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NON-MONOTONIC HEALTH BEHAVIOURS – implications for individual health-related behaviour in a demand-for-health framework^{*}

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ABSTRACT

A number of behaviours influence health in a non-monotonic way. Physical activity and alcohol consumption, for instance, may be beneficial to one's health in moderate but detrimental in large quantities. We develop a demand-for-health framework that incorporates the feature of a physiologically optimal level. An individual may still choose a physiologically non-optimal level, because of the trade-off in his or her preferences for health versus other utility-affecting commodities. However, any deviation from the physiologically optimal level will be punished with respect to health. A set of steady-state comparative statics is derived regarding the effects on the demand for health and health-related behaviour, indicating that individuals will react differently to exogenous changes, depending on the amount of the health-related behaviour they demand. We also show (a) that a steady-state equilibrium is a saddle-point and (b) that the physiologically optimal level may be a steady-state equilibrium for the individual. Our analysis suggests that general public-health policies may, to some extent, be counterproductive due to the responses induced in parts of the population.

Keywords: Human capital; Grossman model; non-monotonic health investments; health; steadystate and stable equilibria.

JEL classification: I12

1. INTRODUCTION

Most human behaviours are related to health. Individual health affects consumption patterns, but consumption patterns also affect individual health. While the sole intention of health-care utilisation is either to improve current health, whenever it has fallen below a certain illness-defining threshold value, or to prevent future illness, rather than to consume it for the sake of its direct utility (which might even be negative), the intention of many other behaviours may be twofold: both to gain direct consumption utility and to improve health (or to decrease the risk of illness). The latter category includes, for instance, physical exercise, certain consumption and composition of food, alcohol consumption and, as a matter of fact, any recreational activity (art, literature, music, etc). Obviously, health effects may be more or less intentional, and certain consumption patterns may also be detrimental to your health. Smoking is an unambiguous example of the latter.

Smoking is always bad for your health – and increasingly so with increased consumption (Doll et al, 1976; Doll et al, 1994; Colditz, 2000; Vineis et al, 2004). In contrast, there appears to be a physiologically determined, individually optimal level of activity (greater than zero) as regards, for instance, physical exercise, food intake, alcohol consumption, and sleep, implying that activity levels below or above that level would result in a level of health which is lower than the maximum achievable level; see Figure 1 for an illustrative example of a typically U-shaped relation.

Figure 1 about here

A consistently positive association between physical-activity level and health-related quality of life has been found (Bize et al, 2007). Certainly, too small amounts of physical exercise means that the human body atrophies and that the risks of several diseases, including coronary heart disease, hypertension, stroke, diabetes, depression, osteoporosis, and cancers of the breast and colon, increase (Garrett et al, 2004). However, too much or too intensive physical exercise means that the human body will wear down and/or that the risk of injury increases (Tisi and Shearman, 1998; Locke, 1999; Ji, 2001; Randolph, 2007; Howatson G and van Someren, 2008; Morton et al, 2009). A varied and balanced diet is emphasised in guidelines on healthy eating; see, for instance (Swedish National Food Agency, 2012). Too little food or too one-sided diet lead to health problems (Steinhausen, 2002). Too much also creates health problems (Steinhausen and Weber, 2009), in particular in combination with too little physical exercise.

Overweight $(25 \le BMI < 30)^1$ and obesity (BMI ≥ 30) increase the risks of asthma, coronary heart disease, hypertension, diabetes, osteoarthritis, and cancer, including cancers of the breast and colon (Colditz, 1999; Must et al., 1999); Dal Grande, 2009). Also underweight (BMI < 18.5) has been shown to be associated with health problems; for instance, coronary heart disease, diabetes, and gallbladder disease (Must et al., 1999). Light to moderate drinkers are at lower risk of coronary heart disease, stroke, diabetes, and gallstone disease than non-drinkers, while an increasing intake increases the risks of dementia, liver cirrhosis, pancreatitis, osteoporosis, and most cancers, including cancer of the oesophagus, breast, pancreas, colon, and rectum (Grönbaeck, 2009). Finally, both short and long sleep durations appear to be related to increased likelihood of obesity, diabetes, hypertension, and cardiovascular disease (Buxton and Marcelli, 2010; Sabanayagam and Shankar, 2010).

It should be emphasised, though, that which level of physical exercise, food intake, alcohol consumption, and sleep is physiologically optimal differs among individuals, and if you have

^{*}We thank Martin Forster for insightful comments and useful suggestions.

¹ BMI (body mass index) is calculated as weight in kilograms divided by height in meters.

good genes and/or are lucky, you may suffer less from "unhealthy" behaviour than less advantaged people.

In general terms, these associations have been known for decades. Yet, there are no clear temporal trends worldwide towards healthier life-styles (Knuth and Hallai, 2009), and the population variance of these behaviours is large; for instance, many people do not perform any, or very little, physical exercise, others perform very large amounts. We will demonstrate that such polarization may be possible to explain, within a modified version of Grossman's demand-for-health model, assuming that there is a (strictly positive) physiologically optimal level of the corresponding health behaviour.

The demand-for-health model extended the human capital theory by explicitly incorporating health and recognising that there are both consumption and investment motives for investing in health (Grossman, 1972a, b). It resulted in an economic theory of individual health-related behaviour. The basic features of the model are (1) that the individual demands health (a) for its utility enhancing effects (the consumption motive), and (b) for its effect on the amount of healthy time (the investments motive), (2) that the demand for investments in health is derived from the more fundamental demand for health, (3) that the investments in health are produced by the individual, and (4) that the stock of health depreciates at each point in time. The production aspect implies that the produced amount of investments in health has to be assimilated by the individual. Thus, the effects of, for instance, physical exercise, is assimilated and transformed into health by the individual at rates that differ between individuals. This goes beyond the effect of the depreciation of the stock of health at each point in time.

Although *some* variance in health-related behaviours may be readily understood within Grossman's original version of the demand-for-health model, the observed variance seems to be

greater than what would be expected, solely taken the variability in physiologically determined, individually optimal level of activity into account. In this paper we develop a version of Grossman's demand-for-health model, modified in order to focus on individually optimal choices of health-related behaviour, distinguished by physiologically optimal activity levels.

Since its introduction, the demand-for-health model has been extended in various ways; incorporating risk and uncertainty (Dardanoni and Wagstaff, 1987, 1990; Selden, 1993; Chang, 1996; Liljas, 1998, 2000; Picone et al., 1998; Asano and Shibata, 2011), the family as producer of health (Jacobson, 2000; Bolin et al., 2001, 2002b), the employer as producer of health (Bolin et al., 2002c), social capital (Bolin et al., 2003), healthy and unhealthy consumption (Forster, 2001), decreasing returns to scale in the production of health investment (Ehrlich and Chuma, 1990; Galama, 2011), imperfect financial markets (Liljas, 2000, 2002), and allowing for corner solutions (Galama and Kapteyn, 2011). To our knowledge, however, the effect on the demand for health and health investments of the double-facetted nature of individual behaviours with physiologically determined optimal levels as regards health and negative or positive health effects, depending on the level of activity, has never been analysed.² While the emphasis of the paper is on extending theory, it will be shown that such an analysis has important implications for the understanding of individual health-related behaviour and, hence, for designing and evaluating health policies.

The structure of the rest of the paper is as follows. Next, we will present the model. After that, we will derive the optimality conditions. Following this, we will analyse the properties of the

 $^{^2}$ Forster (2001) studied health-related effects of there being two types of consumption: good for health and bad for health. In both cases the effect on health is monotonic in consumption. In our case, the relationship between the amount of behaviour and its health effect is not monotonic. Grossman (1972a) examined the importance of joint production in the production of gross health investment. He argued that several goods are demanded as inputs into the production of commodities, other than health, that yield utility but may have adverse health effects.

dynamic system in terms of steady-state and stability conditions. The final section contains a discussion and some conclusions.

