



COPY-MOVE FORGERY DETECTION: A SURVEY ON TIME COMPLEXITY ISSUES AND SOLUTIONS

^{1,a} SITI FADZLUN MD SALLEH, ² MOHD FOAD ROHANI, ³ MOHD AIZAINI MAAROF

^{1,2,3} Information and Assurance Research Group, Computer Science Department, Faculty of Computing, Universiti Teknologi Malaysia, UTM Skudai, 81310 Johor, Malaysia

^a Information Security Department, Faculty of Computer Science & Information Technology, Universiti Tun Hussein Onn Malaysia (UTHM), Johor, Malaysia

E-mail: ¹ fadzlun.salleh@gmail.com, ² foad@utm.my, ³ aizaini@utm.my

ABSTRACT

As the image processing especially image editing software evolve, more image manipulations were possible to be done, thus authentication of image become a very crucial task. Copy-move forgery detection (CMFD), a popular research focus in digital image forensic, is used to authenticate an image by detecting malicious copy-move tampering in an image. Copy-move forgery occurs when a region in an image is copied and paste into the same image. There were many survey and review papers discussed about CMFD robustness and accuracy yet less attention was given to performance and time complexity. In this paper, we attempts to highlight the key factors contribute to the time complexity issue. Before that, the CMFD processes were first explained for better understanding. The trends of tackling those issues are then explored. Finally, numbers of proposed solutions will be outlined to conclude this paper.

Keywords: *Copy-Move Forgery, Digital Image Forensic, Duplicated Region Detection, Block Matching, Time Complexity.*

1. INTRODUCTION

Copy-move forgery detection (CMFD) has become a popular research topic in digital image forensic. CMFD techniques are used to authenticate an image by detecting and locating malicious copy-move tampering, if exist in an image. Copy-move forgery occurs when a region in an image is copied and paste into the same image. Two major ways an image could be changed in this forgery are concealing an object in an image or duplicating object from an image [1, 2]. The fact that the forged region comes from the same image plus additional retouching done before being pasted makes the detection a very challenging task. Existence of some geometrical transformation such as rotation and scaling with post-processing alteration such as blurring, jpeg compression and noise adding in the duplicated region increase the difficulty of forgery detection.

Image with some post-processing attacks may cause many methods to reduce in detection rate, but not fail completely. However, geometric transforms such as scaling, translation or rotation can cause total failure to detect any forgery [3]. Robust copy-move forgery detection, which

invariant to geometric transformation and combined manipulations is highly needed. Unfortunately, since research progresses towards developing more robust methods of CMFD, the algorithms being proposed have higher and higher complexity. Complex computation adopted to get a high accurate and robust feature vector may result in high accurate detection, but it leads to high computation and detection time.

In view of that, this paper will highlight the reasons to this time complexity issue, previous solutions and provide general proposal to overcome it. We hope that this paper will help researcher in producing a fast and accurate CMFD method. As we live in a fast-paced world today, fast and accurate CMFD method which provides a near real-time result is highly needed. The rest of this paper is organized as follows. Section 1.1 highlights few scenarios in copy-move forgery, followed by brief explanation on copy-move forgery detection process in Section 1.2. Time complexity issue is elaborated in Section 2 while Section 3 discuss on an extensive survey of previous solutions. Discussion and some future works are proposed in Section 4, and finally Section 5 concludes this paper.

1.1 Scenario in Copy-Move Forgery

Copy-move forgery was initially highlighted by Fridrich in 2003 [4]. In their paper, copy-move forgery was described as just a plain copy-move forgery, where it is only involve translation or copied of a region in an image pasted to another region in the same image. The possibility that some signal processing attacks such as JPEG compression, noise or blurring adopted in the forged image were also considered in detection process.

As the image processing especially image editing software evolve, more manipulations were possible to be done. Forgery is no longer limited to plain copy and then move, instead involve geometrical transform such as rotation, scaling, flipping, affine transform and etc. before region were pasted to another region in an image. These manipulations were done to adapt and looks coherent with the remaining of the image. Not only that, these manipulations was combined with signal processing attacks or named as post-processing attacks to smoothen any noticeable traces and to make it difficult for forgery to be detected. More post-processing attacks also were taken into consideration such as bright adjustment, color enhancement and in-painting attacks. Earlier researches which handle plain copy-move with JPEG compression, noise or blurring were extended to be able to handle those complicated manipulations.

Another scenario in CMFD that should be considered is categories of an image. Images and duplicated region may come in small, medium or large in size. Content of image also impacts the detection rate. For example, keypoint-based methods are known as scale invariant and robust to compression and rotation, unfortunately it face with low detection accuracy when involves with featureless or homogeneous region such as walls and grassland, repetitive objects such as building blocks and small structure of duplicated region.

Copy-move forgery or region duplication could also be done in multiple copies within an image. As such, CMFD must be developed with a deep consideration so it would be able to handle the cases which involves not only plain copy-move, but also with the existence of geometrical transform, post-processing attack, the combination of all the above and with possible multiple copied regions!

