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Workflow Simulation Aware and Multi-Threading Effective Task Scheduling for Heterogeneous Computing

Vasilios Kelefouras

Karim Djemame

Abstract—Efficient application scheduling is critical for achieving high performance in heterogeneous computing systems. This problem has proved to be NP-complete, heading research efforts in obtaining low complexity heuristics that produce good quality schedules. Although this problem has been extensively studied in the past, first, all the related algorithms assume the computation costs of application tasks on processors are available a priori, ignoring the fact that the time needed to run/simulate all these tasks is orders of magnitude higher than finding a good quality schedule, especially in heterogeneous systems. Second, low complexity heuristics consider application tasks as single thread implementations only, but in practice tasks are normally split into multiple threads.

In this paper, we propose two new methods applicable to several task scheduling algorithms, addressing the above problems in heterogeneous computing systems. We showcase both methods by using HEFT well known and popular algorithm, but this work is applicable to other algorithms too, such as HCPT, HPS, PETS and CPOP. First, we propose a methodology to reduce the number of computation costs required by HEFT (and therefore the number of simulations), without sacrificing the length of the output schedule. Second, we give heuristics to find which tasks are going to be executed as Single-Thread and which as Multi-Thread implementations, as well as the number of threads used, without requiring all the computation costs.

The experimental results considering both random graphs and real world applications show that extending HEFT with the two proposed methods achieves better schedule lengths, while at the same time requires from 4.5 up to 24 less simulations.

Keywords-static task scheduling; simulation; multithreading; HEFT; Heterogeneity; multi-core;

I. INTRODUCTION

A well-known strategy for efficient execution of an application on a heterogeneous computing environment is to partition the application into independent tasks and schedule such tasks over a set of available processors [1]. Normally, the application is represented as a Directed Acyclic Graph (DAG), which includes the characteristics of an application program such as the computation costs of the tasks, the data transfer time between tasks and task dependencies. The objective of the Task Scheduling (TS) problem is to map the tasks on the (co)-processors and order their execution so that task precedence requirements are satisfied and a minimum schedule length is obtained (for the remainder of this paper we will refer to both processors and coprocessors as processors). TS can be performed at compile-time or at run-time, referred as static or dynamic scheduling.

Static TS has proven to be NP-complete, even for the homogeneous case. Therefore, research efforts in this field have been mainly focused on obtaining low-complexity heuristics that produce good schedules [2], which is the topic of this paper. Although this problem has been extensively studied in the past, first all the related State of the Art (SotA) algorithms assume the computation costs in the DAG are available a priori, ignoring the fact that the time needed to run/simulate all these tasks is orders of magnitude higher than finding a good quality schedule; this is because the number of simulations/runs required is very large especially for heterogeneous systems where different execution time values occur among different processors. Second, SotA TS heuristics consider application tasks as single thread implementations only, but in practice application tasks are normally split into multiple threads.

In this paper, we propose two new methods addressing the above problems. The first method reduces the number of computation costs required by HEFT and therefore, the number of simulations required/performed, without sacrificing the length of the output schedule. The second method refers to heuristics finding which tasks are going to be executed as Single-Thread (ST) and which as Multi-Thread (MT) implementations, as well as the number of threads used, without requiring all the computation costs in the DAG. We showcase both methods by using HEFT [3] algorithm, but this work is applicable to several TS algorithms such as HCPT [4], HPS [5], PETS [1], CPOP [3].

This work has resulted in three contributions, a) a novel TS methodology reducing the number of simulations performed, b) novel TS heuristics considering tasks as both ST and MT implementations, c) two TS methods applicable to several TS algorithms.

The evaluation of the proposed methods includes a large number of synthetic DAGs as well as five real world applications. The experimental results show that by using the proposed methods, HEFT provides better schedule lengths by facing tasks as both ST and MT implementations, while at the same time requires from 4.5 up to 24 less simulations.

The remainder of this paper is organized as follows. In Section II, we introduce the TS problem. In Section III, the related work is reviewed. The proposed methods are given in Section IV, while the experimental results are discussed in Section V. Finally, Section VI is dedicated to conclusions and future work.

II. TASK SCHEDULING FORMULATION

The problem addressed in this paper is the static scheduling of a single application in a heterogeneous platform with a set P of m processors, either multi/single-core processors or co-processors, with p cores per processor at maximum, that have diverse capabilities. The $n \times m \times p$ computation cost matrix W stores the execution costs of the tasks, where n , is the number of the tasks. Each element $w_{t,j,k} \in W$ refers to the computation cost of task t on processor p_j , when t is split into k threads; if the processor is a co-processor or a single-core processor, $k = 1$. We consider every task as an m -thread implementation, where $m = [1, q]$ and q is the number of cores. The core utilization factor is defined as, $factor_{t,i,k} = w_{t,i,1}/w_{t,i,k}$. The $w_{t,j,k}$ values are found by simulation, emulation or by running the application tasks on the hardware (HW). For the rest of this paper, we will use the word simulation. The computation costs of the tasks are assumed to be monotonic when $k = 1$, but not when $k > 1$. In other words, if $(w_{t1,i,1} \geq w_{t1,j,1})$ for a task $t1$, then $(w_{t,i,1} \geq w_{t,j,1})$, for every task t ; these assumptions differ from the uniform parallel machine scheduling problem. The execution of any task is considered nonpreemptive.

The application is represented by a Directed Acyclic Graph (DAG), $G=(V,E)$, where V is the set of n nodes and each node $u_i \in V$ represents an application task. E is the set of e communication edges between tasks; each $e(i,j) \in E$ represents the task-dependence constraint such that task n_i should complete its execution before task n_j can be started [2]. Each edge $e(i,j) \in E$ is associated with a non negative weight value $d_{i,j}$ that represents the amount of data to be transmitted from task t_i to task t_j .

The communication cost of an edge (t_i, t_j) equals to the amount of data transmitted from task t_i to task t_j ($d_{i,j}$), divided by the data transfer rate of the network which is assumed fixed and constant [6]. Since the data transfer rate of the intra-processor bus is much higher than the data transfer rate of the interprocessor network, the communication cost between two tasks scheduled on the same processor is taken as zero. These model simplifications are common in this scheduling problem [2] [3] [6].

Next, we present some common attributes used in TS problem, which we will refer to in the following sections.

Definition 1: $pred(t_i)$ denotes the set of immediate predecessors of task t_i in a given DAG. A task with no predecessors is called an entry task, t_{entry} .

Definition 2: makespan or schedule length denotes the finish time of the last task in the DAG and is defined ($makespan = \max\{AFT(n_{exit})\}$), where $AFT(n_{exit})$ denotes the Actual Finish Time of the exit node.

