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Experimental study of the $\gamma p \rightarrow \pi^0 \eta p$ reaction with the A2 setup at the Mainz Microtron

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The data available from the A2 Collaboration at MAMI were analyzed to select the $\gamma p \rightarrow \pi^0 \eta p$ reaction on an event-by-event basis, which allows for partial-wave analyses of three-body final states to obtain more reliable results, compared to fits to measured distributions. These data provide the world's best statistical accuracy in the energy range from threshold to $E_\gamma = 1.45$ GeV, allowing a finer energy binning in the measurement of all observables needed for understanding the reaction dynamics. The results obtained for the measured observables are compared to existing models, and the impact from the new data is checked by the fit with the revised Mainz model.

DOI: [10.1103/PhysRevC.97.055212](https://doi.org/10.1103/PhysRevC.97.055212)**I. INTRODUCTION**

The unique extraction of partial-wave scattering amplitudes and universal baryon-resonance parameters from experimental data, as well as their precise interpretation in QCD, ranks among the most challenging tasks in modern hadron physics. During the last decades, an enormous effort to

study baryon resonances in photoinduced meson production at various laboratories has started. Very significant progress was made in single- and double-meson photoproduction [1–6]. The important advantage of studying multimeson final states is the possibility of accessing cascading decays of higher-lying resonances through intermediate excited states, whereas single-meson production is limited to decays into a meson and a ground-state nucleon. In addition, multimeson final states can be used for investigating the decay modes of already established resonances as well as for investigating the

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long-standing problem of “missing resonances,” which could couple to intermediate states involving excited nucleons rather than to states consisting of a meson and a ground-state nucleon.

Among double-meson final states, the photoproduction of two pions, in particular of $\pi^0\pi^0$ pairs, was studied extensively within the last two decades (see, e.g., Refs. [7–16]). In comparison to the widely studied $\gamma N \rightarrow 2\pi^0 N$ reaction, the $\gamma N \rightarrow \pi^0\eta N$ reaction provides a more selective identification of contributing resonances and their decay modes. In particular, for the incoming-photon energy range from the production threshold up to $E_\gamma = 1.5$ GeV, various analyses indicate the dominance of the D_{33} partial wave [17–24], which couples strongly to the $\Delta(1700)3/2^-$ resonance close to the production threshold and to the $\Delta(1940)3/2^-$ at higher energies. Furthermore, the η meson, acting as an isospin filter, is only emitted in transitions between either two N^* or two Δ resonances, introducing additional selectivity into the investigated decay modes. Thus, the $\gamma N \rightarrow \pi^0\eta N$ reaction is well suited for studying production of the $\Delta(1700)3/2^-$ resonance not only on free protons, but also on nucleons bound in nuclei, where the interpretation of ambiguities in resonance contributions and decays is, however, more complicated, compared to the free-proton case.

So far, the unpolarized total and differential cross sections for $\pi^0\eta$ photoproduction on the free proton, as well as polarization observables with circularly and linearly polarized photon beams, were measured with the CBELSA/TAPS experimental setup at the ELSA accelerator [22–24], with the A2 setup at the MAMI accelerator [19–21], with the GRAAL detector at the ESRF accelerator [25], and at the LNS accelerator [26]. The unpolarized cross section and the beam-helicity asymmetry for photoproduction of $\pi^0\eta$ pairs on the deuteron and on helium nuclei have been recently published by the A2 collaboration [27]. Further data sets, using circularly polarized photons and heavier nuclear targets (carbon, aluminum, and lead), were recently acquired with the A2 setup at MAMI and will be published in a forthcoming paper.

Reliable experimental measurement and theoretical analysis of the $\gamma N \rightarrow \pi^0\eta N$ reaction, with the three-body final state, is quite challenging because of its five-dimensional phase space. The most efficient way of analyzing such a reaction would be a partial-wave analysis (PWA) that enables fitting experimental data on an event-by-event basis, allowing one to track all correlations in the five-dimensional phase space. The event-based PWA of the $\gamma p \rightarrow \pi^0\eta p$ CBELSA/TAPS data by the Bonn-Gatchina (BnGa) group is a good example of such a technique [22–24,28]. Another method of analyzing a reaction like $\gamma N \rightarrow \pi^0\eta N$ is a simultaneous fit of various experimentally measured distributions for observables sensitive to the reaction dynamics. A special model for the analysis of three-body final states, especially aiming for understanding the features of $\gamma N \rightarrow \pi\pi N$ and $\gamma N \rightarrow \pi^0\eta N$, was developed by the Mainz group [18,19,29–31], paying particular attention to the analysis of specific angular distributions, which could be measured experimentally. The experimental data presented in this paper are compared to the previous solutions from the BnGa and Mainz groups, as well as to a new fit with the revised Mainz model.

The $\gamma N \rightarrow \pi^0\eta N$ reaction recently became a subject of specific interest, after a new analysis of the data acquired earlier with the GRAAL facility observed a narrow structure in the invariant-mass spectrum of the ηN system that could be interpreted as a contribution from a $N(1685)$ state [32]. The largest signal was observed in the $\gamma p \rightarrow \pi^0\eta p$ reaction, but the statistical accuracy of the measurement was quite low. This mass range attracted much attention after the observation of a narrow bump in the $\gamma n \rightarrow \eta n$ excitation function near the center-of-mass (c.m.) energy $W = 1.68$ GeV [33–37], while the $\gamma p \rightarrow \eta p$ total cross section showed a dip at the same energy [38,39]. So far this effect, which was called a “neutron anomaly,” has no unique explanation in various partial-wave analyses (PWA) [28,40]. Meanwhile, the latest analysis of the available $\gamma p \rightarrow \eta p$ data with the revised η MAID model describes the dip at $W = 1.68$ GeV well, without introducing any narrow state [39].

The most reliable identification of the $\gamma p \rightarrow \pi^0\eta p$ reaction in the A2 setup comes by detecting its four-photon final state, with η mesons decaying into two photons. For the $\eta \rightarrow 3\pi^0$ decay mode, the experimental acceptance drops significantly and there is a large chance of misidentifying the η meson in the $4\pi^0$ final state. Although the four-photon final state also has a large contribution from the $\gamma p \rightarrow \pi^0\pi^0 p$ production, the kinematic-fit technique allows a reliable separation of the $\pi^0\eta \rightarrow 4\gamma$ final state from $\pi^0\pi^0 \rightarrow 4\gamma$. The previous analyses of the $\gamma p \rightarrow \pi^0\eta p$ A2 data [19–21] were based on the information available after the initial reconstruction of the detected events, and all observables for $\gamma p \rightarrow \pi^0\eta p$ were measured by fitting the $\eta \rightarrow 2\gamma$ signal above the background remaining mostly from $\gamma p \rightarrow \pi^0\pi^0 p$ events. Such an approach provides a poorer experimental resolution, compared to using the kinematic fit, and does not allow making any PWA on the event-by-event basis. Because the $\gamma p \rightarrow \pi^0\eta p$ reaction has three particles in its final state, the event-by-event fit of the data is much more efficient than fitting separate spectra measured for individual observables.

The A2 data used in the present analysis were taken in 2007 (Run I) and 2009 (Run II). The production properties of the $\gamma p \rightarrow \pi^0\eta p$ reaction, which are not related to polarization observables, were earlier presented in Ref. [20], based on the analysis of Run I. The circular beam asymmetry for this reaction was reported for the first time in Ref. [21], based on the analysis of Run II. In the present work, all results are obtained from both Run I and Run II, after using a kinematic-fit technique for event identification and reconstruction. The same technique was used previously in the analyses of the same data sets for measuring the reactions $\gamma p \rightarrow \eta p$ [38,39], $\gamma p \rightarrow \pi^0\pi^0 p$ [13], $\gamma p \rightarrow K^0\Sigma^+$ [41], and $\gamma p \rightarrow \omega p$ [42]. Compared to previous $\gamma p \rightarrow \pi^0\eta p$ measurements, the present analysis improves both the statistical accuracy, with a total of 1.5×10^6 accumulated events, and the data quality, allowing a finer energy binning in the measurement of all observables needed for understanding the reaction dynamics. The data from Run II, which were taken with a higher beam energy, provide the ηN invariant-mass distribution with good statistical accuracy in the vicinity of 1.685 GeV. This makes it possible to search for a narrow structure, the observation of which was reported in Ref. [32].

II. EXPERIMENTAL SETUP

The $\gamma p \rightarrow \pi^0 \eta p$ reaction was measured by using the Crystal Ball (CB) [43] as a central calorimeter and TAPS [44,45] as a forward calorimeter. These detectors were installed in the energy-tagged bremsstrahlung photon beam of the Mainz Microtron (MAMI) [46,47]. The photon energies were determined by the Glasgow tagging spectrometer [48–50].

The CB detector is a sphere consisting of 672 optically isolated NaI(Tl) crystals, shaped as truncated triangular pyramids, which point toward the center of the sphere. The crystals are arranged in two hemispheres that cover 93% of 4π , sitting outside a central spherical cavity with a radius of 25 cm, which contains the target and inner detectors. In this experiment, TAPS was arranged in a plane consisting of 384 BaF₂ counters of the hexagonal cross section. It was installed 1.5 m downstream of the CB center and covered the full azimuthal range for polar angles from 1° to 20°. More details on the energy and angular resolution of the CB and TAPS are given in Refs. [38,51].

The present measurement used electron beams with energies of 1508 and 1557 MeV from the Mainz Microtron, MAMI-C [47]. The data with the 1508-MeV beam were taken in 2007 (Run I) and those with the 1557-MeV beam in 2009 (Run II). Bremsstrahlung photons, produced by the beam electrons in a 10- μ m Cu radiator and collimated by a 4-mm-diameter Pb collimator, were incident on a liquid hydrogen (LH₂) target located in the center of the CB. The LH₂ target was 5-cm and 10-cm long in Run I and Run II, respectively.

The target was surrounded by a particle identification (PID) detector [52] used to distinguish between charged and neutral particles. It is made of 24 scintillator bars (50-cm long, 4-mm thick), arranged as a cylinder with a radius of 12 cm.

The energies of the incident photons were analyzed up to 1402 MeV in Run I and up to 1448 MeV in Run II, by detecting the postbremsstrahlung electrons in the Glasgow tagged-photon spectrometer (Glasgow tagger) [48–50]. The uncertainty in the energy of the tagged photons is mostly determined by the segmentation of the tagger focal-plane detector in combination with the energy of the MAMI electron beam used in the experiments. Increasing the MAMI energy increases the energy range covered by the spectrometer and also has the corresponding effect on the uncertainty in E_γ . For both the MAMI energy settings of 1508 and 1557 MeV, this uncertainty was about ± 2 MeV. More details on the tagger energy calibration and the corresponding uncertainties can be found in Ref. [50].