The best or desired copy-move forgery detection is a system which robust enough to handle all the above mentioned scenarios. Unfortunately, with the long list of system's requirements to be met, it has created another issue, which is time complexity.

1.2 Copy-Move Forgery Detection Process

Before the issues exist in CMFD are elaborated, it is important to understand the CMFD processes. There are two options in detecting copy-move forgeries; 1) block-based method 2) keypoint-based method. The general workflow of copy-move forgery detection [5] is illustrated in figure 1. It consists of several phases which are pre-processing, blocks tiling or keypoint scanning, feature extraction, matching and verification.

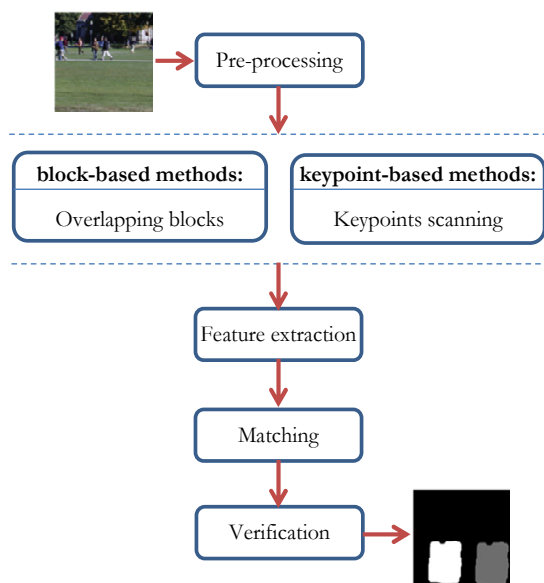


Figure 1: General Copy-Move Forgery Detection Process

Detection process starts once image which suspected to be containing copy-move forgery is input to the system. Image then optionally pre-processed to reduce feature dimension, e.g. by converting color image to grayscale, or applying Gaussian pyramid decomposition, Discrete Wavelet Transform (DWT) or Principal Component Analysis (PCA).

After that, under block-based method, image is divided into several overlapping blocks for segmentation of image region. For keypoint-based method, the whole image is scanned through to find high-entropy image regions (i.e., the “keypoints”)

without dividing it into blocks. Numbers of keypoints extracted are depended on the feature descriptor used. This brings to the next process which is feature extraction process.

In feature extraction process, raw features of each blocks or keypoints are computed to bring significant value or characteristic using feature descriptor. A good feature extractor or feature descriptor should be able to extract the best or robust features for forgery detection. Computed features are then stored in respective feature vector for matching purpose.

In matching process, the arrays of feature set will be compared between each other to find similar features. Two feature sets with high similarity is a sign for a duplicated region. The process did not stop here since usually upon completion of block matching, a lot of similar blocks can be seen exist in the image. This is where verification process took place.

Verification is a filtering process, proposed to reduce the possibility of false matches in the detection image. The final output of this process is the detection map which shows duplicated image region in the image.

CMFD pipeline seem a very smooth processes, however, in actual situation it is very difficult to determine the real duplicated region in the image. To date, CMFD still incapable of accurately detect duplicated region when exist geometric transformation and post-processing manipulation. Accuracy of detection rate may reduce for image with some post-processing attacks, but not fail completely. However, duplicated region which involves geometric transforms such as scaling, translation or rotation can cause total failure to be detected [3].

2. TIME COMPLEXITY IN COPY-MOVE FORGERY DETECTION

Robust copy-move forgery detection, which invariant to geometric transformation and post-processing manipulation is highly needed. Unfortunately, robust methods of CMFD lead to higher complexity and processing time.

Many factors contribute to this problem including the image size, block size, huge number of overlapping blocks, large feature vector

dimension, method used in feature extraction and method used in block matching process [6].

2.1 Image Size, Block Size and Overlapping Blocks (F1)

The first main process in CMFD for block-based method is to divide image into several overlapping blocks of size $B \times B$. It is very important to determine the suitable block size to be used since it will directly impact the detection accuracy as well as computational time. If bigger block size is initiated, number of overlapping blocks will be decreased, hence lower computational time is achieved. This however may lead to missing accuracy in detecting small duplicated region. On the other hand, smaller block size may improves detection accuracy yet produce high computational time due to increasing number of overlapping blocks to be processed.

Overlapping blocks, A for image size of $M \times N$ and block size is $B \times B$ is calculated as;

$$A = (M-B+1)(N-B+1) \quad (1)$$

For instance, if image size is 3000×2300 and block size is defined as 16×16 , total overlapping blocks are $(3000-16+1)(2300-16+1) = 6,820,725$. And if block size 8×8 is chosen, there will be $(3000-8+1)(2300-8+1) = 6,862,949$ number of overlapping blocks. This indeed is a very huge number of overlapping blocks to be processed.

As image size is also one of the variable, with current trend where better quality image equivalent to bigger image size, this will leads to tremendous number of overlapping blocks to be processed to get a high accuracy detection result.