Definition 3: $EST(t_i, p_j)$ denotes the Earliest Start Time (EST) of node/task t_i on processor p_j and is defined as

$$EST(t_i, p_j) = \max \left\{ T_{Avail}(p_j), T_{pred}(t_i, p_j) \right\} \quad (1)$$

$$T_{pred}(t_i, p_j) = \max_{t_m \in pred(t_i)} \{AFT(t_m) + c_{(m,i)}\}$$

where $T_{Avail}(p_j)$ is the earliest time at which processor p_j is ready and $T_{pred}(t_i, p_j)$ is the time at which all data needed by task t_i arrive at the processor p_j . The communication cost $c_{m,i}$ is zero if the predecessor node t_m is assigned to processor p_j . For the entry task, $EST(t_{entry}, p_j) = 0$.

Definition 4: $EFT(t_i, p_j)$ denotes the Earliest Finish Time of a node t_i on a processor p_j and is defined as

$$EFT(t_i, p_j) = EST(t_i, p_j) + w_{t,j,k} \quad (2)$$

which is the earliest start time of a node t_i on a processor p_j plus the computation cost of t_i on processor p_j .

Algorithm 1 HEFT Algorithm

- 1: Set the computation costs of tasks and communication costs of edges with mean values
 - 2: Compute $rank_u$ for all tasks by traversing graph upward, starting from the exit task
 - 3: Sort tasks in a scheduling list by decreasing order of $rank_u$ values
 - 4: **while** there are unscheduled tasks in the list **do**
 - 5: Select the first task, t_i , from the list for scheduling
 - 6: **for** each processor p_k in the processor-set **do**
 - 7: Compute $EFT(t_i, p_k)$ value using the insertion-based scheduling policy
 - 8: **end for**
 - 9: Assign task t_i to the processor p_k that minimizes EFT of task t_i
 - 10: **end while**
-

Algorithm 2 HEFT with TSRS or METS

- 1: Sort in an increasing order all the groups of processors according to their computation capability (CC). Set the computation costs of tasks according to p_{ref} only ($w_{t,p_{ref},1}$) and the communication costs of edges with mean values.
 - 2: Compute $rank_u$ for all tasks by traversing graph upward, starting from the exit task
 - 3: Sort tasks in a scheduling list by decreasing order of $rank_u$ values
 - 4: **while** there are unscheduled tasks in the list **do**
 - 5: Select the first task, t_i , from the list for scheduling
 - 6: $[w_{t,i,1}(), SL()]=TSRS(t); / [w_{t,i,k}(), SL()]=METS(t);$
 - 7: **for** each processor p_k in SL (simulation list) **do**
 - 8: Compute $EFT(t_i, p_k)$ value with/without the insertion-based scheduling policy
 - 9: **end for**
 - 10: Assign task t_i to the processor p_k that minimizes EFT of task t_i
 - 11: **end while**
-

III. RELATED WORK

To the best of our knowledge, all the related algorithms assume the computation costs of application tasks on processors are available a priori and there is no related work reducing the number of simulations. Moreover, there are no low complexity heuristics considering tasks as both ST and MT implementations. The second is close to the problem of scheduling moldable tasks with the restriction that tasks can only use the cores of one processor [7], but these approaches are not very relevant.

The DAG values can be found using a number of tools. The Pegasus Workflow Management System [8] is a framework for mapping complex scientific workflows onto

distributed resources. SKOPE [9] is a framework that produces a descriptive model about the semantic behaviour of a workload. StarPU [10] is a task programming library for hybrid architectures. In [11], a theoretical insight on the performance of HeteroPrio is provided.

The static task scheduling algorithms are classified in two main categories. The first one includes algorithms that are based on heuristics, such as list scheduling [2] [3], clustering [12], node duplication, or more sophisticated algorithms [13], while the second includes stochastic search algorithms, where the problem is modelled as an optimization problem using either ILP, CP models. The heuristic methods provide a good solution in low time while the search algorithms provide a (near)-optimum solution but in a prohibitively large simulation time especially for complex applications. Clustering heuristics are mainly proposed for homogeneous systems [12]. The duplication heuristics produce higher quality solutions than list scheduling heuristics, but result in higher time complexity as well as to more processor power and availability [2]. List scheduling heuristics, produce the most efficient schedules, without compromising the quality of the solution and with a lower complexity. Some of the most important list scheduling heuristics for heterogeneous systems are: PEFT [2], HEFT [3], HCPT [4], HPS [5], PETS [1], Lookahead [14], LDCP [6].

HEFT algorithm is shown in Algorithm 1 and has two phases: a task prioritizing and a processor selection phase. In the first phase, task priorities are defined by using $rank_u$ which represents the length of the longest path from task t_i to the exit node, including the computation cost of t_i and is given by $rank_u(t_i) = \overline{w}_i + \max_{t_j \in succ(t_i)} \{\overline{c}_{(i,j)} + rank_u(t_j)\}$. For the exit task, $rank_u(t_{exit}) = \overline{w}_{exit}$. The task list is ordered by decreasing value of $rank_u$. The task with the highest rank is scheduled first. In the processor selection phase, the task with the higher $rank_u$ value is assigned to the processor p_j giving the EFT.

IV. PROPOSED TS METHODOLOGY AND HEURISTICS

In this section we introduce two novel TS methods. These are TSRS and METS and they are given in Subsection IV-A and Subsection IV-B, respectively.

A. Task Scheduling methodology Reducing the number of task Simulations (TSRS)

This methodology consists of two stages, i.e., initialization stage and main stage. In Algorithm 2, we show HEFT with TSRS or METS. The main stage of TSRS extends/modifies the processor selection phase, lines 6-8 in Algorithm 1. The algorithms differ only in lines 1,6,7 of Algorithm 2. TSRS and METS return a list containing all the candidate processors (SL) and their computation values.

Initialization step: In this step (line 1 in Algorithm 2), processors are divided into groups. A group of processors contains identical processors only and the number of the groups equals to the number of different processors. All the groups are sorted in an increasing Computation Capability

(CC) order; regarding multi-core processors, the CC refers to the one core only (ST implementations). In the case that the CC of two different processors is approximately the same, we can consider both in the same processor group. For example, consider a cluster with 2 type1 coprocessors, 2 type2 multi-core processors and 2 type3 multi-core processors, where $(w_{t1,type2,1} \geq w_{t1,type3,1} \geq w_{t1,type1,1})$ for task $t1$; then, we assume that $(w_{t,type2,1} \geq w_{t,type3,1} \geq w_{t,type1,1})$ for every task t and $proc_order = (p_{type2}, p_{type3}, p_{type1})$; the previous inequalities do not hold for MT implementations and may $w_{t,type2,6} \leq w_{t,type3,4} \leq w_{t,type1,1}$. This assumption is common in heterogeneous systems. The above procedure where all the groups of processors are sorted according to their CC is not necessary for all the processors; however, in case we cannot classify a processor into a group, all the tasks are simulated on that processor, increasing the number of simulations performed in total.

