Quantum oscillations near the metamagnetic transition in Sr₃Ru₂O₇

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We report a detailed investigation of quantum oscillations in Sr₃Ru₂O₇, observed inductively (the de Haasvan Alphen effect) and thermally (the magnetocaloric effect). Working at fields from 3 to 18 T allowed us to straddle the metamagnetic transition region and probe the low- and high-field Fermi liquids. The observed frequencies are strongly field dependent in the vicinity of the metamagnetic transition, and there is evidence for magnetic breakdown. We also present the results of a comprehensive rotation study. The most surprising result concerns the field dependence of the measured quasiparticle masses. Contrary to conclusions previously drawn by some of us as a result of a study performed with a much poorer signal-to-noise ratio, none of the five Fermi-surface branches for which we have good field-dependent data gives evidence for a strong-field dependence of the mass. The implications of these experimental findings are discussed.

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I. INTRODUCTION

Quantum criticality is a topic of continued interest in condensed-matter physics.¹ Quantum critical points (QCPs) have been found in various metallic systems, notably heavy fermion intermetallics and transition-metal oxides, using tuning parameters such as hydrostatic pressure, chemical doping, or magnetic field. They are usually accompanied by a significant enhancement of the low-temperature electronic specific heat, which is thought to stem from a quasiparticle mass renormalization due to strong quantum fluctuations associated with the continuous phase transition.²

QCPs have been studied by a large variety of methods but surprisingly little is known about the microscopic nature of the processes involved. In particular, it is not clear if, in a multiband system, the quasiparticles from all the bands will experience mass renormalization. The method of choice to determine electronic properties in *k*-space has traditionally been the study of quantum oscillation measurements, which allow, in principle, the determination of the full Fermi surface and the associated quasiparticle masses,³ and can be studied over a wide range of magnetic fields.

The subject of this paper, Sr₃Ru₂O₇, gives an opportunity to probe the nature of quasiparticle mass enhancement in the vicinity of quantum criticality. It features a first-order metamagnetic transition which terminates in a critical point.⁴ The depression of its critical temperature towards 0 K using a tilted magnetic field leads to a QCP, situated near 7.9 T when the field is aligned with the crystalline *c*-axis.^{4,5} Anomalous power laws in the resistivity were observed in its vicinity, typical of quantum critical systems.⁴ A pronounced enhancement of the specific heat was reported near the QCP, with a

logarithmic divergence of C/T at fields near the critical field.⁶ Moreover, a previous de Haas–van Alphen (dHvA) study revealed the existence of at least five different electronic bands, of moderately high quasiparticle mass, two of which were reported to become enhanced when approaching the QCP with a magnetic field.⁷ Away from the critical region, these masses were confirmed in an angular-resolved photoemission spectroscopy (ARPES) study by Tamai $et\ al.^8$

In ultrapure crystals, the approach to the QCP is signaled by a strong enhancement in the low-temperature specific heat⁹ which is cut off by the formation of a new phase, within which transport properties develop a strong anisotropy under the application of tiny in-plane magnetic fields. ¹⁰ In a recent letter, we reported the observation of the dHvA effect inside this anomalous phase and demonstrated the importance of a chemical-potential shift in determining the field dependence of the dHvA frequencies. ¹¹

In this paper, we report a thorough investigation of quantum oscillations in Sr₃Ru₂O₇ through the critical region. Performing this experiment required the growth of a new generation of crystals, screened in a series of dHvA measurements in order to obtain the highest dHvA signal amplitude. Mean-free paths of up to approximately 300 nm were measured, which enabled the detection of the dHvA effect down to fields as low as 2.4 T, as well as the observation of entropy oscillations using the magnetocaloric effect. We present here a detailed study of the quasiparticle masses of five out of six of the known bands as a function of the tuning parameter, the magnetic field. For each of these five bands, no significant increase in quasiparticle mass was detected. These results contrast with previous dHvA measurements by some of us, and so we explain the origin of this discrepancy in depth. We furthermore report measurements of the field and angle dependence of the measured dHvA frequencies. The implications of these results are discussed.

II. FERMI SURFACE

The determination of the electronic structure in $Sr_3Ru_2O_7$ is not a simple problem, and has not yet been completely solved experimentally. It is a complex system partly due to the high degree of electronic correlations, and partly due to Fermi-surface (FS) reconstructions arising from lattice distortions. To introduce the relevant issues, we first show the relationship between the $Sr_3Ru_2O_7$ Fermi surface and the simpler one of its single layer relative Sr_2RuO_4 .

 $\rm Sr_2RuO_4$ possesses a body-centered tetragonal crystal structure, of space-group symmetry $\rm \it I4/mmm.^{12}$ Consequently, it has fourfold rotational and inversion symmetry. Early work on $\rm Sr_3Ru_2O_7$ reported that it possessed the same space group $\rm ^{13}$ but it was later found using neutron diffraction that this symmetry is broken by a 7° rotation of the RuO octahedra. $\rm ^{14,15}$ The resulting space group is $\it Bbcb$, corresponding to a $\it B$ centered orthorhombic structure with the $\it a$ and $\it b$ of sides being effectively $\rm \sqrt{2}$ larger than those of the undistorted crystal. This rotation of the octahedra has a significant effect on the electronic system. $\rm ^{16}$

The FS in Sr₃Ru₂O₇ can be derived schematically without involving band-structure calculations, as shown in Fig. 1. One starts from the FS in Sr_2RuO_4 , where three bands, α , β , and γ , are present. These originate from the hybridization of the various d bands of the Ru atoms, the d_{xz} , d_{yz} , and d_{xy} , which, due to crystal-field splitting, are the ones crossing the Fermi level. The d_{xz} and d_{yz} give rise to only weak dispersion either in the z and, respectively, y and x directions, due to quasi-one-dimensional hopping. Consequently, the Fermi surface corresponding to these bands should be close to planar in the $k_x k_z$ and $k_y k_z$ directions. These cross in certain regions of the Brillouin zone (BZ), where hybridization gaps appear, and the sheets reconnect into closed surfaces and produce the α and β bands [Fig. 1(a)]. The d_{xy} orbital, however, allows hopping in both the x and y directions, and the corresponding Fermi surface is close to a perfect circle in the $k_x k_y$ plane, the γ band. The resulting FS with all bands is shown in Fig. 1(b). This construction is consistent with the fourfold rotation symmetry of the I4/mmm space group.

