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EXPERIMENTAL AND NUMERICAL INVESTIGATION OF SAND COMPRESSION PECULIARITIES

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Abstract. Investigation of the compression properties of Klaipėda sand by oedometer testing and numerical modeling is presented. Klaipėda sand is characteristic of the Baltic seashore region sand. Experimental investigation was performed with fraction corresponding to diameter variation bounds of 0.6 and 0.425 mm. Compression test was realized with initial maximal void ratio ($e_0 = 0.800$) of sand. Employed vertical stress ramp value is 800.0 kPa/min, maximum loading $\sigma_{max} = 400.0$ kPa. Applying loading within the range of 50.0 to 120.0, two vertical stress jumps have been identified. A rubber sample compression test has been performed aiming to deny an assumption, that vertical stress jumps are influenced by device construction. Experiment viewed that not any vertical stress jumps have been recognized. Numerical simulation yielded exactly the same two vertical stress jumps found by compression with oedometer. It proves that the nature of rearrangement of sand grains has been properly reflected by modeling compaction process by DEM. Sand compaction velocity is higher versus applied vertical stress ramp. This is the reason for appearing of the vertical stress jumps. Numerical simulation viewed that location of the largest compression in oedometer is at the top of the sample.

Keywords: sand compression, oedometer test, discrete element method (DEM), numerical simulation, morphological parameters.

1. Introduction

An analysis of actual deformed behaviour stages of ground in many cases is possible only by applying simulation results at the level of soil particles or grains. Such an approach is important not only for rational, sometimes being in conflict to routine design procedures, employing the partial coefficients of safety. This is also important for identifying the real bearing capacity and deformable response of geotechnical structures, especially for complicated ones.

Still one can state, that numerical simulation of deformed behaviour of soil even at the level of particles can lead to contradictory and unreliable results. Therefore it should be accompanied by some experimental investigation of soil behaviour and proper validation of results. This is necessary for accurate identifying of mechanical properties for numerical modeling, also when applying DEM with large computer resources or widely employed FEM with less computer resources.

The Discrete Element Method (DEM) introduced by Cundall (1974) and Cundall and Strack (1979) is a numerical method used to compute the stresses and displacements in a volume containing a large number of particles such as grains of sand. The granular material is modeled

as an assembly of rigid particles and the interaction between each particle is explicitly considered. DEM could be viewed as a generalized finite element method (FEM).

The aim of the current investigation is to analyse the sand compression via oedometer testing and simulating analogous process by applying DEM techniques. Validation of experimental and numerical results, also necessary interventions for corrections due to identified reasons of inaccuracies for creating proper numerical physical model of compression test leads to proper accuracy of numerical modeling.

The reader can be referred to many investigations on comparison of experimental (physical) investigation and adequate numerical modeling of tests (Cheng *et al.* 2009; Ferellec, McDowell 2010; Kruggel-Emden *et al.* 2008; Sukumaran *et al.* 2008; Zhu *et al.* 2008), but many of them do not sufficiently evaluate the actual shapes of soil particles for deformable behaviour and/or peculiarities of testing equipment. The investigation via DEM in Lithuania is in its primary stage (Amšiejus *et al.* 2010; Balevičius *et al.* 2006; Kačianauskas *et al.* 2010; Pocius, Balevičius 2012).

For creating relevant physical models of actual sand grains, the extended microscopic analysis and relevant

processing of results should be performed at first (see Maeda *et al.* 2009; Szarf *et al.* 2009; Tsomokos, Georgiannou 2010). Such primary investigations prescribe the parameters of particles to be considered (Cavarretta 2009), namely: particle shape, form coefficient, area, perimeter, roundness, angularity and sphericity. The friction between individual particles should be also properly evaluated (Chandler, Sands 2010).

