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Insights from atomistic models on loop nucleation and growth in α -Fe thin films under Fe⁺ 100 keV irradiation

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Abstract

The question of how loops nucleate and grow in α -Fe under irradiation is addressed using object kinetic Monte Carlo with parameters from molecular dynamics and density functional theory calculations. Two models are considered for the formation of <100>loops, both based on recent atomistic simulations. In one model <100> loops are formed by the interaction between $\frac{1}{2} < 111 >$ loops. In a second model small interstitial clusters, nucleated in the collision cascade, can grow as <100> or $\frac{1}{2}<111>$ loops. Comparing results from the calculations to experimental measurements of loop densities, ratios and sizes produced by Fe⁺ 100 keV irradiation of UHP Fe thin films at room temperature, the validity of the models is assessed. For these experimental conditions, the reaction model does not seem to be very efficient in the production of $\langle 100 \rangle$ loops due to the fast recombination of $\frac{1}{2} < 111 > 100$ to surfaces. Therefore, in our thin film simulations (at very low carbon concentrations) most <100> loops are a result of the nucleation model. In bulk simulations this effect could change since the probability of interactions between $\frac{1}{2} < 111 >$ loops would increase. Moreover, simulations show that total visible cluster concentration depends strongly on sample thickness and carbon content, while crystal orientation does not seem to have a significant role. Finally, the ratio of <100>to $\frac{1}{2} < 111 >$ visible clusters changes with increased carbon concentration.

Keywords: Monte Carlo simulation, Ion irradiation, Iron, Irradiation effect, In situ transmission electron microscopy

1 1. Introduction

An outstanding question in the field of radiation damage effects in Fe-based alloys is how loops nucleate and grow under irradiation. Experimentally, it is well known since the 1960s that two types of loops are formed: <100> and $\frac{1}{2}<111>$ [1–7]. However,

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the character (vacancy or self-interstitial), concentration, ratio and sizes of these loops 5 differs considerably depending on the experimental conditions. Moreover, the reason 6 why both families of loops are observed is still not completely clear. Elasticity theory and simulations predict that $\frac{1}{2} < 111 >$ loops have lower energies than <100 > loops and 8 should be the dominant defect at low temperatures [8, 9]. As temperature increases, 9 <100> loops become more stable due to the magnetic transition that iron experiences at 10 770° C [10]. On the other hand $\frac{1}{2} < 111 >$ loops are highly mobile according to computer 11 simulations [11-13] in what could be considered as an athermal migration [14]. Therefore, 12 13 these clusters should quickly migrate to sinks such as dislocations, grain boundaries or surfaces and not be observed in the bulk. 14

Several explanations have been given within the past few years for the presence of 15 both <100> and $\frac{1}{2}<111>$ loops, coming from computer simulations as well as detailed 16 experimental measurements. The observation of $\frac{1}{2} < 111 >$ loops despite their fast migra-17 tion is explained by the presence of traps, that slow down the motion of these clusters. 18 Experiments performed by Arakawa et al. [15] have shown that the migration energy of 19 these loops is closer to 1 eV than to the 0.1 eV values obtained from atomistic simula-20 tions [11–13]. Several candidates have been proposed as possible traps for these clusters 21 [16–19]. MD simulations have shown that vacancies can be weak traps for self-interstitial 22 loops [18], but binding energies are too low to explain trapping at room temperature. 23 Carbon, that is always present even if in very low concentrations, is often considered to 24 affect the mobility of these loops [16, 17]. This interaction could be aided by vacancies, 25 forming C-vacancy complexes that can then trap self-interstitial loops [18, 19]. Moreover, 26 other interstitial atoms that form stable clusters with vacancies, namely N and O [20], or 27 He [21] may have a similar effect. Substitutional impurities, such as P, may also interact 28 with gliding loops and slow down their motion [22]. In addition, the interaction of these 29 loops among themselves could also form junctions that make them immobile, as assumed 30 in some models [16]. 31