In Sr₃Ru₂O₇, one expects each band to duplicate, due to bilayer splitting.¹⁷ Consequently, the result is slightly different than for Sr₂RuO₄. One starts from six surfaces [Fig. 1(c)], four that originate from the d_{xz} and d_{yz} orbitals, which reconnect at the points of crossing, and one should obtain a result similar to that shown in Fig. 1(d). This is what the FS would be without the $\sqrt{2} \times \sqrt{2}$ reconstruction due to the octahedral rotation. But since the BZ reconstructs into a square of half the area, backfolding of the bands occurs, shown in Fig. 1(e). In this plot, many band crossings appear, and the way in which the surfaces reconnect is complex. According to dHvA and ARPES experiments, 7,8 six orbits are expected, shown in Fig. 1(f). These take the form of square and crossshaped hole pockets in the center, originating from the d_{xz} and d_{yz} orbitals, two lens-shaped electron pockets at the M point, resulting from hybridization between d_{xy} and d_{xz} , d_{yz} ,

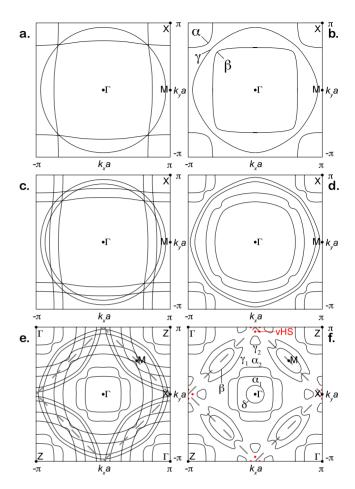


FIG. 1. (Color online) Schematic construction of the Fermi surface of Sr_2RuO_4 , a and b, and of $Sr_3Ru_2O_7$, c, d, e, and f, where in the last two, the $\sqrt{2} \times \sqrt{2}$ reconstruction of the BZ accompanied by backfolding was included, and the new BZ is represented by the dashed diamond. All axes were scaled by the parameters of the undistorted lattice. The red dots represent the location of a putative Van Hove singularity.

and a small pocket near the X point. These were labeled, respectively, α_1 , α_2 , γ_1 , β , and γ_2 [see Fig. 1(f)]. Finally, there is a small circular pocket centered on Γ , labeled δ , that has no direct analogy in $\mathrm{Sr_2RuO_4}$. It has strong Ru $d_{x^2-y^2}$ character, and results from the depression in energy of a band that is unfilled in $\mathrm{Sr_2RuO_4}$ due to the lower symmetry of $\mathrm{Sr_3Ru_2O_7}$. ¹⁶

III. EXPERIMENT

Sr₃Ru₂O₇ crystals were produced using a floating-zone image furnace, using the method published by Perry and Maeno. ¹⁸ Ten crystal rods were grown, from which more than 50 individual samples were cut. Each was nearly cylindrical, 2 mm in diameter and 3 mm long, with the crystalline *c*-axis along the principal axis. These were the subject of a series of characterization experiments, which enabled us to select the best four to use in these experiments, according to two criteria: disorder, due to vacancies and impurities, and phase purity, affected by the appearance of intergrowth re-

TABLE I. Electronic data for all six bands observed in $Sr_3Ru_2O_7$. The type refers to whether bands are electron-like (e) or hole-like (h) and the multiplicity refers to possible bilayer splitting times its number of occurrences inside the BZ. F is the dHvA frequency, the number of electrons refers to the fraction of the BZ area covered by a band, which includes the multiplicity. Finally, m^*/m_e is the quasiparticle mass and γ_{el} is the associated contribution to the electronic specific-heat coefficient, including the multiplicity. Note that the data originates from the low field side of the metamagnetic transition.

Label	Туре	Mult.	<i>F</i> (kT)	Electrons	m^*/m_e	$\gamma_{el.}$ mJ/mol Ru K ²
γ_2	h	8	0.11	4-0.128	8 ± 1	47 ± 6
β	e	2	0.15	0.044	5.6 ± 0.3	8.3 ± 0.4
δ	e	2	0.43	0.126	8.4 ± 0.7	12 ± 1
γ_1	e	4	0.91	0.532	7.7 ± 0.3	23 ± 1
α_1	h	1	1.78	2-0.260	6.9 ± 0.1	5.1 ± 0.1
α_2	h	1	4.13	2-0.602	10.1 ± 0.1	7.5 ± 0.1
Filled	e	8	13.7	8		
Total				15.71		103 ± 8

gions with $n \neq 2$ consecutive RuO planes (SrRuO₃, Sr₂RuO₄, Sr₄Ru₃O₁₀, etc.).

Low disorder crystals were selected in a two-step process in which preliminary residual resistivity measurements were followed by short dHvA experiments performed in an adiabatic demagnetization refrigerator. This featured the use of first-harmonic detection, a dc field between 6 and 7 T and a temperature of 250 mK. The samples selected for the main experiments were those showing the largest amplitude of the 1.78 kT frequency (see Table I).

In order to determine impurity phase volume fractions, we used the magnetic properties of the competing phases: superconductivity below 1.5 K (n=1, Sr_2RuO_4), ¹² ferromagnetism below 160 K ($n=\infty$, SrRuO₃), ¹⁹⁻²¹ and ferromagnetism below 105 K $(n=3, Sr_4Ru_3O_{10})^{.22}$ Since $Sr_3Ru_2O_7$ is paramagnetic²³ and produces only a small signal in susceptibility and magnetization experiments, these properties were easily detected quantitatively for small amounts using zerofield ac susceptibility (superconductivity) and magnetization measurements using a Quantum Design Magnetic Property Measurement System (MPMS) superconducting quantum interference device magnetometer (ferromagnetism). The samples used in the quantum oscillation experiments featured residual resistivities typically of less than 0.4 $\mu\Omega$ cm, and impurity phase volume fractions of a few percent or less for Sr₂RuO₄ and 0.1% for SrRuO₃ and Sr₄Ru₃O₁₀.

The de Haas–van Alphen effect was measured using a dilution refrigerator located in the Cavendish Laboratory in Cambridge, equipped with an 18 T superconducting magnet. The samples were placed in well-compensated coil pairs, each comprising 1000 turns of 25-μm-diameter Cu wire. These were placed onto a rotation mechanism which allowed the measurement of the magnetic susceptibility at angles between the field and the crystalline *c*-axis of up to about 60°, both along the [100] and [110] directions. The coil pairs were connected to the input coils of low-temperature transformers, which were themselves coupled with room-temperature preamplifiers. The magnetic susceptibility was measured using first- and second-harmonic detection, with digital lock-in amplifiers and an excitation field of 20 G at 7.9 Hz. These

values for the modulation field were chosen in order to ensure that eddy current heating in the samples was negligible. They were selected following an extensive study which demonstrated both that the measured masses were independent of modulation fields up to this level, and that, under the conditions selected for the experiments on $\rm Sr_3Ru_2O_7$, the well-known masses of all sheets of $\rm Sr_2RuO_4$ were obtained correctly. The noise floor at the compensated coils was of around 30 pV rms/ $\sqrt{\rm Hz}$, when using an analog magnet discharge field sweep method, and 150 pV rms/ $\sqrt{\rm Hz}$ when using linear field sweeps.

For the majority of the measurements presented here, second-harmonic detection was employed in order to minimize the effects of the large magnetic background near the metamagnetic transition. A series of sweeps was performed between 18 and 2.5 T, at rates of approximately 0.04 T/min for B > 10 T and 0.02 T/min for lower fields. These were carried out at ten different temperatures between 90 and 500 mK with the field aligned with the crystalline c axis, and then at angles from -15° to 55° using a step of about 1.6° , at a temperature of approximately 55 mK. For one aspect of the data set, the field dependence of very low dHvA frequencies at low fields, we performed additional measurements. Oscillations were studied in St Andrews using the magnetocaloric effect in which the sample temperature is monitored while the field is swept. The relaxation times associated with this kind of measurement favor low frequencies over higher ones. To follow those up with dHvA, we worked with firstharmonic detection, maximizing the low-frequency signal at the expense of a large magnetic background which restricted the experiment to fields below 7 T.

