

# Design Method for Negative Group Delay Circuits Based on Relations among Signal Attenuation, Group Delay, and Bandwidth

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## Abstract

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Typical negative group delay circuits (NGDC) are analyzed in terms of signal attenuation, group delay, and bandwidth using  $S$ -parameters. By inverting these formulations, we derive and present the design equations (for NGD circuit elements) for a desired specification of the two among the three parameters. The proposed design method is validated through simulation examples for narrow- and wide-band pulse inputs in the time and frequency domains. Moreover, an NGDC composed of lumped elements is fabricated at 1 GHz for measurement. As a function of frequency, the circuit-/EM-simulated and measured group delays are in good agreement. The provided simple NGDC design equations may be useful for many applications that require compensations of some signal delays.

**Key Words:** Bandwidth, Negative Group Delay, Passive Element, Signal Attenuation, Synthesis.

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## I. INTRODUCTION

Negative group delay (NGD) was initially presented by Brillouin [1] in the 1960s, and it has been studied actively since the research on superluminal effects was published in [2]. The NGD characteristics have been demonstrated in various systems. In the microwave area, NGD circuits are used to compensate for group delays usually caused by the use of filters or amplifiers [3, 4]. Many studies have been conducted to utilize the NGD phenomenon by employing various structures, such as a defected microstrip structure and a defected ground structure [5]. In [6], the familiarity between a non-Foster reactive property and NGD networks with loss compensation was discussed theoretically and experimentally. A loss-compensated NGD network composed of cascading two unit cells and amplifiers was also presented for

larger NGD effects. Some design equations were proposed through an  $S$ -parameter analysis [6–9], a lossy coupling matrix synthesis [10], and a filter analysis [11]. The design equations for negative group delay circuit (NGDC) using lumped RLC resonators are also available based on the specification of the signal attenuation and NGD [12, 13]. In this study, we derive the mathematical relations among signal attenuation, NGD, and bandwidth for a convenient and systematic design of the NGDC composed of RLC resonators. The effects of the NGDC are evaluated in the time and frequency domains using narrow- and wide-band pulse inputs. To verify the proposed design equations, we fabricate an NGDC composed of lumped elements at 1 GHz. The group delays of the fabricated NGDC are measured and compared with those obtained from the presented design equations.

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## II. ANALYSIS AND SYNTHESIS OF A GROUP DELAY CIRCUIT

### 1. Analysis

Fig. 1(a) shows an equivalent circuit consisting of a parallel resonant circuit connected in a series with a transmission line.  $Z_0$  is the characteristic impedance of the host transmission line. Fig. 1(b) shows an equivalent circuit consisting of a series resonant circuit connected in parallel with a transmission line.  $Y_0$  is the characteristic admittance. Most passive NGD structures can be modeled on the basis of these equivalent circuits in Fig. 1(a) and (b).

In Fig. 1(a), the admittance of  $Y_{NGD}$  of the parallel resonant circuit can be expressed as

$$Y_{NGD} = G_0 + j\sqrt{\frac{C_0}{L_0}}\left(\frac{\omega}{\omega_0} - \frac{\omega_0}{\omega}\right) \approx G_0 + j2C_0(\omega - \omega_0), \quad (1)$$

where  $G_0$  is the conductance,  $\omega$  is the angular frequency,  $\omega_0$  is the resonant angular frequency given by  $1/\sqrt{C_0L_0}$ , and  $\sqrt{C_0/L_0}$  (or  $\omega_0C_0$ ) is the susceptance slope parameter. The last expression in (1) is an approximation based on the assumption that  $\omega$  is near  $\omega_0$ .

The impedance  $Z_{NGD}$  can be approximated as

$$Z_{NGD} = \frac{1}{Y_{NGD}} \approx \frac{G_0 - j2C_0(\omega - \omega_0)}{G_0^2}. \quad (2)$$

Then, the input impedance  $Z_{in}$  is the sum of  $Z_{NGD}$  and  $Z_0$ . The reflection coefficient  $S_{11}$  is obtained as

$$S_{11} = \frac{V_1^-}{V_1^+} = \frac{Z_{in} - Z_0}{Z_{in} + Z_0} = \frac{Z_{NGD}}{Z_{NGD} + 2Z_0} = \frac{G_0^2(1 + 2Z_0G_0) + 4C_0^2(\omega - \omega_0) - j4Z_0G_0^2C_0(\omega - \omega_0)}{G_0^2(1 + 2Z_0G_0)^2 + 4C_0^2(\omega - \omega_0)^2}. \quad (3)$$

