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1 **An Automated Method for Mapping Geomorphological Expressions of Former**
2 **Subglacial Meltwater Pathways (Hummock Corridors) From High Resolution**
3 **Digital Elevation Data**

4

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26 **1. Introduction**

27

28 Understanding the dynamic response of former (palaeo) continental ice sheets to
29 climate change can provide valuable information for assessing the recent and
30 predicting the future behaviour of the ice sheets in Antarctica and Greenland and
31 their contribution to sea level rise (e.g. Ó Cofaigh and Stokes, 2008; Stokes et al.,
32 2015 and references therein). Subglacially-produced landforms - exposed after
33 glacial retreat - provide a rich record for reconstructing palaeo-ice sheets. Their
34 distribution allows former ice sheet extent, relative thickness and retreat patterns to
35 be reconstructed (e.g. Dyke & Prest, 1987; Boulton & Clark, 1990; Clark et al., 2004,
36 2012; Evans et al., 2005; Ottessen et al., 2008) and provides insight into ice sheet
37 dynamics, thermal regime and subglacial hydrology (e.g. Kleman, 1992; Clark &
38 Walder, 1994; Kleman & Borgstrom, 1996; Stokes & Clark, 1999; Kleman & Glasser,
39 2007; Margold et al., 2013, 2015; Storrar, et al., 2014; Livingstone et al., 2016).

40

41 Subglacial hydrological processes have been identified as a key factor of ice
42 sheet dynamics (e.g. Iken, 1981; Boulton et al., 2001; Anderson et al., 2004; Schoof,
43 2010; Bartholomew et al., 2010). However, as the bed of contemporary ice sheets
44 cannot be directly observed, the configuration of the subglacial drainage network is
45 largely inferred from tracer and borehole monitoring studies and the use of ice
46 dynamic proxies (e.g. Chandler et al., 2013; Andrews et al., 2014; Tedstone et al.,
47 2015). In contrast, palaeo-ice-sheet-beds provide direct access to the landforms
48 created by palaeo-subglacial meltwater drainage. These landforms can be used to
49 determine the properties of the former subglacial drainage system at an ice sheet
50 scale and throughout deglaciation, providing much needed context for spatially and

51 temporally limited contemporary observations. Subglacial meltwater landforms, such
52 as meltwater channels, tunnel valleys and eskers, are widely observed in the
53 geological record (e.g. Wright, 1973; Sharp et al., 1989; Clark and Walder, 1994;
54 Greenwood et al., 2007; van der Vegt et al., 2012; Storrar et al., 2014; Livingstone
55 and Clark, 2016) and have been routinely employed in glacial reconstructions to
56 constrain former subglacial water flow direction, ice sheet surface slope and the
57 position of the ice margin. The vastly improved resolution and coverage of digital
58 elevation models (DEMs) today means that these landforms can be studied in
59 greater detail and more comprehensively for such purpose. The associated datasets
60 may thus also extend our understanding of some of the more complex processes
61 related to subglacial meltwater flow (e.g. Makinen et al., 2017; Clark and Livingstone,
62 2018).

63
64 Here we focus on elongated tracts of hummocks that have been variously termed
65 'hummock corridors', 'glaciofluvial corridors' or 'subglacial meltwater corridors' (e.g.
66 St-Onge, 1984; Rampton, 2000; Utting et al., 2009; Sharpe et al., 2017; Peterson
67 and Johnson, 2018). Hummock corridors are believed to record former large-scale
68 subglacial meltwater flow beneath ice sheets that is known to have been
69 widespread, but whose origin is not yet fully understood (section 2). Given this
70 uncertainty we use the non-genetic term 'hummock corridor' as per Peterson and
71 Johnson (2018). Hummock corridors have been previously detected at a range of
72 scales from field observations, aerial photographs, surficial geology maps and
73 remotely sensed data (see references within Utting et al., (2009) and Sharpe et al.,
74 (2017) for a review of previous work in Canada and Peterson and Johnson (2018) for
75 Sweden). The recent release of freely available high resolution DEMs (e.g.

76 ArcticDEM, Ladmateriat and Finland's National Land Survey) have vastly increased
77 the evidence base of glacial features on palaeo-ice sheet beds. So widespread in
78 fact, that the relatively slow process of manual mapping has become a major
79 bottleneck for obtaining information about these features.

80

81 The objective of this paper is to demonstrate the utility of a new automatic
82 method for mapping the large-scale distribution of hummock corridors from high-
83 resolution DEMs to gain insight into their formation. The method is developed and
84 tested on three test sites in northern Canada and northern Scandinavia. The success
85 of the method was quantitatively determined by its ability to reproduce the large-
86 scale distribution and morphometric characteristics (length and width) of the
87 manually mapped hummock corridors.

88

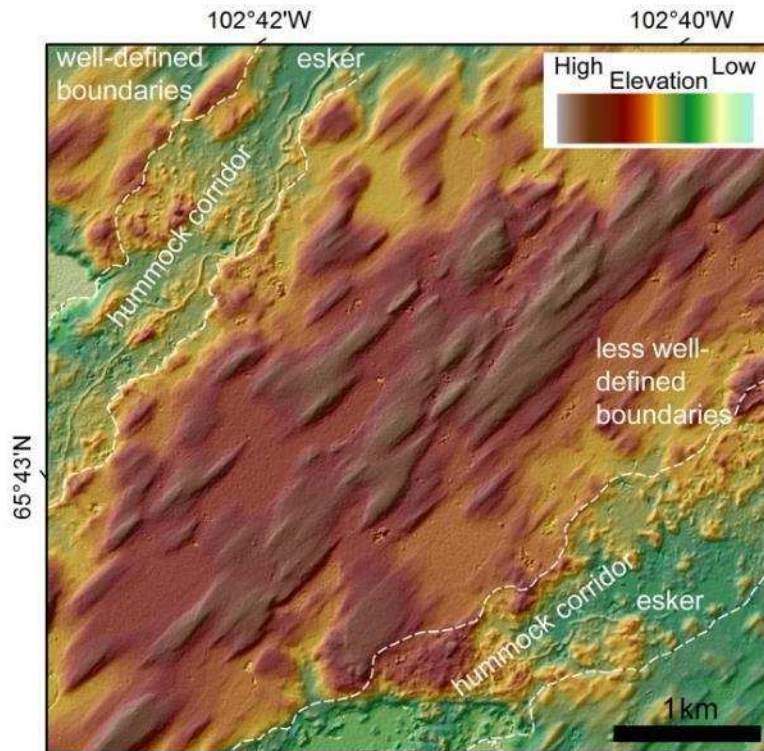
89

90 **2. Hummock Corridors**

91

92 Hummock corridors have been identified and studied in detail in Canada (St-
93 Onge, 1984; Rampton, 2000; Utting et al., 2009; Sharpe et al., 2017; Storrar and
94 Livingstone, 2017) and Sweden (Peterson et al., 2017; Peterson and Johnson,
95 2018). They are defined as elongated tracts of irregular shaped hummocks which
96 stand out from the surrounding smooth, streamlined bed (Fig. 1). Typical corridors
97 are a few km to over 100 km long and 100s of m to several km wide (Table 1). The
98 individual hummocks within the corridors vary in size (10s to 100s m in width/ length
99 in plan view), shape (mostly irregular) and relief (1 to 10s of m) (Peterson and
100 Johnson, 2018). In general, hummocks within the corridors tend to show no

101 consistent plan-form shape, although triangular-shaped hummocks have been
102 identified in some corridors in Finland (Makinen et al., 2017) and Sweden (Peterson
103 et al., 2017).



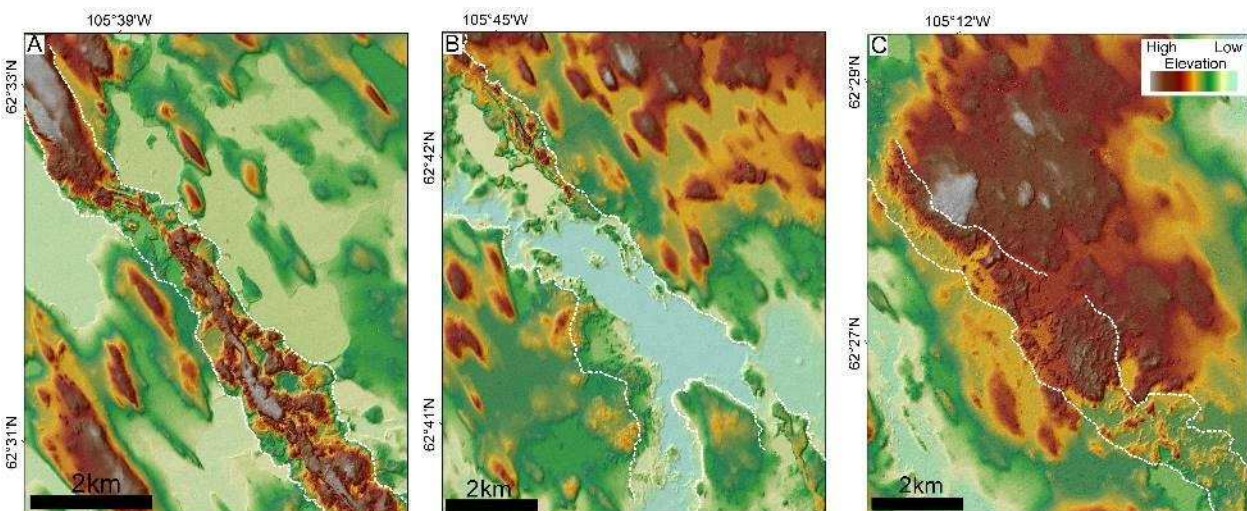
104
105 Figure 1. Hummock corridors in Keewatin, Nunavut, Canada (ArcticDEM). The corridors are
106 aligned with and bordered by streamlined features on the bed that indicate ice-flow from the
107 south to north.

108
109 Hummock corridors vary in topographic expression (Fig. 2); for example,
110 adjacent corridors or different parts of the same corridor can be cut down into the
111 surrounding former ice-sheet bed and/ or elevated above the surrounding terrain
112 while other corridors branch and have tributaries. Some hummock corridors exhibit
113 sharp boundaries with significant vertical relief, while other boundaries are more
114 diffuse and characterised by subdued relief. Hummock corridors longitudinal
115 elevation profiles are typically undulating and they often contain eskers. Although

116 tracts of hummocks can be traced over long distances (>100 km), they are often
117 discontinuous with intervening segments of smoother terrain, tunnel valleys or
118 eskers.

119

120 At a regional scale - i.e., a horizontal scale exceeding the size of individual
121 corridors and approaching the size of the collection of multiple corridors and/ or the
122 ice sheet - corridors appear to exhibit a radial pattern (e.g. Peterson and Johnson,
123 2018), indicative of a larger divergent network (Utting et al., 2009) and appear to be
124 quasi-regularly spaced. Locally, corridors display a high degree of parallel conformity
125 with each other and with other subglacial bedforms such as drumlins and lineations,
126 suggesting a relationship with palaeo-ice flow.



127

128 Figure 2. The variable expression of hummock corridors: (A) positive relief with a central
129 esker (B) flat bedded sections and branching and (C) corridors without significant relief or
130 eskers, identified simply as elongated tracts of hummocks. A-C are examples taken from
131 within test site 1 (Fig. 9).

132

133 Adverse and undulating long profiles, orientations parallel to former glacier
 134 flow lines, the presence of eskers within the hummock corridors and the termination
 135 of corridors at or near former ice margins indicate a likely subglacial meltwater origin.
 136 However, the source of meltwater and the magnitude and duration of flow remains
 137 uncertain.

138

139 Table 1. Metrics of 'hummock corridor' type features reported in the literature.

Location	Source	Term used	Frequency	Length (km)	Width (km)	Spacing (km)
Southwestern Finland	Makinen et al. (2017)	Triangular-shaped landforms within distinguishable route	Single feature(s) selected for purpose	40 (longest feature)	1 – 2.5 (most distinct features)	1 – 4 (most distinct features)
Southern Swedish Uplands (SSU), Sweden	Peterston and Johnson (2018)	Hummock corridor	76 hummock tracts	1.5 – 11.8 (mean 5.2)	0.2 – 4.9 (mean 1.1)	0.8 – 54.5 (mean 14.5)
Southern Fraser Plateau, Canada	Burke et al. (2011)	Erosional corridor	Single	~ 40	~ 0.25 - 1	-
Southern Slave Province, Canada	Rampton (2000)	Meltwater corridor	-	-	0.5 - >2	-
East Arm Area, Great Slave Lake, Canada	Sharpe et al. (2017)	Meltwater erosional corridor	Approx. 22 corridors	80 - 120	~0.3 - 3	5 - 15
East-central Alberta and South-central Michigan	Sjogren et al. (2002)	Incipient tunnel channel	-	-	0.2 - 4	-
Redrock Lake Area, Canada	St-Onge (1984)	Glaciofluvial meltwater corridor	>15 (estimated from map)	Commonly > 20 (estimated from map)	Up to 1	12 – 15
Kivalliq region, Nunavut, Canada	Storrar and Livingstone (2017)	Corridor-like tracts of glaciofluvial deposits	-	-	Up to 6	-
Walker Lake, Canada	Utting et al. (2009)	Glaciofluvial corridor	>20 (estimated from map)	~ 5 - 12	~0.2 - ~ 0.7	5 – 10

140

141

142 Hummock corridors have similar widths, lengths and spacing as tunnel valleys
143 (Table 1) which has led Peterson and Johnson (2018) to classify them as such.
144 Proposed formation theories for the corridors thus far focus on similar concepts: (i)
145 time-transgressive formation with small sections forming behind a retreating margin
146 (St-Onge, 1984); (ii) low-frequency, high-magnitude regional outbursts with whole
147 networks formed over relatively short periods (e.g. Rampton, 2000; Sharpe et al.,
148 2017); or (iii) formation of individual channels by the sudden rapid drainage of large
149 volumes of meltwater to the bed (e.g. Utting et al., 2009; Peterson and Johnson,
150 2018).