IV. dHvA DATA, SPECTRA, AND QUASIPARTICLE MASSES

In Fig. 2, we present susceptibility data between 3 and 18 T and the dHvA spectrum of data between 5 and 6.5 T. The top panel shows that dHvA oscillations can be detected throughout the available field range. Three metamagnetic

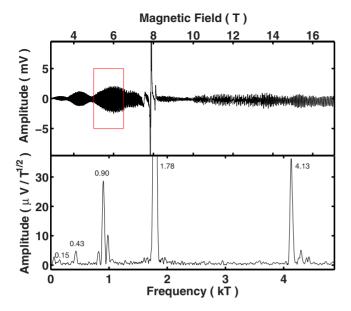


FIG. 2. (Color online) Top panel: typical second-harmonic dHvA oscillations measured with B||c-axis, at a temperature of 55 mK [see Mercure *et al.* for a discussion of the thermometry in this system (Ref. 11)]. Bottom panel: Fourier transform of the data in the top panel between 5 and 6.5 T (shown as a red square). Five frequencies were observed, at 0.15, 0.43, 0.90, 1.78, and 4.13 kT.

signatures can be seen near 8 T, which consist of asymmetric peaks centered at 7.5, 7.9, and 8.1 T. The first corresponds to a metamagnetic crossover and the second to two first-order transitions, as determined using the out-of-phase component of the first-harmonic ac susceptibility (not shown).⁵ The region between 7.9 and 8.1 T corresponds to the anomalous phase discussed by Borzi et al. 10 and our recent work in which we reported dHvA oscillations. 11,24 The dHvA spectrum shown in the lower panel of Fig. 2 features five peaks, situated at 0.15, 0.43, 0.90, 1.78, and 4.13 kT. In previous ARPES work by some of us,8 we associated these with bands labeled, respectively, β , δ , γ_1 , α_1 , and α_2 , where the first three correspond to electron orbits and the last two to hole orbits. A sixth frequency also exists at 110 T, as will be discussed in Sec. V. Note that the splitting of the peak at 0.9 kT into four peaks is associated with bilayer splitting of this band, as well as to a normal corrugation of this branch of the FS while the splitting of the peak at 4.13 kT is due to magnetic breakdown, as detailed in Sec. VI.

Taking into consideration all the bands reported, the ARPES map of the BZ and the predicted multiplicity and bilayer splitting of these bands, we were able to put forward a model which allowed us to perform the Luttinger sum and account for the total electronic specific-heat coefficient in Sr₃Ru₂O₇, which was reported by Ikeda *et al.* as 110 mJ/mol Ru K².²³ It involves assigning multiplicities to bands and determining whether they are electronlike or hole-like. Table I shows a summary of this model, along with the dHvA frequencies of the six bands, the associated number of electrons which occupy these, their associated quasiparticle masses, and their contribution to the total specific heat. The number of electrons was calculated by normalizing the dHvA frequencies by that corresponding to the in-plane area

of the BZ, 13.7 kT, multiplied by the multiplicity of the bands, and taking into account the spins. For holelike bands, these are expressed as the number of filled zones minus the fraction of electrons covered by these bands. The contributions to the specific heat were calculated using the quasiparticle masses, times the multiplicity, and a conversion factor of 0.74 mJ/mol Ru K^2 . Moreover, a number of electrons are included in zones that become filled in the process of the backfolding of the bands, which accounts for eight electrons. The total number of electrons counted in this way nearly matches the required amount, 15.71 compared to 16 electrons while the calculated specific heat is consistent with that measured previously, 103 ± 8 compared to 110 mJ/mol Ru K^2 .

V. MAGNETOTHERMAL DETECTION OF LOW FIELD, HIGH MASS OSCILLATIONS

One of the predictions of the ARPES work of Tamai et al. was the possible existence of tiny Fermi-surface sheets associated with extremely flat bands that they labeled γ_2 . Observing tiny frequencies against the background of many other oscillatory components is not easy, especially since the flatness of the bands means that for any given field range, the signal size is likely to be suppressed relative to that of other components of the overall signal. This effect is exacerbated when working with second-harmonic dHvA in which relative signals for low frequencies go as F^2 . In order to search for the oscillations, we profited from bespoke equipment developed in St. Andrews for the study of the magnetocaloric effect. In contrast to second-harmonic dHvA, the relative signal size will be independent of F, in principle, but subject to a damping factor that will grow rapidly with F since more rapid oscillations will be damped more strongly in a measurement system with long intrinsic relaxation times.

In Fig. 3(a), we show low-frequency oscillations detected by the magnetocaloric effect for up and down sweeps of the field in red and blue, respectively. The sign reversal of the temperature change is a key diagnostic that these are genuine magnetothermal oscillations. If, for example, they were due to sample heating due to eddy currents subject to the Shubnikov-de Haas effect, they would have a sign independent of field sweep direction. Their Fourier transformation is shown in the black trace in Fig. 3(b). The previously undiscovered peak at 110 T is shaded. In the same panel, the green trace shows the Fourier spectrum of a subsequent dHvA run taking data on the first harmonic with a modulation field of 3 G. While confirming the existence of the 110 T peak, it emphasizes the relative signal enhancement that magnetocaloric oscillations can provide for very low-frequency signals.

An important aspect of magnetocaloric oscillations is that the amplitude of the signal is proportional to dM/dT rather than to M directly³ so the temperature dependence expected of the oscillations is that of the first temperature derivative of the usual Lifshitz-Kosevich (LK) form [see Eq. (1) below]. This is shown in red in Fig. 3(c) which shows the result of a "control" experiment detecting magnetocaloric oscillations from the well-known α sheet of Sr_2RuO_4 . In spite of the different temperature dependence of the raw signal, the mass

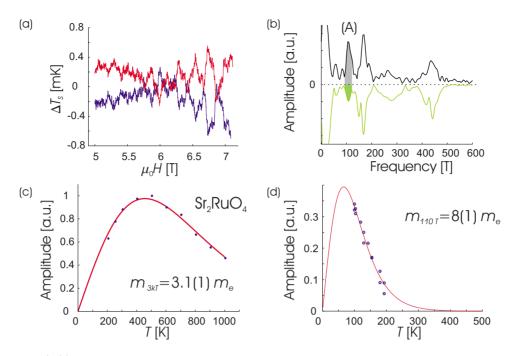


FIG. 3. (Color online) (a) The change in sample temperature T_S during a sweep of the magnetic field at 0.04 T/min (blue) and -0.04 T/min (red) as a function of magnetic field μ_0H . The average sample temperature is 160 mK. (b) Fourier transform in $1/\mu_0H$ of the blue trace in panel (a). In green is given the Fourier transform of a dHvA measurement using first harmonic detection over a comparable magnetic field region at base temperature. The label (A) indicates the new frequency found at 110 T. (c) Temperature dependence of the amplitude of the 3 kT frequency of Sr_2RuO_4 as measured by magnetothermal oscillations. The red curve is a fit of the temperature derivative of the Lifshitz-Kosevich formula to the data. (d) Amplitude of the 110 T peak in the Fourier transform of the data in panel (a) as a function of sample temperature T_S . The red curve is a fit of the temperature derivative of the Lifshitz-Kosevich function to the data. This fit gives a mass m_{110} T for the newly observed frequency of $8(1)m_e$.

deduced agrees well with that obtained by standard dHvA, providing a useful verification of the calibration of the magnetocaloric apparatus.