2.2 Method Used In Feature Extraction (F2)

In feature extraction process raw features of each blocks or keypoints are computed to bring significant value or characteristic using feature descriptor. A good feature extractor or feature descriptor should be able to extract the best or robust features for forgery detection. This is a very important step in CMFD processes since the output will determine the accuracy of detection result.

There are numbers of feature extractor methods have been proposed to be used in feature extraction process. These approaches could be divided to five major groups which are 1) moments- based, 2) dimensionality reduction-based, 3) intensity-based, 4) frequency-based and

Table 1: Overview of CMFD Methods Robustness and Complexity

Author	Feature Extraction	Duplicated Matching Technique	Robustness to Geometric Transform			Robustness to post-processing			Complexity
			Rotation	Scaling	Affine	JPEG	Noise	Blurring	
Fridrich, 2003, [4]	Discrete Cosine Transform (DCT)	Lexicographical sorting	✓ small	✗	✗	✓	✓	✗	High
Popescu, 2004, [7]	PCA	Lexicographical sorting	✗	✗	✗	✓	✓	✗	Low
Weiqi, 2006, [8]	Seven characteristics features	Lexicographical sorting	✗	✗	✗	✓	✓	✓	Low
Guohui, 2007, [9]	DWT -SVD	Lexicographical sorting	✗	✗	✗	✓	✓	✓	Low
Mahdian, 2007, [10]	Blur moment	KD-tree	✗	✗	✗	✓	✓	✓	High
Xiao Bing, 2008, [11]	Singular value decomposition (SVD)	Lexicographical sorting	✗	✗	✗	✓	✓	✓	Low
Bayram, 2009, [12]	Fourier Melin Transform (FMT)	Counting Bloom filters	✓ small	✓ small	✗	✓	✗	✗	Very High
Lin, 2009, [13]	Average intensity function	Radix sort	✗	✗	✗	✓	✓	✗	Low
Wang, 2009, [14]	Hu moments, circle blocks	Lexicographical sorting	✓	✗	✗	✓	✓	✓	High
Junwen, 2009, [15]									
Liu, 2011, [16]									
Ryu, 2010, [17]	Zernike moments	Lexicographical sorting	✓	✗	✗	✓	✓	✓	High
Bashar, 2010, [18]	DWT & KPCA	Lexicographical sorting	✓	✗	✗	✓	✓	✓	Very High
Amerini, 2011, 2013, [19, 20]	Scale Invariant Features Transform (SIFT)	Second Nearest neighbor (2NN)	✓	✓	✓	✓	✓	✗	High
Shivakumar, 2011, [21]	Speeded Up Robust Features (SURF)	KD-Tree	✓	✓	✓	✓	✓	✗	High
Li, 2013, [22]	Local Binary Pattern (LBP)	Lexicographical sorting	✓	✗	✗	✓	✓	✓	High
Li, 2013, [23]	Polar Cosine Transform (PCT)	ANN & LSH	✓	✗	✓	✓	✓	✓	Very High
Guo, 2013, [24]	Adaptive non-maximal suppression and DAISY descriptor	Euclidean Distance & 2NN	✓	✓	✗	✓	✓	✓	High
Chen, 2013, [25]	Harris corner points and step sector statistics	Best-bin-first algorithm	✓	✓	✓	✓	✓	✗	High
Akbarpour Sekeh, 2013, [6]	Archimedean Spiral	Sequential block clustering	✓	✗	✗	✓	✓	✓	High
Lynch, 2013, [26]	Average gray value	Expanding block algorithm	✗	✗	✗	✓	✗	✓	Low
Davarzani, 2013, [27]	Multiresolution Local Binary Patterns (MLBP)	K-d Tree	✓	✓	✗	✓	✓	✓	High
Zhao, 2013, [28]	DCT & SVD	Lexicographical sorting	✗	✗	✗	✓	✓	✓	Low
Li, 2014, [29]	Polar Harmonic Transform (PHT)	Lexicographical sorting	✓	✓	✓	✓	✓	✓	Very high
Thajjeel, 2015, [30]	Completed Robust Local Binary Pattern (CRLBP)	Lexicographical sorting	✓	✗	✗	✓	✓	✓	High
Emam, 2015, [31]	Polar Complex Exponential Transform (PCET)	ANN & LSH	✓	✓	✗	✓	✓	✗	High
Lee, 2015, [32, 33]	Histogram of orientated gradients & Gabor magnitude	Lexicographical sorting	✓ small	✓ small	✗	✓	✓	✗	Low
Xiuli, 2016, [34]	Multi-Level Dense Descriptor (MLDD)	Hierarchical Feature Matching	✓ small	✓ small	✗	✓	✓	✗	High

5) keypoint-based method [5]. Each of the approaches has advantages and disadvantages. Details of the capabilities and weakness of these feature extractors could be found in many comprehensive survey and review papers done earlier by many researchers [5, 35-40], thus will not be discussed in this paper.