The experimental trigger in Run I required the total energy deposited in the CB to exceed ~ 320 MeV and the number of so-called hardware clusters in the CB (multiplicity trigger) to be two or more. In the trigger, a hardware cluster in the CB was a block of 16 adjacent crystals in which at least one crystal had an energy deposit larger than 30 MeV. Depending on the data-taking period, events with a cluster multiplicity of two were prescaled with different rates. TAPS was not included in the multiplicity trigger for these experiments. In Run II, the trigger on the total energy in the CB was increased to ~ 340 MeV, and the multiplicity trigger required ≥ 3 hardware clusters in the CB.

III. DATA HANDLING

The events from the $\gamma p \rightarrow \pi^0 \eta p$ reaction were searched for in the four-photon final state produced via the $\eta \rightarrow 2\gamma$ decay mode. The $\gamma p \rightarrow 4\gamma p$ candidates were extracted from events with four or five clusters reconstructed in the CB and TAPS together by a software analysis. Five-cluster events were analyzed by assuming that all final-state particles had been detected, and four-cluster events by assuming that the detected particles were photons.

Because another strong contribution to the four-photon final state comes from the $\gamma p \rightarrow \pi^0 \pi^0 p$ reaction, the latter events have to be separated from $\gamma p \rightarrow \pi^0 \eta p \rightarrow 4\gamma p$ events. To identify these two processes, both hypotheses were tested with a kinematic fit and its output was used to reconstruct the reaction kinematics. Details of the kinematic-fit parametrization of the detector information and resolutions are given in Ref. [51]. The selection criteria for $\gamma p \rightarrow \pi^0 \eta p \rightarrow 4\gamma p$ events were optimized by using Monte Carlo (MC) simulations of both reactions and from knowing the production rate of $\gamma p \rightarrow \pi^0 \pi^0 p$ [13] with respect to the $\pi^0 \eta$ final state. The selection criteria were optimized to leave less than 1% of the $\gamma p \rightarrow \pi^0 \pi^0 p$ background remaining in the selected $\gamma p \rightarrow \pi^0 \eta p \rightarrow 4\gamma p$ events within the entire energy range of the measurement. The analysis of the MC simulations showed that, for both the reactions that contribute to the four-photon final state, there are events for which both tested hypotheses give a reasonable probability. It was found that the contribution from $\gamma p \rightarrow \pi^0 \pi^0 p$ becomes less than 1% after applying the following criteria for the kinematic-fit probabilities: The probability P for the $\gamma p \rightarrow \pi^0 \eta p \rightarrow 4\gamma p$ kinematic-fit hypothesis had to be larger than 3% for five-cluster events and larger than 8% for four-cluster events, while $P(\gamma p \rightarrow \pi^0 \pi^0 p \rightarrow 4\gamma p)$ had to be less than 0.1% for both cluster multiplicities.

The background remaining in the selected $\gamma p \rightarrow \pi^0 \eta p \rightarrow 4\gamma p$ events originated from only two sources, which could both be directly subtracted from the experimental spectra. The first background was from interactions of the bremsstrahlung photons in the windows of the target cell. The subtraction of this background was based on the analysis of data samples that were taken with an empty (no liquid hydrogen) target cell. The statistical weight for the subtraction of the empty-target spectra was taken as a ratio of the photon-beam fluxes for the data samples with the full and the empty target. The second background was caused by random coincidences between tagger counts and experimental triggers. The subtraction of this background was carried out by using event samples for which all coincidences were random (see Refs. [38,51] for more details).

The MC simulations of the $\gamma p \rightarrow \pi^0 \pi^0 p$ reaction were based on a previous study of this reaction with the same data sets [13], which, in the given energy range, revealed the dominance of the $\gamma p \rightarrow \Delta(1232)\pi^0 \rightarrow \pi^0 \pi^0 p$ process, with a smaller contribution from $\gamma p \rightarrow D_{13}(1520)\pi^0 \rightarrow \pi^0 \pi^0 p$. The tests carried out for both processes showed the same efficiency for eliminating the $\gamma p \rightarrow \pi^0 \pi^0 p$ reaction with the above selection cuts.

The simulations of $\gamma p \rightarrow \pi^0 \eta p \rightarrow 4\gamma p$ events used four models: phase space, $\gamma p \rightarrow \Delta(1232)\eta \rightarrow \pi^0 \eta p$, $\gamma p \rightarrow$

$S_{11}(1535)\pi^0 \rightarrow \pi^0\eta p$, and $\gamma p \rightarrow a_0(980)p \rightarrow \pi^0\eta p$, with the $\Delta(1232)$, $S_{11}(1535)$, and $a_0(980)$ Breit-Wigner (BW) parameters taken from the Review of Particle Physics (RPP) [1]. All production angles and the resonance decay distributions were generated isotropically.

For all reactions, the generated events were propagated through a GEANT (version 3.21) simulation of the experimental setup. To reproduce the resolutions observed in the experimental data, the GEANT output (energy and timing) was subject to additional smearing, allowing both the simulated and experimental data to be analyzed in the same way. Matching the energy resolution between the experimental and MC events was achieved by adjusting the invariant-mass resolutions, the kinematic-fit stretch functions (or pulls), and probability distributions. Such an adjustment was based on the analysis of the same data sets for reactions having almost no background from other physical reactions (namely, $\gamma p \rightarrow \pi^0 p$, $\gamma p \rightarrow \eta p \rightarrow \gamma\gamma p$, and $\gamma p \rightarrow \eta p \rightarrow 3\pi^0 p$ [51]). The simulated events were also tested to check whether they passed the trigger requirements.

IV. MAINZ MODEL

The theoretical analysis of the present $\gamma p \rightarrow \pi^0\eta p$ data was made within the framework of a revised isobar model, developed earlier by the Mainz group. In this model, the photoproduction amplitude consists of the three parts: (i) the Born amplitude, (ii) the resonant terms, and (iii) additional background contributions,

$$t = t^B + t^R + t^{Bc}. \quad (1)$$

The first two terms are basically similar to those used in the earlier model version and the analysis [19] of the data from Run I. The Born term t^B contains the diagrams in which the intermediate state includes a virtual nucleon or the $N(1535)1/2^-$ resonance in the direct or the crossed channel [see diagrams (a)–(f) in Fig. 2 of Ref. [19]].

The resonance part t^R is represented by the standard nonrelativistic BW form. Based on the two dominant $\pi\eta N$ decay modes, the resonance amplitude can be represented as the intermediate formation of the two quasi-two-body states $\eta\Delta(1232)$ and $\pi N(1535)$,

$$t^R = t^{R(\eta\Delta)} + t^{R(\pi N^*)}. \quad (2)$$

Each term in Eq. (2) has the form,

$$t_{m_f\lambda}^{R(\alpha)} = \sum_{R(J^\pi)} \frac{A_\lambda^R f_{R\alpha}}{W - M_R + \frac{i}{2}\Gamma_{\text{tot}}^R(W)} \times F^{J^\pi(\alpha)} \Omega_{m_f\lambda}^{J^\pi}(\Omega_\pi, \Omega_\eta, \Omega_p), \quad \alpha = \eta\Delta, \pi N^*, \quad (3)$$

where the quantum numbers of the initial and final states are the total γN helicity λ and the z projection m_f of the final-nucleon spin. The summation in Eq. (3) is over the Δ -like resonance states $R(J^\pi)$, determined by their spin-parity J^π and having the BW masses and widths M_R and Γ_{tot}^R . A_λ^R are the helicity functions of the transition $\gamma p \rightarrow R$ with $\lambda = 1/2, 3/2$. For the

$\Delta(1700)3/2^-$ resonance, A_λ^R is energy dependent according to

$$A_\lambda^R(W) = A_\lambda^R(M_R) \left(\frac{\omega_\gamma}{\omega_\gamma^R} \right)^{3/2}, \quad (4)$$

where ω_γ is the c.m. photon energy and ω_γ^R is its energy calculated at the resonance position $W = M_R$.

The coupling constants $f_{R\alpha}$ in Eq. (3) determine the decay of the resonance R into the quasi-two-body channel $\alpha = \eta\Delta, \pi N^*$. Depending on the invariant energies $\omega_{\eta N}$ and $\omega_{\pi N}$ of the ηN and πN subsystems, the factors $F^{J^\pi(\alpha)}$ are

$$F^{J^\pi(\eta\Delta)} = \frac{f_{\Delta\pi N}}{m_\pi^{L_\eta+1}} G_\Delta(\omega_{\pi N}) q_\eta^{L_\eta} q_\pi^*, \quad (5)$$

$$F^{J^\pi(\pi N^*)} = \frac{f_{N^*\eta N}}{m_\pi^{L_\pi}} G_{N^*}(\omega_{\eta N}) q_\pi^{*L_\pi}, \quad (6)$$

where G_Δ and G_{N^*} are the Δ and N^* propagators that have the same nonrelativistic BW form. The quantum numbers L_η and L_π , determined by J^π , are the relative orbital angular momenta associated with the $\eta\Delta$ and πN^* decays of the resonance R . The functions $\Omega_{m_f\lambda}^{J^\pi}$ in Eq. (3) describe the full angular dependence of the transition amplitude $t_{m_f\lambda}^{R(\alpha)}$.

Compared to the previous model [19], the photoproduction amplitude from Eq. (1) now includes a new term that represents the background amplitude t^{Bc} . This term involves only the lowest partial waves with $J \leq 5/2$ and, as described below, was treated in a phenomenological manner. The major constraint of the theory is that the t^{Bc} contribution should be small, wherever possible, and should have a weak energy dependence. Although the background term does not have a simple physical picture, by introducing this term, it is accepted that there is no present theory capable of correctly predicting nonresonant contributions in the lower partial waves of the reaction under study. Indeed, in the earlier analysis of Ref. [19], the nonresonant part of the photoproduction amplitude was represented only by the Born amplitude t^B , whereas, in the BnGa model [28], the known dominant Regge exchanges were used instead. In addition, including the t^{Bc} term effectively takes into account possible contributions from resonances with larger masses, which are not included in the model but can affect our energy range through their BW tails.