When  $\omega = \omega_0$ ,  $S_{11}$  (3) is simplified to

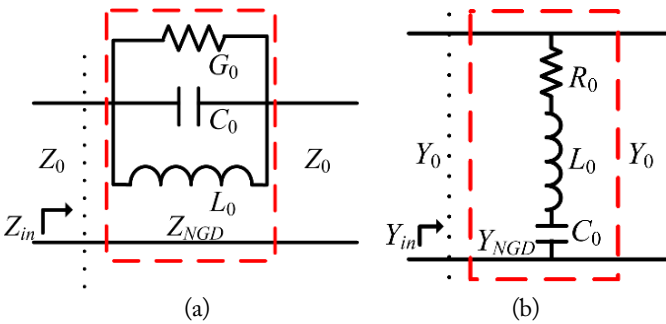


Fig. 1. (a) Equivalent circuit for the NGD structure made of a parallel GCL resonator connected in a series with a transmission line. (b) Equivalent circuit for the NGD structure made of a series RLC resonator connected in parallel with the transmission line.

$$S_{11} = \frac{1}{1 + 2Z_0G_0}. \quad (4)$$

The transmission coefficient ( $S_{21}$ ) of the NGDC unit cell can be obtained by the ratio of the transmitted voltage ( $V_2^-$ ) and input voltage ( $V_1^+$ ) given by

$$S_{21} = \frac{V_2^-}{V_1^+} = \frac{2Z_0}{2Z_0 + Z_{NGD}} \approx \frac{2Z_0G_0(1 + 2Z_0G_0) + j4Z_0C_0(\omega - \omega_0)}{(1 + 2Z_0G_0)^2}. \quad (5)$$

The real and imaginary parts of  $S_{21}$  are represented by

$$\text{Re}[S_{21}] = \frac{2Z_0G_0}{1 + 2Z_0G_0} \quad (6)$$

and

$$\text{Im}[S_{21}] = \frac{2Z_0[2C_0(\omega - \omega_0)]}{(1 + 2Z_0G_0)^2}, \quad (7)$$

respectively.

$S_{21}$  (5) at  $\omega_0$  is simplified to

$$S_{21}(\omega_0) = \frac{2Z_0G_0}{1 + 2Z_0G_0}, \quad (8)$$

which is purely real and positive. That is, the transmission at  $\omega_0$  across the NGDC in Fig. 1(a) occurs without a phase delay. The phase for the NGDC is obtained as

$$\phi(\omega) = \angle S_{21} = \tan^{-1} \frac{\text{Im}[S_{21}]}{\text{Re}[S_{21}]} = \tan^{-1} \frac{2C_0(\omega - \omega_0)}{G_0(1 + 2Z_0G_0)}. \quad (9)$$

Then, the group delay ( $\tau$ ) [8] can be shown to be given by

$$\tau(\omega) = -\frac{d\phi}{d\omega} = -\frac{2C_0G_0[1 + 2Z_0G_0]}{G_0^2[1 + 2Z_0G_0]^2 + [2C_0(\omega - \omega_0)]^2}, \quad (10)$$

which is negative, and its magnitude is observed to become maximum at the resonant angular frequency  $\omega_0$  and zero when  $\omega$  is far away from  $\omega_0$ . The group delay is another word for a signal envelope delay [14]. The frequency dependence in (10) prevents a pulse input from being entirely copied in advance of the input at the output terminal. The maximum NGD is expressed as

$$\tau(\omega_0) = -\left.\frac{d\phi}{d\omega}\right|_{\omega=\omega_0} = -\frac{2C_0}{G_0(1 + 2Z_0G_0)}. \quad (11)$$

As  $G_0$  becomes smaller, the signal transmission becomes smaller, as implied by (8), but the effect of the NGD becomes larger, as shown by (11). The magnitude of the NGD is shown to be proportional to  $C_0$  as is the susceptance slope  $\omega_0C_0$ .