Table 1 show an overview of some CMFD methods robustness and complexity which have been proposed in the past. From the table, we could see that methods which able to handle more geometrical transform manipulations involved higher complexity level. By taking into consideration that the duplicated region might went through some geometrical transform before being pasted, many methods have tried to increase chance of detection after rotation and scaling. Unfortunately, a robust feature sets involves complex computation and leads to longer detection time.

2.3 Large Feature Vector Dimension (F3)

Feature vector dimension is a length of feature set produce during feature extraction process. Some feature vector basically stores blocks' pixel values, which depend on block size, e.g. $16 \times 16 = 256$, while others depend on block or image content respectively, with extra important value after computation. Some feature set exist in only one feature matrix but many stores as many feature matrices with different method of computation and criterion, thus leads to increasing number of feature vector's dimension. Large feature vector dimension may effect in high computational time during feature extractions process itself as well as next process in the pipeline which is matching process.

Feature extraction method plays a significant role in determining the size of feature set. To have a robust feature sets it usually involves large feature vector dimension together with complex computational process. Similar to block-size, feature vector dimension usually also directly impact the detection accuracy as well as computational time. Robust feature set usually available in large feature vector dimension, unfortunately, large feature vector dimension leads to higher computational time and longer matchings process

2.4 Method Used in Block Matching (F4)

In matching process, comparison is done between each feature sets to find the duplicate

region. Region is suspected to be duplicated if high similarity found between two feature sets. This straightforward method, which called as exhaustive search was very inefficient, since its computes and compares the distance from one feature set to all others. The time complexity of this method is $O(MN)$ for an image of size $M \times N$.

To expedite the matching process, [4] introduced lexicographical sorting. Lexicographical sorting was done to the array which consists of rows storing the feature vector of blocks. By using this lexicographical sorting, the matching rows are easily search by finding for the two consecutive rows that are identical through all rows in the sorted matrix. Lexicographical sorting has become a common step in matching process and used by many previous researchers in their works [7-9, 14, 17, 18, 27-29, 41].

Nevertheless, it was observed that matching process still contributes to high computational time in overall CMFD process. Computational time in matching process may rely on many factors including the image size, block size, huge number of overlapping blocks, large feature vector dimension, method used in feature extraction and method used in block matching process [6]. This has motivated many researchers to propose many matching scheme which could improves time complexity yet produce a high accurate detection result.

3. EXISTING SOLUTIONS

A lot have been done by previous researchers to overcome time complexity issue. These approaches generally could be grouped into five main categories, which are decreasing number of instance blocks, enhance feature extraction algorithm and reducing feature vector dimension, adopting alternative computation formula, improving block matching algorithm and implementing parallel processing scheme. Table 2 summarizes the existing solutions to this time complexity issue grouped by the five main categories, and the time complexity factors which were tackled by the solutions. The explanations on each solution are given in next sub-sections.

3.1 Decreasing Number of Instance Blocks

The first factor to time complexity issue is a huge number of overlapping blocks due to block size and image size. In order to tackle this, keypoint based method is implemented as one of the

