

**STRUCTURAL DETERMINATION AND  
ANALYSIS OF SOME NEW SCHIFF BASE AND  
TRIANGULO-TRIRUTHENIUM COMPOUNDS**

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**STRUCTURAL DETERMINATION AND ANALYSIS OF SOME  
NEW SCHIFF BASE AND TRIANGULO-TRIRUTHENIUM  
COMPOUNDS**

**by**

**YEAP CHIN SING**

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# PENENTUAN DAN ANALISIS STRUKTUR BARU SEBATIAN SCHIFF BASE DAN *TRIANGULO*-TRIRUTHENIUM

## ABSTRAK

Lapan sebatian Schiff base dikaji dalam kajian ini. Mereka terhablur dalam sistem hablur yang biasa iaitu, empat sebatian dalam monoklinik  $C2/c$ , dan masing-masing satu dalam monoklinik  $Cc$ ,  $P2_1$  and  $Pn$  dan triklinik  $P\bar{1}$ . Salah satu sebatian Schiff base dalam bentuk zwitterion. Struktur bagi dua sebatian Schiff base adalah berantakan. Salah satu sebatian Schiff base adalah hablur kembar rasemik. Unit asimetrik bagi dua sebatian Schiff base mengandungi molekul pelarut air. Semua sebatian Schiff base adalah dalam bentuk konfigurasi  $E$  mengenai ikatan ganda N=C. Nilai purata bagi jarak ikatan ganda N=C ialah 1.282 Å. Lapan belas sebatian *triangulo*-triruthenium dikaji dalam kajian ini. Kesemuanya terhablur dalam sistem hablur yang biasa iaitu, tujuh sebatian dalam triklinik  $P\bar{1}$ , tujuh lagi dalam monoklinik  $P2_1/c$ , dua dalam monoklinik  $C2/c$ , and masing-masing satu dalam ortorombik  $Pbca$  and  $Pca2_1$ . Empat struktur sebatian *triangulo*-triruthenium adalah berantakan. Unit asimetrik bagi lapan sebatian mengandungi molekul perlarut seperti air, diklorometana atau kloroform. Semua molekul perlarut berantakan kecuali satu daripada lapan sebatian tersebut adalah tidak berantakan. Salah satu sebatian *triangulo*-triruthenium adalah hablur kembar rasemik dan satu lagi adalah hablur kembar pseudomeroedral. Ligand kumpulan-15 menduduki kedudukan khatulistiwa dalam semua sebatian *triangulo*-triruthenium disebabkan oleh reaksi sterik. Perbezaan yang signifikansi bagi jarak ikatan Ru—Ru dan jarak ikatan dengan sudut ligand karbonil akibat daribada kesan penggantian. Nilai purata jarak ikatan antara tiga Ru—Ru adalah 2.840 Å, 2.860 Å dan 2.878 Å. Jarak ikatan Ru—C axial adalah lebih panjang daripada jarak ikatan Ru—C khatulistiwa. Nilai purata jarak ikatan

Ru—C axial adalah 1.931 Å dan nilai purata jarak ikatan Ru—C khatulistiwa adalah 1.892 Å. Ikatan Ru—C khatulistiwa yang menyambung kepada atom Ru yang menyambung kepada ligand monopenggantian adalah ikatan yang paling pendek bagi kebanyakan sebatian. Nilai purata bagi jarak ikatan Ru—C ini adalah 1.882 Å. Sudut Ru—C—O khatulistiwa adalah hampir linear manakala sudut Ru—C—O axial adalah bengkok sedikit. Nilai purata sudut Ru—C—O adalah 177.1° khatulistiwa dan nilai purata sudut Ru—C—O axial adalah 173.4°.



# STRUCTURAL DETERMINATION AND ANALYSIS OF SOME NEW SCHIFF BASE AND *TRIANGULO*-TRIRUTHENIUM COMPOUNDS

## ABSTRACT

Eight Schiff base compounds were studied in this research. They crystallized out in the common space groups, i.e. four compounds are in monoclinic  $C2/c$ , and one each in monoclinic  $Cc$ ,  $P2_1$  and  $Pn$  and triclinic  $P\bar{1}$ . One Schiff base compound exists in a zwitterion form. The structures of two Schiff base compounds are disordered. One Schiff base compound is a racemic twin crystal. Water solvent exists in the asymmetric unit of two Schiff base compounds. The Schiff base compounds all exist in an *E* configuration with respect to the N=C. The average N=C double bond value is 1.282 Å. Eighteen *triangulo*-triruthenium complexes were studied in this research. All of them crystallized out in the common space groups, i.e. seven compounds are in triclinic  $P\bar{1}$ , seven in monoclinic  $P2_1/c$ , two in monoclinic  $C2/c$ , and one each in orthorhombic  $Pbca$  and  $Pca2_1$ . The *triangulo*-triruthenium complex structures in four compounds are disordered. The asymmetric unit of eight compounds contains solvent molecules, e.g. water, dichloromethane or chloroform. All solvent molecules are disordered except for one of them. One *triangulo*-triruthenium compound is a racemic twin crystal and one *triangulo*-triruthenium compound is a pseudomerohedral twin crystal. In all *triangulo*-triruthenium complexes, the group 15 ligands occupy the equatorial position due to steric reaction. The effect of substitution results in significant differences in Ru—Ru bond lengths and carbonyl-ligands bond lengths and angles. The average three Ru—Ru bond lengths are 2.840 Å, 2.860 Å and 2.878 Å. The axial Ru—C bonds are longer than the equatorial Ru—C bonds. The average axial Ru—C bond lengths is 1.931 Å and the average equatorial Ru—C bond lengths is 1.892 Å. The bond length of equatorial

Ru—C when connected to the same Ru atom with the monodantate ligand is the shortest bond in most of the molecules. The average of these Ru—C bonds is 1.882 Å. The equatorial Ru—C—O angles are close to linear whereas the axial Ru—C—O angles are slightly bent. The average equatorial Ru—C—O angles is 177.1° and the axial Ru—C—O angles is 173.4°.