Fig. 2 shows the magnitudes and phases of  $S_{21}$  when  $\tau(\omega_0)$  (11) is assumed to be  $-0.5$ ,  $-1$ , and  $-5$  ns and  $S_{21}(\omega_0) = 0.5$  at

1 GHz. In the case of  $\tau(\omega_0) = -1$  ns,  $Z_0 = 50 \Omega$ ,  $G_0 = 1/100$  ( $1/\Omega$ ),  $C_0 = 10$  pF, and  $L_0 = 2.53$  nH. As the magnitude of  $\tau(\omega_0)$  becomes larger, the bandwidth of the NGD becomes smaller. This will result in more signal distortion if an input signal bandwidth is wider than the NGDC bandwidth. The positive phase slopes near 1 GHz shown in Fig. 2(b) lead to NGD s, as explained in (10).

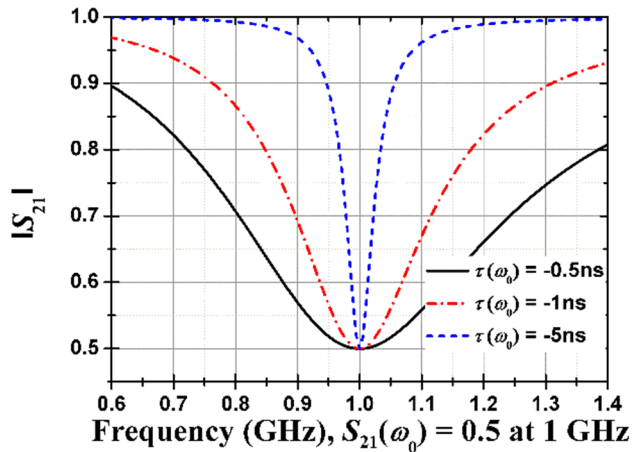
So far, we have analyzed the NGD equivalent circuit given in Fig. 1(a) in terms of the signal transmission  $S_{21}$  and NGD  $\tau$ .

## 2. Synthesis

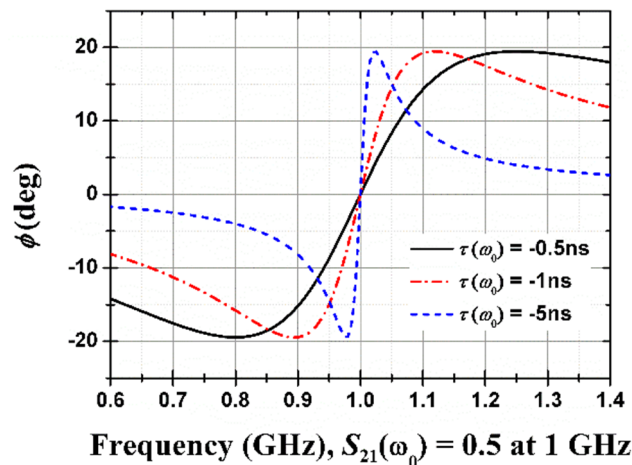
On the contrary, if specific values of  $S_{21}(\omega_0)$  and  $\tau(\omega_0)$  are desired for a particular NGD circuit design, (8) and (11) can be simultaneously solved for the design equations given by

$$G_0 = \frac{S_{21}(\omega_0)}{2Z_0[1 - S_{21}(\omega_0)]}, \quad (12)$$

$$C_0 = \frac{|\tau(\omega_0)|G_0(1 + 2Z_0G_0)}{2} = \frac{|\tau(\omega_0)|S_{21}(\omega_0)}{4Z_0[1 - S_{21}(\omega_0)]^2}, \quad (13)$$



(a)



(b)

Fig. 2. (a) Magnitudes of  $S_{21}$ . (b) Phases of  $S_{21}$  for different group delays when  $S_{21}(\omega_0)$  is fixed at 0.5 at 1 GHz.

and  $L_0$  is obtained with

$$L_0 = \frac{1}{\omega_0^2 C_0}. \quad (14)$$

Fig. 3 shows the capacitance values of the NGD circuit for different  $S_{21}(\omega_0)$  and  $\tau(\omega_0)$  at 1 GHz using (13). Whereas  $G_0$  (12) depends only on  $S_{21}(\omega_0)$ ,  $C_0$  and  $L_0$  depend on both  $S_{21}(\omega_0)$  and  $\tau(\omega_0)$ . Expressions (12)–(14) are actually the design equations to realize the specifically required values of  $S_{21}(\omega_0)$  and  $\tau(\omega_0)$ . With (12) and (13), the quality factor of the NGD circuit may be expressed as

$$Q_{NGD} = \frac{\omega_0 C_0}{G_0} = \frac{\omega_0 |\tau(\omega_0)|}{2[1 - S_{21}(\omega_0)]}. \quad (15)$$