In Fig. 3(d), we show the temperature dependence of the magnetocaloric signal of the new frequency at 110 T, along with the fit that allows an effective-mass estimate of $8m_e \pm 1m_e$. A subsequent first-harmonic dHvA study involving careful signal averaging increased the precision of the measurement to $7.2m_e \pm 0.2m_e$. This mass corresponds to a Fermi velocity of only 9 km s⁻¹, a factor of 6 smaller than that of the γ sheet of Sr_2RuO_4 .

VI. FIELD DEPENDENCE OF dHVA FREQUENCIES AND POSSIBLE MAGNETIC BREAKDOWN

As was already suggested by Borzi *et al.*,⁷ and described in more detail in our recent work,¹¹ the dHvA frequencies are not constant along the field range but change as the system crosses the metamagnetic transition. Variations are observed as one increases the magnetic field and are especially significant above 7 T.

In Fig. 4, we present an analysis of the field dependence of the dHvA frequencies along the field range. It was calculated using multiple Fourier transforms taken over short field ranges of equal inverse field width. 100 such windows were used, of width of 0.02 T⁻¹, which overlap and are distributed evenly in inverse field space.²⁶ The intensity of each spectrum calculated is plotted on a color scale. The hidden cen-

tral area corresponds to the metamagnetic region, where a large nonoscillatory signal arises (see Fig. 2 near 8 T). We have recently succeeded in detecting a tiny oscillatory signal on top of the large background, as reported in Ref. 11.

On the low-field side of the metamagnetic transition, the same five dHvA frequencies are observed as in Fig. 2 (excluding γ_2). However, near 7 T, increases are observed, par-

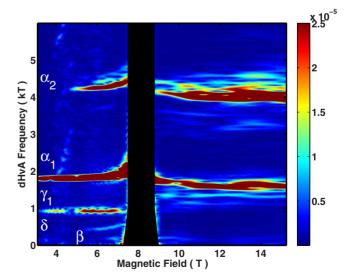


FIG. 4. (Color online) Field dependence of the dHvA spectra observed with the field aligned with the direction of the c-axis. The color scale corresponds to the amplitude of the spectrum.

ticularly with the 1.78 and 4.13 kT frequencies, which correspond to the α_1 and α_2 bands. This is discussed in detail in Ref. 11, and corresponds to a change in the size of these parts of the FS, due to a change in Fermi level. Note that the fact that the α_1 and α_2 bands remain of similar size in high fields compared to low fields excludes any further $\sqrt{2} \times \sqrt{2}$ reconstruction of the FS at the metamagnetic transition.

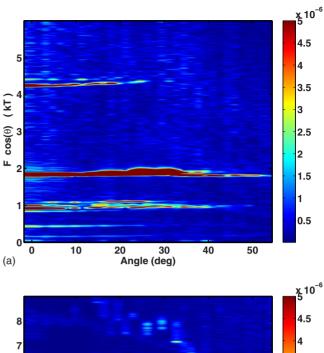
One can also observe in Fig. 4 that the data become more complex as the magnetic field increases, and that most dHvA peaks split into several components. The new frequencies might originate from magnetic breakdown, activated as the field increases. In particular, for the case of α_2 [see Fig. 1(f)], symmetry considerations allow four magnetic breakdown regions with the γ_1 pocket, which increase the cross-sectional area by small amounts. This leads to a large number of possibilities, each new orbit occurring with a slightly different probability. In such a case, the amplitude of the dHvA signal becomes divided between a large number of possible frequencies all situated near 4 kT. The same reasoning holds with the α_1 pocket, from which the electrons can tunnel toward the α_2 pocket and back in four different locations, leading to a similar number of possibilities.

It is difficult to explore this in any more detail since the topography of the Fermi surface obviously changes slightly across the metamagnetic transition and is not known above 8 T. It is thus impossible to know the magnetic breakdown field values precisely. We note however that, as can be seen in Fig. 4, the frequency splitting that we associate with magnetic breakdown appears at fields lower than that of the metamagnetic transition, with the 4.1 kT peak splitting into three or more between 6 T and the metamagnetic transition. This suggests that the breakdown and the metamagnetism are not directly related.²⁷

VII. ANGLE DEPENDENCE OF dHvA FREQUENCIES

Measurements of the angle dependence of the dHvA signal allow one, in principle, to determine the three dimensional topography of the FS. In quasi-two-dimensional materials, orbits are open in the k_7 direction, and the frequencies follow a simple angular dependence of the form $F(\theta)$ $=F_0/\cos\theta$, where F_0 is the frequency when the field is aligned with the c-axis direction. ²⁸ This is observed in the case of Sr₃Ru₂O₇, for fields lower than that of the metamagnetic transition. Figure 5, top panel, presents Fourier transforms of the data between 5 and 6.5 T measured at angles between 0° and 54°, plotted with the frequency multiplied by $\cos(\theta)$, such that cylindrical FS pockets appear as horizontal lines. The amplitude of the spectra are represented in color in vertical strips for each angle. All of the FS pockets observed follow almost perfectly the expected behavior for a 2D system, and small deviations are due to their small warping.²⁹ This agrees well with the predictions made by band-structure calculations.8,30

The situation is not quite the same at fields above that of the metamagnetic transition. We found that frequencies are not continuous functions of angle; some of them appear while others vanish at specific angles. In particular, the frequency at 1.6 kT, related with the α_1 pocket, disappears be-



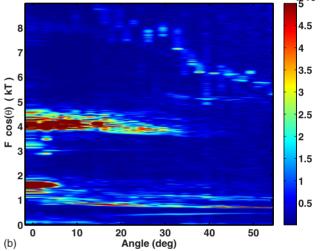


FIG. 5. (Color online) Top panel: angular dependence of the dHvA spectra observed in the low-field side of the metamagnetic transition, where the color represents the spectral intensity while the horizontal and vertical axes represent the angle and the dHvA frequency multiplied by $\cos(\theta)$, respectively. Fourier transforms were taken between 5 and 6.5 T. Bottom panel: angular dependence of the spectra in the high-field side of the metamagnetic transition. Fourier transforms were taken between 10 and 18 T.

tween 5° and 10° while that at $1.0 \, kT$, probably related to the γ_1 pocket, is not present for $B \parallel c$ axis and appears at a similar angle. We observed a similar behavior with the frequency near $0.43 \, kT$, which appears near 20° . Finally, frequencies near $3 \, kT$ appear briefly at low angles. These phenomena may also be related to the magnetic breakdown effects mentioned earlier. Effectively, when a two-dimensional FS possesses small corrugations, magnetic breakdown fields can vary as the field angle is changed, due to a changing k-space distance between FS pockets. If such a distance decreases significantly, magnetic breakdown becomes overwhelmingly probable, to the extent that the original orbit becomes less probable, and may escape detection. Varying magnetic breakdown gaps might therefore make the angle dependence of dHvA frequencies appear as if the FS changed topology

with angle while no such changes occur in reality.