In this investigation we employed the air-dry Klaipėda sand particles with diameters varying within bounds of 0.6 and 0.425 mm. This corresponds to one fracture, obtained by performing usual sieve analysis. This fracture was the dominating and prescribing compressibility of Klaipėda sand (Skuodis, Amšiejus 2011). Such an approach with analysis of one fracture was applied aiming to reduce the number of unknowns (Arasan *et al.* 2011), id est, for reducing computational time of DEM simulations. The physical and numerical experiments have been started with maximal initial void ratio soil aiming to investigate nature of compaction processes during loading (Thewes *et al.* 2010). Current numerical investigations have been performed by applying DEM software “EDEM 2.2.1” (DEM solutions 2009) and FEM software “Plaxis 3D Foundation” (Plaxis 2007). Physical experiments have been performed by applying universal oedometer apparatus ADS 1/3 (Wille Geotec Group 2010).

2. Experimental set-up

Baltic Sea sand from the area of Klaipėda was chosen because of naturally larger smoothness and size of grains.

The sieve analysis according to standards ISO3310:2-1999 and BS410-1:2000 has been performed. The fraction of 0.6–0.425 mm grains was employed for further investigations. For avoiding water influence on interaction of grains, the air-dry sand has been used.

The microscopic analysis of grains shapes for selected fraction has been performed (Kavrus, Skuodis 2012) for identifying morphological parameters of grains. The scanning electronic microscope and specialized software for processing of views “STIMAN” (STIMAN 2010) have been employed. The view analysis of microscopic investigations yielded the following morphological parameters of sand grains: roundness $C = (2(\pi A))^{0.5}/P$ (where A is area of a particle, μm); sphericity $R = (d/D)^{0.5}$ (where d is internal particle diameter, μm and D is external particle diameter, μm) and form coefficient $K_f = a/b$ (where a is internal particle diameter, μm and b is external particle diameter, μm).

Processing data of 33 grains of sand yielded the minimum ($K_{f,min} = 0.3413$), maximum ($K_{f,max} = 0.8808$) and mean ($K_{f,mid} = 0.6970$) form coefficients for physical models of particles.

Compression test has been performed by universal oedometer apparatus ADS 1/3 (Wille Geotec Group 2010), see Fig. 1. The poured via free fall soil was applied aiming to make identical conditions for numerical and physical experiments. Such an approach to sample preparations for physical experiments yielded the maximal initial void ratio $e_o = 0.800$.



Fig. 1. Universal oedometer apparatus ADS 1/3 (Wille Geotec Group 2010)

Amongst negative side effects met when preparing the compression test is creating a contact between soil and porous stone (compressing stamp) of oedometer. Obviously, the vertical pressure on top of soil sample is not a zero value. Thus, one cannot exactly identify the initial void ratio e_o of sample (Amšiejus *et al.* 2006). Note, that discrete model for simulation is free from this side effect.

To check an influence of loading velocity (rate), the particles of fraction (0.6–0.425 mm) have been loaded with different velocities, namely: 25.0; 50.0; 100.0; 200.0; 400.0 and 800.0 kPa/min. All velocities resulted in the same character of compression curve. Therefore all experiments further have been performed with 800.0 kPa/min loading rate. This rate, the maximal available for employed testing equipment was also used for numerical simulation of compression (compaction) test.

The maximal loading value of 400.0 kPa was taken for ensuring only compaction and for avoiding crash of separate sand particles. The average duration of compaction test was 30 sec; results have been fixed with 0.5 sec intervals.

3. DEM simulation

Numerical simulation of compression test has been simulated by applying discrete element method (DEM). The method is applied for modeling of noncohesive grained material. The DEM analysis method “EDEM 2.2.1 Academic code” (DEM solutions 2009) has been employed for simulations.

A method of parametric reduction is applied rather often as performing test for actual sample dimensions requires large computational resources and time.

Therefore, the reduced sample dimensions employed for numerical simulations were as follows: height $h = 0.005$ m, diameter $\varnothing = 0.01$ m. The dimensions of particles filled into the volume remained as of original ones (see Fig. 2).

