Conceptual design of a fifth generation unmanned strike fighter

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Unmanned aircraft have significantly transformed aerial warfare through a combination of new technologies, extended operational capabilities, and reduced risks and costs. Similarly, computational modelling techniques have accelerated the rate of development for aircraft by being able to explore a large number of design options from the earliest design stages, further reducing time, risks, and costs. The near future will see the proliferation of unmanned combat aerial vehicles under a variety of roles such as unmanned tankers, strike aircraft, and even air-to-air fighters. In this paper the GENUS aircraft design framework is used to develop an unmanned weapons carrying platform able to partially match the performance of 5th generation fighters such as the Joint Strike Fighter F-35A. The vision of future joint operations is for a single lead manned fighter to command and designate targets to its various *loyal wingmen* unmanned aircraft, extending the combat capabilities and significantly multiplying force and air superiority.

I. Nomenclature

$f(x)$	=	objective function
$g_j(x)$	=	inequality constraints
$h_k(x)$	=	equality constraints
x	=	input vector

II. Introduction

The recent developments on 5th generation stealth fighters, such as the F-35 program, has created a new demand not only for 5th generation aircraft, but for entire 5th generation air forces, where advanced designs are taken full advantage of by a highly integrated, collaborative network between air force, navy, army, and industry. It can be argued that the defining characteristic of 5th generation fighters, besides high degrees of stealth, is their advanced data processing and fusion, allowing them to perform in highly contested airspace in a networked manner [1].

The new class of 5th generation fighters allows for smoother integration of 4th generation 'legacy' aircraft that offer unique combat capabilities, as well as with the future generation of unmanned combat aerial vehicles (UCAVs) which can serve as weapon carrying platforms and force multipliers. This is indeed the vision of future aerial warfare as envisioned by various armed forces around the globe, as seen in Fig. 1.

Furthermore, a 5th generation UCAV aligns with the US Air Force 2030 air superiority vision by supporting the *Penetrating Counterair* (PCA) roles through an affordable and reliable platform able to engage in strike missions, and provide data through its advanced array of sensors and highly integrated avionics systems. Furthermore, swarms of UCAVs with limited performance and payload capabilities have been envisioned to play a significant role in the future of aerial warfare [2].

The mission requirements appropriate for this new class of unmanned aerial vehicles include ground strike capabilities, as well as limited supersonic air combat segments. An aircraft conceptual design analysis and optimization framework will be employed in order to evaluate numerous design options in order to establish feasible design solutions.

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Fig. 1 F-35 with loyal wingmen UCAVs (Source: US Air Force[3])

III. The GENUS aircraft design environment

The GENUS aircraft design environment is a flexible and robust aircraft conceptual design framework developed at Cranfield University's Aircraft Design group. GENUS consists of 9 essential, highly abstract modules and a set of special modules to meet specific design and analysis needs, as shown in Fig. 2; this framework relies heavily on polymorphism in order to achieve a flexible and robust aircraft design environment.

The core philosophy of the GENUS architecture is flexibility, robustness, and expandability; its name derives from the taxonomical classification of biological organisms representing its capability to design and analyze various aircraft *species* through a common framework and common analysis methodologies. The GENUS aircraft design environment has been applied to the conceptual design of hypersonic transports, blended wing body aircraft, solar-powered UAVs [3], supersonic business jets [4], and subsonic low-observable UCAVs [5]. A brief description of the GENUS modules is given in the subsections below.
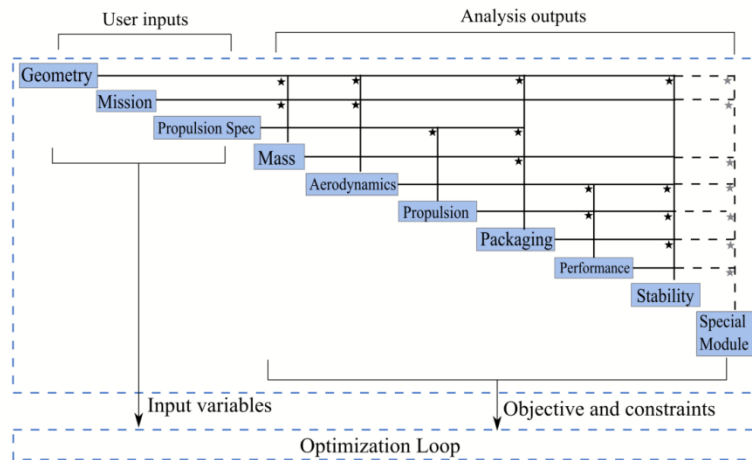

Fig. 2 Basic GENUS modules and interactions

A. Geometry

The geometry module consists of discrete geometrical elements divided into body components and lifting surfaces. Simple cross sectional shapes define the various sections of a body component allowing for the representation of basic fuselages, engine nacelles, and tail booms. Lifting surfaces are defined by sectional and planform characteristics. An airfoil library containing NACA4, NACA5, NACA6, biconvex, and hexagonal airfoils is available. Despite the simplicity, this module allows for great flexibility as shown in Fig. 3.