VIII. QUASIPARTICLE MASSES

The enhancement of the specific heat previously reported near the metamagnetic transition is expected, in a metal, to be reflected in the quasiparticle masses measured from quantum oscillations.⁶ Borzi et al. reported strong enhancements of the quasiparticle mass of the α_1 and α_2 bands, below and above the metamagnetic transition.7 It was moreover expected that, although not possible to determine at the time, the masses of the other bands should be enhanced as well, stemming from quantum critical fluctuations coupling to the whole Fermi sea. Indeed, the desire to confirm and extend the findings of Ref. 7 was the main factor motivating this study using samples and detection methods designed to deliver an improved signal-to-noise ratio. To our surprise, we did not reproduce our previous findings. In contrast, we demonstrate here that no such enhancement occurs for the five bands which we detected in second-harmonic dHvA; α_1 , α_2 , δ , γ_1 , and β [see Fig. 1(f)]. We furthermore show that the data analysis method used by us in Ref. 7 to calculate quasiparticle masses can lead to erroneous results if used with data of low signal-to-noise ratio, as we discuss in detail in the Appendix.

In Fig. 6, we present the field dependence of the quasiparticle masses of the dHvA frequencies at, in order from top to bottom, 0.15, 0.43, 0.90, 1.78, and 4.13 kT, which correspond, respectively, to β , δ , γ_1 , α_1 , and α_2 (excluding γ_2), using a magnetic field aligned with the crystalline c axis. The field-dependent masses were calculated using 100 field windows of equal inverse field width of 0.01 T⁻¹ between 4 and 18 T, over which Fourier transforms were performed for all measured temperatures. The amplitude of the oscillations at specific frequencies was obtained by integrating peaks in the power spectra. These were subsequently analyzed using the standard LK relation,

$$LK(B_0, T) = A \frac{Cm^*T/B_0}{\sinh(Cm^*T/B_0)}, \quad B_0 = \frac{2}{1/B_1 + 1/B_2},$$
 (1)

where A is a temperature independent factor, B_0 is the inverse of the average inverse magnetic field, C contains all universal constants and is approximately equal to 14.7 T/K m_e , and m^* is the quasiparticle mass. Note that the change to B_0 due to the increase in internal field around the metamagnetic transition is of less than 0.2% and was neglected. Nonlinear fits of this relation to the data were performed using two parameters, A and m^* , for each field window, and each fit was carefully inspected by eye, rejecting field windows which produced inappropriate data distributions. The resulting masses are plotted in Fig. 6 as a function of B_0 . The error bars were obtained from the standard nonlinear regression procedure. Figure 7 shows four of these LK fits for the frequencies at 0.15, 1.78, and 4.13 kT in selected field regions, which are shown as color boxes in the respective insets. The fits are mostly very good.

It is clear from the data in Fig. 6 and from the fits in Fig. 7 that no strong enhancements of the quasiparticle masses of the bands β , δ , γ_1 , α_1 , and α_2 are present near the metamag-

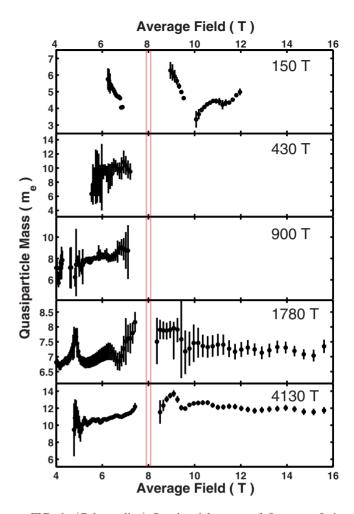


FIG. 6. (Color online) Quasiparticle mass of five out of six frequencies identified in the low-field side as a function of applied magnetic field. These correspond, respectively, to the bands α_1 , α_2 , δ , γ_1 , and β . The anomalous phase region, situated between 7.9 and 8.1 T, is indicated with vertical red lines. The fits were calculated over field ranges of 0.01 T⁻¹ except for the 0.15 kT frequency, for which a width of 0.02 T⁻¹ was necessary in order to properly resolve the corresponding peaks in the spectra. Gaps in the data are due to the amplitudes becoming too small to fit because of beat patterns in the data.

netic transition. Changes of at most four electron masses were seen, which originate from fitting errors when the signal to noise decreases at, for instance, nodes of beating patterns. For the case of γ_2 , situated at 0.11 kT, its resolution from the peak at 0.15 kT required a field range on the lowfield side of around 4 to 7 T, making the calculation of the field dependence of its mass impossible. The secondharmonic data shown here suppress its signal so much in relation to that of the 0.15 kT frequency that the temperature dependence of the latter could be successfully isolated. Note furthermore that the absence of data for the peaks at 0.43 and 0.90 kT on the high-field side of the metamagnetic transition is due to the absence of signal in that region for these bands (see Fig. 4). The signal for these bands appears at higher angles (see Fig. 5), suggesting that another process suppresses the amplitude of their quantum oscillations at low angle but that these bands are still present in that region. This

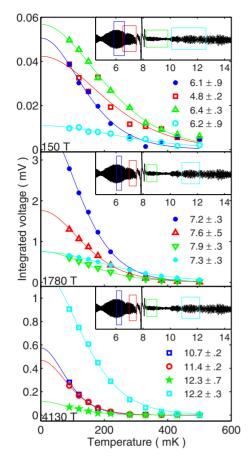


FIG. 7. (Color online) LK fits performed in various field ranges for three of the six detected frequencies, 0.15, 1.78, and 4.13 kT, which correspond to the β , α_1 , and α_2 bands. As in the data of Fig. 6, for the case of 0.15 kT, inverse field windows of a width of 0.02 T⁻¹ were used while for the other two, the width was of 0.01 T⁻¹. The field regions are indicated in color boxes in the respective insets, and the same color schemes are respected for the data. Integrated peaks in the Fourier spectra are represented with various symbols while fitted LK curves are shown with solid lines. The values in the legends correspond to the extracted quasiparticle masses.

result has been reproduced several times, and additional verifications have been performed using first-harmonic detection and a lower modulation field (3 G compared to 20 G).