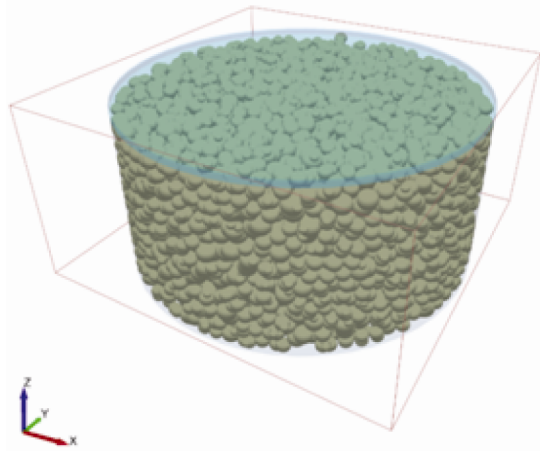


Fig. 2. Discrete model of oedometer and sample

For more accurate description of shape of grains (e.g. spherical shape of particle is the most rough discretization), the grain shape model was created applying the multi-sphere (MS) approach. This approach allows creating the discrete model of actual sand grain as a compound of a clump of spheres of different radii. In our case discrete models of grains consisted of 3–5 spheres.

Three characteristic MS particles (see Fig. 3) with different morphological parameters (see Table 1) have been created by processing morphological parameters obtained via microscope view analysis with software “STIMAN” (STIMAN 2010).

The following physical parameters of discrete model of particles were chosen for numerical simulations, namely: Poisson’s ratio $\nu = 0.14$, density $\rho = 2650 \text{ kg/m}^3$, shear modulus $G = 3.1e + 07 \text{ Pa}$, coefficient of restitution 0.5, coefficient of static friction 0.3, coefficient of rolling friction 0. Shear modulus was also reduced due to limited computational resources, respectively.

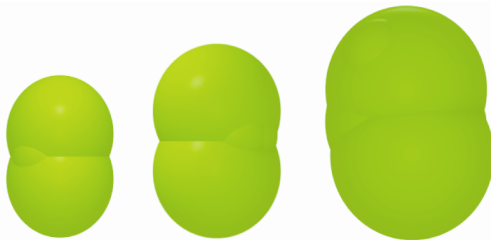


Fig. 3. Characteristic shapes of modeled particles

Table 1. Parameters of created discrete models of particles

| | Mass, kg | Volume, m ³ | Total number of particles |
|------------|-----------|------------------------|---------------------------|
| Particle 1 | 7.308E-08 | 2.758E-11 | 2310 |
| Particle 2 | 1.036E-07 | 3.908E-11 | 2309 |
| Particle 3 | 1.975E-07 | 7.451E-11 | 1101 |

The particles were created randomly setting them to the larger volume than created oedometer. Then particles were dropped into oedometer via gravity force. Surface

flattening was performed until it reached oedometer’s height by controlled mass of the particles and this process did not affect initial porosity.

The maximum magnitude of initial void ratio $e_o = 0.668$ has been obtained by filling procedures.

At the second stage the filled particles have been compressed. Duration of numerical experiment was $t = 0.3 \text{ s}$, with the linearly constant velocity $v = 0.00075 \text{ m/s}$ of porous stone (compressing plate).

Selected simulation time step was $1 \mu\text{s}$. The total duration of numerical experiment was 18.3 hours.

Analogous modeling of oedometer and that of process of compression have been performed by “Plaxis 3D Foundation” finite element method (FEM) software (Plaxis 2007). The following soil parameters have been employed: void ratio $e = 0.798$; deformation modulus $E_{oed} = 58.6 \text{ MPa}$; Poisson’s ratio $\nu = 0.270$; unit weight $\gamma = 14.56 \text{ kN/m}^3$; angle of internal friction $\varphi = 33^\circ$; cohesion $c = 12.0 \text{ kPa}$. Internal friction angle and cohesion values were taken by processing simple shearing tests results of investigated sand of Klaipėda.