The application DAG is created by using the computation costs of the tasks on the one core of p_{ref} only (reference processor), i.e., $w_{t,pref,1}$. In terms of output schedule length, it is more efficient to select a Highest Computational Capability Processor (HCCP) as p_{ref} (a last group processor). However, in METS (Subsection IV-B), p_{ref} cannot be a HCCP in all cases, because it has to be the multi-core processor containing the maximum number of cores (cannot be a coprocessor). Thus, given that TSRS is applied as both standalone method and together with METS, we will not consider p_{ref} as a fixed value.

By using the computation costs on p_{ref} only, the $rank_u$ values are no longer computed using the average costs but using the computation costs of p_{ref} , slightly affecting the task priority list; the priority list is not strongly affected because the computation costs are monotonic. In [15], the rank function of HEFT algorithm is investigated by using the mean, median, worst and best computation costs; it is shown that for random computation costs (not monotonic as in our case) first, different ways of computing $rank_u$ affects HEFT performance and second, the mean computation costs is not the best choice. In Subsection V-B1, we show that HEFT's schedule length is not degraded by TSRS and in addition to [15], we showcase that the mean computation costs do not provide better solutions than the p_{ref} ones.

Main Step: In this paper, we provide the TSRS without the insertion based scheduling policy as it is more complex and the page size is limited. However, in Section 4 we have evaluated TSRS with and without the insertion policy.

The main step of TSRS (line 6 in Algorithm 2) reduces the number of candidate processors in the processor selection phase. The procedure follows. The EFT is given by Eq. 2 and consists of two parts, EST and $w_{i,j,k}$. The second part of Eq. 2 ($w_{i,j,k}$) is an unknown value, as task t is not simulated on every processor group but on p_{ref} only, while the first part of Eq. 2 is known, as it refers to the processor availability time as well as to the finish time of

the previously scheduled tasks. Given that first, the processor groups are sorted in an increasing CC order and second, the first part of Eq. 2 is known, we are able to reduce the number of candidate processors for task t , without excluding any processor with minimum EFT value. As an example, assume that the EFT values of t on 4 different single core processors are those in Eq. 3 and also p_{ref} is p_3 .

$$\begin{aligned} EFT(t, p_1) &= w_{t,1,1} + 10 \\ EFT(t, p_2) &= w_{t,2,1} + 9 \\ EFT(t, p_3) &= 2 + 9 \end{aligned} \quad (3)$$

Given that $(w_{t,1,1} \geq w_{t,2,1} \geq w_{t,3,1} = 2 \geq w_{t,4,1})$, there is no need to simulate t on p_1 and p_2 as these two processors always give a larger EFT value than p_3 and therefore they will never be allocated for t by HEFT algorithm.

Algorithm 3 TSRS without using the insertion based scheduling policy

```

1: [ $w_{t,i,1}()$ ,  $SL()$ ] = TSRS ( $t$ ) {
2:
3: for ( $i = 1, Proc.groups$ ) do
4:   compute  $EFT(t, j)$  for every  $p_j$  in group  $i$ , by using
       $w_{t,i,1} = w_{t,p_{ref},1}$ 
5:   Put the min  $EFT(t, j)$  value from every processor group  $i$ 
      in  $S(i)$ 
6: end for
7:
8:   /*Reduce the search space*/
9: Put all processor groups in the simulation list ( $SL$ )
10: for ( $i = Proc.groups, 2, -1$ ) do
11:   for ( $j = i - 1, 1, -1$ ) do
12:     if ( $S(i) \leq S(j)$ ) then
13:       remove processor group  $j$  from  $SL$ 
14:     end if
15:   end for
16: end for
17:   /*this step is optional*/
18: if ( $p_{ref} \notin HCCP$  group) then
19:   for ( $i = 1, Proc.groups - 1$ ) do
20:     if ( $S(i) \leq min\_EFT\_on\_p_{HCCP}$ ) then
21:       remove  $p_{HCCP}$  group from  $SL$ 
22:     end if
23:   end for
24: end if
25:
26: Get the  $w_{t,i,1}$  values that  $i \in SL$  (if any) /*simulation*/
27: Return  $w_{t,i,1}()$ ,  $SL()$  }

```

The proposed method is given in Algorithm 3. First, we compute the EFT values for all the processors by using $w_{t,p_{ref},1}$ instead of $w_{t,j,1}$ and put the minimum EFT value of every processor group i in $S(i)$ (lines 3-6). All the processors inside a group have identical computation costs.

In lines 8-16, we compare $S(i)$ with $S(j)$, where always holds ($i > j$) (and therefore always $w_{t,i,1} \leq w_{t,j,1}$). If the $EFT(t, i)$ value referring to processor group i is smaller or equal to any other $EFT(t, j)$ value to a slower group j , then j is not a candidate group and it is removed from the simulation list (SL). Let us follow the above example of Eq. 3

for lines 8-16 (Algorithm 3), where $w_{t,p_{ref},1} = 2$ and thus $EFT(t, p_1) = 12$, $EFT(t, p_2) = 11$, $EFT(t, p_3) = 11$, $EFT(t, p_4) = 15$. First, the $EFT(t, p_4)$ value is compared to $EFT(t, p_3)$, $EFT(t, p_2)$ and $EFT(t, p_1)$ but the *if-condition* in line 12 is never true. Then, the $EFT(t, p_3)$ value is compared to $EFT(t, p_2)$ and $EFT(t, p_1)$ and because $EFT(t, p_2)$ and $EFT(t, p_1)$ give larger or equal values, they are both excluded from SL etc. Thus, the processor groups with $j = 1$ and $j = 2$ are removed from the list. The number of candidate processors is reduced without excluding any processors with minimum EFT value.

In case that ($p_{ref} \in HCCP$ group), the lines 18-24 in Algorithm 3 are not needed. On the other hand, when p_{ref} is not a HCCP, the method given in lines 8-16 (Algorithm 3) is not able to reduce the number of simulations on the HCCP group. To do so, we have to define a lower bound value regarding how fast the HCCP is. We can define a very low unreachable lower bound value on the HCCP, e.g., task t will never run 50 times faster than p_{ref} ($w_{t,p_{ref},1}/50 \leq w_{t,p_{HCCP},1} \leq w_{t,p_{ref},1}$) for every task t . This procedure is given in lines 18-24 in Algorithm 3; if $S(i)$ (where $i < Proc.groups - Proc.groups$ is the last group, HCCP group) is lower or equal to the minimum $EFT(t, HCCP)$ value that the HCCP group can get, then the HCCP group is removed from SL. Let us follow the previous example (Eq. 3), where the method given in lines 8-16 (Algorithm 3) has already excluded p_1 and p_2 from SL. If we apply the method given in lines 18-24 (Algorithm 3) with ($min_EFT_on_p_{HCCP} = 2/50 + 13$), then the minimum value that p_4 can get is always larger than $EFT(t, p_3)$ and thus p_4 is also excluded from SL.