151

152 The formation of individual hummocks within the corridors has been ascribed
153 to both deposition of glaciofluvial sediments within cavities during periods of sudden
154 large meltwater influxes (e.g. Utting et al., 2009) and erosion by distributed braided
155 canals on the bed of the valley or turbulent meltwater flow during valley formation
156 (e.g. Sjogren et al., 2002; Peterson et al., 2018). Where the corridors and hummocks
157 cut down into thicker till, formation is thought to be by subglacial fluvial erosion
158 (Peterson and Johnson 2018), whereas positive relief corridors, or those containing
159 tracts of glaciofluvial sands and gravels, have been associated with sediment
160 deposition (e.g. Utting et al., 2009) and typically occur in areas where sediment
161 thickness is low or the substrate is difficult to penetrate (Peterson and Johnson,
162 2017).

163

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166

167

168 **3. Methods**

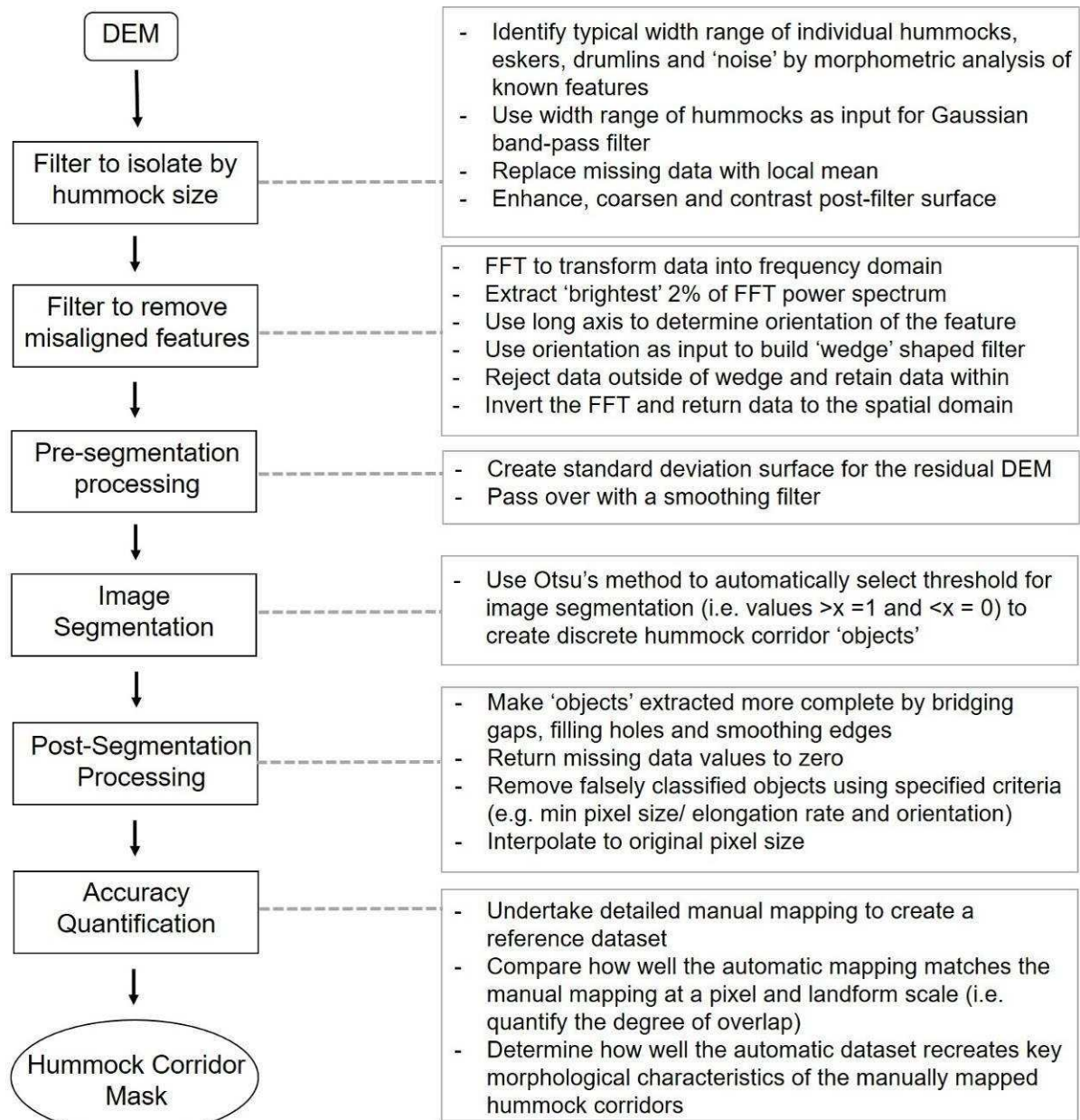
169

170 Traditionally, information on subglacial bedform distribution and morphology
171 has been obtained by visual identification and onscreen digitization of feature
172 boundaries (e.g. Clark et al., 2004; Greenwood and Clark, 2008; Hughes et al.,
173 2010; Storrar et al., 2014; Livingstone and Clark, 2016). However, several issues are
174 apparent with this approach, including the subjectivity of landform and boundary
175 identification, concerns over which visualisation/ illumination techniques provide the
176 best results (e.g. Smith and Clark, 2005; Hughes et al., 2010), and uncertainty
177 regarding whether different practitioners produce the same consistent results (e.g.
178 Hillier et al., 2015). Moreover, with the increasing availability and resolution of DEMs
179 and remote sensing imagery, the immensity of data analysis required to manually
180 explore and map large regions at such fine resolution is becoming a major
181 bottleneck. Automatic or semi-automatic methods offer an alternative means of
182 rapidly mapping and extracting quantitative information directly from DEMs (see
183 Evans, 2012 and Bishop et al., 2012 for discussions).

184

185 Several studies have attempted to employ semi-automatic/ automatic
186 techniques for mapping subglacial bedforms, particularly drumlins. These methods
187 typically rely on an object based image analysis approach (OBIA) (e.g. Saha et al.,
188 2011; Evans, 2012; Jorge and Brennand, 2017; Yu et al., 2015; Foroutan and
189 Zimbelman, 2017), which uses a multi-resolution algorithm (Baatz and Schäpe,
190 2000) to group pixels into image objects and classify them based on predetermined
191 rules (e.g. elevation, slope, axis, length, entropy and eccentricity).

192



193

194

195 Figure 3. Main steps of our automatic method to identify and extract hummock corridors (left-
 196 hand sequence) with details about each step expanded on (right).

197

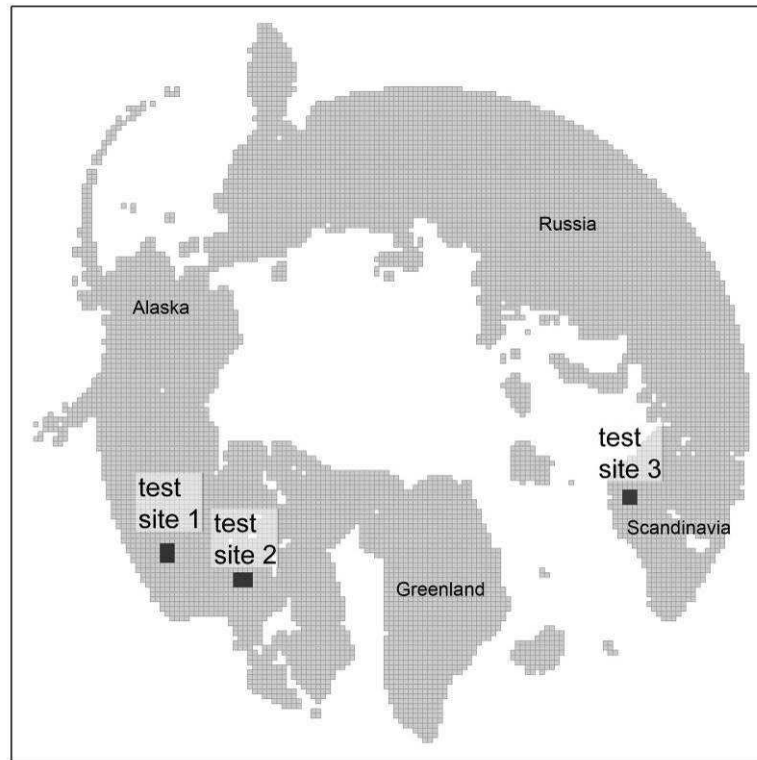
198

199 This study develops the first method to automatically map hummock corridors.

200 Its main steps - detailed in Sections 3.1 to 3.4 - are outlined in Figure 3. The DEM

201 tiles used come from the freely-available ArcticDEM dataset

202 (<https://www.pgc.umn.edu/data/arcticdem>), which provides 50 x 50 km tiles at 5 m
203 resolution for all land area above 60°N. It was generated by applying stereo auto-
204 correction techniques to overlapping pairs of high-resolution optical satellite images
205 (Noh and Howat, 2015).
206



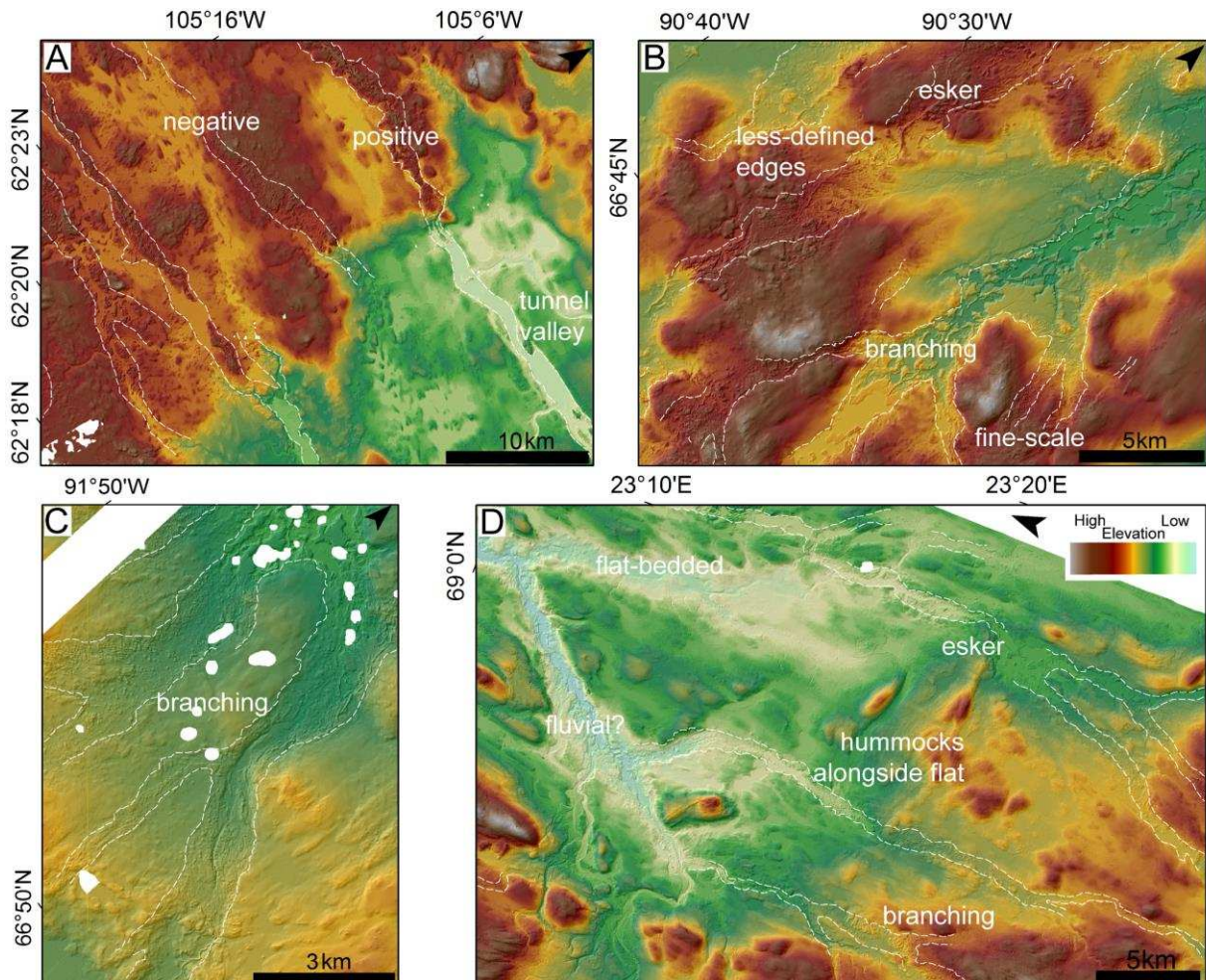
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208

209 Figure 4. Location of the three test sites used in our study: (1) Northwest territories, Canada
210 (30,000 km²), (2) Nunavut, Canada (30,000 km²) and (3) Northern Scandinavia (22,500
211 km²). Grey background indicates the total extent of Arctic DEM data. See Fig. 5 for example
212 of typical terrain from each test site.

