# <sup>1</sup>/<sub>2</sub> Butane dihedral angle dynamics in water is <sup>3</sup>/<sub>4</sub> dominated by internal friction

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10The dihedral dynamics of butane in water is known to be rather insen-11 sitive to the water viscosity, possible explanations for this involve 12inertial effects or Kramers' turnover, the finite memory time of fric-13tion, and the presence of so-called internal friction. In order to dis-14entangle these factors, we introduce a method to directly extract the 15friction memory function from simulations in the presence of an arbi-16trary free-energy landscape. By analysis of the dihedral friction in bu-17tane for varying water viscosity, we demonstrate the existence of an 18 internal friction contribution. At normal water viscosity the internal 19 friction turns out to be eight times larger than the solvent friction and 20thus completely dominates the effective friction. By comparison with 21simulations of a constrained butane molecule that has the dihedral 22as the only degree of freedom, we show that internal friction comes 23from the six additional degrees of freedom in unconstrained butane 24that are orthogonal to the dihedral angle reaction coordinate. While 25the insensitivity of butane's dihedral dynamics to water viscosity is 26solely due to the presence of internal friction, inertial effects never-27theless crucially influence the resultant transition rates. In contrast, 28non-Markovian effects due to the finite memory time are present but 29do not significantly influence the dihedral barrier crossing rate of 30 butane. These results not only settle the character of dihedral dy-31 namics in small molecular systems such as butane, they also have 3233 important implications for the folding of polymers and proteins.

35 molecular friction  $\mid$  reaction rates  $\mid$  memory effects

or the understanding of conformational and biochemical 3738reactions, a low-dimensional stochastic description in suit-39 able reaction coordinates is a powerful approach. In particular 40in the context of protein folding, diffusion in a one-dimensional 41 free-energy landscape is a prominent model to come to terms 42with the high-dimensional phase-space dynamics of proteins (1– 433). By projection onto a one-dimensional reaction coordinate, 44orthogonal degrees of freedom produce effective friction and 45random force contributions (4, 5). These byproducts of pro-46 jection cannot be neglected, since friction decisively influences 47reaction rates (6). 48

Obviously, the friction that characterizes a protein folding 49 coordinate contains contributions from the surrounding solvent 50as well as from internal protein degrees of freedom (7), but it 5152is less clear how to separately measure these two contributions 53(experimentally or in simulations). Typically, the prime object 54in protein studies concerned with friction effects is the folding time  $\tau_{\rm fold}$ . In the overdamped limit, when inertia and memory 55effects are neglected,  $\tau_{\rm fold}$  scales with the effective friction 56 coefficient  $\gamma$  as  $\tau_{\rm fold} \sim \gamma^{-1}$  (6). By the addition of viscogenic 57 agents the solvent viscosity  $\eta$  increases relative to the pure 58water value; assuming that solvent and internal friction are 59additive according to  $\gamma = \gamma_{\rm sol} + \gamma_{\rm int}$  and furthermore that 60 Stokes' law holds for the solvent friction contribution,  $\gamma_{\rm sol} \sim$ 61  $\eta$ , the internal contribution  $\gamma_{int}$  can be obtained by linear 62

72extrapolation of  $\tau_{\text{fold}}^{-1} \sim \gamma_{\text{sol}} + \gamma_{\text{int}}$  down to vanishing solvent viscosity (7). Via this procedure, internal friction has been 7374demonstrated for various proteins (7-16). In fact, deviations 75from a linear dependence  $\gamma_{\rm sol} \sim \eta$  have been experimentally 76observed for some proteins (9), while for other proteins no 77 internal friction was detected at all (17). Even in simulations, 78where—in contrast to experiments—the water friction can be 79reduced and a modification of the folding free energy landscape 80 with changing viscosity can be excluded, the extrapolation 81 down to vanishing solvent friction is not trivial (18-22). 82

