

HYBRID GENETIC ALGORITHM AND PARTICLE FILTER OPTIMIZATION
MODEL FOR SIMULTANEOUS LOCALIZATION AND MAPPING PROBLEMS

MOHSEN MAHRAMI

A thesis submitted in fulfilment of the
requirements for the award of the degree of
Doctor of Philosophy (computer science)

Faculty of Computing
Universiti Teknologi Malaysia

MARCH 2016

I would like to dedicate this to my late mother.

ACKNOWLEDGMENT

In the name of Allah the Most Gracious and the Most Merciful, I thank thee with all my heart for granting Thy Servant immeasurable help during this study.

I would like to express my gratitude to my supervisor Prof. Dr. Habibollah Haron for his guidance and encouragement in completing this work also I am thank full to my co-supervisor Dr. Azurah Bt. Abu Samah for her cooperation during this research.

My sincere thank also goes to UTM, Faculty of Computing and RMC for supporting this study, researchers, and academicians for their contribution towards my understanding and thoughts.

And finally I express my gratitude to my family especially my wife for her self-devotions who endured all of hardships for my study and advancement.

ABSTRACT

Determining position of a robot and knowing position of the required objects on the map in unknown environments such as underwater, other planets and the remaining areas of natural disasters has led to the development of efficient algorithms for Simultaneous Localization and Mapping (SLAM). The current solutions for solving the SLAM have some drawbacks. For example, the solutions based on Extended Kalman Filter (EKF) are faced with limitation in non-linear models and non-Gaussian errors which are causes for decrease of accuracy. The solutions based on particle filter are also suffering from high memory complexity and time complexity. One of the major approaches to solve the SLAM problem is the approach based on Evolutionary Algorithm (EA). The main advantage of the EA is that it can be used in search space which is too large to be used with high convergence while its disadvantage is high time and computational complexity. This thesis proposes two optimization models in solving SLAM problem namely Hybrid Optimization Model (HOM) and Lined-Based Genetic Algorithm Optimization Model (LBGAOM). These models do not have the limitations of EKF, memory complexity of particle filter, and disadvantages of EA in search space. When the results of HOM compared with original EA, it showed an increase of accuracy based on presented fitness function. The best fitness in original EA was 16.36 but in HOM has reached to 16.68. Both models applied a proposed new representation model. The representation model is designed and used to represent the robot and its environment and is based on occupancy grid and genetic algorithm. There are two types of representation models proposed in this thesis namely Layer 1 and Layer 2. For each layer, related fitness function is created to evaluate the accuracy of map in the model that was tested with some different parameters. The proposed HOM is designed based on genetic algorithm and particle filter by creating a new mutation model inspired by particle filter. The search space is reduced and only suitable space will be explored based on proposed functions. The proposed LBGAOM is a new optimization model based on extraction line from laser sensor data to increase the speed. In this model, search space in the map is a set of lines instead of pixel by pixel and it makes searching time faster. The evaluation of the proposed representation model shows that Layer 2 has better fitness value than Layer 1. The HOM has better performance compared to original GA Layer 1. The LBGAOM has decreased the search space compared to pixel based model. In conclusion, the proposed optimization models have good performance in solving the SLAM problem in terms of speed and accuracy.

ABSTRAK

Menentukan posisi sesebuah robot dan mengetahui posisi objek yang dikehendaki di atas peta, di persekitaran yang tidak diketahui seperti di bawah paras laut, planet lain dan di lokasi bencana alam telah mendorong kepada pembangunan algorithma yang efisien bagi Pemetaan dan Penempatan Serentak (SLAM). Penyelesaian terkini bagi menyelesaikan SLAM mempunyai beberapa kelemahan. Antaranya adalah penyelesaian berdasarkan Penapis Kalman yang Dilanjutkan (EKF) berhadapan dengan had yang terdapat dalam model bukan linear dan ralat bukan-Gaussian yang menjadi sebab untuk mengurangkan ketepatan. Penyelesaian berdasarkan saringan partikel berhadapan dengan masalah storan tinggi yang kompleks. Salah satu pendekatan utama untuk menyelesaikan permasalahan SLAM adalah pendekatan berdasarkan Algoritma Berevolusi (EA). Kelebihan utama EA adalah ianya boleh digunakan dalam ruang carian yang sangat besar dengan tumpuan yang tinggi manakala kelemahannya pula adalah dari segi masa yang lama dan pengkomputeran yang kompleks. Tesis ini mencadangkan dua model pengoptimuman dalam menyelesaikan permasalahan SLAM iaitu Model Pengoptimuman Hibrid (HOM) dan Model Pengoptimuman Algoritma Genetik Berasaskan Garisan (LBGAOM). Kedua-dua model tidak mempunyai had EKF, memori yang kompleks bagi saringan partikel dan kelemahan EA dalam ruang carian. . Apabila keputusan HOM dibandingkan dengan EA yang asal, ia menunjukkan ketepatan keputusan meningkat berdasarkan fungsi kecergasan yang dihitung. Kecergasan terbaik dalam EA asal adalah 16.36 tetapi dalam HOM telah mencapai ke 16.68. Kedua-dua model mencadangkan perwakilan model yang baru. Perwakilan model tersebut direka dan digunakan untuk mewakili robot dan persekitarannya, dan adalah berdasarkan penggunaan grid dan algoritma genetik. Terdapat dua jenis perwakilan model yang dicadangkan di dalam tesis ini iaitu Lapisan 1 dan Lapisan 2. Bagi setiap lapisan, fungsi padanan yang berkaitan dibina untuk menilai ketepatan peta bagi sesuatu model yang kemudiannya diuji menggunakan beberapa parameter yang berlainan. HOM yang dicadangkan, direka bentuk berdasarkan algoritma genetik dan saringan partikel dengan membina suatu model mutasi baru yang diilhamkan oleh saringan partikel. Ruang carian dikesilkan dan hanya ruang yang bersesuaian sahaja dijelajah berdasarkan fungsi-fungsi yang telah dicadangkan. LBGAOM yang dicadangkan adalah sebuah model pengoptimuman baru, berdasarkan garisan ekstrak dari data imbasan laser, bertujuan meningkatkan kelajuan. Dalam model ini, ruang carian dalam peta adalah satu set garisan dan bukannya piksel yang mana menjadikan masa carian lebih pantas. Penilaian model perwakilan yang dicadangkan, menunjukkan bahawa Lapisan 2 mempunyai nilai padanan yang lebih baik dari Lapisan 1. HOM mempunyai prestasi yang lebih baik berbanding Lapisan 1 GA yang asal. LBGAOM pula telah mengecilkan ruang carian berbanding model berasaskan piksel. Sebagai kesimpulan, model-model pengoptimuman yang telah dicadangkan memiliki prestasi yang baik dalam menyelesaikan permasalahan SLAM dari segi kelajuan dan ketepatan.

