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Spectral ageing analysis and dynamical analysis of the double-double radio galaxy J1548–3216

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ABSTRACT

Context. Determining ages of the outer and the inner lobes of so-called double-double radio galaxies (DDRGs) is crucial for understanding the active cycles of galactic nuclei, the phases of interruption of the jet flow, and physical conditions in the surrounding galactic and intergalactic medium governing the jets' propagation. A recognition and understanding of these conditions during the restarted jet activity is of special interest.

Aims. We determine the ages and other physical characteristics of the outer and the inner lobes of the DDRG J1548–3216, as well as the properties of the surrounding environment during the original and the restarted phase of the jets' activity.

Methods. Using the new low-frequency and high-frequency radio images of this galaxy, we determined the shape of the spectrum along its lobes and performed the classical spectral-ageing analysis. On the other hand, we applied the analytical model of the jet's dynamics, which allowed us to derive the physical conditions for the source's evolution during the original jet propagation through the unperturbed IGM, as well as those when the restarted new jet propagates inside the outer cocoon formed by the old jet material that passed through the jet terminal shock.

Results. The dynamical age estimate of the outer and the inner lobes is 132 ± 28 Myr and $\sim 9 \pm 4$ Myr, respectively. The synchrotron age in the outer lobes systematically rises from ~ 25 Myr in the vicinity of the lobes' edges to about 65–75 Myr in the centre of the old cocoon. These ages imply an average expansion speed along the jets' axis: $(0.012 \pm 0.003)c$ in the outer lobes and $(0.058 \pm 0.025)c$ in the inner lobes, but the latter speed would be $\sim 0.25c$ when they were of age less than 1 Myr. We find that the jet power during the restarted activity is about ten-fold fainter than that of the original jet. Similar disproportion is found for the internal pressures and the magnetic field strengths in the old cocoon and those in the inner lobes. This disproportion can be effectively reduced by assuming the same equations of state for the emitting particles and the magnetic fields within the old and the new lobes. However, we think that our assumption of the non-relativistic equation of state for the old cocoon and the relativistic one for the new lobes is more justified.

Key words. galaxies: active – galaxies: evolution – radio continuum: galaxies – galaxies: individual: J1548–3216

1. Introduction

Although the intrinsic time evolution of powerful radio sources of Fanaroff-Riley type II (FR II; Fanaroff & Riley 1974) is largely understood and described with a number of analytical models (e.g. Kaiser et al. 1997; Blundell et al. 1999; Manolakou & Kirk 2002; Kino & Kawakatu 2005), there are still several unanswered questions about the duty-period of the active galactic nucleus (AGN), the jet production processes, its interaction with the external gaseous environment including the intergalactic medium (IGM), and the contents of the radio lobes as a part of the low-density “cocoon”.

The double-double radio galaxies (DDRGs) are characterized by two pairs of unequally-sized edge-brightened (FR II-type) lobes sharing the same radio core. In most of them the outer and inner double structures are aligned well. The existence of such radio sources is the evidence that the jet activity in AGN may be not continuous during the lifetime of a source. In fact, an intermittent production of jets can be connected with stochastic transitions between two accretion modes: the standard one – with angular momentum transmitted outwards by viscous torques within the accretion disk – and the “magnetic” one, with the developed large-scale magnetic fields and related

MHD winds (Nipoti et al. 2005; Körding et al. 2006). Sikora et al. (2007) incorporated the above idea into the spin paradigm scenario. Postulating that the efficient production of relativistic jet requires both a large black hole (BH) spin (as in the model of Blandford & Znajek 1977) and an efficient collimation mechanism (cf. Begelman & Li 1994), they noted that the intermittent jet activity observed in active galaxies accreting at high rates may be due to intermittent collimation of the central Poynting flux-dominated (so called “Blandford & Znajek”) outflow by heavier and slower MHD wind generated in the inner parts of the accretion disk undergoing state transitions. In the framework of this interpretation, the jet axis in the subsequent jet activity epochs is expected to be the same, since this axis is determined by the spin of the central BH, which should not change substantially on short ($\ll 100$ Myr) timescales (see the discussion in Sikora et al. 2007).

Such an interrupted production of jets is evidently imprinted in the radio morphology of DDRGs. We are interested in certain aspects of these sources. Are the ages and internal densities of the inner lobes much lower than these values for most “normal” radio sources of similar physical size as the inner lobes? Is the density of the pre-existing cocoon much lower than in the unperturbed galactic and IGM environment, or is this density higher?

Table 1. Observing log.

Telescope	Array	Obs. freq. [MHz]	Primary beam [arcmin]	Ang. resol. [arcsec]	rms noise [mJy beam ⁻¹]	Observing date
GMRT		334	80	15	0.24	2008, May 24
GMRT		619	43	7.5	0.12	2008, Mar. 8
ATCA+VLA*		1384	40	3.5	0.04	2001, Dec. 2
VLA*	BnA	1384	30	3.5	0.04	2002, May 31
ATCA*		2495	24	5	0.05	1999, Mar. 7
VLA	DnC	4860	9	15	0.03	2008, Jun. 5
VLA*	BnA	4910	9	1.3	0.02	2002, Jun. 2

Notes. (*) Archival data; courtesy of Vicky Safouris and Ravi Subrahmanyan.

The first case would strongly suggest that the new inner structure is formed in a channel drilled through the old cocoon by the former jet activity cycle, which has been modelled by the numerical MHD simulations of Clarke & Burns (1991). They predict that “the restarted jet will always be overdense (denser than its immediate surroundings) if the original jet is underdense relative to the quiescent IGM”. While the restarting jet model accounts for many of the observations, there remain some profound discrepancies difficult to be reconciled (cf. Clarke 1997). The second case would imply an efficient replacement of the inner lobes by the heavier external medium (e.g. Kaiser et al. 2000; Brocksopp et al. 2007).

The radio galaxy J1548–3216 (PKS B1545–321) is a remarkable example of DDRG in which the newly restarted jets propagate through the remnant cocoon of a previous active phase (Subrahmanyan et al. 1996; Saripalli et al. 2003, hereafter referred to as SSS2003). This galaxy has recently been extensively studied by Safouris et al. (2008, hereafter referred to as S2008), especially under the aspect of an observational constraint for the 2D and 3D numerical simulations of the restarted jet provided by Clarke & Burns (1991) and Clarke (1997), respectively. In S2008, the authors suggest that observational data are consistent with a picture that the restarted jets generate narrow-bow shocks, and the inner lobes in this galaxy are a mixture of cocoon plasma re-accelerated at the bow shock and new jet material re-accelerated at the termination shock. They propose that the evolution of the restarted jets and the inner lobes is strongly influenced by an entrainment of the external IGM into the pre-existing cocoon.

In this paper the spectral-ageing and dynamical analyses of J1548–3216 are performed with the aim of (i) determining the synchrotron age distribution in the outer lobes of this galaxy (in the old cocoon); (ii) estimating of this age in the inner lobes; (iii) comparing these ages with the dynamical ages estimated with the DYNAGE algorithm of Machalski et al. (2007); (iv) determining the jet powers during the first and the second phase of activity, as well as other physical parameters characterizing the lobes and their environments, such as the particle density, energy density, internal pressure, magnetic field strength and its density, propagation speeds of the lobes along the jets’ axis, etc. Most working approaches in this paper are similar to those applied in our previous publications on other giant-sized radio galaxies: DDRG J1453+3308 (Konar et al. 2006) and a further ten selected galaxies (Jamrozy et al. 2008; Machalski et al. 2009, hereafter referred to as MJS2009). The analyses presented in this paper are based on the new radio observations recently conducted with the Giant Metrewave Radio Telescope (GMRT) and Very Large Array (VLA), and on the Australia Telescope Compact Array (ATCA) and VLA archival data kindly provided to us by Vicky Safouris and Ravi Subrahmanyan. The new

observations and the data reduction are presented in Sect. 2. The resulting total-intensity 334, 619, 1384, 2495, and 4860 MHz total-intensity images are used in Sect. 3 to derive radio maps of the outer double structure of the investigated galaxy, as well as to extract the inner double structure from a background of the underlying cocoon formed during the earlier phase of the nuclear activity. The spectral-ageing analysis of the outer and the inner structures is described in Sect. 4. while the dynamical analysis is presented in Sect. 5. Results of these analyses, as well as our contribution to the aspects of the restarted nuclear activity, the environmental conditions ruling the new jets propagation within the relict cocoon, and their energetics – derived with another approach than applied in the previous studies of this radio galaxy by SSS2003 and S2008 – are discussed in Sect. 6.

For the purpose of calculating the linear size, volume, and luminosity of the lobes, we use cosmological parameters $\Omega_m = 0.27$, $\Omega_{vac} = 0.73$, and $H_0 = 71 \text{ km s}^{-1} \text{ Mpc}^{-1}$.

2. Observational data and their reduction

The observing log for all the observations is listed in Table 1, which is arranged as follows. Columns 1 and 2 show the name of the telescope and the array configuration for the former and the recent VLA observations; Cols. 3 and 4 give the frequency of observations and the primary beamwidth; Cols. 5 and 6 show a typical angular resolution and an rms noise level achieved in the resulting images of the radio galaxy investigated. The last Col. 7 gives the dates of the observations. More details of these observations are given below.

The low-frequency GMRT observations at 334 and 619 MHz were made in the standard manner, with each observation of the target source interspersed with observations of calibrator sources. The phase calibrators B1714–252 (at 334 MHz) and B1626–298 (at 619 MHz) were observed after each of several 20 min-lasting exposures of the target centred on the core position. 3C 286 was used as the flux density and bandpass calibrator based on the scale of Baars et al. (1977). At each of the two frequencies the total observing time on the target source was only about 150 min because of very limited observing time scheduled for the project. Unfortunately, a large part of 334-MHz data were strongly affected by radio frequency interference, and these data had to be flagged in the reduction process, which further reduced the quality of the data. Acceptable data were edited and reduced with the NRAO AIPS package. All these data were self-calibrated to produce the best possible images.

At the frequencies of 1384 and 2495 MHz, the archival data taken with the ATCA and VLA arrays are used. In particular, the ATCA 2495 MHz map of the total structure published by SSS2003, as well as the combined ATCA+VLA 1384 MHz of the total structure and the high-resolution VLA 1384 and

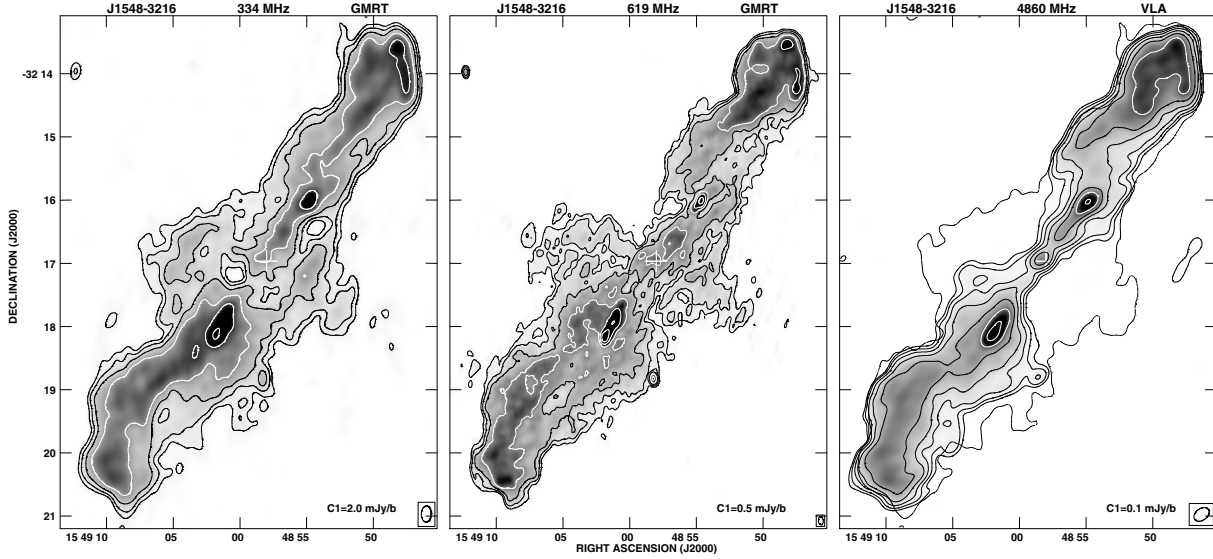


Fig. 1. Full-resolution GMRT 334 and 619 MHz, as well as VLA DnC-array 4860 MHz images of the entire structure of the radio galaxy J1548–3216 (PKS 1545–321). The first contour level, C_1 , is given in each image. The contour levels are $(1, 2, 4, 8, \dots) \times C_1$ mJy/beam. In all the images, the restoring beam is indicated by an ellipse. The cross indicates the position of the optical parent galaxy. The dashed outermost contour on the VLA image encloses an area of the flare of the emission bridge within which a missing 4.86 GHz flux density is estimated in the text.