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[3] Still from US Air Force Research Lab promotional video "Air Force 2030 – Call to Action"
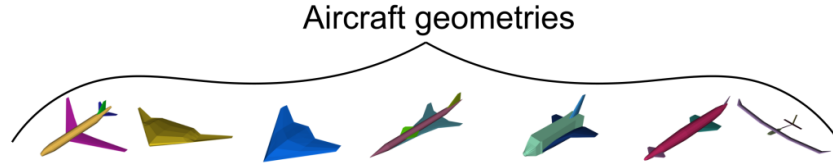
Fig. 3 Geometry flexibility in GENUS

B. Mission

The mission module defines the basic mission parameters such as cruise speed or Mach, cruise altitude, range, loiter, fixed and droppable payload, maximum longitudinal and vertical acceleration factors, as well as estimated maximum take-off mass. Additional mission requirements can be added in individual modules such as performance and stability.

C. Propulsion Specification and Analysis

This module sets the basic engine parameters such as type, number of engines of each type, dimensions, pressure ratios, materials, and type of fuel. Several engine types can be specified for missions that require transitional modes, such as for high supersonic or hypersonic configurations. For turbojet engines (afterburning and nonafterburning), turbofans, and ramjets, NASA's open source applet EngineSim has been included [6]. This simple tool allows the user to set an engine design point, which can then be frozen to obtain the off-design engine performance.

D. Mass Breakdown

Mass breakdown methods are design sensitive, avoiding purely statistical methods. In the case of UCAVs, this module follows the approach recommended by Gundlach [7, chap.6], where equations for manned fighters and unmanned vehicles are employed and modified to account for possible system differences. Other Class II methods are also included to account for structural, and systems masses[8,9].

E. Aerodynamics

GENUS contains various aerodynamic analysis packages, allowing for low fidelity, empirical, fast calculations up to medium fidelity potential flow solver for subsonic and supersonic speeds, like PANAIR. Flexibility and increased fidelity levels can be included through legacy code written in other programming languages. Source codes, C++ wrappers, and Java classes and native methods are compiled into a dynamic link library (DLL) through the process shown in Fig. 4. Aerodynamic analysis tools currently available in GENUS include Digital DATCOM [10], AVL [11], SHABP [12], PANAIR [13], FRICTION [14], and a modified Harris wave drag [15].
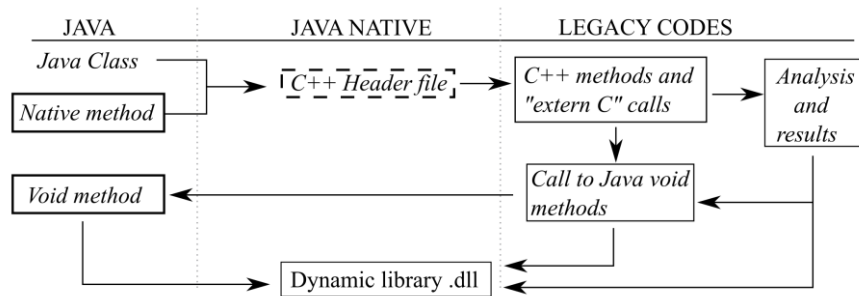

Fig. 4 Legacy code integration into GENUS through Java Native interface

F. Packaging and C.G.

This module calculates the available wing fuel tank volume, as well as the volumes of other internal components. Landing gear sizing and load calculation is also performed in this module. Internal weapon bays are sized depending on user-specified payload and weapon type. Internal components can be displaced in longitudinal and lateral direction to manage clashes and interferences.

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G. Performance

The full mission analysis is carried out in the performance module, as well as additional mission requirements such as point performance and maneuvers. A variety of methods are available for the analysis of field performance [16], energy optimized climb [17], various cruise segment types, descent profiles, and maneuver requirements.

This module determines if a design instance is able to comply with the basic mission and operational requirements. Some of the main outputs from this module are total fuel required, altitude-speed-attitude profiles, engine throttle settings, drag polar at various Mach-altitude conditions, and mass changes throughout mission segments. Additionally, individual 'flight conditions' can be set in order to investigate the stability and trim conditions.

H. Stability

Stability constraints such as static margin, maximum control effectors deflections, and CG range limit can be set in this module. Digital DATCOM's source code has been integrated into the stability analysis following the procedure shown in Fig. 6. Automatic geometry and control surface format conversion between GENUS and DATCOM formats allows the users to quickly size longitudinal and lateral control surfaces.

I. Radar Cross Section

Radar cross section (RCS) analysis forms part of the special modules, as it is not commonly used during aircraft conceptual design. This module converts the geometry into triangulated facets, and RCS analysis is carried out through physical-optics approximation adapted from the well-known and freely available POFACETS code [18]. Results have been verified against the original Matlab code for monostatic radar cross section of clean configurations with perfect electric conductor materials.

J. Optimizers

GENUS includes two algorithms for multivariate design optimization. A custom made genetic algorithm can be used to explore a large area of the design space for a given mission; results can be later refined by the robust LSGRG2 algorithm [19]. Currently, only single objective optimization is implemented.

IV. Mission Requirements

Operational and mission requirements have been derived from the AIAA's original subsonic unmanned strike fighter request for proposal [20], unclassified information on the F-35 program [21,22], as well as a generic air-to-air fighter mission [23, chap.1.11].

A conventional take-off and landing configuration is assumed. Payload capabilities have been estimated by assuming that a single lead manned fighter can command a formation of several UCAVs. The mission is summarized in Table 1 and Fig. 5. Performance and mass allowances are shown in Table 2.