Table 2: Solutions to Time Complexity Issues

Solutions / Method	Authors	Time complexity factors			
		F1	F2	F3	F4
1. Decreasing Number of Instance Blocks					
Implementing key-point based method	Hailing <i>et al.</i> , 2008 [42], Bo <i>et al.</i> , 2010 [43], Xunyu and Siwei, 2010 [44], Shivakumar and Baboo, 2011 [21], Amerini <i>et al.</i> , 2011 [19].	✓			
Divide image to non-overlapping block	Wang <i>et al.</i> , 2011 [45]	✓			
Image Resizing	Xiuli <i>et al.</i> , 2016 [34]	✓			
2. Enhance Feature Extraction Algorithm and Reducing Feature Vector Dimension					
Converting a coloured image to grayscale	Fridrich <i>et al.</i> , 2003 [4], Yang and Huang, 2009 [46], Zhao and Guo, 2013 [28], Li <i>et al.</i> , 2014 [29].			✓	
Adopting PCA/PCT	Popescu and Farid, 2004 [7], Mahdian & Saic, 2007 [10], Al-Qershi and Khoo [47]			✓	
7 characteristics features	Weiqi <i>et al.</i> , 2006 [8]		✓	✓	
Using low frequency subband of Wavelet Transform/ improved DWT	Li <i>et al.</i> , 2007 [9], Myna <i>et al.</i> , 2007 [48], Zhang <i>et al.</i> , 2008 [49] Zimba and Xingming, 2011 [50] Yang <i>et al.</i> , 2013 [51], Zimba, 2014 [52]		✓	✓	
Using SVD	Zhao and Guo, 2013 [28], Yang & Huang, 2009 [46], Zhang and Wang [53]			✓	
Adopting Gaussian pyramid decomposition and truncate features	Wang <i>et al.</i> , 2009 [14], Junwen <i>et al.</i> , 2009 [15], Liu <i>et al.</i> , 2011 [16].				
Adopting low-pass filtering during pre-processing	Li <i>et al.</i> , 2013 [22], Li <i>et al.</i> , 2014 [29], Emam <i>et al.</i> , 2015 [31].			✓	
Adopting improved DCT	Huang <i>et al.</i> , 2011 [54]. Cao <i>et al.</i> , 2012 [41]		✓	✓	
3. Adopting alternative computation formula					
Using approximate nearest neighbour searching, free from dimensionality	Yuenan Li, 2013 [23]				✓
Using Manhattan distance instead of Euclidean distance	Zulkurnain, 2015 [3], Ashwini <i>et al.</i> , 2016 [55]				✓
Using fast Walsh-Hadamard Transform (FWHT)	Yang <i>et al.</i> , 2013 [51]		✓		
4. Improving Block Matching Algorithm					
Adopting lexicographical sorting	Fridrich <i>et al.</i> , 2003 [4], Popescu and Farid, 2004 [7], Weiqi <i>et al.</i> , 2006 [8], Li <i>et al.</i> , 2007 [9], Wang <i>et al.</i> , 2009 [14], Cao <i>et al.</i> , 2012 [41], Bashar <i>et al.</i> , 2010 [18], Ryu <i>et al.</i> , 2010 [17], Davarzani <i>et al.</i> , 2013 [27], Zhao and Guo, 2013 [28], Li <i>et al.</i> , 2014 [29]				✓
Using k-d tree algorithm	Mahdian & Saic [10], Zhang and Wang [53], Davarzani <i>et al.</i> , 2013 [27].				✓
Using Counting bloom filters	Bayram <i>et al.</i> , 2009 [12].				✓
Implementing an ANN searching using means of LSH	Yuenan Li, 2014 [23], Emam <i>et al.</i> , 2015 [31].				✓
K-means clustering LSH	Al-Qershi and Khoo [47]				✓
Using Radix sort	Lin <i>et al.</i> , 2009 [13], M. Zimba, 2014 [52], Sridevi <i>et al.</i> , 2012 [56]				✓
Using Efficient subwindow search (ESS)	Zhang <i>et al.</i> , 2010 [57].				✓
Implementing coarse-to-fine approach	Sekeh <i>et al.</i> , 2011 [1]				✓
Using expanding block	Lynch <i>et al.</i> , 2013 [26]				✓
Clustering by similar color textures	Xiuli <i>et al.</i> , 2016 [34]				✓
Multi-hop jump (MHJ) algorithm	Yang <i>et al.</i> , 2013 [51]				✓
5. Implementing Parallel Processing Scheme					
Utilising Parallel algorithm in CPU environment	Sridevi <i>et al.</i> , 2012 [58]	✓	✓	✓	✓
Utilising task parallelism in GPU (Graphics Processing Units)	Singh <i>et al.</i> , 2012 [59], Zulkurnain, 2015 [3].	✓	✓	✓	✓

solutions to reduce number of instance blocks. Instead of dividing image into blocks, keypoint-based method scan whole image and detect high entropy point without dividing the image into blocks [19, 21, 42-44]. Working with keypoint-based feature however has several weaknesses especially when dealing with small size tampered regions. The main drawback of keypoint-based feature descriptor compared with block-based descriptors is its sensitive to homogenous region, little structure and repetitive object. Inability to detect homogenous region and little structure will result in missed detection (false negative) while showing repetitive structure as tampered region increase false positive result.

In block-based method, some researcher chose to divide image to non-overlapping block instead of overlapping blocks [45]. Using example of formula in (1) for an overlapping blocks, total overlapping blocks to be processed are 6,820,725. In contrast, for non-overlapping blocks, D is calculated as;

$$D = M \times N / B^2 \quad (2)$$

For the same example, total number of non-overlapping blocks are $3000 \times 2300 / 16^2 = 26,953$. Numbers of block to be processed were extremely reduced, nonetheless, it might affected the accuracy level. Some previous works [34] also suggested in image resizing during preprocessing step to improve computational efficiency. Nonetheless this process may change some pixels' values and impact the detection result.

3.2 Enhance Feature Extraction Algorithm and Reducing Feature Vector Dimension

The dimension reduction could lower the computation complexity in feature extraction and expedite the sorting and matching processes. Since the features were extracted during feature extraction process, to resolve large feature dimension, enhancements were needed to be done to the feature extraction algorithm itself. As such the solutions were not only to reduce the large feature dimension but also to enhance the method used in feature extraction process.

The basic process in reducing feature vector dimension is by converting a colored image to grayscale before further analysis [4, 28, 29, 46, 51]. This is a popular step done by many researchers during preprocessing stage and usually the first step in CMFD workflow.

Principal Component Analysis (PCA) is a method for simplifying a multidimensional dataset to lower dimension for analysis or visualization. It was first introduced in CMFD domain by [7] to yield a reduced dimension representation. Compared to DCT [4] which has feature dimension of 256 for 16x16 block size, PCA reduced feature dimension to half of the original size for 8x8 block size. PCA was then used as a tool to reduce the feature vector size which was extracted from the image blocks by many other authors [10, 47].