The absence of a quasiparticle mass enhancement as a function of magnetic field in Sr₃Ru₂O₇ is a surprise to us. Both the electronic specific heat⁹ and the weight of the Fermi-liquid T^2 term⁴ show approximately consistent enhancements that, together, imply an average rise of the quasiparticle mass of a factor of between 2 and 3 between low fields and 7.5 T. It was therefore vital that we checked the sensitivity of our analysis techniques to an enhancement of this scale for all the detectable frequencies in our signal. We decided that the only way to test this in practice was using simulated dHvA data. Starting with the same parameters as those of our experiment (including modulation field, data sampling rate, relative amplitude factors for the different oscillatory components, and estimated sample mean-free path), we modeled a composite signal comprising the β , δ , γ_1 , α_1 , and α_2 frequencies to which we added random uncorrelated

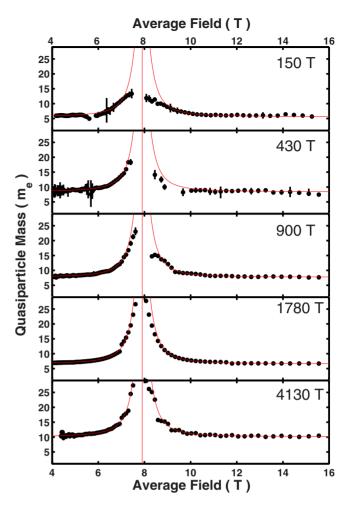


FIG. 8. (Color online) Quasiparticle mass of five simulated dHvA frequencies similar to those detected in our experiments, calculated using the same method as that used in Fig. 6. The data was modeled using quasiparticle masses which were strongly enhanced near 8 T. The oscillations were calculated using the masses and mean-free path extracted from the experiment, as well as amplitudes, field-dependent frequencies, and beat patterns similar to those in the data and uncorrelated Gaussian distributed noise was added to the oscillations.

Gaussian noise of a similar magnitude to that present in our experiments.

The simulated data were subsequently analyzed using exactly the same procedure as for the experimental data. The first data set used a field varying quasiparticle mass for the five bands simulated, using the experimental value away from the metamagnetic transition, and a strong, gradual enhancement shown by the red lines in Fig. 8. The onset of this increase was determined approximately from that of specificheat data. In contrast, the second simulation featured no quasiparticle mass enhancements but instead an increase in scattering rate of a factor of 2 at 8 T in order to replicate the observed decrease in signal at the metamagnetic transition (see Fig. 2, top panel).

In Fig. 8, we present the results of the analysis of the simulated data featuring mass enhancements for all the bands. The red curves indicate the values of the mass used in the calculations. We observed that depending on the signal to

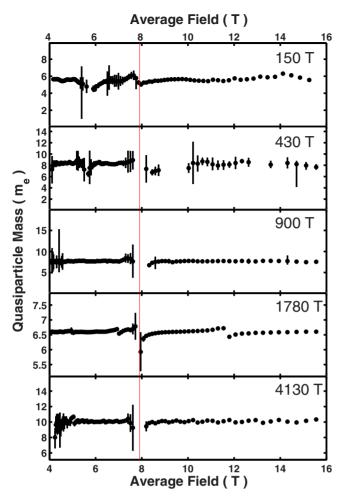


FIG. 9. (Color online) Quasiparticle mass of five simulated dHvA frequencies similar to those detected in our experiments, calculated using the same method as that used in Fig. 6. The data was modeled using a constant quasiparticle mass and a scattering rate which was strongly enhanced near 7.9 T, driving the amplitude to zero at this field value, similar to the experimental observations.

noise of the various oscillatory components, the extracted masses track the original ones very well for mass changes of up to around $10m_e$ for the component with lowest signal-to-noise ratio (0.15 kT), to above $25m_e$ for that with the highest-quality signal (1.78 kT), all of which are much larger than the largest mass changes measured in our data (of at most $4m_e$). We thus conclude that if such mass changes had been present in our dHvA data, we would have detected them.

In Fig. 9, we show the mass analysis of the second data set which does not feature mass enhancements, and yields the appropriate mass values. The Appendix describes how the previous incorrect result probably arose as a consequence of using a free offset as a third parameter in the Lifshitz-Kosevich fit to attempt to process data with a low signal-to-noise ratio. Since the current data had a much better signal-to-noise ratio, the use of either two or three parameter fits did not produce significantly different results.

In a third set of tests, we experimented with assigning a diverging mass individually to different frequencies, in case the entire specific-heat change were due to a diverging mass on only one Fermi-surface sheet. In doing so, we confirmed

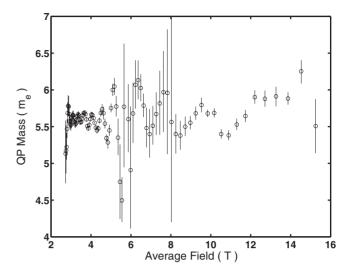


FIG. 10. Quasiparticle mass extracted from the merged peak composed of the frequencies at 0.11 and 0.15 kT, originating, respectively, from the γ_2 and β bands, where in the simulation, the mass of γ_2 band is strongly enhanced while that of the β band is not. The mass enhancement is washed out by the β band, which possesses a mass of $5.5m_e$.

that if this were happening, our data analysis procedures would be sensitive to it. The only exception to this came when trying to include a diverging mass for a frequency at 0.11 kT. Here, it is impossible to perform the field-dependent mass analysis and still resolve that component of the signal from the one at 0.15 kT. In first-harmonic dHvA, the integrated weight of the 0.11 kT component is much less than that of the 0.15 kT component, and the effect of the 0.11 kT component experiencing a rapid change in amplitude with temperature is masked by the much weaker temperature dependence of the 0.15 kT component. This is demonstrated in Fig. 10, which shows the result of a simulation incorporating the experimental oscillatory amplitudes in which the mass of γ_2 is enhanced by an order of magnitude between low/high fields and the transition region. The relative integrated weights of our magnetocaloric data are similar at our lowest temperature of measurement, but for that apparatus the base temperature is only 100 mK, and resolving a strongly fielddependent mass for the 0.11 kT component would require lower-temperature data. We conclude, therefore, that we can neither definitely detect nor rule out a strong-field dependence of the quasiparticle mass from this Fermi-surface sheet on the basis of the current data.

IX. CONCLUSION

The first two pieces of information that we have presented in this paper concern the magnetic field and field-angle dependence of the dHvA frequencies both below and above the metamagnetic transition fields in Sr₃Ru₂O₇. Although the data contain some unusual features, it seems possible to account for these in terms of previously known effects. Field-dependent frequencies are a consequence of backprojection in the presence of itinerant metamagnetism. ^{11,31} The "fragmentation" of the observed frequencies at high fields can be

qualitatively accounted for by magnetic breakdown effects, although we do not have sufficient information to perform the full quantitative analysis that would be required to prove that this is the sole cause of the observations.

The finding that we observe essentially no systematic field dependence of the quasiparticle masses is more surprising. Taking a conventional viewpoint, it is tempting to assume that since the specific heat shows a large change over the same field range, some quasiparticle mass enhancement must be taking place, and hence that it must be associated with the γ_2 frequency for which we have no reliable dHvA information on the field dependence of the mass. Adopting that assumption would imply an order of magnitude change in its mass between low field and 7.5 T.³² It would be dangerous to draw a firm conclusion on this point in the absence of firm data; this aspect of our work motivates further experimental and theoretical study.