However, the procedure in lines 18-24 slightly degrades HEFT's output schedule length because we do not know how larger the $w_{t,i,1}$ values can be in comparison with $w_{t,p_{ref},1}$. Let us give an example, consider we have to compute the EFT values of t on 4 different single core processors and p_3 is the p_{ref} . Moreover, consider that Eq. 2 gives the following:

$$\begin{aligned} EFT(t, p_1) &= w_{t,1,1} + 9 \\ EFT(t, p_2) &= w_{t,2,1} + 9 \\ EFT(t, p_3) &= 2 + 15 \\ EFT(t, p_4) &= w_{t,4,1} + 13 \end{aligned} \quad (4)$$

The lines 8-16 in Algorithm 3 exclude p_1 and p_3 from SL. The lines 18-24 (Algorithm 3), with ($min_EFT_on_p_{HCCP} = 2/50 + 13$), exclude p_4 from SL, meaning that t is assigned on p_2 , which is not always the processor with the minimum EFT (it depends on the $w_{t,2,1}$ value). We know that ($w_{t,2,1} \geq 2$), but we don't know how large $w_{t,2,1}$ is; thus, if ($w_{t,2,1} + 9 > (2/50 + 13)$) and therefore ($w_{t,2,1} > 2/50 + 4$), then t may run faster on p_4 than on p_2 , and in that case, it shouldn't have been removed from the list. In that case, the more the processor groups, the more the makespan degradation. However, the above refer to special cases only and therefore the makespan degradation is very low. This step (lines 17-24) is optional.

At last, t is simulated on all the processors in SL (line 26) and the computation costs are returned (line 27).

TSRS is applicable to most of the TS heuristics using the minimum EFT value as the heuristic cost function, such as HCPT [4], HPS [5], PETS [1], CPOP [3] [16] list scheduling algorithms, [12] [17] clustering algorithms, and others.

B. Multi-Threading Effective Task Scheduling heuristics (METS)

In this paper, METS is applied together with TSRS, in order to achieve both less simulations and better schedule lengths, however, standalone METS provides better makespan values. So, before METS is introduced, we present the modified version of TSRS used by METS.

The modified version of TSRS being used by METS is given in Algorithm 4. Algorithm 4 is similar to Algorithm 3, but has been extended to support MT implementations too. The $EFT(t, j)$ values for the ST implementations are computed as in Algorithm 3, while the $EFT(t, j)$ values for the MT implementations are computed by using median core utilization factor values (between realistic minimum and maximum values), i.e., ($fact. = 1.5, 2, 2.8, 3, 3.5$) for (2, 3, 4, 5, 6) threads, respectively (line 5 in Algorithm 4); the median factor values are used to find which MT implementation (from 2 up to f threads) is better. We store both the best ST and MT $EFT(t, j)$ value for each processor group into $S(i)$ and $M(i)$, respectively. It is important to note that a) the best MT EFT value is not always the one using the maximum number of cores/threads and b) the MT EFT value is not always smaller than the ST EFT, e.g., consider the case where the five out of six cores are not available in the near future. Lines 10-17 in Algorithm 4, are similar to lines 8-16 in Algorithm 3, but in Algorithm 4 a processor group is removed from SL if both the best ST and MT values are larger than those of another group. The same holds for the second loop kernel in Algorithm 4 too; when the minimum EFT value is given by a MT implementation, in Line 27 we use the highest EFT value that $M(i)$ can get. Standalone METS is more efficient in terms of makespan as the median core utilization factor values degrade the quality of the output schedule.

The key points of METS are the following:

- 1) ST implementations are more efficient for tasks with high Communication to Computation Ratio (CCR)
- 2) MT implementations are more efficient when the task parallelism is low
- 3) When the task parallelism is high, ST/MT implementations are more efficient when the range of $w_{t,i,j}$ values among different tasks t , is low/high, respectively.
- 4) We get $factor_{t,i,f1}$ value and we predict $factor_{t,j,f2}$, where $f1 \succ f2$

Regarding the first key point, ST implementations are more efficient for high CCR values. The data transfer cost is minimized when the tasks are executed on the same

Algorithm 4 TSRS (Algorithm 3) when it is called by METS (without insertion based scheduling policy)

```

1: [SL(), S(), M()] = TSRS (t) {
2:
3: for ( $i = 1, Proc.groups$ ) do
4:   compute ST  $EFT(t, j)$  for every  $p_j$  in group  $i$ , by using
       $w_{t,i,1} = w_{t,pre,f,1}$ 
5:   compute MT  $EFT(t, j)$  for every  $p_j$  in group  $i$  and for
      all thread combinations, by using  $w_{t,i,1} = w_{t,pre,f,1}$  and
       $w_{t,i,f} = w_{t,pre,f,1} \times fact.(f)$ 
6:   Put the min ST and MT  $EFT(t, j)$  values from every
      processor group  $i$  in  $S(i)$  and  $M(i)$ , respectively
7: end for
8:
9:   /*Reduce the search space*/
10: Put all the processor groups in the simulation list (SL)
11: for ( $i = Proc.groups, 2, -1$ ) do
12:   for ( $j = i - 1, 1, -1$ ) do
13:     if ( $\min(S(i), M(i)) \leq \min(S(j), M(j))$ ) then
14:       remove processor group  $j$  from SL
15:     end if
16:   end for
17: end for
18:
19: if ( $p_{ref} \notin HCCP$  group) then
20:   for ( $i = 1, Proc.groups - 1$ ) do
21:     if ( $S(i) \leq M(i)$ ) then
22:       if ( $S(i) \leq \min\_EFT\_on\_pHCCP$ ) then
23:         remove  $pHCCP$  group from SL
24:       end if
25:     else
26:       Put in  $maxMT$  the  $EFT(t, i)$  by using the worst
         speedup value; if  $fact.(f) = 1$  then  $maxMT = S(i)$ 
27:       if ( $maxMT \leq \min\_EFT\_on\_pHCCP$ ) then
28:         remove  $pHCCP$  group from SL
29:       end if
30:     end if
31:   end for
32: end if
33: Return SL(), S(), M() }

```

processor as the data remain in the processor's disk/memory. The more tasks each processor can handle in parallel (i.e., the more the cores each processor contains), the less the communication cost, as the intra-processor transfer cost is very low. The *if-condition* in line 11 (Algorithm 5) implements the above idea. By using a ST implementation for a parent task that gives too much data to its children, we reduce the probability of its children tasks to get data from another processor(s). On the other hand, by using a ST implementation for a child task which gets too much data from its parents, we increase the probability of the other children (with the same parents) to be assigned to the same processor and therefore minimize the transfer cost.