213

214 To develop and test the automatic method, three test sites were selected from
215 the ArcticDEM (Fig. 4), chosen to ensure a range of hummock corridor morphologies
216 and background conditions were sampled (e.g. varying relief, presence/ absence of
217 fluvial features etc.). At test site 1, corridors typically exhibit strong positive or

218 negative relief with well-defined edges, and are qualitatively clearly distinguished
 219 from their surroundings (Fig. 5A). The site includes relatively straight hummock
 220 corridors extending significant distances across the bed. At test site 2, the
 221 background topography is more complex and hummock corridors tend to curve
 222 across the landscape, exhibit less pronounced relief and have poorly defined
 223 boundaries (Fig. 5B and C. The hummock corridors at test site 3 are typically
 224 discontinuous and more subdued, and the surrounding landscape is characterised
 225 by a strong fluvial network and significant vertical relief in the south-west of the site
 226 (Fig. 5D).



227
 228 Figure 5. Example of hummock corridors (outlined in white dashed lines) from each of the
 229 test sites with locations identified in Figures 9 -11. (A) Test site 1 - note the transition down-

230 flow (inferred ice flow from east to west) from tunnel valley to hummock corridor associated
231 with an increase in elevation and the alternating positive and negative hummock corridors.
232 (B and C) Test site 2 – note the more complex hummock corridors that branch and can be
233 difficult to identify on the bed owing to their more subdued relief. (D) Test site 3 – example of
234 hummock corridors branching off a large central channel with few/ no hummocks in places.

235

236 **3.1 Processing Step One: Filter to isolate hummocks by size**

237

238 Elevation values in a DEM vary significantly, depending on the presence of
239 large-scale topographic features (e.g. valleys, hills, mountains etc.) and/ or the type
240 of landforms present. Typically, landforms fall within a definable length-scale range.
241 In theory, mathematical operations can be applied to a DEM to isolate a particular
242 feature based on this knowledge. Using length-scales to separate morphological
243 features of interest from background topography is well established within the earth
244 sciences (e.g. Wessel, 1998; Hillier and Watts, 2004; Hillier and Smith, 2008) and
245 has been used within glacial geomorphology to enhance the detection of subtle
246 features such as lineations (Hillier and Smith, 2008).

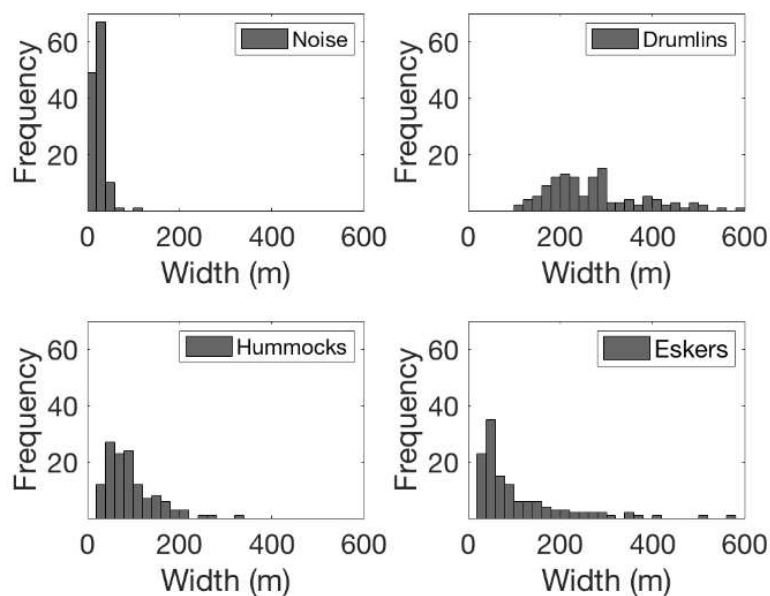
247

248 Individual hummocks from the three test sites were randomly selected,
249 measured (long axis) and recorded to determine their typical length-scale range. To
250 minimise overlap with features which tend to co-occur with hummock corridors,
251 drumlins, eskers and background 'noise' in the DEM (artefacts which often occur in
252 elongate patches) were also sampled (their minor axis). The results (Fig. 6) reveal a
253 typical length-scale of 40 - 180 m for hummocks. This is distinguishable from the
254 'noise' and the drumlins at the lower and upper bounds. Although eskers display

255 similar length-scale as hummocks, their low density largely precludes their
256 classification as hummock corridors at later stages of our processing.

257

258 The length-scale range was used to inform the design of a 2D Gaussian-
259 weighted band-pass filter (filt2: written by Chad A. Greene of the University of Texas
260 Institute for Geophysics for use in Matlab - freely available at:
261 [https://uk.mathworks.com/matlabcentral/fileexchange/61003-filt2-2d-geospatial-data-](https://uk.mathworks.com/matlabcentral/fileexchange/61003-filt2-2d-geospatial-data-filter)
262 filter). The band-pass filter suppresses spatial frequencies outside the specified
263 length-scale range, thus attenuating (although not eliminating) a large amount of the
264 topographic variation associated with other features on the bed. Values of 40 and
265 150 m were selected as the lower and upper bounds as this struck the best balance
266 between retaining information whilst preventing false detections. This resulted in a
267 residual surface with a large amount of background topographies removed,
268 emphasising areas with features within the length-scale of individual hummocks.



269

270 Figure 6. Histograms showing the horizontal widths of 'noise', drumlins, hummocks and
271 eskers (n = 130) randomly selected and measured from the three test sites. Note that the

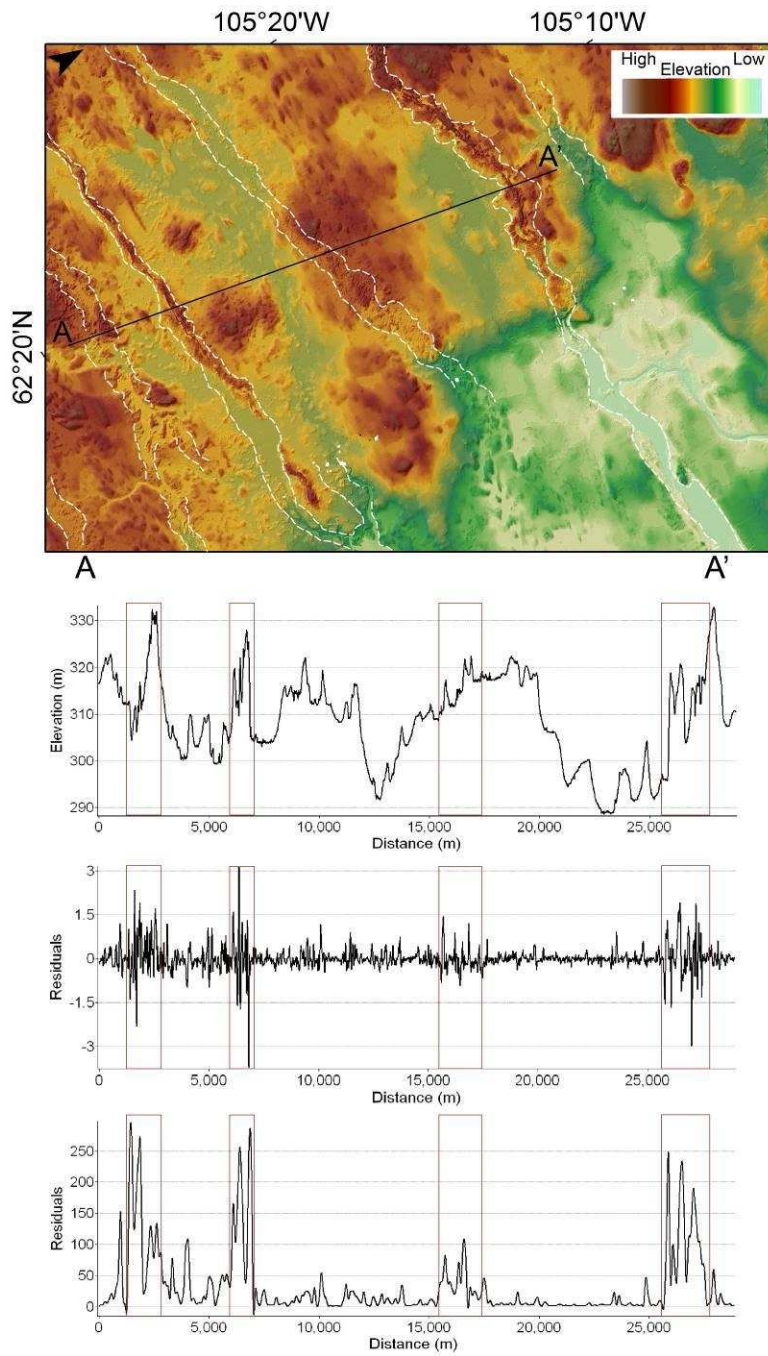
272 hummocks form their own population with only a small overlap at the upper and lower ends.
273 A large amount of the 'noise' (artefacts in the DEM that sometimes occur in linear zones)
274 was smaller than 10 m thus preventing accurate measurement.

275

276 For some hydrological features (e.g. lakes and rivers) and in areas of cloud
277 cover or shadows, the ArcticDEM tiles contain no elevation data and were coded as
278 NaN (i.e. Not a Number). While the 2D Gaussian-weighted band-pass filter is
279 designed to work on data with NaNs, several of the subsequent processing steps
280 require continuous data so a method to fill in the NaNs was implemented. Standard
281 interpolation or smoothing methods (e.g. `inpaint_nans` -
282 https://uk.mathworks.com/matlabcentral/fileexchange/4551-inpaint_nans) can be
283 used to fill NaNs with realistic values over smaller areas; however, the large size of
284 some missing data patches here (up to ~480 km²) would result in the introduction of
285 artefacts and thus render this approach inappropriate. To address this, we
286 developed a method for 'flooding' isolated NaN patches with their individual local
287 mean. Firstly, a mask of contiguous patches of NaNs was created. The mean
288 elevation of a 100-pixel wide buffer around each patch was then used to replace the
289 NaNs within. This was carried out after the initial filtering, which removed a large
290 amount of elevation variations, creating more uniform values within the NaN buffers
291 and reducing the likelihood of steep jumps in elevation across short distances. While
292 this approach precluded the detection of hummock corridors within these areas, it
293 effectively blended the missing data with its surroundings preventing spurious
294 artefacts. NaN values in the original data were returned to zero at the final stage to
295 ensure that no areas were falsely classified.

296

297 To further enhance the contrast in relief at the length-scale created by the
298 band-pass filter, the residuals were converted to absolute values and each pixel
299 replaced with the maximum of the adjacent pixels if the original value was greater
300 than the tile median or replaced with the minimum of the adjacent pixels if the
301 original value was less than the median. (This process is analogous to ‘contrast
302 stretching’ in the processing of grey-scaled images.) This ‘enhanced’ residual
303 surface was then normalised by rescaling the data so values fell between 0 and 255
304 (i.e. unsigned 8-bit integers) to ensure consistency between different tiles and to
305 minimise memory requirements for storing data (Fig. 8a).



306

307 Figure 7. Cross-profiles across four hummock corridors (red boxes) showing top to bottom:

308 (i) original elevation data with significant elevation variations, (ii) residual surface created

309 post band-pass filter and (ii) residual surface created following enhancement.

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313

314 **3.2 Processing Step Two: Filter to remove misaligned features**

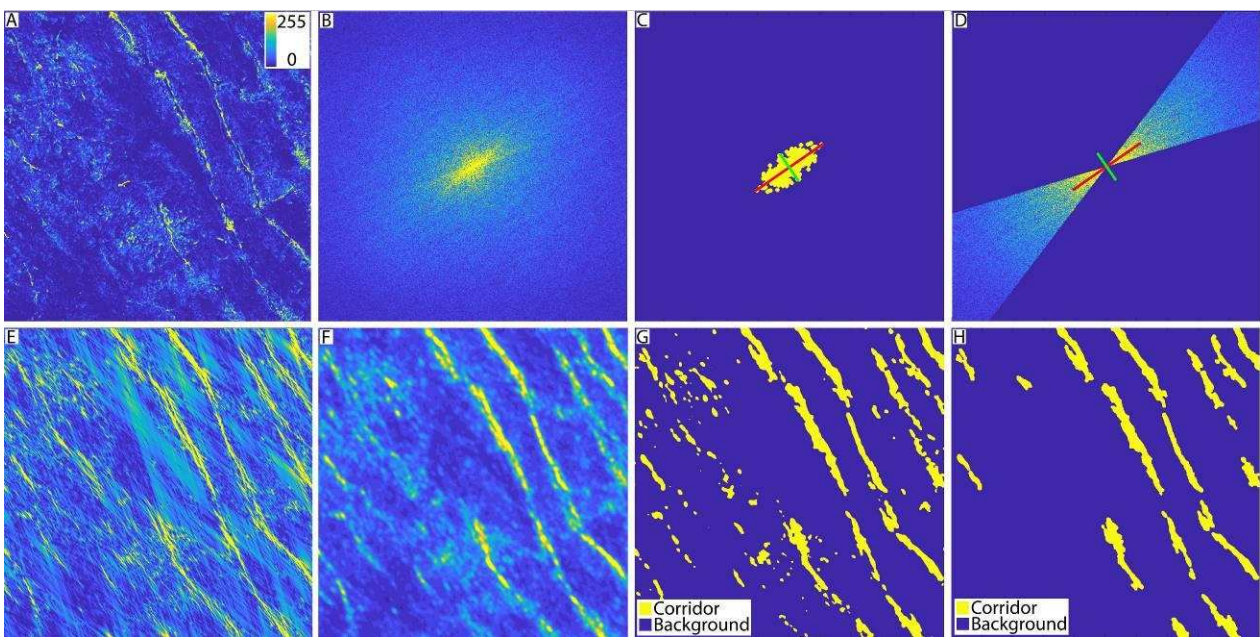
315

316 At regional scales, long axes of hummock corridors are typically observed to
317 have a (sub-) parallel arrangement (e.g. Peterson et al., 2017). We therefore applied
318 a Fast Fourier Transform (FFT) to each enhanced DEM tile to identify the dominant
319 orientation of hummock corridors and remove misaligned features. FFTs are
320 commonly used in image analysis to identify and remove interference or artefacts
321 and to analyse repeating patterns and extract features (e.g. Van Buren, 1987; Tsai
322 and Hsieh, 1999; Jordan and Schott, 2005; Arrell et al., 2008; Munch et al., 2009). In
323 glaciology, FFTs have been used to map crevasses from remotely sensed images
324 (e.g. Williams et al., 2018) and to automatically derive the spectral signature of
325 mega-scale glacial lineations (MSGs) (Spagnolo et al., 2017).