TABLE OF CONTENTS

CHAPTER	TITLE	PAGE
	DECLARATION	ii
	DEDICATION	iii
	ACKNOWLEDGMENT	iv
	ABSTRACT	v
	ABSTRAK	vi
	TABLE OF CONTENTS	vii
	LIST OF TABLES	xi
	LIST OF FIGURES	xiv
	LIST OF ABBREVIATIONS	xix
	LIST OF APPENDICES	xx
1	INTRODUCTION	1
	1.1 Overview	1
	1.2 Problem Background	4
	1.3 Problem Statement	6
	1.4 Purpose of Study	8
	1.5 Objectives	8
	1.6 Research Scope	8
	1.7 Significance of Research	9
	1.8 Thesis Overview	10
2	LITERATURE REVIEW	12
	2.1 Introduction	12
	2.2 Effective Parameters in SLAM	13

2.2.1	Sensor Uncertainty	13
2.2.2	Correspondence Issue	14
2.2.3	Loop Closing	15
2.2.4	Computational Complexity	16
2.2.5	Dynamic Environment	16
2.3	Models of Map in Robotic	16
2.3.1	Metric Map	17
2.3.2	Topologic Map	18
2.3.3	Conceptual Map	19
2.3.4	Cognitive Map	19
2.4	Tools in Solving SLAM	20
2.4.1	Extended Kalman Filter (EKF)	20
2.4.2	Particle Filter	24
2.4.3	Particle Swarm Optimization (PSO)	27
2.4.4	Genetic Algorithm	27
2.5	Previous Solutions for Solving SLAM	35
2.5.1	Traditional Solutions for Solving SLAM	35
2.5.2	Heuristic Solutions for Solving SLAM	38
2.6	Discussion of SLAM and GA Performance	43
2.7	Finding from Literature	46
2.8	Summary	47
3	RESEARCH METHODOLOGY	49
3.1	Introduction	49
3.2	Research Methodology	50
3.3	Literature Review and Problem Analysis	53
3.4	Design the Simulation Model and Experimental Setup	53
3.4.1	Procedure of Design the Map and Implementation	53
3.4.2	Procedure and Functions of Experimental Setup	57
3.5	Development of Optimization Models	62
3.5.1	New Representation of Occupancy Grid	62

	3.5.2 Hybrid Optimization Model based on GA and Particle Filter	62
	3.5.3 Line-Based Genetic Algorithm Optimization Model	63
	3.6 Implementation and Evaluations	63
	3.7 Summary	64
4	NEW REPRESENTATION OF OCCUPANCY GRID BASED ON GENETIC ALGORITHM AND PARAMETERS TUNING	65
	4.1 Introduction	65
	4.1.1 Occupancy Grid Representation	67
	4.2 Proposed Model	68
	4.2.1 GA-Based Algorithm for Increase the Accuracy	70
	4.2.2 Layer 1 Model	75
	4.2.3 Layer 2 Model	76
	4.3 Results and Discussion	77
	4.3.1 Results and Discussion for 1 Layer Model	77
	4.3.2 Results and Discussion for 2 Layers Model	87
	4.4 Chapter Summary	99
5	A HYBRID OPTIMIZATION MODEL BASED ON GENETIC ALGORITHM AND PARTICLE FILTER	101
	5.1 Introduction	101
	5.2 Hybrid Model	102
	5.3 Result and Discussion	109
	5.3.1 1st Experiment: Evaluation of Epsilon Parameter in Mutation	108
	5.3.2 2th Experiment: Evaluation of Nmutation & Popsiz Parameters	115
	5.4 Comparison and Conclusion	122
	5.5 Summary	122

6	A LINE-BASED GENETIC ALGORITHM OPTIMIZATION MODEL (LBGAOM)	124
6.1	Introduction	124
6.2	Design the Parameters of Proposed Algorithm	125
6.2.1	Chromosome Design	127
6.2.2	Fitness Function	129
6.2.3	Selection	131
6.2.4	Mutation	131
6.3	New Genetic Algorithm Development Based on Line Extraction	131
6.4	Simulation and Evaluation	132
6.4.1	Results and Discussion	134
6.5	Chapter Summary and Conclusion	145
7	SUMMARY AND CONCLUSION	147
7.1	Research Summary	147
7.2	Research Contributions	149
7.3	Limitations and Future works	150
	REFERENCES	151
	Appendices A –D	163 - 244

LIST OF TABLES

TABLE NO.	TITLE	PAGE
2.1	Comparison between the useable methods in SLAM based on common parameters	34
2.2	Comparison between current solutions for SLAM	42
2.3	Comparison between heuristic solutions based on their operations	43
3.1	Correlation between Research Questions, Objectives, and Optimization Model Developments	52
4.1	The evaluated values for generation number and population size in experiment 1	78
4.2	The best fitness of each run and average of those in Test 1	79
4.3	The comparison between best fitness of all Tests in experiment 1	80
4.4	The evaluated values for p mutation in experiment 2	80
4.5	The best fitness of each run and average of those in Test 9	81
4.6	The comparison between best fitness of all Tests in experiment 2	82
4.7	The evaluated values for p crossover in experiment 3	82
4.8	The best fitness of each run and average of those in Test 15	83
4.9	The comparison between best fitness of all Tests in experiment 3	84
4.10	The evaluated values for q tournament in experiment 4	85

4.11	The best fitness of each run and average of those in Test 21	86
4.12	The comparison between best fitness of all Tests in experiment 4	86
4.13	The evaluated values for generation number & population size in experiment 5	87
4.14	The comparison between best fitness of all Tests in experiment 5	89
4.15	The evaluated values for p mutation in experiment 6	89
4.16	The comparison between best fitness of all Tests in experiment 6	91
4.17	The evaluated values for p crossover in experiment 7	92
4.18	The comparison between best fitness of all Tests in experiment 7	93
4.19	The evaluated values for q tournament in experiment 8	94
4.20	The comparison between best fitness of all Tests in experiment 8	96
4.21	The evaluated values for w1 and w2 in experiment 9	96
4.22	The comparison between best fitness of all Tests in experiment 9	99
5.1	1st Test main parameters	108
5.2	The best fit and average for 1st Test in 4 runs	109
5.3	2nd Test main parameters	110
5.4	The best fit and average for 2nd Test in 3 runs	110
5.5	3rd Test main parameters	111
5.6	The best fit and average for 3rd Test in 3 runs	111
5.7	4th Test main parameters	112
5.8	The best fit and average for 4th Test in 3 runs	112
5.9	5th Test main parameters	113
5.10	The best fit and average for 5th test in 4 runs	114
5.11	comparison between best fitness in all tests in 1th experiment	115
5.12	6th Test main parameters	116
5.13	The best fit and average for 6th Test in 3 runs	116

5.14	7th Test main parameters	117
5.15	The best fit and average for 7th Test in 3 runs	117
5.16	8th Test main parameters	118
5.17	The best fit and average for 8th Test in 3 runs	119
5.18	9th Test main parameters	120
5.19	The best fit and average for 9th Test in 3 runs	120
5.20	comparison between best fitness in all tests in 2th experiment	121
5.21	Comparison between the best fitness value in original GA and hybrid model of GA and particle filter	122
6.1	1st Experiment main parameters	135
6.2	Algorithm run fitness per iterations in experiment 1 based on 10 runs	135
6.3	2th Experiment main parameters	137
6.4	Algorithm run fitness per iterations in experiment 2 based on 10 runs	138
6.5	3rd Experiment main parameters	139
6.6	Algorithm run fitness per iterations in experiment 3 based on 30 runs	140
6.7	Comparison between all 3 experiments	143
6.8	Parameters of second discussion	144

