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Genetic algorithms used for the optimization of light-emitting diodes and solar thermal collectors

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ABSTRACT

We present a genetic algorithm (GA) we developed for the optimization of light-emitting diodes (LED) and solar thermal collectors. The surface of a LED can be covered by periodic structures whose geometrical and material parameters must be adjusted in order to maximize the extraction of light. The optimization of these parameters by the GA enabled us to get a light-extraction efficiency η of 11.0% from a GaN LED (for comparison, the flat material has a light-extraction efficiency η of only 3.7%). The solar thermal collector we considered consists of a waffle-shaped Al substrate with NiCrO_x and SnO₂ conformal coatings. We must in this case maximize the solar absorption α while minimizing the thermal emissivity ϵ in the infrared. A multi-objective genetic algorithm has to be implemented in this case in order to determine optimal geometrical parameters. The parameters we obtained using the multi-objective GA enable α -97.8% and ϵ -4.8%, which improves results achieved previously when considering a flat substrate. These two applications demonstrate the interest of genetic algorithms for addressing complex problems in physics.

Keywords: genetic algorithm, optimization, light-emitting diode, solar thermal collector, GaN, Al, cermet

1. INTRODUCTION

Nature has developed its own algorithms for determining optimal solutions. With genetic algorithms (GA), we actually mimic natural selection in order to determine the optimal solutions of complex problems in physics. The idea to implement natural selection to problems that are not related to biology is due to Holland.¹ Other pioneering works on this subject were presented by De Jong,² Baker,³ Goldberg,⁴ Harik,⁵ etc. While fundamental aspects of these evolutionary algorithms continue to be investigated,⁶ their usefulness is proven by a growing number of applications.^{7.9}

The idea of genetic algorithms consists in working with a population of individuals, each of them representing a given set of physical parameters and therefore a given value of the objective function we seek at optimizing. The initial population usually consists of individuals with random parameters. The best individuals are selected for the next generation. They are also allowed to breed in order to generate new individuals. Mutations are finally introduced as additional mean of exploration. When applied from generation to generation, this evolutionary strategy makes it possible to get closer and closer to the global optimum of a problem.

These general principles actually leave room for a variety of interpretations regarding the way a genetic algorithm should be implemented. The differences appear in the details when implementing the different steps of the algorithm. The coding of parameters, the definition of an effective fitness to work with when the objective function has several components and the strategy to use for the selection are a few examples. Every developer of a genetic algorithm will finally implement his own tricks to help the genetic algorithm converge more efficiently to the global optimum. For a given implementation of a genetic algorithm, one must take decisions regarding the size of the population, the rate of crossover and the rate of mutation. This is essentially done from experience.

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We present in this article a genetic algorithm we developed for the optimization of light-emitting diodes and solar thermal collectors. The genetic algorithm is presented with details in Sec. II. Sec. III presents the application of the GA to the optimization of a GaN light-emitting diode. Sec. IV presents the optimization of a solar thermal collector using a multi-objective version of the GA. We finally conclude this work in Sec. V.

2. DESCRIPTION OF THE GENETIC ALGORITHM

Let $f = f(\vec{x})$ be an objective function of *n* physical parameters x_i , where $x_i \in [x_i^{\min}, x_i^{\max}]$ with a specified granularity of Δx_i in the representation of each parameter. A solution in the mathematical sense will consist of a given set of physical parameters. We want to find, amongst this whole set of possibilities for the parameters x_i the values that maximize globally the objective function *f*.

Each parameter x_i is represented by a string of n_i bits (0 or 1), also called a "gene". The corresponding value of x_i is given in most applications by

$$x_i = x_i^{\min} + \left\langle gene \right\rangle_i \frac{x_i^{\max} - x_i^{\min}}{2^{n_i} - 1} \tag{1}$$

where $\langle gene \rangle_i \in [0, 2^{n_i} - 1]$ stands for the value coded by the gene *i* in Gray binary coding.¹⁰ The length n_i of each gene is chosen so that $(x_i^{\max} - x_i^{\min})/(2^{n_i} - 1) \le \Delta x_i$.

If a strict enforcement of the granularity Δx_i is required, one can use instead of Eq. (1) the expression

$$x_i = x_i^{\min} + \langle gene \rangle_i \Delta x_i \tag{2}$$

where $\langle gene \rangle_i \in [0, 2^{n_i} - 1]$ as previously. The genetic algorithm must reject in this case gene values that lead to $x_i > x_i^{\text{max}}$. The advantage of working with a strict representation of the parameters x_i is that the number of possibilities to explore is smaller. The genetic algorithm is therefore likely to converge more rapidly to the solution.

A given set of parameters $\{x_i\}_{i=1}^n$ is finally represented by the juxtaposition of the *n* genes used for the representation of each parameter. These strings of *n* genes are also called "DNA". The genetic algorithm actually works on the DNA representation of these parameters when searching for the optimal solution.