The presence of <100> loops has been more difficult to elucidate and it is still an 32 open question. These defects should only become dominant at high temperature, but 33 in fact they can be created and observed experimentally also at temperatures as low as 34 140 K. Thus, the inversion of stability between the two classes of loops with increasing 35 temperature is not a sufficient criterion to explain the existence of <100> loops. There 36 are currently two main explanations, both based on computer simulations. Marian et 37 al. [23] proposed the formation of these loops from reactions between $\frac{1}{2} < 111 >$ loops, 38 supported by molecular dynamics (MD) simulations and based on the earlier work of 39 Masters [1]. Later on, Xu et al. [24] obtained the formation of complete <100> loops 40 by reactions between $\frac{1}{2} < 111 >$, using different interatomic potentials in MD [25–27] to-41 gether with advanced kinetic Monte Carlo calculations. More recently, a new possible 42 mechanism of formation of these loops, already speculatively discussed in [28], has been 43 proposed based on the work of Marinica et al. [27]: <100> loops could grow from small 44 immobile clusters, C15 clusters [29] originally observed in MD simulations by Bacon et 45 al. [11], that are characterized by a complex structure, not defined as a collection of 46 parallel dumbbells or crowdions. 47

⁴⁸ Microstructure evolution in irradiated Fe has been simulated with kinetic Monte ⁴⁹ Carlo and rate theory models by several groups [16, 19, 30–32]. However, except for a ⁵⁰ recent work by Terentyev and Martin-Bragado for electron irradiation [19], no distinction ⁵¹ is made between the different types of self-interstitial clusters, and the ratios between 52 <100> and $\frac{1}{2}$ <111> loops are not followed. In this work, we have gathered the existing information about cluster stabilities and mobilities together with the different models for growth of loops in Fe explained above. All these parameters and reactions have been implemented in a kinetic Monte Carlo model and have been used to simulate irradiation at low energies, 100 keV, in UHP Fe thin films at room temperature. A model for the interaction of carbon with vacancies and self-interstitials based on the work of Serra [18] and Terentyev [33, 34] is used to introduce a mechanism for the trapping of loops.

Results obtained from the simulations in terms of defect densities and sizes have been 59 60 contrasted with corresponding experimental measurements [6]. These experiments have been performed by Yao et al. [6] as a series of systematic in-situ transmission electron 61 microscopy (TEM) studies of irradiation of thin films of Fe and Fe-Cr alloys with heavy 62 ions. Fe^+ and Xe^+ ions of energies of 100 keV and 150 keV were used for irradiations 63 both at room temperature and 300° C. Loops were first observed at doses above 10^{16} m⁻² 64 and both <100> and $\frac{1}{2}<111>$ loops could be identified, with a much higher proportion 65 of <100> loops, especially for those foils consisting of pure Fe. In this work we focus 66 on the results for room temperature Fe samples irradiated with 100 keV Fe⁺ ions. The 67 comparison between experiments and simulations allows us to extract some conclusions 68 about the most probable mechanism for loop growth under these irradiation conditions. 69

70 2. Model parametrization

We have used our database of 100 keV cascades of Fe irradiation of Fe thin films. 71 MD simulations were used to reproduce the resulting damage after ion implanation by 72 73 sending an Fe ion with the energy of interest towards an Fe thin film. This resulted in damage with characteristics very different from bulk irradiation. Firstly, an imbalance 74 between the number of vacancies and interstitials was found that was attributed to the 75 faster diffusion of SIAs that escape to the surface where they stay as ad-atoms [35]. 76 77 Secondly, vacancy clusters are larger than those obtained in bulk cascades while selfinterstitial clusters are smaller. The resulting cascades were stored so they could be 78 randomly sampled when called from the Object Kinetic Monte Carlo code MMonCa, 79 developed by I. Martin-Bragado et al. [36]. Each cascade of point defects is finally 80 inserted while running our simulations and centered in a random XY position to mimic 81 homogeneous ion irradiation of the surface. The simulation cells we have used are also 82 thin films whose thicknesses range from 15 to 85 nm, reproducing the different thicknesses 83 of the thinned sample used in the experimental work of Yao et al. [6]. A compromise 84 between simulation time and computational resources usage has been chosen to select 85 the area of the simulation cells. Accordingly, these areas range from 516×516 nm² for 86 15 nm thick samples, to 216×216 nm² for 85 nm, resulting in simulation box volumes of 87 about 4×10^6 nm³ for all the samples. The temperature in the simulation box is set to 88 294.15 K, at which <100> loops are considered immobile as shown in Table 1 following 89 MD calculations [23]. 90

In our code, small self-interstitial atom (SIA) clusters up to a size of 4 SIA are mobile with migration energies given in Table 1, obtained from density functional theory (DFT) calculations [37]. These self-interstitial clusters are considered to move in three dimensions. From size 5, as obtained in [38] from DFT calculations, the orientation of the clustered dumbbells changes from <110> to <111> as it is energetically favoured. Then, the formation of <100> loops is implemented in our code according to one of these two models:

Reaction model: In this model all interstitial clusters above size 4 transform into 98 $\frac{1}{2}$ <111> loops with migration energies given also in Table 1 and obtained from classical 99 molecular dynamics simulations [13]. These loops move one-dimensionally, unlike vacan-100 cies or smaller SIA clusters. According to this model, the interaction between $\frac{1}{2} < 111 >$ 101 loops might result in the formation of <100> loops if two specific conditions are simul-102 taneously satisfied: a) the sum of their Burger's vector gives as a result a Burger's vector 103 belonging to the family of <100> directions, and b) the sizes of both interacting loops 104 are larger than a threshold (about 20 according to Marian et al. [23, 39]), the influence of 105 which was studied, and both are about the same size (within a 5% margin of difference, 106 as suggested by the simulations of Marian et al. [23, 39]). If the former conditions are not 107 fulfilled, then the resulting loop becomes a bigger $\frac{1}{2} < 111 > 100$ with its Burger's vector 108 oriented along the direction of the bigger interacting loop. The minimum size of the 109 resulting <100> loop that can be formed under these conditions is one of the parameters 110 that has been evaluated in this work. Once the <100> loops are formed, they can grow 111 by the incorporation of small interstitial clusters (<5 SIA), by capturing smaller $\frac{1}{2} < 111 >$ 112 loops and by coalescence with other immobile <100> loops or immobilized smaller C-113 $\frac{1}{2}$ <111> loops. In case of interacting with a larger SIA cluster, the Burger's vector of 114 the resulting dislocation loop is the one corresponding to the larger SIA cluster. 115

Nucleation model: In this model $\frac{1}{2} < 111 >$ and < 100 > loops can be formed indepen-116 dently. SIA clusters from size 5 can either transform into $\frac{1}{2} < 111 >$ loops or into < 100 >117 loops with a given ratio. This ratio was initially taken as 5%, following the idea of 118 Marinica et al. [27] that considers this as the ratio of immobile C15 clusters formed in a 119 collision cascade, and assuming that all these clusters will grow into <100> loops. The 120 influence of this ratio has also been evaluated and discussed in the next section. Once 121 formed, both types of loops can grow following the same conditions as described for the 122 reaction model. 123

In both models $\frac{1}{2} < 111 >$ loops can be stopped by the interaction with carbon-vacancy 124 and carbon-interstitial clusters following the work of Terentyev and Martin-Bragado [19]. 125 These immobile C- $\frac{1}{2}$ <111> loops can then grow by addition of SIA clusters < 5 and 126 mobile $\frac{1}{2} < 111 >$ loops of similar size. Also, <100> vacancy loops have been included in 127 the models. The equation derived by Gilbert in [40] has been used for the binding energy 128 of the vacancies in the loop. In this equation the radius of the loop is calculated using 129 the size and the density of the loop. For the binding energies of $V_{n>4}$ and $I_{n>4}$ clusters, 130 we have used the usual extrapolation law [37] $E_b(n) = E_f + [E_b(2) - E_f][n^{2/3} - (n - 1)n^{2/3}]$ 131 $1)^{2/3}/(2^{2/3}-1)$. For the smaller species up to 4, DFT values have been used [37]. These 132 small vacancy clusters are considered mobile, with a 3D mobility, while larger vacancy 133 clusters are immobile. Table 1 summarizes the most important parameters of the species 134 involved. These parameters are also used to calculate point defects emission rates from 135 clusters, as described elsewhere [36]. 136

One specific feature of MMonCa is that the location of all defects in a cluster are explicitly defined. This provides more flexibility for the definition of capture volume of a defect, since it is not restricted to a sphere, but it is given by the shape of the cluster defined by the defects that form that cluster. The interaction between two clusters will then happen when the distance between two defects belonging to each cluster is smaller than, or equal to, the specified capture distance. The capture distance for all defects as