326

327 The FFT produces a power spectrum array of the enhanced DEM in the
328 frequency domain, with the zero-frequency component (measuring the ‘average’
329 elevation) located at the centre of the array. In the frequency domain, directional
330 features are identified as a concentration of high-intensity pixels (i.e. bright areas),
331 reaching out from the centre, perpendicular to the direction of the feature in the
332 spatial domain (Fig. 8b). We applied a ‘wedge-shaped’ filter to the FFT of the
333 enhanced DEM to extract features aligned with the dominant direction of the image,
334 and reject misaligned features. To automate this process and allow the width and
335 orientation of the wedge filter to vary with each input tile, we extracted the highest
336 2% of the power spectrum, creating a binary mask (Fig. 8c). The shape of this mask
337 varies depending on the ‘strength’ of the directionality in the image. The amplitude
338 distribution of a tile’s FFT (in the 2D frequency domain) generated an ellipse-shaped

339 mask when there were well-defined hummock corridors while less well-defined/ no
 340 corridors resulted in a circular shape. Identifying the start and end points of the long
 341 axis of the mask allowed us to use trigonometry to determine its angle relative to the
 342 x-axis ($\tan(x) = \text{change in } x / \text{change in } y$) and this was used as the orientation input
 343 for the wedge-filter. Next, we calculated the length of the minor-axis and divided it by
 344 three –based on sensitivity analysis – to determine the wedge filter width (i.e. how far
 345 it could deviate from the centreline Fig. 8d). Once the filter had been applied and the
 346 misaligned features removed, the FFT was inverted to return the filtered data back
 347 into the spatial domain (e.g. Fig. 8e).



348
 349 Figure 8. Example of directional filter: (A) DEM tile post-spatial filter and enhancement (but
 350 pre FFT filter) with scale bar representing intensity. (B) FFT power spectrum in the
 351 frequency domain with the 'average' at the centre and the directional trend evident from the
 352 peaks reaching out. (C) FFT mask i.e. highest 2% of the power spectrum with long (red) and
 353 short (green) axes identified. (D) 'Wedge' shaped filter overlain on the FFT – inside the
 354 wedge information is retained whilst outside (blue) is rejected. (E) Tile post spatial and FFT
 355 filtering i.e. data returned to the spatial domain (colour scale limited to intensity of 50 to

356 highlight corridors). (F) Tile post standard deviation and smoothing (colour scale limited to
357 intensity of 20 to highlight corridors). (G) Tile post segmentation. (H) Tile post clean up i.e. a
358 binary image where corridors have a value of 1 (yellow) and the background has a value of 0
359 (blue).

360

361 **3.3 Processing Step Three: Image Segmentation**

362

363 Image segmentation is the final processing stage used to extract hummock
364 corridors. It is commonly used in image processing to divide an image into distinct
365 regions, each containing pixels with similar characteristics e.g. colour or texture (e.g.
366 Haralick and Shapiro, 1985; Ryherd and Woodcock, 1996; Baatz and Schape,
367 2000). Thresholding is the simplest image segmentation technique and produces a
368 binary image with two sections, each containing solely pixels with intensity values
369 either greater or smaller than the threshold. Here, we wished to select a threshold
370 which separates pixels which likely contain hummock corridors (high values) from
371 those which do not (low values). The above steps have been designed to enhance
372 the contrast between these two areas.

373

374 To minimise user input, an automatic method for selecting the threshold was
375 chosen. Here, we used the approach of Otsu (1979) which detects a threshold based
376 on a histogram of pixel intensity values. Otsu's method is optimal when the
377 foreground is distinctly different from the background (e.g. a white object on a black
378 background) and when there is limited intensity variation within each of the two
379 regions. To ensure the best output, we enhanced the difference between hummock
380 corridors and their background further. Standard deviation was used as a measure of
381 topographic roughness, highlighting areas with a high degree of local variations (i.e.

382 'rough' sections of the bed within the hummock corridors where topographic
383 variations had been retained). A 12-by-12 moving average filter was then passed
384 over the residual surface to homogenise the corridors (Fig. 8f).

385

386 The image was then segmented using the threshold determined by the Otsu
387 (1979) method creating a binary image of corridors (with a value of 1) and
388 background (with a value of 0) (Fig. 8g). Next, we applied several post-processing
389 methods to improve the segmentation output (Fig. 8h). To improve the corridors
390 longitudinal completeness, we used a series of morphological operations available in
391 Matlab to bridge gaps ('bwmorph, bridge') in the data. We then filled any interior
392 holes ('imfill, holes') and smoothed the edges (imopen with a disk structuring
393 element). False classifications were recognisable in the data as small 'speckles',
394 objects with low elongation values or objects which did not conform to the dominant
395 orientation. To remove these, we specified several criteria. Firstly, individual objects
396 in the final mask must have (i) an area exceeding 1500 pixels, (ii) an elongation ratio
397 greater than 1.5 (comparison with manual mapping suggests that rough regions with
398 a value less than this are not corridors), and (iii) they must be aligned within +/- 40°
399 of the dominant direction. The last criterion removed erroneous 'patches' since 'real'
400 misaligned features had already been removed by the FFT.

401

402 **3.4 Accuracy Quantification**

403

404 Finally, to quantify how well the automatic output captured 'reality' we
405 undertook an accuracy assessment. Detailed manual mapping of hummock corridors
406 at the three test sites were used as a reference dataset to compare with the

407 automatic output. Hummock corridors were mapped as polygons to allow for direct
408 comparison with the automatic output through on-screen digitization in ArcGIS 10.4.
409 Hummock corridors were identified as regions of hummocks which stood out from
410 the surrounding smooth, streamlined bed, often exhibiting a positive/ negative relief
411 and association with eskers.

412

413 The spatial scale selected for accuracy assessment is important and will likely
414 influence the results (e.g. Dungan, 2002; Stehman and Wickham, 2011). As a first-
415 order measure of accuracy we compared the manual and automatic datasets at the
416 pixel-scale. More detailed analysis at the landform-scale was then performed to
417 assess the methods' utility in reproducing the spatial distribution, pattern and
418 morphology of hummock corridors at an ice-sheet scale. We consider the landform
419 scale accuracy assessment the more appropriate measure for determining the
420 method's ability to provide insight into the formation and evolution of subglacial
421 meltwater pathways.

422

423 **3.4.1 Pixel-scale**

424

425 To compare the datasets at a pixel-scale, the manual and automatic output
426 were overlain and each pixel classified as either:

427

- 428 • True Positive (TP) – positive in the reference and automatic output
- 429 • False Positive (FP) – negative in the reference and positive in the
430 automatic output
- 431 • True Negative (TN) – negative in the reference and automatic output

- 432 • False Negative (FN) – positive in the reference and negative in the
433 automatic output

434

435 where TP represents the location of pixels classified as hummock corridors, FP
436 represents pixels classified as hummock corridors in the automatic but not in the
437 reference (i.e. over-estimation), TN represents background pixels in both data and
438 FN represents pixels classified as hummock corridors in the manual but not in the
439 automatic (i.e. under-estimation). This information was recorded in an error matrix.

440

441 Using this information, we calculated more specific measures of quality:

442

443
$$\text{recall} = \frac{TP}{(TP+FN)} * 100$$
 (equation 1)

444
$$\text{precision} = \frac{TP}{(TP+FP)} * 100$$
 (equation 2)

445

446 where recall indicates how much of the reference data are captured by the automatic
447 output (i.e. ‘completeness’) and precision indicates how much of the automatic
448 output matches the reference data (i.e. ‘correctness’). These measures have been
449 used in remote sensing and OBIA accuracy assessments (e.g. Hillier et al., 2015;
450 Zhang et al., 2015; Pratomo et al., 2017).

451

452 **3.4.2 Landform-scale**

453

454 To quantify landform-scale accuracy, we used region-based precision and
455 recall indicators. The approach was similar to the pixel-scale method described in
456 section 3.4.1, but, instead of overlaying and comparing individual pixels, we

457 compared individual corridors. To achieve this, we first determined our match criteria
458 and mapping direction. A match criteria specifies the minimum overlap required
459 between the manual and automatic mapping before a 'match' is confirmed. This
460 criterion varies in the literature; d'Oleire-Otmanns et al., (2013) consider any overlap
461 a success, Eisank et al., (2014) select a minimum of 50% overlap and Jorge and
462 Brennand (2017) use two criteria (i) a 'morphometric detection rate' requiring a 50%
463 minimum overlap and additional divergence criteria and (ii) a 'general detection rate'
464 requiring a 10% minimum overlap. Here, we select a minimum overlap of 25%. While
465 this is lower than the 50% often used, the size of many of these features is
466 significantly greater than those in the literature above (which is focussed on
467 drumlins) and visual assessment suggests that a minimum 25% match is able to
468 capture the hummock corridors sufficiently.

469

470 The mapping direction determines which way we compare the two datasets –
471 i.e. manual to automatic or automatic to manual. This alternates when calculating
472 precision and recall for region-based measures (Zhang et al., 2015). For recall (i.e.
473 'completeness'), we matched the automatic segments to the reference. Conversely,
474 for precision (i.e. 'correctness'), we matched the reference polygons to the automatic
475 segments. For both recall and precision, corridors which overlapped by greater than
476 the minimum overlap (25%) were classified as true positives, while corridors which
477 were overlapped by less than the minimum overlap or with no overlap, were
478 classified as false positives and false negatives respectively.

479

480

481

482 3.4.3 Morphology

483

484 If we wish to use the output of the automatic method to gain meaningful
485 information about the morphometry of hummock corridors, it is important to assess
486 how well the automatic mapping matches the morphometric characteristics of the
487 manually mapped dataset. Here, we automatically extracted metrics (length and
488 width) for each corridor from both datasets. To obtain the most representative
489 results, pre-processing of the manual and automatic mapping were undertaken to
490 separate corridor networks and individual corridors into discrete features. This was
491 done manually in ArcGIS with care taken to avoid bias in the results by splitting
492 features only where there was obvious evidence of trunk/ tributary corridors, merging
493 (e.g. small pixel bridges), clear change in orientation of features or evidence of
494 elongated sections joining falsely classified 'patches'. The overall clarity of the output
495 may be further improved by separating the 'patches' (i.e. falsely classified sections)
496 from the elongated data (i.e. the hummock corridors) and selectively removing them.

497

498 The length of each corridor was calculated automatically by identifying the
499 furthest two boundary pixels and measuring the straight-line distance between them.
500 As hummock corridors can be long, width was measured using perpendicular
501 transects at 5% intervals along each corridor. An average value was then assigned,
502 ensuring that variations in width were captured for all corridors, regardless of their
503 length. Finally, 'real-length' was approximated by dividing the area of the hummock
504 corridor by its mean width (henceforth referred to simply as 'length').

505

506

507 **4. Results**

508

509 **4.1 Automatic method performance**

510

511 **4.1.1 Pixel-scale assessment**

512 [??] [??]

513 At test site 1 (Table 2), recall was 45% and precision 33%. This was the
514 highest recall value of the three test sites and likely reflects the fact that test site 1
515 contains the longest, widest corridors with the most pronounced relief and clear
516 boundary edges. Test site 2 had a 42% recall and 36% precision. This was the
517 highest precision value of the test sites, indicating the lowest percentage of ‘false’
518 classifications. At test site 3, recall was 16% and precision 6%, which is significantly
519 lower than the other two sites and visual inspection confirms this is because the
520 automatic method misidentifies several large valleys as hummock corridors.

521

522 Table 2. Error matrix showing the number of correctly/ incorrectly identified pixels at each
523 test site. These values were used to calculate further measures of accuracy i.e. precision
524 and recall (equations 1 and 2).

525

		Automatic: Yes	Automatic: No
TS 1	Manual: Yes	31001304 (TP)	37947732 (FN)
	Manual: No	62046071 (FP)	1061300000 (TN)
TS2	Manual: Yes	46188919 (TP)	63775215 (FN)
	Manual: No	81485389 (FP)	1008300000 (TN)
TS3	Manual: Yes	4057104 (TP)	21866102 (FN)
	Manual: No	63649814 (FP)	810426980 (TN)

532

533 **4.1.2 Landform-scale assessment**

534

535 **4.1.2.1 Region-based recall and precision**

536

537 The number of corridors correctly/ incorrectly identified at each test site is
 538 summarised in table 3. These values were used to produce a measure of precision
 539 and accuracy (equations 1 and 2).

540

541 Table 3. Error matrix showing the number of correctly/ incorrectly mapped hummock
 542 corridors at each test site. Results for both matching directions are included i.e. manual to
 543 automatic (for calculating recall) and automatic to manual (for calculating precision) as
 544 manual and automatic datasets do not always have the same number of hummock corridors.