4910 MHz map of the inner double published by S2008. For the purpose of specifying a high-frequency spectrum of diffuse lobes of the outer double structure, we made other 4860 MHz observations of the target source with the VLA in its DnC configuration. Again, 3C 286 and B1522–275 were used for the amplitude and the phase calibrations, respectively. Two 20 min exposures of the fields centred on each of the two outer lobes were reduced, self-calibrated, and combined into one image of the entire source.

3. Observational results

3.1. New radio images

A full-resolution GMRT 334 and 619 MHz images, as well as the VLA/DnC 4860 MHz image, are presented in Fig. 1. Our new images, especially those at low frequencies, confirm the overall morphology of J1548–3216 already presented and discussed by SSS2003 and S2008, i.e. that both the outer lobes are edge-brightened and rather sharply bounded. Likewise in those papers, our images also do not show any evident hot spots or very compact structures at the ends of the lobes, and both low-frequency images confirm a distinct pair of emission peaks along a bright rim at the western end of the NW lobe. As in the archival ATCA and ATCA+VLA data, the inner double structure (a pair of relatively bright, narrow lobes) is strongly immersed into the diffuse bridge of emission extended from the bright edges of the outer lobes towards the radio core. A flare of the bridge transverse to the source’s axis in the vicinity of the core, very well shown at the ATCA 1384 MHz image in SSS2003, is also pronounced at both low frequencies. This flare is missing at the 4860 MHz image, which suggests a very steep radio spectrum in that part of the structure (cf. Sect. 3.4). However, a missing flux density at this frequency is negligible. Indeed, the area marked with the dashed line in the right panel of Fig. 1 is about 60 restoring beams, and a missing flux is likely between the rms noise level and the first contour C_1 in this image, both multiplied by ~ 60 beams, i.e. between ~ 1.8 mJy and ~ 6 mJy. Even the missing flux of 6 mJy will be about 1.3% of the total flux density of

449 mJy given in Table 2. Such a loss does not affect the spectral analysis performed in Sect. 3.4.

However, the new radio images, showing nothing especially new in respect to the archival ones, extend the observational data from two to the five different frequencies ranging from 334 MHz to 4860 MHz. This is the necessary and sufficient condition for performing the undertaken analyses.

3.2. Extraction of the inner double structure

To perform the spectral-ageing and dynamical analyses separately for the outer and the inner structures, we have to extract emission of the inner lobes from the underlying “background” radiation of the outer lobes. At the observing frequencies of 334 and 619 MHz this is made by excluding of the visibility data taken with baselines shorter than 2 k λ and 3 k λ , respectively, while at 4860 MHz visibilities with spatial frequencies less than 2.5 k λ are excluded. This effectively resolved out a large part of the underlying bridge’s emission. Somewhat different approach was applied at 2495 MHz. Having the final ATCA image at this frequency only but not the original UV data, we used the AIPS task IM2UV which allows a Fourier transformation of the image reconverting the data back to a UV data file. Then a similar procedure, as described above, was applied to the reconverted 2495-MHz UV data excluding the visibilities at baselines shorter than 2.5 k λ .

The resulting 334, 619, 2495, and 4860 MHz images of the inner double structure are shown in Fig. 2. The corresponding archival ATCA 1384 MHz and VLA/BnA 4910 MHz images are included for comparison. Besides the brightest parts with the leading heads of the inner lobes, our new images confirm the presence of another weak emission region in the inner NW lobe detected by SSS2003 in their 2495-MHz total intensity images of the inner structure. Unfortunately, the dynamic range of our images is too low to detect more of the connecting emission seen in their Fig. 6. We estimate that such a missing flux is from about 10% at 334 MHz to about 2% at 4860 MHz. All these images, except VLA/BnA, brought to a common scale using the

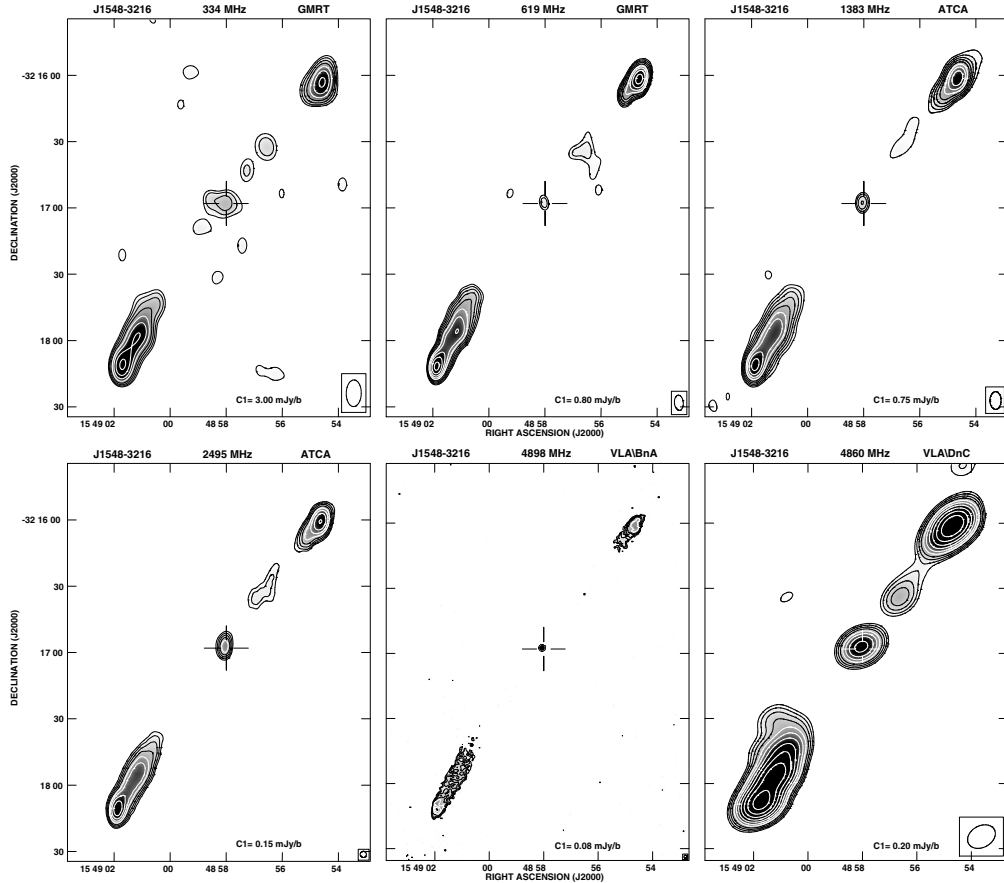


Fig. 2. GMRT, ATCA and VLA images of the inner double structure of J1548–3216. The first contour level is given in each image. The contour levels are (1, 1.41, 2, 2.83, 4, 5.66, ...) \times C1 mJy/beam. The restoring beam is indicated by an ellipse. The cross marks the position of the optical galaxy.

Table 2. Flux densities of the total structure (Total) and the outer (outNW and outSE) and inner (innNW and innSE) lobes of J1548–3216.

Freq. [MHz]	Total [mJy]	outNW [mJy]	outSE [mJy]	innNW [mJy]	innSE [mJy]	Ref.
(1)	(2)	(3)	(4)	(5)	(6)	(7)
160	8700 \pm 870	(3900 \pm 360)*	(4500 \pm 480)*			(1)
334	4926 \pm 740	2095 \pm 314	2642 \pm 396	58.0 \pm 9.2	130.0 \pm 19.7	(5)
619	3274 \pm 265	1383 \pm 111	1758 \pm 141	43.4 \pm 4.6	87.6 \pm 7.6	(5)
843	2519 \pm 200					(2)
1384	1815 \pm 90	820 \pm 41	913 \pm 46	26.5 \pm 3.3	53.3 \pm 4.0	(4)
1400	1842 \pm 764					(3)
2495	1019 \pm 31	479 \pm 15	484 \pm 15	17.5 \pm 3.0	35.5 \pm 3.2	(4)
4860	449 \pm 25	198 \pm 20	217 \pm 22	11.8 \pm 1.6	19.7 \pm 2.2	(5)
4910				11.9 \pm 0.9	23.1 \pm 1.5	(4)

Notes. (*) Estimated division of the total 160 MHz flux density between the outer lobes, cf. the text.

References. (1) Slee (1995); (2) Jones & McAdam (1992); (3) NVSS (Condon et al. 1998); (4) Flux densities measured on the archival ATCA and VLA images (Saripalli et al. 2003; Saffouris et al. 2008); (5) this paper;

AIPS task HGEOM and convolved to the angular resolution of $16'' \times 16''$, are used to make a longitudinal section along the inner structure. Such “slices” at the five observing frequencies are shown in Fig. 3. To avoid problems with any missing flux, we restrict our spectral and dynamical analyses of the inner lobes to their brightest regions indicated in Fig. 3.

3.3. Outer lobes cleaned from the inner structure

To analyse physical properties of pure outer lobes of J1548–3216, the inner double structure was subtracted from the

images of the entire radio source partly shown in Fig. 1. For this purpose, all of those images were also brought to a common scale (a map size, cell size, coordinates of the map centre) and convolved to the angular resolution of $16'' \times 16''$. The images of the inner structure were blanked over regions outside the extracted inner lobes and then subtracted from the convolved maps of the entire source using the AIPS task COMB. The net images of the outer lobes (rotated by 35°) are shown in Fig. 4. On the first of these images, a division of the radio structure into 18 strips, each of them $28''$ wide, is shown. The first plotted contour on the ATCA+VLA image is exceptionally high (about

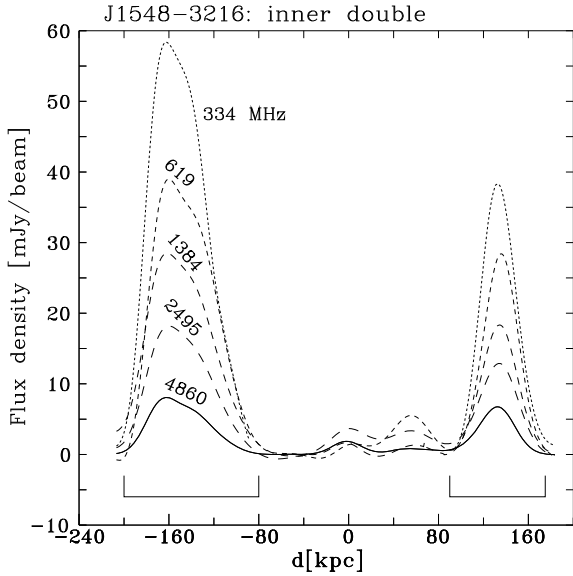


Fig. 3. Longitudinal section along the inner double structure. The horizontal brackets indicate regions of the structure subject to the spectral and dynamical analyses.

8× rms noise level) to clear it from spurious jagged contours that appeared after the convolution of the original map with the beam of $16'' \times 16''$. The integrated flux densities measured in the consecutive strips and plotted vs. distance of the strip’s centre from the core position (the strips’ centres are separated by the angular distance of $28'' / \cos 35^\circ$) form a longitudinal section along the cleaned outer structure shown in Fig. 5a. The flares or spurs in the central region of the outer structure increase the total flux density in the strips S7, S8 and N11, N12 causing its peaks marked F1, F2, and F3 in Fig. 5a. The brightness peaks of the leading heads of the new inner lobes lying at the radio axis (indicated with the dotted vertical lines), almost coincide with the positions of these strips. A spectral steepening and the spectral age within the strips are analysed in Sect. 4.1.

3.4. Radio spectra

The integrated flux densities of the total source, as well as of its outer and inner lobes, are given in Table 2. All columns are self-explanatory; outNW and outSE indicate the NW and SE lobes of the outer double structure, while innNW and innSE – the NW and SE inner lobes, respectively. Because a spectral fit, especially with the SYNAGE, is very sensitive to a lack of low-frequency data (cf. MJS2009), the 160-MHz flux densities of the outer lobes are estimated by subtracting 300 mJy (assumed flux density of the inner double at this frequency based at a spectral index of about 0.6, cf. Sect. 4.2) from the total flux density measured with the Culgoora array, and dividing the net flux between the two lobes in a proportion similar to those observed at the higher frequencies.

Distributions of the low-frequency α_{1384}^{334} and high-frequency α_{4860}^{1384} spectral index vs. distance from the core measured along the axis of the outer structure cleaned from the inner lobes are shown in Fig. 5b. The wavy ridge and its side flares do not show any peculiarity in the spectral index distribution shown in Fig. 5b. Both the low-frequency and the high-frequency indices exhibit a systematic steepening from the heads of the outer lobes towards the centre. The low-frequency spectral index rises from ~ 0.5 to ~ 0.9 , while the high-frequency one steepens

Table 3. Flux densities of the radio core.

