# Buckling behavior of steel column with triangularly corrugated web

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**Abstract.** The paper presents a study of behaviour of axially loaded columns that consist of two flanges and a thin triangularly corrugated web, connected by automatic welding. In the literature, the buckling behaviour of steel columns was dealt with mostly for members with plate webs. Researches of that problem for columns with corrugated webs were found out to be very limited. A parametric study is carried out for various column slenderness and corrugation densities. A general-purpose finite element analysis software ABAQUS was used. The corrugation densities adopted in this study represent practical geometries, which are commonly used for such structures in building practice. Plot showing the influence of section slenderness on value of reduction factor for lateral buckling is presented. It is determined that existing buckling curves poorly describe the dependence of the reduction factor on slenderness for axially compressed members with triangularly corrugated webs. Finally, recommendations were proposed for the design of pin-ended columns with corrugated webs at lateral buckling in accordance with numerical results.

### 1 Introduction

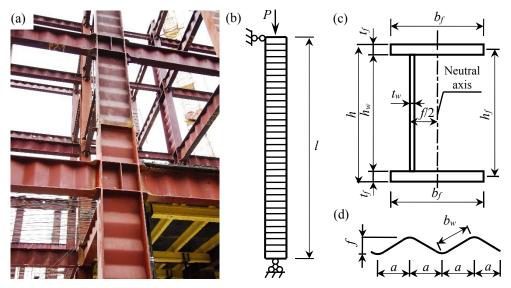
Corrugated webs are often used in building practice to reduce metal consumption and increase the rigidity of the I-sections. Nowadays such structures are generally used as ceiling girders in multi-story apartment houses, large span roof girders in industrial and administrative buildings, etc. However, from such profiles, it is possible to produce also column compressed elements and the whole building frame – see fig. 1.

In the world practice sections with trapezoidal, sinusoidal and triangular corrugation profiles are most widely used. Triangularly corrugated webs have several advantages over others. For example, they do not require expensive equipment for the production and the webs could be thicker than sinusoidal ones and therefore could resist heavier loads. Through its profiled form, web exhibits enhanced shear stability and therefore eliminate the need for additional transverse stiffeners or thicker web plates. An original feature of I-sections with a corrugated web is the almost complete perception of the bending moment and longitudinal force by the flanges. Due to so-called "accordion effect" [1-3, 7] the normal stresses along the height of the web are significant just in narrow areas near the flanges and insignificant for most of the web height. This situation at first glance reduces

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the load-bearing capacity of the structure at buckling, but on the other hand, such structure can be considered as a lattice column in which corrugated web fulfils the lattice's role and possesses increased stability in the strong plane.



**Fig. 1.** (a) Frame structure of residential building with corrugated web beams and columns; (b) Considered column design scheme; (c) Cross section of column with corrugated web; (d) Geometrical parameters of corrugated web with triangular shaped corrugations.

Lateral buckling problem of compressed members was solved in 1757 by Euler [4]. He derived the theoretical solution for an axial force that a long, slender, ideal bar can carry without buckling. Practical experiments performed by Shanley in 1947 [4] have made a great contribution to the study of the inelastic buckling of columns. It was established that for stocky columns, the strength is governed by plastic "squashing". For inelastic buckling, the value of initial imperfections has the greatest importance what was noted by Calladine in 1973 [5].

Most research studies of structures with corrugated webs are devoted to various aspects of the bending elements and very few studies are devoted to axially compressed members. One of the first was performed by Fraser in 1956 [6]. He studied the interaction between the compressive flange and corrugated webs in multiweb beams, but its topic is similar to the study of columns since both structures involve the interaction between flange and the web when flange is under compression. Aravena and Edlund in 1987 [7] considered the combined effect of axial compression and shear and recommended formula to evaluate influence of axial force on shear capacity of corrugated web. Wang in 2003 [7] performed a series or full-scale tests and finite element analysis of axially compressed columns with tubular flanges and trapezoidally corrugated web.