As far as the second key point is concerned, when the number of the ready tasks is smaller than the number of the processors, there is no reason to save any cores, and thus the implementation giving the minimum EFT value is selected, no matter the number of cores used (the imple-

mentation giving the minimum EFT is not always MT). The *if-condition* in line 14 (Algorithm 5) implements the above idea. In Algorithm 5, ST&MT means that we seek for the solution giving the minimum EFT value no matter the number of threads/cores used (either ST or MT). This heuristic does not hold for high CCR values for the reason explained in the previous paragraph and therefore, the 'else if' condition in line 14.

Let us explain the second key point further, consider there are four identical multi-core processors and only 4 ready tasks. In that case, it is not efficient to save any cores and therefore MT implementations for all the tasks is the best solution no matter the number of threads used. However, if there are 5 ready tasks, it might not be efficient to use MT implementations for all the tasks, because other thread combinations have to be investigated too. This is why we have used the 'Threshold' value in line 8 (Algorithm 5), indicating the number of ready tasks should exist in order to use ST&MT implementations; in this case, the 'Threshold' value in line 8 is ($Threshold = 4$). Keep in mind that MT refers to the best MT solution, no matter how many threads are used. Now consider the case that there are 5 ready tasks and a HW environment with three identical multi-core processors and one GPU (let us assume that the tasks run two times faster on the GPU). One could think that it is not efficient to use MT implementations for all the multi-core processors because one ready task will have to wait until another finishes its execution. However, if the tasks are executed 2 times faster on the GPU than on the processor, the GPU will have executed 2 tasks until the three processors finish their execution. Thus, the GPU 'counts' for 2 processors and there is no reason to save any cores. In this case, ($Threshold = 5$) and not ($Threshold = 4$). The 'Threshold' value depends on a) the number of the processors, b) the number of the cores each processor has, c) how faster/slower is one processor to another. The 'Threshold' value is application independent and depends solely on the HW infrastructure. Thus, it can be found 'off-line'. In Section 4, ($Procs \leq Threshold < 2 \times Procs$), where $Procs$ is the number of the processors.

Regarding the third key point above, i.e., when the number of ready tasks is larger than the 'Threshold' value, the MT implementations are efficient only in the case that the range of the $w_{t,i,j}$ values for different tasks t is high and in particular for the tasks having larger $w_{t,i,j}$ values than the others. This is because the core utilization factor value is always lower than the number of cores and therefore the time needed for a task to be executed as an f -thread implementation is always larger than executing f different tasks. Let us give an example, consider 8 identical tasks ready for execution and two identical 4-core processors. Also consider that the eight tasks need (10, 6, 4, 3) secs to be executed, using (1, 2, 3, 4) threads, respectively. If all the tasks are considered as ST, then 10 secs are required

for them to be executed. On the other hand, by using 4-thread or 2-thread implementations only, 12 secs are needed. However, if half of the tasks need (15, 9, 6, 4.5) and the other half (10, 6, 4, 3) seconds to be executed by using (1, 2, 3, 4) threads, respectively, then using only ST implementations is not the best option. If we run the heavy tasks as 4-thread implementations and the light ones as ST ones, then the overall execution time is 14.5 secs, while by using ST only, it is 15 secs. The *if-condition* in line 21 (Algorithm 5) satisfies that only the tasks with high $w_{t,i,j}$ values are considered as MT. If a task's rank value is larger than 1.3 times the minimum rank value of C (the tasks that are going to be executed in the near future), it is further processed as an ST&MT implementation, otherwise it is assigned as a ST.

In contrast to line 16, where an ST&MT implementation is always selected regardless of whether t is effectively split into multiple threads or not, in line 22, the number of tasks waiting for execution is higher than the number of processors and thus we have to consider the scenario that t may give a low core-utilization factor. Thus, we get $w_{t,pref,f}$ value, where f is the maximum number of threads in SL, and compute the utilization factor. If the factor is large enough, we use a ST&MT implementation, otherwise, we give a second chance for t to be executed with fewer threads, i.e., $\lceil f/2 \rceil$ (line 29). The good utilization factor values used are (1.6, 2.35, 3.4, 3.9, 4.7) for (2, 3, 4, 5, 6) threads, respectively.

Regarding the fourth key point above, we assume that $factor_{t,i,f} = factor_{t,j,f}$, where i, j are multi-core processors. Moreover, we measure $factor_{t,i,f1}$ and predict $factor_{t,j,f2}$, where $f1 > f2$; $factor_{t,j,f2} = (f2 \times factor_{t,i,f1})/f1$. This procedure is applied in lines 26 and 33 (Algorithm 5) in order to update the EFT values on the other processors according to $factor_{t,pref,f}$ value.

METS is given in Algorithm 5. All the coefficients are found experimentally. First, TSRS finds the candidate processors for task t (line 3). If there is no multi-core candidate processor, the procedure is trivial. Otherwise, the multiple *if-conditions* take place finding whether the selected processor will use a ST or a ST&MT implementation. In the case that a ST is selected, we simulate t as ST only. Otherwise, if a ST&MT is selected, we simulate t on the remaining processors but t is simulated either as ST or MT, not both.

The heuristics presented in Subsection IV-B, can be applied together with TSRS to the algorithms that TSRS is applicable to. Moreover, METS can be applied as a standalone method. In this case, METS is applicable to more algorithms such as PEFT [2] and lookahead [14].