4. Analysis of results

The view analysis of microscopic investigations yielded the following morphological parameters of sand grains: roundness $C = 0.49$; sphericity $R = 0.79$; form coefficient $K_f = 0.697$ (see Fig. 4).

When analyzing Fig. 4, one can find that some particles (due to the diameters) are larger or less than the mesh of sieves. This phenomenon can be explained as follows: the oblong particles get through mesh of sieves (Žurauskienė et al. 2010), therefore they appear in other fractions of investigated sand.

When comparing the results of numerical and physical experiments, the following features have been identified, namely:

1. The maximum void ratio of numerical experiment ($e_o = 0.668$) is less comparing it by physical experiment ($e_o = 0.800$).

2. The created discrete models of soil grains fit the morphological parameters obtained by microscopic analysis. But the actual shape of discrete models of grains (see Fig. 4) differs from the actual shapes of grains (see Fig. 5).

3. The stress jumps have been observed at certain time points when performing compression tests, both numerically and physically.

When analyzing some discrepancy between maximum initial void ratios, it is obvious that the simulated mixture of discrete models of grains for numerical simulations is not completely the same when comparing it with the natural mixture, corresponding one fracture (0.6–0.425 mm, obtained from sieve analysis). It is obvious that the sand fracture mixture, containing relatively much larger particles in diameter, results in lower initial void ratio (Skuodis, Amšiejus 2011).

One can also state that the actual surface of discrete models of particles is more smooth and soft when compared with actual ones of sand grains.

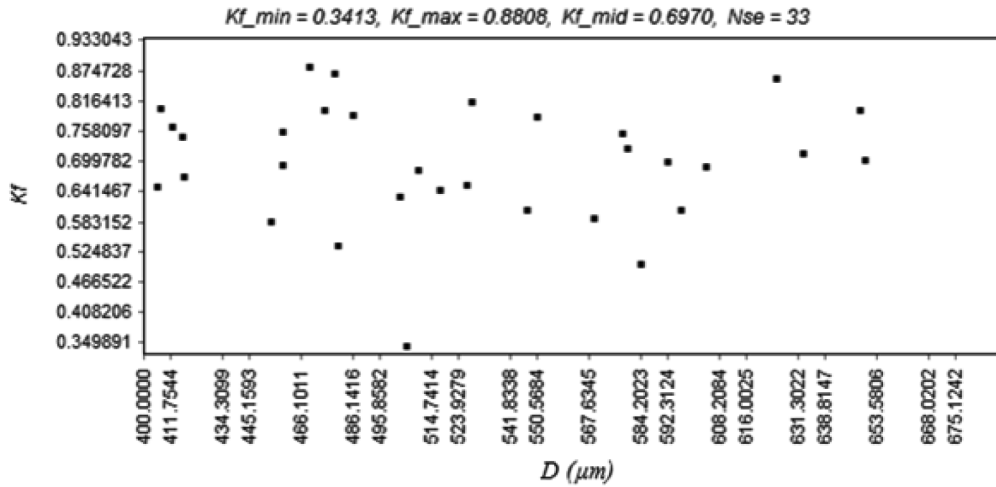


Fig. 4. Distribution of form coefficient versus particle diameter for characteristic Baltic seashore sand

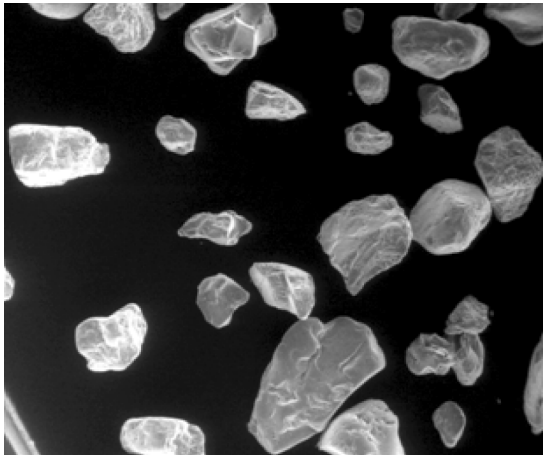


Fig. 5. Characteristic shapes of the Baltic seashore sand

The stress jumps of vertical pressure were observed both in numerical and physical tests. Theoretically, the compressed soil sample during physical test had to be loaded by constantly increasing load, id est, by 800.0 kPa/min (Fig. 6), but one observed the maximum jumps of vertical load within an interval of 50.0–120.0 kPa.