Table 1 – Unmanned Strike Fighter Mission Profile

Phase	Description
1-2	Warm up and take-off. Fuel allowance of 5 min at idle power for taxi + 1 min mil power. Take-off distance ≤ 1500 m.
2-3	Minimum time to climb in mil power to cruise Mach and altitude (0.8M/12 km)
3-4	Subsonic cruise-climb, total range for climb and cruise is 1090 km
4-5	Descent to 250 m altitude and Mach 0.9
5-6	Low altitude subsonic ingress, total range 80 km, deliver air-to-surface payload
6-7	Low altitude subsonic egress, 80 km 0.9M/250 m
7-8	Subsonic minimum time to climb to Mach 0.8 and 9.5 km
8-9	Accelerate to Mach 1.5 and perform supersonic scape dash and combat for 50 km in mil power. Combat includes one 360 deg, 5g sustained turn and firing 2 AIM-132.
9-10	Minimum time to climb to 12 km and Mach 0.8.
10-11	Subsonic cruise climb at Mach 0.8 and 12 km, until total range after egress is 1090 km.
11-12	Descend and land. Landing distance must be ≤ 1500 m.

Table 2 – Performance requirements

Payload	Fully internal, 2 x 2000 lbs Mk 84 and 2 x AIM-132 ≈ 2030 kg
Field performance	Conventional take-off and landing ≤ 1500 m
Ceiling	Above 15 km

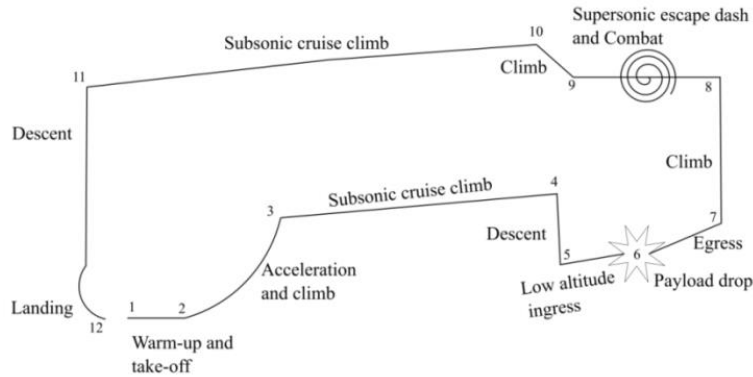| Supercruise	1.5M/9.5 km
Instantaneous G	+7.5, 0.75M/4500 m
Specific Excess Power	*(1g)* 120 m/s at Mach 0.8, 4.5 km altitude with 50% fuel and 2 x AIM-132
Acceleration	Mach 0.8 to 1.2 in < 120 seconds at 9.5 km altitude max power
Sustained Turn Rate	+5g at 1.5M/9.5 km with 25% fuel and 2 x AIM-132
Avionics	Advanced sensor package, 300 kg allowance
Stealth	Very low signature, 200 kg allowance

Fig. 5 Mission schematic for a 5th generation UCAV

As can be seen from the mission segments, wing size and wing loading demands imposed by subsonic cruise and instantaneous turn rate oppose those for supersonic, and low-altitude, high-speed flight. Furthermore, typical means of achieving good aerodynamic performance during subsonic flight (low sweeps, high aspect ratios) will stand contrary to efficient design strategies for transonic and supersonic mission segments.

V.   UCAV Design and Analysis of Results

An initial parametric analysis has been performed for the mission requirements shown in Section III, the initial design point is shown in Fig. 6 alongside other subsonic UCAVs and the F35-A. From the figure, it can be seen that specific excess power and acceleration requirements are likely to drive the engine size. Gross mass has been estimated at 18,000 kg, requiring a wing area of 50.45 m^2, and sea level thrust of 125.4 kN.

This analysis has been performed with low fidelity methods and will only serve as a starting point for dimensioning the configurations. The dominating design constraints might vary significantly by applying higher fidelity methodologies.
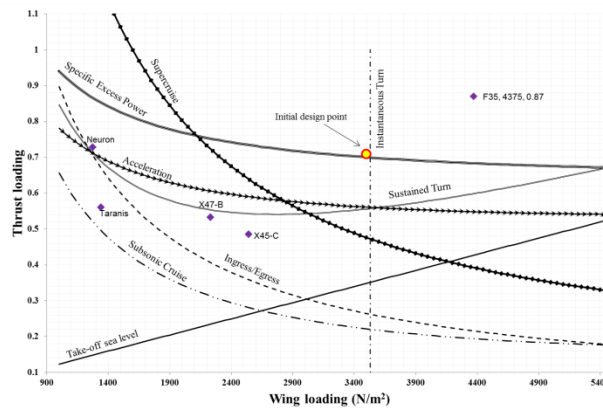

Fig. 6 Parametric analysis and initial design point wing and thrust loading

A flying wing design has been assumed through the initial design process due to its inherent low observability characteristics. The baseline configuration consists of a highly swept central section (Λ_{LE}=72°) acting as a fuselage, followed by a moderate sweep outer wing (Λ_{LE}=53°). NACA 63 airfoils have been assumed as the initial choice. A central, buried turbojet engine has been sized for all flight conditions and performance requirements. The payload

has been divided into two internal weapon bays. Figure 7 shows a plan view of the baseline UCAV design superimposed on an F35-A, as well as a schematic arrangement of internal components.