The parametrization of the t^{Bc} term is similar to Eqs. (2) and (3),

$$t^{Bc} = t^{Bc(\eta\Delta)} + t^{Bc(\pi N^*)}, \quad (7)$$

but with the BW dependence replaced with energy-dependent functions $f_{J^\pi}^{(\alpha)}(W)$:

$$t_{m_f\lambda}^{Bc(\alpha)} = \sum_{J^\pi} f_{J^\pi}^{(\alpha)}(W) F^{J^\pi(\alpha)} \Omega_{m_f\lambda}^{J^\pi}(\Omega_\pi, \Omega_\eta, \Omega_p). \quad (8)$$

To determine the energy dependence of the t^{Bc} terms, the data were first fitted with only four principal resonances: $\Delta(1700)3/2^-$, $\Delta(1905)5/2^+$, $\Delta(1920)3/2^+$, and $\Delta(1940)3/2^-$, which, according to analyses reported in Refs. [19,28], dominate in the given energy range. The parameters of these four resonances were fixed to the results obtained for them in Ref. [19]. With such an input, the amplitudes

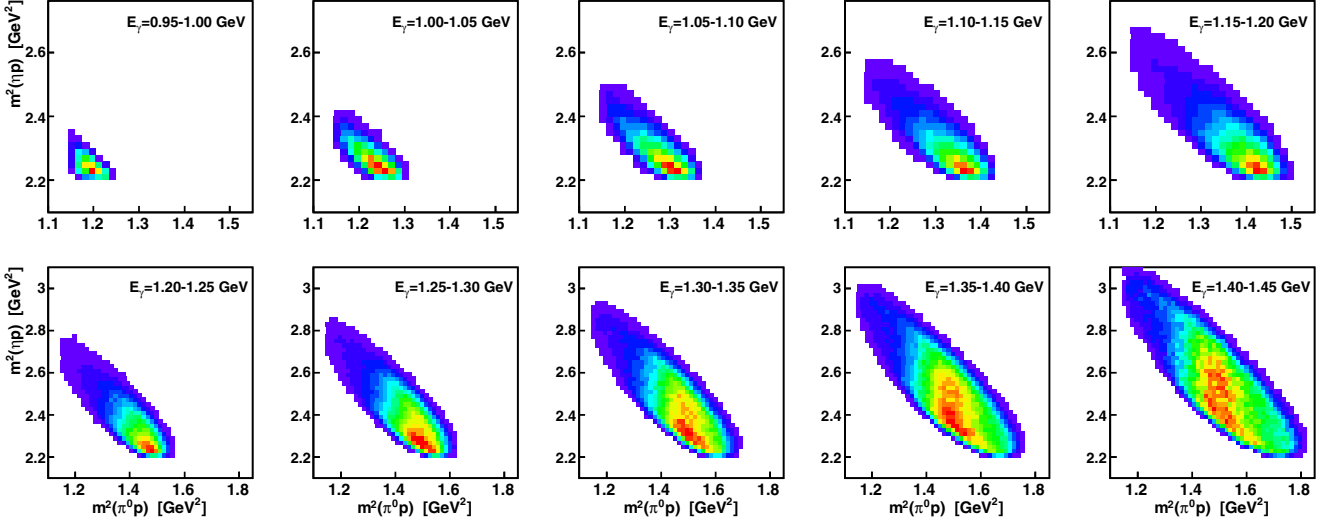


FIG. 1. Experimental Dalitz plots of $m^2(\eta\pi)$ vs $m^2(\pi^0\pi)$ combined from Run I and Run II, shown for 10 energy intervals between $E_\gamma = 0.95$ GeV and 1.45 GeV.

t^{Bc} were adjusted by fitting the data independently for each individual energy bin. After the full energy range was covered, the energy dependence of these background amplitudes was analyzed in each partial wave J^π to look for a resonancelike behavior. Where the function $f_{J^\pi}^{(\alpha)}$ from Eq. (8) demonstrated strong variation with energy, an additional BW resonance was introduced into the amplitude J^π . The parameters of the new resonances were then determined during the subsequent fit to the data, performed over the full energy range. The parameters of the four principal resonances were also allowed to vary during the second fit. Free resonance parameters included M_R , $A_\lambda^R(M_R)$, $\sqrt{\beta_{\eta\Delta}}A_{1/2}$, $\sqrt{\beta_{\pi N^*}}A_{1/2}$, and the ratio $A_{3/2}/A_{1/2}$, with quantities $\beta_\alpha = \Gamma_{(\alpha)}^R/\Gamma_{\text{tot}}^R$ for $\alpha = \eta\Delta, \pi N^*$ are the partial decay widths for $R \rightarrow \alpha$. As explained previously in Ref. [19], because the resonance amplitudes depend on the product of the

electromagnetic and hadronic vertices, the helicity functions A_λ^R and the partial decay widths $\Gamma_{(\alpha)}^R$ cannot be determined separately with reliable accuracy, forcing the use of their products $\sqrt{\beta_\alpha}A_{1/2}$ together with the ratio of $A_{3/2}/A_{1/2}$. The total widths of resonances Γ_{tot}^R were fixed in the fits to their magnitudes from RPP [1] or previous PWAs [22–24,28]. As explained in Ref. [19], the reason for fixing these values lies in the closeness of the resonances, especially the $\Delta(1700)3/2^-$ state, to the reaction threshold, so that the experimental data do not provide sufficient constraints to extract resonance widths from the fit.

To assure the smooth energy dependence of the background amplitudes remaining after introducing the new resonances, the functions $f_{J^\pi}^{(\alpha)}$ in Eq. (8) were parametrized in terms of polynomials of order 2 (where the nonessential index J^π is

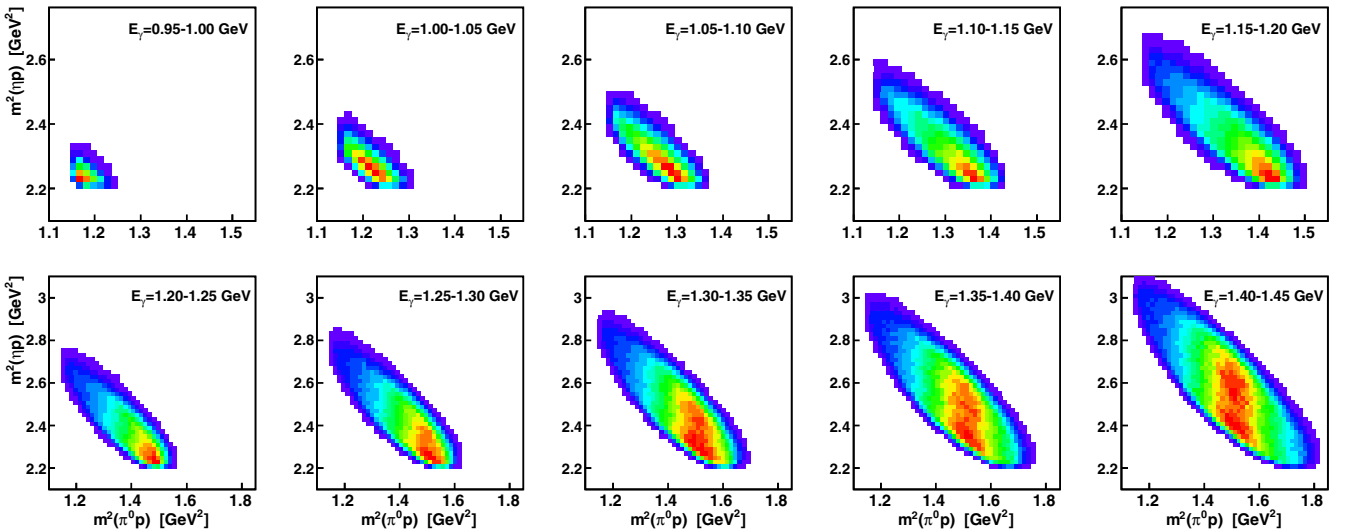
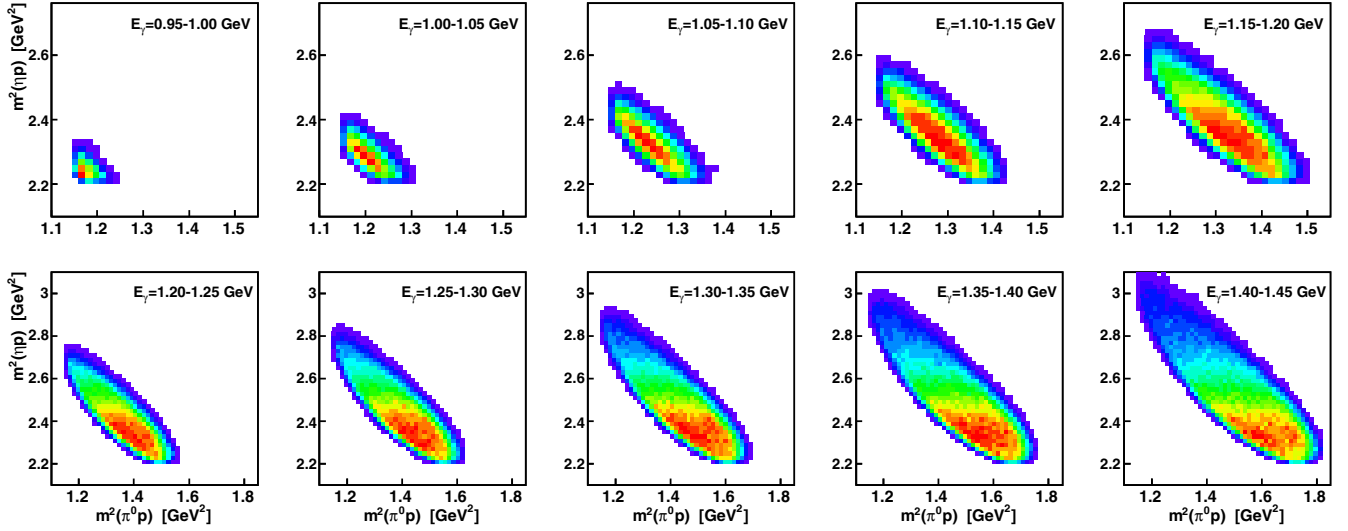


FIG. 2. Same as Fig. 1, but for MC simulation of $\gamma p \rightarrow \Delta(1232)\eta \rightarrow \pi^0\eta p$.

