = 0.2 \text{ eV}$ ), the calculated results are shown in Fig. 2. It presents ambipolar characteristics for  $V_d \geq 0.5$  V and n-type characteristics for  $V_d \leq 0.25$  V. These characteristics are the same as that for the CNTFETs with Si Fermi level locating 0.3 eV below the conduction band ( $\Delta E_{cf} = 0.3 \text{ eV}$ ) [9]. The reasons for these characteristics have been discussed in detail in reference 9.



Fig. 2 Calculated transfer characteristics of the CNTFET with the Fermi level of Si locating 0.2 eV below the conduction band. The band gap of the SWNT is 0.6 eV.

Here, we focus on the differences between them. We find that both the n-branch current (at  $V_q > 0$  V) and

p-branch current (at  $V_g < 0$  V) change with  $\Delta E_{cf}$ . The minimum current points corresponding to different positive  $V_d$  also shift apparently. These can be seen much clearly in Fig. 3 which shows the transfer characteristics of the CNTFETs for three different  $\Delta E_{cf}$ at  $V_d = 0.75$  V. The blue, red and black curves represent  $\Delta E_{cf} = 0.1$  eV, 0.2 eV and 0.3 eV, respectively. First, the n-branch current increases with decreasing  $\Delta E_{cf}$ . The minimum current for  $\Delta E_{cf} = 0.2$  eV is significantly higher than those for the other two cases. These phenomena can be understood using a band diagram, as shown in Fig. 4.



Fig. 3 Calculated transfer characteristics of the CNTFETs with different Si doping level at  $V_d = 0.75$  V. The black, red and blue curves are for  $E_c - E_f = 0.3$ , 0.2 and 0.1 eV, respectively. The band gap of the SWNT is 0.6 eV.



Fig. 4 Band diagrams of the CNTFETs with different Si doping level at the source side.

At a positive  $V_d$ , the band of the SWNT at the drain side bends downwards. The center channel band shifts upwards under a negative  $V_g$ , leading to a thin SB between SWNT and the drain. If it is thin enough, holes can be injected from the drain to channel, and be collected by the source, contributing to the p-branch current of the ambipolar characteristics. Since the Si band gap (1.1 eV) is fixed, the valence band for  $\Delta E_{cf} = 0.2$  eV is much lower than that for  $\Delta E_{cf} = 0.3$  eV, as shown in Fig. 4. This builds a larger barrier for holes. At the same positive  $V_d$ , the lower valence band blocks more holes injected from the drain. As a result, the hole current decreases with decreasing  $\Delta E_{cf}$ , as shown in Fig. 3.

The n-branch current in the ambipolar characteristics is contributed by source electrons at a positive  $V_d$ . The center channel band shifts downwards when a positive gate voltage is applied. As the increases of the gate voltage, the SB between the source and the Si becomes transparent, allowing electron injection from the source to channel. These electrons are collected by the drain, forming n-branch current. The current depends on the shape of the SB which is defined by the alignment of the Si Fermi level and the gate voltage. At the same gate voltage, the alignment of the Fermi level plays a key role in controlling the current. A smaller  $\Delta E_{cf}$ means the Fermi level is much closer to the conduction band, and both the electron density and the transmission probability through the SB are higher. Therefore, the electron current increases with decreasing  $\Delta E_{cf}$ , as shown in Fig. 3.

The minimum current happens at the point where the n-branch current and the p-branch current meet together. Therefore, the position of this point depends on the relative height of the two branch currents. Since the p-branch current increases with increasing  $\Delta E_{cf}$  and the n-branch current decreases with increasing  $\Delta E_{cf}$ , the p-branch current for  $\Delta E_{cf} = 0.1$  eV is much lower than its n-branch counterpart, and hence the minimum current point is close to the p-branch part. The situation for  $\Delta E_{cf} = 0.3$  eV is in contrast to that for  $\Delta E_{cf} = 0.1 \text{ eV}$ , the minimum current point is thus on the opposite direction of the former one. The n-branch current and p-branch current for  $\Delta E_{cf} = 0.2$  eV are almost symmetric with  $V_g$ , leading to a minimum current point closing to  $V_q = 0$  V, and the minimum current is apparently higher than those for the other two cases.

The band gap of carbon nanotubes has important influence on the characteristics of the planar CNTFETs [19]. It is useful to know the performance of our vertical CNTFETs with different band gap. Given  $\Delta E_{cf} = 0.3$ eV for Si, the transfer characteristics of the CNTFETs with different band gap are shown in Fig. 5. For the ambipolar characteristics at positive drain voltage, for example,  $V_d = 1$  V, the n-branch current keeps unchanged for three different SWNT band energies, as shown in Fig. 5(a). This is because the n-branch current are contributed by the electron injection from the source, and the current depends on the SB between the source and Si. This SB does not change with the variation of the SWNT band gap. Therefore, the n-branch current are the same for the three different SWNT band gaps.