Defect	Migration	Binding	Migration
	barrier (eV)	energy (eV)	type
Ι	0.34		3D
I_2	0.42	0.80	3D
I_3	0.43	I to $I_2 \ 0.92$	3D
I_4	0.43	I to $I_3 \ 1.64$	3D
$\frac{1}{2} < 111 > \text{loop: } I_{n \ge 5}$	0.05	As in ref. [41]	1D
$<100>$ loop: $I_{n\geq 5}$	Immobile	As in ref. $[41]$	_
V	0.67		3D
V_2	0.54	0.3	3D
V_3	0.43	V to $V_2 \ 0.37$	3D
V_4	0.62	V to $V_3 \ 0.62$	3D
$V_{n>5}$	Immobile	As in ref. $[41]$	_
<100> loop: V _{n>5}	0.5	As in ref. $[40]$	$1D^{\star}$
С –	0.86		3D
$CI_{n>5}$	Immobile	C to I _n $\{0.4 - 0.66\}^{\dagger}$	_
$C_{m>2}\overline{I}_{n>5}$	Immobile	C to $C_{m-1}I_n \ 0.70$	_
ĒV -	Immobile	0.68	_
CV_2	1.1	C to CV 1.01	3D
$C_m V_n$	Immobile	As in ref. $[34]$	_

Table 1: Type of defect, migration and binding energies of the objects defined in our OKMC model. Last column corresponds to the dimensionality of migration. For the mono-defects, V and I, the formation energy is taken from ab initio calculations [37], $E_f(V) = 2.07$ eV and $E_f(I) = 3.77$ eV.

 * <100> vacancy clusters introduced into OKMC as obtained from MD cascade simulations.

[†] $E_{bind} = 0.4 \text{ eV} (n < 20), 0.45 \text{ eV} (20 < n < 50), 0.50 \text{ eV} (50 < n < 90), 0.66 \text{ eV} (n > 90)$

well as for interfaces has been set equal to 1 times the lattice parameter of BCC iron:
0.287 nm.

As mentioned above, the database of damage created by the collision cascade used 145 for these simulations has been obtained from molecular dynamics simulations with the 146 specific experimental conditions: 100 keV Fe⁺ ion irradiation of Fe substrates [35]. Those 147 simulations showed that the damage distribution for this particular irradiation energy 148 is very different from that in the case of bulk irradiation. Particularly, <100> vacancy 149 loops with more than 400 defects were produced. These loops are always located within 150 a few layers from the surface. Vacancy <100> loops can only be created in cascades, 151 based on the input from molecular dynamics simulations. Thus, the only vacancy clusters 152 that are considered as loops in the kinetic Monte Carlo calculations are those that come 153 from the cascades, while all other vacancy clusters are considered as voids. In principle, 154 <100> loops have a very low mobility [23] and are thus often considered immobile (for 155 example in Table 1 the <100> loops of interstitial nature are considered immobile). 156 However, if we consider that also all <100> vacancy loops formed in the MD simulations 157 do not migrate or recombine with the surface, then the concentration of <100> loops 158 is extremely high and in complete disagreement with the experimental, that observe 159 these type of loops occasionally and always at very low doses and close to the surface. 160 Therefore, if we accept the defect size distribution obtained from MD, there must be a 161 mechanism of recombination of the <100> loops located very close to the surface, which 162 in this case are all vacancy type. The interaction of these dislocation loops with surfaces 163 can be modelled using an elastic approach [42] or dislocation dynamics [43], however, 164 since elastic interactions were not implemented so far in this model, we propose that this 165 recombination is due to image forces as discussed in Ref. [44] and include this effect in the 166 OKMC code by assigning a migration energy of 0.5 eV, strictly only in the case of <100>167 loops of vacancy nature introduced directly by cascades, so that they can recombine with 168 the surface. 169

The conditions for the irradiation follow those in the experiment by Yao et al. [6]. 170 Simulations are performed at room temperature, with a dose rate of 8×10^{14} ions/m²/s 171 in pure Fe and Fe with different carbon concentrations. Foil orientations along (100)172 and (111) planes are studied. The concentration of defects as a function of dose is 173 analyzed under different conditions of foil orientation, foil thickness, carbon concentration 174 as well as the type of model for loop growth: the reaction and the nucleation model, as 175 explained above. In order to compare with experimental measurements of defect densities 176 obtained by TEM it is important to take into account the minimum visible size resolvable 177 experimentally. The authors mentioned in their work that they could resolve dislocation 178 loop sizes of about 1.5 nm in diameter, which corresponds to 30 SIA [45, 46]. So this is 179 the value used as visibility threshold in this work and therefore as the lower limit in size 180 for the first bin (i.e.: 1-2 nm) of all the represented histograms. 181

182 3. Results

Figures 1a and 1b show the concentration of visible defects as a function of irradiation dose obtained from the two models for loop growth described above, considering each model independently. In these simulations no carbon was included, therefore, due to the fast migration of $\frac{1}{2} < 111 >$ loops to the surface, all remaining loops are of <100> type. These calculations are done for test structures consisting of thin films of $270 \times 270 \times 50$



¹⁸⁸ nm³ and crystal orientation Fe(100). The Fe ion flux was set to 8×10^{14} ions/m²/s and ¹⁸⁹ the maximum dose achieved was 1×10^{18} ions/m².