The present paper deals with the elastic and inelastic buckling behaviour of steel columns with triangularly corrugated webs – see fig. 1. A numerical parametric study was carried out for pin-ended corrugated web columns. Various cases were considered including length, height of the column and the corrugation density expressed as a ratio between height and length of half-wave of corrugation. The software ABAQUS (2017) was used to carry out linear buckling analyses (LBA) and Riks analyses to obtain the elastic and inelastic critical axial forces for columns. Results compared with estimations of the currently available design guidance [3, 8-11].

# 2 Design of triangularly corrugated web steel column

Rules for design of compressed steel members with sinusoidal corrugated webs are given in Russian design code SP 294.1325800.2017 [11]. Design features of triangularly corrugated web columns are given in manual [3]. Since the corrugated web is not supposed to resist axial forces, compressed corrugated web columns are designed considering that only the flanges resist the longitudinal axial force. Thus, for the structure stability, the following condition must be satisfied

$$P \le 2\chi b_f t_f R_{\nu} \gamma_c \,, \tag{1}$$

in which P is applied axial force,  $b_f$  and  $t_f$  are flange width and thickness respectively,  $\chi$  is reduction factor for axial buckling,  $R_y$  is the material yielding strength,  $\gamma_c = 1.0$  is working condition factor specified by [10].

According to Russian design code [10], the value of reduction factor for corrugated web column can be adopted as for the column with a flat web that can be described as

$$\chi_{SP} = 1 \text{ for } \overline{\lambda} < 0.6,$$

$$\chi_{SP} = \pi^2 / \gamma_m \cdot \overline{\lambda}^2 \text{ for } \overline{\lambda} > 4.4 ,$$
 (3)

$$\chi_{SP} = 0.5 \left( \delta - \sqrt{\delta^2 - 39.48 \overline{\lambda}^2} \right) / \overline{\lambda}^2 \text{ for other cases,}$$
(4)

in which  $\delta = 9.87 \left(0.96 + 0.09\overline{\lambda}\right) + \overline{\lambda}^2$ ,  $\overline{\lambda} = l/i_{min} \sqrt{R_y/E}$ , l is a design length of column,  $i_{min}$  is a minimum value between radius of gyration about strong  $i_x = 0.5 \left(h_w + t_f\right)$  and weak  $i_y = 0.289 b_f$  axis of corrugated web section,  $\gamma_m = 1.3$  is a safety factor for elastic buckling.

It will be seen that expression (2) corresponds to the material yielding strength whereas expression (3) represents Euler's formula for elastic buckling and expression (4) represents case of inelastic buckling. The last one formula is obtained taking into account initial bow imperfections of member that can be expressed as

$$e_{SP} = i_{min}/20 + l/750 \ . {5}$$

Unfortunately, in European EN 1993-1-5 [9] are given recommendations only for corrugated web beams and not specified any recommendations for columns with corrugated web, but it can be possible to obtain reduction factor for corrugated web column as

$$\chi_{EN} = 1 \text{ for } \overline{\lambda}_{EN} \le 0.2,$$
(6)

$$\chi_{EN} = \frac{1}{\Phi + \sqrt{\Phi^2 - \overline{\lambda}_{EN}^2}} \text{ for other cases,}$$
 (7)

in which  $\,\Phi=0.5\Big\lceil 1+0.49\Big(\overline{\lambda}_{\it EN}-0.2\Big)+\overline{\lambda}_{\it EN}^2\,\Big\rceil$  ,  $\,\lambda_{\it EN}=\overline{\lambda}/\pi$  .

The upper formulas (6) and (7) were obtained with initial bow imperfections equal to

$$e_{EN} = l/150$$
. (8)

Axial buckling curves described by the different design codes are shown in fig. 3.

## 3 Numerical parametric study

Typical finite element (FE) model adopted for the study is shown in fig. 2a. Models are composed of upper and lower flanges with thickness 10mm and width 200 mm and corrugated web with thickness 4mm and height of 600mm, 400mm and 200mm for different cases. Also, in the models were added transverse stiffeners with thickness 30mm at both ends of the column. For the webs were assumed two different corrugation densities f/a = 50 mm/100 mm and f/a = 70 mm/200 mm that represent practical geometries, which are commonly used for such structures in building practice [3].