The initial mass estimate has been refined through the GENUS methodologies and a significantly lower mass was found. The resulting take-off mass is 12190 kg, with a fuel consumption of 2210 kg, and an empty mass of 7950 kg. The dominating design constraint was found to be the engine thrust requirements during the supersonic dash segment at 9.5 km altitude, as well as sustained turn requirements at supersonic speeds.
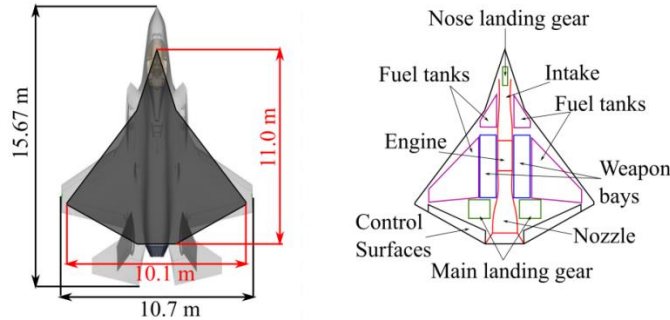

Fig. 7 Top view comparison to F35-A[4] and packaged UCAV

A. Airfoil trade-offs

The overall aerodynamic choice should reflect the subsonic, transonic, and supersonic compromise resulting from the mission requirements. Good subsonic aerodynamic performance dictates certain geometric and airfoil choices that will result in poor supersonic performance. The effect of typical subsonic airfoils compared to transonic and purely supersonic airfoils are shown in terms of the mission segment fuel and drag polar plots at various Mach/altitude conditions in Figs. 8 and 9.

While aerodynamic performance during subsonic cruise segments is very similar for all airfoils, the advantages of supercritical and supersonic airfoils are obvious for transonic and supersonic Mach numbers. During the low-altitude, high-speed ingress/egress segments the SC(2)-0406 supercritical airfoil reduces compressibility drag by 15% and 30% when compared to NACA63$_1$-207 and NACA2307 airfoils respectively. In the case of supersonic flight, the supercritical airfoil matches the performance of the biconvex airfoil. In summary, choosing a supercritical airfoil for the outer wing segment reduces the maximum take-off mass by 5.3%, and fuel by 6.5% for a leading edge sweep angle of 53°.
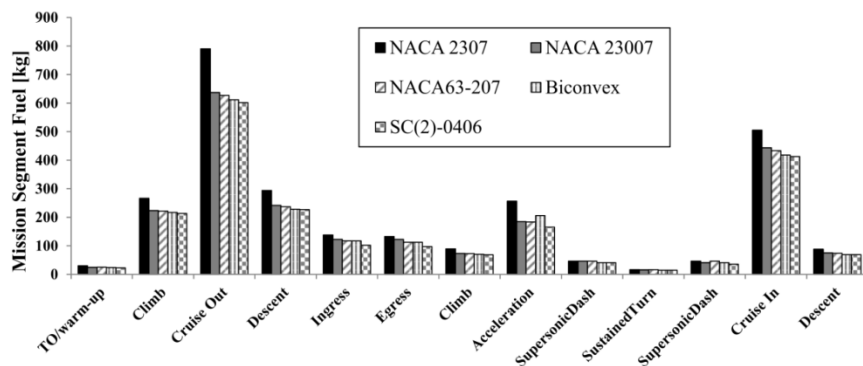

Fig. 8 Effect of airfoil on mission segment fuels

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[4] Wikimedia Commons https://commons.wikimedia.org/wiki/File:F-35A_three-view.PNG
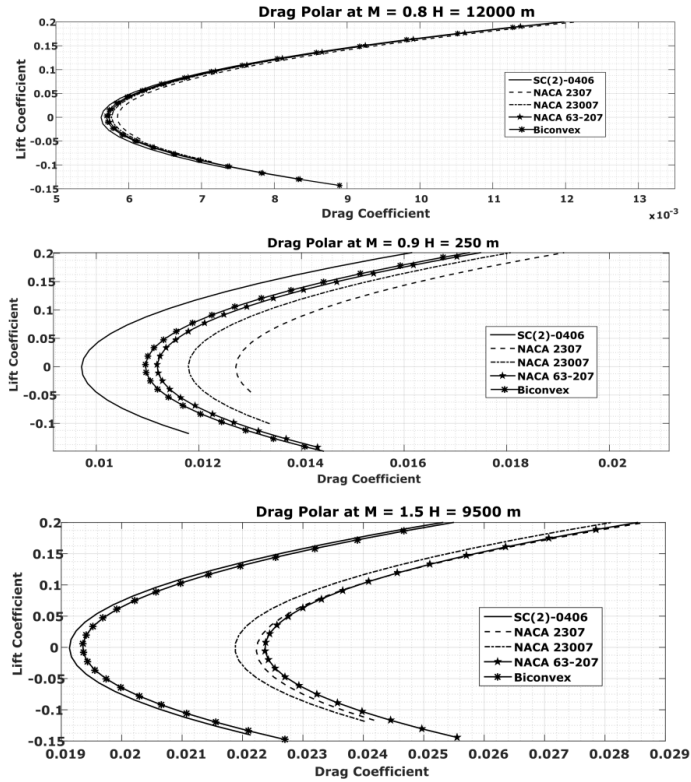
Fig. 9 Drag polar plots for subsonic, transonic, and supersonic airfoils