Furthermore, it hinges on a few critical assumptions which 83 are not necessarily satisfied in real systems: i) It was pointed 84 out that inertia effects lead to deviations from the simple 85law  $\tau_{\rm fold} \sim \gamma^{-1}$  and ultimately to Kramers turnover, which 86 can be misinterpreted as internal friction (23-25). While one 87 would intuitively think that the effective mass of a protein 88 reaction coordinate is small, the balance of effective inertial 89 and friction parameters of reaction coordinates that describe 90complex reactions is not really settled. ii) Friction will in 91general not be constant along a reaction coordinate (15, 18, 9226), so the linear additivity assumption  $\gamma = \gamma_{\rm sol} + \gamma_{\rm int}$  not 93 necessarily holds when averaged over the reaction coordinate 94 and needs to be checked directly. iii) Most serious are memory 95 effects, which decisively influence barrier crossing dynamics 96 (19, 27–29). Recently it was shown that memory effects can, 97 depending on the value of the memory time, slow down or 98even accelerate barrier crossing (30), which starkly invalidates 99the overdamped Kramers scaling  $\tau_{\rm fold} \sim \gamma^{-1}$ . 100

Previous theoretical approaches to internal friction are based on reaction times, they suffer from the indirect connection between transition times and friction and necessarily rely on various model assumptions (18-22) (not so different from

# Significance Statement

The interpretation of rates of reactions that take place in a solvent is complicated because of the entanglement of freeenergy and history-dependent friction effects. In this context, the dihedral dynamics of butane has played a paradigmatic role since it is simple yet relevant for conformational transitions in polymers and proteins. Using a novel method we directly extract the friction that governs the dihedral dynamics in butane from simulations. We show that about 89% of the total friction comes from intrinsic butane degrees of freedom that are or-thogonal to the dihedral reaction coordinate and only 11% from the solvent friction. This shows that the hydrodynamic estimate of friction severely fails even in the simplest molecular reaction.

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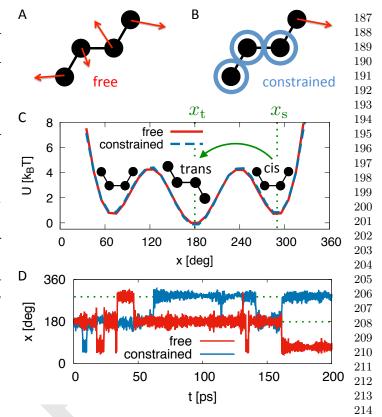
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the experimental situation). Direly needed are models which allow to check for the presence of internal friction independently of any theoretical assumptions that relate friction to reaction times, as well as methods to extract friction and memory functions directly from simulations instead of inferring friction effects indirectly from measured reaction times.

132In this paper we introduce methods to meet both chal-133134lenges. We consider butane, since it is the simplest molecule that shows a non-trivial conformational transition in a solvent 135and since it has been a testing ground for theoretical and 136experimental developments (31-42). Despite the fact that the 137138solvent has a strong influence on the equilibrium properties of 139butane (33, 41), dihedral isomerization rates are known to be quite insensitive to the solvent viscosity (19–22, 24, 36, 43–46). 140The origin of the insensitivity was argued to be due to inertial 141142and memory effects (19, 47, 48). In our work, we first simulate a single butane molecule in water and compare two scenar-143ios, the free scenario, where all four carbons can freely move, 144subject to bond length and bond angle constraints, and the 145146constrained scenario, where three carbons are fixed in space and only one terminal carbon can move. While the free energy 147148landscape for the dihedral is the same in both scenarios, the 149transition times differ for high water viscosities (which we modify in our simulations by changing the water mass) by 150a factor of ten. This unequivocally demonstrates that the 151additional butane degrees of freedom (which are orthogonal 152to the dihedral angle) in the free scenario significantly change 153154the effective friction along the reaction coordinate. Secondly, we introduce a method to extract the friction memory kernel 155that couples to the reaction coordinate, in our case the di-156hedral angle, from simulation trajectories. A memory kernel 157accounts for the fact that friction on the molecular scale is 158not instantaneous but rather depends on the system's history 159160in a non-Markovian manner. Our calculated memory kernels 161reveal that indeed the friction substantially differs between the constrained and free butane scenarios. The friction coefficients, 162which follow by an integral over the memory kernels, are used 163164to predict the transition times of the free and constrained 165butane scenarios in quantitative agreement with direct simulation results. For this we need to use reaction rate theory 166 that accounts for inertial effects. It shows that our theoret-167ical framework, which simultaneously yields reaction times 168as well as friction effects, is consistent. Finally, the internal 169170friction contribution is determined by a fit of the extracted 171total friction versus the water viscosity: for the constrained 172butane the internal contribution is negligible, as expected, 173while for the free butane the internal contribution overwhelms 174the solvent contribution by a factor of eight, which explains why the butane dihedral reaction is rather insusceptible to an 175176increase of the water viscosity.