Freq. [MHz]	S_{core} [mJy]	Observing date
619	1.52	2008, Mar. 8
1384	2.17	2002, May 31
2495	2.50	1999, Mar. 7
4860	2.53	2008, Jun. 5
4910	2.57	2002, Jul. 30

from ~ 0.8 to ~ 2.0 at the evident depression of emission at the centre of the bridge. Such a large continuous steepening of the spectra suggested a systematic increase in the synchrotron age of relativistic particles enclosed in the old cocoon, i.e. an increase from the lobes’ head towards their flaring ends.

We do not attempt to analyse a distribution of the synchrotron age in directions transverse to the main axis of the source, hence spectral index distributions over the entire area of the outer structure are beyond the scope of this paper. Nevertheless our data show similar spectral features as those seen in the map of the spectral index α_{1384}^{2495} in SSS2003 (their Fig. 3), i.e. the steepest spectra appear at eastern ends of the strips S7 and S8, and at western ends of the strips N11 and N12. We cannot confirm a distinctly steeper spectrum along the southwestern edge of the outSE lobe appearing in their map, but at least something similar is not pronounced in the spectral index α_{334}^{1384} or α_{619}^{1384} .

3.5. The radio core

The J2000.0 position of the radio core determined from the high-resolution images is RA: $15^{\text{h}}48^{\text{m}}58^{\text{s}}.05$ and Dec: $-32^\circ 16' 56''.9$, which is less than 1 arcsec away from centre of the parent galaxy imaged with the Anglo-Australian Telescope (AAT) by S2008. The flux densities of the core, measured on the images presented in this paper, are collected in Table 3. These flux densities suggest a mildly inverted spectrum without a sign of time variability.

4. Spectral ageing analysis

Remembering all the serious problems with both the principles and the practical application of spectral-ageing calculations to physical conditions in radio sources described in detail in MJS2009, the spectral age in different parts of the lobes, i.e. the time elapsed since the radiating particles were last accelerated, is determined using the classical theory that describes the time evolution of emission spectrum of a single population of particles with an initial power-law energy distribution (e.g. Myers & Spangler 1985; Carilli et al. 1991). The initial energy distribution of the relativistic particles is a power-law function, $n(\gamma_i)d\gamma_i = n_0\gamma_i^{-p}d\gamma_i$, of their initial Lorentz factor, γ_i . The power p corresponds to the initial (injection) spectral index α_{inj} , which can be, in principle, estimated from the observational data until the synchrotron frequency of the minimum electron Lorentz factor lies far outside the observable low-frequency spectrum. Fortunately, a spectral turnover at low frequencies is not observed in the radio spectra of the extended FR II-type radio sources. On the other hand, the spectral break frequency above which the radio spectrum steepens from the injected power law, ν_{br} , is related to the spectral (synchrotron) age, τ_{syn} , and the magnetic field strength, B , through

$$\tau_{\text{syn}} [\text{Myr}] = 50.3 \frac{B^{1/2}}{B^2 + B_{\text{IC}}^2} [\nu_{\text{br}}(1+z)]^{-1/2}, \quad (1)$$

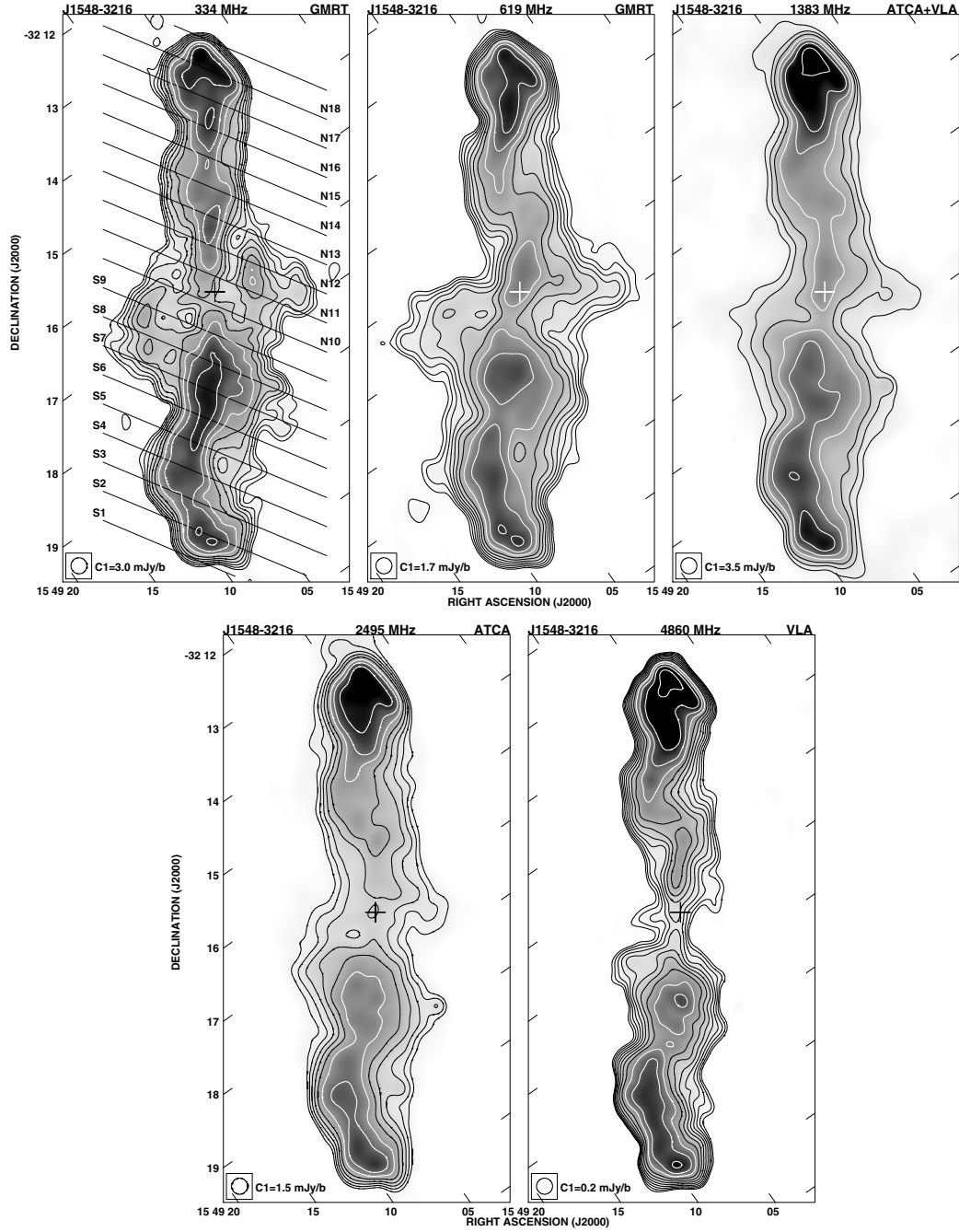


Fig. 4. Radio images of the outer lobes cleaned from the inner double structure and convolved to the angular resolution of $16'' \times 16''$. The first contour level is given in each image. The contour levels are as in Fig. 2. The division into 18 $28''$ -wide strips, used for the spectral steepening and spectral age analysis, is shown in the first of these images.

where $B_{iC} = 0.318(1+z)^2$ is the magnetic field strength equivalent to the inverse-Compton microwave background radiation. B and B_{iC} are expressed in units of nT, while ν_{br} is in GHz. Values of α_{inj} and ν_{br} are found by the fit to the observed radio spectra using the SYNAGE algorithm of Murgia (1996).

4.1. The outer structure

4.1.1. Determination of α_{inj} and ν_{br} values

To determine the value of α_{inj} , we fit the CI, CIE, and JP models to the flux densities of the entire outer lobes (given in Cols. 3 and 4 of Table 2) treating α_{inj} as a free parameter, and realizing that decidedly the best fit to the data is achieved with the

JP model. Fits of the JP model of radiative losses to the flux densities of the outer SE and NW lobes are shown in Fig. 6. The values of $\alpha_{inj} = 0.583^{+0.151}_{-0.070}$ and $\alpha_{inj} = 0.540^{+0.096}_{-0.051}$ found by the fit correspond to the α_{1384}^{2495} indices of ~ 0.7 and ~ 0.6 previously determined by SSS2003 for the brightest regions at the SE and NW heads of the outer structure, respectively. These fitted α_{inj} indices are used to determine values of ν_{br} in the 18 parallel strips covering the entire outer structure of the radio source. The JP models of the spectra within these 18 strips are collected in Fig. 7. A distance of the strip's centre from the core, the resulting value of ν_{br} , and the relevant value of χ_{red}^2 , giving a goodness of the fit in each of 18 strips, are given in Cols. 2–4 of Table 4, respectively.

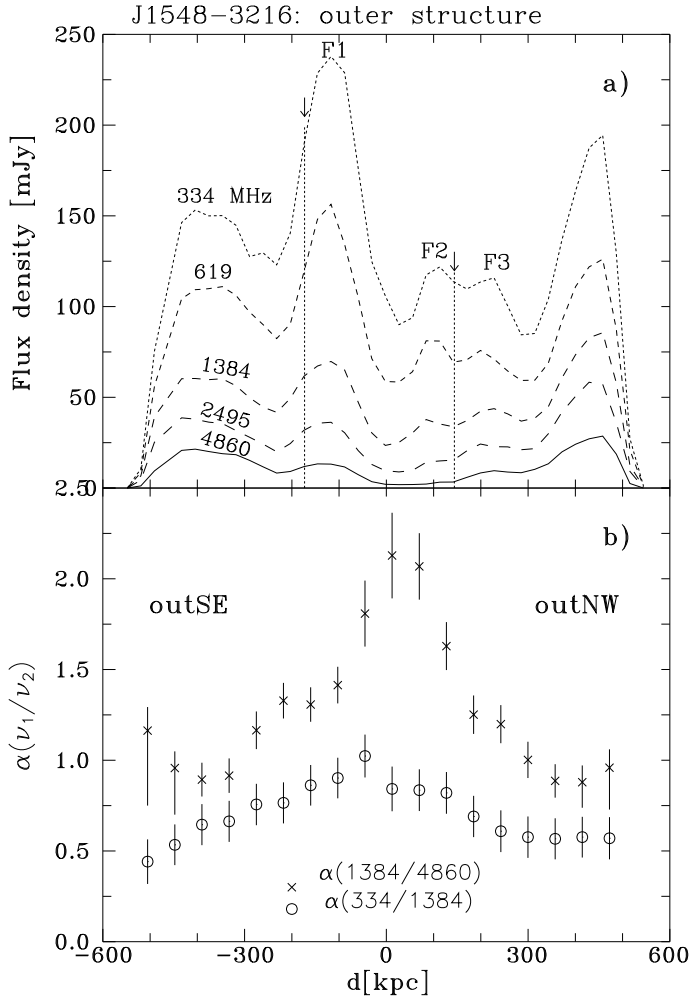


Fig. 5. a) Integrated flux densities in the consecutive strips along the outer double structure vs. distance from the core. The vertical lines indicate positions of brightness peaks in the inner lobes. b) Low-frequency and high-frequency spectral indices in these strips.

4.1.2. Determination of magnetic field strength values and the spectral ages

In consistency with the approach applied in our previous spectral-ageing analyses of giant radio galaxies (Jamrozy et al. 2005, 2008; Konar et al. 2006), the magnetic field in Eq. (1) is identified with an “equipartition field”, B_{eqv} , which provides equipartition between the total energy densities of the relativistic particles and the magnetic field ($u_e \approx u_B$). The required values of B_{eqv} are computed with Miley’s (1980) prescription for the general formula

$$B_{\text{eqv}} \propto (1+k) \left(\frac{L}{V} \right)^{2/7}, \quad (2)$$

where k is the ratio of the energy content of relativistic protons to that of electrons (adopted as $k = 1$), L is the luminosity of a given strip calculated by integration of its spectrum from a frequency equivalent to a minimum Lorentz factor, $\gamma_{\text{min}} \sim 1$ for the relativistic electrons to the upper limit of 100 GHz, and V is the volume corresponding to that slice. The derived values of B_{eqv} and the resulting spectral ages, τ_{syn} , are given in Cols. 5 and 6 of Table 4, respectively.

The distribution of this spectral age vs. distance from the core measured along the axis of the outer structure is shown in Fig. 8.