B. Outer Wing Sweep Angle

The leading edge sweep angle has a strong influence on aerodynamic performance, fuel consumption and engine sizing. Also, higher sweep angles often result in higher wing masses, therefore the weight advantages and penalties need to be accounted for to identify viable sweep angle ranges that can be later refined through multivariate optimization. Trade-off studies for the outer wing leading edge sweep shown in Fig. 10 demonstrate that sweep angles below 50 degrees result in aerodynamic and fuel penalties for transonic and supersonic flight segments. Configurations with sweep angles higher than 60 degrees show that structural mass penalties outweigh the aerodynamic advantages.
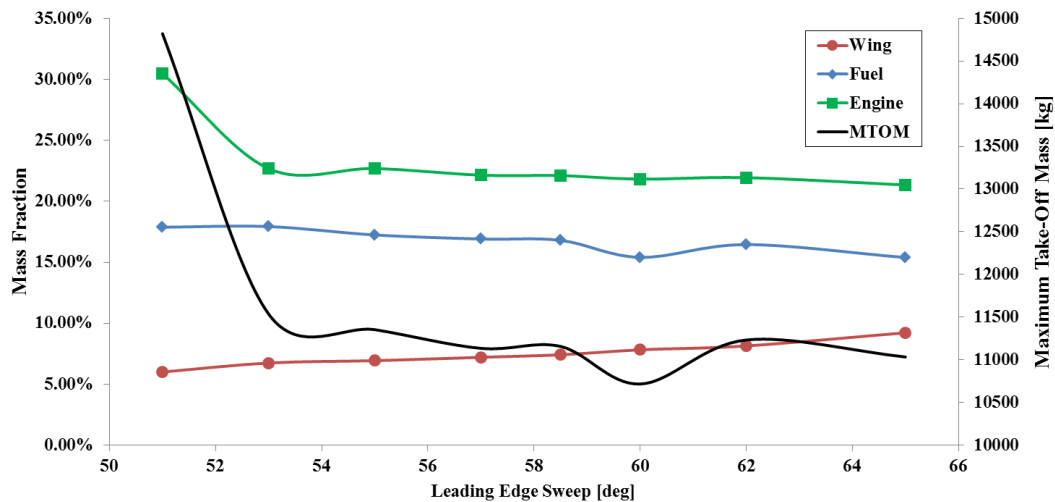

Fig. 10   Leading edge sweep effect on vehicle and component masses

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C. Engine By-pass Ratio

Additionally, changes in by-pass ratio have been investigated for afterburning turbofans and compared to the initial afterburning turbojet engine. Results have been normalized with respect to the original afterburning turbojet configuration. Figure 11 shows that despite the fact that the fuel consumption decreases for by-pass ratios above 0.4, overall vehicle masses are still higher, due to the heavier turbofan engine. However, afterburning turbofan engines can reduce the infrared signature due to reduced plume temperatures, as well as the temperature of surrounding structures, and should still be considered a viable option in further design stages where a more comprehensive low observability analysis is performed.
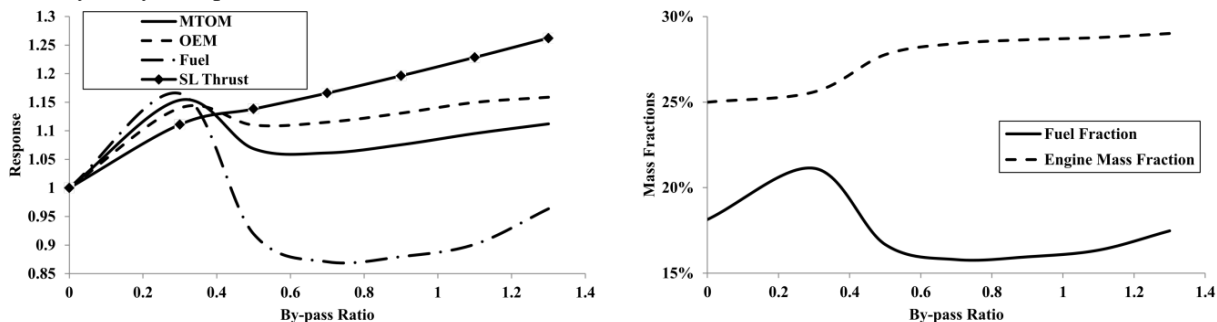

Fig. 11   By-pass ratio effects on vehicle mass, required thrust and fuel consumption

D. Multidisciplinary Optimization

The trade-off studies shown above have been used to select some of the aircraft's characteristics. A supercritical airfoil SC(2)-0406 will be used for the outer wing section, along with a central buried afterburning turbojet engine. Improved engine modelling has been adopted for the optimization results below in order to arrive at a more realistic fuel consumption; overall engine efficiency does not exceed 60%.

Multivariate optimization will be used to find a configuration with minimum take-off mass, while also subjecting the design to static longitudinal stability and trim during all flight conditions.

The optimization problem can be formally defined as:
- Minimize: $f(x)$
- Subject to:
  - $g_j(x) \leq 0 \; for \; j = 1,2,\dots,J$
  - $h_k(x) = 0 \; for \; k = 1,2,\dots,K$
  - $x_i^L \leq x_i \leq x_i^U \; for \; i = 1,2,\dots,N$

Design variables, upper and lower boundaries, and design and operational constraints are given in Table 3.