LIST OF FIGURES

FIGURE NO.	TITLE	PAGE
1.1	Activities that must be performed to obtain an accurate model of the environment.	3
1.2	Model extraction by robot based on features (doors) and transfer to uni-modal Gaussian diagram for use in EKF.	5
1.3	Model extraction by robot based on features and showing the number of particles in high probability places	5
2.1	Some effective parameters in SLAM.	13
2.2	A sample of error in map representation because of uncertainty in input data of robot.	14
2.3	Correspondence is where the robot moves in a loop.	15
2.4	An example of closing the loop.	15
2.5	Kind of map representation in robotic	17
2.6	Occupancy grid as a metric map.	18
2.7	Topologic map: a graph of nodes and links.	18
2.8	The hierarchical structure of a conceptual map. On the left side, the geometric information is collected by the robot and the right side contains semantic information.	19
2.9	Tools and methods for using in SLAM.	20
2.10	Representation of probability distribution by group of particles.	24
2.11	Particle filter re-sampling	25
2.12	Particle filter in update step	26
2.13	One point and two point and uniform crossover.	32

2.14	The overall process of genetic algorithms	34
2.14	Previous solutions for SLAM.	35
2.15	One example of ancestry tree for update the maps in DP-SLAM.	37
3.1	The Research Methodology Framework.	51
3.2	The overall procedure of initial setup	54
3.3	procedure of setup a map	55
3.4	A sample of map and robot movement in this map. the red points are obstacles and blue line is the robot path.	56
3.5	Pseudo code of makegrid function.	58
3.6	Pseudo code of robotmove function.	58
3.7	Pseudo code of obstacle function.	60
3.8	Pseudo code of lasserDirection function.	61
4.1	the first representation model of occupancy grid	67
4.2	the second representation model of occupancy grid	68
4.3	Parameters for determine the position of obstacle from robot	69
4.4	three different collected map from one instant part in three step	72
4.5	difference between real path and reported map	73
4.6	chromosome model design based on path	74
4.7	A schema of two layers model of occupancy grid.	76
4.8	Comparison between average fitness from all tests in experiment 1	79
4.9	Comparison between average fitness from all tests in experiment 2	81
4.10	Comparison between average fitness from all tests in experiment 3	83
4.11	Comparison between average fitness from all tests in experiment 4	85
4.12	Comparison between average fitness from all tests in experiment 5	88
4.13	Comparison between average fitness1 from all tests in experiment 5	88

4.14	Comparison between average fitness2 from all tests in experiment 5	88
4.15	Comparison between average fitness from all tests in experiment 6	90
4.16	Comparison between average fitness1 from all tests in experiment 6	90
4.17	Comparison between average fitness2 from all tests in experiment 6	91
4.18	Comparison between average fitness from all tests in experiment 7	92
4.19	Comparison between average fitness1 from all tests in experiment 7	93
4.20	Comparison between average fitness 2 from all tests in experiment 7	93
4.21	Comparison between average fitness from all tests in experiment 8	95
4.22	Comparison between average fitness1 from all tests in experiment 8	95
4.23	Comparison between average fitness2 from all tests in experiment 8	95
4.24	Comparison between average fitness from all tests in experiment 9	97
4.25	Comparison between average fitness1 from all tests in experiment 9	97
4.26	Comparison between average fitness2 from all tests in experiment 9	98
5.1	The scheme of hybrid Particle filter and genetic algorithm	104
5.3	A diagram of an equation and some selected points for finding the highest point of diagram.	106
5.4	Addition of a fixed value in common mutation operation in original genetic algorithm.	107

5.5	Addition of different values based on position of selected point in new model of mutation operation in original genetic algorithm.	107
5.6	Average of best fit in 1st test with 100 generation	109
5.7	Average of best fit in 2nd test with 100 generations	110
5.8	Average of best fit in 3rd test with 100 generations	111
5.9	Average of best fit in 4th test with 100 generations	113
5.10	Average of best fit in 5th test with 100 generations	114
5.11	Comparison between averages of best fit in 5 tests with 100 generations	114
5.12	Average of best fit in 6th test with 100 generations	116
5.13	Average of best fit in 7th test with 100 generations	118
5.14	Average of best fit in 8th test with 100 generations	119
5.15	Average of best fit in 9th test with 100 generations	120
5.16	Comparison between averages of best fitness in 4 tests with 100 generations	121
6.1	Overview of flowchart of proposed procedure.	126
6.2	The real map	127
6.3	The map obtained by the robot	127
6.4	Pre-processing of the map obtained by the robot by lines	128
6.5	Presented chromosome model for LBGAOM	129
6.6	Overview of proposed algorithm	132
6.7	Base map	133
6.8	Robot observation	133
6.9	A sample map before correction	134
6.10	The map after correction by algorithm.	134
6.11	The 1st Experiment : the robot navigation path	136
6.12	The average of best cost (fitness) of population based on running the algorithm ten iterations in 10 consecutive generations	137
6.13	The 2st Experiment : the robot navigation path	138
6.14	The average of best cost (fitness) of population based on running the algorithm ten times (iteration) in 10 consecutive generations	139

6.15	The 3st Experiment : the robot navigation path	141
6.16	The average of best cost (fitness) of population based on running the algorithm ten times (iterations) in 10 consecutive generations	142
6.17	The comparison between three experiments based on the average of best cost (fitness) of populations in 10 algorithm runs (iterations) in 30 consecutive generations	143
6.18	observed map by robot	144
6.19	The average of best cost (fitness) of populations based on running the algorithm ten times (iterations) in 30 consecutive generations	145

LIST OF ABBREVIATIONS

DP-SLAM	-	Distributed Particle Simultaneous Localization and Mapping
EA	-	Evolutionary Algorithm
EKF	-	Extended Kalman Filter
ELF	-	Evolutionary Localization Filter
GA	-	Genetic Algorithm
HOM	-	Hybrid Optimization Model
KF	-	Kalman Filter
LBGAOM	-	Line-Based Genetic Algorithm Optimization Model
PF	-	Particle Filter
PSO	-	Particle Swarm Optimization
SLAM	-	Simultaneous Localization and Mapping

LIST OF APPENDICES

APPENDIX	TITLE	PAGE
A	The big image of text file created by software	162
B	Robot movement and observation output file	165
C	Some functions matlab code	195
D	Results of chapter 4	199

CHAPTER 1

INTRODUCTION

1.1 Overview

With current technological advances in the science of robotics, we have seen robots built to work autonomously on other planets, under seas and oceans and other unknown environments. Considering that the robots do not have any information about the environment, they should have the ability to build an environment map on the move and to estimate its location on that map correctly.

Mapping is to obtain a model of the robot environment, and localization is to estimate the position of robot in obtained map. For building map, we need to acknowledge the location of robot and for localization we need to map (chicken and egg problem) so solving these problems simultaneously is reasonable: simultaneous localization and mapping (SLAM) (Thrun, 2003; Bailey, *et al.*, 2006; Thrun, 2008).

Maps are often used for guidance and localization, thus for mapping, robots must be equipped with several sensors. Sensors that are commonly used for this work are sonar sensors to measure the distance, laser, radar, infrared, GPS, camera etc. (Karlsson, 2010). It should be noted that all sensors have at least a bit of measurement error and most sensors have a limited operating range. Because of these limitations, robots for building the map should move in the environment and use sophisticated

methods (Thrun, 2003; Frese, 2006). In order to perform their duties, robot need to identify their surroundings and estimate their location with high precision. This action is called simultaneous localization and mapping (SLAM). Because robot do not have any information about environment that they have entered, they begin to construct a map and to find its location in that map using of its odometer and sensor data (Durrant-Whyte, *et al.*, 2006).