In 2006, [8] used only seven characteristics features for each block to be computed in feature extraction process. The computations involve average of red, green, and blue components as well as summations of 2 equal parts of four directions. With this lower computational complexity was achieved and it was more robust against various types of post-processing manipulations, such as noise adding, blurring, lossy compressing and a combination of these operations.

Other than PCA, Discrete Wavelet Transform (DWT) also has been widely used as method to reduce the dimension of image representation. Li *et al.* [9] and Myna *et al.* [48] reduced the image dimension by taking only the low frequency sub-band of DWT before the Singular Value Decomposition (SVD) is applied to the fixed-sized overlapping blocks. With this approach, feature size is reduced $\frac{1}{4}$ of its original size. Not only the experimental results demonstrated that the proposed approach decrease computational complexity, but it also localize the duplicated regions accurately even when the image was highly compressed or edge processed. Works by [49, 51] could be seen utilizing DWT for the same reason.

Zimba and Xingming [50] used an improved Discrete Wavelength Transform (DWT) together with PCA Eigenvalue Decomposition (PCA-EVD) in their works. They improved time complexity by reducing the feature vector to 8. In [52] Zimba enhanced his previous works to increase robustness and reduced time complexity by extracting features from all the four subbands of DWT, applied PCA-EVD, adopted radix-sort and finally applied SATS to verify duplicated. The proposed algorithm was claimed not only fast but also more robust compared to the algorithms proposed by [8, 13].

[46, 53] used SVD not only to extract unique feature vectors of image blocks, but also to reduce blocks features dimension and increase resistance of noise. Before applying SVD, proposed method by Yang & Huang transformed image to grayscale and further down sampled image to lower resolution of 128x128. Only the first component of the sv-vector for each block is chosen to be used for matching process. With this sorting complexity and memory space was reduced dramatically. In 2013, after applying 2D-DCT to each block to generate the quantized coefficient, [28] used SVD to extract only the largest singular value from each quantized block to reduce the feature dimension. With this approach, feature size also was reduced $\frac{1}{4}$ of its original size.

[14-16] proposed adopting Gaussian pyramid decomposition to reduce the image size. Sub-image in low frequency which produced by this process is chosen to reduce the complexity of the detection algorithm and help to improve the detection result when there are some post-processing operation such as JPEG compression and noise contamination. In his works, image is first reduced in dimension by Gaussian pyramid, before the blocks' features were extracted. Figure 2 gives the illustration about Gaussian pyramid decomposition used by [16].

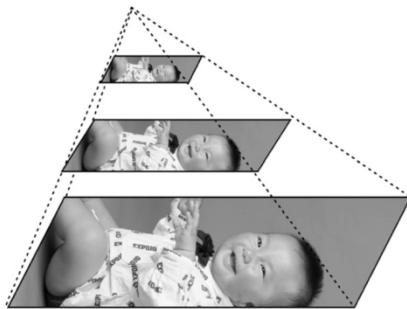


Figure 2: The illustration of Gaussian pyramid decomposition from [16]

Hu moment was applied to the fixed sized overlapping blocks of low-frequency image in [14, 16] while in [15] mean of image pixel value in each circle region were calculated and adopted as features. Apart of that, to further reduce the computational complexity, only the first four moments and four features of the circle block were used as the feature for above works respectively.

Apart of that, low-pass filtering also adopted during pre-processing stage by few researcher to improve the detection performances, especially in the case of signal processing attacks. By adopting low-pass filtering, high frequency disturbances or smooth image modification were alleviated thus giving a better detection result [60]. Li *et al.* utilized Gaussian low-pass filter in both works [22, 29] and followed by other researchers [31] for the same purpose.

Improved DCT-based feature extraction was used by [54]. In order to reduce the feature dimension, higher frequency coefficients were truncated. Consideration was made due to the nature of DCT where the energy of transformed coefficients is focused on the lower frequency coefficients which located at the first several values. Almost similar to [54], [41] applied DCT coefficients for each block, before represented it as a circle block and only four features are extracted to reduce the dimension of each block.

In summary, most of the solutions were done by adding pre-processing or post processing steps in feature extraction algorithm. These include grayscale conversion, Gaussian pyramid decomposition, applying PCA, DWT or SVD, feature truncation or selection of dedicated features as well as improved DCT. Pre-processing steps were done to reduce time complexity during feature extraction process, while post-processing steps were done to ease matching process. Many hybrid feature extractors were also proposed in order to get the high robustness with reduced time complexity in feature extraction and matching process.

3.3 Adopting Alternative Computation Formula

Lower computation complexity also could be achieved by adopting less complex formula. Yang *et al.* [51] adopting fast version of Walsh–Hadamard transform (FWHT) during features extraction process. The fact that FWHT only use addition and subtraction makes the computations simpler and runs more efficiently.