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We unambiguously show that the dihedral angle dynam-179ics of a butane molecule is dominated by internal friction, 180181 which stems from the coupled dynamics of the four carbons. This demonstrates that internal friction exists already for the 182simplest molecular system that possesses a conformational 183transition, in line with previous works where dihedral angle 184isomerization has been argued to be a source of internal friction 185in protein folding (9, 20-22, 45, 46). 186



**Fig. 1.** Schematic illustration of (A) a free butane molecule where all four carbons can move and (B) a constrained butane where three carbons are fixed in space and only one terminal carbon can move. (C) Comparison of the free energy *U* as a function of the dihedral angle *x* for the free and constrained butane solvated in SPC/E water, extracted from simulation trajectories. The starting and target angles  $x_s$  and  $x_t$  for the calculation of the *cis*-to-*trans* dihedral barrier crossing time are indicated by dotted vertical lines. (D) Typical dihedral angle simulation trajectories for free and constrained butane for elevated water viscosity  $\eta = \sqrt{10}\eta_0$ .

### 1. Results and Discussion

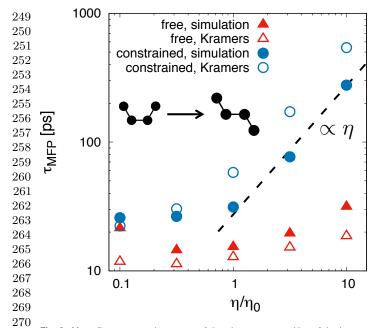
**A.** Butane dihedral barrier crossing times. In our simulations 225we place a single butane in a water box. We systematically 226vary the mass of water molecules  $m_{\rm w}$  while keeping the butane 227mass fixed. This modifies all intrinsic water time scales and 228in particular also the water viscosity according to  $\eta \propto \sqrt{m_{\rm w}}$ . 229but leaves all equilibrium distribution functions invariant (18). 230 We use a united-atom force field for butane that neglects the 231hydrogens and approximates butane by four Lennard-Jones 232beads that are subject to fixed bond lengths and fixed bond 233angles, for water we use the SPC/E model (see Materials 234and Methods). We compare the free scenario, where all four 235butane carbons can move, with the constrained scenario, where 236three carbons are fixed in space and only one terminal carbon 237can rotate, see Fig. 1A and B for an illustration. The only 238degree of freedom in the constrained scenario is the dihedral 239angle, while in the free scenario one has six additional degrees 240of freedom, three translational and three orientational. The 241free energy profiles in the free and constrained scenarios in 242Fig. 1C perfectly overlap, as expected based on translational 243and orientational invariance of the problem. 244

The mean first-passage times  $\tau_{\rm MFP}$  for the *cis*-to-*trans* 245 transition of the dihedral, as defined in Fig. 1C and extracted 246 from the simulation trajectories as shown in Fig. 1D, are 247 depicted as a function of the rescaled water viscosity  $\eta/\eta_0$  in 248

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**Fig. 2.** Mean first passage times  $\tau_{MFP}$  of the *cis*-to-*trans* transition of the butane dihedral for free (triangles) and constrained (circles) butane extracted from simulation trajectories (filled symbols) are shown as a function of the rescaled water viscosity  $\eta/\eta_0$ , where  $\eta_0$  refers to the SPC/E water viscosity. The estimates based on the Kramers formula for medium to strong friction eq. (5) are included as open symbols.