V. EXPERIMENTAL RESULTS

This section shows the application of TSRS and METS to HEFT algorithm. The comparison metric used for evaluating the schedule's length is speedup (Eq. 5). The speedup value for a given graph is computed by dividing the sequential execution time (i.e., cumulative computation costs of the tasks in the graph) by the parallel execution time. The

Algorithm 5 METS with TSRS

```
1: [ $w_{t,i,thr}()$ ,  $SL()$ ] = METS (t) {
2:
3: [ $SL(),S(),M()$ ] = TSRS(t);
4: if (SL contains no multi-core processor) then
5:   Get the  $w_{t,i,1}$  values that  $i \in SL$  (if any) -  $thr = 1$ 
6: else
7:   A  $\leftarrow$  next 6 ready tasks
8:   B  $\leftarrow$  next 'Threshold' tasks
9:   C  $\leftarrow$  ready tasks that ( $Rank_u > 0.7 \times Rank_u(t)$ ) /*tasks
   to be executed in the near future only*/
10:
11: if (at least half of the tasks in A contain an edge (either
   parent or child edge), where  $c_{n,m}/w_{t,pre,f,1} \geq 1.5$ ) then
12:   /*processors are faced as ST only*/
13:   [ $w_{t,i,1}()$ ,  $SL()$ ] = kernel (ST,t);
14: else if (at least one task in B is not ready) then
15:   /* Task parallelism is low. Use the implementation giving
   the min EFT, no matter the # of the threads*/
16:   [ $w_{t,i,thr}()$ ,  $SL()$ ] = kernel (ST&MT,t);
17: else
18:   /* task parallelism is high */
19:
20:   /*if the range of  $w_{t,pre,f,1}$  values among diff. tasks is
   high*/
21:   if ( $Rank_u(t) > (1.3 \times \min(Rank_u(C)))$ ) then
22:     Get  $w_{t,pre,f}$ , where f is the max number of threads
     in SL
23:      $factor_{t,pre,f} = w_{t,pre,f,1}/w_{t,pre,f}$ 
24:     if ( $factor_{t,pre,f} > good.factor(f)$ ) then
25:       /*Use the implementation giving the min EFT, no
       matter the # of the threads*/
26:       Use  $factor_{t,pre,f}$  to update EFT to other procs
27:       [ $w_{t,i,thr}()$ ,  $SL()$ ] = kernel (ST&MT,t);
28:     else
29:       Get  $w_{t,pre,f,[f/2]}$ 
30:        $factor_{t,pre,f,[f/2]} = w_{t,pre,f,1}/w_{t,pre,f,[f/2]}$ 
31:       if ( $(factor_{t,pre,f,[f/2]} > good.factor([f/2]))$ 
       AND ( $([f/2]) > 1$ )) then
32:         /*Use the implementation giving the min EFT,
         no matter the # of the threads*/
33:         Use  $factor_{t,pre,f,[f/2]}$  value to update EFT to
         other processors
34:         [ $w_{t,i,thr}()$ ,  $SL()$ ] = kernel (ST&MT,t);
35:       else
36:         /*processors are faced as ST only*/
37:         [ $w_{t,i,1}()$ ,  $SL()$ ] = kernel (ST,t);
38:       end if
39:     end if
40:   else
41:     /*processors are faced as ST only*/
42:     [ $w_{t,i,1}()$ ,  $SL()$ ] = kernel (ST,t);
43:   end if
44: end if
45: end if
46: Return  $w_{t,i,thr}()$ ,  $SL()$  }
47:
48: [ $w_{t,i,thr}()$ ,  $SL()$ ] = kernel (T,t) {
49: if ( $T == ST$ ) then
50:   [ $SL(),S(),M()$ ] = TSRS(t) - by using S() only, not M()
51:   Get the  $w_{t,i,1}$  values that  $i \in SL$  (if any) -  $thr = 1$ 
52: else
53:   [ $SL(),S(),M()$ ] = TSRS(t)
54:   Get the  $w_{t,i,thr}$  values (if any) where  $i \in SL$  and  $thr$  is
   the number of threads of the min( $S(i), M(i)$ )
55: end if
56: Return  $w_{t,i,thr}()$ ,  $SL()$  }
```

sequential execution time is computed by assigning all tasks to the HCCP; if the HCCP is a multi-core processor, then the numerator of Eq. 5 refers to max-thread implementations.

$$Speedup = \frac{\min_{p_j \in P} \{\sum_{t_i \in V} w_{(i,j,k)}\}}{makespan} \quad (5)$$

The simulation gain is given by (Simulation gain = number of simulations in total / number of simulations performed), where the numerator is given by $((\sum_{i=1}^P c_i + co) \times tasks)$, where P is the number of multi-core processor groups, c_i is the number of group i cores and co is the number of coprocessor groups.

A. Hardware (HW) Infrastructure

The HW infrastructure used in this paper, consists of 9 different groups of processors (6 multi-core processor and 3 coprocessor groups), 3 common processors in each group (27 processors in total) and 6 cores per processor at maximum. The groups of processors are sorted in increasing computational capability (CC), i.e., ($w_{t,9,1} \leq w_{t,8,1} \leq \dots \leq w_{t,1,1}$). The HW infrastructure is described by $D.procs(9)$, $C.procs(3)$, $cores(6)$ arrays, giving the number of different processors, common processors and cores, respectively. We assume that each task runs faster on the coprocessors than the one core of every processor and thus the coprocessors refer to processors with number 7, 8 and 9. So, for instance, the HW infrastructure described by $\{D.P(0, 1, 1, 1, 1, 1, 0, 0)$, $C.P(0, 1, 1, 1, 3, 3, 1, 0, 0)$ and $cores(0, 2, 4, 4, 6, 6)\}$, refers to one 2-core processor of type2, one 4-core processor of type3, one 4-core processor of type4, three 6-core processors of type5, three 6-core processors of type6 and one coprocessor of type7.

B. Random graphs and computation/communication costs

We have evaluated our work to 14580 random generated application graphs. For this purpose, we used the synthetic DAG generation program Daggen [18] with five different parameters defining the DAG shape:

- n: number of DAG nodes (i.e., application tasks), $n = [50, 100, 200, 300]$
- fat: this parameter affects the height and the width of the DAG, $fat = [0.2, 0.5, 0.8]$
- density: determines the number of edges between two levels of the DAG, $density = [0.2, 0.5, 0.8]$
- regularity: the regularity determines the uniformity of the number of tasks in each level, $regularity = [0.2, 0.5, 0.8]$
- jump: indicates that an edge can go from level l to level $l + jump$, $jump = [1, 2, 4]$

We used this synthetic DAG generator to create the DAG structure, which includes the specific number of nodes and their dependencies. To obtain the computation and communication costs, the following parameters are used:

- CCR: Communication-to-Computation Ratio: ratio of the sum of the edge weights to the sum of the node weights in a DAG, $CCR = [0.1, 0.2, 0.5, 1, 2, 5, 10]$

- β_w (Range percentage of computation costs among different tasks for p_{ref}): β_w is given by the following formula where \bar{w} is the average computation cost of the DAG and is selected randomly, $\beta_w = [0.5, 1, 1.5]$

$$\bar{w} \times (1 - \frac{\beta_w}{2}) \leq w_{t,pref,1} \leq \bar{w} \times (1 + \frac{\beta_w}{2}) \quad (6)$$
- β_c (Range percentage of communication costs among the edges of the DAG): β_c is given by the following formula where \bar{c} is the average communication c value of the DAG and $\bar{c} = \bar{w} * CCR$. $\beta_c = [0.5, 1, 1.5]$

$$\bar{c} \times (1 - \frac{\beta_c}{2}) \leq c_{i,j} \leq \bar{c} \times (1 + \frac{\beta_c}{2}) \quad (7)$$