Moreover, the 3 dB fractional bandwidth (BW) is roughly given by

$$BW \approx \frac{1}{Q_{NGD}} = \frac{G_0}{\omega_0 C_0} = \frac{2[1 - S_{21}(\omega_0)]}{\omega_0 |\tau(\omega_0)|}. \quad (16)$$

The bandwidth (16) becomes large as  $S_{21}(\omega_0)$  (8) or  $\tau(\omega_0)$  (11) becomes small. Note that if the two among the three design parameters  $S_{21}(\omega_0)$  (8),  $\tau(\omega_0)$  (11), and bandwidth (16) are specified, the rest is determined automatically. This relation is summarized in Table 1.

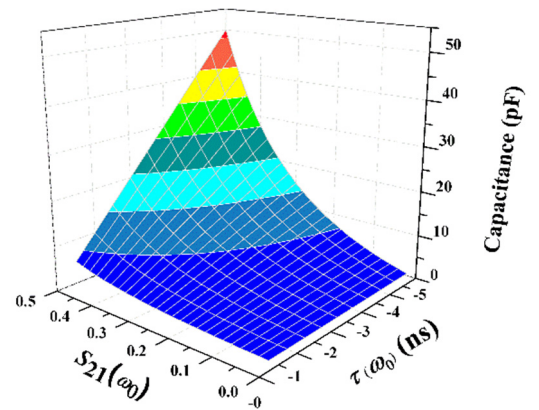


Fig. 3. Capacitance values for different  $S_{21}(\omega_0)$  and  $\tau(\omega_0)$ .

Table 1. Relation among design parameters  $S_{21}(\omega_0)$ ,  $\tau(\omega_0)$ , and BW

Specified design parameters for NGDC		Determined design parameter
$\tau(\omega_0)$	$S_{21}(\omega_0)$	$BW \approx \frac{2[1 - S_{21}(\omega_0)]}{\omega_0  \tau(\omega_0) }$
$\tau(\omega_0)$	$BW$	$S_{21}(\omega_0) \approx \frac{2 - \omega_0  \tau(\omega_0)  BW}{2}$
$S_{21}(\omega_0)$	$BW$	$ \tau(\omega_0)  \approx \frac{2[1 - S_{21}(\omega_0)]}{\omega_0 BW}$

Fig. 4(a) shows the group delay  $\tau(\omega)$  (10) as a function of frequency for different  $S_{21}(\omega_0)$ 's of -6, -10, and -20 dB when  $\tau(\omega_0)$  is -1 ns at 1 GHz. As  $S_{21}(\omega_0)$  becomes smaller, the bandwidth of  $\tau(\omega)$  becomes larger; this is the important trade-off feature of the presented NGDC. Fig. 4(b) shows  $S_{21}(\omega)$  as a function of frequency for the different  $S_{21}(\omega_0)$ 's of -10, -20, -30, and -40 dB when  $\tau(\omega_0)$  is fixed at -1 ns at 1 GHz. The symbols represent the calculated results using (5), and the lines represent the circuit-simulated results based on Fig. 1(a).