276Fig. 2 for the free and constrained scenarios. Here  $\eta_0$  denotes 277the bulk viscosity of water with the normal mass.  $\tau_{\rm MFP}$  for free 278but ne is rather insensitive to  $\eta$ , in agreement with previous 279results (19, 36). Constrained butane behaves differently for 280 $\eta > \eta_0$  and shows a linear increase of  $\tau_{\rm MFP}$  with  $\eta$  (indicated 281by a broken straight line), while for  $\eta < \eta_0$  the results for the 282free and constrained scenarios are rather similar and depend 283only weakly on  $\eta$ , which will later be explained by inertial 284effects (i.e. Kramers turnover). The stark deviation between 285the free and constrained scenarios for  $\eta > \eta_0$ , amounting to 286a difference in the reaction times by a factor of ten for the 287 highest viscosity  $\eta = 10\eta_0$ , is caused by the six additional 288degrees of freedom for free butane that are orthogonal to the 289dihedral angle coordinate. Since the dihedral free energy is 290the same for both scenarios, we conclude that the friction is 291different in the two scenarios and that this friction difference 292is caused by the additional degrees of freedom that are present 293in the free scenario and absent in the constrained scenario. 294We will later show that the difference in the total friction 295between the free and constrained scenarios is accompanied by 296an internal friction contribution for the free case. 297

**B. Memory kernels and friction coefficients.** To quantify the friction that acts on the dihedral angle, we map the dynamics of the butane dihedral angle x onto the generalized Langevin equation (GLE)

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$$m\ddot{x}(t) = -\int_0^t dt' \,\Gamma(t')\dot{x}(t-t') - \nabla U[x(t)] + F_R(t), \quad [1]$$

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306 where  $\Gamma(t)$  denotes the memory kernel. The random force 307  $F_R(t)$  obeys the fluctuation-dissipation theorem and satisfies 308  $\langle F_R(t)F_R(t')\rangle = k_{\rm B}T\Gamma(t-t')$ . For vanishing potential, the 309 GLE has been derived by linear projection techniques (4, 5). 310 The mass *m* is an effective one and follows directly from the simulated dihedral angle trajectory x(t) via the equipartition 311theorem  $m\langle \dot{x}^2 \rangle = k_{\rm B}T$  (see Materials and Methods). The 312potential U(x) in the GLE is in fact a free energy and follows 313 from the simulated equilibrium probability density along the 314reaction coordinate, p(x), as  $U(x) = -k_{\rm B}T\log p(x)$  and is 315shown in Fig. 1C. To extract  $\Gamma(t)$  from simulation trajectories 316we extend previous methods (26, 49-51) to account for a finite 317potential U(x). For this we multiply eq. (1) by  $\dot{x}(0)$  and 318average to obtain 319

$$a \langle \dot{x}(0)\ddot{x}(t) \rangle = -\int_{0}^{t} dt' \, \Gamma(t') \left\langle \dot{x}(0)\dot{x}(t-t') \right\rangle - \langle \dot{x}(0)\nabla U[x(t)] \rangle, \quad \begin{array}{c} 320\\ 321\\ 322\\ [2] & 323 \end{array}$$

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where we used that the random force is not correlated with the initial velocity, i.e.  $\langle \dot{x}(0)F_R(t)\rangle = 0$  (4). Discretizing all functions as  $\Gamma_i = \Gamma(i\Delta t)$  with a timestep  $\Delta t$  we obtain the iteration equation

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$$\Gamma_{i} = -\frac{1}{\omega_{i,i}\Delta t C_{0}^{\dot{x}\dot{x}}} \left( \sum_{j=0}^{i-1} \omega_{i,j}\Delta t \Gamma_{j} C_{i-j}^{\dot{x}\dot{x}} + m C_{i}^{\dot{x}\ddot{x}} + C_{i}^{\dot{x}\nabla U} \right),$$
[3]

332where we defined the correlation function  $C_i^{\dot{x}\ddot{x}} = \langle \dot{x}(0)\ddot{x}(i\Delta t)\rangle$ (and similarly  $C_i^{\dot{x}\dot{x}}$  and  $C_i^{\dot{x}\nabla U}$ ) and the integration weight 333 334  $w_{i,j} = 1 - \delta_{i,0}/2 - \delta_{i,j}/2$ . The correlation function  $C_i^{\dot{x}\nabla U} =$ 335  $\langle \dot{x}(0) \nabla U[x(i\Delta t)] \rangle$  is obtained by cubic spline interpolation of 336 U(x). In the SI we demonstrate the numerical robustness of 337 our method. Compared to alternative methods for the compu-338 tation of memory kernels in the presence of a finite potential 339(26, 52), the butane molecule does not have to be constrained 340 for our method, which excludes a possible uncontrolled system-341atic error caused by the confinement-dependence of molecular 342friction in water (53). 343