Euclidean distance which usually used by many researchers in measuring similarity were replaced by Manhattan distance in works done by Zulkurnain, 2015 [3], and Ashwini *et al.*, 2016 [55]. Compared to Euclidean distance, Manhattan distance avoids calculation of squares and square roots required in Euclidean distance.

The above two computations were only some example of many other fast or simpler computation adopted by many researcher during CMFD process to reduce computation time. This is a popular option since it can save computation time with just a slight reduction in the accuracy of the calculation.

3.4 Improving Block Matching Algorithm

In matching process, more options had been proposed to reduce the processing time. Instead of using exhaustive search to compute the distance from the block to all others, [4] introduced lexicographical sorting in matching process. By using this lexicographical sorting, the matching rows are easily search by finding for the two consecutive rows that are identical through all rows in the sorted matrix. Lexicographical sorting has become a common step in matching process and used by many previous researchers in their works [7-9, 14, 17, 18, 27-29, 41].

Some hierarchical structures also have been proposed to enhance the neighboring blocks searching efficiency. One of a commonly used structure is the k-d tree (k-dimensional space). Mahdian and Saic [10] proposed k-d tree representation in their works where the feature extraction used were moment feature and PCA. Zhang and Wang [53] in their works used SVD together with k-d tree resulted in lower computational complexity and was more robust to various post image processing except jpeg compression compared to [4, 7, 8].

Davarzani *et al.* [27] utilized both lexicographical sorting and KD-tree in their proposed method. Lexicographical order was first used in sorting the feature vectors while k-d tree were implement to determine duplicated image blocks in the block matching step to achieve more time reduction and accuracy in the matching process. This method however, is still time consuming for forgery detection in high resolution images compared to DCT and SIFT.

Bayram [12] used Counting bloom filters in their matching process to improve the time efficiency. This proposed method works by comparing the hashes of features instead of the features themselves. Time efficiency was considerably improved with the expense of a slight reduction in the robustness.

An approximate nearest neighbor (ANN) searching using means of locality-sensitive hashing (LSH) was adopted in the proposed work by Yuenan Li [23] and later followed by [31]. LSH is one of the most effective tool for approximate nearest neighbor searching, and has been successfully applied in a number of areas such as information retrieval and large-scale database indexing. Approximate nearest neighbor searching is accomplished in LSH by hashing the vectors using a set of hash functions and picking up those with identical hash values. Experiment result demonstrated a higher degree of robustness against post-processing operations, faster running time and free from dimensionality. LSH also has been adopted in [47] where Al-Qershi and Khoo proposed k-means clustering and LSH method to match the blocks based on Zernike moments. Processing time was said to reduce to 10% with enhancement to detection accuracy

Radix sort was proposed by Lin *et al.* [13] to sort the feature vectors instead of lexicographic sorting. Apart of that feature dimension of each block was earlier reduced by representing it in 9-dimensional feature vector in spatial domain. Employing the radix sort improves the detection time efficiently with slight reduction in the robustness. Radix-sort however only permits integer value as feature vector elements and this has limits its feasibility to other type of feature vector [6]. Some researcher which also employ Radix-sort were [52, 58].

Efficient subwindow search (ESS) is one of the most efficient methods based on subwindow search to accomplish the localization work. In proposed method by [57], a voting method was adopted before ESS was applied to find the potential source-target region pair. The proposed methods was claim to reduce the time complexity from best reported $O(P \log P)$ to $O(P)$, where P is the number of pixels in the image for the simple pure translation cases. The experiments done however did not show the comparison table between ealier method and the proposed method.

Sekeh *et al.* [1] proposed to add some intelligence to the process by implementing coarse-to-fine approach. In his work, he used sequential block clustering to minimize the search space in block matching. This significantly improves time complexity as it eliminates several extra block-comparing operations. The mathematical analysis, supported by experimental results demonstrated

that the proposed model is more cost-effective than lexicographically-based sorting for small block size. Almost similar to [1], expanding block was suggested by Lynch *et al.* [26] where blocks are grouped and sorted together according to their dominant features before the matching process took place. This approach however produced high number of false positive result and slower compared to DCT and statistical which using sliding block.

Yang *et al.* [51] proposed multi-hop jump (MHJ) algorithm to ignore some of the “unnecessary testing blocks” (UTB) to make the range matching more efficient, Experimental results demonstrated that the proposed method is able to accurately detect the copy-move forgery with significant reduction in the processing time compared with other methods. This proposed method however is weak in detecting images which undergone geometrical transformation attacks.

In the recent years, some enhancement were done involving clustering by similar color textures, proposed by Xiuli *et al.* [34]. Computational expense was much decreased using this method, with promising results in robustness against various attacks.

From exhaustive search to lexicographic sorting, followed by kD-tree, counting bloom filters, ANN, radix sort, ESS, coarse-to-fine and latest is clustering technique. The research work is actively on going. In short, more options were explored to reduce the search space in order to minimize the block comparison process as well as improve the time complexity.