It is natural that in such a case we are faced with a large search space. For exact performance of the robot and with reasonable speed, we need a solution that the robot can use to cover a large search space in shortest possible time and in the best way. Mapping has a long history. In the 80's and early 90's, mapping was mostly divided in two categories: metric and topologic. One example of the first category is occupancy grid that represents the map with a network of some full as well as empty cells. The topologic maps represent the environment with a list of important locations that are connected by some arcs. These arcs contain information about how robot navigate between different locations (Thrun, *et al.*, 1998; Thrun, 2003).

In simultaneous localization and mapping, the mobile robot captures data from the environment with own sensors, interprets this date and after building an appropriate map, determines its location in that map. Obtaining an unknown environment model must respond to three activities: mapping, localization and motion control. Mapping is shaping the collected data from robot sensors to the desired form. Localization is estimating the robot position and motion control answers this question; how to navigate the robot to favourite location or proposed path (Huang, *et al.*, 2004; Dissanayake, *et al.*, 2001).

Figure 1.1, shows the shared domain of these three activities. Active localization involves navigating the robot to special places in the map for enhancement of position estimation. Other methods use robot navigation in unknown environments and explore the environment. The central region of the figure shows an integrated strategy: SLAM and motion control.

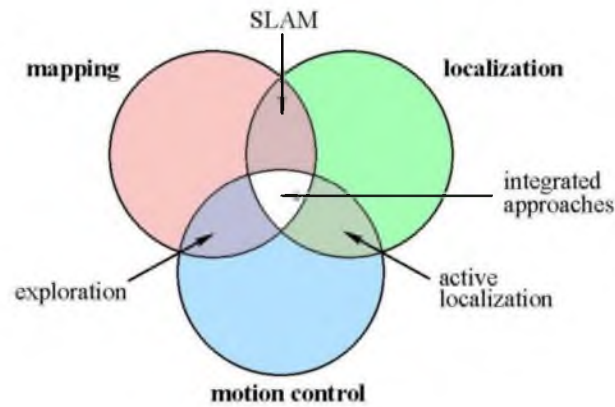


Figure 1.1 Activities that must be performed to obtain an accurate model of the environment (Makarenko, 2002).

Note that the robot should do the localization and mapping simultaneously, and should determine its path during the mapping. Typically the robot motion operation is called exploration. Although it is easy to move around a completely modelled environment, the explorer robots are face uncertainties and inefficient models. Thus each successful exploration process should have the ability to deal with unpredictable and unexpected situations, thus the issues in this case should be solved with heuristic solutions. The correct position estimation is necessary for data correct correlation. It means that we should determine if the measurements that have been done up to now match with our built map. So building maps are necessary for robot navigation in unknown environments, is needed for other activities such as localization, path planning, interaction with manipulators, and interaction with operator. As said before, this activity is called SLAM and it is a hard problem because the same, noisy sensor data must be used for both mapping and localization (Carrillo, *et al.*, 2012; Blanco, *et al.*, 2008). Sources of uncertainty in solving this problem can be divided in to two major categories:

1. The continuous uncertainties in the localization of the robot and the robot observations from environment (e.g., due to sensor noise, error in execution of commands in motors and manipulators, etc.)

2. The synthetic problem of data association (e.g., landmark extractions, feature recognition, place labelling, etc.) in which a correspondence must be detected between sensor measurements and observed features in the map.

Most of current solutions for solving the SLAM problem consider only the first category of uncertainty, and assume that the data association problem will be solved when observations are integrated into the map (e.g., it is typical to assume that all landmarks can be identified uniquely). However, this assumption is doomed to fail sooner or later for modern robots activities in unknown environments (Kang, *et al.*, 2012). In brief, failure in data association will input error in localization, which can lead to catastrophic errors in the map. Otherwise, the robot must somehow doing the search in space of possible maps. So the SLAM problem can be defined as a global optimization problem in which the objective is to search the space of possible robot maps (Duckett, 2003; Pegden, *et al.*, 1980; Kollar, *et al.*, 2008).

1.2 Problem Background

SLAM is the process by which a mobile robot can build a map of an environment and at the same time use this map to compute its own location. The past decade has seen rapid and exciting progress in solving the SLAM problem together with many compelling implementations of SLAM methods. Two famous and useful methods are extended Kalman filter (EKF) and particle filter.

The Extended Kalman Filter (EKF) is one of the first probabilistic SLAM algorithms that solve the SLAM problem using a linearized Kalman filter and this is the most important drawback of EKF. It means that the EKF should transfer all non-linear equations to a linear equation (for example with Taylor series). However, this method uses only uni-modal Gaussians to model non-Gaussian probability density function. Another disadvantage of EKF is $O(N^3)$ matrix inversion required for its calculations (Castellanos, *et al.*, 2004; Paz, *et al.*, 2006; Hui-Ping, *et al.*, 2009).

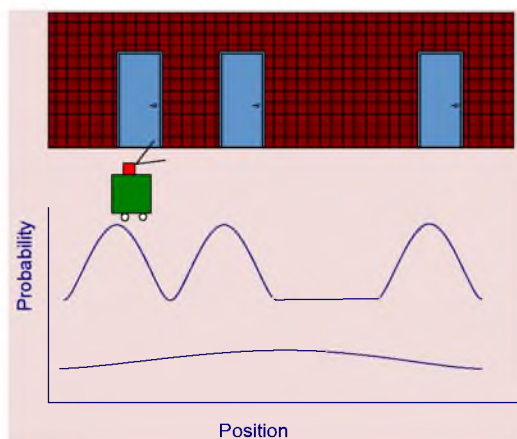


Figure 1.2 Model extraction by robot based on features (doors) and transfer to uni-modal Gaussian diagram for use in EKF.

Another method for solving the SLAM problem is particle filter. Particle filter represents probability distribution as a set of discrete particles which occupy the state space. This method can represent multi-modal distributions.

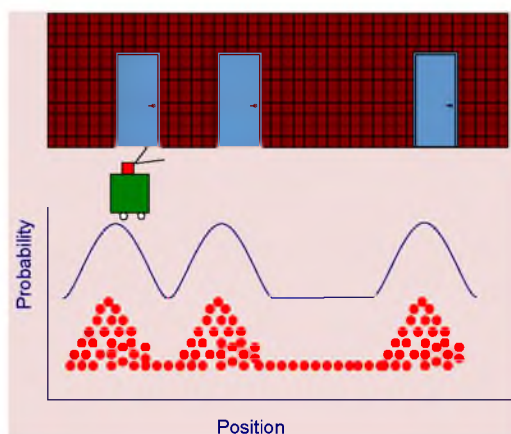


Figure 1.3 Model extraction by robot based on features (doors) and showing the number of particles in high probability places

Two problems with this method are that the number of particles grows exponentially with the dimensionality of the state space and high memory complexity (Thrun, 2002; Törnqvist, *et al.*, 2009; Gustafsson, 2010).

One of the major approaches to solve the SLAM problem is the approach based on evolutionary algorithm like Genetic Algorithm (GA). The proposed optimization model in this study is in the same category. GA is a class of search algorithm that inspired by the style evolution of living beings have arisen. The main advantage of the evolutionary algorithm is that these algorithms can be used to search space which is too large to be used with high convergence. A number of solutions are using the GA for solving the SLAM problem like Duckett solution, Begum solution or Shiry solution. Each of these solutions has some problems and drawbacks that are explained by detail in Chapter 2. Generally the main problem of solutions based on GA is connected to high computational complexity and time complexity (Begum, *et al.*, 2006; Begum, *et al.*, 2007). GA has three kind of operators for keeping the diversity and variety which are selection, mutation and crossover. Each of these operators also have some kind or model of implementations like uniform and two point model for crossover operation or Roulette wheel and Q-tournament model for selection operation. Choosing the appreciate model for each operators is very effective in time and computational complexity based on desired optimization problem. So for increase the speed of GA and decrease the time and computational complexity of that, the new ideas and contributions should be applied in these operators or have contribution in procedure of GA based on fitness function and other parameters of GA. The most important operator is mutation because if the pattern of response doesn't exists in initial population, the GA couldn't coverage to optimal answer. In original mutation selection of a gen for mutation is completely random and this is one on the problems of mutation because there is not any control in selection of gen and it is completely random. So because this operation is not targeted, the searching time will be increased and the speed of GA will be decreased consequently (Duckett, 2003).