2. THE MODEL

Our theoretical model takes its departure in the demand-for-health model developed by Michael Grossman (1972a, b). It differs from Grossman's original formulation mainly (1) by avoiding an explicit treatment of the individual's time allocation problem³, and (2) by considering health-related behaviours that are not monotonic in their effect on health.

2.1 Preferences

We consider a version of the demand-for-health model in continuous time, in which health at each point in time, H(t), is produced by the individual through a specific health behaviour, B(t). The behaviour B(t) influences health positively below a certain level, and negatively above that level; we assume that the smallest amount of behaviour B(t) is zero. The individual derives utility from his or her stock of health, H(t), from health-related behaviour, B(t), as well as from consumption unrelated to health, Z(t). More specifically, we assume that preferences are additively separable, time additive, and concave in all arguments. In order to reduce complexity and, hence, to increase the capability of the model to generate unambiguous predictions, we also assume that the marginal utility of (the health-unrelated) consumption is constant. Further, throughout the paper we deal with individuals that choose strictly positive levels of the *B*-behaviour but spend strictly less than total available resources on *B*, i.e., $0 < B(t) < B^{max}$, where B^{max} is defined as the level of *B* where the utility of an additional unit of *B* is exactly balanced by the reduction in utility brought about by the necessary reduction in the consumption of *Z*, dictated by the budget restriction. Formally, individual preferences are represented by the

 $^{^{3}}$ Instead, we utilise the individual's cost function, pertaining to the allocation problem that he or she faces. This means that we – implicitly – assume that the individual has solved the time allocation problem.

following quasi-linear continuous utility function $(u' > 0; u'' = \overline{u} < 0; v' > 0; v'' = \overline{v} < 0;$ and $v(0) = m > 0)^{4.5}$:

$$U(H(t), B(t)) = u(H(t)) + v(B(t)) + k \cdot C(t), \tag{1}$$

where k is the marginal utility of consumption.

The positive health effect produced by the behaviour, B(t), is partially offset by a natural depreciation – at rate δ ($0 < \delta < 1$) – of the existing stock of health capital.⁶ For tractability of dynamic analysis we consider a model in which the rate of depreciation is time independent.⁷ Further, we distinguish between the ability to produce (see below) the behaviour, B(t), and the rate at which the behaviour is transformed into gross health investments, I(t). Thus, the equation of motion for the stock of health capital is:

$$\frac{dH(t)}{dt} = B(t) - \varphi \cdot (B(t) - B^*)^2 - \delta \cdot H(t) \equiv I(t) - \delta \cdot H(t).$$
(2)

This equation comprises two sources of bodily decay: the natural depreciation, by rate δ , which can be *compensated for* by the health-related behaviour, B, and atrophy of the body, which can be *avoided* – at $B(t) = B^*$ there is no atrophy. This level of the B-behaviour reflects the amount by which the body atrophies, when the individual does not partake in the healthy behaviour, i.e., when (t) = 0. At the zero activity level, the body atrophies at the rate $-\varphi \cdot (B^*)^2$; the parameter φ ($\varphi > 0$) reflects the rate at which the individual may reduce the amount of atrophy by

⁴ Throughout the paper, a subscript indicates a partial derivative. Deviating somewhat from established practice, we denote the time derivative as $\frac{d}{dt}$.

⁵ Quasi-linear utility functions have been extensively applied in economic analyses of the family, and related issues; see, for instance, Chang (2009, 2007); Chang and Weisman (2005); Konrad et al., (2002); Konrad and Lommerud (2000). Essentially, the quasi-linearity assumption means that the analysis is focused on the importance of relative prices, since there is no income effect for goods other than the linear-utility good.

⁶ Fundamentally, one may argue that the health-related behaviour is an input into the production of gross health investments and not the output of that production process. In an analysis of the composition of inputs into the production of gross health investments, this distinction would be necessary. Here, however, our focus is on the effects of a specific behaviour, having a negatively U-shaped effect on health.

⁷ In this paper, we analyse time-paths and stability of equilibrium. This is considerably less difficult in autonomous systems, which require a time-independent rate of depreciation, or that total depreciation at each point in time is independent of the health stock. This is in contrast to Grossman (1972), Muurinen (1982), Wagstaff (1986), Liljas (1998), Jacobson (2000), and Bolin et al. (2001a), who all examined models with time-dependent rates of depreciation.

modifying the *B*-behaviour. Different behaviours are characterised by different φ 's. Starting at B(t) = 0 and moving towards more *B*-behaviour will gradually offset the atrophy until it is exactly balanced at $B(t) = \frac{1}{2\varphi} + B^* - \sqrt{\frac{1+4B^*\varphi}{4\varphi^2}}$. At $B(t) = \frac{1}{2\cdot\varphi} + B^*$, the *B*-behaviour exerts its maximum health-enhancing effect: $I^{max}(t) = \frac{1}{4\cdot\varphi} + B^*$. Thus, $B(t) = \frac{1}{2\cdot\varphi} + B^*$ is the physiologically optimal level of the *B*-behaviour. Increasing *B* beyond that point will start to reduce the health effect of the behaviour.

Figure 2 about here

Figure 2 illustrates the influence on gross health investment produced by the *B*-behaviour. It facilitates our analysis to distinguish between three individual types: those that exert less and more, respectively, than the physiologically optimal level, $\frac{1}{2\cdot\varphi} + B^*$, and those that exert exactly the physiologically optimal level – these types will be referred to as type 1, 2 and 3. A higher rate at which the atrophy increases when the individual moves away from B^* implies (1) that the physiologically optimal level of *B* moves closer to B^* , and (2) that the level of *B* that exactly offsets atrophy or adverse health effects moves closer to B^* (the distance between the intersections with the horizontal axis and B^* gets smaller).

2.2 Production technology and cost function

For simplicity, we assume that the technology used for producing the health-related behaviour is homogenous and exhibits constant returns to scale. Thus, the technology is formally represented by a production function that is homogenous, of degree 1 in the quantity of investment. Thus, the dual cost-of-behaviour function is homogenous of degree 1 with respect to the quantity of the behaviour, i.e., the cost of producing the behaviour is constant with respect to its quantity. Formally, the cost function is:

$$C(B(t)) = \pi(q, w; E) \cdot B(t), \tag{3}$$

where $\pi(q, w; E)$ is the one-unit cost of producing the behaviour, q is the composite price of market goods and services used in the production, w is the wage rate, and E is the level of knowledge. Thus, differences between individuals regarding their production efficiencies are comprised in w and E.

2.3 Budget constraint

For convenience, we assume that there are no financial markets and, hence, that total spending at time t equals market income at time t.⁸ Hence, the individual's budget constraint can be expressed as:

$$p \cdot Z(t) = y(H(t)) - \pi \cdot B(t), \tag{4}$$

where y denotes full market income (the market value of total time that is available for market work or the *B*-behaviour), and p the price of the consumption good. We express full market income as a function of health, since health determines the total amount of time, which is available for the individual to allocate between B and market work. This amount of time equals total time, Ω , reduced by time spent being sick, $\tau(H(t))$. Thus, full market income is:

$$y(t) = w \cdot \left(\Omega - \tau(H(t)) \right). \tag{5}$$

Available time that the individual may allocate freely between its two productive uses increases as the stock of health capital increases. Formally, the amount of time spent being sick is inversely

⁸ In this way an autonomous dynamic model is obtained without introducing time as yet another state variable. Analysing properties of non-autonomous dynamic system is beyond what can be achieved using most economists' tool box. Autonomous systems are considerably more straightforward, while still allowing for important issues to be analysed. Dynamic models of health behaviour, when there are no financial markets, have been used by, for instance, Liljas (1998) and Forster (2001). Here, the absence of capital markets means that the only way that the individual can transfer resources between different points in time is by investing in health capital. We have made the assumption that preferences, prices, technology and the rate of depreciation are time invariant, which means that individual incentives for transferring resources between stages of the lifecycle do not comprise any timing-of-investment considerations. With time-varying prices for the inputs into production of health capital, this would be a major purpose for transferring resources in time.

related to the stock of health capital, i.e., $\tau_H < 0$. Further, we assume that the productivity of health in producing healthy time is diminishing, i.e., $\tau_{HH} > 0$, at a constant rate, i.e., $\tau_{HHH} = 0$. Thus, potential income is increasing and concave in health capital, since $y_H(t) = -w \cdot \tau_H > 0$; and $y_{HH}(t) = -w \cdot \tau_{HH} < 0$.