4.2. The inner structure

The spectrum of each of the two inner lobes, i.e. the flux densities given in Cols. 5 and 6 of Table 2, is fitted with the CI model. The fits (shown in Fig. 9) suggest a similar initial slope of the spectrum of both the lobes of $\sim 0.6 \pm 0.1$ and the spectral break of $161_{-156}^{\text{dex}(11)}$ GHz and $44_{-42}^{\text{dex}(11)}$ GHz for the NW and SE lobes, respectively. (The formal $\pm 1\sigma$ errors are enormous due to the practically straight spectra.) The volume of the lobes is calculated assuming their cylindrical geometry with a minimum angular size $24'' \times 7''$ (height \times base diameter) for the NW lobe and $42'' \times 8''$ for the SE lobe where these dimensions are measured in the VLA image of S2008 (their Fig. 5). In this case, the equipartition magnetic field strength, calculated with the prescription of Miley (1980), is 0.63 ± 0.16 nT and 0.65 ± 14 nT, respectively. Using these values, a “mean” spectral age of the radiating particles in the lobes is $5.4_{-4.9}^{+2.8}$ Myr for innNW lobe and $10.1_{-9.5}^{+5.0}$ Myr for innSE lobe. However, adopting the full length of the lobes as the cylinder’s height, i.e. $74''.6$ and $89''.5$ for innNW and innSE lobes, the magnetic field strengths reduce to 0.46 ± 0.10 nT and 0.43 ± 0.10 nT, while the ages increase to $7.0_{-6.5}^{+3.0}$ Myr and $13.9_{-13.3}^{+6.1}$ Myr, respectively. The resulting spectral ages of the inner lobes are discussed in Sect. 6.1.

5. The dynamical age analysis

This analysis is performed using the DYNAGE algorithm of Machalski et al. (2007) which is based on the analytical model for the evolution of FR II type radio sources, combining the pure dynamical model of Kaiser & Alexander (1997) with the model for expected radio emission from a source under the influence of the energy loss processes published by Kaiser et al. (1997, known as the KDA model). With this algorithm we derive the dynamical age of the lobes t , both the outer and the inner ones, the *effective* injection spectral index α_{inj} , which approximates the initial electron continuum averaged over a very broad energy range and over the present age of the source, the jet power Q_{jet} , and the central density near the radio core ρ_0 , which determines the ambient density in which the jet propagates.

A detailed description of how to apply the above algorithm is published in MJS2009. It is worth explaining here that determining of values of these four free parameters of the model is possible by a fit to the observational parameters of a source (or its lobes): its projected linear size D , the volume V , the radio power P_ν and the radio spectrum α_ν , which provides $(P_\nu)_i$ at a number of observing frequencies $i = 1, 2, 3, \dots$. As in the KDA model, we assume a cylindrical geometry of the lobes (cocoon), thus $V = \pi D^3 / 4 R_T^2$ where R_T is their axial ratio. The values of the few other free parameters of the model have to be assumed. These are the central core radius a_0 , the exponent β describing the ambient density profile in the simplified King’s (1972) model $\rho(d) = \rho_0 (d/a_0)^{-\beta}$, the Lorentz factors determining the energy range of the relativistic particles used in integration of their initial power-law distribution $\gamma_{i,\text{min}}$ and $\gamma_{i,\text{max}}$, the adiabatic indices of the three “fluids” with individual energy densities: the jet material, Γ_{jet} , the magnetic field, Γ_B , and the ambient medium, Γ_x (cf. Kaiser et al. 1997). Since the emitting region consists of these three fluids, the model also takes the adiabatic index of the lobe (cocoon) into account as a whole, Γ_c . The two other free parameters we have to assume are k' – the ratio of the energy density of thermal particles to that of the relativistic electrons – and θ , the orientation of the jet axis to the observer’s line of sight. Following KDA, in the DYNAGE algorithm the assumed energy equipartition is expressed by the ratio

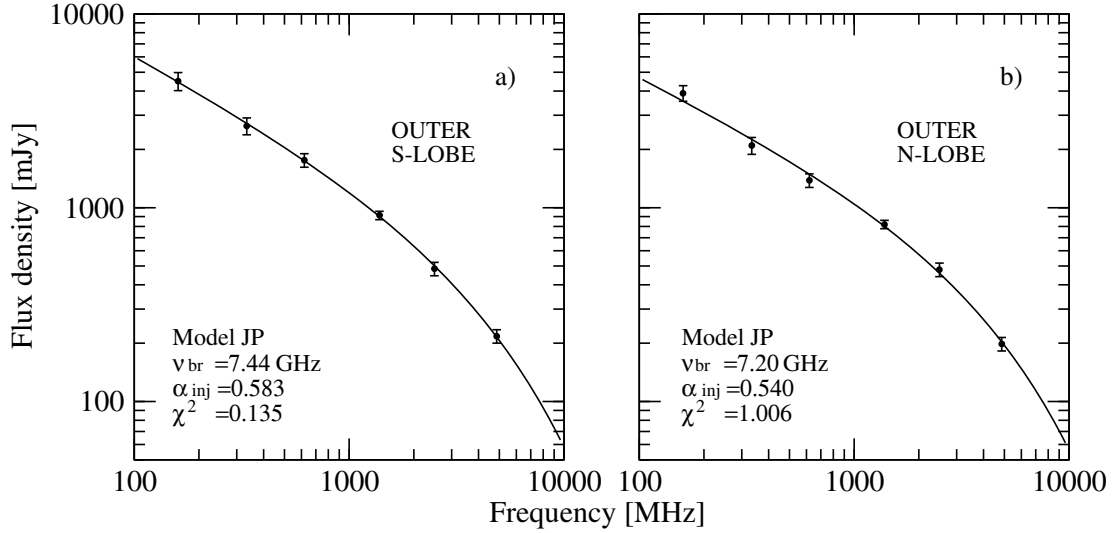


Fig. 6. Spectra of the outer lobes fitted with the JP model, as described in the text.

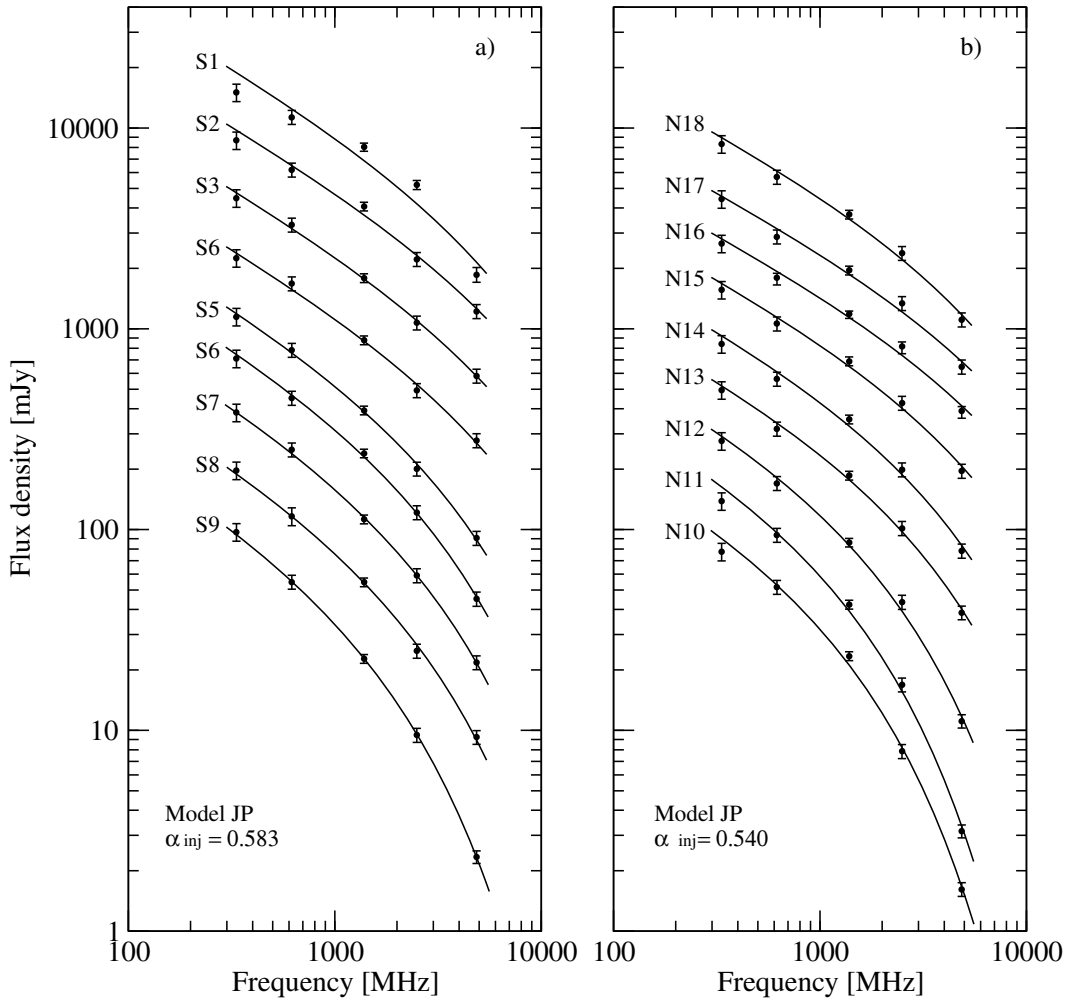


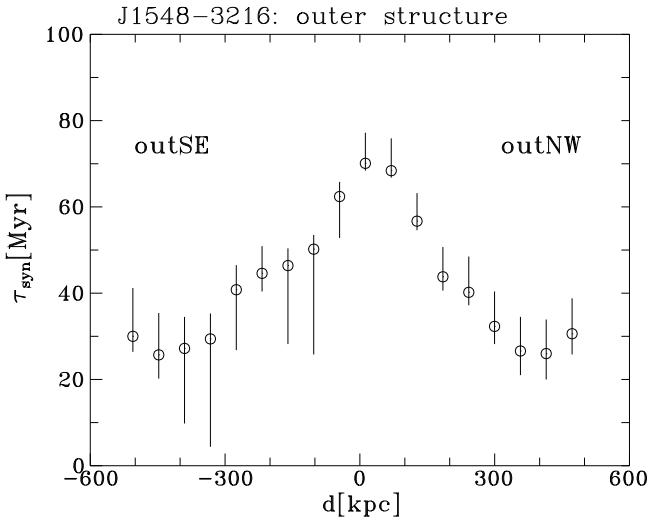
Fig. 7. Spectra of the slices S1–S9 in the outSE lobe and N10–N18 in the outNW lobe, fitted with the JP model. The spectra of particular strips are arbitrarily shifted. Reduced values of χ^2 and resulting values of the spectral break, ν_{br} , are given in Table 4.

of the energy densities of the magnetic field and of the particles, $\zeta = (1 + p)/4 = (1 + \alpha_{inj})/2$. The values adopted for the whole source are $a_0 = 10$ kpc, $\beta = 1.5$, $\gamma_{i,min} = 1$, $\gamma_{i,max} = 10^7$, and $\theta = 90^\circ$. A decrease in θ to $\sim 70^\circ$ (cf. S2008) would result in $\sim 6\%$ increase of D and $\sim 7\%$ increase of t (cf. Eq. (6) in

Sect. 5.3). As we are interested in an age difference between the lobes rather than in their absolute age value, the latter one is less important. The values of Γ_c , Γ_B , Γ_x , and k' assumed for the outer and the inner lobes are given in next sections. The observational data of these lobes, used in the DYNAGE fitting procedure, are

Table 4. Break frequency, equipartition magnetic field strength, and spectral age of emitting particles in consecutive strips through the outer lobes of J1548–3216 (cf. Fig. 4).

Strip	Dist. from core [kpc]	ν_{br} [GHz]	χ_{red}^2	B_{eqv} [nT]	τ_{syn} [Myr]
(1)	(2)	(3)	(4)	(5)	(6)
		outSE-lobe	$\alpha_{\text{inj}} = 0.583$		
S1	−505	$13.43^{+3.24}_{-10.0}$	8.34	0.293 ± 0.020	$29.6^{+11.2}_{-3.6}$
S2	−447	$18.23^{+7.80}_{-13.7}$	1.93	0.291 ± 0.015	$25.5^{+9.7}_{-5.5}$
S3	−390	$15.79^{+20.2}_{-8.41}$	0.26	0.269 ± 0.014	$27.7^{+7.3}_{-17.4}$
S4	−332	$13.37^{+29.8}_{-5.36}$	0.65	0.260 ± 0.014	$30.3^{+5.9}_{-25.0}$
S5	−275	$6.93^{+4.76}_{-1.91}$	0.33	0.257 ± 0.014	$42.1^{+5.7}_{-14.0}$
S6	−217	$5.64^{+1.05}_{-1.58}$	0.35	0.242 ± 0.012	$46.9^{+6.3}_{-4.2}$
S7	−160	$5.15^{+4.05}_{-0.88}$	0.21	0.238 ± 0.011	$49.1^{+4.0}_{-18.2}$
S8	−102	$4.42^{+4.29}_{-0.58}$	0.40	0.240 ± 0.012	$53.0^{+3.3}_{-24.4}$
S9	−45	$2.87^{+0.88}_{-0.31}$	0.05	0.241 ± 0.013	$65.7^{+3.4}_{-9.6}$
		outNW-lobe	$\alpha_{\text{inj}} = 0.540$		
N10	+12	$2.27^{+0.10}_{-0.46}$	2.24	0.240 ± 0.013	$73.9^{+7.1}_{-1.7}$
N11	+70	$2.38^{+0.10}_{-0.52}$	2.19	0.240 ± 0.012	$72.2^{+7.5}_{-1.6}$
N12	+127	$3.46^{+0.25}_{-0.79}$	1.04	0.238 ± 0.012	$59.9^{+6.5}_{-2.1}$
N13	+185	$5.99^{+0.87}_{-1.87}$	0.77	0.256 ± 0.014	$45.3^{+6.9}_{-3.2}$
N14	+242	$7.21^{+1.05}_{-2.98}$	1.72	0.264 ± 0.015	$41.1^{+8.3}_{-3.0}$
N15	+300	$11.56^{+2.94}_{-5.77}$	1.25	0.293 ± 0.017	$31.9^{+8.1}_{-4.1}$
N16	+357	$17.32^{+7.26}_{-10.2}$	1.28	0.309 ± 0.018	$25.7^{+7.9}_{-5.6}$
N17	+415	$18.29^{+8.42}_{-11.1}$	1.42	0.328 ± 0.018	$24.6^{+7.9}_{-6.0}$
N18	+472	$13.17^{+4.00}_{-7.00}$	1.19	0.330 ± 0.021	$28.9^{+8.2}_{-4.8}$


Fig. 8. Spectral age of relativistic particles in the outer structure cleaned from the inner lobes plotted vs. distance from the radio core.

given in Table 5. Most columns are self-explanatory, the entries in Cols. (6)–(9) give the ratios of the size and luminosity of the given lobes.