1.3 Problem Statement

As discussed in the previous section, two methods for solving the SLAM problem, EKF and particle filter, have faced some drawbacks. In EKF, the main problem connected to this method is working solely with linear systems and uni-modal

Gaussians equations. In addition, for solving the aforementioned problem, EKF needs to convert non-linear equations to linear equations using for example Taylor series which causes additional errors to the system. In the particle filter, the main problem is the high memory and computation time required when increasing the number of particles. Although genetic algorithm demonstrates very good performance with large search spaces, it has some weaknesses and drawbacks such as computational and time complexity which result in low speed. There are two main causes of low speed in GA: the first is untargeted search involving replacement or adding a fixed value for mutation operation and the second is large search space. In brief, the problem can be stated as below:

“Low speed and accuracy in solutions based on Genetic Algorithm for solving the SLAM problem in mobile robots”

For study on solving the SLAM problem in mobile robots, a map representation as experimental setup and test bed is needed as preprocessing. Thus a new representation model based on Genetic Algorithm should first be designed and developed for implementation of new models and then comparison of the obtained results. For this propose, in each step the best values for GA parameters should be found (parameter tuning) for better comparison of original GA and hybrid optimization model.

The following research questions will be answered in this research:

- I. How can a new representation model based on occupancy grid be modified for represent the robot and its environment?
- II. How can the genetic algorithm be hybrid with particle filter by increasing the accuracy perspective?
- III. How can reduce the search space in SLAM problem for increase the speed?

1.4 Purpose of Study

To propose new optimization model in increase the speed and accuracy of SLAM problem using new hybrid of particle filter and GA algorithm for avoidance of random selection in mutation step.

To increase the speed of optimization model with a line based GA and a new representation of occupancy grid for decrease the search space.

1.5 Objectives

Objectives of this research are as follows:

1. To propose and design simulation model of new representation model of occupancy grid based on Genetic algorithm.
2. To develop a hybrid optimization model (HOM) of GA and Particle filter on the proposed representation model.
3. To develop a line based genetic algorithm optimization model (LBGAOM) on the proposed representation model.

1.6 Research Scope

In this study, the scope of the optimization model is mainly based on the following items:

1. The proposed algorithm is based on raw data of robot odometer movement and received data from its laser sensors in a static environment which obstacles are static.
2. In the new representation model of occupancy grid, the map representation performance will be checked with presented fitness functions.
3. The hybrid optimization model (HOB) target is to investigate the increased convergence and speed.
4. The proposed LBGA optimization model is for working in indoor environments only.
5. The new optimization model will be implemented on some simulated maps and the accuracy of model will be evaluated with presented fitness functions.
6. MATLAB software and some related software are used for simulation.

1.7 Significance of Research

The significance of this project is to propose an enhanced optimization model for solving the simultaneous localization and mapping (SLAM) problem by covering the weaknesses of representation of occupancy grid. Another significance of this project is that the solutions based on Kalman filter are highly dependent on the motion model while in this study the presented optimization model is completely independent from motion model. Thus the benefit of this research is the increase in accuracy of SLAM algorithm and improved performance of occupancy grid for map representation. In detail, some significant algorithms are listed below:

1. Two new representation model of occupancy grid for using solving the SLAM problem are presented (Layer 1 and Layer 2) and two new fitness functions are designed and used for each model also.

2. An hybrid optimization model (HOM) based on genetic algorithm and particle filter are presented and new chromosome model and desired fitness function for use in model are designed and presented also.
3. A Line-based genetic algorithm optimization model (LBGAOM) for reduce the search space and increase the speed is presented and new chromosome model and desired fitness function for use in model are designed and presented also.

1.8 Thesis Overview

This research consists of seven chapters. In Chapter 1 an introduction, problem background, problem statement, Purpose of Study, objectives, scope and significant of this research are presented.

In Chapter 2, some basic background about SLAM is presented then some mapping models and localization algorithms are presented. The effective parameters and existing methods and tools for solving the SLAM problem are introduced and compared. Finally the existing solutions based on each methods or hybrid of some methods are presented and compared.

In Chapter 3 methodology which is used in this research discussed.

In Chapter 4 a development of a new representation of occupancy grid based on GA and tune the parameters for comparison in other Chapters, is presented. In this chapter a new representation model with a new fitness function is presented which has best performance in increase the accuracy.

The Chapter 5 is about develop a hybrid model of genetic algorithm and particle filter for solving the problem of mutation operation in genetic algorithm with particle

filter concept and avoidance of random selection and adding a fixed value to chromosome.

In Chapter 6 a line base genetic algorithm optimization model is develop for decrease the search space and increase the speed consequently. Finally, Chapter 7 is contained the conclusion and future work of this research

REFERENCES

- Angeline, P. J., Saunders, G. M. and Pollack, J. B. (1994). An evolutionary algorithm that constructs recurrent neural networks. *IEEE Transactions on Neural Networks*, 5(1), 54-65.
- Back, T. (1994). Selective pressure in evolutionary algorithms: A characterization of selection mechanisms. *Proceedings of the First IEEE Conference on World Congress on Computational Intelligence*, 57-62.
- Bäck, T. (1995). Generalized Convergence Models for Tournament-and (μ , λ)-Selection.
- Back, T., Fogel, D. B. and Michalewicz, Z. (1997). *Handbook of evolutionary computation*: IOP Publishing Ltd.
- Back, T., Fogel, D. B. and Michalewicz, Z. (2000). *Evolutionary computation 1: Basic algorithms and operators* (Vol. 1): CRC Press.
- Bailey, T. and Durrant-Whyte, H. (2006). Simultaneous localization and mapping (SLAM): Part II. *IEEE Robotics & Automation Magazine*, 13(3), 108-117.
- Baker, J. E. (1987). Reducing bias and inefficiency in the selection algorithm. *Proceedings of the second international conference on genetic algorithms*, 14-21.
- Bayindir, L. and Sahin, E. (2007). A review of studies in swarm robotics. *Turkish Journal of Electrical Engineering & Computer Sciences*, 15(2), 115-147.
- Beasley, J. E. and Chu, P. C. (1996). A genetic algorithm for the set covering problem. *European Journal of Operational Research*, 94(2), 392-404.
- Begum, M., Mann, G. K. and Cosine, R. (2006). An evolutionary SLAM algorithm for mobile robots. *IEEE/RSJ International Conference on Intelligent Robots and Systems*, 4066-4071.