FIG. 3. Same as Fig. 1, but for MC simulation of $\gamma p \rightarrow N(1535)\pi^0 \rightarrow \pi^0\eta p$.

omitted),

$$f^{(\omega)}(W) = \sum_{n=0}^2 C_n \left(\frac{W}{M_N + m_\eta + m_\pi} \right)^n, \quad (9)$$

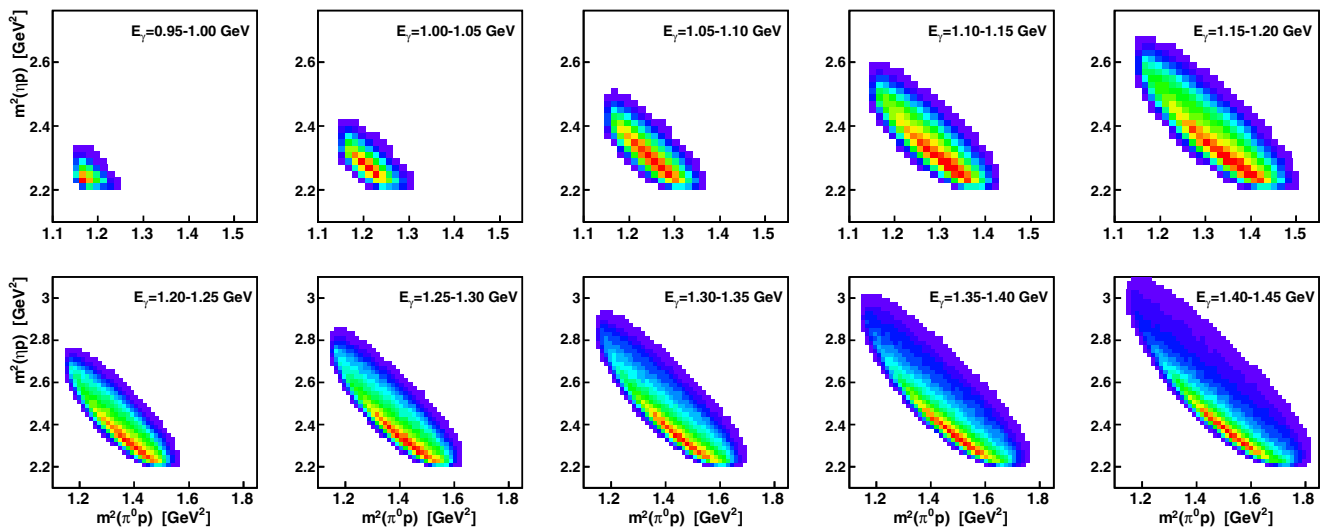
with complex coefficients C_n .

Speaking of the reliability of the present fit to the data, it is well known that, with limited polarization data, the fit solution may not be unique. Therefore, a rapid change in the background parameters within a narrow energy range could occur, not because of a real resonance, but owing to an accidental jump from one solution to another similar solution. Such a possibility was not investigated systematically here. However, the possible existence of alternative solutions was studied by varying the initial parameters for the four principal resonances mentioned above. In the end, although initial single-energy fits were yielding quite different background

amplitudes, the subsequent fits, with all model parameters released, converged to the same solution.

V. RESULTS AND DISCUSSION

One of the most informative distributions for the three-body final-state reactions are their Dalitz plots and the energy dependence of their density distributions. In Fig. 1, the experimental Dalitz plots of $m^2(\eta p)$ vs $m^2(\pi^0 p)$, obtained by combining the results of Run I and Run II together, are shown for ten 50-MeV-wide incident-photon energy intervals in the range from $E_\gamma = 0.95$ GeV to 1.45 GeV. In Figs. 2–4 the corresponding Dalitz plots are shown, respectively, for the MC simulations of $\gamma p \rightarrow \Delta(1232)\eta \rightarrow \pi^0\eta p$, $\gamma p \rightarrow N(1535)\pi^0 \rightarrow \pi^0\eta p$, and $\gamma p \rightarrow a_0(980)p \rightarrow \pi^0\eta p$, where all resonance decays were generated isotropically. As seen from the comparison with Fig. 1, the production of the $\pi^0\eta p$ final state in the given energy range occurs mostly via the $\Delta(1232)\eta$ intermediate

FIG. 4. Same as Fig. 1, but for MC simulation of $\gamma p \rightarrow a_0(980)p \rightarrow \pi^0\eta p$.

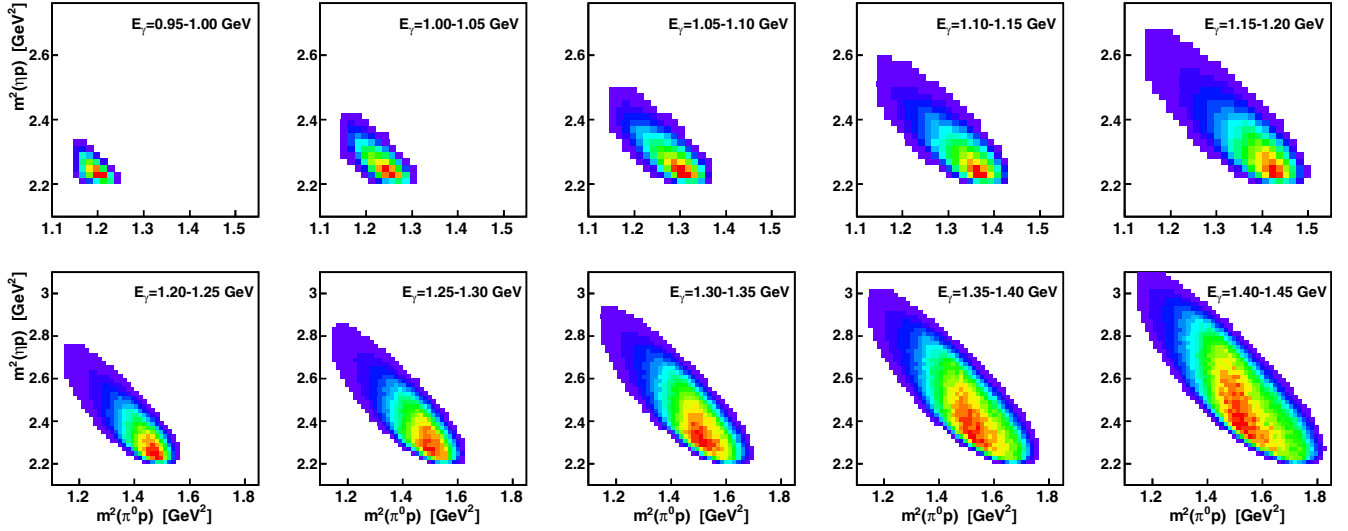


FIG. 5. Same as Fig. 1, but for the phase-space MC simulation weighted with BnGa PWA of the CBELSA/TAPS data [24].

state. The difference in the density along the Δ band reflects the deviation from the isotropic distribution of Δ decay products, used in the MC simulation, with respect to the Δ direction. The higher density of the experimental Δ band at low $m(\eta p)$ masses means that the π^0 mesons from $\Delta \rightarrow \pi^0 p$ decays are produced more in the direction of the Δ . The contribution from $N(1535)1/2^-$ seems to be significantly smaller than from $\Delta(1232)$. According to the analysis of CBELSA/TAPS data [24], the contribution from $\gamma p \rightarrow a_0(980)p \rightarrow \pi^0 \eta p$ reaches a few percent at energies around $E_\gamma = 1.4$ GeV. However, as seen from the Dalitz plots, the visual observation of such a contribution is complicated because the $a_0(980)$ band overlaps with the $\Delta(1232)$ band at this energy. The phase-space MC simulation weighted with BnGa PWA of the CBELSA/TAPS data [24], illustrated in Fig. 5, demonstrates reasonable agreement

with the experimental plots of the present work. For a better comparison with theoretical analyses, the present results for the invariant-mass spectra of $m(\pi^0 p)$, $m(\eta p)$, and $m(\pi^0 \eta)$ are compared in Figs. 6–8 with the BnGa PWA of CBELSA/TAPS data [24] and with the Mainz model used to fit the present data. As seen, the agreement of the experimental results with both the BnGa PWA and Mainz model is quite good, with some discrepancies appearing only for highest energies. The earlier solution of the Mainz model [19,20] is not shown here, as the invariant-mass distributions were not included in that fit.

In addition, it is important to note that, the Dalitz plots and invariant mass spectra at the highest photon energy range shown in Figs. 1 and 7 do not clearly indicate any narrow structure in the vicinity of $m(\eta p) = 1.685$ GeV (or $m^2(\eta p) = 2.84$ GeV²) reported in Ref. [32]. However, it is worth noting

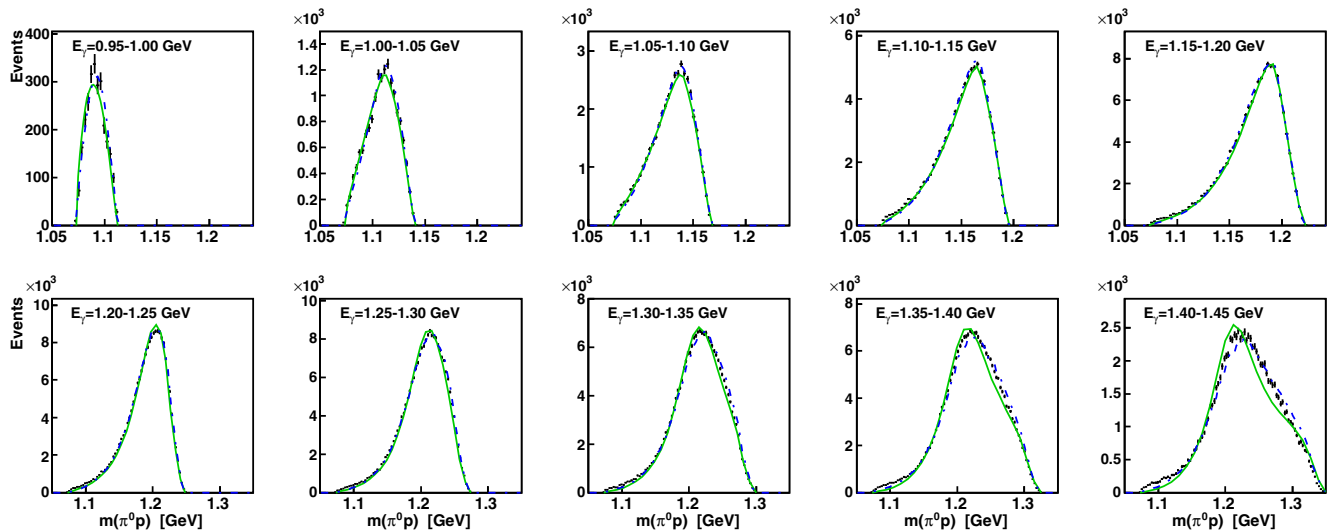
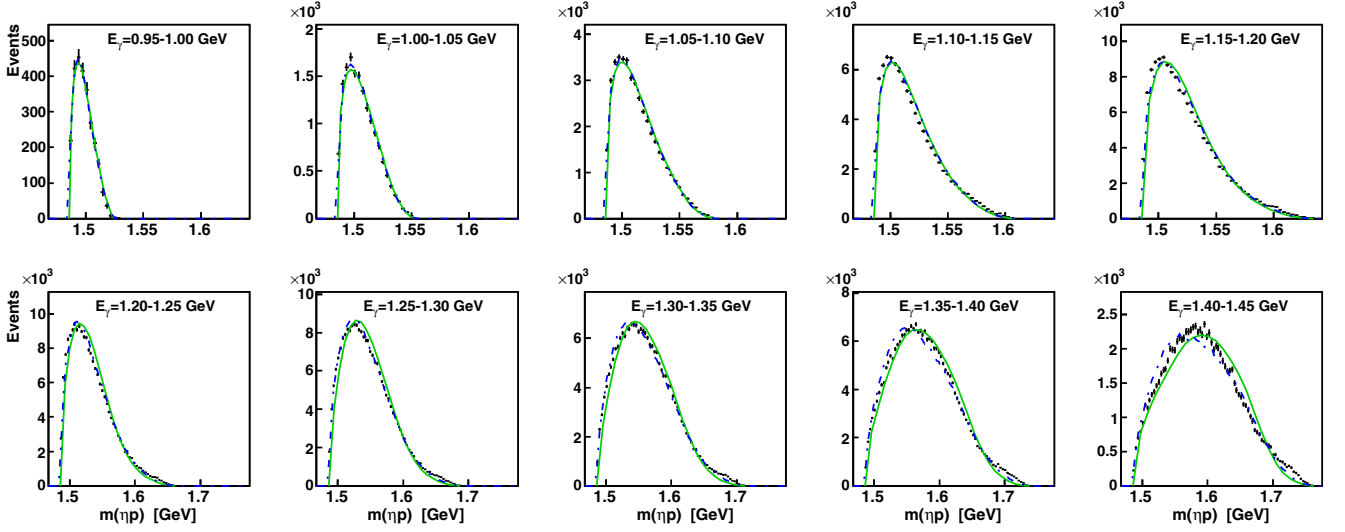