2.4 The individual's control problem

The individual's objective is to maximize his or her lifetime utility. Formally, this means solving the intertemporal optimization problem of choosing the time path of health capital that maximizes lifetime utility by partaking optimally in the health-related behaviour. We assume a fixed end-point for the individual's planning horizon and that the shadow price of health capital must be 0 at t = T, or that H(T) equals the smallest permitted health level. Thus, discounting future utility at the rate ρ , the individual acts as if solving the following problem:⁹

$$\max_{B_t, H_t} \int_0^T e^{-\rho \cdot t} \cdot \left[u \big(H(t) \big) + v \big(B(t) \big) + k \cdot Z(t) \right] dt \tag{6}$$

subject to: $\frac{dH(t)}{dt} = B(t) - \varphi \cdot (B(t) - B^*)^2 - \delta \cdot H(t),$

and the transversality condition $\lambda(T) \cdot (H_T - \underline{H}) = 0$; $H_T \ge \underline{H} \ge 0$, where \underline{H} is the smallest permissible level of health. The individual inherits a known stock of health H^0 , i.e., $H(0) = H^0$.

3 RESULTS

3.1 Conditions for optimal paths of behaviour and health

The solution to the maximisation problem is obtained by means of the maximum principle of optimal control theory, which gives necessary and sufficient conditions for the optimal control of

⁹ For convenience, we formulate the individual's optimisation problem as a vertical terminal line problem, which means that the terminal time is fixed, but the terminal state is free (Chiang, 1992, p.182). This is to be distinguished from a horizontal terminal line problem in which the terminal time, T, is free, and, hence, that the terminal state is restricted to $H(T) \ge \underline{H}$. The optimality conditions resulting from these two problems only differ regarding the transversality conditions. In the horizontal terminal line problem, optimal length of life is, implicitly, determined by the transversality conditions; see, for instance, Ehrlich and Chuma (1990). The individual's life-time optimisation problem was formulated as a vertical time line problem by, for instance, Bolin et al (2001; 2002b, c).

B(t), given the time path of the state variable H(t).¹⁰ The current-value Hamilton function for the maximisation problem is, substituting for Z(t) using (4):

$$\mathcal{H}(t) = u(H(t)) + v(B(t)) + k \cdot \frac{y(H(t)) - \pi \cdot B(t)}{p} + \lambda(t) \cdot (B(t) - \varphi \cdot (B(t) - B^*)^2 - \delta \cdot H(t)).$$

$$(7)$$

The maximum principle yields the following equations of motion. First, for the stock of health:

$$\frac{d\lambda(t)}{dt} = -\mathcal{H}_H(t) + \lambda(t) \cdot \rho = -u' + k \cdot \frac{w}{p} \cdot \tau_H(t) + \lambda(t) \cdot (\delta + \rho) \equiv f(t)$$
(8)

The optimal choice of the single control variable, B(t), satisfies the first-order (sufficient) condition:

$$\mathcal{H}_B(t) = \nu' - k \cdot \frac{\pi}{p} + \lambda(t) \cdot \left(1 - 2 \cdot \varphi \cdot (B(t) - B^*)\right) = 0.$$
⁽⁹⁾

The optimal level of the **B**-behaviour

Let us begin by restating a useful result: since u' > 0, we know that $\lambda(t) > 0 \forall t \in [0,T]$ (Caputo, 2005; p. 56) and, hence, optimal choices can be analysed, for each type, by using the sign of $v' - k \cdot \frac{\pi}{p}$. Thus, condition (9) implies that the type-1 individual partakes in the *B*-behaviour at a level $\widehat{B}_1(t) \in (\underline{B}, B^* + \frac{1}{2 \cdot \varphi})$, where \underline{B} is defined by $v'(\underline{B}) - k \cdot \frac{\pi}{p} = 0$. Similarly, the type-2 individual partakes at a level $\widehat{B}_2(t) \in (B^* + \frac{1}{2 \cdot \varphi}, \overline{B})$, where \overline{B} is defined by $v'(\overline{B}) - k \cdot \frac{\pi}{p} = m - k \cdot \frac{\pi}{p} = 0$. This is clear from, *first*, the assumption that for both types: $v'(0) - k \cdot \frac{\pi}{p} = m - k \cdot \frac{\pi}{p} > 0 \Rightarrow \mathcal{H}_B(t)|_{B=0} > 0$; and, *second*, the definition of the type-1 individual $v'(B^* + \frac{1}{2 \cdot \varphi}) < k \cdot \frac{\pi}{p} \Rightarrow \mathcal{H}_B(t)|_{B=B^* + \frac{1}{2 \cdot \varphi}} < 0$ (analogously for type 2). Thus, due to continuity we are assured that for some $B(t) = \widehat{B}_1$, such that $\underline{B} < \widehat{B}_1 < B^* + \frac{1}{2 \cdot \varphi}$, $\mathcal{H}_B(t)|_{B=\overline{B}_1} = 0$. Similarly, for the type-2

¹⁰ By the Mangasarian sufficiency theorem, (8) and (9) are necessary and sufficient conditions for an optimum if the Hamiltonian function, \mathcal{H} , is jointly and strictly concave in (H, B). First, notice that $\mathcal{H}_{HB} = \mathcal{H}_{BH} = 0$. That leaves only the diagonal terms of the Hessian matrix, H, for the Hamiltonian function. These are: $\mathcal{H}_{HH} = u'' + k \cdot y_{HH} < 0$, and $\mathcal{H}_{BB} = v'' - \lambda(t) \cdot 2 \cdot \varphi \cdot B(t) < 0$, which means that |H| > 0 and, hence, that the Hamiltonian is jointly and strictly concave in (H, B).

individual we have $\mathcal{H}_B(t)|_{B=B^*+\frac{1}{2\cdot\varphi}} > 0$, and $\mathcal{H}_B(t)|_{B=\overline{B}} < 0$. Then, since, by assumption, \overline{B} is affordable, we are guaranteed that for some $B(t) = \widehat{B_2}$, such that $B^* + \frac{1}{2\cdot\varphi} < \widehat{B_2} < \overline{B}$, $\mathcal{H}_B(t)|_{B=\widehat{B_2}} = 0$. Finally, a necessary and sufficient condition for optimal behaviour for a type-3 individual is: $v'\left(B^* + \frac{1}{2\cdot\varphi}\right) = k \cdot \frac{\pi}{p}$.