- Begum, M., Mann, G. K. and Gosine, R. G. (2007). An evolutionary algorithm for simultaneous localization and mapping (SLAM) of mobile robots. *Advanced Robotics*, 21(9), 1031-1050.
- Bibby, C. and Reid, I. (2007). Simultaneous localisation and mapping in dynamic environments (SLAMIDE) with reversible data association. *Proceedings of Robotics: Science and Systems*.
- Blanco, J.-L., Fernandez-Madrigal, J.-A. and González, J. (2008). A Novel Measure of Uncertainty for Mobile Robot SLAM with Rao—Blackwellized Particle Filters. *The International Journal of Robotics Research*, 27(1), 73-89.
- Blickle, T. and Thiele, L. (1995). A comparison of selection schemes used in genetic algorithms: TIK-Report.
- Blickle, T. and Thiele, L. (1996). A comparison of selection schemes used in evolutionary algorithms. *Evolutionary Computation*, 4(4), 361-394.
- Boada, B., Blanco, D., Castejón, C. and Moreno, L. (2003). A genetic solution for the slam problem. *Proceedings of the 11th International Conference on Advanced Robotics (ICAR'03)*, Coimbra, Portugal, 270-275
- Boada, B. L., Blanco, D. and Moreno, L. (2002). Localization and modelling approach using topo-geometric maps. *Proceedings of the IEEE/RSJ International Conference on Intelligent Robots and Systems*.484-489.
- Bosse, M., Newman, P., Leonard, J., Soika, M., Feiten, W. and Teller, S. (2003). An Atlas framework for scalable mapping. *ICRA'03. Proceedings of the IEEE International Conference on Robotics and Automation, 2003*, 1899-1906.
- Branke, J. (1998). Creating robust solutions by means of evolutionary algorithms. *Proceedings of the Parallel Problem Solving from Nature—PPSN V*, 119-128.
- Carrillo, H., Reid, I. and Castellanos, J. A. (2012). On the comparison of uncertainty criteria for active SLAM. *Proceedings of the IEEE International Conference on Robotics and Automation (ICRA)*, 2080-2087.
- Castellanos, J. A., Neira, J. and Tardós, J. D. (2004). Limits to the consistency of EKF-based SLAM 1. *5th Symposium On Intelligent Autonomous Vehicles*, Lisboa, Portugal, 7-13.
- Chatterjee, A., Rakshit, A. and Singh, N. N. (2013). Simultaneous Localization and Mapping (SLAM) in Mobile Robots. *Vision Based Autonomous Robot Navigation*, 167-206.

- CHEN, B., CAI, Z. and Yuan, C. (2009). Mobile robot SLAM method based on particle swarm optimization. *Robot*, 31 (6), 513–517
- Choset, H. and Nagatani, K. (2001). Topological simultaneous localization and mapping (SLAM): toward exact localization without explicit localization. *IEEE Transactions on Robotics and Automation*, 17(2), 125-137.
- Coello Coello, C. A. (2012). Constraint-handling techniques used with evolutionary algorithms. *Proceedings of the fourteenth international conference on Genetic and evolutionary computation conference companion*, 849-872.
- Davis, L. (1991). *Handbook of genetic algorithms* (Vol. 115): Van Nostrand Reinhold New York.
- Deb, K. and Agrawal, R. B. (1995). Simulated binary crossover for continuous search space. *Complex systems*, 9(2), 115-148.
- Deb, K., Pratap, A., Agarwal, S. and Meyarivan, T. (2002). A fast and elitist multiobjective genetic algorithm: NSGA-II. *IEEE Transactions on Evolutionary Computation*, 6(2), 182-197.
- Diosi, A. and Kleeman, L. (2004). Advanced sonar and laser range finder fusion for simultaneous localization and mapping. *Proceedings of the IEEE/RSJ International Conference on Intelligent Robots and Systems. (IROS 2004)*, 1854-1859.
- Dissanayake, M. G., Newman, P., Clark, S., Durrant-Whyte, H. F. and Csorba, M. (2001). A solution to the simultaneous localization and map building (SLAM) problem. *IEEE Transactions on Robotics and Automation*, 17(3), 229-241.
- Duckett, T. (2003). A genetic algorithm for simultaneous localization and mapping. *Proceedings of the IEEE International Conference on Robotics and Automation*, 434-439.
- Dudek, G., Jenkin, M., Milios, E. and Wilkes, D. (1993). A taxonomy for swarm robots. *Proceedings of the IEEE/RSJ International Conference on Intelligent Robots and Systems' 93, IROS'93*, 441-447.
- Durrant-Whyte, H. and Bailey, T. (2006). Simultaneous localization and mapping: part I. *IEEE Robotics & Automation Magazine*, 13(2), 99-110.
- Durrant-Whyte, H., Majumder, S., Thrun, S., de Battista, M. and Scheduling, S. (2003). A bayesian algorithm for simultaneous localisation and map building. In *Springer Robotics Research journal*, 49-60.

- Eberhart, R. C. and Shi, Y. (2001). Particle swarm optimization: developments, applications and resources. *Proceedings of the Congress on the 2001 Evolutionary Computation*, 81-86.
- Eiben, Á. E., Hinterding, R. and Michalewicz, Z. (1999). Parameter control in evolutionary algorithms. *IEEE Transactions on Evolutionary Computation*, 3(2), 124-141.
- Elfes, A. (1989). Using occupancy grids for mobile robot perception and navigation. *Computer*, 22(6), 46-57.
- Eliazar, A. and Parr, R. (2003). DP-SLAM: Fast, robust simultaneous localization and mapping without predetermined landmarks. *Proceedings of the International Joint Conference on Artificial Intelligence*, 1135-1142.
- Eliazar, A. I. and Parr, R. (2004). DP-SLAM 2.0. *Proceedings of the IEEE International Conference on Robotics and Automation ICRA'04*, 1314-1320.
- Engelbrecht, A. P. (2007). *Computational intelligence: an introduction* (Book) John Wiley & Sons publication, London, England.
- Feng, D. J., Wijesoma, S. and Shacklock, A. P. (2006). Genetic algorithmic filter approach to mobile robot simultaneous localization and mapping. *Proceedings of the 9th International Conference on Control, Automation, Robotics and Vision, 2006. ICARCV'06, Singapore*, 1-6.
- Fogarty, T. C. (1989). Varying the probability of mutation in the genetic algorithm. *Proceedings of the third international conference on Genetic algorithms*, 104-109.
- Frese, U. (2006). A discussion of simultaneous localization and mapping. *Autonomous Robots*, 20(1), 25-42.
- Frese, U. and Hirzinger, G. (2001). Simultaneous localization and mapping-a discussion. *Proceedings of the IJCAI Workshop on Reasoning with Uncertainty in Robotics*, 17-26.
- Gen, M. and Cheng, R. (2000). *Genetic algorithms and engineering optimization* (Vol. 7): John Wiley & Sons.
- Goldberg, D. E. (2006). *Genetic algorithms*: Pearson Education India.
- Grefenstette, J. J. (1986). Optimization of control parameters for genetic algorithms. *Systems, IEEE Transactions on Man and Cybernetics*, 16(1), 122-128.