## CHAPTER 1

### INTRODUCTION

X-ray crystallography is a method of using a beam of X-ray to strike onto a crystal to determine the arrangement and geometrical parameters of atoms within a crystal (Fig. 1.1). The X-ray beams will be diffracted into many specific directions, and then with the angles and intensities of these diffracted beams, a crystallographer can produce a three-dimensional picture of the electron density within the crystal. From this electron density, the mean positions of the atoms in the crystal can be determined, as well as various information including connectivity, conformation, and bond lengths and angles. In addition, it gives information of the stoichiometry, the density, the symmetry and the three dimensional packing of the atoms in the solid.

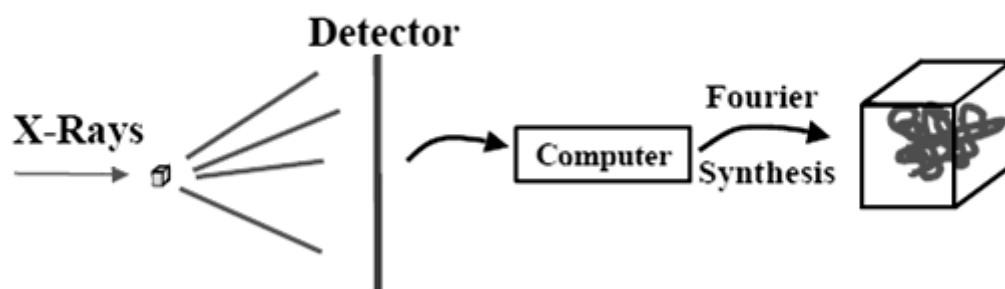


Fig. 1.1 The process of X-ray crystallography (Soman, 2007).

## 1.1 X-rays

X-ray is electromagnetic radiation with wavelength,  $\lambda$ , in the range of 0.1 to 100 Å (1 Å =  $10^{-10}$  meters). X-rays have wavelengths similar to the dimensions of atoms ( $\sim 1$  Å) and therefore able to explore within crystals. X-rays are produced when fast-moving electrons collide with a metal target. The electron obtained enough energy to knock out an electron from the inner shell of the metal atom and as a result electrons from higher energy levels then fill up the vacancy and X-ray photons are emitted.

From  $E = h\nu$

and  $c = \nu\lambda$

$$E = hc/\lambda$$

where  $E$  is the energy,  $h$  is the Planck's constant,  $\nu$  is the frequency of the X-ray,  $c$  is the velocity of light and  $\lambda$  is the wavelength.

Since X-rays have a very small wavelength, their energy is high enough for them to penetrate matter, the depth of penetrate depending on the density of the matter.

X-rays can be produced by a device called an X-ray tube (Fig. 1.2), cathode. There are two electrodes in an X-ray tube, an anode which is the metal target and a cathode with a tungsten filament which are situated in an evacuated chamber. Electrical current is passed through the tungsten filament and heating it to emit electrons. The electrons are accelerated to the anode target by high voltage applies across the electrodes. When the electrons strike the atoms in the target, the electron from the inner shell of the metal atom being knocked out and as a result

electrons from outer shell or higher energy levels then replace the vacancy and photons are emitted. This electronic transition results in the generation of X-rays. The X-rays then move through a beryllium window in the X-ray tube.

When the target material of the X-ray tube is bombarded with electrons accelerated from the cathode filament, two types of X-ray spectra are produced, the continuous and characteristic spectra. The characteristic spectra have been explained. The continuous spectra consist of a range of wavelengths of X-ray with minimum wavelength and intensity dependent on the target material and the voltage across the X-ray tube. The minimum wavelength decreases and the intensity increases as voltage increases.

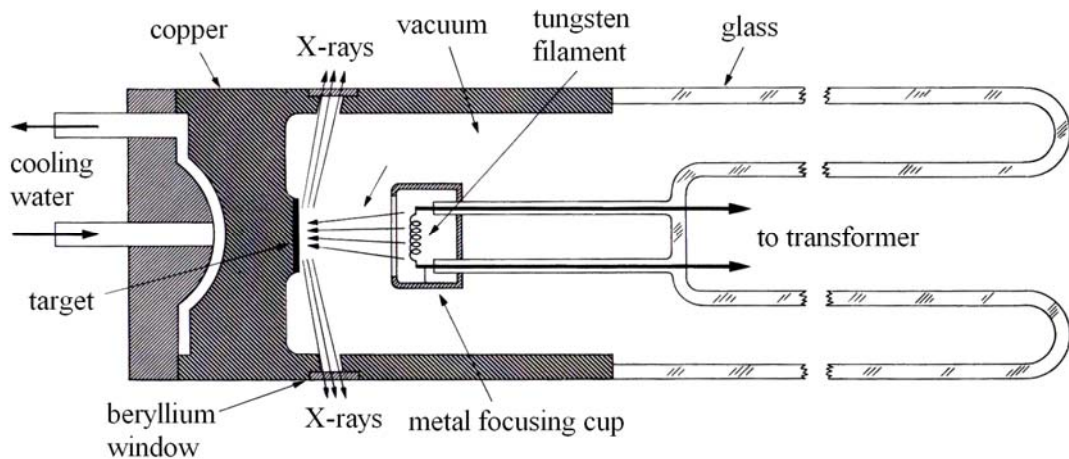


Fig. 1.2 Cross section of filament X-ray tube (Cullity, 1967).

## 1.2 Crystal Structure

A crystal structure is a solid substance consisting of an orderly arrangement of atoms repeated in the three-dimensional and bounded by plane faces. The structure of a crystal is described by space lattice and a basis with the basis of atoms assigned to each lattice point. The unit cell is the repeating volume of the lattice used to describe the crystal structure. It is characterized by six parameters, three axial lengths ( $a, b, c,$ ) and three inter-axial angles ( $\alpha, \beta, \gamma$ ). The angle  $\alpha$  is between  $b$  and  $c$ ,  $\beta$  is between  $a$  and  $c$ , while  $\gamma$  is between  $a$  and  $b$ .

Crystals can be group into seven systems by the unit cell parameters which are triclinic, monoclinic, orthorhombic, tetragonal, trigonal, hexagonal and cubic. The crystal lattices are subdivided into 14 Bravais lattices and the basis can be assigned to 32 point groups. Combining the 14 Bravais lattices with the 32 point groups lead to 230 unique arrangements of motifs in space or 230 space groups.