Table 3   Design inputs and constraints

Input Variable	Lower Bound	Upper Bound
Outer wing sweep [degrees]	45	70
Outer wing span [m]	2.9	4.0
Outer wing taper ratio [-]	0.01	0.4
Fuel fraction [%]	15	40
Engine diameter [m]	0.5	1.2
Component positions [m]	Component dependent	

Constraint	Type
Maximum take-off mass error	= 0
Fuel volume	≥ Required
Fuel mass error	= 0
Acceleration time	≤ Required
Specific excess power	≥ Required
Sustained turn thrust	≥ Required
Cruise segments thrust	≥ Required
Static margin(All Flight Conditions)	-15%≤ k_n ≥15%

Generational histories of outer wing sweep angle and maximum take-off mass, as well as mass convergence error and fuel mass compared against engine diameter are shown in Fig. 12 below. As can be seen, the main geometric and mass values converged after only 10 generations; however, some performance parameters were not

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compliant at the end of the evolutionary optimization. A robust gradient based optimizer has been used to finalize the engine size and fuel consumption.
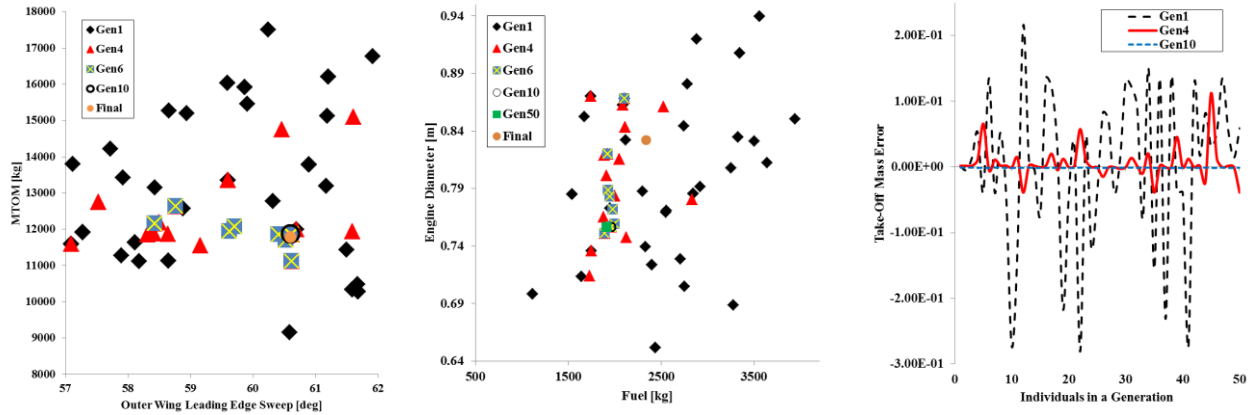

Fig. 12   Generational history of optimization variables and convergence errors

The final vehicle characteristics consist of a maximum take-off mass of 11791 kg, a total fuel consumption of 2336 kg, and an outer wing leading edge sweep angle of 60.6° with supercritical SC(2)-0406 airfoils. The engine consists on a buried afterburning turbojet, with a diameter of 0.84 m and a sea level thrust (dry) of 93 kN. Payload is distributed inside fully internal twin weapon bays on the sides of the engine. A schematic top view, mass breakdown, and a preliminary CAD are shown in Fig. 13 below. Table 3 shows a comparison between the F-35A and the *loyal wingman* UCAV.
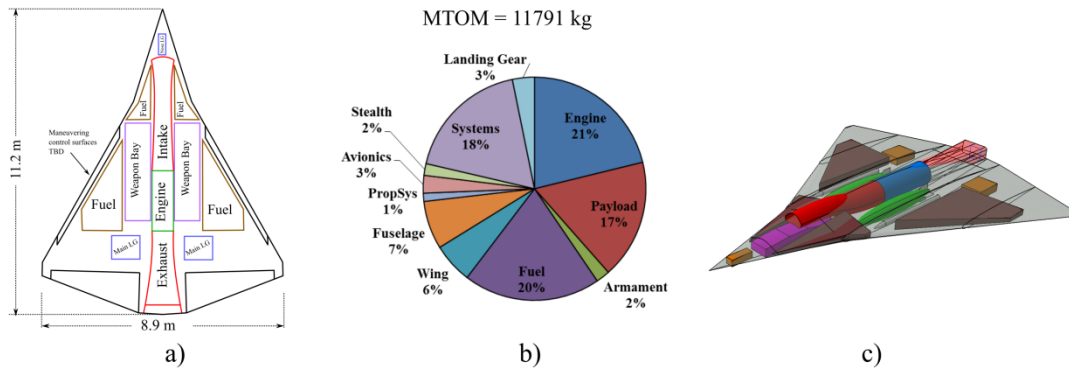

Fig. 13   a) Top view of packaged UCAV, b) mass breakdown, c) preliminary CAD

Table 3 – Comparison of F-35A and UCAV

Parameter	F-35A	UCAV
Total Length [m]	15.67	11.2
Wing span [m]	10.7	8.9
Wing Surface [m^2]	42.7	47.73
Empty Weight [kg]	13300	7425
Maximum Take-Off Weight [kg]	31800	11790
Internal payload capacity [kg]	1820 (approx..)	2030
Maximum operating Mach	1.8	1.76
Dry Thrust (Sea Level) [kN]	125	93
Wet Thrust (Sea Level) [kN]	191	112

Mass, altitude, Mach number, and angle of attack profiles are given in Fig. 14, while fuel scheduling and static margin throughout the mission segments are given in Fig. 15. It can be seen that the configuration is longitudinally stable for all mission segments except for the initial climb segment. Trim analysis has been performed by assuming elevons in the outer wing section with an inboard chord fraction of 20%.