At numerical study were considered four different length of column l equal to 4m, 6m, 8m and 10m. All models were loaded by point axial force  $P = 1 \mathrm{kN}$  located at one end of the column at the cross-section centre line. Boundary conditions were applied to either end of the column models by restraining appropriate degrees of freedom to simulate the pinned supported condition. An elastic-perfectly plastic material model was assumed with a yield strength value of 240MPa, modulus of elasticity  $E = 206000 \mathrm{MPa}$  and Poisson's ratio 0.3.

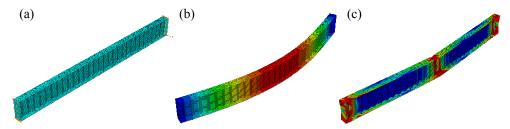


Fig. 2. (a) FE model of triangularly corrugated web column adopted for analysis; (b) Example of the global elastic buckling mode; (c) Deformed shape of structure at ultimate load

# 4 Results of the parametric study

In this work numerical parametric study was performed at two stages.

At the first stage, all models were assumed to elastic buckle under perfect conditions without any initial imperfections. Overall view of the global buckling mode that was obtained from lateral buckling analysis is shown in fig. 2b. To calculate the critical elastic buckling load  $P_{cr}$ , the load factors from the eigenvalue's analysis were multiplied by the applied load. In this case reduction factor for elastic axial buckling can be obtained as

$$\chi_{el} = P_{cr}/2R_{\nu}b_{f}t_{f}\gamma_{m} . \tag{9}$$

At the next stage the non-linear response and ultimate strength of the models including initial imperfection and nonlinear geometrical effects were examined through FEA by Riks method realized in ABAQUS (2017). This method uses the load magnitude as an additional unknown and solves simultaneously for loads and displacements. The solution is obtained as a series of increments, with iterations to obtain equilibrium within each increment. Deformed shape after the attainment of ultimate load is shown in fig. 2c. Such approach allows determinate reduction factor for inelastic buckling as follows

$$\chi_{pl} = P_{ult}/2R_{\nu}b_{f}t_{f} , \qquad (10)$$

in which  $P_{ult}$  is ultimate axial force for column obtained from FEA.

Considering that by different design codes initial bow imperfection is described by various equations the ultimate strength analysis was performed twice for each value of

imperfections and were got two values of the ultimate force  $P_{ult1}$  and  $P_{ult2}$  for initial imperfection determined by formulas (5) and (8) respectively. FEA results and the values of the reduction factors are given in Table 1 and Table 2 for various corrugation densities.

**Table 1.** FEA results and reduction factors for columns with corrugation density f/a = 50 mm/100 mm

Model	$P_{cr}$ , kN	χel	$P_{ult1}$ , kN	Xpl1	χsp	$P_{ult2}$ , kN	Xpl2	χEN
$l=4$ , $h_{\rm w}=0.2$	1672.2	1.340	750.24	0.781		641.17	0.668	
$l=4, h_{\rm w}=0.4$	1668.7	1.337	847.06	0.882	0.767	750.10	0.781	0.693
$l=4$ , $h_{\rm w}=0.6$	1670.2	1.338	836.94	0.872		740.54	0.771	
$l=6, h_{\rm w}=0.2$	745.53	0.597	592.80	0.618		433.42	0.451	
$l=6, h_{\rm w}=0.4$	744.89	0.597	619.36	0.645	0.534	467.78	0.487	0.470
$l=6, h_{\rm w}=0.6$	745.38	0.597	589.55	0.614		470.34	0.490	
$l=8, h_{\rm w}=0.2$	420.65	0.337	384.25	0.400		333.23	0.347	
$l=8, h_{\rm w}=0.4$	420.41	0.337	448.23	0.467	0.341	354.78	0.370	0.314
$l=8, h_{\rm w}=0.6$	420.67	0.337	454.54	0.473		360.22	0.375	
$l=10, h_{\rm w}=0.2$	269.19	0.216	294.30	0.307		261.71	0.273	
$l=10, h_{\rm w}=0.4$	269.08	0.216	338.31	0.352	0.218	278.70	0.290	0.218
$l=10, h_{\rm w}=0.6$	269.23	0.216	351.10	0.366		285.19	0.297	