### 1.3 Reciprocal Lattice

The X-ray diffraction patterns are interpreted in the form of reciprocal lattice. The relationship between the crystal lattice and the reciprocal lattice can be expressed in term of vectors (Glusker & Trueblood, 1985).

$$\mathbf{a}^* \cdot \mathbf{a} = 1; \mathbf{a}^* \cdot \mathbf{b} = \mathbf{a}^* \cdot \mathbf{c} = 0$$

$$\mathbf{a}^* = \frac{\mathbf{b} \times \mathbf{c}}{\mathbf{a} \cdot \mathbf{b} \times \mathbf{c}} = \frac{\mathbf{b} \times \mathbf{c}}{V} \qquad \mathbf{a} = \frac{\mathbf{b}^* \times \mathbf{c}^*}{\mathbf{a}^* \cdot \mathbf{b}^* \times \mathbf{c}^*} = \frac{\mathbf{b}^* \times \mathbf{c}^*}{V^*}$$

$$\mathbf{b}^* = \frac{\mathbf{c} \times \mathbf{a}}{\mathbf{a} \cdot \mathbf{b} \times \mathbf{c}} = \frac{\mathbf{c} \times \mathbf{a}}{V} \qquad \mathbf{b} = \frac{\mathbf{c}^* \times \mathbf{a}^*}{\mathbf{a}^* \cdot \mathbf{b}^* \times \mathbf{c}^*} = \frac{\mathbf{c}^* \times \mathbf{a}^*}{V^*}$$

$$\mathbf{c}^* = \frac{\mathbf{a} \times \mathbf{b}}{\mathbf{a} \cdot \mathbf{b} \times \mathbf{c}} = \frac{\mathbf{a} \times \mathbf{b}}{V} \qquad \mathbf{c} = \frac{\mathbf{a}^* \times \mathbf{b}^*}{\mathbf{a}^* \cdot \mathbf{b}^* \times \mathbf{c}^*} = \frac{\mathbf{a}^* \times \mathbf{b}^*}{V^*}$$

where  $\mathbf{a}$ ,  $\mathbf{b}$ ,  $\mathbf{c}$  is the vector unit in crystal lattice,  $\mathbf{a}^*$ ,  $\mathbf{b}^*$ ,  $\mathbf{c}^*$  is the vector unit in reciprocal lattice,  $V$  is the volume in crystal lattice and  $V^*$  is the volume of reciprocal lattice.

## 1.4 X-ray Diffraction

The diffraction of X-ray can be described by a simple equation which introduced by W. L. Bragg called Bragg's law (Fig. 1.3).

$$2d \sin \theta = n\lambda, \quad n = 1, 2, 3, \dots$$

where  $d$  is the lattice spacing,  $\theta$  is the angle between the wavevector of the incident plane wave and the lattice planes,  $\lambda$  is its wave length and  $n$  is an integer, the order of the reflection.

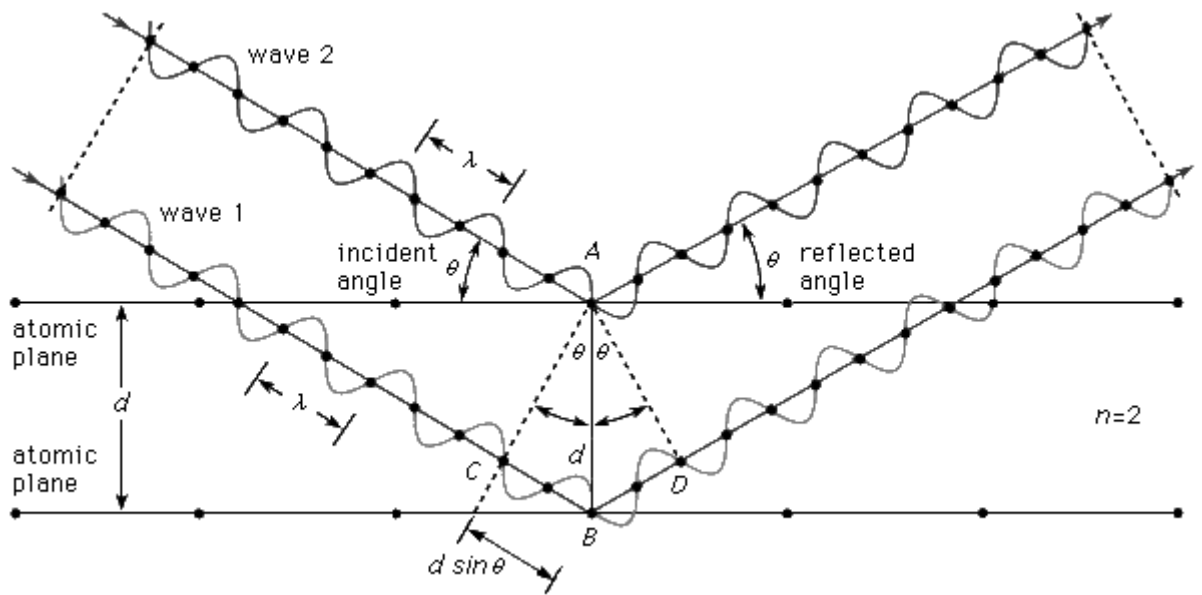


Fig. 1.3 Bragg's law diffraction (Bragg reflection, 2010).



Fig. 1.4 shows the Ewald sphere and the limiting sphere. The Ewald sphere construction shares the properties of Bragg's law. For a crystal and an X-ray beam of wavelength,  $\lambda$ , let  $\mathbf{s}_0$  be the unit vector in the direction of the primary beam and  $\mathbf{s}$  be the unit vector of the diffracted beam concerning a lattice plane with the normal vector  $\mathbf{H}$ . The vectors  $\mathbf{H}$ ,  $\mathbf{s}_0$  and  $\mathbf{s}$  are related by the equation

$$\mathbf{H} = \frac{\mathbf{s} - \mathbf{s}_0}{\lambda}$$

It can be seen that

$$\frac{|\mathbf{H}|/2}{1/\lambda} = \sin \theta$$

with  $d = 1/|\mathbf{H}|$ , we get  $\lambda = 2d \sin \theta$  which is Bragg's law. For a diffraction to take place, Ewald states that a lattice plane  $L$  is in the diffraction position if its normal vector  $\mathbf{H}$  lies on the surface of the Ewald sphere of radius  $1/\lambda$  with the crystal at its center. For any reciprocal space vector, only those that fall on the surface of the Ewald sphere obey Bragg's law and therefore lead to diffraction.