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APPENDIX: SYSTEMATIC ERRORS IN dHvA MASS ANALYSIS

We present in this appendix a discussion of dHvA quasiparticle mass analysis methods, and how certain assumptions in the analysis method can lead to large systematic errors. In particular, we try to explain how the analysis performed in the work of Borzi *et al.*⁷ led to the apparent observation of a strong quasiparticle mass enhancement of the α_1 and α_2 bands (at 1.78 and 4.13 kT).

The usual analysis method of the temperature dependence of the amplitude of dHvA oscillations consists of performing Fourier transforms of data for all temperatures over the same field range. Integrals are performed over a specific peak in the resulting power spectra of which the square root is taken. The field-dependent amplitudes are then analyzed using a nonlinear fit of the standard LK expression of the form given in Eq. (1). This function saturates at the lowest temperatures toward the parameter *A* of Eq. (1), and exponentially decreases at high temperatures.

However, in quantum oscillation data which feature appreciable levels of noise compared to the signal, the integral of the power spectra never decreases to zero amplitude at high temperatures. Effectively, if we write the signal as $A\cos(F_0/B+\phi)+f(B)$, where f(B) consists of random noise, the power spectrum W(F) as a function of frequency F of the Fourier-transformed signal can then be written as

$$W(F) = |\delta(F - F_0) + \tilde{f}(F)|^2, \tag{A1}$$

where $\delta(F-F_0)$ corresponds to a peak centered at F_0 and $\tilde{f}(F)$ is the Fourier transform of f(B). At high temperatures, the peak vanishes and one is left with $W(F)=|\tilde{f}(F)|^2$, which

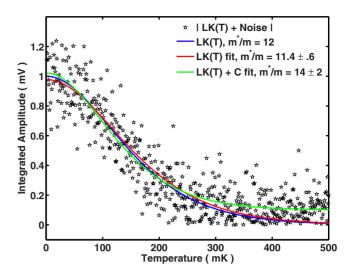


FIG. 11. (Color online) Example of the two types of nonlinear LK fits to the data. The absolute value of the sum of the LK function (blue curve) and random Gaussian noise is shown in black stars, using a quasiparticle mass of $12m_e$. To this data was fitted the LK expression using a two parameter fit (red curve), which yielded a small underestimate of $11.4m_e \pm 0.6m_e$. A three parameter fit was also performed, featuring a free offset (green curve), which yielded an overestimate of the mass of $14m_e \pm 2m_e$.

is not zero. In the analysis of Ref. 7 Borzi *et al.* subtracted the apparent resulting offset in the high-temperature range of the temperature dependence of the dHvA amplitude by using a nonlinear fit procedure involving a free offset,³³ of the form

$$LK(B_0, T) = A \frac{Cm^*T/B_0}{\sinh(Cm^*T/B_0)} + \text{Const.},$$
 (A2)

using three fit parameters, A, m^* , and Const. We will demonstrate in the following that such a procedure always leads to an overestimate of the mass m^* .

Effectively, adding a free offset to the fitting procedure is equivalent to the assumption that the power spectrum is equal to $|\delta(F-F_0)|^2 + |\tilde{f}(F)|^2$, i.e., the sum of the signal and noise in frequency space. However, as stated in Eq. (A1), it is not the case, but rather, we have that

$$|\delta(F - F_0)|^2 + |\tilde{f}(F)|^2 \ge |\delta(F - F_0) + \tilde{f}(F)|^2, \quad (A3)$$

and the difference between the two sides of this inequality depends on the temperature. As the noise amplitude increases, the difference between these expressions increases, and the signal becomes "buried" into the noise. Consequently, the width of the peak emerging from the noise at low temperature appears to decrease, yielding a larger mass m^* when using a free offset. It is however not what happens when one uses the usual two parameter fit.

In Fig. 11, we illustrate this situation. We took the normal LK distribution (blue curve), using a mass of $12m_e$, to which we added random Gaussian noise, and took the absolute value (the square root of the power spectrum), shown in black stars. We used 500 data points in order to show that the problem does not arise due to undersampling. We then

performed the two different types of fits with (green curve) and without (red curve) a free offset. The resulting masses are different, where the two parameter fit obtains a slight underestimate (5%) while the three parameter fit overestimates the value by 17%. While neither of the two methods yields the correct value, the three parameter fit always deviates more strongly, and always overestimates the value.

This effect depends strongly on the signal-to-noise ratio. Consequently, if the signal-to-noise ratio decreases gradually as a function of magnetic field, then the overestimates generated by three parameter fits usually increases gradually, giving the impression of a field varying mass. In order to demonstrate the serious nature of this problem, we performed a simulation of typical dHvA data (similar to that of the α_2 band), which featured beat patterns, a Dingle amplitude reduction factor, and a constant level of uncorrelated Gaussian distributed noise of various amplitudes,

$$LK(B,T)D(B)[\cos(2\pi F_1/B) + \cos(2\pi F_2/B)] + f(B),$$
(A4)

where LK is the LK function, which uses a mass of $12m_e$, D is the Dingle factor, which uses a mean-free path of $1~\mu m$ and a frequency of 4.2~kT and f(B) is the noise.

In Fig. 12, top three panels, we show simulated raw data, the first without noise and the following two with different noise amplitudes. The bottom three panels present the respective extracted field-dependent masses when using three parameter fits. The procedure for this calculation was the same as that which was used for the experimental data, described earlier. We found strong systematic errors in both cases where noise was added to the data, which are largest at each node of the beat pattern in the region where the overall signal-to-noise ratio is the lowest. We performed the same analysis while using two parameter fits, not shown here, and this problem was not encountered.

In $Sr_3Ru_2O_7$ dHvA data, the signal-to-noise ratio decreases near the metamagnetic transition, mainly due to a combination of the Dingle reduction factor and scattering which increases near the QCP and reduces the amplitude of quantum oscillations. Consequently, it is natural that this problem could have arisen specifically in this field range. However, it did not arise in the analysis of the data reported

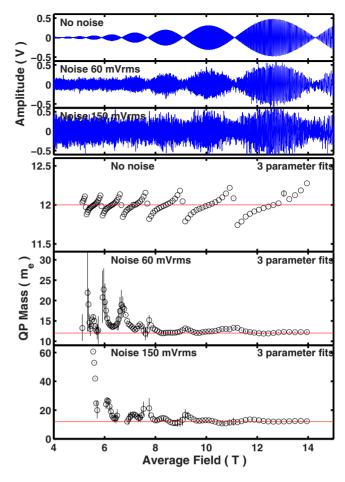


FIG. 12. (Color online) Simulations of dHvA data featuring a field-dependent signal-to-noise ratio, and its mass analysis using a three parameter fit featuring a free offset. The top panel presents noiseless simulated dHvA data, featuring two frequencies of 4.20 and 4.25 kT, leading to beat patterns, a mean-free path of 1 μ m, and a quasiparticle mass of $12m_e$. The following two panels show the same data with two different added noise levels. These sets of data were analyzed with three parameter fits, the results of which are presented in the bottom three panels.

in this paper which featured a much higher signal-to-noise ratio, where the resulting offset was generally close to zero. Such fits generated the same results as two parameter fits.