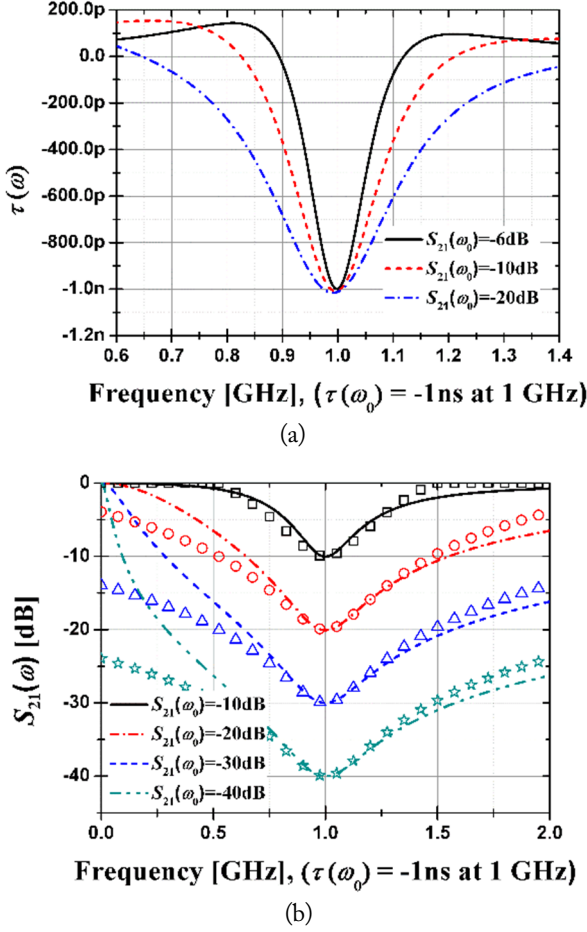


Fig. 4. (a) Group delay  $\tau(\omega)$  as a function of frequency for the different  $S_{21}(\omega_0)$ 's of -6, -10, and -20 dB. (b)  $S_{21}(\omega)$  as a function of frequency for the different  $S_{21}(\omega_0)$ 's of -10, -20, -30, and -40 dB when  $\tau(\omega_0) = -1$  ns at 1 GHz (symbols using (5), lines circuit simulations).

Table 2. Q-factors and bandwidth for the different  $S_{21}(\omega_0)$ 's of -10, -20, -30, and -40 dB when  $\tau(\omega_0) = -1$  ns at 1 GHz

	$S_{21}$ (dB)			
	-10	-20	-30	-40
Q-factor	4.595	3.491	3.244	3.173
BW (GHz) (16)	0.218	0.286	0.308	0.315
BW (GHz) (circuit)	0.24	0.29	0.325	0.325

In Table 2, we show the Q factors and compare the bandwidths based on (16) and circuit simulations. The results in Fig. 4(b) and Table 2 prove the theory to be accurate enough when  $\omega$  is near  $\omega_0$ .

In Fig. 5, we show the 3 dB fractional bandwidth (16) of the NGDC as a function of  $S_{21}(\omega_0)$  and  $\tau(\omega_0)$ . The bandwidth increases as  $S_{21}(\omega_0)$  decreases and  $|\tau(\omega_0)|$  gets smaller.

Table 3 shows the circuit element values of the NGDC obtained using the design Eqs. (12)–(14) assuming that  $S_{21}(\omega_0) = 1/2, 1/\sqrt{10},$  and  $1/10$  and  $\tau(\omega_0) = -0.5, -1,$  and  $-2$  ns at 1 GHz. Based on these circuit values, the NGDC circuits as shown in Fig. 1(a) can be easily realized.

Fig. 6 shows the diagram of the NGDC combined with an amplifier. The attenuated signal through the NGDC is shown to be properly amplified using the amplifier. The output signal may be somewhat distorted because the bandwidth of the NGDC is usually smaller than the bandwidth of the input signal.

Fig. 7 shows the envelopes and spectra of the input and output signals. The rising/falling time and the width of the input pulse are 3 ns and 1 ns, respectively. The 1 GHz carrier signal is shown only in Fig. 7(a) and is hidden in Fig. 7(b). The output with the NGDC is shown to have some NGD features with an attenuation of about 1/10. The effect of NGD is more pronounced after amplification 10 times. The spectrum of the output has more high-frequency components than that of the input, consistent with the time signals in Fig. 7(b).

In Fig. 8(a), we show the envelopes of the input and output

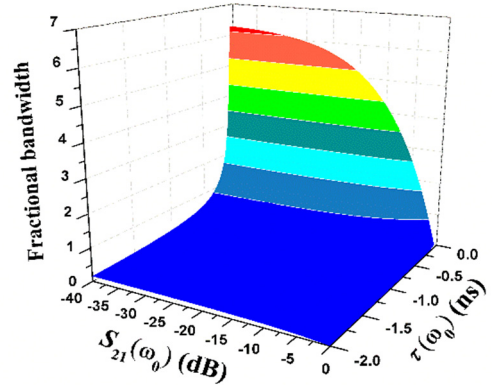


Fig. 5. The 3-dB bandwidth of NGDC as a function of  $S_{21}(\omega_0)$  and  $\tau(\omega_0)$  at 1 GHz.

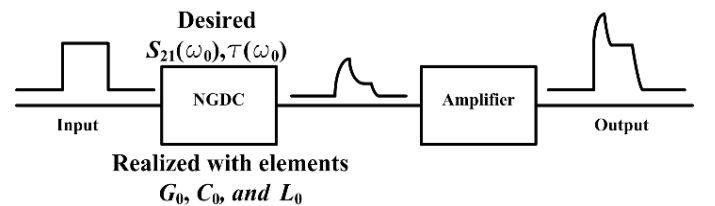


Fig. 6. Diagram of the NGDC combined with an amplifier (brief sketches of the input and output are shown).