FIG. 6. Comparison of the invariant-mass $m(\pi^0 p)$ spectra combined from Run I and Run II (crosses) with BnGa PWA [24] (blue dash-dotted line) and the Mainz model used to fit the present data (solid green line).

FIG. 7. Same as Fig. 6, but for the invariant mass $m(\eta p)$.

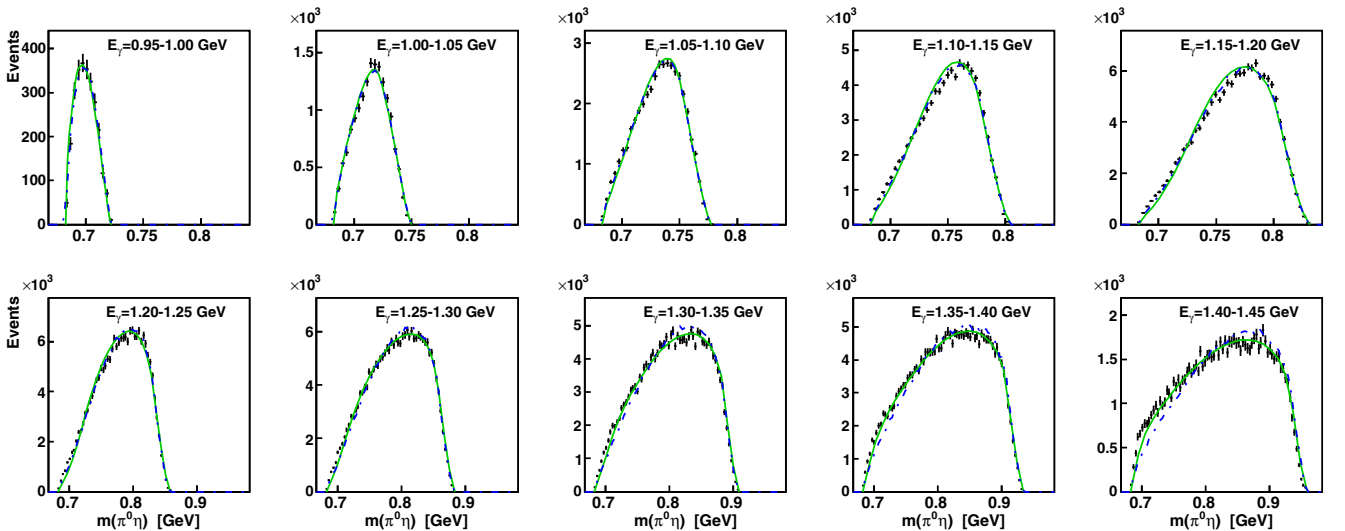
that, compared to the present measurement, the data in Ref. [32] cover higher photon-energy range, reaching $E_\gamma = 1.5$ GeV. Further search for a potential narrow state in the region of $m(\eta p) = 1.685$ GeV or determination of the corresponding upper limit is beyond the topic of the present paper.

Because of the five-dimensional phase space of the $\gamma p \rightarrow \pi^0 \eta p$ reaction, guided by the results for the experimental Dalitz plots and invariant-mass spectra, the acceptance determination was based on MC simulations for $\gamma p \rightarrow \Delta(1232)\eta \rightarrow \pi^0 \eta p$, with a small fraction of phase space added. Thus, the following results for the total and differential cross sections include some systematic uncertainties stemming from approximations in the acceptance correction. Based on the tests with different MC simulations, such systematic uncertainties were estimated to be around 5% at the lowest energies, increasing to 8% at the largest energies. A more precise determination of the reaction dynam-

ics could be made with a PWA based on the event-by-event data, and this work will provide such data for future PWAs.

The $\gamma p \rightarrow \pi^0 \eta p$ total cross sections from Run I and Run II, obtained for the energies of each tagger channel above the reaction threshold, are shown in Fig. 9, illustrating good agreement with each other as well as with previous data and theoretical analyses. In addition to the total cross section, the individual contributions from $\gamma p \rightarrow \Delta(1232)\eta$, $\gamma p \rightarrow N(1535)\pi^0$, and $\gamma p \rightarrow a_0(980)p$ are plotted for BnGa PWA [24], confirming the dominance of the $\Delta(1232)\eta$ intermediate state, seen in the features of the experimental Dalitz plots. For the Mainz model, the individual contributions are plotted for Born (t^B), resonant (t^R), and background (t^{Bc}) terms from Eq. (1), demonstrating the strong dominance of the resonant term.

In the context of the Mainz model [19,20], the most informative observables for understanding the internal dynamics

FIG. 8. Same as Fig. 6, but for the invariant mass $m(\pi^0 \eta)$.

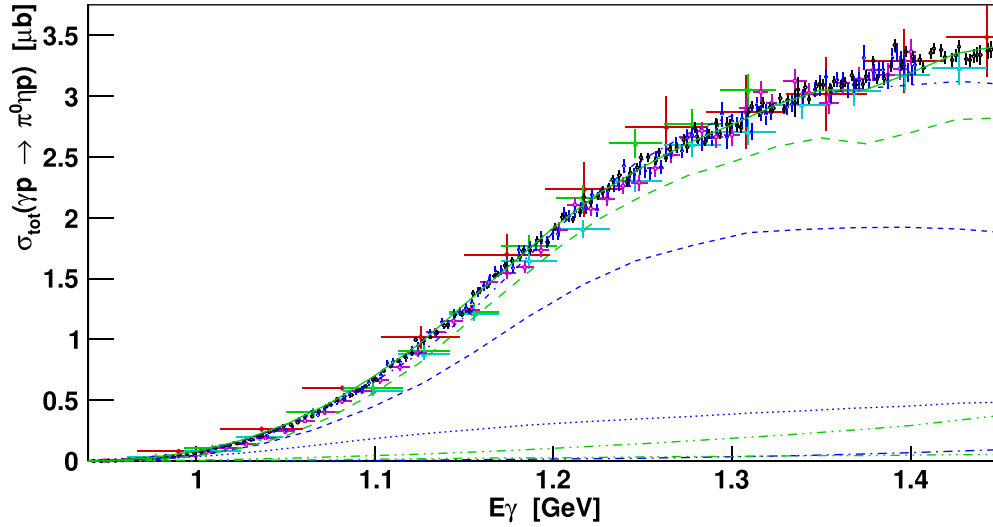


FIG. 9. Comparison of the $\gamma p \rightarrow \pi^0 \eta p$ total cross sections from Run I (blue solid triangles) and Run II (black open circles) with each other and with previous data by CBELSA/TAPS [22,24] (green stars and cyan open triangles, respectively), GRAAL [25] (red crosses), and A2 [20] (magenta open squares). The predictions from BnGa PWA [24] are shown by blue lines for the total cross section (dash-dotted) and individual contributions from $\gamma p \rightarrow \Delta(1232)\eta$ (dashed), $\gamma p \rightarrow N(1535)\pi^0$ (dotted), and $\gamma p \rightarrow a_0(980)p$ (long-dash-dotted). The results from analysis with the Mainz model are shown by green lines for the total cross section (solid) and individual contributions from the resonant (long-dashed), background (dash-double-dotted), and Born (dash-triple-dotted) terms.

of the $\gamma p \rightarrow \pi^0 \eta p$ production are angular distributions in any two-particle rest frame of the three-particle final state. Because the production is dominated by $\gamma p \rightarrow \Delta(1232)\eta$, the $\pi^0 p$ rest frame was chosen for measuring π^0 angular distributions in the canonical and helicity coordinate systems (x', y', z'). In the helicity system, the z' axis was taken along the $\pi^0 p$ total momentum, the y' axis was directed along the vector product of the η and beam-photon vectors taken in the $\pi^0 p$ rest frame. The x' axis is just a vector product of the y' and z' axes. In the canonical system, the z' axis was taken along the beam-photon momentum in the c.m. frame, the y' axis was directed along the vector product of the η and beam-photon vectors also taken in the c.m. frame. In the CBELSA/TAPS analysis [24],

the Gottfried-Jackson (GJ) frame was used instead of the canonical. In the GJ frame, all vectors used in the canonical system are taken in the $\pi^0 p$ rest frame, which makes the π^0 angular distributions very similar, but not identical, for these two systems.