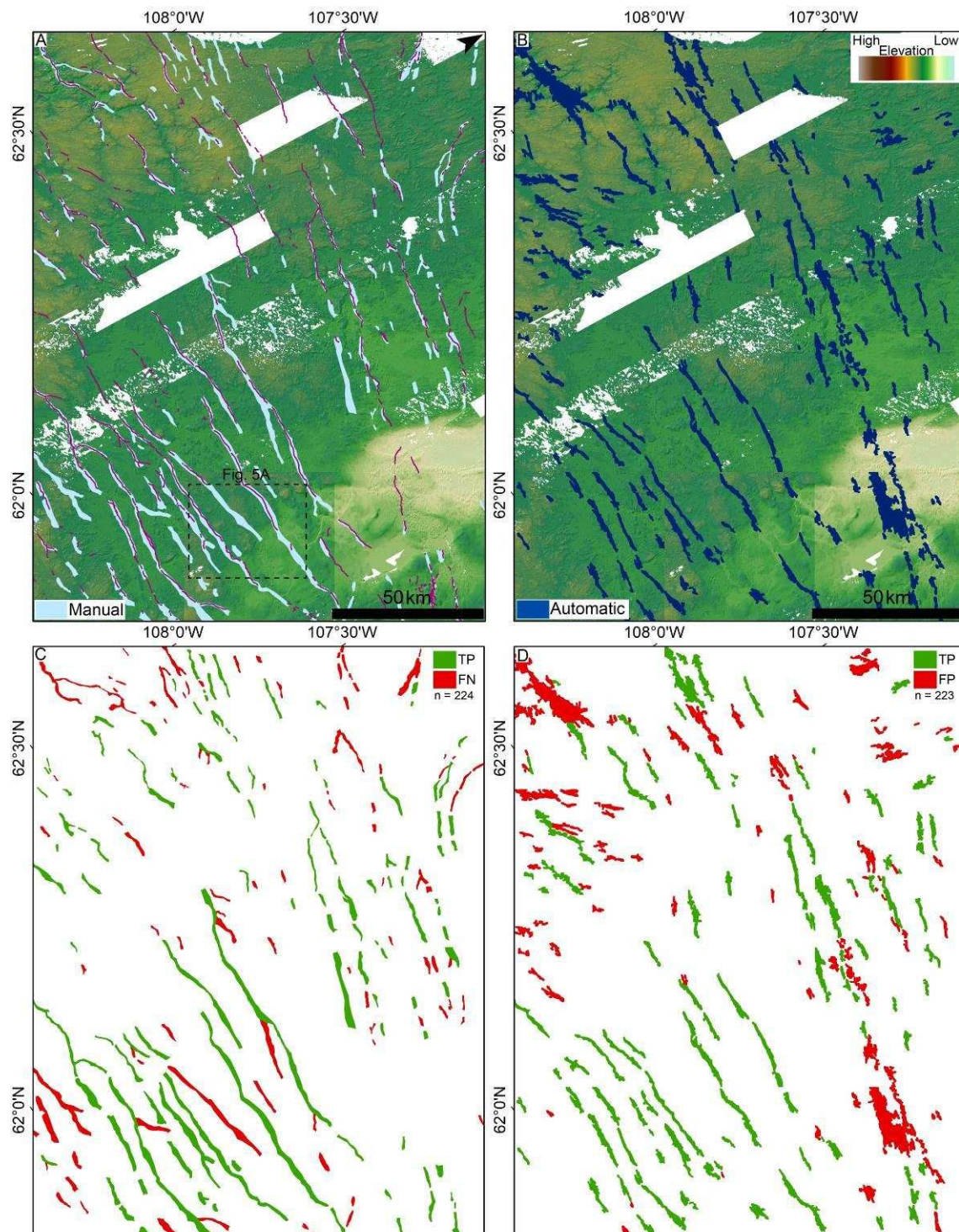
545

		Automatic: Yes	Automatic: No	Total Manual
TS 1 Recall	Manual: Yes	118 (TP)	106 (FN)	224
	Manual: No			
	Total Automatic			
TS 1 Precision	Manual: Yes	108 (TP)		
	Manual: No	115 (FP)		
	Total Automatic	223		
TS 2 Recall	Manual: Yes	194 (TP)	371 (FN)	565
	Manual: No			
	Total Automatic			
TS 2 Precision	Manual: Yes	153 (TP)		
	Manual: No	153 (FP)		
	Total Automatic	306		
TS 3 Recall	Manual: Yes	64 (TP)	105 (FN)	169
	Manual: No			

546
547
548
549
550

TS 3 Precision

Total Automatic		
Manual: Yes	43 (TP)	
Manual: No	150 (FP)	
Total Automatic	193	



551

552 Figure 9. Large-scale manual (a) and automatic (b) mapping of hummock corridors in test
 553 site 1 (near Dubawnt Lake, Canada - former ice-flow from E to W). Manually mapped eskers
 554 are also shown in (a) as pink lines. The success of the method is assessed in (c) and (d).
 555 Corridors which exhibit a > 25% minimum overlap are coloured green (i.e. True Positives –
 556 match in the manual and automatic) while corridors with < 25% minimum overlap are

557 coloured red. In (c) these are False Negatives (i.e. manual corridors missed) and in (d) False
558 Positives (i.e. incorrectly identified automatic corridors). N = the total number of corridors in
559 each group.

560

561 Comparison of the manual and automatic outputs (table 4) indicates a
562 combined recall of 39% and precision of 42%. However, there is considerable inter-
563 test site variation, with site 1 giving the highest recall (53%) and site 2 the lowest
564 (34%). The highest precision is at site 2 (50%) and the lowest at site 3 (22%). In
565 general, the quality of the automatic mapping is improved when compared at the
566 landform scale rather than per pixel, particularly in more complex regions (e.g. site 3
567 – Fig. 11).

568

569 Table 4. Summary of region-based recall and precision measures (equations 1 and 2) by
570 test site using a > 25% minimum overlap criteria.

571

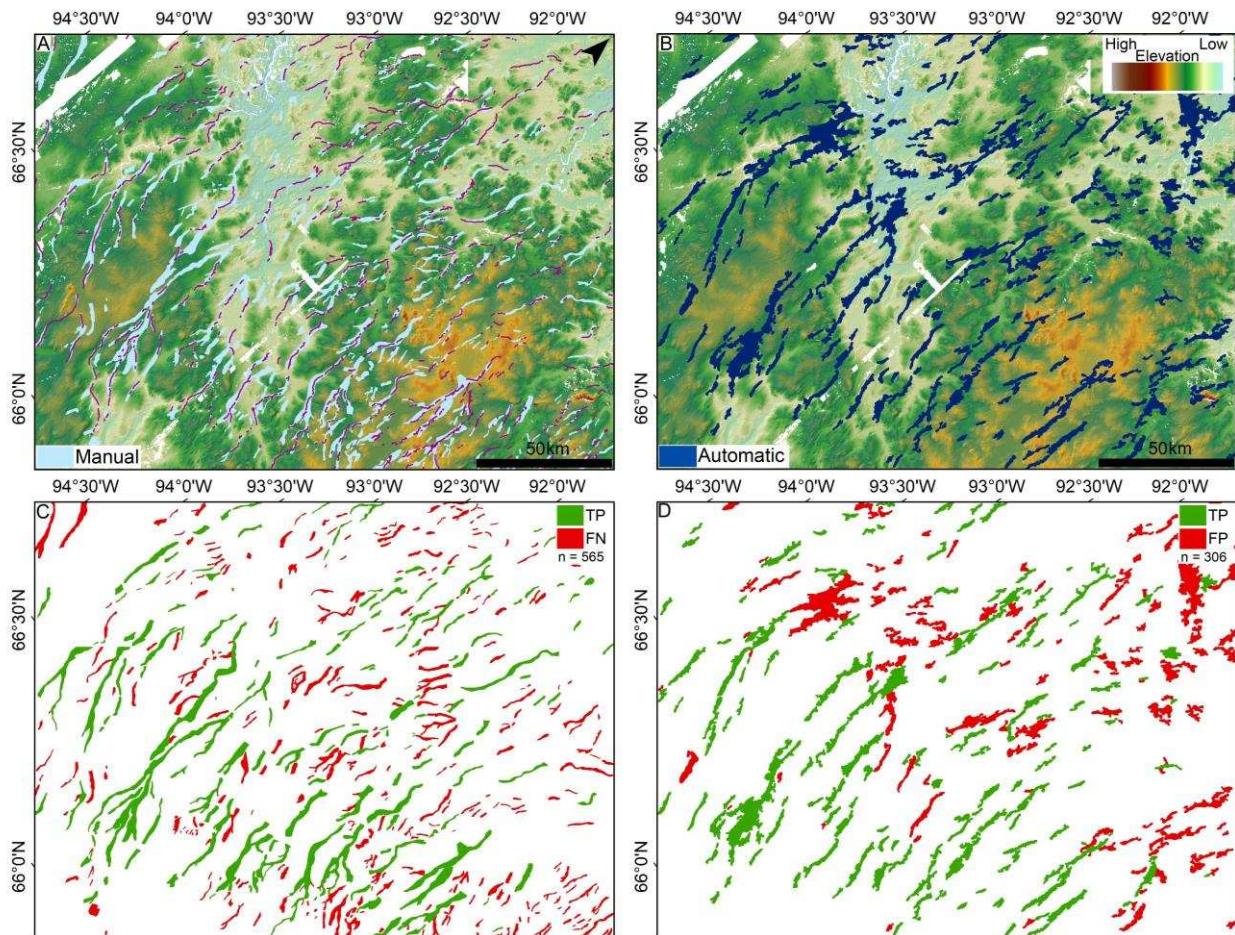
	Recall (%)	Precision (%)
TS1	53	48
TS2	34	50
TS3	38	22
Combined Results	39	42

576

577

578 Manual and automatic mapping for each test site can be seen in Figures 9, 10
579 and 11 (a) and (b) respectively. The outcome of the accuracy assessment can be
580 visualised in (c) and (d) with corridors with > 25% overlap coloured green and those
581 with < 25% overlap coloured red.

582



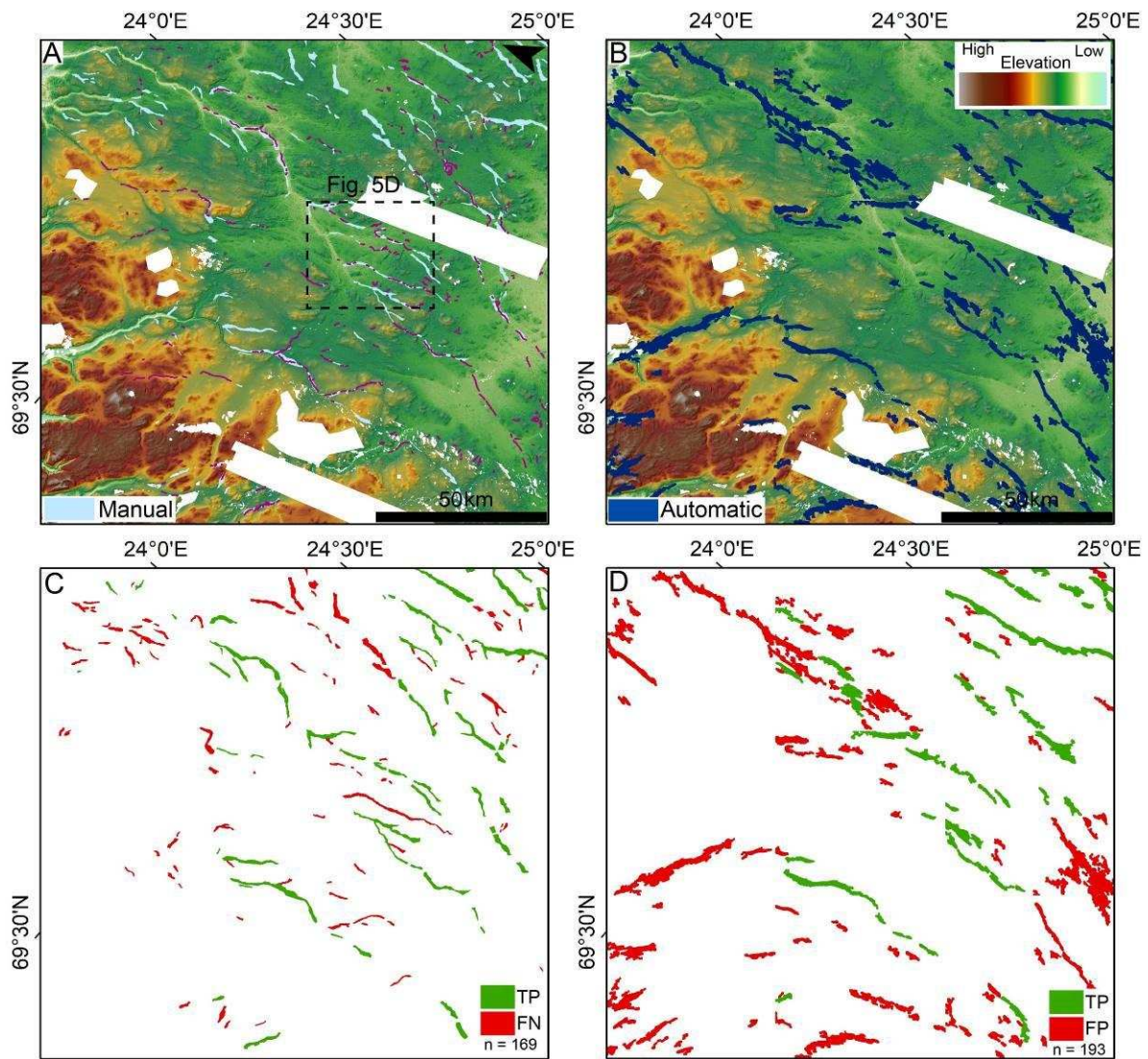
583

584 Figure 10. Large-scale manual (A) and automatic (B) mapping of hummock corridors in test
 585 site 2, Nunavut, Canada (former ice-flow from S to N). Manually mapped eskers are also
 586 shown in (A) as pink lines. The success of the method is assessed in (C) and (D). Corridors
 587 which exhibit a > 25% minimum overlap are coloured green (i.e. True Positives – match in
 588 the manual and automatic) while corridors with < 25% minimum overlap are coloured red. In
 589 (C) these are False Negatives (i.e. manual corridors missed) and in (D) False Positives (i.e.
 590 incorrectly identified automatic corridors). N = the total number of corridors in each group.