When results are plotted using vertical stress versus vertical strain diagram (see Fig. 7), it explains the results of Fig. 6.

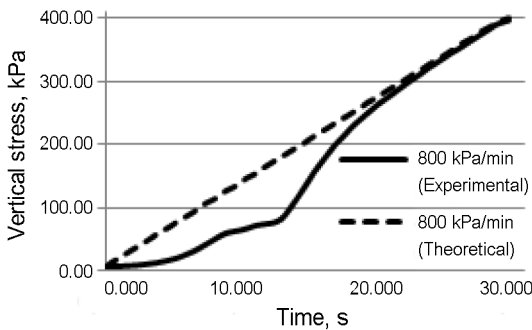


Fig. 6. Controlled vertical stress ramp (800.0 kPa/min) versus time

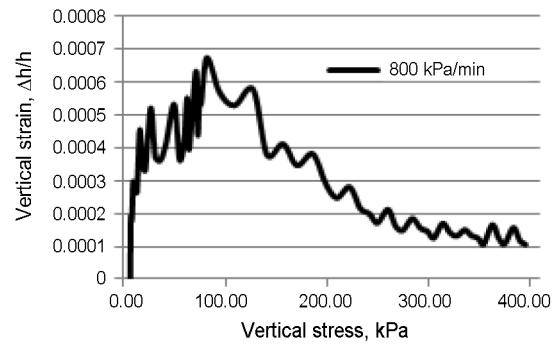


Fig. 7. Vertical stress versus vertical strain (800.0 kPa/min)

Analyzing the results of Fig. 7 it was observed that when vertical stress is less than 200 kPa, vertical strain values increase. When vertical stress is between 200 and 400 kPa, vertical strain values stabilize and vertical stress ramp becomes equal to theoretical. This process depends on initial soil sample void ratio. Vertical strain values increase when soil sample void ratio is high. When soil density increases, then vertical strain values decrease.

The direction line, created according to loading velocity and load application time, shows that loading velocity was not linear (Fig. 8). In case of homogeneous material the direction line corresponds to the horizontal one.

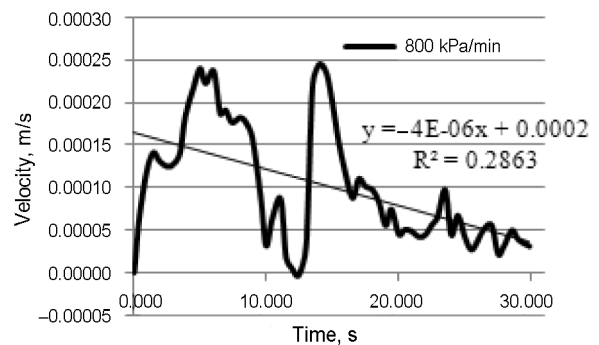


Fig. 8. Vertical stress ramp velocity versus vertical stress loading time

The jumps of vertical pressure have been identified by compressing soil with different rates: 25; 50; 100; 200 and 400 kPa/min (see Figs 9–13).