Given the values of α_{inj} , Q_{jet} , ρ_0 , and t , several other physical parameters of the source can be specified, e.g. the internal pressure in the lobes $p_c(t)$, their energy density $u_c(t)$, a ratio of the kinetic energy delivered by the jet to the energy radiated out, $(Q_{\text{jet}} \times t)/(u_c \times V)$, and an average expansion speed of the lobes, $D/(c \times t)$. The assumption of the energy equipartition condition allows the magnetic field density $u_B(t)$ and the field's strength

$B(t)$ to be estimated. The detailed expressions were given in our previous paper (cf. MJS2009). The table with all notations for physical parameters used through the paper is given in the Appendix.

However, the age and other physical parameters, fitted independently for either lobe of a given double source, may be significantly different; i.e., any difference between the fitted values of a parameter is found to be greater than the uncertainty of the fits. This is a consequence of the usual asymmetries between the lobes in their length and luminosity. The difference arises if the same density profile of the ambient medium along the opposite lobes is assumed. The ratios between these parameters of the lobes of J1548–3216, both the outer and the inner ones, are shown in Cols. (6)–(9) in Table 5. On the other hand, we can expect that Q_{jet} and ρ_0 have the same values in the solutions for the opposite lobes, since they characterize an energy-emitting process in the central AGN. Also a large difference in age is rather unlikely. Therefore, following a similar ageing analysis in MJS2009, we consider the *independent* solutions, as well as the two *self-consistent* solutions for the opposite lobes, hereafter denoted as solutions A and B.

5.1. Independent solutions for the individual outer lobes

The images in Fig. 4 suggest that the diffused outer lobes may comprise a fraction of thermal particles, thus the lobes, as a whole, may have a non-relativistic equation of state. Therefore, we assume $\Gamma_c = \Gamma_B = \Gamma_x = 5/3$ and $k' = 10$. The latter value is less than $\sim(25\text{--}140)$ calculated by S2008 with the assumption that the hot spot pressure, p_{hs} , equals a minimum pressure p_{min} , though they expected that a true hot spot pressure should be higher, i.e. $p_{\text{hs}} \geq p_{\text{min}}$. Indeed, when studying the

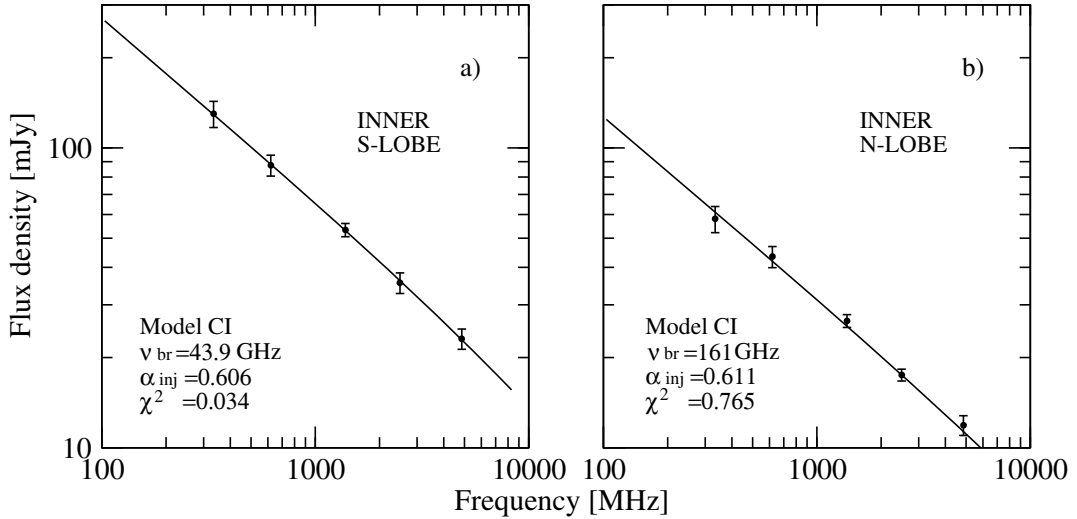


Fig. 9. Spectra of the inner lobes fitted with the CI model, as described in the text.

Table 5. Observational parameters of the outer and the inner lobes used to fit the dynamical model.

Parameter (1)	-----Lobes-----				SE out/inn (6)	NW out/inn (7)	Outer SE/NW (8)	Inner SE/NW (9)
	outSE (2)	out NW (3)	innSE (4)	innNW (5)				
D [kpc]	513	485	173	144	2.96	3.37	1.06	1.20
R_T	2.7	3.1	11.8	10.6				
$\log P_{334}$	24.756	24.654	23.470	23.115	19.32	34.59	1.26	2.26
$\log P_{619}$	24.585	24.481	23.300	22.991	19.27	30.90	1.27	2.04
$\log P_{1384}$	24.310	24.263	23.085	22.780	16.79	30.41	1.11	2.02
$\log P_{4860}$	23.716	23.668	22.705	22.432	11.46	17.22	1.12	1.68

Notes. The monochromatic powers are expressed in $\text{W Hz}^{-1} \text{sr}^{-1}$.

large-scale X-ray environment of selected FR II radio sources, Belsole et al. (2007) find that the internal pressure in their lobes, p_c , is $\sim(1-5)$ times higher than the minimum (equipartition) pressure. Considering that the ratio p_{hs}/p_c in the DYNAGE algorithm varies from ~ 4 to ~ 20 (depending on the value of R_T), the assumed value k' is justified.

The model solutions, i.e. the parameter values resulting from the independent fits, are listed in Cols. 2 and 3 of Table 6.

5.2. Self-consistent solutions for the outer lobes

The differences between the values of the model parameters for the opposite lobes found in the independent solutions come from different environmental conditions (and/or different magnetic fields) on both sides of the core region. For this reason, in the first kind self-consistent solution (solution A), we averaged the values of $Q_{\text{jet,out}}$ and $\rho_{0,\text{out}}$ found for the opposite outer lobes (given in Cols. 2 and 3 of Table 6), and now treat them as the fixed free parameters of the model, $\langle Q_{\text{jet,out}} \rangle = 1.115 \times 10^{38} \text{ W}$ and $\langle \rho_{0,\text{out}} \rangle = 5.445 \times 10^{-22} \text{ kg m}^{-3}$, respectively. Given these values, we can determine another value of β for each of the two lobes, hereafter denoted as $\beta_{\text{sc,A}}$. To do that (following MJS2009), we equalize values of the ambient density at the head of the outer lobes resulting from the independent solution and the self-consistent solution A:

$$\rho_{a,\text{out}} = \rho_{0,\text{out}}(D/a_0)^{-\beta} \approx \langle \rho_{0,\text{out}} \rangle (D/a_0)^{-\beta_{\text{sc,A}}}, \quad \text{hence}$$

$$\beta_{\text{sc,A}} \approx \frac{\log(\langle \rho_{0,\text{out}} \rangle / \rho_{a,\text{out}})}{\log(D/a_0)}. \quad (3)$$

Given a value of $\beta_{\text{sc,A}}$, the expected age of a lobe in the frame of the self-consistent solution is

$$t_{\text{out}} \approx \left(\frac{D}{c_1} \right)^{(5-\beta_{\text{sc,A}})/3} \left(\frac{\langle \rho_{0,\text{out}} \rangle a_0^{\beta_{\text{sc,A}}}}{\langle Q_{\text{jet,out}} \rangle} \right)^{1/3}, \quad (4)$$

where c_1 is a dimensionless constant dependent on the values of β , Γ_j , Γ_x , and Γ_c , given by Eq. (25) in Kaiser & Alexander (1997). The model parameter values resulting from the self-consistent solution A are listed in Cols. 4 and 5 of Table 6.

The data in Table 6 show that the difference between the lobes' ages inferred from the solution A is greater than the found in the independent solution. This is not what we would expect for the actual ages of the opposite lobes¹. Another alternative, self-consistent solution is plausible in which these ages are very similar (especially if we suspect that an orientation of the jets' axis in giant radio galaxies is close to $\theta \approx 90^\circ$), and any differences between the linear extent and luminosity of the lobes come from an inhomogeneity either in density distribution of the ambient gaseous environment or in magnetic field. Since significant differences between the jet power and the radio core parameters in the opposite directions along the jets' axis are not plausible, in the self-consistent solution B we assume the same values of $\langle Q_{\text{jet,out}} \rangle$ and $\langle \rho_{0,\text{out}} \rangle$ for both outer lobes (as in solution A) and the same age $\langle t_{\text{out}} \rangle = 132 \text{ Myr}$, i.e. a mean of the ages determined in the independent solution, and $a_0 = 10 \text{ kpc}$. In such a scenario,

¹ In MJS2009 we showed that for some sources the solution A can diminish the age difference. This usually happens if the shorter lobe is brighter than the larger one.

Table 6. Fitted physical parameters of the outer lobes, with brackets $\langle \rangle$ showing the values assumed within the given solution, (cf. the text).

Parameter	Independ. solution		Self-consist. solut. A		Self-consist. solut. B	
	outSE	outNW	outSE	outNW	outSE	outNW
(1)	(2)	(3)	(4)	(5)	(6)	(7)
$\beta, (\beta_{\text{sc.A}})(\beta_{\text{sc.B}})$	1.50	1.50	1.494	1.507	1.586	1.402
α_{inj}	0.552	0.531	0.536	0.545	0.527	0.554
$Q_{\text{jet,out}} (\times 10^{38} \text{ W})$	1.211	1.019	$\langle 1.115 \rangle$	$\langle 1.115 \rangle$	$\langle 1.115 \rangle$	$\langle 1.115 \rangle$
$\rho_{0,\text{out}} (\times 10^{-23} \text{ kg m}^{-3})$	5.585	5.297	$\langle 5.445 \rangle$	$\langle 5.445 \rangle$	$\langle 5.445 \rangle$	$\langle 5.445 \rangle$
$\rho_{\text{a,out}} (\times 10^{-25} \text{ kg m}^{-3})$	1.521	1.570	1.535	1.574	1.040	2.382
$t_{\text{out}} (\text{Myr})$	142	122	146	119	$\langle 132 \rangle$	$\langle 132 \rangle$
$p_{\text{c,out}} (\times 10^{-13} \text{ Pa})$	1.472	1.459	1.393	1.552	1.291	1.687
$B_{\text{out}} (\text{nT})$	0.322	0.320	0.313	0.330	0.300	0.345
$U_{\text{out}} = u_c \times V (\times 10^{53} \text{ J})$	1.884	1.200	1.784	1.280	1.624	1.399
$D/(t_{\text{out}} \times c)$	0.0118	0.0130	0.0115	0.0133	0.0128	0.0120

a value of $\beta_{\text{sc.B}}$ can be calculated from Eq. (4) substituting $\langle t_{\text{out}} \rangle$ for t_{out} and $\beta_{\text{sc.B}}$ for $\beta_{\text{sc.A}}$. As a result,

$$\beta_{\text{sc.B}}(D) = \left\{ 3 \log \langle t_{\text{out}} \rangle + \log \left(\frac{\langle Q_{\text{jet,out}} \rangle}{\langle \rho_{0,\text{out}} \rangle} \right) - 5 \log \left(\frac{D}{c_1} \right) \right\} / \log \left(\frac{a_0}{D/c_1} \right). \quad (5)$$

This solution does not give an unequivocal result for the fit, because c_1 is a rising function of β . As shown and discussed in MJS2009, the parameter space within which opposite lobes of a significantly asymmetric source would have the same age is usually large. Nevertheless, an example of a reliable solution B for $\beta_{\text{sc.B}}$ (calculated with $c_1(\beta = 1.5)$, the corresponding value of α_{inj} , and other model parameters of the outer SE and NW lobes are shown in Cols. 6 and 7 of Table 6, respectively, for a comparison. It is worth noting that in this solution the product $\langle Q_{\text{jet,out}} \rangle \times \langle t_{\text{out}} \rangle$ does not provide a minimum of the jet kinetic energy that is assured in the independent solutions. However, such a minimum is always shallow (cf. Machalski et al. 2007) and the above objection is not very important.