591

592 Results indicate that the automatic method can capture corridors of varying
 593 morphology, including those with positive and negative relief and branching
 594 networks. Automatically detected hummock corridors can be traced over significant
 595 distances, even when the features curve across the landscape or cross DEM tile

596 boundaries. However, it is also clear that the corridors missed in the automatic
 597 output are often narrower and 'finer-scale' in expression i.e. they have more subdued
 598 relief, fewer, more widely distributed or smaller individual hummocks, or they are
 599 separated by bounding sections of flat-bed that are unlikely to be detected.



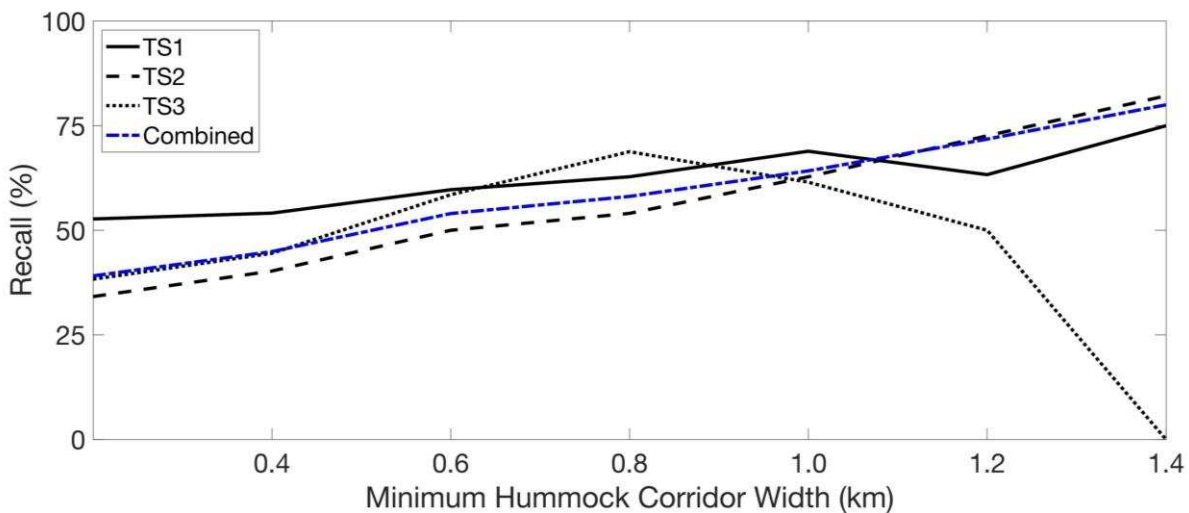
600

601 Figure 11. Large-scale manual (A) and automatic (B) mapping of hummock corridors
 602 in test site 3, northern Scandinavia (former ice-flow from S to N). Manually mapped eskers
 603 are also shown in (A) as pink lines. The success of the method is assessed in (C) and (D).
 604 Corridors which exhibit a > 25% minimum overlap are coloured green (i.e. True Positives –
 605 match in the manual and automatic) while corridors with < 25% minimum overlap are

606 coloured red. In (C these are False Negatives (i.e. manual corridors missed) and in (D)
607 False Positives (i.e. incorrectly identified automatic corridors). N = the total number of
608 corridors in each group.

609

610 Given that the automatic method under-detects narrower corridors, we
611 explored whether there was a critical value below which the method was less able/
612 unable to detect features. This was investigated by evaluating the recall value (i.e.
613 percentage of the manually mapped corridors correctly identified) as minimum
614 corridor width was increased (Fig. 12). Corridor detection rate increased from 39%
615 for all corridors to 80% when just corridors wider than 1.4 km were considered.
616 Recall values increased roughly linearly with corridor width at test sites 1 and 2. At
617 test site 3, recall values increased up until ~0.6 km whereupon they started to drop
618 again. This is attributed to the narrower corridors at this site, with only two corridors
619 wider than 1.2 km.



620

621 Figure 12. Change in recall value as minimum width of hummock corridors included in the
622 calculation increases (all to only > 1.4 km).

623 As the automatic output does a better job at detecting wider corridors, we also
624 calculated the overall area of correctly identified corridors. At test site 1, the corridors
625 identified as true positives account for 69% of the total area of manually mapped
626 corridors. Similarly, the corridors identified as true positives account for 64% and
627 62% of the total area for test sites 2 and 3 respectively. Therefore, while 50 - 60% of
628 the corridors are missed by the automatic approach (Table 4), the corridors that
629 match represent a higher proportion of the overall area. This suggests that the
630 automatic method is capable of approximating the large-scale distribution and
631 pattern of hummock corridors, even though some of the finer-scale detail is lost.

632

633 **4.1.2.2 Morphology**

634

635 The length and width of hummock corridors in the manual and automatic
636 outputs are first compared by investigating their frequency distributions (Fig. 13) and
637 descriptive statistics (Table 5). The manual mapping and automatic mapping display
638 similarity in these distributions, including a positive skew indicating a high abundance
639 of shorter (less than 10 km) and narrower (less than 2 km) hummock corridor
640 segments. In general, the mean and median are similar, particularly for the combined
641 data set (~ 1,000 corridor segments for all 3 sites) and for corridor length.

642

643

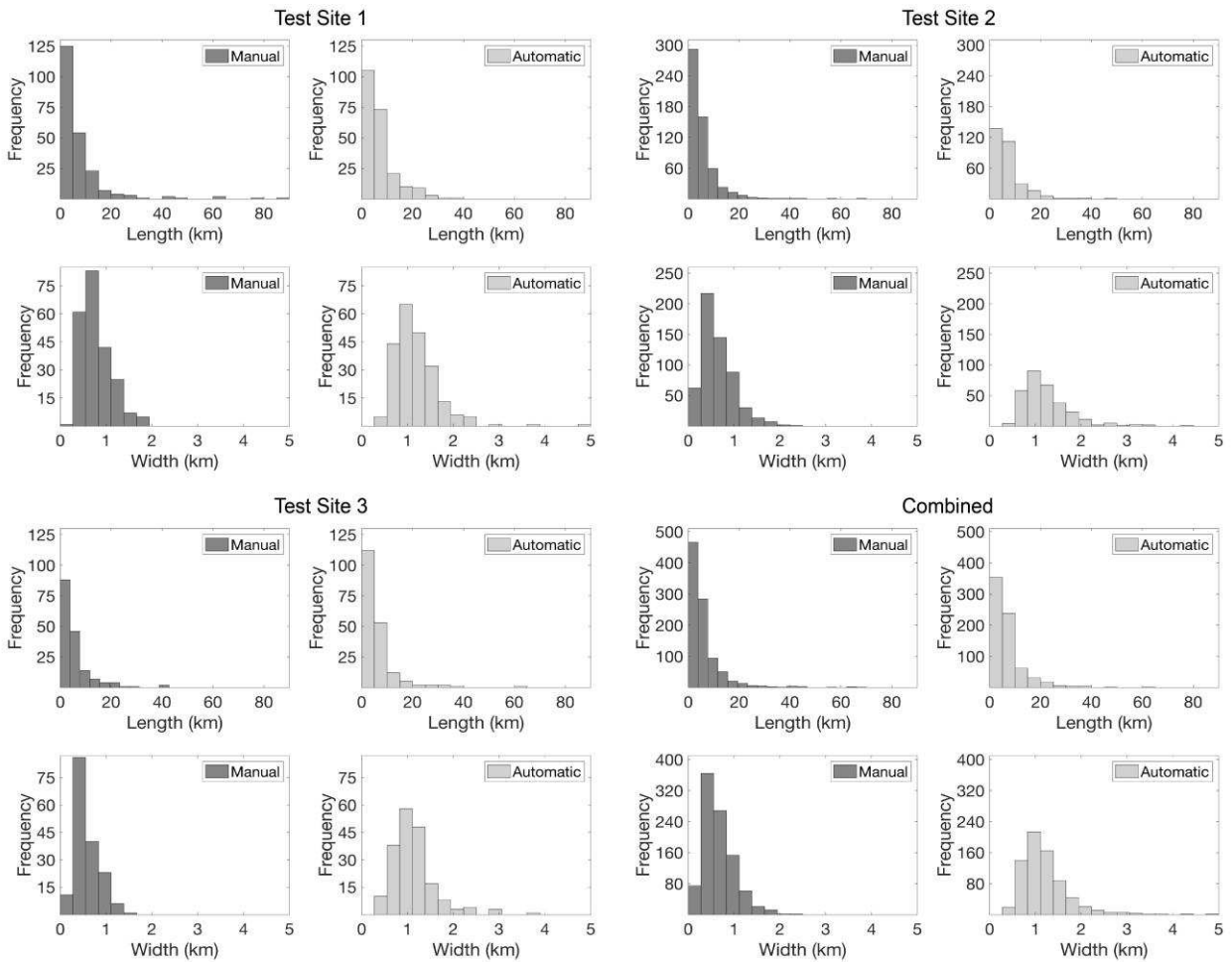
644

645

646

647

648



649

650 Figure 13. Frequency distribution of automatic and manually mapped hummock corridor
 651 real- length and width for each test site. (Width bins of 5 km for length and 0.2 km for width.)

652

653 Nonetheless, there are also some differences between the manual and
 654 automatic metrics; noticeably, a lack of data in the narrowest width bins in the
 655 automatic output, which helps explain the overall higher mean and median widths of
 656 hummock corridors at each test site (Table 5). In section 4.1.2.1, above, we
 657 demonstrate that this systematic under-estimation occurs because the automatic
 658 method struggles to identify narrower corridors.

659

660 The automatic output fails to capture the longest manually mapped segments
 661 as is shown by significantly lower maximum lengths (Table 5). However, in general
 662 the mean and median values for manual and automatic lengths are much closer than
 663 the widths (only varying by 0.7 km and 0.5 km for the combined dataset: n = 958 for
 664 the manual corridors and n = 722 for the automatic). This suggests that the
 665 automatic method does a better job at capturing length than width. A Wilcoxon Rank
 666 Sum Test (equivalent to Mann-Whitney U-Test) was used to test the similarity of the
 667 automatic and manual measurements at each test site. The null hypothesis (i.e. that
 668 the automatic and manual measurements were from distributions with the same
 669 median) was rejected at the 5% significance level for all comparisons, excluding the
 670 automatic and manual lengths at test site 1 (p-value = 0.2056).

671

672 Table 5. Descriptive statistics for manual and automatic mapping (length and width (km)) for
 673 each test site and combined across all three.

674

		Test Site 1		Test Site 2		Test Site 3		Combined	
		Length (km)	Width (km)	Length (km)	Width (km)	Length (km)	Width (km)	Length (km)	Width (km)
Mean	manual	8.1	0.8	5.7	0.6	5.7	0.6	6.3	0.7
	automatic	7.4	1.2	7.1	1.2	6.4	1.1	7.0	1.2
Median	manual	4.6	0.7	3.8	0.6	3.7	0.5	4.0	0.6
	automatic	5.4	1.1	5.3	1.1	4.2	1.1	5.0	1.1
Standard Dev.	manual	11.3	0.3	6.3	0.4	6.2	0.3	7.8	0.3
	automatic	6.2	0.5	6.0	0.5	7.0	0.5	6.3	0.5
Min	manual	1.1	0.2	0.7	0.1	0.8	0.0	0.7	0.0
	automatic	1.1	0.5	1.2	0.5	1.1	0.5	1.1	0.5
Max	manual	90.0	1.9	69.0	2.5	39.2	1.6	90.0	2.5
	automatic	35.9	4.9	46.4	4.4	61.3	3.9	61.3	4.9

675

676

677

678 **5. Discussion**

679

680 **5.1 Overall performance**

681

682 Our approach has facilitated the identification and mapping of almost 1,000
683 hummock corridor segments across 82,500 km², largely reproducing their overall
684 distribution (i.e. successfully capturing 69%, 64% and 62% of their total area at each
685 test site) and morphometry compared to manual mapping (i.e. largely reproducing
686 the length/ width distributions). The output of this study provides insight into the
687 expression and variation of these features, and contributes to an increasing body of
688 literature on them (e.g. St-Onge, 1984; Rampton, 2000; Utting et al., 2009; Sharpe et
689 al., 2017; Peterson and Johnson, 2018).

690

691 The output of the automatic method has created a near-continuous map of
692 hummock corridors which aligns hummock corridor segments across adjacent
693 ArcticDEM tile boundaries and is able to recreate the general pattern across a large
694 area. While some of the finer detail is lost, this method nevertheless has value for
695 rapidly (< 80 seconds per 50 x 50 km² 5m resolution tile, run on the University of
696 Sheffield High Performance Computer cluster – Iceberg – with a specified memory of
697 32 GB) assessing significant volumes of data and providing information on hummock
698 corridor distribution and spatial arrangement and extracting information on
699 morphometry. Furthermore, assessing many hummock corridors across significant
700 areas makes it more likely that we will capture a more representative dataset and
701 allows us to assess their association with other bed features.

702

703 **5.2 Limitations**

704

705 **5.2.1 Hummock corridor morphology**

706

707 Despite progress in the automatic detection and mapping of subglacial
708 bedforms, several limitations exist which need to be acknowledged before assessing
709 and using the output. The automatic method fails to identify all the manually mapped
710 hummock corridors across the three test sites. While this does not appear to
711 influence our understanding of the general location nor the large-scale trends of
712 hummock corridors (i.e. general direction, length and width) or their association with
713 other bedforms, it does suggest that some detail is being lost.