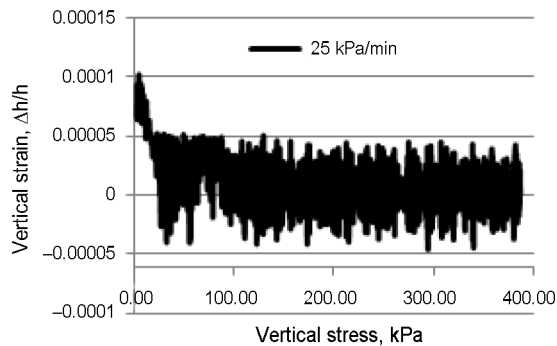


Fig. 9. Vertical stress versus vertical strain (25.0 kPa/min)

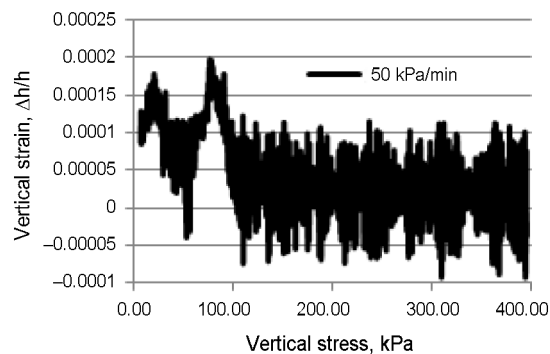


Fig. 10. Vertical stress versus vertical strain (50.0 kPa/min)

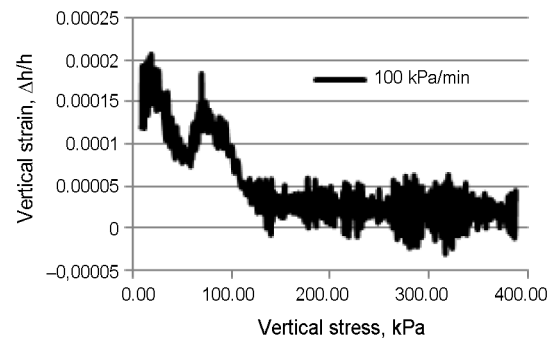


Fig. 11. Vertical stress versus vertical strain (100.0 kPa/min)

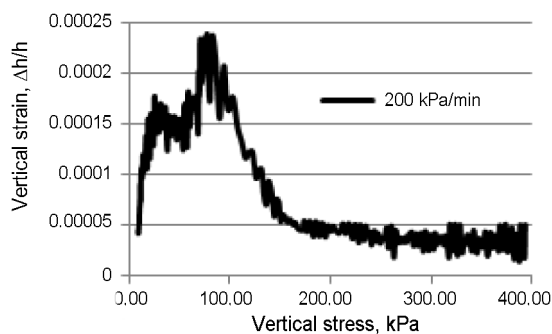


Fig. 12. Vertical stress versus vertical strain (200.0 kPa/min)

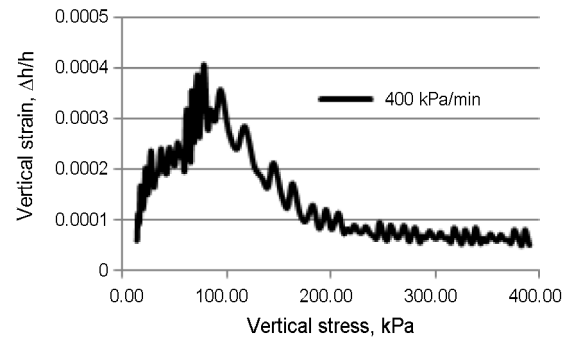


Fig. 13. Vertical stress versus vertical strain (400.0 kPa/min)

Basing on analysis results of Fig. 7 and Figs 9–13, one can state that vertical stress jumps are induced by loading velocity. Aiming to reject the influence of technical reasons or technical peculiarities of testing equipment, an additional compression test was performed with rubber sample under loading velocity of 100 kPa/min. The loading interval within 50.0 and 120.0 kPa was analyzed (see Figs 14 and 15).