Since the diameter of Ewald sphere is  $1/\lambda$  only those reflections in reciprocal lattice space inside the sphere of radius  $2/\lambda$  (the limiting sphere) can be observed. The radius of the limiting sphere is twice of that of the Ewald sphere (Fig. 1.4).

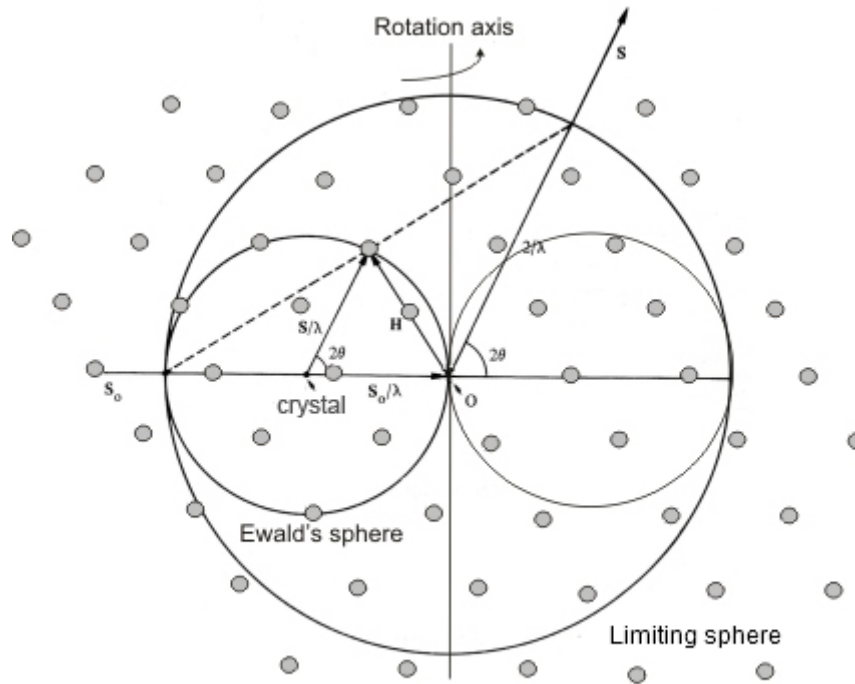


Fig 1.4 Ewald sphere, radius  $1/\lambda$  and limiting sphere, radius  $2/\lambda$  (Crystallography, 2009).

### 1.5 Superposition of waves

Each of the electrons in the crystal structure scatters a small fraction of the incident energy when a crystal is subjected to the electromagnetic field of an X-ray beam. By the principle of superposition, for these scattered waves combined to give the resultant wave reflected from each set of planes  $hkl$  (Stout & Jensen, 1989). It states that the amplitude resulting from the simultaneous action of several waves at a point is the sum of the displacements of the individual waves. The reflection of  $hkl$  consists of combined scattering waves by all atoms in the structure. An Argand diagram (Fig. 1.5) shows three waves with amplitudes  $f_1, f_2, f_3$  and phase angles  $\delta_1, \delta_2, \delta_3$ .

The x component of the resultant vector

$$x = f_1 \cos \delta_1 + f_2 \cos \delta_2 + f_3 \cos \delta_3 = \sum_{j=1}^3 f_j \cos \delta_j \quad (1.1)$$

and correspondingly for the y component

$$y = f_1 \sin \delta_1 + f_2 \sin \delta_2 + f_3 \sin \delta_3 = \sum_{j=1}^3 f_j \sin \delta_j \quad (1.2)$$

The magnitude of the resultant  $|F|$  is

$$|F| = (x^2 + y^2)^{1/2} = \left[ \left( \sum_{j=1}^3 f_j \cos \delta_j \right)^2 + \left( \sum_{j=1}^3 f_j \sin \delta_j \right)^2 \right]^{1/2} \quad (1.3)$$

and the phase angle is

$$\alpha = \tan^{-1} \frac{\sum_{j=1}^3 f_j \sin \delta_j}{\sum_{j=1}^3 f_j \cos \delta_j} \quad (1.4)$$

The result can be generalised to  $n$ th number of waves

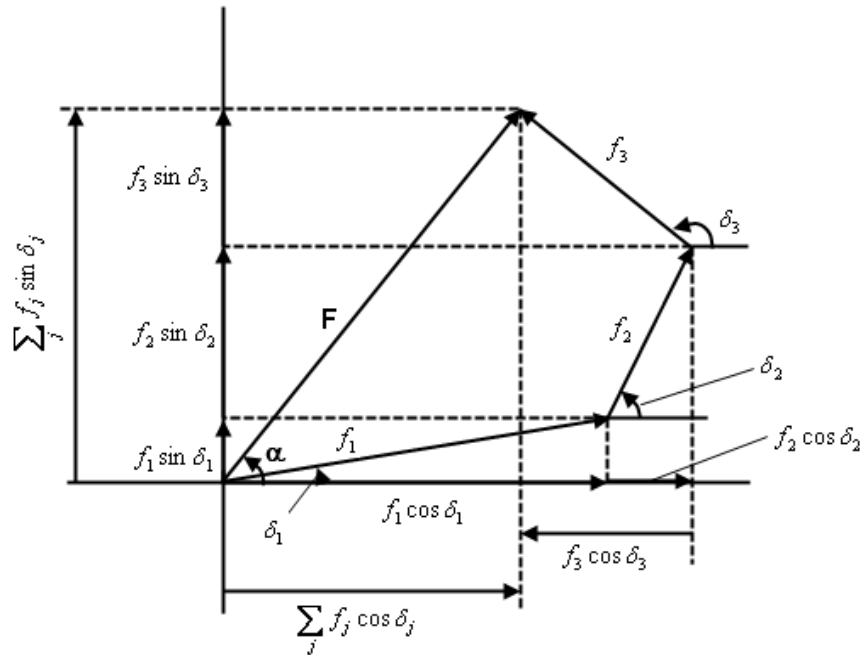


Fig. 1.5 Components on the coordinate axes of a sum of vectors are equal to the sums of the components of the individual vectors (Stout & Jensen, 1989).