3.2 Phase diagrams

In this section we will explore the qualitative properties of possible solutions to the optimization problem (6). The phase diagrams (in state-control space) that we use distinguish between the three individual types. We begin by tracing out the $\frac{dH(t)}{dt} = 0$ and $\frac{dB(t)}{dt} = 0$ loci for all three types in the same diagram. Let h(t) denote the equation of motion for H(t):

$$h(t) \equiv \frac{dH(t)}{dt} = B(t) - \varphi \cdot (B(t) - B^*)^2 - \delta \cdot H(t).$$
⁽¹⁰⁾

In order to obtain the corresponding equation of motion for B(t), take the total time derivative of (9), and solve for $\frac{dB(t)}{dt}$, which yields: $\frac{d\lambda(t)}{dt} \cdot (1 - 2 \cdot \varphi \cdot (B(t) - B^*)) - (\lambda(t) \cdot 2 \cdot \varphi - \nu'')$, and, setting $\frac{dB(t)}{dt} = 0$:

$$\frac{dB(t)}{dt} = \frac{f(t)\cdot(1-2\cdot\varphi\cdot(B(t)-B^*))}{(\lambda(t)\cdot2\cdot\varphi-\nu'')} \equiv \frac{g(t)}{(\lambda(t)\cdot2\cdot\varphi-\nu'')}$$
(11)

where f(t) is defined by (8). The dynamics of the system is described by equations (10) and (11). The isoclines can be found by setting h(t) = g(t) = 0. Let us begin with the $\frac{dH(t)}{dt} = 0$ locus, for which it is possible to obtain an explicit expression. Rearranging the equation h(t) = 0yields: $H(t) = \frac{1+4\cdot B^* \cdot \varphi}{4\cdot \delta \cdot \varphi} - \frac{\varphi}{\delta} \cdot (B(t) - \frac{1/\varphi + 2B^*}{2})^2$. Figure 3 illustrates the principal shapes of the loci. The graphs drawn in the figure are obtained as follows: H(t) is a parabola having a vertex $(H^{max} = \frac{1+4\cdot B^* \cdot \varphi}{4\cdot \delta \cdot \varphi})$ at $B(t) = \frac{1}{2\varphi} + B^*$, and intersections with the B-axis at $B(t) = \frac{1}{2\varphi} + B^* \pm$ $\sqrt{\frac{1+4B^*\varphi}{4\varphi^2}}$. Notice that if the steady-state behaviour is $B(t) = B^*$, equation (2) implies that the steady-state health stock is $H(t) = \frac{B^*}{\delta}$. In the appendix, we show that the $\frac{dB(t)}{dt} = 0$ locus has one branch at each side of $B(t) = \frac{1}{2\varphi} + B^*$, and that it is decreasing in the left branch, increasing in the right, and concave in both. From equation (11) it is clear that a third $\frac{dB(t)}{dt} = 0$ locus is $B(t) = \frac{1}{2\varphi} + B^*$. When φ changes, the $\frac{dH(t)}{dt} = 0$ locus will change in the same way as the graph of I(t) in Figure 2.

Figure 3 about here

The shape of the loci and the admissible state-control set for the type-1 and type-2 individuals are illustrated in Figure 3. For each type, the admissible set is bounded by $\underline{H}, \underline{B}/\overline{B}$, and the locus that depicts the maximum level of the *B*-behaviour that is affordable for each level of health, B^{max} . B^{max} is found by setting Z(t) = 0 in the budget restriction. It is straightforward to show that the B^{max} -locus is increasing and convex. The shaded area in Figure 3 shows the admissible state-control set for the type 1 individual.

Steady state

Equilibrium points, (H^e, B^e) , in the state-control space are relevant, not only as predictors of individual behaviour, but as points of reference for the dynamics of individual behaviour predicted by the model. It is clear from the shape of the stationary-points loci that at most one steady-state is located in the interior of the admissible state-control set of type-1 and type-2 individuals. We summarize the relationship between the location of steady state and the rate of "punishment" for deviating from B^* , φ , and the stability properties of a steady state, in the following two claims (additional comparative-statics results, with respect to other parameters of the model, are reported in the appendix):

Claim 1: the effects on steady state (H^e, B^e) of an increase in φ are:

(*i*) for type 1:
$$\frac{dH^e}{d\varphi} \leq 0$$
 (0 when $B^e = B^*$); $\frac{dB^e}{d\varphi} \geq 0$ when $B^e \leq B^*$ (0 when $B^e = B^*$); and
 $\frac{dB^e}{d\varphi} >< 0$ when $B^* < B^e < \frac{1}{2 \cdot \varphi} + B^*$;
(*ii*) for type 2: $\frac{dH^e}{d\varphi} < 0$ and $\frac{dB^e}{d\varphi} < 0$; and
(*iii*) for type 3: $\frac{dH^e}{d\varphi} = 0$ and $\frac{dB^e}{d\varphi} = 0$.

Proof. The proof is a straightforward comparative-static computation. See appendix.

The stability properties of steady state are summarized in Claim 2:

Claim 2: a steady state is saddle-point stable for types 1 and 2, and globally stable for type 3. *Proof.* See appendix.

The intuition behind the results for the type-1 individual is as follows. *First*, consider the case when $B(t) \leq B^*$: then an increase in the rate at which deviating from B^* is "punished" will have a negative impact on the equilibrium demand for health capital, since each amount of *B* will produce a smaller amount of gross investments in health. However, when the health stock decreases, the marginal utility value of future health capital produced by *B* goes up, due to $\lambda(t) \cdot (1 - 2 \cdot \varphi \cdot (B(t) - B^*))$ (both $\lambda(t)$ and φ increases), which means that the marginal instantaneous utility of *B* must also increase (due to (9)). Thus, B^e must increase in this case. *Second*, when $B^* < B(t) < \frac{1}{2\cdot\varphi} + B^*$, the marginal utility value of future health capital produced by *B* produced by *B* must increase in this case.

3.3 Trajectories and solutions

The dynamic properties of the model for different points in the state-control space can be expressed using h(t) and g(t). Taking the derivative with respect to H(t) of respective function, leaving out the arguments, results in $h_H = -\delta$, and $g_H = f_H \cdot \frac{(1-2\cdot\varphi \cdot (B(t)-B^*))}{(\lambda(t)\cdot 2\cdot\varphi - u'')} > (<) 0$ when $B(t) < (>) \frac{1}{2\cdot\varphi} + B^*$. This means that $\frac{dH(t)}{dt} > 0$ below the $\frac{dH(t)}{dt} = 0$ locus, and $\frac{dH(t)}{dt} < 0$, above it; and, further, that $\frac{dB(t)}{dt} > (<)0$ below the $\frac{dB(t)}{dt} = 0$ locus when $B(t) < (>) \frac{1}{2\cdot\varphi} + B^*$. Figures 4a-c illustrates the dynamic behaviour of the three different types of individuals and solutions to the optimization problem (6).

Figure 4a about here Figure 4b about here Figure 4c about here

Interpretation

Figures 4a-c are constructed in the same way as Figure 3. In Figures 4a-c we have added trajectories in the state-control space. For the type-1 individual (Figure 4a) we have to consider the left part of Figure 3 (to the left of $B(t) = \frac{1}{2\cdot\varphi} + B^*$). At $H(0) = H_0$ the direction of each trajectory depends on the location of B(0). Any B(0) to the right of the equilibrium level, B^e , implies a trajectory which is inconsistent with the transversality condition and, hence, cannot be a solution to (6). The trajectory **C** is an example of such a case. Trajectories **A** and **B**, both fulfill the optimality and transversality condition and are solutions to (6), albeit with different planning horizons (different Ts). Several other locations of the isoclines and initial and end states may be analyzed using modified versions of Figure 4a. For the type-2 individual, similar conclusions can be drawn, using Figure 4b. Trajectories **B** and **C** are solutions to (6) for different planning

horizons, while trajectory A does not meet the transversality condition. For the type-2 individual, any control starting point, B(0), which is at a level *lower* than the equilibrium level, B^e , is inconsistent with the transversality condition and, hence, cannot be a solution to (6).

In more detail, trajectories that are consistent with the transversality condition $\lambda(T) = 0$ are depicted by setting $\lambda(T) = 0$ in (9): $\mathcal{H}_B(T) = v' - k \cdot \frac{\pi}{p} + \lambda(T) \cdot (1 - 2 \cdot \varphi \cdot (B(T) - B^*)) = 0$, which gives $v' - k \cdot \frac{\pi}{p} = 0$. Thus, as time approaches the planning horizon, the level of the type 1 (2) *B*-behaviour approaches <u>*B*</u>(\overline{B}).