The computation costs for the other processors are generated according to the computation costs on p_{ref} . The computation costs of the remaining processors are random values within the following range: $w_{t,pref,1} \times R(i, 1) \leq w_{t,i,1} \leq w_{t,pref,1} \times R(i, 2)$, where $R=[2,2.5; 1.8,2; 1.4,1.5; 1.2,1.3; 1.05,1.15; 1,1; 0.12,0.2; 0.08,0.18; 0.05,0.15]$; we have used both wider and narrower values than R and the results are similar. Regarding multi-thread computation costs, we have used random realistic speedup range values, i.e., $w_{t,i,j} = w_{t,i,1} \times speedup(j)$, where the speedup value is a random value within the following range $(1.1, 1.9), (1.2, 2.8), (1.3, 3.7), (1.4, 4.5), (1.5, 5.4)$, for $(2, 3, 4, 5, 6)$ threads, respectively. The speedup values are monotonic, i.e., $(w_{t,i,j1} \leq w_{t,i,j2})$, where $j1 > j2$.

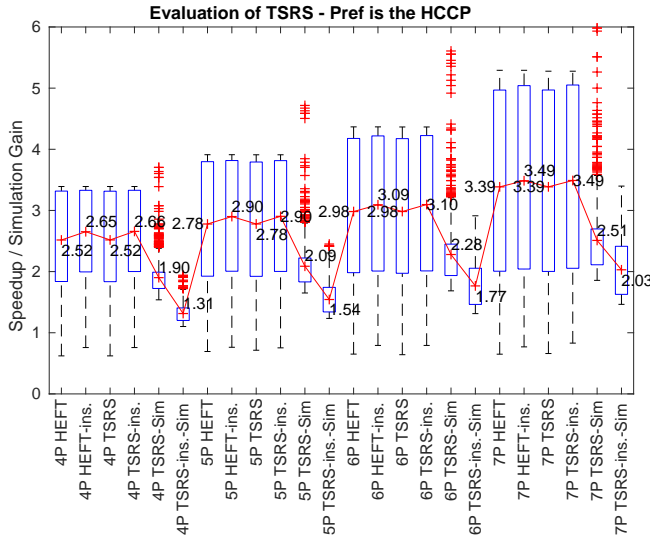


Figure 1. Evaluation of TSRS (972 different DAGs)

1) *Evaluating TSRS*: In this Subsection, TSRS is evaluated. The results are illustrated by using boxplots in Matlab. The ('Sim','ins.') in the x-axis of Fig. 1 indicate simulation gain and insertion policy, respectively. In Fig. 1, 972 different DAGs have been used (all different fat, regularity, density and jump combinations) with $n = 100, CCR = [0.1, 0.5, 2, 10], \beta_w = \beta_c = [0.5, 1, 1.5]$ as well as several processor configurations. The '4P' indicates 4 different single-core processors. In this subsection, all the processors are either single-cores or co-processors. The

TSRS makespan is approximately the same as that of the standalone HEFT, in all cases. Furthermore, both HEFT and TSRS perform better by using the insertion scheduling policy but the gains are small. By using the insertion scheduling policy lower simulation gain values occur because in that case the number of computation costs needed is higher.

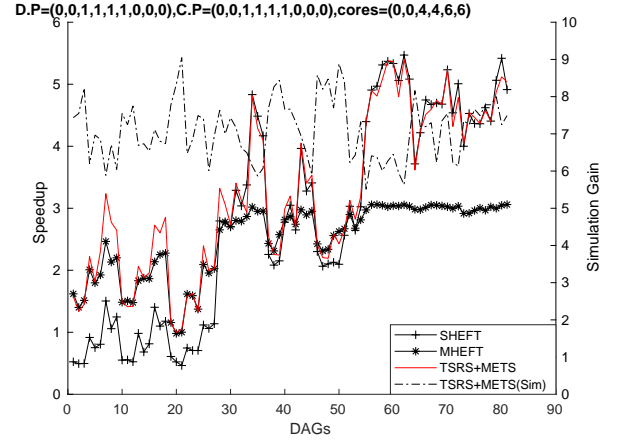


Figure 2. METS with TSRS ($n = 100, CCR = 0.5, \beta_w = \beta_c = 0.5$)

2) *Evaluating METS with TSRS*: In this Subsection, METS with TSRS is evaluated (Fig. 2, Fig. 3) - $p_{ref} = 6$ in all cases. Given that HEFT algorithm doesn't include multi-threading, we have implemented HEFT to use a) ST implementations only (SHEFT) and b) maximum thread implementations only (MHEFT). In this Subsection we have evaluated METS without using the insertion scheduling policy because the makespan improvement is not significant comparing to the simulation loss. Therefore, by using the insertion scheduling policy, METS achieves slightly better makespan values than those shown in Fig. 2-Fig. 4; standalone METS gives better makespan values, as in Algorithm 4 the $M(i)$ values are computed by using median core utilization factor values and not the real ones. SHEFT and MHEFT use the insertion scheduling policy.

In Fig. 2, a total of 81 different DAGs is considered combining fat, regularity, density and jump. The first 27 DAGs refer to skinny DAGs, the next 27 to medium fat and the last 27 DAGs refer to fat DAGs. As it can be observed, skinny DAGs give low speedup but high simulation gain values, while fat DAGs give high speedup but lower simulation gain values. SHEFT is more efficient than MHEFT when the task parallelism is high, as by providing more cores, more tasks are executed in parallel. On the other hand, when the task parallelism is low, MHEFT gives always higher speedup values, as it is preferable to use less processors but with high CC. It is important to note that our method follows the trend of the best of the two.