714

715 Further exploration of the reasons for this suggests that hummock corridor
716 morphology influences whether they are detected and retained in the final output.
717 The automatic output is sensitive to hummock corridor width, with detection rates
718 increasing as corridor width increases (from 39% when all corridors are included to
719 64% for corridors wider than 1 km and up to 80% for corridors greater than 1.4 km).
720 It is likely that narrower corridors are removed during the filtering stages or when the
721 data resolution is reduced and the results smoothed. Many of the wider corridors are
722 also longer and this highlights issues related to the discontinuous nature of
723 hummock corridors. Hummock corridor segments detected automatically likely
724 represent parts of a larger corridor/ network of corridors, fragmented because of
725 'real' gaps in the corridor (e.g. areas of flat bed or areas with too few hummocks to
726 be detected/ retained) or because of the side-effects of processing prior to metric
727 extraction (i.e. separating trunk/ tributary corridors). This means that they should be

728 taken as a minimum hummock corridor length and should we choose to interpolate
729 between segments, it is likely that the hummock corridors would reach greater
730 lengths and form more complete networks. Assessing the automatic map of
731 hummock corridors without interpolating between the segments, means that we are
732 unlikely to capture the full length of the manual mapping as a single, complete
733 feature. The gaps along flow may be a possible reason for not detecting more
734 complete corridors despite increased widths.

735

736 **5.2.2 Background conditions**

737

738 As hummock corridor morphology cannot fully explain why corridors were/
739 were not detected, we must also consider other possible causes for imperfect
740 detection (rates below 100%). One such consideration is differences in surface
741 roughness across the bed. Hummock corridors display variations in expression (e.g.
742 relief, definition, hummock density) both within and across sites and this makes it
743 difficult to develop a method which can automatically detect all of them whilst also
744 minimising false classifications. Despite our best efforts to filter out the background,
745 confounding roughness elements are sometimes retained. Large sections of the bed
746 surrounding test site 3 in northern Scandinavia have greater variation in relief than
747 those in Canada and there is more likely to be evidence of human activities. These
748 areas of confounding roughness may be classified as hummock corridors regardless
749 of their possible lack of exposure to subglacial meltwater flow, especially if they
750 exhibit characteristics comparable with the pre-defined criteria for hummock
751 corridors. Similarly, other background features such as fluvial channels and
752 geologically controlled landforms may also be classified as hummock corridors. This

753 is a particular problem when these features have a 'stronger' directional trend than
754 any hummock corridors in the same tile skewing the FFT wedge filter and thus
755 inadvertently removing hummock corridors. It is possible that these features are part
756 of the same subglacial hydrological network (e.g. Fig. 5D); however, if they are not,
757 inclusion of additional steps such as overlying the automatic output on the DEM/
758 geology map would allow the user to manually identify erroneous areas (often by
759 shape and size) and assess case by case whether these should be deleted or
760 retained.

761

762 **5.2.3 Manual mapping and Accuracy Quantification Methods**

763

764 It is important to acknowledge the subjectivity and limitations of manually
765 mapping hummock corridors in general, especially those on complex backgrounds or
766 those which form part of a larger glaciofluvial complex where boundaries are unlikely
767 to be discrete. Some of the hummock corridors observed across the study sites are
768 less pronounced in terms of their overall relief and/ or the relief/ number of the
769 hummocks within them making them difficult to manually map. It is therefore unlikely
770 that the automatic method will be able to capture these either given that the filtering
771 and coarsening steps remove some detail. It is also likely that individual manual
772 mappers would map these differently. As such, manual mapping is not necessarily
773 'true' nor should we expect the automatic method to reproduce it perfectly.

774

775 Furthermore, instead of just missing corridors, there are examples from the test
776 sites where the automatic method can differentiate hummock corridors from complex
777 backgrounds, even identifying some which were missed/ incompletely mapped by

778 the manual mapping. Ultimately, the automatic method relies on pre-defined
779 decision-making criteria which determine the eventual mapping of corridors. This
780 means that the results are consistent, repeatable and defensible (Saha et al., 2011).

781

782 Finally, we must also consider how we interpret the accuracy measures when
783 determining how well the automatic output fits the reference data. While it is useful
784 for providing a quantitative summary of how many corridors are detected at each
785 site, it does not consider additional factors which are relevant here. For example,
786 individual inspection of corridor segments suggests that in some cases, using a
787 minimum of 25% meant that some 'real' corridors were incorrectly missed.
788 Furthermore, the method gives equal weighting to every corridor, regardless of its
789 size.

790

791 **5.3 Future work**

792

793 **5.3.1 Methodological developments**

794

795 Depending on the desired use and output of this method, several steps can be
796 undertaken to enhance the results, should they be required. For example, mapping
797 can be compared to geological maps, maps of water bodies and maps of other
798 subglacial bedforms (e.g. rogen moraines, tunnel valleys etc.) which may have been
799 misclassified as hummock corridors by the automatic method. Furthermore, visually
800 assessing the output in a GIS software will draw the eye to areas which are
801 particularly 'blocky' in nature and which clearly stand out. The user can then make
802 their own decision as to whether this information should be removed.

803 Visual assessment of the results suggests that misidentification is typically
804 associated with narrower features or additional features on the bed exhibiting strong
805 directional trends, such as fluvial channels in test site 3, or in some cases linear
806 tracts of drumlins. Future work may reduce the influence of this for example, by
807 trialling the code on different resolution data or by using different sized sample tiles.
808 Determining the scale at which the hummock corridors remain aligned may allow the
809 user to alter the input tile size as a way of reducing the likelihood of additional
810 directional features influencing the FFT filter.

811

812 **5.3.2 Applications**

813

814 Within the test sites, there is a clear association between hummock corridors and
815 other subglacial meltwater landforms. For example, at test site 1, the down-flow
816 transition from tunnel valleys to hummock corridors coincides with an increase in
817 elevation of approximately 30 m (Fig. 5A). At test sites 1 and 2 there is a striking
818 similarity in the overall pattern and distribution of eskers (Storrar et al., 2014) and
819 hummock corridors (Fig. 9 - 11). By running the automatic method over a large
820 section of northern Canada, we will be able to compare the general distribution and
821 pattern to that of eskers at an ice-sheet scale. The output of this can be used to
822 guide more detailed manual mapping, significantly reducing mapping time by
823 drawing the eye to areas of interest, after which the manual mapper can 'fill in the
824 gaps'. While this method is yet to be tested on other features, theoretically it should
825 be possible to use our approach to identify other bedforms which share a predefined
826 horizontal size range and orientation. For example, it may be possible to alter the
827 parameters slightly and use this to map eskers or drumlins.

828 **6. Conclusions**

829

830 This work has been motivated by the large-scale release of high resolution
831 ArcticDEM data which allows subglacial bedforms to be mapped at an
832 unprecedented spatial and temporal scale. Hummock corridors have been widely
833 identified on the beds of palaeo-ice sheets, and the results of our automated
834 mapping method offer the potential to rapidly gain a large amount of information on
835 the morphological characteristics and large-scale distribution of hummock corridors.
836 This will add to the existing literature and can be used to inform the development of
837 hypotheses for hummock corridor formation.

838

839 Given the increasing availability of high-resolution data, there is a need to
840 develop new methods which can rapidly obtain meaningful information directly from
841 DEMs. While automatic mapping may never reach the same level of detail and
842 precision as manual mapping for individual bedforms, it has potential when the main
843 aim is to quantify the large-scale pattern of landforms. In this study, we add to an
844 increasing body of literature on the development of automatic methods for the
845 identification and mapping of palaeo-subglacial bedforms by developing the first
846 automatic method for extracting spatial information on hummock corridors. We apply
847 this method to three test sites across the ArcticDEM and demonstrate that hummock
848 corridors with varying expressions and varying background conditions can be
849 identified. Results suggest that our method can capture the general location and
850 spatial pattern/ distribution of hummock corridors and provides a decent 'first pass'
851 map which can later be refined manually depending on the desired output.

852

853 For this study, the ability to correctly identify each hummock is less important
854 than the method's ability to capture the location and overall pattern of corridors and
855 when considering a large sample size, the results (i.e. Table 5 – combined sites)
856 suggest that the automatic method can accurately characterise their morphology.
857 The next step will be to use this method to map hummock corridors using the
858 ArcticDEM data for Canada and northern Scandinavia, thus gaining unprecedented
859 insight into the large-scale distribution and pattern of hummock corridors and their
860 association with other subglacial bedforms and meltwater features. This will provide
861 evidence for formation theories as well as information which can be used to better
862 understand the distribution and nature of subglacial meltwater flow beneath former
863 and current ice-sheets.

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865

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867

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877

878 **8. Data availability**

879

880 The numerical code developed in this paper is archived at:
881 <https://doi.org/10.15131/shef.data.7999445>.

882

883 **9. References**

884

885 Anderson, R.S. et al., 2004. Strong feedbacks between hydrology and sliding of a
886 small alpine glacier. *Journal of Geophysical Research*. 109(F3).

887

888 Andrews, L.C. Catania, G.A. Hoffman, M.J. Gulley, J.D. Luthi, M.P. Ryser, C.
889 Hawley, R.L. Neumann, T.A. 2014. Direct observations of evolving subglacial
890 drainage beneath the Greenland Ice Sheet. *Nature*. 514(7520): 80-3.

891

892 Arrell, K. Wise, S. Wood, J. Donoghue, D. (2008). Spectral filtering as a method of
893 visualising and removing striped artefacts in digital elevation data. *Earth
894 Processes and Landforms*. 33(6): 943-61.

895

896 Baatz, M. Schäpe, A. (2000) Multiresolution Segmentation: An Optimization
897 Approach for High Quality Multi-Scale Image Segmentation. In: Strobl, J.,
898 Blaschke, T. and Griesbner, G., Eds., *Angewandte Geographische
899 Informations-Verarbeitung, XII*, Wichmann Verlag, Karlsruhe, Germany, 12-
900 23.

901

902 Bartholomew, I. Nienow, P. Mair, D. Hubbard, A. King, M.A. Sole, A. 2010. Seasonal
903 evolution of subglacial drainage and acceleration in Greenland outlet glacier.
904 Nature Geoscience. 3: 408-11.

905

906 Bishop, M.P. Allan James, L. Shroder, J.F. Walsh, S.J. (2012). Geospatial
907 technologies and digital geomorphological mapping: Concepts, issues and
908 research. Geomorphology. 137: 5-26.

909 Boulton, G.S. Clark, C.D. (1990). A highly mobile Laurentide Ice Sheet revealed by
910 satellite images of glacial lineations. Nature. 346: 813-17.

911 Boulton, G.S. Dobbie, K.E. Zatsepin, S. 2001. Sediment deformation beneath
912 glaciers and its coupling to the subglacial hydraulic system. Quaternary
913 International. 86: 3-28.

914

915 Burke, M.J. Brennand, T.A. Perkins, A.J. (2011). Erosional corridor evolution in
916 south-central British Columbia: insights from ground-penetrating radar
917 surveys. Proceedings of Geohydro 2011.

918

919 Chandler, D.M. Wadham, J.L. Lis, G.P. Cowton, T. Sole, A. Bartholomew, I. Telling,
920 J. Nienow, P. Bagshaw, E.B. Mair, D. Vinen, S. Hubbard, A. 2013. Evolution
921 of the subglacial drainage system beneath the Greenland Ice Sheet revealed
922 by tracers. Nature Geoscience. 6.

923 Clark, C.D. Evans, D.J.A. Khatwa, A. Bradwell, T. Jordan, C.J. Marsh, S.H. Mitchell,
924 W.A. Bateman, M.D. (2004). Map and GIS database of glacial landforms and
925 features related to the British Ice Sheet. Boreas. 33: 359-75.

926 Clark, C.D. Hughes, A.L.C. Greenwood, S.L. Jordan, C. Sejrup, H.P. (2012). Pattern
927 and timing of retreat of the last British-Irish Ice Sheet. *Quaternary Science*
928 *Reviews*. 44: 112-46.

929 Clark, C.D. Livingstone, S.J. (2018). Glacial curvilineations found along the southern
930 sector of the Laurentide Ice sheet and a hypothesis of formation involving
931 subglacial slope failure in tunnel valleys and subglacial lakes. *Earth Surface*
932 *Processes and Landforms*. 43(7): 1518-1528.

933 Clark, P.U. Walder, J.S. (1994). Subglacial drainage, eskers and deforming beds
934 beneath the Laurentide and Eurasian ice sheets. *Geol. Soc. Am. Bull.* 106:
935 304-14.

936 d'Oleire-Oltmanns, S. Eisank, C. Dragut, L. Blaschke, T. (2013). An object-based
937 workflow to extract landforms at multiple scales from two distinct data types.
938 *IEEE Geoscience and Remote Sensing Letters*. 10(4): 947-51.

939 Dungan, J.L. (2002). Toward a comprehensive view of uncertainty in remote sensing
940 analysis. In *Uncertainty in Remote Sensing and GIS*, G.M. Foody and P.M.
941 Atkinson (Eds). Pp 25-35. (Chichester, UK: Wiley).

942 Dyke, A.S. Prest, V.K. (1987). Late Wisconsinan and Holocene history of the
943 Laurentide ice sheet. *Geog. Phys. Quat.* 41: 237-64.

944 Eisank, C. Smith, M.J. Hillier, J.K. (2014). Assessment of multiresolution
945 segmentation for delimiting drumlins in digital elevation models.
946 *Geomorphology*. 214: 452-64.

947 Evans, D.J.A. Clark, C.D. Mitchell, W.A. (2005). The last British Ice Sheet: a review
948 of the evidence utilised in the compilation of the Glacial Map of Britain. *Earth*
949 *Science Reviews*. 70: 253-312.