4. DISCUSSION

By introducing – into the theoretical framework of the demand-for-health model – a nonmonotonic influence of health-related behaviour on health as well as punishments with respect to health for deviations from a certain given activity level, B^* , we were able to identify three types of individuals and one unique equilibrium for each type, using the relation between the exerted level of the health-related behaviour and B^* . The effect on the equilibrium location of changes in exogenous parameters, in particular, the rate at which any deviation from B^* is "punished", was analysed. The qualitative properties of trajectories fulfilling both optimality and transversality conditions were illustrated in a series of phase diagrams. The relationship between the location of equilibria and the set of state-control trajectories that may solve the dynamic optimization problem faced by the individual was analysed.

The phase diagram for the type-1 individual, Figure 4a, illustrates two possible solutions in the control-state space, and one trajectory that does not fulfil the transversality condition which implies that either $B(T) = \underline{B}$ or $H(T) = \underline{H}$. It is clear from Figure 4a, that the location of the isoclines in relation to both initial health and end-point health, determines the location of

potential solution trajectories. Moreover, individual preferences for the *B*-behaviour play a critical role – the stronger the preferences for *B*, the further to the right is the vertical line $B(t) = \underline{B}$, and the smaller is the set of admissible optimal trajectories. At the point where $\underline{B} = B^e$, the type-1 individual cannot identify any control-state trajectory that meets both optimality and transversality conditions. Directly analogous conclusions can be drawn for the type-2 individual's optimal choices. Thus, one fundamental implication of the model is that there is not a continuous range of admissible B(0) values. Instead, the type-1 and type-2 individuals will choose initial *B*-behaviours within separate sets of values.

The type-3 individual is characterised by choosing exactly the physiological optimal level of *B* at all times. The optimal trajectory is vertical and goes from H_0 to the equilibrium amount of health capital. Thus, if the type-3 individual starts at a health level above the equilibrium level, health will decrease at the optimal trajectory. Notice, that the transversality condition is satisfied for the type-3 individual in steady state: $\lambda(T) = 0 \Rightarrow v'(T) - k \cdot \frac{\pi}{p} = 0$, which is fulfilled, since, by definition, for $B(T) = B^* + \frac{1}{2 \cdot \varphi}$, $v'\left(B^* + \frac{1}{2 \cdot \varphi}\right) = k \cdot \frac{\pi}{p}$.

The model developed in this paper is very rich in that it extends the reach of the theoretical toolbox for the analysis of a broad range of individual health and health-related behaviours, by taking into account that several behaviours may be non-monotonically related to health. We will illustrate the usefulness of the model by applying it to two specific issues: (1) the rate of behaviour-specific atrophy and (2) the somewhat extended role that time preferences play when non-monotonic effects are taken into account.

The fundamental notion behind this extended version of the demand-for-health model is that the relationship between health benefits produced by a specific behaviour and the activity level of

that behaviour may show an inverted U-shape. The steepness of the function that connects the level of behaviour and the resulting health effects reflects the rate at which the benefits diminish, when the individual exert more or less than the level where there is no atrophy. So, what conclusions can be drawn regarding individual decisions to partake in non-monotonic health behaviours that differ regarding this rate (φ)? First, the shape of the isoclines and the position of the corresponding equilibrium differ between behaviours characterised by different φ 's. This is so for all three types of individual. Second, different locations of isoclines and equilibrium mean that both the admissible state-control set and the set of trajectories that are potential solutions to problem (6) also differ between behaviours. The location of equilibrium in state-control space is determined (partly) by the size of φ - see *Claim 1*. The difference between behaviours is also reflected by the relative position of the isoclines, since any change in the location of an isocline will alter the partition of the state-control space in behavioural sub-regions. Figure 5 illustrates the difference between two different behaviours characterised by φ and $\varphi', \varphi < \varphi'$, for the type-1 individual in the case when $B(t) \leq B^*$. This means that the equilibrium corresponding to φ' will lie to the south-east of the equilibrium point in the φ case. The H-isocline will shift according the illustration in Figure 2, around the point $\left(\frac{B^*}{\delta}, B^*\right)$. The shift in the *B*-isocline is indeterminate, although some shifts can be ruled out based on Claim 1.

Figure 5 about here

The influence of time preferences differs between the type-1 and the type-2 individual. For both types, the equilibrium level of health capital would decrease, while the equilibrium level of the *B*-behaviour would decrease for the type-1 and increase for the type-2 individual, if the future was discounted heavier. Thus, as is clear from Figure 4, for the type-1 individual B^e would move closer to <u>B</u>, which means that the range of *B*-behaviours that are consistent with both optimality

and transversality conditions would shrink. Likewise, for the type-2 individual B^e would move closer to \overline{B} , which would reduce the set of potentially optimal trajectories. Differences in time preferences are often suggested as a contributor to the different levels of investment in human capital that are observed – the more farsighted individuals, the more investments in health and, hence, the more advantageous is the level of public health. Our analysis demonstrates that this conclusion is valid also for behaviours which have a non-monotonic influence on health.

The preceding analysis implies that, in general, health-related public policy has to take into account that many behaviours may not be consistently bad or good for one's health but rather that the beneficial or detrimental effects depend on the individually chosen activity level of the behaviour in question. Thus, a first-best health policy would distinguish between individuals who exert low amounts and individuals who exert high amounts of a specific health-related behaviour. An illustrative and, perhaps, provocative, example is alcohol consumption. Given that there is a physiologically optimal level (strictly greater than zero) of alcohol consumption, taxing individuals that consume above a certain threshold level, and maybe subsidizing those who consume below the threshold, would increase population health, ceteris paribus. Obviously, the same qualitative conclusion can be made concerning all health-related behaviours that may influence health both positively and negatively. Thus, in order to affect such behaviours in a health-promoting way, policy-makers would, in principle, have to incorporate not only knowledge about the relationship between health and the target behaviour, but also a mechanism that is dependent on the type of individual that will be affected. The lesson for policy-makers is to rely less on general public-health policies and more on tailor-made measures for specific target groups.

APPENDIX

Begin by noticing that along the *B*-stationary locus, we have f(t) = 0 (take the time-derivative of (9)). Then, we need to establish the sign of f(t)'s partial derivatives, using $f(t) = -u' + k \cdot \frac{w}{p} \cdot \tau_H + (\delta + \rho) \cdot \lambda(t)$, and $\lambda(t) = \frac{k \cdot \frac{\pi}{p} - v'}{(1 - 2 \cdot \varphi(B(t) - B^*))}$: $f_H(t) = -u'' + k \cdot \frac{w}{p} \cdot \tau_{HH} > 0$; $f_{HH}(t) = 0$; $f_B(t) = (\delta + \rho) \cdot \frac{-v''}{(1 - 2 \cdot \varphi(B(t) - B^*))} + 2 \cdot \varphi \cdot (\delta + \rho) \cdot \frac{k \cdot \frac{\pi}{p} - v'}{(1 - 2 \cdot \varphi(B(t) - B^*))^2} > < 0$; $f_{BB}(t) = -(\delta + \rho) \cdot \frac{v'' \cdot 2 \cdot \varphi}{(1 - 2 \cdot \varphi(B(t) - B^*))^2} + 2 \cdot \varphi \cdot (\delta + \rho) \cdot \frac{v'' \cdot 2 \cdot \varphi \cdot (1 - 2 \cdot \varphi(B(t) - B^*))^2}{(1 - 2 \cdot \varphi(B(t) - B^*))^4} > 0$, since $\left(k \cdot \frac{\pi}{p} - v'\right) \cdot 2 \cdot \varphi \cdot (1 - 2 \cdot \varphi(B(t) - B^*)) > 0$.

Notice, that $f_B(t) > 0$ but $f_B(t) \cdot (1 - 2 \cdot \varphi \cdot (B(t) - B^*)) > 0$.