The extracted memory kernels  $\Gamma(t)$  for free butane in 344 Fig. 3B are quite similar for different water viscosities, while 345for constrained butane the kernels in Fig. 3A differ strongly 346for different viscosities. In particular, for free butane the long 347 time tail of  $\Gamma(t)$ , which is mostly responsible for the effective 348 friction, is almost independent of  $\eta$  and oscillations appear 349that we associate with the presence of orthogonal degrees of 350 freedom. In qualitative accordance with our results in Fig. 2 351for the barrier crossing time, we can say that for free bu-352tane, the effective friction is less sensitive to solvent viscosity 353compared to constrained butane. 354

In Fig. 4, we show the friction coefficient  $\gamma$  for free and constrained butane as a function of water viscosity, which follows from an integral over the memory function according to  $\gamma = \int_0^\infty dt \, \Gamma(t)$ . For numerical integration, we fit the long time decay of  $\Gamma(t)$  by an exponential function (see SI). The friction for constrained butane is linearly proportional to the solvent viscosity, as expected based on the hydrodynamic Stokes equation.

To make this more explicit, we denote the translational 363 friction coefficient of a methyl group by  $\gamma_{\text{trans}} = 6\pi\eta R_{\text{CH}_3}$ . 364For a methyl group of radius  $R_{\rm CH_3}\approx 0.18\,\rm nm$  that rotates at a 365 fixed bond angle  $\alpha = 111^{\circ}$  and C–C bond length  $l_{\rm B} = 0.15$  nm 366 around a fixed point in space, which approximates the con-367 strained butane case, we estimate the dihedral friction constant 368  $\gamma = (2\pi/360)^2 (l_{\rm B}\sin(\alpha))^2 \gamma_{\rm trans} = 0.01 \cdot (\eta/\eta_0) \,\mathrm{u} \,\mathrm{nm}^2/\mathrm{deg}^2 \,\mathrm{ps},$ 369 not so different from what we extract from the simulations in 370 Fig. 4 for constrained butane. In contrast, the dynamics of 371free butane is characterized by a friction coefficient that very 372

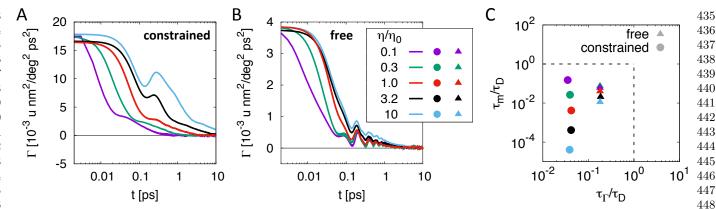


Fig. 3. Memory kernels  $\Gamma(t)$  for different rescaled water viscosities  $\eta/\eta_0$  extracted from simulation trajectories via eq. (3) for (A) constrained and (B) free butane, where  $\eta_0$  449 denotes the SPC/E water viscosity. (C) Inertial and memory timescale ratios  $\tau_m/\tau_D$  and  $\tau_{\Gamma}/\tau_D$  calculated from the memory kernels of free and constrained butane for 450 different viscosities, where  $\tau_D$  denotes the characteristic diffusion time (same color coding as in B). 451

weakly depends on the water viscosity, in stark contrast to the hydrodynamic Stokes equation. Interestingly, the isomerization rate for free butane (in CCl<sub>4</sub>) can also be estimated quite well by hydrodynamic Stokes friction, even though its viscosity dependence is not captured (36).