Figure 1: A real density of visible SIA dislocation loops as a function of dose for several cases of each model. Plot (a) shows the results of the reaction model. Different values of the minimum size of the resulting <100> loop after the collision of two SIA $\frac{1}{2}$ <111> SIA loops are considered. Plot (b) shows the results of the nucleation model after changing the chances of small SIA loops to turn, as they grow (\geq 5 SIA), into either immobile <100> or mobile $\frac{1}{2}$ <111>, being the former the least favorable case. The simulation volume in both cases was set to 270×270×50 nm³.

Both models have one parameter that could change the outcome of the evolution 190 of defects. In the case of the reaction model this parameter is the threshold in size 191 considered for the formation of a <100> loop after the reaction of two $\frac{1}{2}<111>$ loops, 192 while in the case of the nucleation model it is the ratio of transformations of small SIA 193 clusters (exceeding 4 SIA) into <100> loops, considered to be formed within the collision 194 cascade. The rest of the transformations result in $\frac{1}{2} < 111 >$ loops. Concerning the first 195 parameter, according to the work of Marian [23] as well as the work of Xu [24], in order 196 to form a <100> loop the reacting clusters must have similar sizes. Marian [23, 39] 197 also states that loops must have at least ~ 20 defects each in order to form a < 100 >198 loop. We have performed calculations for different threshold sizes of the $\frac{1}{2} < 111 >$ loops 199 that would give rise to the formation of a <100>, presented in Figure 1a) for minimum 200 resulting sizes between 30 and 100 self-interstitials (or 15 and 50 self-interstitials on 201 each interacting loop). This figure shows that, as the minimum size for loop formation 202 increases, the concentration of $\langle 100 \rangle$ loops decreases, according to expectations. This 203 model predicts a very low concentration of <100> for all sizes studied and the irradiation 204 conditions considered in these simulations. Even for the smallest threshold (30 SIA), the 205 concentration at a dose of 1×10^{18} ions/m² is only around 2×10^{14} loops/m². This is the 206 result of the very restrictive conditions to form <100> loops through this mechanism, 207 particularly the fact that the sum of the Burger's vectors must be the appropriate one. 208 Consequently, for thin films most of the $\frac{1}{2} < 111 >$ reach the surface before interacting with 209 each other to form <100> loops. Therefore, under the conditions simulated here, we do 210 not expect a significant contribution of this mechanism in the formation of <100> loops. 211 Turning to the nucleation model and the seed ratio of <100> and $\frac{1}{2}<111>$ loops, 212 according to the work of Marinica [27], about 5% of the clusters produced in a collision 213 cascade are of C15 type. However, not necessarily all these clusters are going to evolve 214



Figure 2: Simulation results for reaction and nucleation models after a radiation dose of 8.0×10^{17} ions/m². Image (a) corresponds to the 40 SIA threshold of the reaction model, whereas its loop size distribution is represented in (c). Image (b) corresponds to the formation of one <100> every 1000 transitions of small SIA clusters to dislocation loops in the nucleation model. The loop size distribution is represented in figure (d). Only one active model for <100> loops (represented as disks formed by white dots) formation is enabled at a time in these simulations. A zoomed detail of a dislocation loop perpendicular to the top view representation is also featured in figure (a).

to <100> loops. Therefore, the ratio of small defects that are considered to transform 215 into $\frac{1}{2} < 111 >$ loops or < 100 > loops is a free parameter in this model. Figure 1b shows 216 the dependence of visible cluster concentration on the ratio of clusters considered to be 217 <100> loops. As expected, the total concentration decreases as the percentage decreases, 218 without any significant change in the dose dependence. As mentioned above, experimen-219 tally visible clusters are only observed for doses above 10^{16}m^{-2} . For the case of pure 220 Fe, concentrations are below 10^{15} m⁻² for the highest doses studied. The ratio of $\langle 100 \rangle$ 221 to $\frac{1}{2} < 111 >$ loops transformed from small SIA loops used in these simulations is 0.1%. 222 This transformation ratio is a parameter that has been adjusted to match experimental 223 data and the information from Figure 1b. It was chosen so that the simulation results 224 agree with experimental measurements of visible cluster concentration for UHP Fe(100)225 for a thickness of 25 nm as shown below (Figure 8a). Nevertheless, for this comparison, 226 higher values would only increase even more the difference between the two models for 227 this particular condition, that is, thin films. 228