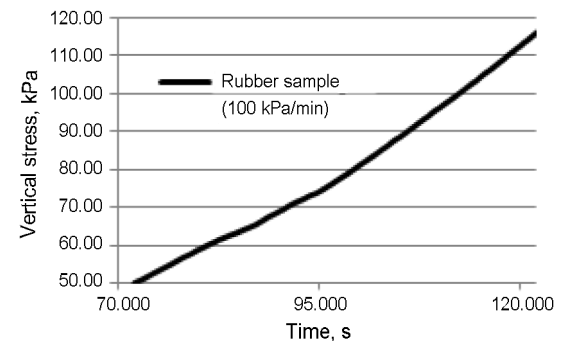


Fig. 14. Controlled vertical stress ramp (rubber compression from 50.0 to 120.0 kPa) versus time

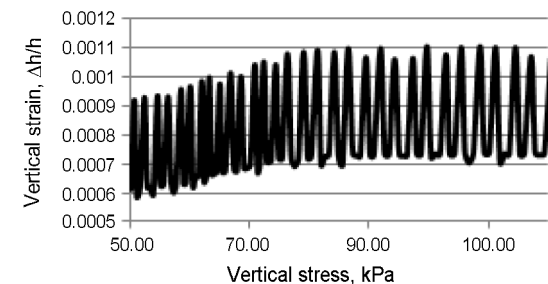


Fig. 15. Vertical stress versus vertical strain (rubber compression from 50.0 to 120.0 kPa)

When comparing compression tests with rubber and soil (see Figs 7 and 15) one can state that the reason of loading jumps is different due to technical peculiarities of oedometer. The appeared stress change on the top of the sample is induced by sudden change of soil structure, id est, the velocity of rearrangement of soil grains is larger comparing with load application velocity. Therefore the load transducer is fixing stress change on the top of soil sample.

When performing soil compression test numerically, one faces the analogous phenomenon, id est, the results

are similar. The loading is described via relative (normalized) units in numerical model which are different from real experiment. Such an approach (also in respect of physical parameters) is widely used currently by many researchers aiming to reduce computational resources, as was described above. Thus, the compression results obtained via numerical simulation (see Figs 16 and 17) are compared with those obtained via actual (physical) experiments qualitatively, aiming to identify the character of compressive curve.

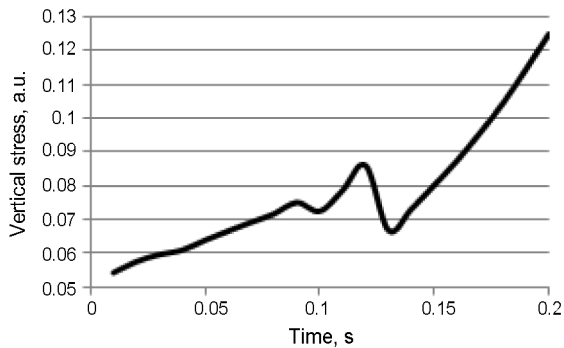


Fig. 16. Characteristic sand compression curve via DEM simulation

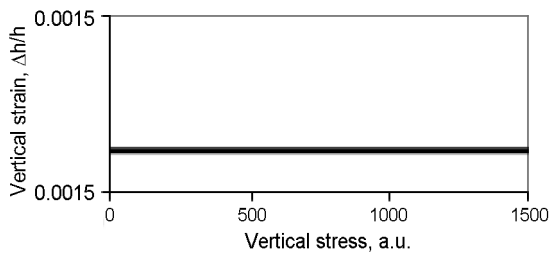


Fig. 17. Vertical stress versus vertical strain via DEM simulation

When analyzing Figs 7 and 17 one can find that soil particles displace in respect of each other during the compression process. This induce the stress jumps under the porous stone. When performing the physical (experimental) tests, the soil was applied incrementally under constant velocity (800.0 kPa/min) with increasing load. When performing numerical simulations the load velocity ($v = 0.00075$ m/s) was constant during the test time.

Fig. 18 shows the view of inter-particle velocities flow of numerical test model. This model was created to analyze reasons of stress changes within sample in oedometer.