**C.** Internal versus solvent friction. We include empirical fits according to (7, 9, 12)

$$\gamma = (\eta/\eta_0) \gamma_{\rm sol,0} + \gamma_{\rm int}$$
[4]

into Fig. 4 as solid lines. The fits are very good, which validates the assumption of additive solvent and internal contributions. For constrained butane we obtain  $\gamma_{int}$  =  $1.8 \cdot 10^{-4}\,\mathrm{u\,nm^2/deg^2\,ps}$  and  $\gamma_{\rm sol,0} = 3.9 \cdot 10^{-3}\,\mathrm{u\,nm^2/deg^2\,ps},$ which corresponds to a ratio of  $\gamma_{\rm int}/\gamma_{\rm sol,0} = 0.05$  and shows that internal friction is negligible in this case. A small spurious internal friction contribution is in fact expected from the finite difference between the friction coefficient of immobilized and free solutes, as was recently demonstrated based on simulations of methane in water (53). In contrast, for free butane we find  $\gamma_{\rm int} = 5.2 \cdot 10^{-4} \,\mathrm{u} \,\mathrm{nm}^2/\mathrm{deg}^2 \,\mathrm{ps}$  and  $\gamma_{\rm sol,0} =$  $6.7 \cdot 10^{-5} \,\mathrm{u} \,\mathrm{nm}^2/\mathrm{deg}^2 \,\mathrm{ps}$ , and thus a ratio  $\gamma_{\mathrm{int}}/\gamma_{\mathrm{sol},0} = 7.7$ . Hence, the dynamics of free butane is dominated by internal friction effects for normal water viscosity  $\eta_0$ . The substantial reduction of the solvent friction contribution  $\gamma_{sol,0}$  in the free 417 case compared to the constrained case is at first sight surpris-418ing. This reduction can be rationalized by the fact that the 419dihedral angle for free butane is a relative coordinate that 420depends on the motion of all four carbons and is governed by 421a relative diffusion constant that results from the weighted 422sum of the individual carbon diffusion constants. 423

It remains to be checked whether the friction coefficients 424we extract from simulation trajectories in Fig. 4 explain the 425426independently measured dihedral barrier crossing times in Fig. 2. This is non-trivial in the present case since, as men-427 tioned earlier, memory and inertia effects invalidate the simple 428Kramers prediction  $\tau_{\rm MFP} \sim \gamma^{-1}$ . To proceed, it is useful to 429introduce the characteristic time scales of the system. These 430are the inertial time  $\tau_m = m/\gamma$ , which measures the time at 431which ballistic motion crosses over to diffusive motion, the 432memory time  $\tau_{\Gamma} = \gamma/\Gamma(0)$ , which measures the decay time of 433the memory kernel, and the diffusive time  $\tau_D = L^2 \gamma / (k_B T)$ , 434

which measures the free-diffusion time to advance over a characteristic angle of  $L = 60^{\circ}$ . In Fig. 3C we demonstrate that  $\tau_m < \tau_D$  and  $\tau_{\Gamma} < \tau_D$  holds for all simulation data, in which case Kramers' formula for the mean first passage time in the medium to strong friction case (6) 458

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$$\tau_{\rm MFP} = \frac{2\pi\,\omega_{\rm max}/\omega_{\rm min}}{\left[\gamma^2/4 + \omega_{\rm max}^2\right]^{1/2} - \gamma/2} \exp\left(\frac{\Delta U}{k_{\rm B}T}\right), \qquad [5] \quad \begin{array}{c} 460\\ 461\\ 462 \end{array}$$

463is expected to be valid. For the barrier height we extract 464  $\Delta U = 3.7 k_{\rm B}T$  from the free energy in Fig. 1C,  $m\omega_{\rm max}^2 = 6 \cdot 10^{-3} k_{\rm B}T/{\rm deg}^2$  and  $m\omega_{\rm min}^2 = 9 \cdot 10^{-3} k_{\rm B}T/{\rm deg}^2$  are the 465466 curvatures of the free energy at the maximum and minimum. 467 The results from eq. (5) for free and constrained butane are 468included as open data points in Fig. 2; the comparison with 469the simulation data, which does not use any adjustable param-470eter, is quite good. This agreement is in line with previous 471applications of diffusion models to butane isomerization in 472solvent (34–37). 473