In Fig. 3, METS with TSRS is evaluated for all the combinations among DAGs' fat, regularity, density and jump as well as $n = [100, 200], \beta_w = \beta_c = [0.5, 1, 1.5]$,

$CCR = [0.1, 0.2, 0.5, 1, 2, 5, 10]$ (3402 different DAGs in total) and four different processor configurations. When only multi-core processors are used, the heuristics given in Subsection IV-B perform very well and give significant speedup values. On the other hand, when fast coprocessors are used apart from multi-core processors, the heuristics given in Subsection IV-B perform better than both SHEFT and MHEFT but the gain is low. The reason lies in the fact that HEFT is a greedy algorithm as it always chooses the processor giving the minimum EFT value; therefore, the coprocessors never become idle and push aside the multi-core processors; thus, most of the tasks are executed on the coprocessors. This is why all three methods give close makespan values. 'TSRS*' refers to the TSRS when the last loop kernel in Algorithm 3 is used (at least one coprocessor exists). The last loop kernel in TSRS reduces the number of simulations on the HCCP group. In the left bottom figure, the makespan degradation in 'TSRS*' is larger because the HCCP group contains 2 processors and therefore excluding the group from SL means that none of the two coprocessors is used. As far as the simulation gain is concerned, it is lower when coprocessors exist because most of the tasks are simulated on the coprocessors while $p_{ref} = 6$; in this case a larger number of extra simulations occurs. On the other hand, when no coprocessor exists, p_{ref} is a HCCP and therefore it is the most preferable processor, meaning that the number of extra simulations is reduced.

C. Real World Applications

TSRS and METS have been evaluated to Montage, CyberShake, Epigenomics, LIGO and SIPHT real world applications [19] [20]. We have used small, medium and large graphs for each one of the 5 applications (from 50 up to 200 tasks, Fig. 4) as well as real communication and computation costs for $w_{t,p_{ref},1}$, taken from [19] [20]. The computation costs for the other processors have been selected as random values within a range as in Subsection V-B. SHEFT performs better than MHEFT when the number of processors is low (as in Fig. 4), as in that case SHEFT uses 20 cores while MHEFT uses 4 processors. However, by increasing the number of the processors MHEFT outperforms SHEFT (our method follows the trend of the best of the two). Moreover, when no coprocessor is used, METS performs better for the reason explained in the previous subsection. Last, Epigenomics and SIPHT are less scalable.

VI. CONCLUSIONS AND FUTURE WORK

TSRS modifies HEFT's processor selection phase in order to discard all the processors which cannot minimize the heuristic cost function, regardless of their computation costs; this way, the DAG computation costs required by HEFT become limited. Although TSRS, never excludes a processor minimizing the heuristic cost function (here EFT), it slightly affects the task priority list. However, the results show that for monotonic computation costs the output makespan is not

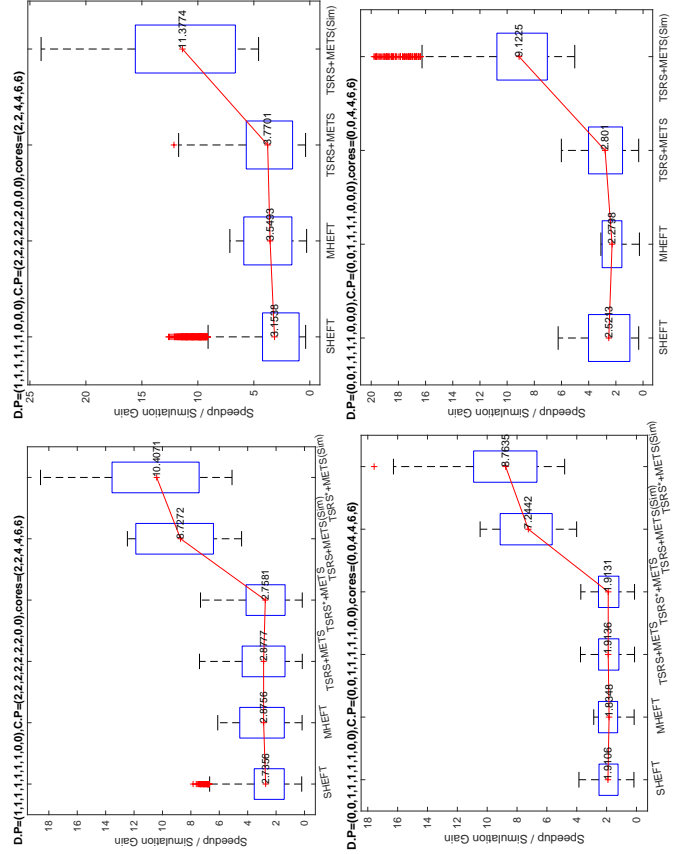


Figure 3. Evaluation of METS with TSRS (3402 different DAGs)

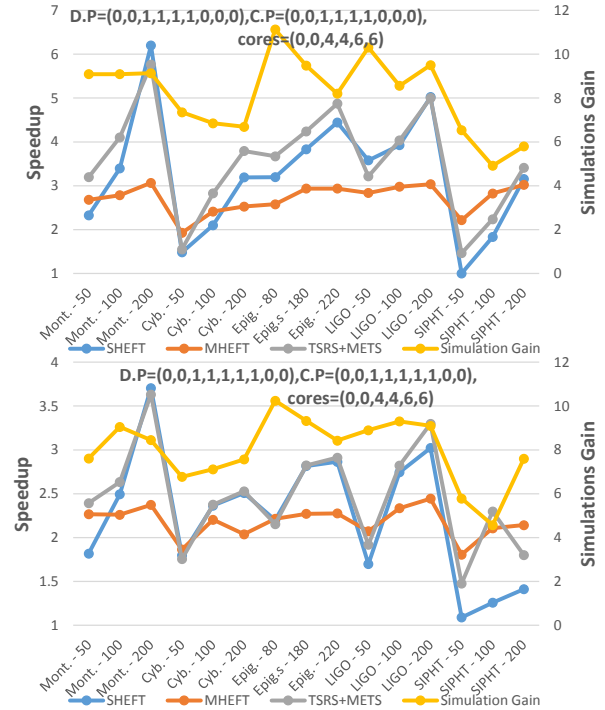


Figure 4. Evaluation of METS with TSRS, for 5 real world applications

degraded; as in [15], we show that the mean $Rank_u$ computation costs is not the best choice. The insertion scheduling policy is not preferred as the makespan improvement is not significant comparing to the simulation loss.

METS refers to heuristics finding which tasks are going to be split into multiple threads as well as the number of threads used, without requiring all the computation costs in the DAG. We evaluated METS with TSRS without using the insertion scheduling policy, as the makespan improvement is not significant comparing to the simulation loss. Standalone METS gives better makespan values.

In our future work, we intend to extend METS with heuristics finding whether a multi-core processor or a co-processor is more efficient for the current task (we believe this will give better makespan values when fast coprocessors are used). Our future work also includes the application and evaluation of both TSRS and METS to other TS algorithms such as HCPT, HPS, PETS, CPOP and others. Furthermore, we aim to develop a tool that takes OmpSs (Barcelona Supercomputing Center programming model) C-code as input and by using both TSRS and METS, it outputs a good quality schedule in low time. We use OmpSs as it extends OpenMP with new directives to support GPUs and FPGAs.

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