The steady state loci

The
$$\frac{dB(t)}{dt} = 0$$
 loci

10(1)

In order to obtain the $\frac{dB(t)}{dt} = 0$ loci, notice that g(t) = 0 implies that: $g(t) = \frac{d\lambda(t)}{dt} \cdot (1 - 2 \cdot \varphi \cdot (B(t) - B^*)) = 0$. When $(1 - 2 \cdot \varphi \cdot (B(t) - B^*)) \neq 0$, the implicit function theorem yields:

$$\frac{dH}{dB} = -\frac{f_B(t)\cdot(1-2\cdot\varphi\cdot(B(t)-B^*))-f(t)\cdot2\cdot\varphi}{f_H(t)\cdot(1-2\cdot\varphi\cdot(B(t)-B^*))} = -\frac{f_B(t)\cdot(1-2\cdot\varphi\cdot(B(t)-B^*))}{f_H(t)\cdot(1-2\cdot\varphi\cdot(B(t)-B^*))}.$$

In order to infer the curvature of the $\frac{dB(t)}{dt} = 0$ loci, take the implicit derivative of $\frac{dH}{dB}$, which is (leaving out arguments for brevity): $\frac{d^2H}{dB^2} = -\frac{(f_{BB}+f_{BH}\cdot\frac{dH}{dB})\cdot f_H - (f_{HH}\cdot\frac{dH}{dB}+f_{HB})\cdot f_B}{f_H^2} = -\frac{f_{BB}}{f_H} < 0$,¹¹ which means that the $\frac{dB(t)}{dt}$ - locus is decreasing in the left branch, and increasing in the right, and concave. In the case when $(1 - 2 \cdot \varphi \cdot (B(t) - B^*)) = 0$ the locus is the vertical line at $B(t) = \frac{1}{2\cdot\varphi} + B^*$. The shape of the the $\frac{dB(t)}{dt} = 0$ locus, combined with the previously shown

 ${}^{11}f_{HH} = f_{HB} = f_{BH} = 0.$

shape of the $\frac{dH(t)}{dt} = 0$ locus, establish that there is one unique steady-state point for each individual type.

Comparative statics - type 1 and 2

For a change in a parameter, x, the effects on steady-state levels of health capital and the B-behaviour, H^e and B^e , can be obtained by applying Cramer's rule to the following system (arguments left out). Notice, in steady state, $g_B = f_B(t) \cdot (1 - 2 \cdot \varphi \cdot (B^e - B^*))$, $g_H = f_H(t) \cdot (1 - 2 \cdot \varphi \cdot (B^e - B^*))$, and $g_{\varphi} = f_{\varphi}(t) \cdot (1 - 2 \cdot \varphi \cdot (B^e - B^*))$. For the type-1 and 2 individuals we have:

$$\begin{pmatrix} h_H & h_B \\ g_H & g_B \end{pmatrix} \cdot \begin{pmatrix} \frac{dH}{dx} \\ \frac{dB}{dx} \end{pmatrix} = \begin{pmatrix} -h_x \\ -g_x \end{pmatrix}.$$

 $J_s = \begin{pmatrix} h_H & h_B \\ g_H & g_B \end{pmatrix}$ is the Jacobian matrix of equations (9) and (11) evaluated in steady state.

Applying Cramer's rule in the case of a change in φ , we have: $\begin{pmatrix} \frac{dH}{d\varphi} \\ \frac{dB}{d\varphi} \end{pmatrix} = \begin{pmatrix} \frac{\begin{vmatrix} -n\varphi & nB \\ -g\varphi & gB \end{vmatrix}}{|J_S|} \\ \frac{\begin{vmatrix} nH & -n\varphi \\ gH & -g\varphi \end{vmatrix}}{|J_S|} \end{pmatrix}$.

The sign of
$$|J_s|$$

$$|J_s| = \begin{vmatrix} -\delta & (1 - 2 \cdot \varphi \cdot (B^e - B^*)) \\ f_H(t) \cdot (1 - 2 \cdot \varphi \cdot (B^e - B^*)) & f_B \cdot (1 - 2 \cdot \varphi \cdot (B^e - B^*)) \end{vmatrix}$$

Since $f_H(t) > 0$; $f_B(t) \cdot (1 - 2 \cdot \varphi \cdot (B^e - B^*)) > 0$, the determinant is always negative.

The steady state effects of φ

Applying Cramer's rule to the equations system above gives, for H^e :

$$\frac{dH^{e}}{d\varphi} = \frac{(B^{e}-B^{*})^{2} \cdot g_{B} + g_{\varphi}(t) \cdot (1-2 \cdot \varphi \cdot (B^{e}-B^{*}))}{|J_{S}|} = \frac{(B^{e}-B^{*})^{2} \cdot f_{B}(t) \cdot (1-2 \cdot \varphi \cdot (B^{e}-B^{*})) + f_{\varphi}(t) \cdot (1-2 \cdot \varphi \cdot (B^{e}-B^{*}))^{2}}{|J_{S}|} = \frac{(B^{e}-B^{*})^{2} \cdot f_{B}(t) \cdot (1-2 \cdot \varphi \cdot (B^{e}-B^{*})) + (\delta+\rho) \cdot \frac{2 \cdot (B^{e}-B^{*})}{(1-2 \cdot \varphi (B^{e}-B^{*}))} \cdot \lambda(t) \cdot (1-2 \cdot \varphi (B^{e}-B^{*}))^{2}}{|J_{S}|} = \frac{(B^{e}-B^{*})^{2} \cdot f_{B}(t) \cdot (1-2 \cdot \varphi \cdot (B^{e}-B^{*})) + (\delta+\rho) \cdot 2 \cdot (B^{e}-B^{*}) \cdot (k \cdot \frac{\pi}{p} - v)}{|J_{S}|} < 0$$

In order to see that $\frac{dH^e}{d\varphi} < 0$, use the second term in $f_B(t)$, and reformulate the second term in the ratio above to get the condition for $\frac{dH(t)}{d\varphi} < 0$: $(B^e - B^*)^2 \cdot 2 \cdot \varphi \cdot (\delta + \rho) \cdot \lambda(t) > 0$ $(\delta + \rho) \cdot 2 \cdot (B^e - B^*) \cdot \lambda(t) \cdot (1 - 2 \cdot \varphi(B^e - B^*)) \Longrightarrow (B^e - B^*)^2 \cdot \varphi > (B^e - B^*) \cdot (1 - 2 \cdot \varphi \cdot (B^e - B^*)).$ When $(B^e - B^*) > 0$ this reduces to the condition $B^e > \frac{1}{3 \cdot \varphi} + B^*$, which will always be fulfilled when $B^e > \frac{1}{2 \cdot \varphi} + B^*$. For $B^* < B^e < \frac{1}{2 \cdot \varphi} + B^*$, the conclusion follows immediately. For $B^e < B^*$, notice that $k \cdot \frac{\pi}{p} - v' > 0$ (follows from (9)), which makes the numerator is positive. When $B^e = B^*$, the numerator is 0.

For B^e , we have:

$$\frac{dB^e}{d\varphi} = \frac{-f_{\varphi}(t)\cdot(1-2\cdot\varphi\cdot(B^e-B^*))\cdot h_H(t)-(B^e-B^*)^2\cdot g_H(t)}{|J_S|} = \frac{\delta\cdot(\delta+\rho)\cdot 2\cdot(B^e-B^*)\cdot\lambda(t)-(B^e-B^*)^2\cdot f_H(t)\cdot(1-2\cdot\varphi\cdot(B^e-B^*))}{|J_S|},$$

which is < 0 if $1 - 2 \cdot \varphi \cdot (B^e - B^*) < 0$, and > 0 if $B^e < B^*$, and 0 when $B^e = B^*$. The sign is indeterminate when $B^* < B^e < \frac{1}{2 \cdot \varphi} + B_t^*$, due to the second term in the numerator.