Other control surfaces, such as leading edge maneuvering controls, belly flaps, spoilers, or airbrakes have not been determined and will be the subject for future detailed studies.
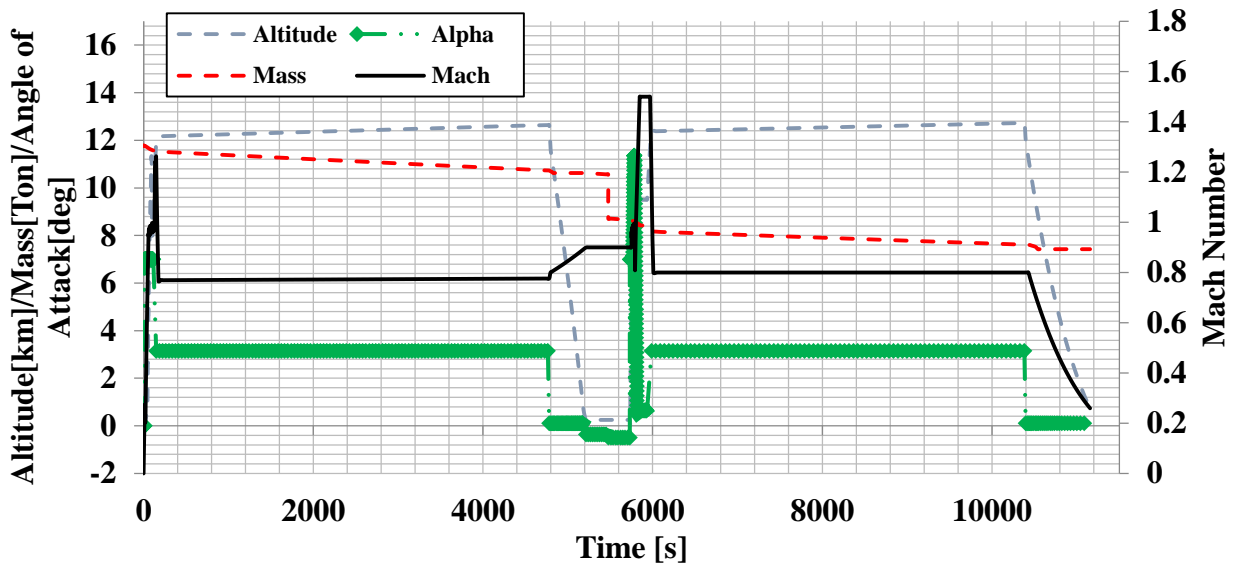
Fig. 14   Mass, Mach, altitude, and angle of attack mission profiles
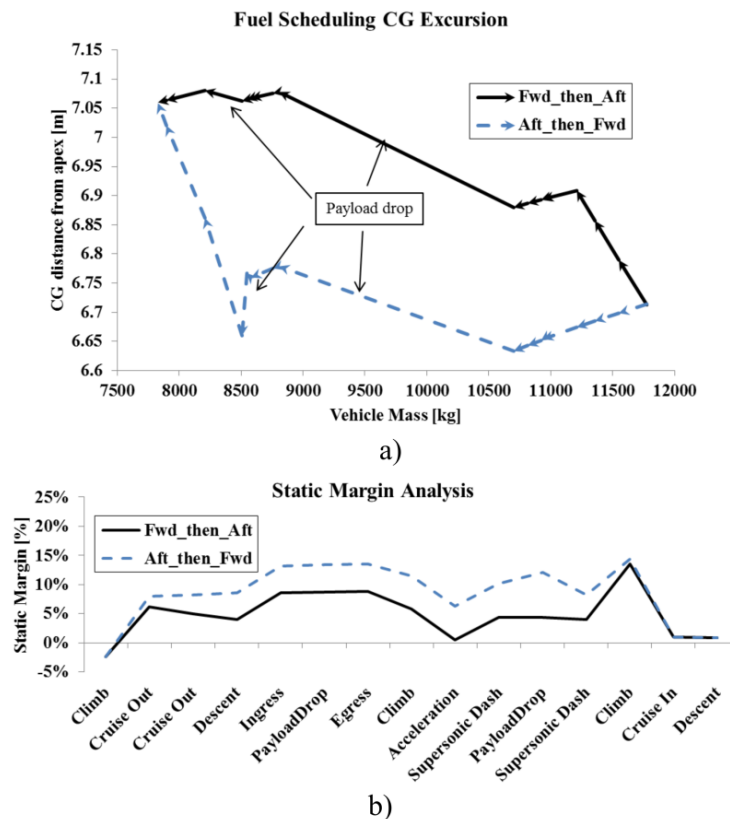

a)

b)