Fig. 5 Calculated transfer characteristics of the CNT-FETs with different SWNT band gaps for  $V_d = 1$  V (a) and  $V_d = -0.75$  V (b). The blue, red, and black curves are for  $E_g = 0.4$ , 0.6 and 0.8 eV, respectively.

In contrast, the p-branch current in Fig. 5(a) increases with decreasing SWNT band gap. The reason is that the p-branch current is contributed by hole injection from the drain when the SWNT band bends downwards at the drain for positive  $V_d$ . The current is controlled by the SB between the SWNT and the drain. It becomes transparent for holes when a small enough  $V_g$  is applied. As the decrease of  $E_g$ , the distance between the sharp SB and the Fermi level of the SWNT decreases and both of the transmission probability and the hole density increase, leading to an increased hole current.

At a negative  $V_d$ , the SWNT band bends upwards at the drain. The electrons can be injected from the drain to the channel and form n-type current of the CNT-FETs. The current depends on the shape of the SB between SWNT and the drain which define the transmission probability of the electron. This current also increases with decreasing  $E_g$  of the SWNT, as shown in Fig. 5(b). The reason is the same as that for the influence of small  $\Delta E_{cf}$  on the n-branch current at a positive  $V_d$ , but the SB between SWNT and the drain instead of that between the source and Si is considered here. As the decrease of the band gap, the Fermi level of the SWNT becomes much closer to the sharp point of the SB, resulting in a higher electron current.

We now turn to the impact of the oxide thickness on the performance of the transistors. One of the most important influences of oxide thickness is on the inverse sub-threshold slope of the CNTFETs. It is a measure of the switching speed of a transistor. The inverse subthreshold slope is calculated using

$$S = dV_q/d(\log I_d). \tag{4}$$

It increases almost linearly from 130 to 290 mV/dec if the oxide thickness is increased from 5 nm to 25 nm, as shown in Fig. 6.



Fig. 6 Inverse sub-threshold slope as a function of the oxide thickness. The Fermi level of Si locates 0.3 eV below the conduction band. The band gap of Si and SWNT are 1.1 eV and 0.6 eV, respectively.



Fig. 7 Drain current as a function of square root of the oxide thickness for the CNTFETs at  $V_d = 1$  V and  $V_g = -1$  V.

In addition to the inverse sub-threshold slope becoming worse, the drain current also degrades significantly with increasing of the oxide thickness. Since the CNT-FETs are Schottky barrier transistors, the electric field distribution in the vicinity of the contact plays a critical role in the transistor performance. This electric field distribution is significantly affected by the oxide thickness if  $V_g$  and  $V_d$  are fixed. Figure 7 shows the  $I_d$ as a function of square root of the oxide thickness at  $V_d = 1$  V and  $V_g = -1$  V. It can be seen clearly that  $I_d$  decreases linearly with increasing square root of the oxide thickness. The current degrades more than one order of magnitude when  $t_{ox}$  increases from 5 nm to 25 nm.

### 3 Conclusion

The performance of a vertical CNTFETs on n-Si was investigated using a semi-classical model. The interesting characteristics of the transistors are that can be ambipolar or unipolar depending on the sign of drain voltage. The CNTFETs show ambipolar characteristics at positive drain voltage and n-type characteristics after reversing the sign of drain voltage. The ambipolar characteristics are affected by both the Si doping level and the carbon nanotube band gap while the ntype characteristics is mainly controlled by the carbon nanotube band gap. The n-branch current for the ambipolar characteristics can be increased by increasing the Si doping level while the p-branch current can be improved by decreasing the Si doping level or decreasing the carbon nanotube band gap. In addition, the current decreases linearly with increasing square root of gate oxide thickness. It can differ by one order of magnitude if the gate oxide thickness is increased from 5 nm to 25 nm. The turn-on performance quantified by sub-threshold slope simultaneously becomes much worse. This study showed the significant basic future for designing the vertical CNTFETs on Si.