Steady state effects of p

Applying Cramer's rule the equations system above (substituting φ for p), gives:

$$\frac{dH^{e}}{dp} = \frac{(\delta + \rho) \cdot \frac{k}{p} \cdot \pi_{p}}{|J_{S}|} \cdot \left(1 - 2 \cdot \varphi \cdot (B^{e} - B^{*})\right) < (>) 0 \text{ if } 1 - 2 \cdot \varphi \cdot (B^{e} - B^{*}) > (<) 0.$$

$$\frac{dB^{e}}{dp} = \frac{(\delta + \rho) \cdot \frac{k}{p} \cdot \pi_{p}}{|J_{S}|} \cdot \delta < 0.$$

Steady state effects of δ

First, $f_{\delta}(t) = \lambda(t)$. Then, again applying Cramer's rule to the equations system above (φ has been substituted for δ):

$$\frac{dH^{e}}{d\delta} = \frac{H(t) \cdot f_{B}(t) \cdot (1 - 2 \cdot \varphi \cdot (B^{e} - B^{*})) + \lambda(t) \cdot (1 - 2 \cdot \varphi \cdot (B^{e} - B^{*}))^{2}}{|J_{S}|} < 0$$

$$\frac{dB^{e}}{d\delta} = \frac{\delta \cdot \lambda(t) \cdot (1 - 2 \cdot \varphi \cdot (B^{e} - B^{*})) - H(t) \cdot f_{H}(t) \cdot (1 - 2 \cdot \varphi \cdot (B^{e} - B^{*}))}{|J_{S}|} > < 0$$

Steady state effects of E Proceeding as before gives:

$$\frac{dH^e}{dE} = \frac{(\delta + \rho) \cdot \frac{k}{p} \pi_E}{|J_S|} \cdot \left(1 - 2 \cdot \varphi \cdot (B^e - B^*)\right) > (<)0 \quad \text{if} \quad 1 - 2 \cdot \varphi \cdot (B^e - B^*) > (<)0, \quad \text{and}$$
$$\pi_E < (>)0.$$
$$\frac{dB^e}{dE} = \frac{(\delta + \rho) \cdot \frac{k}{p} \pi_E}{|J_S|} \cdot \delta < (>) 0 \text{ if } \pi_E > (<) 0.$$

Steady state effects of ρ

First, $f_{\rho}(t) = \lambda(t)$. Then, again applying Cramer's rule to the equations system above gives:

$$\frac{dH^e}{d\rho} = \frac{\lambda(t) \cdot \left(1 - 2 \cdot \varphi \cdot (B^e - B^*)\right)^2}{|J_s|} < 0$$

$$\frac{dB^e}{d\rho} = \frac{\delta \cdot \lambda(t) \cdot \left(1 - 2 \cdot \varphi \cdot (B^e - B^*)\right)}{|J_s|} < (>) 0 \text{ if } 1 - 2 \cdot \varphi \cdot (B^e - B^*) > (<) 0.$$

Comparative statics - type 1 and 2

For the type-3 individual, a change in the parameter x, we have: $\frac{dB^e}{dx} = 0$, except for $x = \varphi$. Thus, the change in H^e is given by (10) and $B(t) = B^e = \frac{1}{2\varphi} + B^*$: $H^e = \frac{1+4\cdot B^* \cdot \varphi}{4\cdot \delta \cdot \varphi} \Rightarrow H^e_{\varphi} < 0$ and $B^e_{\varphi} = -\frac{1}{2\varphi^2}$.

Summary of comparative statics results

Table A1. Comparative static results regarding steady-state levels of health and the *B*-behaviour. We assume that the effect of knowledge, E, on the one-unit cost, π , is negative. If the effect had been positive the results in the third raw would be reversed.

	Туре 1		Type 2	Туре 3
	$B^* < B^e < \frac{1}{2 \cdot \varphi} + B^*$	$B^e \leq B^*$	$B^e > \frac{1}{2 \cdot \varphi} + B^*$	$B^e = \frac{1}{2 \cdot \varphi} + B^*$
$\left(\frac{dH^e}{d\varphi},\frac{dB^e}{d\varphi}\right)$	-,-/+	-/0,+/0	-,-	-,0
$\left(\frac{dH^e}{dp},\frac{dB^e}{dp}\right)$	— , —	_,_	+,-	0,0
$\left(\frac{dH^e}{d\delta},\frac{dB^e}{d\delta}\right)$	-,-/+	-,-/+	-,-/+	-,0
$\left(\frac{dH^e}{dE},\frac{dB^e}{dE}\right)$	+,+	+,+	-,-	0,0
$\left(\frac{dH^e}{d\rho},\frac{dB^e}{d\rho}\right)$	_,_	_,_	-,+	0,0

Equilibrium properties

The cases when
$$B(t) \neq \frac{1}{2 \cdot \varphi} + B^*$$

The terms $G_H(t), G_B(t)$ of the Jacobian matrix J are obtained from $G(t) \equiv \frac{g(t)}{(\lambda(t) \cdot 2 \cdot \varphi - v'')} = \frac{f(t) \cdot (1 - 2 \cdot \varphi \cdot (B(t) - B^*))}{(\lambda(t) \cdot 2 \cdot \varphi - v'')}$. Taking the derivative with respect to H gives:
 $G_H(t) = \frac{(f_H(t) \cdot (1 - 2 \cdot \varphi \cdot (B(t) - B^*))) \cdot (\lambda(t) \cdot 2 \cdot \varphi - v'')}{(\lambda(t) \cdot 2 \cdot \varphi - v'')^2}$. Similarly, taking the derivative of $G(t)$ with respect to B yields: $G_B(t) = \frac{(-f(t) \cdot 2 \cdot \varphi + f_B(t) \cdot (1 - 2 \cdot \varphi \cdot (B(t) - B^*))) \cdot (\lambda(t) \cdot 2 \cdot \varphi - v'')}{(\lambda(t) \cdot 2 \cdot \varphi - v'')^2}$. For a steady state we have:
 $G_B(t) = \frac{(f_B(t) \cdot (1 - 2 \cdot \varphi \cdot (B(t) - B^*))) \cdot (\lambda(t) \cdot 2 \cdot \varphi - v'')}{(\lambda(t) \cdot 2 \cdot \varphi - v'')^2}$.

Together with h_H and h_B we are able to formulate:

$$|J| = -\delta \cdot \frac{f_B(t) \cdot \left(\cdot \left(1 - 2 \cdot \varphi \cdot (B(t) - B^*)\right) \right) \cdot (\lambda(t) \cdot 2 \cdot \varphi - \nu')}{(\lambda(t) \cdot 2 \cdot \varphi - \nu')^2} - \frac{\left(f_H(t) \cdot \left(1 - 2 \cdot \varphi \cdot (B(t) - B^*)\right)^2\right) \cdot (\lambda(t) \cdot 2 \cdot \varphi - \nu'')}{(\lambda(t) \cdot 2 \cdot \varphi - \nu'')^2} < 0.$$

|J| < 0 is a necessary and sufficient condition for a saddle point and, hence, the result follows.

The cases when
$$B_t = \frac{1}{2 \cdot \varphi} + B^*$$

In this case the determinant of the Jacobian matrix is zero, and the trace is strictly negative, i.e., one eigenvalue is zero and the other is strictly negative. This implies a sink.

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Figure 1. Relative risk of mortality in realtion to alcohol intake for middle-aged (-) and elderly (....) people. Risk was set att 1.00 at lowest mortality at 1-6 beverages per week. Vertical lines are 95% confidence intervals for point depicting estimates for all subjects. Reproduced from Grönbaeck et al. (1998) with permission of the Oxford University Press.