Table 3. Calculated circuit values for specific examples

Desired		Solutions for NGD circuit		
$ S_{21}(\omega_0) $	$\tau(\omega_0)$ (ns)	$R_0(\Omega)$ ( $= 1/G_0$ )	$C_0$ (pF)	$L_0$ (nH)
1/2	-0.5	100	5	5.07
	-1		10	2.53
	-2		20	1.27
$1/\sqrt{10}$	-0.5	216.23	1.69	14.98
	-1		3.38	7.49
	-2		6.76	3.75
1/10	-0.5	900	0.31	82.07
	-1		0.62	41.04
	-2		1.23	20.52

signals with  $\tau(\omega_0) = -1$  ns and  $-2$  ns, respectively. The rising/falling time and the width of the input pulse are 3 ns and 3 ns, respectively. The carrier frequency is again 1 GHz but not shown. As the magnitude of  $\tau(\omega_0)$  increases, the output appears more ahead of the input pulse, but its distortion compared with the input pulse becomes larger. In Fig. 8(b), we show the same when  $\tau(\omega_0) = -1, -2,$  and  $-5$  ns. For this case, the rising/falling time and the width of the input pulse are 6 ns and 6 ns, respectively. The input pulse in Fig. 8(b) is slowly varying, and its spectrum should be narrower than that in Fig. 8(a). This leads to less distortion as demonstrated particularly in the case of  $\tau(\omega_0) = -2$  ns.

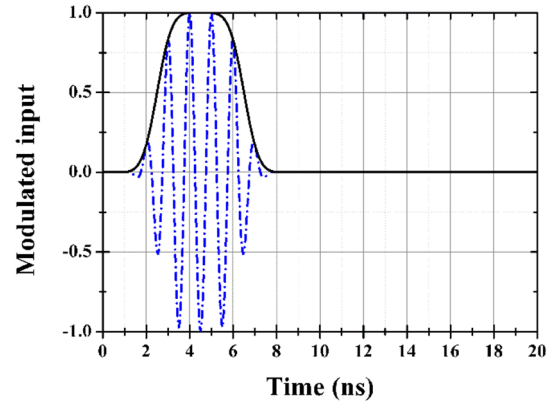
Fig. 9(a) shows the structure of the proposed NGDC composed of lumped RLC elements based on the required  $S_{21}(\omega_0) = -20$  dB and  $\tau(\omega_0) = -1$  ns at 1 GHz. Fig. 1(b) is the photograph of the measurement setup. The permittivity of the microstrip transmission line with a thickness of 1.6 mm and the lumped element values are  $\epsilon_r = 2.2, R_0 = 900 \Omega, C_0 = 0.62$  pF, and  $L_0 = 41$  nH using (12)–(14). The  $S$ -parameters of the structure are measured using a network analyzer. The influence of the transmission line is de-embedded on the reference plane at the center of the structure.

Table 4 presents the circuit element values calculated using Eqs. (12)–(14), tuned by electromagnetic (EM) simulations, and used for fabrication. The values tuned by the EM simulations are different from the theoretical ones. The actually used element values are the ones closest to the available ones.

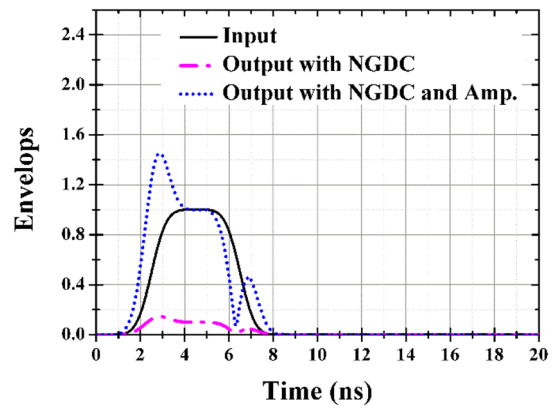
Fig. 10 shows the circuit-/EM-simulated and measured  $S$ -parameters and group delays as a function of frequency in the case shown in Fig. 9. They all show to be in good agreement. The output time signals to the input pulses are similar to the dotted lines with  $\tau(\omega_0) = -1$  ns in Fig. 8(a).