Analyzing the data can be noted that for the relatively slender columns with lengths 8m and 10m the minimum obtained values of reduction factors corresponds to the elastic buckling predicting by Euler's theory. For the relatively rigid columns with lengths 4m and 6m, the minimum obtained values of reduction factors correspond to the inelastic buckling mode. In other words, columns with corrugated webs behave like an ordinary column with a flat web, but the first one has a greater load capacity due to obtained reduction factors are greater for most cases up to 30% compared with the flat web columns of the same slenderness. As can be seen from the presented data the corrugation density weakly affects the buckling performance of the structure and values of the reduction factors for two types of corrugation looks almost similar.

**Table 2.** FEA results and reduction factors for columns with corrugation density f/a = 70mm/200mm

Model	$P_{cr}$ , kN	χel	$P_{ult1}$ , kN	Xpl1	χsp	$P_{ult2}$ , kN	Xpl2	χεN
$l=4$ , $h_{\rm w}=0.2$	1675.4	1.342	755.97	0.787		646.37	0.673	
$l=4$ , $h_{\rm w}=0.4$	1661.6	1.331	862.96	0.899	0.767	762.94	0.795	0.693
$l=4, h_{\rm w}=0.6$	1663.9	1.333	915.18	0.953		881.89	0.919	
$l=6, h_{\rm w}=0.2$	744.51	0.597	559.56	0.583		495.97	0.517	
$l=6, h_{\rm w}=0.4$	743.71	0.596	522.70	0.544	0.534	540.34	0.563	0.470
$l=6, h_{\rm w}=0.6$	744.3	0.596	577.18	0.601		611.57	0.637	
$l=8, h_{\rm w}=0.2$	419.12	0.336	415.80	0.433		387.72	0.404	
$l=8, h_{\rm w}=0.4$	418.79	0.336	453.61	0.473	0.341	426.87	0.445	0.314
$l=8, h_{\rm w}=0.6$	419.06	0.336	421.07	0.439		447.11	0.466	
$l=10, h_{\rm w}=0.2$	268.66	0.215	326.62	0.340		304.31	0.317	
$l=10, h_{\rm w}=0.4$	268.5	0.215	360.60	0.376	0.218	340.78	0.355	0.218
$l=10, h_{\rm w}=0.6$	268.64	0.215	382.10	0.398		353.76	0.369	

1.4  $\chi_{el}$  for  $f/a = 50/1\overline{00}$ Elastic buckling  $\chi_{pl1}$  for f/a = 50/1001.2 REDUCTION FACTOR  $\chi_{p/2}$  for f/a = 50/1001  $\chi_{el} \text{ for } f/a = 70/200$  $\chi_{pl1}$  for f/a = 70/2000.8  $\chi_{pl2}$  for f/a = 70/2000.6 According SP 16.13330.2017 [10] 0.4 According EN 1993-1-1 [8] 0.2 0

Generalizing the results, in fig. 3 is given a graph shows the dependence of the values of reduction factors on the non-dimensional slenderness of member.

2 Fig. 3. Buckling curves for axial compressed column and results of FEA.

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## **5 Conclusions**

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According to the results of the performed work, it is shown that European [8, 9] and Russian [10, 11] design codes are not perfect in evaluation of load carrying capacity for axial compressed members with triangularly corrugated web. So, for practical design procedure, it is recommended to calculate reduction factor for columns with corrugated web according to the existing design codes in the same way like for the flat web columns neglecting the influence of corrugated web on cross sections parameters.

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Surely the buckling performance of such structures requires further investigation considering the influence of various boundary conditions, potential eccentricity of the applied load, imperfections in corrugated web and its alignment relative the flanges.

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