## 1.6 Scattering Factor

The atomic scattering factor is needed to be considered in order to evaluate the combined scattering from the atoms in the unit cell. They are classified as functions of  $(\sin \theta)/\lambda$  and denoted as  $f_{j,\theta}$  or just  $f_j$ . The atomic scattering factor depends upon the nature of the atom, the scattering direction, the wavelength of X-rays used and the thermal vibrations of the atom (Ladd & Palmer, 1979).

Figure 1.6 shows the general form of the atomic scattering factors. The atomic scattering factor,  $f$ , depends on the number of extranuclear electrons in the atom. The maximum value for a given atom  $j$  is  $Z_j$ , the atomic number of the  $j$ th atomic species. Along the direction of the incident beam ( $\sin \theta = 0$ ),  $f$  has maximum value is

$$f_{j,\theta(\theta=0)} = Z_j \quad (1.5)$$

$f$  is measured in units of electrons.

Each atom in a structure vibrates due to thermal vibration of that particular atom in the structure. For simplicity, assuming isotropic vibration, the temperature factor correction to the atomic scattering factor for the  $j$ th atom is

$$T_{j,\theta} = \exp[-B_j(\sin^2 \theta)/\lambda^2] \quad (1.6)$$

where  $B_j$ , the temperature factor of atom  $j$ , is given by

$$B_j = 8\pi^2 \overline{U_j^2} \quad (1.7)$$

and  $\overline{U_j^2}$  is the mean-square amplitude of vibration of the  $j$ th atom from its equilibrium position.

The temperature-corrected atomic scattering factor may be written as

$$g_j = f_{j,\theta} T_{j,\theta} \quad (1.8)$$

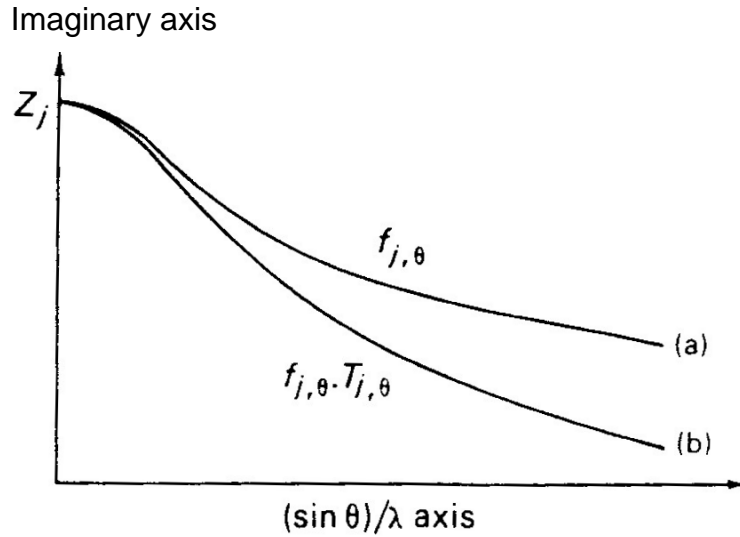


Fig. 1.6 Atomic scattering factors: (a) stationary atom,  $f_{j,\theta}$   
 (b) atom corrected for thermal vibration,  $f_{j,\theta} T_{j,\theta}$ .  
 (Ladd & Palmer, 1979).

## 1.7 Structure Factor

The structure factor,  $F_{hkl}$  is the resultant of  $N$  waves scattered in the direction of reflection  $hkl$  by the  $N$  atoms in the unit cell. Each of these waves have an amplitude proportional to the scattering factor of the atom,  $g_j$  and a phase,  $\phi_j$  with respect to the origin of the unit cell (Stout & Jensen, 1989). Since the scattering factor of an atom is given in terms of an equivalent number of electrons, the structure factor is likewise measured in units of electrons. The total phase difference in radians between the origin and the point  $x, y, z$  is

$$\phi = 2\pi(hx + ky + lz)$$

Substitution in Eq. (1.3) gives for the magnitude of the structure factor

$$|F_{hkl}| = \left\{ \left[ \sum g_j \cos 2\pi(hx_j + ky_j + lz_j) \right]^2 + \left[ \sum g_j \sin 2\pi(hx_j + ky_j + lz_j) \right]^2 \right\}^{1/2} \quad (1.9)$$

$$|F_{hkl}| = (A_{hkl}^2 + B_{hkl}^2)^{1/2} \quad (1.10)$$

where

$$A_{hkl} = \sum g_j \cos 2\pi(hx_j + ky_j + lz_j) \quad (1.11)$$

and

$$B_{hkl} = \sum g_j \sin 2\pi(hx_j + ky_j + lz_j) \quad (1.12)$$

Compare with Eq. (1.4) and referring to Fig. (1.5) will show that  $A$  and  $B$  are the projections of  $F$  on the  $x$  and  $y$  axes of a Cartesian coordinate system, so we may write

$$F_{hkl} = A_{hkl} + iB_{hkl} \quad (1.13)$$

Similarly, in view of Eq. (1.4), the phase of the resultant wave is

$$\alpha_{hkl} = \tan^{-1} \frac{B_{hkl}}{A_{hkl}} \quad (1.14)$$

The structure factor in exponential form is

$$F_{hkl} = \sum_j g_j \exp(i\phi_j) = \sum_j g_j \exp[2\pi i(hx_j + ky_j + lz_j)] \quad (1.15)$$

## 1.8 Friedel's Law

The centrosymmetric property of the diffraction pattern is stated by Friedel's law as  $I(hkl) = I(\overline{hkl})$ . The  $g_j$  will be the same for both  $hkl$  and  $\overline{hkl}$  reflections because of it is a function of  $[(\sin \theta)/\lambda]^2$ , i.e.

$$g_{j,\theta} = g_{j,-\theta} \quad (1.16)$$

because reflection from opposite sides of any plane will occur at the same Bragg angle  $\theta$ . From (1.15),

$$F_{hkl} = \sum_j g_{j,\theta} \exp[2\pi i(hx_j + ky_j + lz_j)] \quad (1.17)$$

and

$$F_{\overline{hkl}} = \sum_j g_{j,-\theta} \exp[-2\pi i(hx_j + ky_j + lz_j)] \quad (1.18)$$