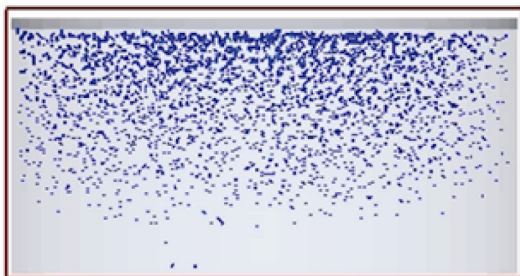


Fig. 18. Particle flow velocity in oedometer

Fig. 18 clearly illustrates that maximum rearrangement of particles is located on the top of oedometer sample in soil, id est, under the porous stone. This inter-particle movement process proves that the velocity of particles when loaded becomes larger (when friction of particles is overcome) compared with velocity of applied loading.

The same compression curve character was obtained having simulated the oedometer and the soil (parameters compatible with the simulated by DEM) by FEM “Plaxis 3D Foundation” (Plaxis 2007), Fig. 19.

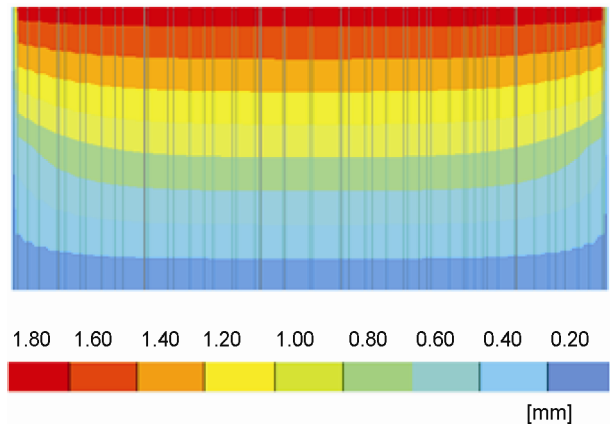


Fig. 19. Total displacement distribution in oedometer

When analyzing Fig. 19, one also can find that maximum displacements of soil are at pore stone, compressing the soil sample. The displacements are significantly less near oedometer walls because of the developed friction between soil and walls. The analogous results have been also obtained from DEM analysis by software “EDEM 2.2.1” (see Fig. 18).

5. Conclusions

1. Despite the fact that the shape of developed discrete models of sand particles fits the form coefficients (determined via microscopic analysis) of actual sand grains, they are not identical to the natural sand ones. This results in different actual and simulated maximal void ratios, they are $e_o = 0.800$, and $e_o = 0.668$, respectively.

2. The nature of stress jumps, identified experimentally can be explained by the results of numerical simulations. When inter-particle friction is overcome, the velocity of rearrangement of particles is larger than the loading velocity. When the loading reaches the 120 kPa limit, the velocity of rearrangement of particles reduces significantly and the movement of particles practically stops.

3. During experimental investigations vertical stress jumps are induced by loading velocity. Aiming to avoid vertical stress jumps it is recommended to do experimental tests with lower than 50 kPa/min vertical stress ramp.

4. Results of numerical simulations proved that the largest compaction is at the top of sample, id est, at location of largest rearrangement of soil particles.

5. Although the nature of compression (compaction of particles) was identified, one should perform numerical simulations with more than two morphological parameters (form coefficient K_f and particle diameter D) of soil grains and, due to the computational possibilities, to perform simulation with closer to actual physical parameters. Such an approach could enable comparing the results of numerical simulation and physical experiment not only qualitatively.

Generalizing the findings of current investigation it can be stated that analysis and qualitative comparison of numerical simulation and physical experiments yielded that numerical simulation adequately describes the nature of compaction processes during compression test. It also allows to evaluate adequately the actual boundary conditions. DEM also allows to qualitatively and quantitatively evaluate the relevant application of FEM and choosing its proper physical parameters. Still, it should be emphasized, that numerical simulation requires performing primary validation of numerical simulation and physical experiments aiming to calibrate initial parameters for adequate evaluation of the boundary conditions.

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