Fig. 15   a) Fuel scheduling and b) static margin throughout the mission

Aerodynamic results showing friction and wave drag, as well as the induced drag factor are shown in Fig.16 (a) plotted against Mach number; subfigure (b) shows the radar cross section at various radar frequencies for a clean geometry assuming perfect electric conductor materials; subfigures (c) and (d) show specific excess power maps at level flight and supersonic sustained turn conditions respectively.
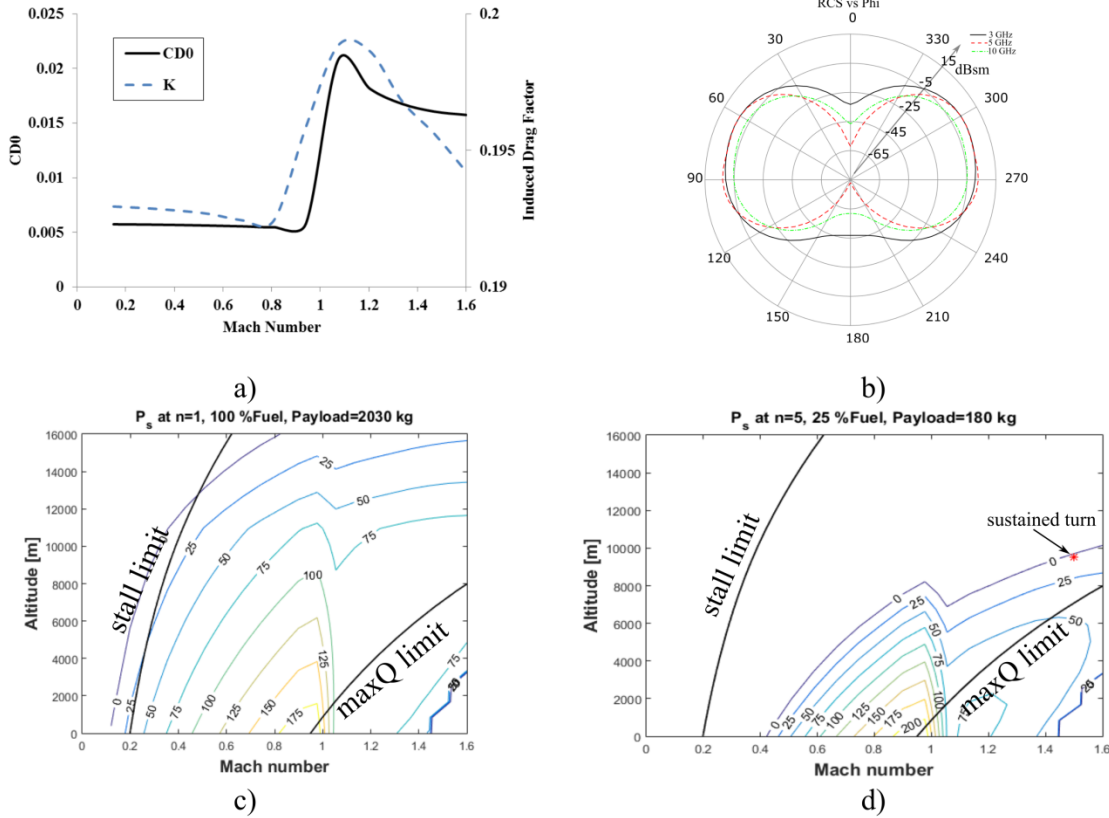
Fig. 16   a) Friction and wave drag and induced drag factor, b) RCS at various frequencies, c) Ps map at level flight conditions, and d) Ps map at sustained turn flight conditions

E. Future studies

Following the conceptual design studies shown thus far, preliminary design studies will be carried out in order to establish a baseline structural concept, initial systems architecture, and engine inlet and exhaust geometries. Preliminary studies will be complemented with more comprehensive low observability studies which will include multi-static radar cross section signatures at various frequencies and radar absorbent materials, as well as an initial estimate of infrared signature. Furthermore, maneuverability levels will be enhanced through the adoption of additional control surfaces and thrust vectoring.

VI. Conclusion

This study introduced the GENUS aircraft conceptual design environment applied to Unmanned Combat Aerial Vehicles, specifically for the mission of a 5th generation unmanned strike fighter designed to operate as *loyal wingmen* to a manned fighter such as the F-35A, especially during *first day of war* operations where they can act as force multipliers reducing the risk to human operators.

An initial parametric analysis was performed and refined through the GENUS framework for a double delta, low observable flying wing. Initial trade-off studies were carried out in order to evaluate the effects of outer wing sweep, taper ratio, choice of airfoil, and engine bypass ratio for afterburning turbofans. Results favor the use of supercritical airfoils and an afterburning turbojet engine due to its lower mass. Engine choice can be revised in order to improve infrared signature.

An evolutionary optimization algorithm has been employed to establish the main geometrical characteristics, as well as to size and locate the internal components in order to comply with longitudinal stability constraints. Results show that acceptable stability levels can be achieved regardless of fuel scheduling procedures. Trim analysis has been carried out by assuming elevons in the outer wing trailing edge section with a chord fraction of 20%, which were found to comply with deflection requirements at all flight conditions.

Radar cross section results show that the clean geometry configuration with perfect electric conductor materials has acceptable levels of low observability, especially from the nose-on and tail angle views. Finally, specific excess power maps show that there is sufficient thrust during subsonic and supersonic maneuvers.

Finally, future preliminary studies of this aircraft include detailed structural and systems layout, engine inlet and exhaust system design, low observability studies including infrared signature, and multirole performance evaluation.

Acknowledgments

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