950 Evans, I.S. (2012). Geomorphometry and landform mapping: what is a landform?
951 *Geomorphology*. 137: 94-106.

952 Foroutan, M. Zimbelman, J.R. (2017). Semi-automatic mapping of linear-trending
953 bedforms using 'Self-Organising Maps' algorithm. *Geomorphology*. 293(A):
954 156-66.

955 Greenwood, S.L. Clark, C.D. (2008). Subglacial bedforms of the Irish Ice Sheet.
956 *Journal of Maps*. 4(1): 325-57.

957 Greenwood, S.L. Clark, C.D. Hughes, A. (2007). Formalising an inversion
958 methodology for reconstructing ice-sheet retreat patterns from meltwater
959 channels: application to the British Ice Sheet. *Journal of Quaternary Science*.
960 22: 637-45.

961 Haralick, R. Shapiro, L. (1985). Image segmentation techniques. *Computer Vision,*
962 *Graphics, and Image Processing*. 29: 100-32.

963 Hillier, J.K. Smith, M. (2008). Residual relief separation: digital elevation model
964 enhancement for geomorphological mapping. *Earth Surface Processes and*
965 *Landforms*. 33: 2266-76.

966 Hillier, J.K. Smith, M. Armugam, R. Barr, I. Boston, CM. Clark, C.D. Ely, J. Fankl, A.
967 Greenwood, S.L. Gosselin, L. Hättestrand, C. Hogan, K. Hughes, A.L.C.
968 Livingstone, S.J. Lovell, H. McHenry, M. Muñoz, Y. Pellicer, X.M. Pellitero, R.

969 Robb, C. Roberson, S. Ruther, D. Spagnolo, M. Standell, M. Stokes, C.R.
970 Storrar, R. Tate, N.J. Wooldridge, K. (2015). Manual mapping of drumlins in
971 synthetic landscapes to assess operator effectiveness. *Journal of Maps*.
972 11(5): 719-29.

973 Hillier, J.K. Watts, A.B. (2004). "Plate-like" subsidence of the East Pacific Rise-South
974 Pacific superswell system. *Geomagnetism and Paleomagnetism/ Marine*
975 *Geology and Geophysics*. 109(B10).

976 Hughes, A. Clark, C.D. Jordan, C. (2010). Subglacial bedforms of the last British ice
977 sheet. *Journal of Maps*. 543-63.

978 Iken, A. 1981. The effect of subglacial water pressure on the sliding velocity of a
979 glacier in an idealized numerical model. *Journal of Glaciology*. 27 (97): 407-
980 21.

981

982 Jordan, G. Schott, B. (2005). Application of wavelet analysis to the study of spatial
983 pattern of morphotectonic lineaments in digital terrain models. A case study.
984 *Remote Sensing of Environment*. 94: 31-38.

985

986 Jorge, M.G. Brennand, T.A. (2017). Semi-automated extraction of longitudinal
987 subglacial bedforms from digital terrain models – Two new methods.
988 *Geomorphology*. 288: 148-63.

989 Kleman, J. (1992). The palimpsest glacial landscape in north-west Sweden.
990 *Geografiska*. 74A: 306-25.

- 991 Kleman, J. Borgstrom, I. (1996). Reconstruction of palaeo-ice sheets: the use of
992 geomorphological data. *Earth Surface Processes and Landforms*. 21: 893-
993 909.
- 994 Kleman, J. Glasser, N.F. (2007). The subglacial thermal organisation (STO) of ice
995 sheets. *Quaternary Science Reviews*. 26(5-6): 585-97.
- 996 Livingstone, S.J. Clark, C.D. (2016). Morphological properties of tunnel valleys of the
997 southern sector of the Laurentide Ice Sheet and implications for their
998 formation. *Earth Surface Dynamics*. 4: 567-89.
- 999 Livingstone, S.J. Utting, D.J. Ruffell, A. Clark, C.D. Pawley, S. Atkinson, N. Fowler,
1000 A.C. (2016). Discovery of relict subglacial lakes and their geometry and
1001 mechanism of drainage. *Nature Communications*. 7. 11767.
- 1002 Makinen, J. Kajuutti, K. Palmu, J.-P. Ojala, A. Ahokangas, E. (2017). Triangular-
1003 shaped landforms reveal subglacial drainage routes in SW Finland.
1004 *Quaternary Science Reviews*. 164: 37-53.
- 1005 Margold, M. Jansson, K.N. Kleman, J. Stroeve, A.P. Clague, J.J. (2013). Retreat
1006 pattern of the Cordilleran Ice Sheet in central British Columbia at the end of
1007 the last glaciation reconstructed from glacial meltwater landforms. *Boreas*. 42:
1008 830-47.
- 1009 Margold, M. Stokes, C.R. Clark, C.D. (2015). Ice streams in the Laurentide Ice
1010 Sheet: Identification, characteristics and comparison to modern ice sheets.
1011 *Earth Science Reviews*. 143: 117-46.

- 1012 Munch, B. Trtik, P. Marone, F. Stampanoni, M. (2009). Stripe and ring artefact
1013 removal with combined wavelet – Fourier filtering. *Optic Express*. 17(10):
1014 8567-91.
- 1015 Noh, M-J. Howat, I.M. (2015). Automated stereo-photogrammetric DEM generation
1016 at high latitudes: Surface Extraction with TIN-based Search-space
1017 Minimization (SETSM) validation and demonstration over glaciated regions.
1018 *GIScience and Remote Sensing*. 52(2): 198-217.
- 1019 Ó Cofaigh, C., Stokes, C.R. (2008). Reconstructing ice-sheet dynamics from
1020 subglacial sediments and landforms: introduction and overview. *Earth Surface
1021 Processes and Landforms* 33(4): 495-502.
- 1022 Otsu, N. (1979). A threshold selection method from gray-level histograms. *IEEE
1023 Transactions on Systems, Man, and Cybernetics*. SMC-9.
- 1024 Ottesen, D. Stokes, C.R. Rise, L. Olsen, L. (2008). Quaternary ice-sheet dynamics
1025 and ice streaming along the coastal parts of northern Norway. *Quaternary
1026 Science Reviews*. 27: 19.
- 1027 Peterson, G. Johnson, M.D. Colby, A. Smith. (2017). Glacial geomorphology of the
1028 south Swedish uplands – focus on the spatial distribution of hummock tracts.
1029 *Journal of Maps*. 13(2): 534-44.
- 1030 Peterson, G. Johnson, M.D. Dahlgren, S. Pässe, T. Alexanderson, H. (2018).
1031 Genesis of hummocks found in tunnel valleys: an example from Hörda,
1032 southern Sweden. *GFF*. 140(2): 189-201.

- 1033 Peterson, G. Johnson, M.D. (2018). Hummock corridors in the south-central sector
1034 of the Fennoscandian ice sheet, morphometry and pattern. *Earth Surface*
1035 *Processes and Landforms*. 43: 919-29.
- 1036 Pratomo, J. Kuffer, M. Martinez, J. Kohli, D. (2017). Coupling uncertainties with
1037 accuracy assessment in object-based slum detection case study: Jakarta,
1038 Indonesia. *Remote Sensing*. 9(11).
- 1039 Rampton, V.N. (2000). Large-scale effects of subglacial meltwater flow in the
1040 southern Slave Province, Northwest Territories, Canada. *Canadian Journal of*
1041 *Earth Sciences*. 37(1): 81–93.
- 1042
- 1043 Ryherd, S. Woodcock, C.E. (1996). Combining spectral and texture data in the
1044 segmentation of remotely sensed images. *Photogrammetric Engineering and*
1045 *Remote Sensing*. 62(2): 181-94.
- 1046
- 1047 Saha, K. Wells, N.A. Munro-Stasiuk, M. (2011). An object-orientated approach to
1048 automated landform mapping: A case study of drumlins. *Computers and*
1049 *Geosciences*. 37(9): 1324-36.
- 1050
- 1051 Schoof, C., 2010. Ice-sheet acceleration driven by melt supply variability. *Nature*.
1052 468(7325): 803–6.
- 1053
- 1054 Sharp, M. Gemmel, J. Tison, J. (1989). Structure and stability of the former
1055 subglacial drainage system of the Glacier de Tsanfleuron, Switzerland. *Earth*
1056 *Surface Processes and Landforms*. 14(2): 119-134.

1057

1058 Sharpe, D. Kjarsgaard, B. Knight, R.D. Russell, H.A.J. Kerr, D.E. (2017). Glacial
1059 dispersal and flow history, East Arm area of Great Slave Lake, NWT, Canada.
1060 Quaternary Science Reviews. 165: 49-72.

1061

1062 Sjogren, D.B. Fisher, T.G. Taylor, L.D. Jol, H.M. Munro-Stasiuk, M.J. 2002. Incipient
1063 tunnel channels. Quaternary International. 90: 41-56.

1064

1065 Smith, M.J. Clark, C.D. (2005). Methods for the visualisation of digital elevation
1066 models for landform mapping. Earth Surface Processes and Landforms.
1067 30(7): 885-900.

1068

1069 Spagnolo, M. Bartholomaus, T.C. Clark, C.D. Stokes, C.R. Atkinson, N. Dowdeswell,
1070 J.A. Ely, J.C. Graham, A.G.C. Hogan, K.A. King, E.C. Larter, R.D.
1071 Livingstone, S.J. Pritchard, H.D. (2017). The periodic topography of ice
1072 stream beds: Insights from the Fourier spectra of mega-scale glacial
1073 lineations. Journal of Geophysical Research: Earth Surface. 122(7): 1355-
1074 1373.

1075 Stehman, S.V. Wickham, J.D. (2011). Pixels, blocks of pixels, and polygons:
1076 Choosing a spatial unit for thematic accuracy assessment. Remote Sensing of
1077 the Environment. 115(12): 3044-55.

1078 Stokes, C.R. Clark, C.D. (1999). Geomorphological criteria for identifying Pleistocene
1079 ice streams. Annals of Glaciology. 28: 67-74.

- 1080 Stokes, C.R. et al., (2015). On the reconstruction of palaeo-ice sheets: Recent
1081 advances and future challenges. *Quaternary Science Reviews*. 125: 15-49.
- 1082 St-Onge, 1984. Surficial deposits of the Redrock Lake area, District of Mackenzie; in
1083 Current Research, Part A, Geological Survey of Canada, Paper 84 (1A): 271-
1084 78.
- 1085
- 1086 Storrar, R.D. Livingstone, S.J. (2017). Glacial geomorphology of the northern Kivalliq
1087 region, Nunavut, Canada, with an emphasis on meltwater drainage systems.
1088 *Journal of Maps*. 13(2): 153-64.
- 1089 Storrar, R.D. Stokes, C.R. Evans, D.J.A. (2014). Increased channelisation of
1090 subglacial drainage during deglaciation of the Laurentide Ice Sheet. *Geology*.
1091 42(3): 239-42.
- 1092 Storrar, R.D. Stokes, C.R. Evans, D.J.A. (2014). Morphometry and pattern of a large
1093 sample (>20,000) of Canadian eskers and implications for subglacial drainage
1094 beneath ice sheets. *Quaternary Science Reviews*. 105: 1-25.
- 1095 Tedstone, A.J. Nienow, P.W. Gourmelon, N. Dehecq, A. Goldberg, D. Hanna, E.
1096 2015. Decadal slowdown of a land-terminating sector of the Greenland Ice
1097 Sheet despite warming. *Nature*. 526: 692-695.
- 1098 Tsai, D.M. Hsieh, C.Y. (1999). Automated surface inspection for directional textures.
1099 *Image and Vision Computing*. 18:49-62.
- 1100 Utting, D.J., Ward, B.C. & Little, E.C. (2009). Genesis of hummocks in glaciofluvial
1101 corridors near the Keewatin Ice Divide, Canada. *Boreas*. 38(3): 471–481.

1102

1103 Van Buren, D. (1987). Fourier removal of stripe artefacts in IRAS images.
1104 Astronomical Journal. 94: 1092- 94.

1105 Van der Vegt, P. Janszen, A. Moscariello, A. (2012). Tunnel Valleys: current
1106 knowledge and future perspectives. In: Husse, M. Reddfern, J. Le Heron, D.P.
1107 Dixon, R.J. Moscariello, A. Craig, J. (Eds), Glaciogenic Reservoirs and
1108 Hydrocarbon Systems. Geological Society Special Publication, vol. 368: 75-
1109 97.

1110 Wessel, P. (1998). An empirical method for optimal robust regional-residual
1111 separation of geophysical data. Journal of Mathematical Geology. 30(4): 391-
1112 408.

1113 Williams, C. O'Leary, M. Luckman, A. Jóhannesson, T. Murray, T. (2018).
1114 Automated crevasse mapping: assisting with mountain and glacier hazard
1115 assessment. Geophysical Research Abstracts. Vol. 20. EGU2018-5137.

1116 Wright, H.E. (1973). Tunnel valleys, glacial surges and subglacial hydrology of the
1117 Superior Lobe, Minnesota. In: Black, R.F. Goldthwait, R.P. and Willman, H.B.
1118 (eds.) The Wisconsin Stage. Geological Society of America, Memoir. 136:
1119 251-76.

1120

1121 Yu, P. Eyles, N. Sookhan, S. (2015). Automated drumlin shape and volume
1122 estimation using high resolution LiDAR imagery (Curvature Based Relief
1123 Separation): A test from the Wadena Drumlin Field, Minnesota.
1124 Geomorphology. 246: 589-601.

1125

1126 Zhang, X. Feng, X. Xiao, P. He, G. Zhu, L. (2015). Segmentation quality evaluation
1127 using region-based precision and recall measures for remote sensing. ISPRS
1128 Journal of Photogrammetry and Remote Sensing. 102: 73-84.