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### References

- R. H. Dennard, F. H. Gaensslen, H.-N. Yu, V. L. Rideout, E. Bassous and A. R. LeBlance, "Design of ion-implanted MOSFET's with very small physical dimensions", IEEE J. Solid-State Circuits 9(5), 256-268 (1974). http://dx.doi.org/10.1109/JSSC.1974. 1050511
- [2] M. Ieong, B. Doris, J. kedzierski, K. Rim and M. Yang, "Silicon device scaling to the sub-10-nm regime", Sci-

ence 306(5704), 2057-2060 (2004). http://dx.doi. org/10.1126/science.1100731

- [3] Ph. Avouris, "Carbon nanotube electronics and photonics", Phys. Today 62(1), 34-40 (2009). http://dx. doi.org/10.1063/1.3074261
- [4] Min Zhang, "Improving the Electrical Contact Property of Single-Walled Carbon Nanotube Ar-rays by Electrodeposition", Nano-Micro Lett. 5(4), 242-246 (2013). http://dx.doi.org/10.5101/nml.v5i4. p242-246
- Q. Cao and S.-J. Han, "Single-walled carbon nanotubes for high-performance electronics", Nanoscale 5(19), 8852-8863 (2013). http://dx.doi.org/10. 1039/c3nr02966b
- [6] A. D. Franklin, M. Luisier, S.-J. Han, G. Tulevski, C. M. Breslin, L. Gignac, M. S. Lundstrom and W. Haensch, "Sub-10 nm carbon nanotube transistor", Nano Lett. 12(2), 758-762 (2012). http://dx.doi.org/10. 1021/nl203701g
- [7] F. Kreupl, "Carbon nanotubes finally deliver", Nature 484, 321-322 (2012). http://dx.doi.org/10.1038/484321a
- [8] J. Li, C. Zhao, Q. Wang, Q. Zhang, Z. Wang, X. Zhang, A. I. Abutaha and H. N. Alshareef, "Vertically aligned carbon nanotube field-effect transistors", Carbon 50(12), 4628-4632 (2012). http://dx.doi.org/10.1016/j.carbon.2012.05.049
- [9] J. Li, Q. Wang, W. Yue, Z. Guo, L. Li, C. Zhao, X. Wang, A. I. Abutaha, H. N. Alshareef, Y. Zhang and X. Zhang, "Integrating carbon nanotubes to Si by means of vertical carbon nanotube field-effect transistors", Nanoscale, accept. http://dx.doi.org/10. 1039/C4NR00978A
- J. Mores, "Turning the world vertical: MOSFETs with current flow perpendicular to the wafer surface", Appl. Phys. A 87(3), 531-537 (2007). http://dx.doi.org/ 10.1007/s00339-007-3986-9
- [11] N. Rouhi, D. Jain, K. Zand and P. J. Burke, "Fundamental limits on the mobility of nanotube-based semiconducting inks", Adv. Mater. 23(1), 94-99 (2011). http://dx.doi.org/10.1002/adma.201003281

- [12] M. Engel, J. P. Small, M. Steiner, M. Freitag, A. A. Green, M. C. Hersam and Ph. Avouris. "Thin film nanotube transistors based on self-assembled, aligned, semiconducting carbon nanotube arrays", ACS Nano 2(12), 2445-2452 (2008). http://dx.doi. org/10.1021/nn800708w
- S. Heinze, M. Radosavljević, J. Tersoff and Ph. Avouris, "Unexpected scaling of the performance of carbon nanotube Schottky-barrier transistors", Phys. Rev. B 68, 235418 (2003). http://dx.doi.org/10. 1103/PhysRevB.68.235418
- [14] S. Heinze, J. Tersoff and Ph. Avouris, "Electrostatic engineering of nanotube transistors for improved performance", Appl. Phys. Lett. 83(24), 5038-5040 (2003). http://dx.doi.org/10.1063/1.1632531
- [15] J. Li, Q. Zhang and M. B. Chan-Park, "Simulation of carbon nanotube based p-n junction diodes", Carbon 44(14), 3087-3090 (2006). http://dx.doi.org/ 10.1016/j.carbon.2006.04.041
- [16] J. Li, Y. C.Cheng, Z. B.Guo, Z. H.Wang, Z. Y.Zhu, Q.Zhang, M. B.Chan-Park, U. Schwingenschlögl and X. X. Zhang, "Influence of contact height on the performance of vertically aligned carbon nanotube fieldeffect transistors", Nanoscale 5(6), 2476-2481 (2013). http://dx.doi.org/10.1039/c3nr33263b
- [17] W. Zhang, C. Chen and Y. Zhang, "Modeling of carbon nanotube field-effect transistor with nanowelding treatment", Microelectron. J. 40(12), 1681-1685 (2009). http://dx.doi.org/10.1016/j.mejo. 2009.08.002
- [18] S. Heinze, J. Tersoff, R. Martel, V. Derycke, J. Appenzeller and Ph. Avouris, "Carbon nanotubes as Schottky barrier transistors", Phys. Rev. Lett. 89, 106801 (2002). http://dx.doi.org/10.1103/ PhysRevLett.89.106801
- [19] A. Javey, J. Guo, Q. Wang, M. Lundstrom and H. Dai, "Ballistic carbon nanotube field-effect transistors", Nature 424(7), 654-657 (2003). http://dx.doi. org/10.1038/nature01797