Figures 2a and 2b present the areal distribution of the loops in the simulation box, projected over the thickness of the thin film as observed from the front surface, for the reaction (Figure 2a) and nucleation (Figure 2b) models, separately, after a radiation dose

of 8.0×10^{17} ions/m². This is similar to what would be observed under TEM, except that 232 here defects of all sizes are shown, and not only visible ones. Disks formed by white dots 233 correspond to <100> loops while dark dots are vacancies and small SIA clusters. In the 234 case of the reaction model a threshold of 40 SIA is considered, while for the nucleation 235 model the results for a ratio of 1 immobile <100> loop every 1000 transitions of small 236 SIA clusters are represented. Histograms representing the self-interstitial cluster sizes 237 for these two cases are shown in Figures 2c and 2d. The main difference between the two 238 models is clearly seen in these figures: the reaction model shows very low concentrations 239 of <100> loops with discrete sizes whereas the nucleation model shows higher concen-240 trations and more spread in terms of size ranges. Note that some of the loops have their 241 plane perpendicular to the surface and they appear as a line (a zoom of one of these 242 loops is shown in Figure 2a). 243

In these simulations, only <100> loops remain in the thin film, due to the recombi-244 nation of the 1D migrating $\frac{1}{2} < 111 >$ loops with the surfaces. Experimentally, however, 245 even in the ultra-high pure Fe samples, both $\frac{1}{2} < 111 >$ and < 100 > loops are observed, 246 although the <100> loops represent 86% of the total, which is high but less than the 247 100% that corresponds to Figures 1 and 2. One possible explanation, as discussed in 248 the introduction, is the trapping of self-interstitial loops by carbon-vacancy or other 249 carbon-interstitial complexes (or equivalent contributions from other interstitial impu-250 rities). Therefore, we have considered different trap concentrations. In the following 251 results both nucleation and reaction models for <100> loop formation are allowed in the 252 simulations. A threshold value for the resulting <100> loop of 40 SIA is considered for 253 the reaction model, following the proposal of Marian et. al [39], and a ratio of formation 254 of <100> of 1 every 1000 transformations of small clusters for the nucleation model. 255 These values have been selected so that the concentration of visible <100> clusters is 256 similar to those measured experimentally under these irradiation conditions. The con-257 centration of visible $\frac{1}{2} < 111 >$ loops will be given by the concentration of carbon in bulk 258 259 due to trapping, as discussed next.



Figure 3: Areal density of $\frac{1}{2}$ <111> and <100> loops obtained for different carbon concentrations when both reaction and nucleation models are activated. The simulation volume was set to $270 \times 270 \times 50$ nm³.

Figure 3 shows the results of the simulations for different concentrations of carbon: 1, 5 and 10 ppm (i.e. 5, 23 and 47 appm respectively), including the visible concentration

of <100> and $\frac{1}{2}<111>$ loops as a function of dose. As can be appreciated in this figure, 262 the areal density of <100> loops is about the same for all the carbon concentrations 263 evaluated, meanwhile the areal densities of $\frac{1}{2} < 111 >$ loops are highly dependent on carbon 264 concentration. Trapped $\frac{1}{2} < 111 >$ loops are barely present for 1 ppm of carbon, whereas 265 $\frac{1}{2}$ <111> and <100> loops are about the same levels of concentrations for 5 ppm, as 266 it can be appreciated in Figure 3. Lastly, the areal density of $\frac{1}{2} < 111 >$ loops is much 267 higher than the concentration of <100> loops when the bulk concentration of carbon 268 is 10 ppm. This is more clearly seen in the histogram of SIA cluster sizes, as shown in 269 Figure 4, where it can be seen that the dominant population of SIA loops is reversed 270 as the carbon concentration in the bulk is increased. For the conditions presented in 271 Figure 4, for 1 ppm C and 50 nm thickness of the foil most of the loops are of <100>. 272 For 5 ppm carbon, the concentration is about the same for both loops, while a clear 273 inversion of the population is obtained for a carbon concentration of 10 ppm, and this 274 is the case for both doses presented here. Note that this behavior is independent of the 275 model for the formation of <100> loops, that is, the inversion of the population is due 276 to trapping of the <111> loops by carbon. 277



Figure 4: Visible loop size distributions obtained for different carbon concentrations (1, 5 and 10 ppm) when both reaction and nucleation models are activated. Histograms in the upper row are obtained after a dose of 5×10^{17} ions/m² while histograms in the lower row were obtained after 10^{18} ions/m².