The data in Table 6 show that the values of the model free parameters do not differ much in the three solutions considered. However, the identity of $Q_{\text{jet,out}}$, $\rho_{0,\text{out}}$, and t_{out} in the opposite outer lobes postulated in the solution B result in a greater difference between the values of $\rho_{\text{a,out}}$ and $p_{\text{c,out}}$ than in the remaining solutions. In particular, it suggests more than twice denser ambient environment around the head of the outer NW lobe than around the head of the opposite SE lobe. These physical conditions seem to be supported by the presence of a distinct pair of emission peaks along the bright rim at the end of the NW lobe, while a similar emission is absent in the SE lobe. Also the mean pressure, $p_{\text{c,out}}$ in the NW lobe is about 30% higher than in the SE lobe, and their ratio found in the solution B is the highest. We discuss this point again in Sect. 6.2.

5.3. Independent solution for the inner lobes

In the case of the inner structure, we assume that (i) the observed emission arises from the narrow lobes (cocoon), not the restarted jets; (ii) the jets' and lobes' material has a relativistic equation of state with $\Gamma_{\text{jet}} = \Gamma_{\text{B}} = \Gamma_{\text{c}} = 4/3$ with no thermal particles, thus $k' = 0$; and (iii) the restarted jets propagate within rarefied and uniform (with $\beta = 0$) medium of the relict outer cocoon formed by the old jets' material that passed through the jet terminal shock. Since the observed spectra of the inner lobes show no curvature below the frequency of 4.9 GHz, especially for the innNW lobe where the SYNAGE fit suggests ν_{br} above 20 GHz

(cf. Fig. 9), the DYNAGE algorithm will not be able to find a unique solution for the dynamical age, i.e. to determine values of $Q_{\text{jet,inn}}$, $\rho_{0,\text{inn}}$, and t_{inn} , even if a value of α_{inj} is known. Its formal fit with the SYNAGE is $0.606^{+0.079}_{-0.096}$ and $0.611^{+0.062}_{-0.086}$ for the innSE and innNW lobes, respectively. Therefore for the purpose of DYNAGE calculations, we assume here that a maximum value of α_{inj} cannot exceed the values of 0.606 and 0.611, but can be as low as 0.510 and 0.525, respectively. Moreover, the width of the inner cocoon can be larger than the lobes' widths determined from the images in Fig. 2, therefore we admit a twice larger width for these lobes corresponding to $R_{\text{T}} = 6.5$ (instead of 11.8 and 10.6) supposing that the best age solution for the innSE lobe lies within the model space parameters limited from one side by the values $\alpha_{\text{inj}} = 0.606$ and $R_{\text{T}} = 11.8$, and from the other side by $\alpha_{\text{inj}} = 0.510$ and $R_{\text{T}} = 6.5$. For the opposite innNW lobe, the limiting pairs of the model parameters are $\alpha_{\text{inj}} = 0.611$, $R_{\text{T}} = 10.6$ and $\alpha_{\text{inj}} = 0.525$, $R_{\text{T}} = 6.5$.

The sets of solutions resulting from the fit of the model's free parameters to the linear size and the radio powers of the inner lobes (given in Cols. (4) and (5) of Table 5), are presented in Fig. 10. This diagram clearly shows that the spaces of model parameters for the opposite inner lobes do not overlap. Obviously the lobes' asymmetries in the luminosity and size are too large to allow a comparable age and jet power solution in the model. Moreover, a selection of adequate pair of $Q_{\text{jet,inn}}$ and t_{inn} values is not possible until a value of $\rho_{0,\text{inn}}$ is fixed by means of some additional constraint.

Let us therefore consider the limiting values for the core density $\rho_{0,\text{inn}}$ within the old outer lobes. On the one hand, the upper limit for the cold gas density may therefore be provided by studies of the internal depolarization of radio emission produced by the extended lobes of FR II-type radio galaxies. For example, Garrington & Conway (1991) found that the product of the cold gas number density and the lobes' magnetic field strength is on average $n_{\text{g}} \times B < 0.5 \times 10^3 \text{ m}^{-3} \text{ nT}$. This, with the $B_{\text{eqv}} \approx 0.64 \text{ nT}$ determined for the inner lobes in Sect. 4.2, gives roughly $\rho_{0,\text{inn}} \approx m_{\text{p}} n_{\text{g}} < 1.3 \times 10^{-24} \text{ kg m}^{-3}$. We note in this context that the above equipartition magnetic field strength is compatible with the typical values $0.3 \text{ nT} < B < 3 \text{ nT}$ found by means of multiwavelength analysis of the non-thermal lobes' emission (e.g. Kataoka & Stawarz 2005; Croston et al. 2005). However, the ambient gas density within the old cocoon of DDRGs is likely lower than that of the typical FR II-type sources with linear sizes comparable to those characteristic for the inner double structures. It can be supposed that $\rho_{0,\text{inn}} < \rho_{\text{a,out}}$, where $\rho_{\text{a,out}} = \langle \rho_{0,\text{out}} \rangle (D_{\text{out}}/a_0)^{-1.5}$. With $\langle \rho_{0,\text{out}} \rangle \approx 5.4 \times 10^{-23} \text{ kg m}^{-3}$ and $D_{\text{out}} \approx 500 \text{ kpc}$, we have $\rho_{0,\text{inn}} < 1.6 \times 10^{-25} \text{ kg m}^{-3}$. This

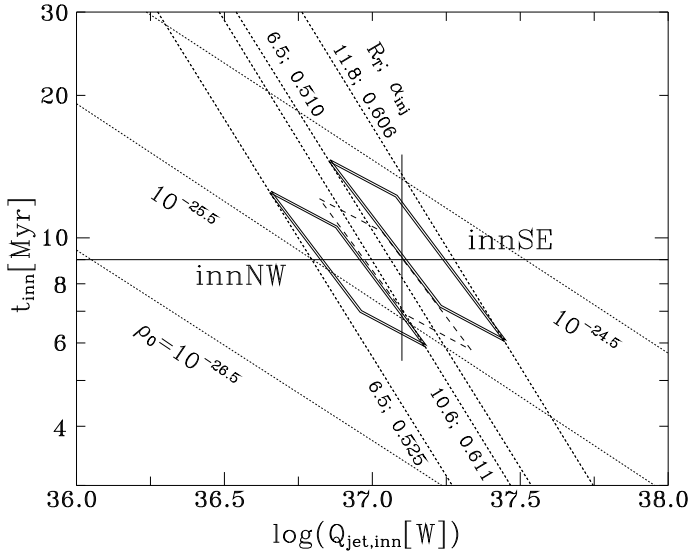


Fig. 10. Model solution for the inner lobes. The two pairs of dotted diagonal lines for each of the lobes indicate the age vs. jet-power relation corresponding to the limiting values of the lobe’s axial ratio, R_T , and injection spectral index, α_{inj} , marked in the diagram. The diamond-shaped solid-line areas show credible dynamical age solutions for the two lobes. The dashed diamond indicates an alternative solution for the innNW lobe providing an equalization of the jet powers for the opposite lobes (cf. the text). The solid vertical line indicates the value of Q_{jet} adopted for the alternative age solution.

value, corresponding exactly to the baryon density of 10^{-4} cm^{-3} (10^2 m^{-3}) typical for the intracluster medium (ICM) of nearby ($z < 0.2$) clusters of galaxies (Croston et al. 2008), can be considered as a very upper limit for $\rho_{0,inn}$.

On the other hand, the lower limit is provided by an amount of matter injected into the outer lobes by the old jet, which is

$$\rho_{0,inn} \approx m_p n_p > \frac{Q_{jet,out} t_{out}}{V_{out} \Gamma_{jet} c^2 (1+k)},$$

where m_p , n_p , and n_e are proton mass, proton, and electron number densities, respectively, and $k = n_e/n_p$. Allowing for mildly relativistic value of v_{jet} on large scales and only slight electron dominance in terms of number density within the outflow (Sikora & Madejski 2000; Celotti & Ghisellini 2008), one can expect roughly $\Gamma_{jet}(1+k) < 10$, and thus the lower limit for the gas density within the old cocoon $\rho_{0,inn} > 10^{-30} \text{ kg m}^{-3}$. However, such a density is extremely low and insufficient to explain the observed characteristics of the inner structure. Indeed, power of the jet propagating through the medium with $\rho_{0,inn} \gtrsim 10^{-30} \text{ kg m}^{-3}$ and $\beta = 0$ (calculated from suitably transformed Eq. (4)) sufficient to expand a lobe with $R_T \approx 11$ ($c_1 \approx 4$) to the length $D \approx 150 \text{ kpc}$ with the speed $v_h \lesssim c$, i.e. during $t \gtrsim 0.5 \text{ Myr}$, is $\sim 5 \times 10^{35} \text{ W}$. Therefore, in the framework of the KDA model, the power radiated out at the frequency of 1.4 GHz will only be about $\sim 1.4 \times 10^{18} \text{ W Hz}^{-1} \text{ sr}^{-1}$, i.e. almost five orders of magnitude lower than the observed one! Kaiser has (2000) already argued that some “additional material must have passed from the environment of the source through the bow shock surrounding the outer source structure into the cocoon”.

Perhaps a better lower limit for the gas density results from the numerical simulation of an intermittent jet by Clarke & Burns (1991). They show that the restarted jet must propagate through a thermalized material left by the old jet, and this medium is about 40 times less dense than the initial ambient

medium. In our case $\rho_{0,inn} > \rho_{0,out}(D_{inn}/a_0)^{-1.5}/40$. Therefore we estimate that $2.5 \times 10^{-26} < \rho_{0,inn} < 1.6 \times 10^{-25} \text{ kg m}^{-3}$. Taking a mean of these extreme values, $\langle \rho_{0,inn} \rangle = 6.3 \times 10^{-26} \text{ kg m}^{-3}$, we achieve further limits for the space of parameters in Fig. 10. The vertices of the solid-line-marked diamonds in Fig. 10 indicate solutions of t_{inn} and $Q_{jet,inn}$ for $\langle \rho_{0,inn} \rangle = 6.3 \times 10^{-26} \text{ kg m}^{-3}$ and the four combinations between the values of α_{inj} and R_T : (i) 0.611 and 10.6; (ii) 0.611 and 6.5; (iii) 0.525 and 10.6, and (iv) 0.525 and 6.5 for the innNW lobe for instance. In particular, the marked areas indicate that the dynamical age of the inner lobes is within a range of 6–13 Myr, which is in accordance with the synchrotron age derived in Sect. 4.2.

The value of $\langle \rho_{0,inn} \rangle$ adopted in our calculations is more than two orders higher than its estimate in S2008 ($< 5 \times 10^{-28} \text{ kg m}^{-3}$) and close to the ionized gas density in clusters of galaxies (cf. Croston et al. 2008). This seems to contradict the finding of SSS2003 that the investigated radio galaxy is not in a cluster, and one could expect that the gas density inside the old cocoon is much lower than the value $\langle \rho_{0,inn} \rangle$ adopted in the above calculations unless an efficient entrainment process occurs. However, an order of magnitude decrease in this value, i.e. to about $6 \times 10^{-27} \text{ kg m}^{-3}$, will result in a two-fold decrease in the estimated age of the inner structure only, i.e. to about $\gtrsim 3 \text{ Myr}$.

Nevertheless, there is a way to avoid any assumption about the environment’s density. It is not an easy task to detect and measure the high-frequency radio spectrum of the inner lobes. The calculation of the flux density expected from the model with $\alpha_{inj} = 0.56$, $Q_{jet,inn} = 1.26 \times 10^{37} \text{ W}$, $\rho_{0,inn} = 6.8 \times 10^{-26} \text{ kg m}^{-3}$, $R_T = 11$, and $t = 9 \text{ Myr}$ are 20.6 mJy, 11.0 mJy, 4.6 mJy, and 1.9 mJy at $\nu = 10.6, 30, 90$, and 230 GHz, respectively. Supplementing the observed spectrum with the above flux densities and fitting the CI model of energy losses, we find $\nu_{br} = 110.4 \text{ GHz}$, which with $B_{eqv} = 0.45 \text{ nT}$ gives $\tau_{syn} = 8.6 \text{ Myr}$.