From (1.13),

$$F_{hkl} = A_{hkl} + iB_{hkl} \quad (1.19)$$

where  $A_{hkl}$  and  $B_{hkl}$  are given by (1.11) and (1.12), respectively. It is known that  $\cos(-\theta) = \cos \theta$  and  $\sin(-\theta) = -\sin \theta$ . Thus,

$$F_{\overline{hkl}} = A_{hkl} - iB_{hkl} \quad (1.20)$$

Fig. 1.7 show the vectorial representations of  $F(hkl)$  and  $F(\overline{hkl})$  on an Argand diagram. Important relationships are:

$$\varphi(\overline{\overline{hkl}}) = -\varphi(hkl) \quad (1.21)$$

$$|F(hkl)| = |F(\overline{hkl})| = [A'^2(hkl) + B'^2(hkl)]^{1/2} \quad (1.22)$$

Since  $I(hkl) \propto |F(hkl)|^2$ , thus,

$$I(hkl) = I(\overline{hkl}) \quad (1.23)$$

which is Friedel's law.

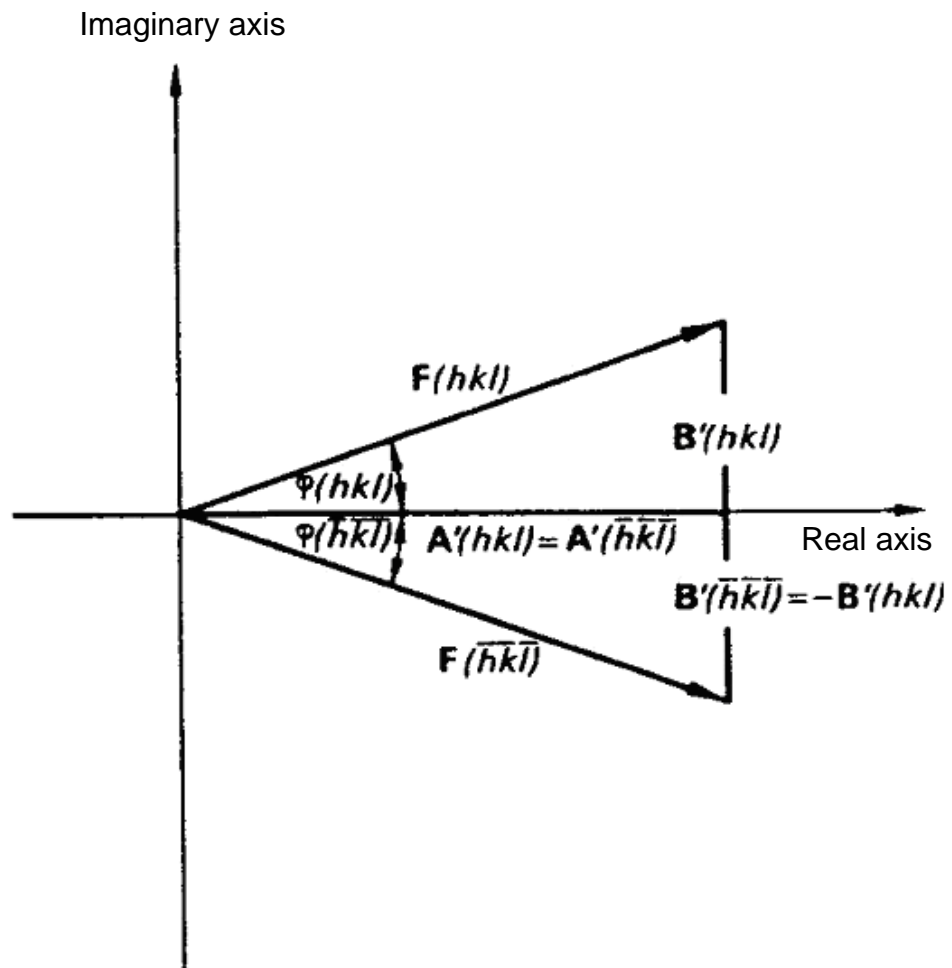


Fig. 1.7 Relationship between  $F(hkl)$  dan  $F(\overline{hk\overline{l}})$  leading to Friedel's law, from which  $|F(hkl)| = |F(\overline{hk\overline{l}})|$  (Ladd & Palmer, 1979).



## 1.9 Electron Density

The electron density,  $\rho$  is the concentration of electrons in the vicinity of atoms in a crystal. It is often measured in electrons per  $\text{\AA}^3$ . Atoms with high atomic numbers will have larger concentration of electrons compared to atoms of low atomic numbers (Ladd & Palmer, 1979).

Atoms appear as peaks in the electron density function and this peak position is assumed to correspond to its atomic centre. The heights of the peaks in an electron density distribution of a crystal are proportional to the corresponding atomic numbers. Situated at the extreme low end of the atomic numbers, the hydrogen atom does not appear in electron density representations. Its small electron density merges into the background density. Nevertheless, hydrogen atoms can be detected through the difference-Fourier technique. In general, the more complete and accurate the experimental  $|F|$  data, the better will be the atomic resolution and the more precise the final structure model (Ladd & Palmer, 1979).

The general electron density function is expressed as a three-dimensional Fourier series, that is

$$\rho(x, y, z) = \frac{1}{V} \sum_h \sum_k \sum_l F_{hkl} \exp[-2\pi i(hx_j + ky_j + lz_j)] \quad (1.24)$$

where  $V$  is the unit-cell volume.