Several aspects of the experimental conditions can thus affect the total concentration 278 of visible clusters measured by TEM, which should be taken into account when comparing 279 to simulation results. The thickness of the irradiated sample is particularly important, 280 as noted by Yao et al [6]. The same authors also mention that the crystal orientation 281 could have an impact on the total visible cluster concentration measured experimentally. 282 Therefore, simulations were performed for different thicknesses of the irradiated sample, 283 from 15 nm up to 85 nm, as shown in Figures 5a and b where the total concentration 284 of visible SIA clusters is represented, as well as different orientations, (100) and (111) 285 (figures (a) and (b) respectively). This particular case corresponds to a carbon concen-286

tration of 3 ppm. As the sample thickness decreases, so does the defect concentration. 287 This is a result of the recombination of mobile SIA with surfaces, which is enhanced 288 for thinner samples. As the sample thickness increases, this trend starts to saturate at 289 about 50 nm, as can be noticed from Figures 5a and b. This saturation is due to the 290 depth of the cascade damage for this energy, which hardly reaches 50 nm as obtained 291 from MD calculations [35]. In the experimental work of Yao et. al [6], they observe a 292 gradual fall-off in the areal concentration with foil thickness, which they attribute to a 293 lower visibility of small loops in thick foils, obtained from TEM image simulations [47]. 294 Areal density differences with sample thickness are more clearly seen in the top view of 295 the simulations for a given dose. Figure 6 shows three sample thicknesses, 15 nm, 37 296 nm and 85 nm, for two different orientations (100) top and (111) bottom figures, and 297 for a total dose of 10^{18} ions/m². The upper row in Figure 6 shows the top view of the 298 thin foils with substrate orientation (100), where one may notice that those <100> loops 299 with Burger's vector along [010], $[0\overline{1}0]$, [001] and $[00\overline{1}]$ directions are hardly visible, as 300 they are perpendicular to the depicted images. Lastly, the corresponding histograms of 301 SIA clusters are represented in Figure 7. 302



Figure 5: Areal density of visible loops as a function of the irradiation dose and foil thickness for two different substrate orientations (a) Fe(100) and (b) Fe(111). The carbon concentration was set to 3 ppm, and both reaction and nucleation models were activated.

303 4. Discussion

From the analysis above, it is clear that a quantitative comparison of the model with 304 experimental measurements must be done with caution when considering only visible 305 cluster concentration. The simulations above show that the total visible cluster concen-306 tration measured depends strongly on actual sample thickness and carbon content, while 307 the dependence with crystal orientation does not seem to be particularly important for 308 the total defect density. In essence, this means that the main parameter affecting the 309 loop ratio is the mobility and thus the rate of removal of the $\frac{1}{2} < 111 >$ loops. These sim-310 ulations also show that the reaction model, under the experimental conditions studied 311 here, that is, damage close to the surface and thin samples, is very inefficient for the pro-312 duction of <100> loops due to the fast recombination of $\frac{1}{2}<111>$ loops with the surfaces. 313

Therefore, the nucleation model is needed in order to reproduce the experimental obser-314 vations. In other words, the picture that emerges is that a small fraction of <100> loops 315 is indeed produced directly upon growth of non-parallel, C15 type interstitial cluster con-316 figurations, and they are hardly mobile; some of them may also be produced by reaction 317 between $\frac{1}{2} < 111 > 100$ loops. If the conditions are such that all the highly mobile $\frac{1}{2} < 111 > 100$ 318 loops are removed, then all or most visible loops will be of <100> type; otherwise, a 319 more or less small/high ratio of <100> over $\frac{1}{2}<111>$ different from 1 will be observed, 320 which will be an indirect index of the effective mobility that impurity concentration and 321 322 irradiation conditions (e.g. thickness of the specimen, but also temperature, etc.) allow for the $\frac{1}{2} < 111 >$ loops. 323

Figure 8 shows a comparison of the visible cluster concentration as a function of dose together with the experimental measurements. The parameters for the simulations are those that optimize the comparison to the experiment, that is, minimum size for <100>loop formation of 40 defects for the reaction model and a ratio of 1 every 1000 for the transformation of small SIA clusters to <100> loops for the nucleation model. In both cases the carbon concentration is 3 ppm, following the experimental conditions in Yao et al. [6]*



Figure 6: Top view of the graphical representation of defects for both reaction and nucleation models after irradiation for different foil thicknesses. The irradiation dose of these images corresponds to 10^{18} ions/m², and the carbon concentration in these simulations was 3 ppm. Disks formed by white dots correspond to <100> loops, while those formed by light blue dots correspond to $\frac{1}{2} < 111 >$ loops.