- Grefenstette, J. J. (2013). Genetic Algorithms and Their Applications. *Proceedings of the Second International Conference on Genetic Algorithms*, Psychology Press.
- Gustafsson, F. (2010). Particle filter theory and practice with positioning applications. *IEEE Aerospace and Electronic Systems Magazine*, 25(7), 53-82.
- Havangi, R., Nekoui, M., Teshnehlal, M. and Taghirad, H. (2013). A SLAM based on auxiliary marginalised particle filter and differential evolution. *International Journal of Systems Science*, (ahead-of-print), 1-14.
- Higuchi, T. (1997). Monte Carlo filter using the genetic algorithm operators. *Journal of Statistical Computation and Simulation*, 59(1), 1-23.
- Holmes, S. A., Klein, G. and Murray, D. W. (2009). An $O(N^2)$ Square Root Unscented Kalman Filter for Visual Simultaneous Localization and Mapping. *IEEE Transactions on Pattern Analysis and Machine Intelligence*, 31(7), 1251-1263.
- Houck, C. R., Joines, J. and Kay, M. G. (1995). A genetic algorithm for function optimization: a Matlab implementation, (Book) North Carolina State University, USA, *NCSU-IE TR*, 95(09).
- Huang, S. and Dissanayake, G. (2007). Convergence and consistency analysis for extended Kalman filter based SLAM. *IEEE Transactions on Robotics*, 23(5), 1036-1049.
- Huang, S., Wang, Z. and Dissanayake, G. (2004). Time optimal robot motion control in simultaneous localization and map building (SLAM) problem. *Proceedings of the IEEE/RSJ International Conference on Intelligent Robots and Systems, 2004 (IROS 2004)*. 3110-3115.
- Hui-Ping, L., De-Min, X., ZHANG, F.-B. and Yao, Y. (2009). Consistency analysis of EKF-based SLAM by measurement noise and observation times. *Acta Automatica Sinica*, 35(9), 1177-1184.
- Jetto, L., Longhi, S. and Venturini, G. (1999). Development and experimental validation of an adaptive extended Kalman filter for the localization of mobile robots. *IEEE Transactions on Robotics and Automation*, 15(2), 219-229.

- Jin, Y., Olhofer, M. and Sendhoff, B. (2002). A framework for evolutionary optimization with approximate fitness functions. *IEEE Transactions on Evolutionary Computation*, 6(5), 481-494.
- Kang, J.-G., Kim, S., An, S.-Y. and Oh, S.-Y. (2012). A new approach to simultaneous localization and map building with implicit model learning using neuro evolutionary optimization. *Applied Intelligence*, 36(1), 242-269.
- Karlsson, L. N. (2010). Robust sensor fusion for mapping and localization in a simultaneous localization and mapping (SLAM) system: Google Patents.
- Karlsson, N., Di Bernardo, E., Ostrowski, J., Goncalves, L., Pirjanian, P. and Munich, M. E. (2005). The vSLAM algorithm for robust localization and mapping. *Proceedings of the IEEE International Conference on the Robotics and Automation ICRA 2005*, 24-29.
- Kennedy, J. and Eberhart, R. (1995). Particle swarm optimization. *Proceedings of the IEEE International Conference on Neural Networks*, 1942-1948.
- Kollar, T. and Roy, N. (2008). Efficient Optimization of Information-Theoretic Exploration in SLAM. *Proceedings of the AAAI*, 1369-1375.
- Konolige, K. (1997). Improved occupancy grids for map building. *Autonomous Robots*, 4(4), 351-367.
- Kwok, N., Fang, G. and Zhou, W. (2005). Evolutionary particle filter: re-sampling from the genetic algorithm perspective. *Proceedings of the IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS 2005)*, 2935-2940.
- Kwok, N. and Rad, A. (2006). A modified particle filter for simultaneous localization and mapping. *Journal of Intelligent and Robotic Systems*, 46(4), 365-382.
- Leonard, J., Durrant-Whyte, H. and Cox, I. J. (1990). Dynamic map building for autonomous mobile robot. *Proceedings of the IEEE International Workshop on Intelligent Robots and Systems. 'Towards a New Frontier of Applications' IROS'90*, 89-96.
- Liu, Z., Chen, D. and von Wichert, G. (2012). 2D Semantic Mapping on Occupancy Grids. *Proceedings of the 7th German Conference on Robotics, Proceedings of ROBOTIK 2012*, 1-6.
- Makarenko, A. A., Williams, S. B., Bourgault, F. and Durrant-Whyte, H. F. (2002). An experiment in integrated exploration. *Proceedings of the IEEE/RSJ International Conference on Intelligent Robots and Systems*, 534-539.

- Montemerlo, M., Thrun, S., Koller, D. and Wegbreit, B. (2002). FastSLAM: A factored solution to the simultaneous localization and mapping problem. *Proceedings of the National conference on Artificial Intelligence*, 593-598.
- Montemerlo, M., Thrun, S., Koller, D. and Wegbreit, B. (2003). FastSLAM 2.0: An improved particle filtering algorithm for simultaneous localization and mapping that provably converges. *Proceedings of the International Joint Conference on Artificial Intelligence*, 1151-1156.
- Montemerlo, M., Thrun, S. and Siciliano, B. (2007). *FastSLAM: A scalable method for the simultaneous localization and mapping problem in robotic* (Book), Springer Verlag Berlin Germany, (Vol. 27).
- Moreno, L., Garrido, S., Blanco, D. and Muñoz, M. L. (2009). Differential evolution solution to the SLAM problem. *Robotics and Autonomous Systems*, 57(4), 441-450.
- Moreno, L., Garrido, S. and Muñoz, M. L. (2006). Evolutionary filter for robust mobile robot global localization. *Robotics and Autonomous Systems*, 54(7), 590-600.
- Mozos, O. M., Stachniss, C., Rottmann, A. and Burgard, W. (2007). Using adaboost for place labeling and topological map building *Robotics Research*, Springer Book, Volume 28, pp 453-472
- Nagla, K., Uddin, M. and Singh, D. (2012). Improved occupancy grid mapping in specular environment. *Robotics and Autonomous Systems*.
- Newman, P. (1999). On the structure and solution of the simultaneous localisation and map building problem. Doctoral diss., University of Sydney.
- Omranpour, H. and Shiry, S. (2009). A Heuristic Algorithm for Simultaneous Localization and Mapping in Mobile Robots. *Proceedings of the 2009 Iran Open Symposium*, Tehran, 4-9.
- Omranpour, H. and Shiry, S. (2012). Reduced Search Space Algorithm for Simultaneous Localization and Mapping in Mobile Robots. *IAES International Journal of Robotics and Automation (IJRA)*, 1(1), 49-63.
- Paz, L. M. and Neira, J. (2006). Optimal local map size for EKF-based SLAM. *2006 IEEE/RSJ International Conference on Proceedings of the 2006 Intelligent Robots and Systems*, 5019-5025.
- Pedrycz, W. (1997). *Computational intelligence: an introduction*. CRC Press.