The simulation data in the constrained case show a shorter 474 barrier crossing time than expected based on the Kramers 475 formula, whereas for free butane we see the opposite. Both 476 trends can be explained based on memory effects, since an 477 intermediate memory time  $\tau_{\Gamma}/\tau_D \approx 0.01 - 0.1$  significantly 478 accelerates barrier crossing, while a longer memory time in- 479 creases the barrier crossing time, as has been shown recently 480 (30). Thus, our results for constrained butane presumably 481correspond to the regime where memory reduces the reaction 482time, while the results for free butane (which have slightly 483larger values of  $\tau_{\Gamma}/\tau_D$ , as shown in Fig. 3C) correspond to 484 the crossover regime where the memory effect switches from 485acceleration to slowing down of the reaction time. The sat- 486 uration of  $\tau_{\rm MFP}$  for the constrained case in the low-viscosity 487 limit in Fig. 2 is thereby shown to be solely due to inertia 488 effects and thus reflects Kramers turnover, this follows from 489the fact that the friction  $\gamma$  for the constrained case in Fig. 4 490 is roughly linear in  $\eta$  over the entire range of water viscosities. 491 In contrast, the behavior of  $\tau_{\rm MFP}$  for the free case can only 492be explained by a combination of inertia and internal friction 493 effects. This shows that the present simulation strategy, which 494compares the free and constrained scenarios and at the same 495time extracts memory functions, is necessary and useful. 496

# 497 2. Conclusions

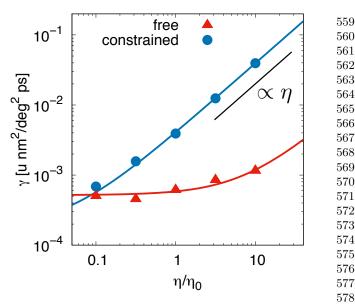
498The dihedral barrier-crossing dynamics of a constrained bu-499tane molecule, where only one carbon atom is allowed to move 500and thus the dihedral angle is the only degree of freedom (be-501sides solvent degrees of freedom) is shown to be very different 502from the dynamics of a free butane, where a total of seven 503positional degrees of freedom are present. This unambiguously 504demonstrates that friction generated by degrees of freedom 505that are coupled but orthogonal to the reaction coordinate 506(in our case the dihedral angle) is dominant in butane. By 507monitoring the friction, which we directly extract from the 508memory kernel, as a function of the solvent viscosity, we show 509that orthogonal degrees of freedom significantly modify the 510solvent friction contribution and also produce an additional 511contribution which we denote, in analogy to experiments on 512protein folding, as internal friction, even though this definition 513of internal friction is solely based on a deviation from normal 514Stokes-like diffusion, and therefore somewhat misleading. The 515internal friction contribution in butane thus stems from the 516dynamic partitioning of energy over the orthogonal degrees 517of freedom (which in addition to the six positional also in-518clude six conjugate momentum degrees of freedom). These 519six degrees of freedom correspond to three translational and 520three orientational degrees of freedom, which do not provide 521an adequate bath for the isomerization reaction in vacuum 522(40). Instead, collisions with the solvent molecules facilitate 523the energy transfer between the intramolecular modes (36). 524

The weak viscosity dependence of the friction memory 525kernel of free butane can be understood by considering that the 526six orthogonal degrees of freedom together will still exchange 527significantly more energy with the solvent than the dihedral 528angle degree of freedom. Therefore, they constitute an energy 529bath that is rather independent of the solvent viscosity. In 530the SI we show that fixing one or two of the central carbon 531atoms of the butane molecule results into internal friction 532contributions of 46% and 9% at  $\eta = \eta_0$  respectively. Since 533butane with one fixed atom has only three rotational degrees 534of freedom in addition to the dihedral angle, we conclude that 535both rotations and translations contribute to the identified 536internal friction mechanism. 537

538 In the GLE eq. (1), the memory kernel does not depend on 539 the reaction coordinate x, whereas the memory kernel of frozen 540 butane is known to have a certain conformational dependence 541 (54), which is, however, significantly less pronounced than the 542 differences between the kernels in Fig. 3A.