Similarly to the previous analysis of Run I [19,20], the distributions of $\cos \theta$ and angle ϕ of the π^0 meson were measured in both the helicity and canonical frames, where θ and ϕ are, respectively, the polar and azimuthal angles of the π^0 vector within the (x', y', z') coordinate system. The present results include both Runs I and II data (doubling the statistics) and are divided into 10 energy bins, compared to the previous four. In the following comparison of the present results to previous

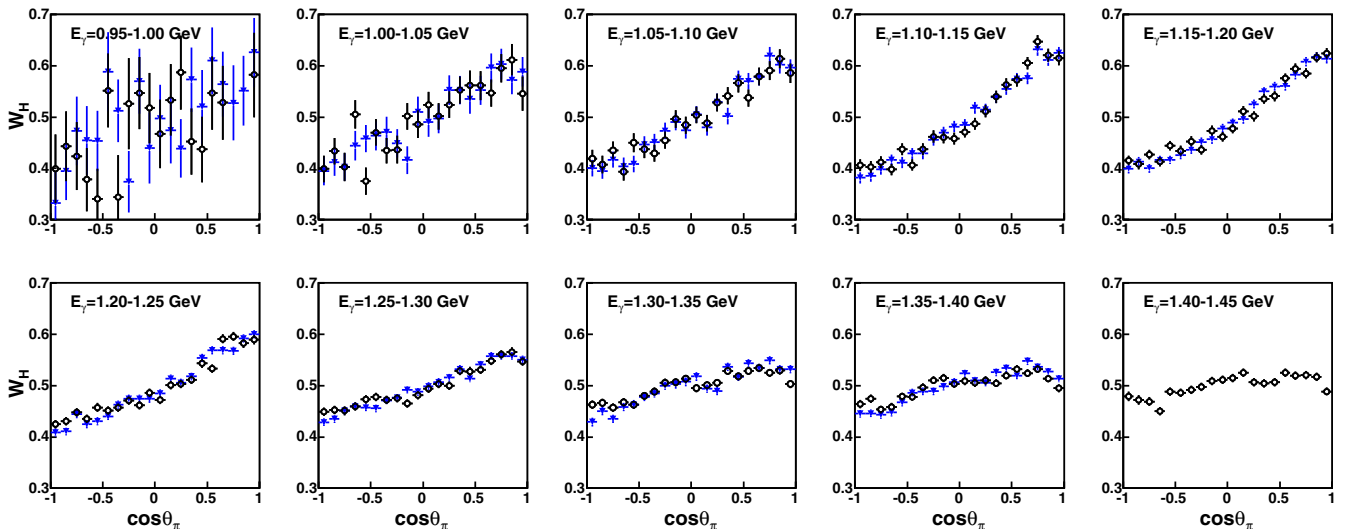
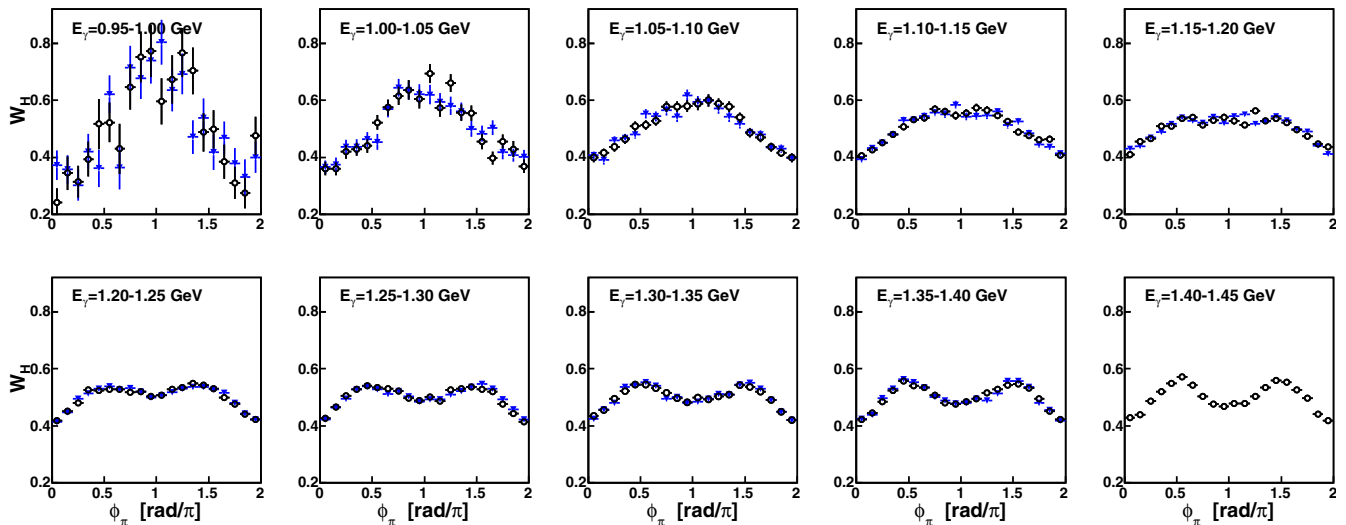


FIG. 10. Comparison of the results from Run I (blue triangles) and Run II (open circles) for the $\cos(\theta_{\pi^0})$ distributions in the helicity frame.

FIG. 11. Same as Fig. 10, but for ϕ_{π^0} .

measurements and predictions of different analyses, the $\cos\theta$ results by CBELSA/TAPS [24] in the GJ frame are used to compare to the canonical-frame results (ϕ distributions were not published by CBELSA/TAPS). For a better comparison of the angular dependencies, all the differential cross sections have been normalized so that their integrals equal one.

Before comparing the present angular distributions to various analyses, the consistency of the results obtained from Run I and Run II is illustrated in Figs. 10 and 11 for the $\cos\theta$ and ϕ distributions obtained for the recoil π^0 in the helicity frame. As seen, the data points from both data sets are in good agreement within their statistical uncertainties. Because the highest-energy bin was not covered in Run I, the combined results are provided only for nine energies.

In Figs. 12 and 13, the combined results for $\cos\theta$ and ϕ of the recoil π^0 in the helicity frame are compared to previous data at similar energies, to predictions by BnGa PWA [24] and by the earlier Mainz model [19], and to the fit of the revised Mainz model to the present data. For better statistical accuracy, the CBELSA/TAPS data points from Refs. [22,24] have been combined together. As seen in Fig. 12, the present $\cos\theta$ distributions in the helicity frame are in better agreement with previous measurements and model analyses for lower energies, and the consistency with the CBELSA/TAPS data and BnGa PWA [24] is better than with the previous A2 analysis [19,20]. The discrepancies are larger for the highest energies, where the results are more sensitive to the acceptance correction, which depends on the reaction dynamics used in the

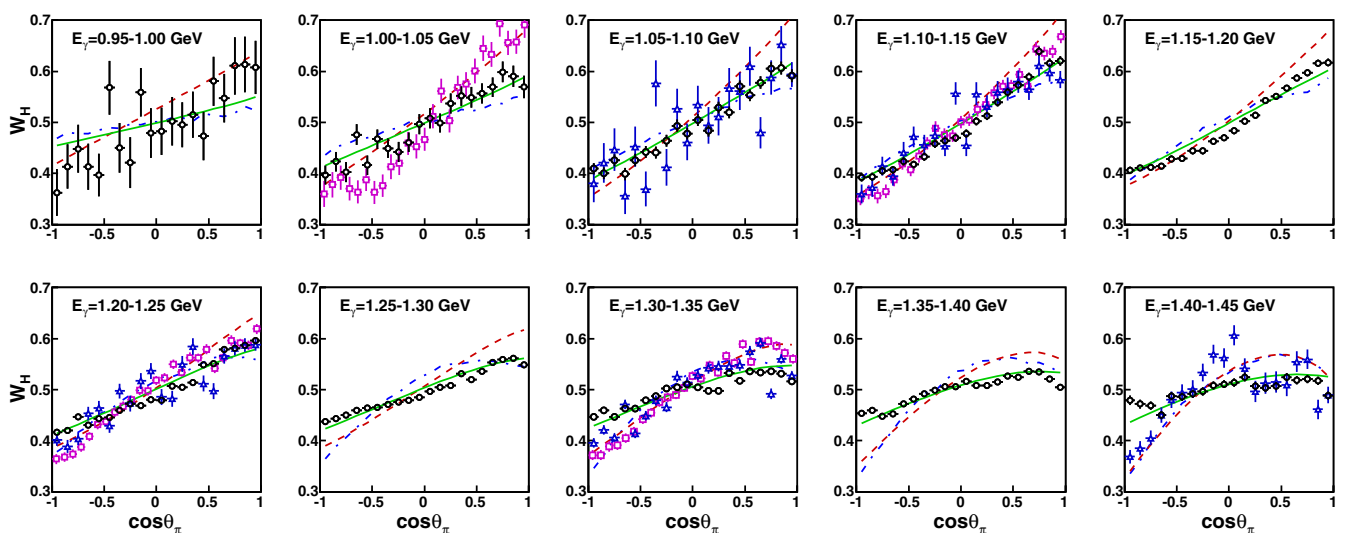
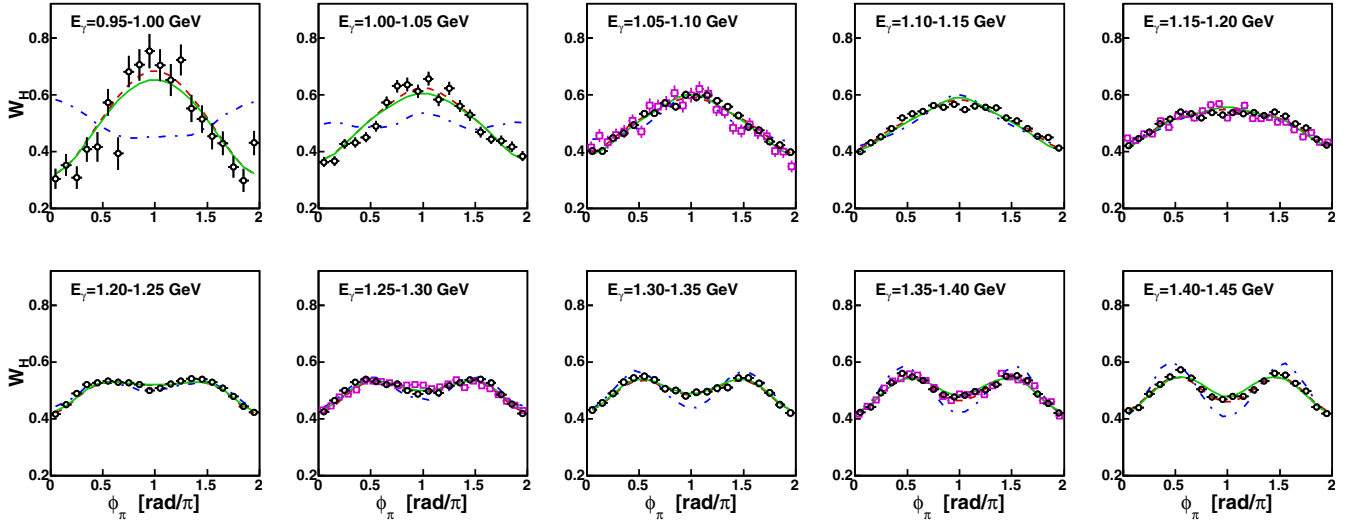


FIG. 12. Comparison of the present helicity-frame $\cos(\theta_{\pi^0})$ distributions, combined from Run I and Run II (open circles), to previous data by CBELSA/TAPS [22,24] (blue stars, data points combined from both the references) and by A2 [20] (magenta open squares) at similar energies, and to predictions by BnGa PWA [24] (blue dash-dotted line) and by the earlier Mainz model [19] (red dashed line), and to the fit of the revised Mainz model to the present data (solid green line).