Similar to the outer lobes, the independent solutions for the inner lobes cannot provide comparable jet powers for the opposite lobes. The diamond-shaped areas in Fig. 10 are significantly separated along the abscissa. We therefore consider an alternative solution of their age.

5.4. Alternative solution

An explanation of the difference in $Q_{jet,inn}$ values by different external density profiles along the opposite new jets is problematic if we assume a constant density with $\beta = 0$. The nearer opposite sides of the “diamonds” correspond to the largest acceptable differences between the parameters R_T and α_{inj} . Even completely different values of these parameters for the opposite inner lobes do not allow even a partial superposition of these diamonds in the (\log) plane $t_{inn}-Q_{jet,inn}$. However, as pointed out and discussed in MJS2009, a plausible equalization of Q_{jet} values can be achieved by changing the ratio between the energy densities of magnetic field and of particles, ζ . For example, the six-fold decrease of ζ in the innNW lobe results in desired increase in $Q_{jet,inn}$ in this lobe. This *alternative* solution is marked in Fig. 10. We discuss this solution in Sect. 6.2.

Adopting the jet power, $\langle Q_{jet,inn} \rangle = 1.26 \times 10^{37} \text{ W}$, which intersects the diamond-shaped areas in the middle indicating the *independent solution* range for the innSE lobe and the *alternative solution* for the innNW lobe (Fig. 10), and considering that $\langle \rho_{0,inn} \rangle = 6.3 \times 10^{-26} \text{ kg m}^{-3}$, as well as $\beta = 0$, a probable age of the inner lobes estimate, t_{inn} , is given by Eq. (4) where the parameters denoted with “out” are replaced by those denoted with “inn”. Given two different values of c_1 corresponding to two extreme values of R_T adopted here for either lobe, the age estimate

Table 7. Fitted physical parameters of the inner lobes for different values of the lobe’s axial ratio R_T .

Parameter	Indepen. solution		Alternat. solution	
	---innSE---	(3)	---innNW---	(5)
(1)	(2)	(3)	(4)	(5)
R_T	11.8	6.5	10.6	6.5
α_{inj}	0.510	0.605	0.525	0.610
$Q_{\text{jet,inn}} (\times 10^{37} \text{ W})$	1.53	1.21	1.39	1.34
$\rho_{0\text{inn}} (\times 10^{-26} \text{ kg m}^{-3})$	7.70	6.07	7.17	6.13
$t_{\text{inn}} (\text{Myr})$	7.9	12.0	6.3	8.8
$p_{\text{c,inn}} (\times 10^{-14} \text{ Pa})$	2.91	3.34	3.45	4.10
$B_{\text{inn}} (\text{nT})$	0.20	0.22	0.22	0.24
$U_{\text{inn}} = u_c \times V (\times 10^{50} \text{ J})$	1.50	5.66	1.27	3.44
$D/(t \times c)$	0.072	0.047	0.075	0.053
$v(r = a_0)/c$	0.286	0.189	0.267	0.189
$v(r = D_{\text{inn}})/c$	0.043	0.028	0.045	0.032

is between 6.3 and 8.8 Myr, and between 7.9 and 12.0 Myr for the innNW lobe and innSE lobe, respectively.

A number of physical parameters fitted with the model for the inner lobes of J1548–3216, with the ages as above, are provided in Table 7. Columns (2) and (3) give their values for the innSE lobe with $R_T = 11.8$ and innNW lobe with $R_T = 10.6$, respectively, while Cols. (4) and (5) give their values for these lobes but with $R_T = 6.5$. Although the fitted values of $Q_{\text{jet,inn}}$ and $\rho_{0\text{inn}}$ differ a little from the values $\langle Q_{\text{jet,inn}} \rangle = 1.26 \times 10^{37} \text{ W}$ and $\langle \rho_{0\text{inn}} \rangle = 6.3 \times 10^{-26} \text{ kg m}^{-3}$ used to estimate the age from Eq. (4), their ratio $\rho_{0\text{inn}}/Q_{\text{jet,inn}}$ always equals $\langle \rho_{0\text{inn}} \rangle / \langle Q_{\text{jet,inn}} \rangle$. This occurs because of the property of the DYNAGE algorithm allowing determination of the values of both ρ_0 and Q_{jet} by the fit of the model free parameters to the observed size and power of a given source (lobe). The last two lines in Table 7 give the expansion velocity of the jet’s head resulting from the model and exhibit its deceleration with time. Since the length of the jet is

$$r(t) = c_1 \left(\frac{Q_{\text{jet}}}{\rho_0 a_0^\beta} \right)^{1/(5-\beta)} t^{3/(5-\beta)}, \quad \text{implying that} \quad (6)$$

$$v(t) = \frac{dr}{dt} = \frac{3 c_1}{5-\beta} \left(\frac{Q_{\text{jet}}}{\rho_0 a_0^\beta} \right)^{1/(5-\beta)} t^{(\beta-2)/(5-\beta)}, \quad \text{or} \quad (7)$$

$$v(r) = \frac{3 c_1}{5-\beta} \left(\frac{Q_{\text{jet}}}{\rho_0 a_0^\beta} \right)^{1/3} \left(\frac{r}{c_1} \right)^{(\beta-2)/3}. \quad (8)$$

The next to last line in Table 7 gives the expansion velocity at the assumed radius of the radio core a_0 , while the last one gives this velocity at the actual length of the given inner lobe D_{inn} .

6. Discussion of the results

In the sections below, we discuss the derived ages and physical parameters of the source, both its outer and inner double structures, as well as those associated with the original unperturbed ambient environment and the relict cocoon.

6.1. Spectral age of the outer and the inner structures

As expected, the synchrotron age of both the outer lobes, τ_{syn} , increases with distance from their edges. It starts from ~ 25 Myr and rises to about 65–75 Myr in the centre of the old cocoon.

The lowest estimated age, far from the zero value, can be related to the time that passed from the last acceleration of the emitting particles at the region of the old jet interaction with the original unperturbed IGM. However, in a number of similar spectral-ageing analyses (cf. Liu et al. 1992; Jamrozny et al. 2005, 2008) a mean of the ratio between the youngest and the oldest emitting particles is always about 0.40 ± 0.15 and is weakly dependent on the size and/or the age of sources. It means that the youngest synchrotron age is found usually between 5 Myr and 20 Myr for FR II-type sources with $D \gtrsim 100$ kpc and $t \gtrsim 20$ Myr (cf. Machalski et al. 2004). Similar values (~ 18.7 Myr and ~ 20.3 Myr) have been found in the detailed ageing analysis of the DDRG J1453+3308 (Konar et al. 2006), for which the time that passed since the jets stopped actively feeding the hot spots was estimated by Kaiser et al. (2000) as about 1.1 Myr. We return to this point again in Sect. 6.3.

The evidently curved age–distance tracks in Fig. 8, especially for the outNW lobe, support the expected deceleration of the jet head’s advance speed and probable backflow present in giant radio galaxies (e.g. Schoenmakers et al. 1998; Lara et al. 2000). Indeed, the advance speed of the jet’s head given by Eq. (8), $v(r) \equiv v_{\text{hs}}$, and a backflow velocity, v_{bf} , will form opposite vectors. If a quotient of separation between the strips in Table 4 and a difference between the derived spectral (synchrotron) ages in these strips, $\Delta r / \Delta \tau_{\text{syn}} = \langle v_{\text{syn}} \rangle$, is more than $v(r)$ at a given distance from the core, a backflow is present. If $\langle v_{\text{bf}} \rangle = \epsilon \langle v_{\text{hs}} \rangle$, then $\langle v_{\text{syn}} \rangle = (1 + \epsilon) \langle v_{\text{hs}} \rangle$. For example, the entries in Table 4 show that, in outSE lobe at $r = 332$ kpc, $\epsilon \approx 2.2$ and $v_{\text{bf}} \approx 0.024 c$, while closer to the core at $r = 131$ kpc: $\epsilon \approx 1.3$ and $v_{\text{bf}} \approx 0.017 c$. In outNW lobe at $r = 300$ kpc, $\epsilon \approx 2.0$ and $v_{\text{bf}} \approx 0.024 c$, while at $r = 98$ kpc: $\epsilon \approx 0.4$ and $v_{\text{bf}} \approx 0.005 c$.

A spectral age for the new inner lobes is quite problematic. Since this structure is relatively smaller and much fainter than the outer structure, we were not able to cut it into strips and to check whether and how much the spectral index varies along the lobes. The spectral index map derived from the the ATCA+VLA and VLA images at 1384 and 2495 MHz, published by S2008 (their Fig. 5), does not indicate any steepening that would signal a spectral ageing. Though the flux densities measured in the entire inner lobes (cf. Cols. (5) and (6) in Table 2) allowed the CI model fit to the data and an estimate of spectral breaks in the observed spectra, the fit’s uncertainty is so large that the resulting “mean” spectral ages within the lobes are very uncertain as being formally in a range from ~ 0.1 Myr to ~ 14 Myr. Taking an uncertainty of the R_T value of the inner lobes into account (which determines their volume, V , used to estimate B_{eqv}), and that even the axial expansion of the lobes with the speed of light would require the time of ~ 0.5 Myr, we may adopt that a spectral age of these lobes is about 9 ± 5 Myr.

6.2. Dynamical age of the outer and the inner structures

Following similar ageing analysis made by MJS2009 for a limited sample of ten giant radio galaxies, we solved the dynamical age and other physical parameters of the two outer lobes independently and explored the resulting formal differences between those fitted parameters that should actually not differ in the opposite lobes, like the jet power and the central core density. In this way we can perform a deeper search for properties of the surrounding ambient medium and conditions of the jets’ propagation during the active phases of the jet production in the common central engine. In the two kinds of proposed *self-consistent* solutions, we require identical values of Q_{jet} and ρ_0 for the opposite lobes both of the outer and of the inner structures. However,

in MJS2009 we showed that the fits with such an assumption results in either decreasing or enlarging the age difference between the lobes, depending on the actual asymmetries in the lobes' length and luminosity. The *self-consistent* solution A for the outer lobes of J1548–3216 enlarges the age difference from ~ 20 Myr in the *independent* solution to ~ 27 Myr (cf. the entries in Cols. (2)–(5) in Table 6). As the above differences are too large to be caused by a projection of the source on the sky, we consider the solution B in which we demand the same age for both lobes. Taking a mean of the age values in the independent solution, i.e. $\langle t_{\text{out}} \rangle = 132$ Myr, we find it as satisfactory for the outer lobes. This is worth emphasizing that this age fully agrees with its estimate in S2008, (30–200) Myr, though they derive it from another consideration about the energy budget.

As expected, the *self-consistent* solution B suggests different exponents $\beta_{\text{sc,B}}$ in the power-law density profiles and different *effective* injection spectral index α_{inj} , where $\beta_{\text{sc,B}}$ value (according to Eq. (6)) governs the lobe's length, while α_{inj} value influences the energy losses and the resulting brightness of a given lobe. Different fitted values of $\beta_{\text{sc,B}}$ and α_{inj} for the opposite outer lobes result in about twice higher IGM density at the edge of the outer NW lobe as compared to that at the SE lobe. As a result, the bright rim and the two “warm” spots in the outNW lobe may indicate a higher pressure ratio between the lobe's head and the IGM, in other words, this lobe may be more overpressured than the opposite outSE lobe.

The age for the inner structure is estimated by assuming a scenario in which the new restarted jets propagate within rarefied and uniform ($\beta_{\text{inn}} = 0$) medium of the old outer cocoon formed by the old jet material that passed through the jet terminal shock and eventually partly mixed with the surrounding thermal gas (cf. the discussion in Kaiser et al. 2000). The assumption of uniformity is justified by the fact that the sound crossing time within the outer lobes is much longer than the dynamical timescales of evolution of the outer structure. In the case of the inner structure, the age solution is formally undefined due to almost pure power-law radio spectrum of the new lobes. On the one hand, such a lack of the spectrum steepening can tell us that the structure is rather young; on the other hand, it prevents determination of its quantitative value (cf. also SSS2003). In the framework of the DYNAGE algorithm the inability to specify an explicit age solution means that the space of the model's free parameters (Q_{jet} , ρ_0 , t , α_{inj}) is very large (the space between two diagonal lines for a given lobe in Fig. 10). Within this space, kinetic energy of the jet, $Q_{\text{jet}} \times t$, is almost constant, so that the criterion of its minimum (a crucial aspect of the algorithm) is not applicable. As shown in Sect. 5.3, the above space can be reduced a little by fixing values of some of these parameters, e.g. the value of ρ_0 (hence the diamond-shaped areas in Fig. 10).