An alternative expression for a three-dimensional Fourier series can be obtained by noting that the structure factor can be written in the form

$$\mathbf{F}_{hkl} = |F_{hkl}| \exp(2\pi i \phi_{hkl}) \quad (1.25)$$

where  $\phi_{hkl}$  is the phase angle in cycles. Substitution into Eq. (1.24) gives

$$\rho(x, y, z) = \frac{1}{V} \sum_h \sum_k \sum_l |F_{hkl}| \exp(2\pi i \phi_{hkl}) \exp[-2\pi i(hx + ky + lz)] \quad (1.26)$$

$$\rho(x, y, z) = \frac{1}{V} \sum_h \sum_k \sum_l |F_{hkl}| \exp[-2\pi i(hx + ky + lz) - \phi_{hkl}] \quad (1.27)$$

Expanding Eq. (1.27) in terms of sine and cosine, and then assuming that Friedel's law holds so that the sine terms cancel for pairs of  $\mathbf{F}_{hkl}$  and  $\mathbf{F}_{\bar{h}\bar{k}\bar{l}}$  leads to

$$\rho(x, y, z) = \frac{1}{V} \sum_h \sum_k \sum_l |F_{hkl}| \cos[2\pi(hx + ky + lz) - \phi_{hkl}] \quad (1.28)$$

To get the  $\rho(x, y, z)$ , both  $|F_{hkl}|$  and  $\phi_{hkl}$  are needed. The  $|F_{hkl}|$  can be obtained from the intensity data from the experiment, but the corresponding phase  $\phi_{hkl}$  is not directly measurable. Basically, there are two methods to obtain the phase  $\phi_{hkl}$ :

- (1) Patterson Method (Heavy atom method)
- (2) Direct method

### 1.10 Patterson Method (Heavy Atom)

The very first solution to the phase problem was introduced by Arthur Lindo Patterson in 1934. He reported a new Fourier series which could be calculated directly from the experimental intensity data by introduced a new function  $P(u, v, w)$  which defines a new space (the Patterson space) and derived a formula known as the Patterson function (a simplification of the information contained in the electron density function).

$$P(u, v, w) = \frac{1}{V} \sum_h \sum_k \sum_l |F_{hkl}|^2 \cos 2\pi(hu + kv + lw) \quad (1.29)$$

The Patterson function removes the term containing the phases, and the amplitudes of the structure factors are replaced by their squares. It is thus a function that can be calculated immediately from the available experimental data. The Patterson function provides a map of interatomic vectors (relative atomic positions), the height of its maxima being proportional to the number of electrons of the atoms implied. A peak at the point  $uvw$  in a Patterson map indicates that atoms exist in the crystal at  $x_1, y_1, z_1$  and  $x_2, y_2, z_2$  such that  $u = x_1 - x_2$ ,  $v = y_1 - y_2$  and  $w = z_1 - z_2$ . The heights of the peaks are approximately proportional to the values of  $Z_i Z_j$ , in which  $Z_i$  is the atomic number of the atom at one end of the vector and  $Z_j$  that of the atom at the other end.

This feature means an advantage in detecting the positions of "heavy" atoms (with many electrons) in structures where the remaining atoms have lower atomic numbers. If a structure contains one or a few atoms of higher atomic number, these atoms will dominate the scattering process. These atoms can usually be located from the Patterson map and the phases of the entire structure will seldom be far from the phases of the heavy atom(s). The remainder of the structure will usually be

revealed in the resulting electron density map, leading to improved phases and better approximations to the structure.

Once the Patterson map is calculated, it has to be correctly interpreted (at least partially) to get the absolute positions  $(x, y, z)$  of the heavy atoms within the unit cell. These atomic positions can now be used to obtain the phases  $\phi_{hkl}$  of the diffracted beams by inverting Eq. (1.28) and therefore this will allow the calculation of the electron density function  $\rho(x, y, z)$ .

The Patterson functions are restricted to certain rules (Stout & Jensen, 1989):-

1. All Patterson functions are centrosymmetric.
2. Their lattice type ( $P, C, F$ , etc.) is the lattice type of the original space group.
3. Their space group is derived from the original space group by replacing all translational symmetry elements (screw, glides) by the corresponding non-translational elements (axes, mirrors) and by adding a center of symmetry if it is not already present.

Although the majority of structural problems are now solved by direct methods, these methods sometimes fail. In addition, there exist problems, especially with macromolecules, that are too large for current direct methods. The alternative approaches generally involve analyzing the intensity data by way of the Patterson function.

## 1.11 Direct Methods

Direct phasing is now the most common and important method to solve structures. The result of 80-90% of the reported small-molecule structures are solved using direct methods.

A very important step in the development of direct methods was the formulation by Sayre of a relationship based only on these two assumptions (Massa, 2004): that the electron density in a structure can never have a negative value, and that it is concentrated in well defined maxima

$$F_{hkl} = \phi_{hkl} \sum \sum \sum F_{h'k'l'} \cdot F_{h-h',k-k',l-l'} \quad (1.30)$$

This equation states that the structure factor for any reflection  $hkl$  can be calculated as the sum of the products of the structure factors of all pairs of reflections whose indices sum to it.

Karl and Hauptman develop the principle into a practical method which is used today more than any other method. For centrosymmetric structures, in which the phase problem is reduced to a “sign problem”, for a so-called  $\Sigma_2$  triplet of strong reflections contributing to the Sayre equation

$$S_{hkl} \approx S_{h'k'l'} \cdot S_{h-h',k-k',l-l'} \quad (1.31)$$

where  $S$  is refer to sign. If both  $S_{h'k'l'}$  and  $S_{h-h',k-k',l-l'}$  have the same sign (positive or negative) it is probable that the sign of  $S_{hkl}$  is positive. When three strong reflections have a triplet relationship to one another,  $hkl$ ,  $h'k'l'$  and  $h-h',k-k',l-l'$ , then the electron density must be concentrated at intervals of  $d$  for all three sets of lattice planes. If the phases of two of the reflections are known, then the phase of the third reflection is determined by them. Each  $\Sigma_2$ -relationship in fact gives the probability

that the sign of a reflection  $hkl$  is determined by those of  $h'k'l'$  and  $h-h',k-k',l-l'$ , the probability depending on how strong the three reflections are. For  $N$  atoms of equal weight in the unit cell, the probability  $p$ , that a phase is correctly determined is given by the relationship

$$P = 1/2 + 1/2 \tanh \left\{ 1/\sqrt{N} \left| E_{hkl} E_{h'k'l'} E_{h-h',k-k',l-l'} \right| \right\} \quad (1.32)$$

where  $E$  is normalized structure factor. It is thus clear that direct methods work less well in principle for more complex structures. The limits for the method currently lie in the region of 200-300 non-hydrogen atoms in the asymmetric unit.