3.5 Implementing Parallel Processing Scheme

The most recent trends in resolving performance issue is exploiting task parallelism. In CMFD, [58] introduced parallel algorithm in CPU environment to decrease the execution time. Overlapping blocks and sorting operations are proposed to be done in parallel. The result reported that the parallel version performs task faster and very well suited for real time applications. Since the images used in the experiment were grayscale images with small block size defined, future works may explore in color images, or high resolution images. It was also observed that this method is only caters for plain copy-move, without taking into consideration other types of manipulations, i.e. geometrical transformation or post-processing

attacks. Nevertheless, this research has open up more options in resolving time complexity issue.

Task parallelism was extended to be used in GPU (Graphics Processing Units) by [59]. In their works, feature vectors were computed based on integral images and radix sort was adopted. Computation of feature vector in GPU shows significant speedup of over 230 times, while the overall process speedup was reduced 12 times compared to CPU version. As the main purpose of this research is to speedup detection process, no conclusive results are shown regarding robustness to geometric or post-processing manipulation. Another works were done by [3] to improve CMFD performance and compare the detection of duplicated region using counting bloom filters and radix sort. He used DCT as feature extraction in this study. Result shown that feature extraction done in GPU-based scheme was 5 times faster than the multi-threaded CPU while counting bloom filters was 18 times faster that radix sort in detecting duplicate region. Overall, the scheme achieved 84% detection rate since DCT is not invariance to geometrical transformation.

It was observed that all these few initial works on utilizing task parallelism is only cater for simple feature extraction process with less computation works. It is also not robust to geometrical distortion. Nevertheless, these seem to give a good sign to this area and open up many more research works to be explored.

4. DISCUSSION

Robust copy-move forgery detection, which invariant to geometric transformation and combined manipulations is highly needed. Unfortunately, since research progresses towards developing more robust methods of CMFD, the algorithms being proposed have higher and higher complexity. Literature shows that it is a very challenging task to get the best balance between accuracy and time complexity.

High time complexity was identified occurs mostly during feature extraction and matching process. Many factors may contributes to this issue including image size, block size, huge number of overlapping blocks, large feature vector dimension, method used in feature extraction and method used in block matching process.

Previous works has shown that many efforts have been done to overcome time complexity issue such as decreasing number of instance blocks, enhance feature extraction algorithm, reducing feature vector dimension, improving block matching algorithm, adopting less complex formula and implementing parallel processing scheme.

Implementing keypoint-based algorithm could be considered as major success since it capable in detecting copy-move forgery even with existence of geometrical transform manipulation in timely manner. Nevertheless keypoint-based algorithm suffer from miss detection issue if the image consist of homogenous region, little structure and repetitive object.

As a result, more and more research was done to resolve time complexity issue within block-based method. In order to reduce feature vector dimension and enhance feature extraction process, many researchers proposed to adopt preprocessing or post processing task. These include grayscale conversion, Gaussian pyramid decomposition, applying PCA and DWT as well as improved DCT. Many hybrid feature extractors were also proposed in order to get the high robustness with reduced time complexity in feature extraction and matching process.

Time complexity also could be reduced by adopting less complex formula in computation. With a slight reduction in the accuracy of the calculation, this option could effectively reduce the computation time.

In matching process, more solutions were explored to increase matching efficiency. Apart of using lexicographical sorting, now more options are available such as K-d tree, counting bloom filters, ANN, Radix sort and many more.

Not only limited to software enhancement, solutions were also extended to hardware environment where CPU and GPU parallel processing were also feasible and given promising result.

With current positive trend, there still many work to be done to improve the efficiency of detection process. Robust feature set usually consist of huge feature set. Having a small yet robust feature set surely will improve time complexity issue in feature extraction as well as matching

process. As such it is recommended for future feature extractor to include pre and post-processing task within the feature extraction process to achieve this goal.

Within the matching process, it was observed that block clustering could reduce the block matching search space, thus could significantly improve the time complexity. With that, researcher may propose more alternative clustering solutions in matching process.

Current CPU and GPU parallel scheme were only done to simple feature extraction algorithm, as such there were no evidence on the efficiency of these solutions should a complex feature extraction is implemented. It is highly recommended if these solutions could be adopted to handle geometric transform manipulation.

Apart of parallel processing, future works should consider multilayer processing. Multilayer processing perhaps could be applied during feature extraction process as well as matching process.

5. CONCLUSION

In this survey we highlighted few scenarios in copy-move forgery based on types of manipulations and image categories. A brief explanation on copy-move forgery detection workflow is given to provide better understanding on how the time complexity issue could exist in CMFD pipeline. Four main factors that contribute to this issue were identified and describe accordingly. Furthermore existing solutions proposed by previous researcher were elaborated and classified to five categories to determine the effectiveness in existing CMFD process. Overall discussion on the issues and solutions was done. Some possible future enhancements were proposed includes enhancement to feature extraction algorithm, adopting block clustering in matching process, utilizing the advancement of parallel processing scheme as well as multilayer processing. It is hope that other researchers will gain from this paper by producing a fast and accurate CMFD method.

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