¹H. v. Löhneysen, A. Rosch, M. Vojta, and P. Wölfle, Rev. Mod. Phys. **79**, 1015 (2007).

²R. Settai, H. Shishido, T. Kubo, S. Araki, T. Kobayashi, H. Harima, and Y. Onuki, J. Magn. Magn. Mater. **310**, 541 (2007).

³D. Shoenberg, *Magnetic Oscillations in Metals* (Cambridge University Press, Cambridge, 1984).

⁴S. A. Grigera, R. S. Perry, A. J. Schofield, M. Chiao, S. R. Julian, G. G. Lonzarich, S. I. Ikeda, Y. Maeno, A. J. Millis, and A. P. Mackenzie, Science **294**, 329 (2001).

⁵S. A. Grigera, R. A. Borzi, A. P. Mackenzie, S. R. Julian, R. S. Perry, and Y. Maeno, Phys. Rev. B **67**, 214427 (2003).

⁶R. S. Perry, L. M. Galvin, S. A. Grigera, L. Capogna, A. J. Schofield, A. P. Mackenzie, M. Chiao, S. R. Julian, S. I. Ikeda, S. Nakatsuji, Y. Maeno, and C. Pfleiderer, Phys. Rev. Lett. 86, 2661 (2001).

⁷R. A. Borzi, S. A. Grigera, R. S. Perry, N. Kikugawa, K. Kitagawa, Y. Maeno, and A. P. Mackenzie, Phys. Rev. Lett. **92**, 216403 (2004).

⁸ A. Tamai, M. P. Allan, J. F. Mercure, W. Meevasana, R. Dunkel, D. H. Lu, R. S. Perry, A. P. Mackenzie, D. J. Singh, Z.-X. Shen, and F. Baumberger, Phys. Rev. Lett. 101, 026407 (2008).

⁹ A. W. Rost, R. S. Perry, J.-F. Mercure, A. P. Mackenzie, and S.

- A. Grigera, Science 325, 1360 (2009).
- ¹⁰R. A. Borzi, S. A. Grigera, J. Farrell, R. S. Perry, S. J. S. Lister, S. L. Lee, D. A. Tennant, Y. Maeno, and A. P. Mackenzie, Science 315, 214 (2007).
- ¹¹J.-F. Mercure, S. K. Goh, E. C. T. O'Farrell, R. S. Perry, M. L. Sutherland, A. W. Rost, S. A. Grigera, R. A. Borzi, P. Gegenwart, and A. P. Mackenzie, Phys. Rev. Lett. 103, 176401 (2009).
- ¹² A. P. Mackenzie and Y. Maeno, Rev. Mod. Phys. **75**, 657 (2003).
- ¹³H. Müller-Buschbaum and J. Wilken, Z. Anorg. Allg. Chem. **591**, 161 (1990).
- ¹⁴Q. Huang, J. W. Lynn, R. W. Erwin, J. Jarupatrakorn, and R. J. Cava, Phys. Rev. B **58**, 8515 (1998).
- ¹⁵H. Shaked, J. D. Jorgensen, O. Chmaissem, S. Ikeda, and Y. Maeno, J. Solid State Chem. 154, 361 (2000).
- ¹⁶I. I. Mazin and D. Singh, Phys. Rev. Lett. **79**, 733 (1997).
- After distortion, Sr₃Ru₂O₇ possesses four instead of two non-equivalent Ru atoms, bringing the number of *d* bands crossing the Fermi level from three to six. For further discussion see W. C. Lee, D. J. Arovas and C. Wu, Phys. Rev. B **81**, 184403 (2010).
- ¹⁸R. S. Perry and Y. Maeno, J. Cryst. Growth **271**, 134 (2004).
- ¹⁹ A. Kanbayashi, T. Miyadai, H. Kondo, and S. Miyahara, J. Phys. Soc. Jpn. **30**, 1754 (1971).
- ²⁰P. B. Allen, H. Berger, O. Chauvet, L. Forro, T. Jarlborg, A. Junod, B. Revaz, and G. Santi, Phys. Rev. B 53, 4393 (1996).
- ²¹G. Cao, S. McCall, M. Shepard, J. E. Crow, and R. P. Guertin, Phys. Rev. B **56**, 321 (1997).
- ²²G. Cao, L. Balicas, W. H. Song, Y. P. Sun, Y. Xin, V. A. Bondarenko, J. W. Brill, S. Parkin, and X. N. Lin, Phys. Rev. B 68, 174409 (2003).
- ²³ S.-I. Ikeda, Y. Maeno, S. Nakatsuji, M. Kosaka, and Y. Uwatoko, Phys. Rev. B **62**, R6089 (2000).
- ²⁴J. F. Mercure, Ph.D. thesis, University of St. Andrews, 2008.
- ²⁵ A. P. Mackenzie, S. R. Julian, A. J. Diver, G. J. McMullan, M. P. Ray, G. G. Lonzarich, Y. Maeno, S. Nishizaki, and T. Fujita, Phys. Rev. Lett. **76**, 3786 (1996).

- 26 The inverse field width of each window is about 3.6 times larger than the inverse field spacing between the centres of consecutive windows.
- ²⁷One could also invoke quantum interference oscillations as a source of splitting of dHvA peaks. However, as shown in Ref. 3, these are by nature insensitive to temperature. We can show with high-temperature data (not shown in the paper) that no oscillations remain above 800 mK over the whole field range from 18 to 2 T.
- ²⁸C. Bergemann, A. P. Mackenzie, S. R. Julian, D. Forsythe, and E. Ohmichi, Adv. Phys. **52**, 639 (2003).
- ²⁹ Note that the data excludes orbits closed near the top of the zone, which would show up, for instance, in the data of the 1.79 kT peak (α_1) since the orbits reach the top of the zone at 52° [the height of zone is k_z =600 Å⁻¹ while the in-plane Fermi vector is k_F =234 Å⁻¹, thus one reaches the top of the zone at $\tan^{-1}(300/234)$ =52°], an angle covered by our data. The α_1 orbit, if closed near the top of the zone, would show a downturn of the frequency at an angle below 52°. Oscillations were searched at higher angles than those shown in this paper but none were detected.
- ³⁰D. J. Singh and I. I. Mazin, Phys. Rev. B **63**, 165101 (2001).
- ³¹ S. R. Julian, P. A. A. Teunissen, and S. A. J. Wiegers, Phys. Rev. B 46, 9821 (1992).
- ³²At first sight it may seem that the combination of specific heat and dHvA is incompatible with previous transport data that show a factor of 7 rise in the strength of T^2 scattering at low T as the critical point is approached (Ref. 4). At zero field and without impurity scattering, the temperature-dependent resistivity contribution from the γ_2 pocket, which comprises a maximum of only one fifth of the Fermi surface, would be shorted out by the other pockets. However, at finite field as well as in the limit of residual scattering dominating the resistivity, a realistic calculation based on the multiband Fermi surface of $Sr_3Ru_2O_7$ shows that the transport could, in principle, be accounted for by a factor of 10 increase in the γ_2 mass.
- ³³R. A. Borzi (private communication).