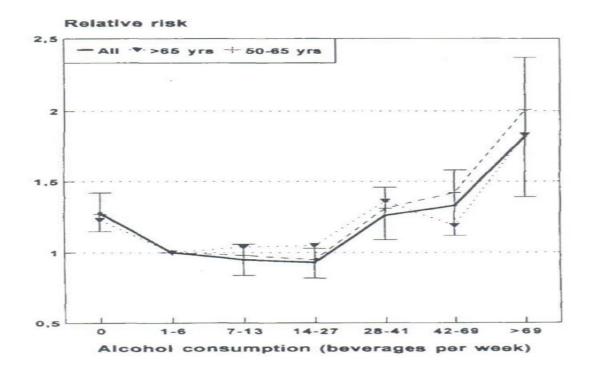


Figure 2. Illustration of the relationship between behaviour, *B*, and the amount of health investment, *I*. The parabola is the graph of the function $I(t) = B(t) - \varphi \cdot (B(t) - B^*)^2$. The maximum influence on health attainable through the behaviour, *B*, is at the inflexion point of the parabola. The solid-line parabola corresponds to the value φ , while the high-location dotted parabola corresponds to the value $\varphi' < \varphi$, and the low-location dotted parabola corresponds to the value $\varphi'' > \varphi$.

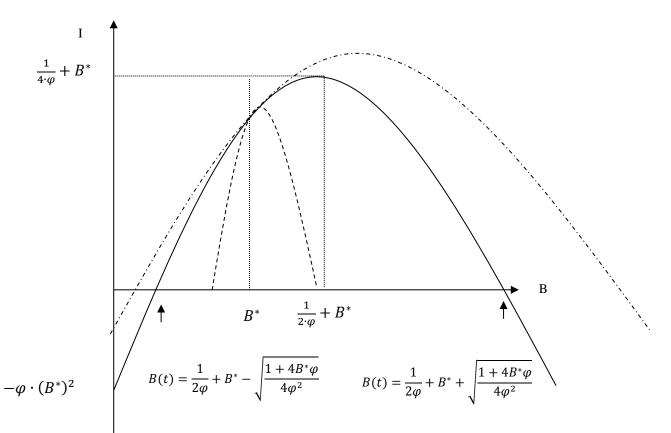


Figure 3. Illustration of stationary loci, and admissible sets, for the control- and state variable. Equilibrium points are marked with a dot. The parabola shows the $\frac{dH(t)}{dt} = 0$ locus, the hyperbolas the $\frac{dB(t)}{dt} = 0$ locus. The filled rectangle marks the admissible state-control set for the type 1 individual. The dotted curve, B^{max} , marks the maximum affordable level of B for each amount of health capital. Since we have assumed that less than the maximum affordable level of B is always demanded by all types, this curve is drawn below the admissible control sets.

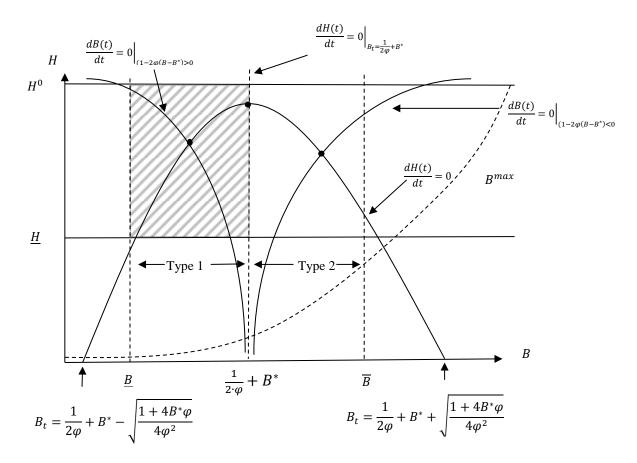


Figure 4a. Illustration of trajectories in state-control space, for the type-1 individual. Trajectories **A**, **B**, and **C** are admissible trajectories. Only **A** and **B** fulfil the transversality conditions and, hence, are both solutions to the optimization problem, but to different lengths of the planning period. The admissible state-control set is bounded by the lines $B(t) = \underline{B}$, $H(t) = \underline{H}$, $B(t) = \frac{1}{2\cdot\varphi} + B^*$, and $H(t) = H^0$.

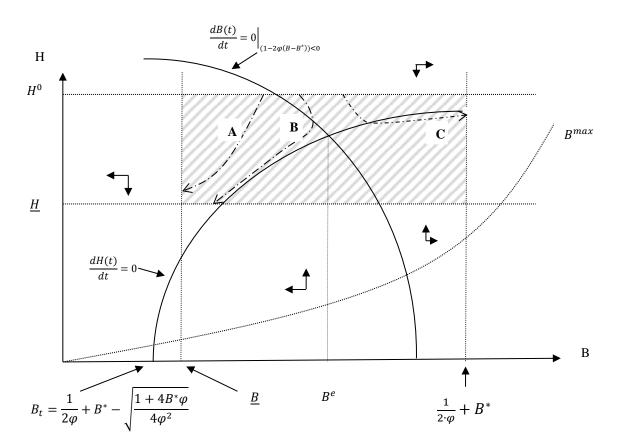


Figure 4b. Illustration of trajectories in state-control space, for the type-2 individual. Trajectories **A**, **B**, and **C** are admissible trajectories. Only **B** and **C** fulfil the transversality conditions and, hence, are both solutions to the optimization problem, but to different lengths of the planning period. The admissible state-control set is bounded by the lines $B(t) = \overline{B}$, $H(t) = \underline{H}$, $B(t) = \frac{1}{2\cdot\varphi} + B^*$, and $H(t) = H^0$.

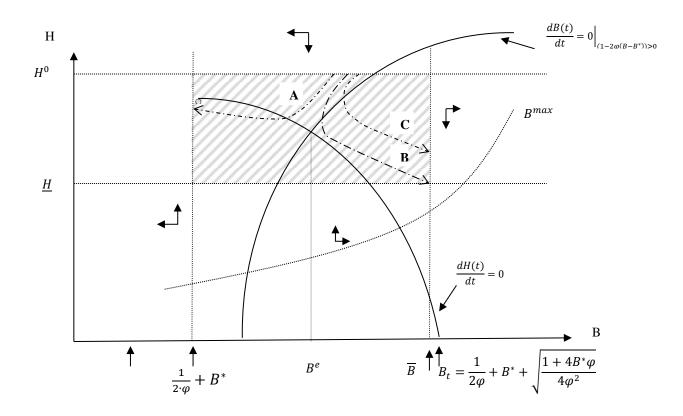


Figure 4c. Illustration of trajectories in state-control space, for the type-3 individual. The admissible state-control space is the "straight" trajectory **A**. This is also the unique solution to the optimization problem for the type-3 individual. The end-point state is the globally stable equilibrium point.

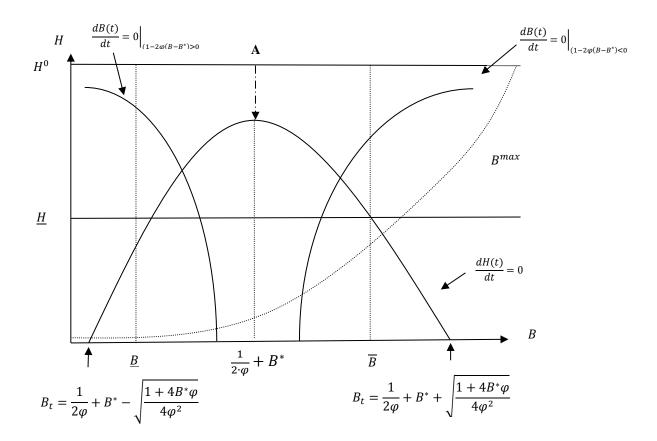


Figure 5a. Illustration of the differences between two different behaviours, distinguished by φ , for the type-1 individual when $B^e \leq B^*$. In this case, the equilibrium point moves down and to the right, which means that the range of B(0)'s that solve (6) increases.