However, the straight, unaged spectra of the inner lobes are not just a single factor precluding age determination. The other one is asymmetry both in their length and brightness, which causes the spaces of parameters allowed for the opposite lobes to not overlap each other. The assumption of uniform density of the pre-existing cocoon with $\beta = 0$ precludes a differentiation of this parameter for the lobes, thus we pointed out another parameter that also rules the age solution, namely the ratio between energy densities of the magnetic field and of the particles, ζ . The calculations indicate that a significant departure from the equipartition conditions in one of the inner lobes (but not in the opposite one) enables a relative equalization of the jet powers and attainment of comparable ages for both lobes. Therefore, a combination of the *alternative* solution for the innNW lobe and the *independent* one for the innSE lobe is required to attain comparable values of

the three parameters involved: $Q_{\text{jet,inn}}$, $\rho_{0,\text{inn}}$, and t_{inn} . Although this alternative age solution for the innNW lobe is only a numerical result of the fitting algorithm, such a departure seems to be supported by X-ray observations, which allow measurements of electron energies of radio lobes and magnetic fields. In the lobes of the well-studied nearby radio galaxies Centaurus B and Fornax A, the inferred electron energy densities exceed those of magnetic fields by a factor of 5–8 (cf. Tashiro et al. 1998, 2009; Isobe et al. 2006).

Of course, the above combined age solution is odd, in which a significant departure from equipartition conditions happens in only one lobe of the inner double structure evolving in supposedly uniform medium, $\rho_{0,\text{inn}} \approx \text{const}$. Perhaps, these different conditions might arise when the magnetic field within the old cocoon is strongly inhomogeneous giving rise to enhanced observable radiation in the high-field regions (cf. Eilek et al. 1997; Kaiser 2005). An inhomogeneity of the field may indicate a faint blob of emission detected at all the observed frequencies between the radio core and the bright end of the innNW lobe (cf. Fig. 2). Understanding an expected criticism of the above speculations, we argue that the estimated dynamical age of the inner lobes of the investigated radio galaxy, $t_{\text{inn}} \approx 9 \pm 4$ Myr, is plausible. This age accords with its spectral age estimate given in Sect. 5.3.

6.3. Kinetic energy and internal pressure

Kinetic energy delivered by the original jets to the old cocoon during the time of ~ 132 Myr is found to be $\sim 10^{54}$ J, while the energy radiated out is $\sim 1.3 \times 10^{53}$ J (cf. entries in Table 6). The latter value is about twice higher than estimated in S2008 using another approach to the energy budget. One of the important results of our dynamical analysis is the power of the old and the new jets. We find that the jet power during the previous phase of the nuclear activity was $\sim 1.2 \times 10^{38}$ W, while the power of the new jets (although we could only determine a range of its value $\sim 5 \times 10^{36}$ W to $\sim 3 \times 10^{37}$ W; cf. Fig. 10) seems to be almost one order less than the former one, but in a good agreement with its range of $[1.1, 4] \times 10^{44}$ erg s $^{-1}$ if $55^\circ < \theta < 78^\circ$ estimated by S2008 (cf. their Fig. 16). Such a high ratio $Q_{\text{jet,out}}/Q_{\text{jet,inn}}$ impairs results of the ageing analysis of a few other DDRGs published by Kaiser et al. (2000) in which they assumed the same Q_{jet} values during two successive phases of activity. The difference between the outer and inner jet power found in our analysis may indicate that the spin of the central BH cannot be the only factor determining the total power of the relativistic outflow, since this spin is not expected to change significantly in a relatively short timescale, which would be involved. However, we note that, in the original Blandford & Znajek (1977) model, the power of the outflow extracted from the ergosphere of the rotating BH depends not only on the BH spin, but also on the magnetic field intensity within the innermost parts of the accretion disk, which in turn should depend on the accretion rate (or, possibly, on the accretion mode). Thus, the difference between the power of the original and the restarted jet in the radio galaxy J1545–3216 may still be reconciled with the modified spin paradigm (Sikora et al. 2007; Sikora 2009) if the accretion disk undergoes significant structural changes between different activity epochs in a single source.

The DYNAGE algorithm clearly shows that a demand of $Q_{\text{jet,out}} \approx Q_{\text{jet,inn}}$ would lead to an unlikely solution of the model for the inner structure with the lobes' age $t_{\text{inn}} \approx 0.8$ Myr, the old cocoon density $\rho_{0,\text{inn}} \approx 3.3 \times 10^{-28}$ kg m $^{-3}$, and the average expansion speed $D_{\text{inn}}/t_{\text{inn}} \approx 0.61 c$! One can conclude that until

an independent measure of $\rho_{0,\text{inn}}$ is available (e.g. from internal depolarization of radio emission and/or X-ray inverse-Compton emission from the region of the inner lobes), a numerical algorithm like the DYNAGE will not be able to specify more accurate values of $Q_{\text{jet,inn}}$, t_{inn} , $D_{\text{inn}}/t_{\text{inn}}$, etc.

The internal (cocoon) pressures, p_c , resemble the jets' disporportion. The pressure in the old cocoon, derived from the fit, is about five times higher than the pressure estimate within the new younger lobes (cf. the entries in Tables 5 and 7). However, this is a result of the different equations of state assumed for the jet, particle, and magnetic field “fluids”: non-relativistic for the old cocoon and the relativistic one for the inner double structure. If $\beta = 0$, the cocoon pressure is

$$p_c \propto \left(\frac{Q_{\text{jet}}}{\rho_0} \right)^{2/5} \rho_0 t^{-4/5}.$$

For a lobe with given D and R_T we find from Eq. (6) that $(Q_{\text{jet}}/\rho_0) \times t^3 = \text{const.}[\text{m}^5]$. Thus

$$p_c \propto \rho_0 t^{-2}.$$

Assuming the non-relativistic equation of state for a lobe at age t , the model requires a higher jet power and predicts proportionally the higher core density needed to fit the lobe's length and power, higher than the values of Q_{jet} and ρ_0 fitted in the relativistic case. As a result, in the lobe at age t , $p_c \propto \rho_0$. The calculations show that even a large decrease in the lobe's age gives little increase of p_c , so that the pressure achieved in the non-relativistic case is not attainable.

6.4. Magnetic fields

With the standard assumption about the energy equipartition between the relativistic particles and magnetic fields, the derived strength of uniform magnetic field in the outer lobes, B_{eqv} , slightly varies from ~ 0.33 nT at the edges of the lobes to ~ 0.24 nT in the centre of the old cocoon. Similar values are derived from the magnetic energy density, u_B , via the dynamical considerations. For the inner lobes, the field estimates are incompatible with the values derived with the Miley (1980) formula during the spectral-ageing analysis, which are almost twice higher than the corresponding values implied by the dynamical analysis. Our calculations (in the framework of the KDA model) show that, to increase strength of magnetic field in the inner lobes to its level derived from the spectral analysis, it is necessary to assume the non-relativistic equations of state for the jet's material and the magnetic field “fluids”, as well as to admit some admixture of thermal particles. Obviously such an assumption would level out the propagation conditions during the initial and the restarted phases of activity, which is rather unacceptable.

7. Conclusions

The new low-frequency and high-frequency radio continuum maps of the double-double radio galaxy J1548–3216 (PKS 1545–321) are used to complement its already published maps at 22 and 13 cm (Saripalli et al. 2003; Sefouris et al. 2008) and to perform both the spectral-ageing and the dynamical analysis of this remarkable giant DDRG, in which the newly restarted jets propagate through the bright cocoon formed by a previous active phase of its AGN. The current activity is indicated by the radio core.

The maps of the outer and the inner radio lobes at five observing frequencies from 334 to 4860 MHz allow determination

of the spectral index distribution along the outer lobes, as well as extension of the spectral index frequency range in the inner lobes. The spectral index distribution in the outer lobes implies a distribution of the spectral (synchrotron) age of emitting particles along the ridge of these lobes, which increases from about 25 Myr at the edges of the extended old cocoon structure to about 65–75 Myr in the vicinity of the core. A velocity equivalent to the quotient of separation between the selected positions on the ridge and the difference in synchrotron age between these positions, which is higher than the advance speed of the jet's head, indicates a significant backflow in the old cocoon. Moreover, its average speed evidently decreases from the cocoon's edges towards the core.

Using the DYNAGE algorithm (Machalski et al. 2007), we attempted to specify the dynamical age of both the outer and the inner pairs of radio lobes. Because each pair is characterized by a specific asymmetry in the lobes' length and brightness, we searched for a self-consistent solution of the analytical model, Demanding the same values for the jet power, central core density, and a comparable age for the opposite lobes, we find that:

- (1) The age of the outer and the inner lobes is 132 ± 28 Myr and $\sim 9 \pm 4$ Myr, respectively. However the derived age of the inner lobes is quite problematic because the almost pure power-law spectrum of its lobes prevents a unique age solution without any independent knowledge of either the restarted jet power or the ambient density within the old cocoon through which it propagates. This problem is solved with the assumption of limiting values for the latter parameter discussed in detail in Sect. 5.3.
- (2) If the above assumption is correct, the jet powers during the initial and the restarted phase of activity are not similar. The restarted jet is one order less powerful than the original one. We think that this can support a hypothesis that the jet power is much more dependent (if not only) on the intermittent jet activity, than on the spin of a black hole. This intermittent activity can be connected with a stochastic transition between two accretion modes – the standard one where the angular momentum is transmitted outwards by viscous torques within a disk and – the “magnetic” one, in which large-scale poloidal fields are developed (cf. Nipoti et al. 2005; Körding et al. 2006).
- (3) The magnetic field strength estimates along the ridge of the outer double structure vary slightly from the edges of the lobes towards the centre of the old cocoon. Unexpectedly, the field strengths in the inner lobes resulting from the dynamical analysis seem to be twice lower than the corresponding values estimated in the spectral-ageing analysis. This discrepancy arises from the assumed different adiabatic indices in the equations of state: a non-relativistic one for the outer structure and the relativistic one for the inner double structure. The non-relativistic equation of state implies some energy dissipation process between magnetic field and thermal particles whose presence in the old cocoon is expected. Therefore in the non-relativistic conditions for the magnetic energy evolution, a stronger magnetic field would be necessary to account for the observed brightness of the inner lobes.

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Appendix A

Table A.1. Notations for the free parameters in the DYNAGE algorithm and other physical parameters used through the paper.

Symbol	Dimension	Parameter
	Model	free parameters to be assumed
a_0	[kpc]	radius of central core
β	[dim. less]	exponent of ambient medium-density profile
$\gamma_{\min}, \gamma_{\max}$	[dim. less]	Lorentz factors of relativistic particles
$\Gamma_{\text{jet}}, \Gamma_{\text{B}}, \Gamma_{\text{x}}, \Gamma_{\text{c}}$	[dim. less]	adiabatic indices of the jet, magnetic field, ambient medium, and cocoon as a whole
ζ	[dim. less]	initial ratio of energy density of the magnetic field to that of particles
k'	[dim. less]	ratio of energy density of thermal particles to that of relativistic ones
θ	[°]	orientation of the jet's axis
	Model	parameters to be fitted
α_{inj}	[dim. less]	injection spectral index
t	[Myr]	dynamical age
Q_{jet}	[W]	jet power
ρ_0	[kg m ⁻³]	central core density
	Other	physical parameters
$\beta_{\text{sc,A}}, \beta_{\text{sc,B}}$	[dim. less]	exponents of ambient density profile in the self-consistent age solution A and B
$p_{\text{hs}}, p_{\text{min}}, p_{\text{c}}$	[N m ⁻²]	hot-spot pressure, its minimum (equipartition) pressure, and cocoon pressure
$u_{\text{e}}, u_{\text{B}}, u_{\text{c}}$	[J m ⁻³]	energy density of relativistic particles, in magnetic field, and in cocoon as a whole
$U_{\text{out}}, U_{\text{inn}}$	[J]	total energy radiated from outer and inner lobes
$B, B_{\text{eqv}}, B_{\text{iC}}$	[nT]	strength of magnetic field, equipartition field, and inverse-Compton field
k	[dim. less]	ratio of energy density of relativistic particles to that of electrons
$n_{\text{p}}, n_{\text{e}}, n_{\text{g}}$	[m ⁻³]	proton, electron number density, and cold-gas number density
m_{p}	[kg]	proton mass
ρ_{a}	[kg m ⁻³]	ambient medium density
$\langle t_i \rangle$	[Myr]	mean of t fit for the opposite lobes; $i \Rightarrow$ out, inn
$\langle Q_{\text{jet},i} \rangle$	[W]	mean of Q_{jet} fit for the opposite lobes
$\langle \rho_{0,i} \rangle$	[kg m ⁻³]	mean of ρ_0 fit for the opposite lobes
$\langle \rho_{\text{a},i} \rangle$	[kg m ⁻³]	mean of ρ_{a} derived for the opposite lobes
τ_{syn}	[Myr]	spectral (synchrotron) age
ν_{br}	[GHz]	frequency of spectral break

Notes. (excluding observational parameters of the radio source: $D, R_{\text{T}}, V, P_{\text{v}}, \alpha_{\text{v}}$, defined in the text).

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