FIG. 13. Same as Fig. 12, but for ϕ_{π^0} .

corresponding MC simulation. On the other hand, the revised Mainz model is able to describe the present data over the entire energy range. Compared to $\cos\theta$, the present ϕ distributions in the helicity frame are in much better agreement with the previous measurements and analyses, except BnGa PWA [24] at the lowest energies, where the CBELSA/TAPS data have very low statistics.

The comparison of the present results in the canonical frame is given in Figs. 14 and 15 for $\cos\theta$ and ϕ of the recoil π^0 , respectively. As seen, in contrast to the helicity frame, better agreement with previous measurements and analyses is obtained for $\cos\theta$, except BnGa PWA [24] at the lowest energies. The present ϕ distributions in the canonical frame are in better agreement with previous measurements and model analyses for lower energies, and the consistency with BnGa PWA [24] is better than with the previous A2 analysis [19,20]. The discrepancies seen in the highest energies could be caused

by a stronger sensitivity of the results to the model used in the MC simulation to determine the experimental acceptance. The revised Mainz model describes the present data in the canonical frame for the entire energy range. The measurement of production angles of the final-state particles is presented for the η and proton, the c.m. $\cos\theta$ distributions of which are shown in Figs. 16 and 17, respectively

The corresponding distributions for π^0 are not shown as they are very similar to $\cos(\theta_{\pi^0})$ in the canonical or GJ frames. As seen, the present results for η are in good agreement with previous measurements over almost the entire energy range, whereas the proton results contradict the predictions of the BnGa PWA [24] near the reaction threshold. The $\cos\theta$ distributions for the recoil proton are not shown for the earlier analysis of the A2 data [20] as they were not extracted there.

In this work, the measurement of helicity photon asymmetry I^\odot was made for 10 energy bins (the same as for the other

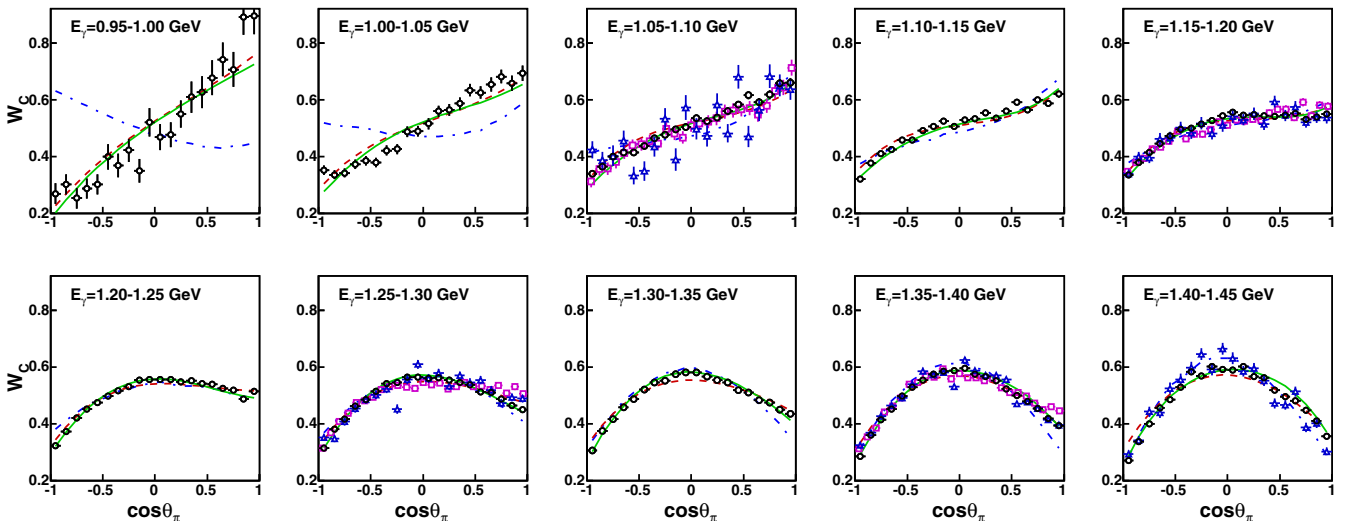
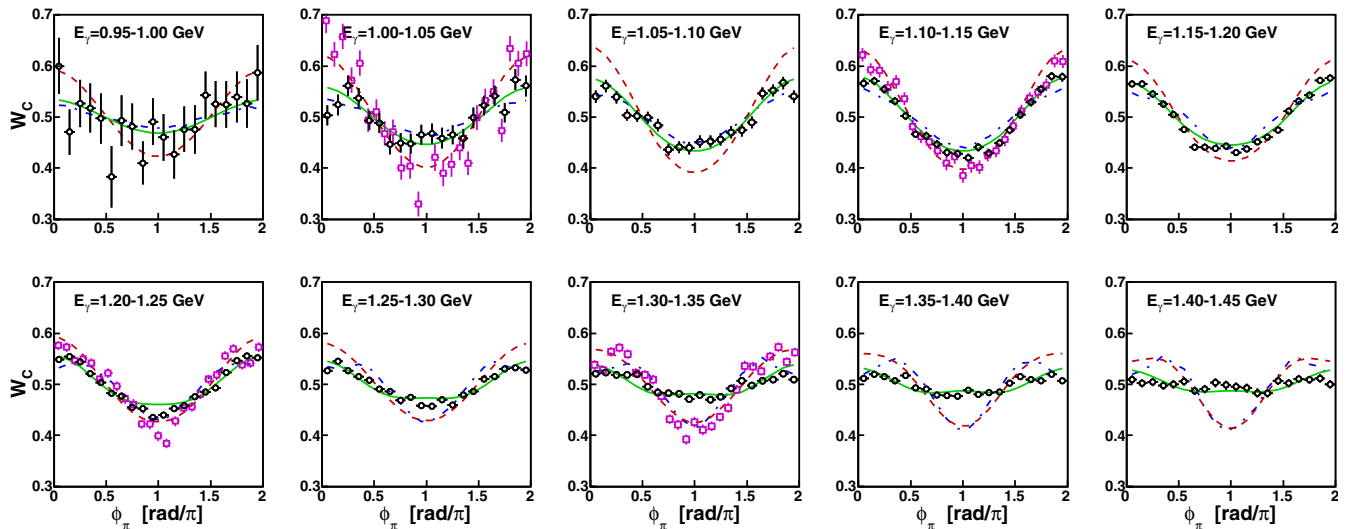


FIG. 14. Same as Fig. 12, but for the canonical frame. The combined data from CBELSA/TAPS [22,24] are shown for the GJ frame.

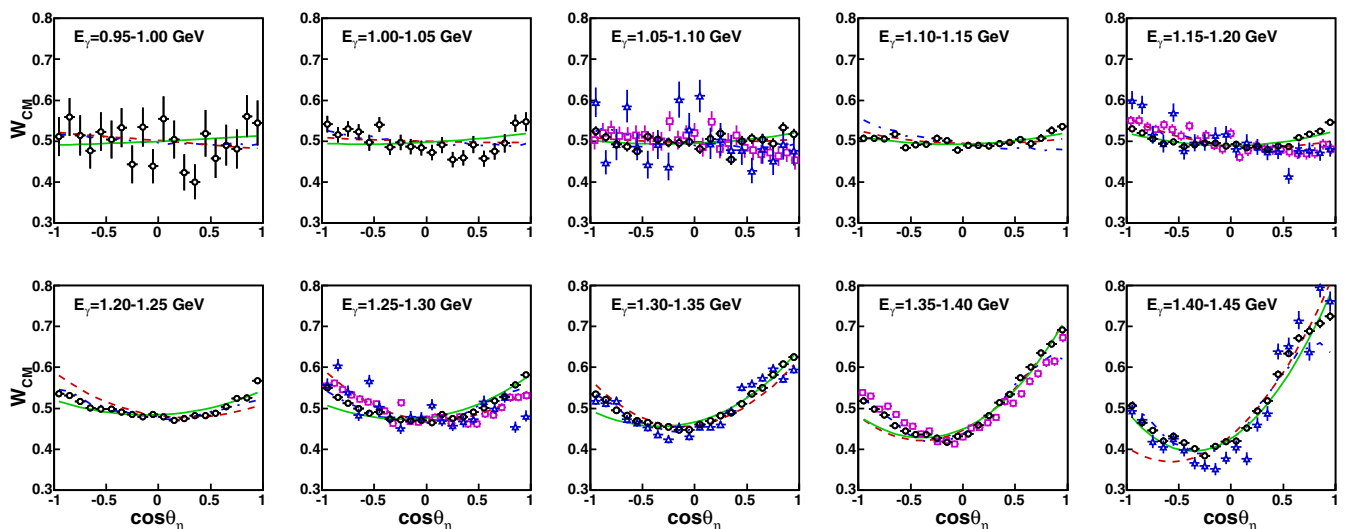
FIG. 15. Same as Fig. 12, but for ϕ_{π^0} in the canonical frame.

observables), compared to four energy bins in Ref. [21], the analysis of which was based on Run II only. In Fig. 18, the present I^\odot results are compared to the previous data from Ref. [21], to predictions by BnGa PWA [24], to the earlier Mainz model [19], and to the fit with the revised model. As seen, the present results for I^\odot are in good agreement with the previous data [21] within the error bars, whereas the fit with the revised Mainz model deviates from the earlier version. The discrepancy with the BnGa PWA [24] is larger, and increases with energy.