^{*} In [6] a carbon concentration of 130 ppm is mentioned. However, the purities of the samples used in the experiments were 5N and $4N^+$, as also indicated in the same article.



Figure 7: Visible loop size distributions for both reaction and nucleation models after irradiation for different foil thicknesses. The irradiation dose of these histograms corresponds to 10^{18} ions/m², and the carbon concentration in these simulations was 3 ppm.



Figure 8: Comparison between the simulated data using both <100> growth models with experimental values from Yao et al. [6]. The filled circles in *a*) correspond to the total visible SIA dislocation loops as a function of the irradiation dose, while the experimental measurements are represented by rings. The histograms depicted in *b*) show the size distribution of loops after a dose of 3×10^{17} ions/m² for the substrate Fe(111) polycrystalline 5N in comparison with simulation results.

Calculations for two different crystal orientations (100) and (111) have also been performed, both presented in Figure 8a. Although there is a slight difference between the two orientations, with lower concentrations for the (111) orientation, in agreement with the experimental results, this difference is much smaller than that observed experimentally. This result seems to indicate that the interaction of the mobile interstitials with the surface should be stronger than what has been considered in the model. Currently, defects interact with the surface only when they are located within a distance equal to

a jump distance, 0.287 nm. However, due to image forces [21] the interaction of the 338 surface with loops could be of much longer range, thereby enhancing disappearance of 339 loops, in particular for the (111) orientation. Moreover, the presence of a nearby grain 340 boundary could explain that strong decrease in the loop density for the (111) case. The 341 histograms in Figure 8b are obtained after a dose of 3×10^{17} ions/m² for the substrate 342 with orientation (111). It shows a small increase in the averaged size of the visible loops, 343 resulting 1.6 \pm 0.2 nm for the experiments of Yao et al. [6] and 1.9 \pm 0.3 nm for the 344 simulation results. 345

346 5. Conclusions

Through kinetic Monte Carlo simulations and parameters obtained both from clas-347 sical molecular dynamics simulations and density functional theory, we have studied 348 microstructure evolution in irradiated Fe including the formation of both <100> and 349 $\frac{1}{2}$ <111> through two different mechanisms: the nucleation model and the reaction model. 350 The models have been contrasted to TEM characterizations of Fe 100 keV irradiation of 351 Fe thin films. From this comparison we conclude that a fraction of the visible <100>352 loops are produced directly in the cascade or from C15 type of clusters. The formation 353 of <100> loops from reactions between $\frac{1}{2}<111>$ loops is also possible, however, under 354 the conditions in these particular experiments where surfaces play a strong role, due to 355 the film thickness and low carbon concentration, this mechanism is not very efficient. 356 These simulations show that the ratio of <100> to $\frac{1}{2}<111>$ loops is very dependent on 357 the efficiency of transport of $\frac{1}{2} < 111 >$ loops to sinks and therefore, it will strongly depend 358 on the irradiation conditions and sample characteristics, particularly sample thickness 359 and impurity content. 360

Although the exact values of concentrations or ratios could change depending on the 361 parameters in the model, some general and important conclusions emerge from this study. 362 Firstly, the comparison to experimental measurements of defect concentrations obtained 363 with TEM must be done with caution. Several factors influence the concentration of 364 defects observed. Besides carbon concentration or the visibility limit, which has been 365 pointed out by several authors before, this work shows that the thickness of the sample, 366 something that is not always available from the experiments, also plays an important 367 role. Secondly, as already mentioned, the concentration of carbon not only influences the 368 total concentration of visible defects but also the ratio of $\frac{1}{2} < 111 >$ to < 100 > loops. In 369 fact, this could be a way of validating this model, by systematic studies of irradiated Fe 370 under different carbon concentrations. Finally, the orientation of the crystal sample does 371 not seem to have an important influence in the total defect concentration, although it 372 could give rise to differences in the cluster size distribution. Based on these simulations 373 we propose several ways of validating this model: systematic studies of ion implantation 374 of iron at low energies and different carbon concentrations and crystal orientations. 375

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Data availability 386

The raw data required to reproduce these findings are available to download from 387 Mendeley Data with the identifier http://dx.doi.org/10.17632/2rxrbjcbcv.1 388

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