For noncentrosymmetric structures where there is no center of symmetry in a structure, then instead of a sign, a phase angle  $\phi_{hkl}$  must be determined. In the general form of the Sayre equation, the structure factors are complex quantities, and an analogous to the sign relationship, a phase relationship may be derive

$$\phi_{hkl} \approx \phi_{h'k'l'} + \phi_{h-h',k-k',l-l'} \quad (1.33)$$

The objective is to derive a phase  $\phi_{hkl}$ , normally from a large number of  $\Sigma_2$ -relationship. Karle and Hauptman derived for this purpose the so-called tangent formula

$$\tan \phi_{hkl} = \frac{\sum_{h'k'l'} 1/\sqrt{N} \left| E_{hkl} E_{h'k'l'} E_{h-h',k-k',l-l'} \right| \cdot \sin(\phi_{h'k'l'} + \phi_{h-h',k-k',l-l'})}{\sum_{h'k'l'} 1/\sqrt{N} \left| E_{hkl} E_{h'k'l'} E_{h-h',k-k',l-l'} \right| \cdot \cos(\phi_{h'k'l'} + \phi_{h-h',k-k',l-l'})} \quad (1.34)$$

(Massa, 2004)

## 1.12 Data Reduction

The collected data intensities consist of raw data from which crystal structures are derived. It represents all the information obtained from physical measurement on the crystal and further development of a structure depends on the skilful extraction of the information contained within the intensities. These raw intensities are corrected for various effects, a process referred to as data reduction (Stout & Jensen, 1989).

The amplitude of structure factor,  $|F_{hkl}|$  is the most important quantity derived from the intensities. It is related to the experimentally observed intensities

$$|F_{hkl}| \propto \sqrt{I} \quad (1.35)$$

As we have described earlier, the structure factors are used to determine the positions of atoms from the electron density maps. It is customary to convert the intensities into “observed” structure amplitudes ( $|F_o|=|F_{\text{observed}}|$ ) by a data reduction program and to use these as the observed data in subsequent calculations.

The relationship between  $|F_{hkl}|$  and  $I$  depends on a number of factors. Normally, it is related to the individual reflection and the apparatus used to measure its intensity (Stout & Jensen, 1989). The proportionality of (1.35) can be rewritten as

$$|F_{hkl}| = (KI_{hkl} / Lp)^{1/2} \quad (1.36)$$

The term  $K$  depends on crystal size, beam intensity, and other fundamental constants. It is usually a constant for any given set of measurements and therefore omitted from data reduction.

The polarization factor,  $p$  is given by

$$p = \frac{(1 + \cos^2 2\theta)}{2} \quad (1.37)$$

and is a simple function of  $2\theta$ , independent of the method of data collection except when a crystal monochromator is used. When a graphite monochromator is used, the reflection by the monochromator affects the direct beam before it reaches the crystal, and an additional factor  $Q$  must be introduced (Massa, 2004) to correct for the monochromator

$$p = \frac{(1 + Q \cos^2 2\theta)}{(1 + Q)} \quad (1.38)$$

The Lorentz factor,  $L$  is depends on the precise measurement technique used, given by

$$L = \frac{1}{\sin 2\theta} \quad (1.39)$$

Normally, these two effects are considered together as the so-called  $Lp$ -correction

$$Lp = \frac{(1 + \cos^2 2\theta)}{(2 \sin 2\theta)} \quad (1.40)$$

Thus, the observed structure factor  $|F_o|$ , on an arbitrary scale, may be calculated as

$$|F_o| = (I_{hkl} / Lp)^{1/2} \quad (1.41)$$



Corrections of absorption are potentially important. In an absorption process, the intensity,  $I$  of a beam after passing through a thickness  $t$  of absorber is given by

$$I = I_o e^{-\mu t} \quad (1.42)$$

where  $I_o$  is the intensity of the incident beam and  $\mu$  is the linear absorption coefficient. To some extent they have become less significant with diffractometer data on small molecules with molybdenum radiation. It is because the coefficient is depended on the empirical formula, size of the crystal, and X-ray source used. In general, absorption correction is applied to improve the accuracy of the results, especially for crystal with large  $\mu$  value.

### 1.13 Refinement

The principle of least squares states that the best value for the parameters are those that minimize the sums of the squares of the properly weighted differences between the observed and the calculated values of the function for all the observational points. The functional form of the structure factor is transcendental and so must be approximated by a truncated Taylor series (Stout & Jensen, 1989). Thus the quantity to be minimized is given by

$$D = \sum_{hkl} w_{hkl} (|F_o| - |kF_c|)^2 \quad (1.43)$$

where  $w$  is the weight to be assigned an observation. In order to obtain the best fit, it will be necessary to consider a scale factor and the positional and temperature parameters of the atoms as variables that can be adjusted to minimize  $D$ . This gives a set of  $n$  equations in  $n$  unknown called the normal equations. These equations are linear equation.

The very weak reflections in an X-ray diffraction data set have relatively large errors and those for which the background exceeds the peak will have negative net intensities. They are undefined and cannot be used when refining against  $|F_o|$ . It is customary to eliminate the very weak reflections by use of a threshold reflections with intensities less than some positive threshold value such as  $2\sigma(I)$  are given zero weight. The use of any threshold, however, introduces a bias in the data and is indefensible in principle; it is much better to refine against  $|F_o|^2$  so that all data can be included. The function is minimized.

$$D' = \sum_{hkl} w'_{hkl} (|F_o|^2 - |kF_c|^2)^2 \quad (1.44)$$

The weighting functions,  $w$ , should be a measure of the reliability of the observation. It has the effect of adjusting the contribution of each observation to the normal equations in such way as to produce the most reliable results. An example would be that the weight is equal to the reciprocal of the square of the standard deviation of the observation (Cruickshank, 1965; Hong & Robertson, 1985).

A useful index often output by least squares refinement programs is the so-called goodness of fit,

$$GOF = \left[ \frac{\sum w(|F_o| - |F_c|)^2}{n - m} \right]^{1/2} \quad (1.45)$$

Sometimes it also termed as the standard deviation of an observation of unit weight. It is a measure of the degree to which the found distribution of differences between  $|F_o|$  and  $|F_c|$  fits the distribution expected from the weights used in the refinement. If these weights are correct, which implies that the errors in the data are strictly random and correctly estimated and if the model properly represents the structure that gives rise to the data, the value of the  $GOF$  is 1.0.