- Pegden, C. D. and Gately, M. P. (1980). A decision-optimization module for SLAM. *Simulation*, 34(1), 18-25.
- Pronobis, A., Jensfelt, P., Sjöö, K., Zender, H., Kruijff, G.-J. M., Mozos, O. M., *et al.* (2010). Semantic modelling of space. *Cognitive Systems*, 165-221.
- Ranganathan, A. and Dellaert, F. (2007). Semantic modeling of places using objects. *Proceedings of the Robotics: Science and Systems Conference*, 27-30.
- Reif, K. and Unbehauen, R. (1999). The extended Kalman filter as an exponential observer for nonlinear systems. *IEEE Transactions on Signal Processing*, 47(8), 2324-2328.
- Remolina, E. and Kuipers, B. (2004). Towards a general theory of topological maps. *Artificial Intelligence*, 152(1), 47-104.
- Rudnick, E. M., Patel, J. H., Greenstein, G. S. and Niermann, T. M. (1994). Sequential circuit test generation in a genetic algorithm framework. *Proceedings of the 31st annual Design Automation Conference*, 698-704.
- Rudol, E. (1960). Kálmán. A new approach to linear filtering and prediction problem. *Journal of Basic Engineering*, 82(1), 35-45.
- Rudolph, G. (1994). Convergence analysis of canonical genetic algorithms. *IEEE Transactions on Neural Networks*, 5(1), 96-101.
- Sasaki, H., Kubota, N. and Taniguchi, K. (2008). Evolutionary computation for simultaneous localization and mapping based on topological map of a mobile robot. *Intelligent Robotics and Applications*, 883-891.
- Sastry, K., Goldberg, D. and Kendall, G. (2005). Genetic algorithms, Search methodologies Book, Springer, USA, (pp. 97-125)
- Schaffer, J. D. and Morishima, A. (1987). An adaptive crossover distribution mechanism for genetic algorithms. *Proceedings of the of the Second International Conference on Genetic Algorithms and their Applications*, 36-40.
- Schmitt, L. M. (2001). Theory of genetic algorithms. *Theoretical Computer Science*, 259(1), 1-61.
- Se, S., Lowe, D. and Little, J. (2002). Mobile robot localization and mapping with uncertainty using scale-invariant visual landmarks. *The international Journal of robotics Research*, 21(8), 735-758.

- Sim, R., Elinas, P., Griffin, M. and Little, J. J. (2005). Vision-based SLAM using the Rao-Blackwellised particle filter. *Proceedings of the IJCAI Workshop on Reasoning with Uncertainty in Robotics*, 9-16.
- Simhon, S. and Dudek, G. (1998). A global topological map formed by local metric maps. *Proceedings of the IEEE/RSJ International Conference on Intelligent Robots and Systems, Victoria, BC, Canada*, (3), 1708-1714.
- Spears, W. M. (1995). Adapting Crossover in Evolutionary Algorithms. *Proceedings of the Evolutionary programming*, 367-384.
- Spero, D. J. and Jarvis, R. A. (2007). A review of robotic SLAM.
- Srinivas, M. and Patnaik, L. M. (1994). Adaptive probabilities of crossover and mutation in genetic algorithms. *IEEE Transactions on Systems, Man and Cybernetics*, 24(4), 656-667.
- Stachniss, C., Hahnel, D. and Burgard, W. (2004). Exploration with active loop-closing for FastSLAM. *Proceedings of the IEEE/RSJ International Conference on Intelligent Robots and Systems(IROS 2004)*, 1505-1510.
- Syswerda, G. (1989). Uniform crossover in genetic algorithms.
- Thrun, S. (2001). A probabilistic on-line mapping algorithm for teams of mobile robots. *The International Journal of Robotics Research*, 20(5), 335-363.
- Thrun, S. (2002). Particle filters in robotics. *Proceedings of the Eighteenth conference on Uncertainty in artificial intelligence*, 511-518.
- Thrun, S. (2003). Robotic mapping: A survey. *Exploring artificial intelligence in the new millennium*, 1, 1-35.
- Thrun, S. (2008). Simultaneous localization and mapping. *Robotics and cognitive approaches to spatial mapping* (pp. 13-41): Springer.
- Thrun, S. (2012). Particle Filters in Robotics (Invited Talk). *arXiv preprint arXiv:1301.0607*.
- Thrun, S. and Bücken, A. (1996). Learning Maps for Indoor Mobile Robot Navigation, Technical report, Carnegie-Mellon University, school of computer science, Pittsburgh, USA.
- Thrun, S., Bücken, A., Burgard, W., Fox, D., Fröhlinghaus, T., Hennig, D., *et al.* (1998). Map learning and high-speed navigation in RHINO. *AI-based Mobile Robots: Case studies of successful robot systems*. MIT Press, Cambridge, MA.

- Thrun, S., Burgard, W. and Fox, D. (2005). *Probabilistic robotics* (Vol. 1): MIT press Cambridge.
- Thrun, S., Fox, D. and Burgard, W. (1998). Probabilistic mapping of an environment by a mobile robot. *Proceedings of the IEEE International Conference on Robotics and Automation*, 1546-1551.
- Thrun, S., Fox, D., Burgard, W. and Dellaert, F. (2001). Robust Monte Carlo localization for mobile robots. *Artificial intelligence*, 128(1), 99-141.
- Thrun, S., Montemerlo, M., Koller, D., Wegbreit, B., Nieto, J. and Nebot, E. (2004). Fastslam: An efficient solution to the simultaneous localization and mapping problem with unknown data association. *Journal of Machine Learning Research*, 4(3), 380-407.
- Todor, B. and Darabos, D. (2005). Simultaneous localization and mapping with particle swarm localization. *Proceedings of the Intelligent Data Acquisition and Advanced Computing Systems: Technology and Applications (IDAACS 2005)*, 216-221.
- Tomatis, N., Nourbakhsh, I. and Siegwart, R. (2001). Simultaneous localization and map building: A global topological model with local metric maps. *Proceedings of the IEEE/RSJ International Conference on Intelligent Robots and Systems*, 421-426.
- Tomatis, N., Nourbakhsh, I. and Siegwart, R. (2003). Hybrid simultaneous localization and map building: a natural integration of topological and metric. *Robotics and Autonomous systems*, 44(1), 3-14.
- Törnqvist, D., Schön, T. B., Karlsson, R. and Gustafsson, F. (2009). Particle filter SLAM with high dimensional vehicle model. *Journal of Intelligent and Robotic Systems*, 55(4-5), 249-266.
- Vasudevan, S., Gächter, S., Nguyen, V. and Siegwart, R. (2007). Cognitive maps for mobile robots—an object based approach. *Robotics and Autonomous Systems*, 55(5), 359-371.
- Viswanathan, P., Meger, D., Southey, T., Little, J. J. and Mackworth, A. K. (2009). Automated spatial-semantic modeling with applications to place labeling and informed search. *Proceedings of the Canadian Conference on Computer and Robot Vision, 2009. CRV'09*. 284-291.
- Vose, M. D. (1999). *The simple genetic algorithm: foundations and theory*, (Book) published by MIT press, (Vol. 12).

- Wang, C.-C. and Thorpe, C. (2002). Simultaneous localization and mapping with detection and tracking of moving objects. *Proceedings of the IEEE International Conference on Robotics and Automation (ICRA'02)*, 2918-2924.
- Weile, D. S. and Michielssen, E. (1997). Genetic algorithm optimization applied to electromagnetics: A review. *IEEE Transactions on Antennas and Propagation*, 45(3), 343-353.
- Welch, G. and Bishop, G. (1995). An introduction to the Kalman filter.
- Whitley, L. D. (1989). The GENITOR Algorithm and Selection Pressure: Why Rank-Based Allocation of Reproductive Trials is Best. *Proceedings of the ICGA*, 116-123.
- Wright, A. H. (1991). Genetic algorithms for real parameter optimization. *Foundations of genetic algorithms*, 1, 205-218.
- Yamauchi, B., Langley, P., Schultz, A. C., Grefenstette, J. and Adams, W. (1998). MAGELLAN: An Integrated Adaptive Architecture for Mobile Robotics: DTIC Document.
- Zender, H., Martínez Mozos, O., Jensfelt, P., Kruijff, G.-J. and Burgard, W. (2008). Conceptual spatial representations for indoor mobile robots. *Robotics and Autonomous Systems*, 56(6), 493-502.
- Zhang, B. T. and Kim, J. J. (2000). Comparison of selection methods for evolutionary optimization. *Evolutionary Optimization*, 2(1), 55-70.