In the case of using  $N$  unit cells in Fig. 1(a), (8) can be shown to be generalized to

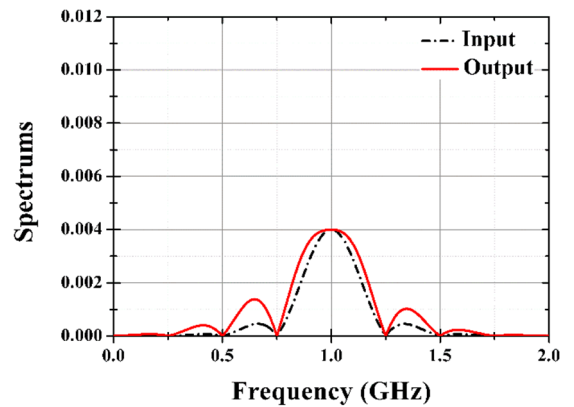
$$S_{21}(\omega_0) = \frac{2Z_0G_0}{N + 2Z_0G_0} \quad (17)$$



(a)



(b)



(c)

Fig. 7. (a) Modulated input signal and carrier as a function of time. The rising/falling time and the width of the input pulse are 3 ns and 1 ns, respectively. The carrier frequency is 1 GHz. (b) Envelopes of the input and output as a function of time with the desired  $\tau(\omega_0) = -1$  ns and  $S_{21}(\omega_0) = -20$  dB. (c) Spectra of the input and output as a function of frequency.

and (11) to

$$\tau(\omega_0) = -\left. \frac{d\phi}{d\omega} \right|_{\omega=\omega_0} = -\frac{2NC_0}{NG_0 + 2Z_0G_0^2}. \quad (18)$$

As the number  $N$  of the identical unit cells increases, the signal transmission (17) decreases but the NGD (18) does not change



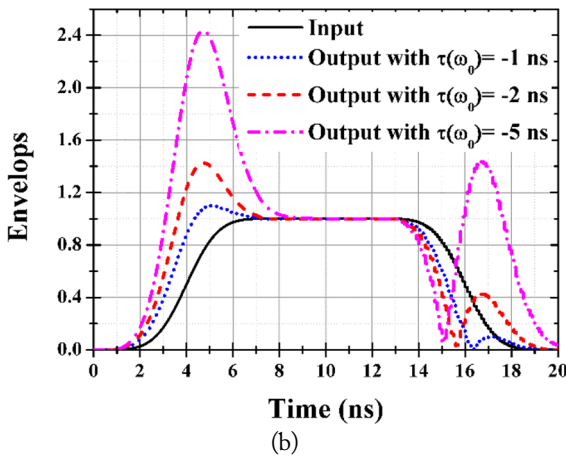
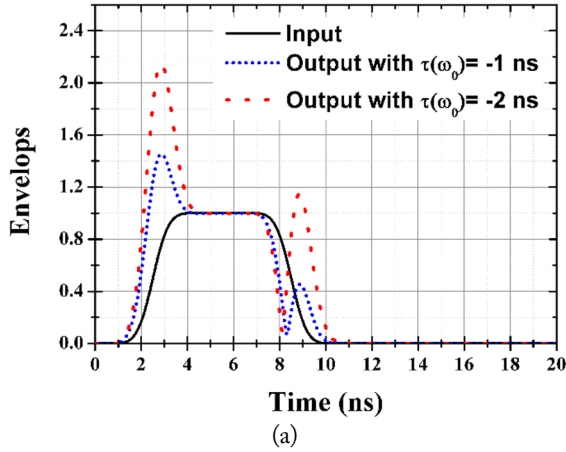


Fig. 8. (a) Circuit-simulated envelopes of the input and output signals as a function of time with the desired  $S_{21}(\omega_0) = -20$  dB for different  $\tau(\omega_0) = -1$  ns and  $-2$  ns. The rising/falling time and the width of the input pulse are 3 ns and 3 ns, respectively. The hidden carrier frequency is 1 GHz. (b) Envelopes of the input and output as a function of time with the desired  $S_{21}(\omega_0) = -20$  dB for different  $\tau(\omega_0) = -1, -2,$  and  $-5$  ns. The rising/falling time and the width of the input pulse are 6 ns and 6 ns, respectively. The hidden carrier frequency is 1 GHz.

Table 4. Lumped element values for the case in which  $S_{21}(\omega_0) = -20$  dB and  $\tau(\omega_0) = -1$  ns at 1 GHz

	$R$ ( $\Omega$ )	$L$ (nH)	$C$ (pF)
Theory (12)–(14)	900	41	0.62
Tuned by EM	900	37	0.55
Used for fabrication	900	33	0.5

much.