In summary, the present $\gamma p \rightarrow \pi^0 \eta p$ data demonstrate better statistical accuracy, with finer energy binning, compared to previous measurements. The consistency of the present results with the earlier data and analyses is partial for some observables and energy ranges. For the most part, the observed discrepancies could be explained by the sensitivity of results to the five-dimensional acceptance correction and by

poorer statistics and wider energy binning of the previous measurements. The discrepancies with the BnGa PWA [24] are expected to be reduced by adding the present data into their new fit on the event-by-event basis. Such an analysis is now in progress and will be published by the BnGa group separately. Compared to the earlier Mainz model [19], its revised version includes more observables in the fit and, as demonstrated in the figures, is able to describe their shape and energy dependencies over the entire energy range.

As discussed above, the earlier Mainz model [19] included only the first two terms of the amplitude (1), used in the revised version. The main reason for introducing the purely phenomenological term t^{Bc} was the fact that refitting the parameters of the earlier model to the entire set of the new results was not sufficient for a good description. After introducing the background amplitudes, it was found that the set of the four principal isobars ($\Delta(1700)3/2^-$, $\Delta(1905)5/2^+$,

FIG. 16. Same as Fig. 12, but for $\cos(\theta_\eta)$ spectra in the c.m. frame.

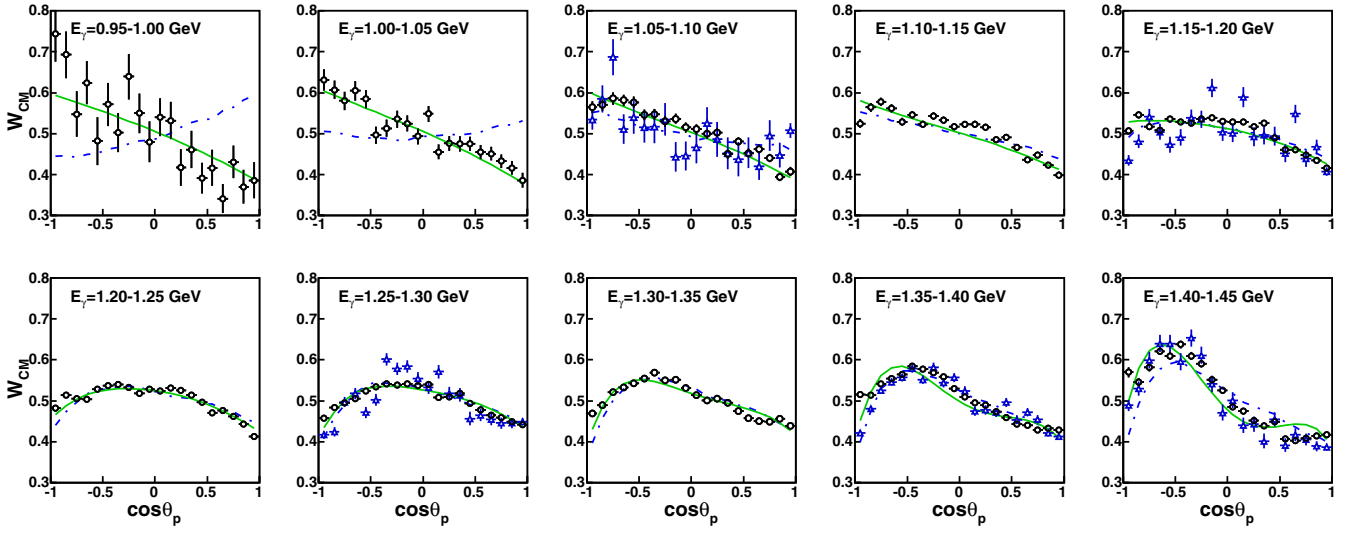


FIG. 17. Same as Fig. 12, but for the recoil proton $\cos(\theta_p)$ spectra in the c.m. frame.

$\Delta(1920)3/2^+$, and $\Delta(1940)3/2^-$) is sufficient for the resonance term t^R to describe the data, and the $\Delta(1600)3/2^+$ and $\Delta(1750)1/2^+$ states, the contributions of which were less important in the analysis of Ref. [19], were found to be unnecessary now. Also, similarly to the previous analysis [19], there was no clear need to include resonances in the $1/2^-$ and $5/2^-$ waves to improve the data description. Though the contribution from the background term t^{Bc} is considerably smaller than the resonant term t^R (see Fig. 9), its introduction improves the fit's χ^2/ndf from 7.3 to 3.7, using the statistical uncertainties only. Another observation made from the fit to the present data is that the background amplitudes tend to cancel the Born amplitudes at higher energies, especially in the dominant $3/2^-$ wave.

The resonance parameters obtained in the fit to the present data are listed in Table I, along with the corresponding resonances and parameters obtained for them in Ref. [19]. As seen, the parameters of the dominant resonance $\Delta(1700)3/2^-$ are practically the same, whereas those of the other resonances changed. Similarly to Ref. [19], the systematic uncertainties were not used in the fit with the revised Mainz model.

VI. SUMMARY AND CONCLUSIONS

The data available from the A2 Collaboration at MAMI were analyzed to select the $\gamma p \rightarrow \pi^0 \eta p$ reaction on an event-by-event basis, which allows for partial-wave analyses of three-body final states to obtain more reliable results, compared

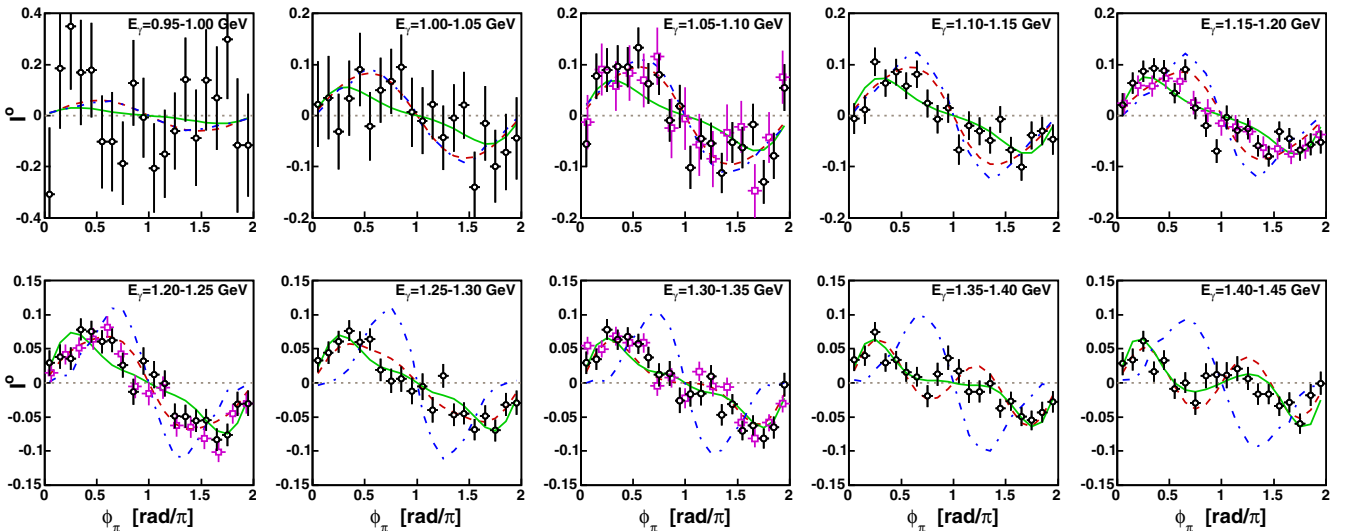


FIG. 18. Comparison of the present results for helicity photon asymmetry I^0 (open circles) to the previous analysis from Ref. [21] (magenta open squares) at similar energies, to predictions by BnGa PWA [24] (blue dash-dotted line) and by the earlier Mainz model [19] (red dashed line), and to the fit with its revised version to the present data (solid green line).

TABLE I. Parameters found for the resonances included in the revised Mainz model, compared in the second row with the corresponding values obtained in the earlier analysis of Ref. [19]. The quantities $\beta_\alpha = \Gamma_{(\alpha)}^R / \Gamma_{\text{tot}}^R$ for $\alpha = \eta\Delta, \pi N^*$ are the partial decay widths for $R \rightarrow \alpha$.

$J^\pi [L_{2T2J}(M_R)]$	M_R (MeV)	$\Gamma_{\text{tot}}^R(M_R)$ (MeV)	$\sqrt{\beta_{\eta\Delta}} A_{1/2}(M_R)$ ($10^{-3}\text{GeV}^{-1/2}$)	$\sqrt{\beta_{\pi N^*}} A_{1/2}(M_R)$ ($10^{-3}\text{GeV}^{-1/2}$)	$A_{3/2}(M_R)/A_{1/2}(M_R)$
$\Delta(1700)3/2^-$	1704 ± 1	375	12.0 ± 0.2	8.4 ± 0.1	0.80 ± 0.02
	1701 ± 1	375	10.6 ± 0.2	8.9 ± 0.4	0.95 ± 0.01
$\Delta(1905)5/2^+$	1990 ± 4	330	-44.8 ± 0.5	-1.5 ± 0.2	-0.71 ± 0.02
	1873 ± 4	330	-25.5 ± 0.6	-2.4 ± 0.4	-0.70 ± 0.03
$\Delta(1920)3/2^+$	1948 ± 5	260	5.7 ± 0.3	2.1 ± 0.1	4.40 ± 0.05
	1894 ± 3	200	11.9 ± 0.4	4.4 ± 0.4	1.15 ± 0.06
$\Delta(1940)3/2^-$	1819 ± 1	450	10.7 ± 1.0	3.5 ± 0.2	2.30 ± 0.02
	1870 ± 1	450	19.9 ± 1.2	9.3 ± 0.7	1.65 ± 0.02

to fits to measured distributions. These data provide the world's best statistical accuracy in the energy range from threshold to $E_\gamma = 1.45$ GeV, allowing a finer energy binning in the measurement of all observables needed for understanding the reaction dynamics. In this work, the $\gamma p \rightarrow \pi^0 \eta p$ data are compared to the existing BnGA PWA and to the earlier Mainz model. The potential impact of the present data on future analyses was demonstrated by fitting these results with the revised Mainz model, which was able to describe all the differential cross sections and their energy dependencies over the entire energy range. The invariant-mass distributions and Dalitz plots measured in this work for energies $E_\gamma < 1.45$ GeV do not show any clear indication for a narrow structure in the region of $m(\eta p) = 1.685$ GeV reported in Ref. [32].

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