Based on our finding that already for butane, which ar-543guably is a very simple system for which the orthogonal de-544grees of freedom in fact correspond to the translational and 545orientational degrees of freedom, internal friction dominates 546the dynamics, we expect that for larger and more complex 547molecules, which possess more orthogonal degrees of freedom, 548internal friction plays an even more important role for the dy-549namics. For macromolecular conformational transitions where 550the rate-limiting step involves dihedral angle isomerization 551(20, 24, 25, 55, 56), our findings constitute one mechanism for 552the emergence of internal friction effects. But other mecha-553nisms, for example based on interactions between molecular 554subunits, certainly also exist. 555

556 Beyond these applications to polymers and proteins, dihe-557 dral isomerization of butane is also interesting in its own right 558 and has been studied by two-dimensional infrared spectroscopy



**Fig. 4.** Friction coefficient  $\gamma$  extracted from the memory kernels in Fig. 3A and B as a function of the rescaled water viscosity  $\eta/\eta_0$  for free and constrained butane. Empirical fits according to eq. (4) (denoted by lines) yield internal-to-solvent friction ratios of  $\gamma_{\rm int}/\gamma_{\rm sol,0} = 7.7$  for free and  $\gamma_{\rm int}/\gamma_{\rm sol,0} = 0.05$  for constrained butane.

(42). The experimental dihedral isomerization time of a butane derivative solvated in  $CCl_4$  was found to be in the 10 ps range, which agrees with predictions from classical MD simulations (36) and is similar to the simulation results we obtain here. Our analysis thus reveals that in such experiments the internal friction, which for normal water viscosity makes up about 89% of the total friction, dominates the dynamics, a fact that does not transpire from the simulations per se.

It seems difficult to derive the empirical eq. (4), according 592to which internal and solvent contributions, the latter being 593defined as the contribution that scales linearly with solvent 594viscosity  $\eta$ , are additive, from first principles. We note that the 595friction coefficient follows (in a non-trivial way) from the force-596force autocorrelation function (53); a decomposition of the 597 force acting on a reaction coordinate into solute and solvent 598contributions (which is exactly possible) would necessarily 599600 give rise to a solvent, a solute and a mixed solute-solvent 601 contribution, and the linear additivity in eq. (4) is not obvious. The good comparison between eq. (4) and the simulation data 602 in Fig. 4 validates the linear additivity thus only in a heuristic sense, and could break down for more complicated systems.

## Materials and Methods

All simulations are carried out using the GROMACS 5.1 (57, 58) 608 simulation package with double precision. The butane molecule 609 is parameterized by the GROMOS (59) united atom force field, 610 for water we use the SPC/E (60) model. All angles and bonds 611 of water and butane are constrained to their equilibrium values 612 using the SHAKE (61) algorithm. Real butane possesses additional 613 degrees of freedom that we neglect in our classical simulations, 614 namely bond angle and bond length vibrations of carbon-carbon 615 as well as carbon-hydrogen bonds, which have been pointed out to 616 alter the equilibrium distribution and the dynamics of butane in 617 liquid solvents (32). However, they are not expected to contribute 618 significantly to the dynamics due to the high quantum-mechanical 619 excitation energies for carbon-carbon bonds and due to the relatively 620

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621 small effective mass of carbon-hydrogen bonds. We perform NVT 622 molecular dynamics (MD) simulations and vary the water molecule 623 mass  $m_{\rm w}$  in order to change the water viscosity. For water mass 624 larger or equal to the normal water mass, we use a time step of 2625 fs, for lighter water mass we lower the timestep by a factor  $\eta/\eta_0 \propto$ 626  $\sqrt{m_{\rm w}}$ . The temperature  $T = 300 \,{\rm K}$  is controlled by the velocity 627 rescaling (62) thermostat, which is coupled only to the solvent with 628 a time constant of  $\eta/\eta_0 \cdot 1$  ps. In the SI we compare results for the 629 memory kernels calculated from NVT and NVE simulations of a free 630 butane molecule at a water viscosity of  $\eta/\eta_0 = 0.3$  and demonstrate 631 that the ensemble and thus the thermostat have no influence on 632 our results. Effective masses are extracted from the equipartition theorem  $m\langle \dot{x}^2 \rangle = k_{\rm B}T$ , see the SI for a short discussion. A python 633634 package for the memory kernel extraction is available on GitHub

635 (https://github.com/jandaldrop/memtools).

#### 636

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