In the case of the NGDC in Fig. 1(b), the analysis and design equations are obtained by simply converting  $Z_0, G_0, C_0, L_0,$  and  $Z_{in}$  in this study to  $Y_0, R_0, L_0, C_0,$  and  $Y_{in}$  using the duality principle. The presented design method is applicable to other previous passive NGD circuits, not just the one demonstrated in this study.

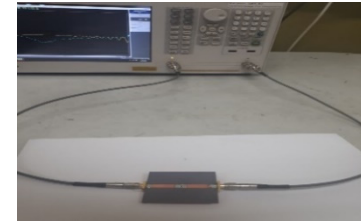
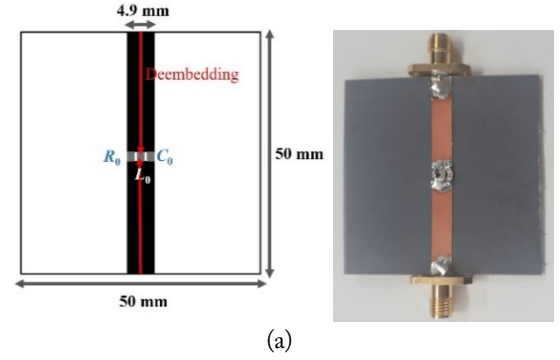


Fig. 9. (a) Fabricated NGDC composed of lumped RLC elements based on the required  $S_{21}(\omega_0) = -20$  dB and  $\tau(\omega_0) = -1$  ns at 1 GHz ( $\epsilon_r = 2.2$ , thickness = 1.6 mm,  $R_0 = 900 \Omega$ ,  $C_0 = 0.5$  pF, and  $L_0 = 33$  nH). (b) Photograph of the measurement setup.

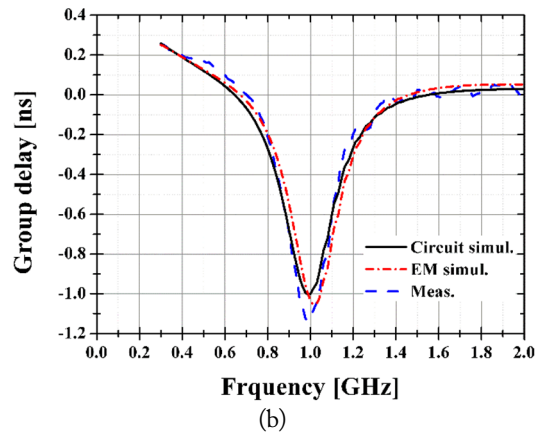
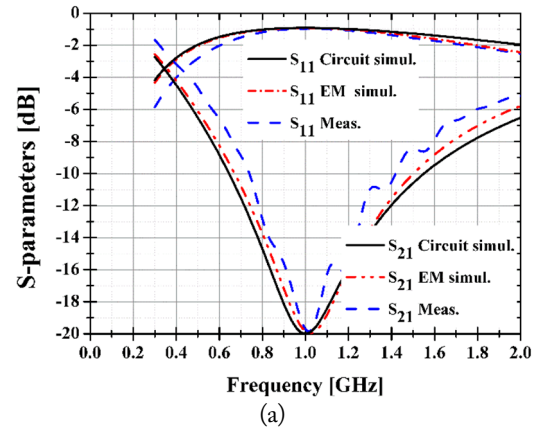


Fig. 10. Circuit-/EM-simulated and measured results of the NGD circuit when  $S_{21}(\omega_0) = -20$  dB and  $\tau(\omega_0) = -1$  ns at 1 GHz. (a)  $S$ -parameters  $S(\omega)$ . (b) Group delay  $\tau(\omega)$ .

### III. CONCLUSION

Then characteristics of NGD circuits are systematically characterized using  $S_{21}(\omega_0)$ ,  $\tau(\omega_0)$ , and bandwidth. Some design examples are provided and analyzed in the time and frequency domains. The relations among  $S_{21}(\omega_0)$ ,  $\tau(\omega_0)$ , and the group delay bandwidth are explained using closed-form expressions. The circuit-/EM-simulated and the measured  $S$ -parameters and group delays are all shown to be in good agreement. The presented NGDC design methods may be useful for many applications, such as filters, feed-forward amplifiers, array antennas, and non-Foster reactive elements, among others.

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