We work with a population of $n_{pop}=100$ individuals. Each individual has its own DNA. It is therefore representative of a given set of parameters. The initial population usually consists of random individuals. These individuals must be evaluated in order to determine their fitness. When the objective function *f* is a scalar function, the fitness is simply taken as the value of this function. When the objective function *f* has several components, we work with an effective fitness that depends on the different components f_j of this objective function and on the Pareto-classification of the individuals regarding these different components (see the Appendix). The evaluation of these individuals can be done in parallel on most recent computers since multi-core architectures are today the standard. This makes genetic algorithms especially suited to parallel-programming techniques.

The individuals are then sorted according to their fitness. We select $n_{pop}/2$ individuals ("the parents") by a rank-based "Roulette Wheel Selection". This is a random selection procedure in which the probability for an individual to be selected is proportional to its weight on a "wheel".¹⁰ The individual with the highest fitness receives a weight of n_{pop} , the second-best individual receives a weight of n_{pop} -1, etc. The individual with the smallest fitness receives a weight of 1. A given individual can be selected several times. This enables the best individuals to progressively dominate the population.

The parents are transferred to the next generation. In addition, they determine new individuals ("the children"). For any pair of parents, two children are obtained either (i) by a one-point crossover of the parents' DNA (probability of 90%), or (ii) by a simple replication of the parents' DNA (probability of 10%). The point at which the two parts of the parents' DNA is exchanged is chosen randomly.¹⁰ The transmission of unchanged individuals to the next generation enables the conservation of good solutions. The exploration of new solutions is achieved by the individuals obtained when crossing the parents' DNA. These individuals combine the features of individuals that passed the selection process. These

individuals will from time to time have a higher fitness than their parents, which makes the genetic algorithm progress in its search for optimal solutions.

We finally introduce random mutations on the children's DNA. Each bit of the children's DNA has a probability of 1% to be reversed. This is an essential ingredient for the exploration of parameters. When the rate of mutation is too small, the genetic algorithm may converge too quickly, without finding the global optimum. When the rate of mutation is too high, the exploration of parameters tends to be essentially random and therefore inefficient considering the number of possibilities to explore. The mutation rates to use are typically between 0.1% (mild value for easy convergence) and 5% (aggressive value). We use a value of 1% based on experience with previous problems.

These steps of selection, crossover and mutation must be repeated from generation to generation until convergence is achieved (maximum of 100 generations). By this game of natural selection, the genetic algorithm will progressively converge to the global optimum of the function f. We implemented elitism in order to make sure that the best individual is not lost when going from one generation to the next. We also replaced the bottom 10% of the population by random individuals. This incorporation of random individuals at each generation enables the introduction of seeds to the global optimum that may have been missing in the initial population. It also enables the genetic algorithm to consider useful directions in the exploration of parameters. Although this requires additional evaluations of the fitness, experience shows that convergence is actually improved when doing so. Since the evaluation of the fitness was especially time-consuming for the applications presented in this paper, we established a record with all individuals that were evaluated. This record was checked systematically by the genetic algorithm before each evaluation of the fitness in order to avoid unnecessary repetitions of these calculations.

3. OPTIMIZATION OF A LIGHT-EMITTING DIODE

The first application we consider aims at optimizing the light-extraction efficiency η of GaN light-emitting diodes (LED). This application is essentially an extension of the work presented by Bay et al. in Refs 11 and 12. It was demonstrated in this previous work that the light-extraction efficiency of existing GaN light-emitting diodes can be improved by considering a periodic texturation of the surface. This texturation consisted of the periodic repetition of structures made of photoresist with a "factory-roof" geometry.

The main wavelength λ of the GaN LED is 425 nm. The light-extraction efficiency is defined by

$$\eta = \int_{0}^{2\pi\pi/2} \int_{0}^{2\pi/2} T(\theta, \phi, \lambda) \sin\theta d\theta d\phi$$
(3)

where $T(\theta, \varphi, \lambda)$ is the transmittance of the system for a radiation of wavelength λ coming from the GaN substrate with (θ, φ) directional angles. The transmittance was calculated by using a Rigorous Coupled-Waves Analysis within the transfer-matrix methodology.¹³⁻¹⁴ The dielectric constant of GaN at the wavelength considered is 6.4.¹⁵ The dielectric constant of the current-spreading layer (nickel and gold alloy) was calculated considering ε_{Ni} =-3.7+i 8.1 and ε_{Au} =-1.6+i 6.3.¹⁶ The dielectric constant ε of the photoresist is 2.763 (manufacturer's value for photoresist AZ 9245®).¹⁷

The parameters that were considered in the work of Bay et al. are the period *P* and the height *H* of factory-roof structures made of photoresist. By scanning on *P* and *H* for values between 1 and 15 μ m with a step of 1 μ m, a maximum for the light-extraction efficiency η was found for *P*=5 μ m and *H*=6 μ m. The value of η reported in Ref. 12 is 5.7%, which corresponds to a relative increase of 55% compared to the value achieved without the photoresist (η = 3.7% for the flat GaN).

We extend this previous work by considering periodic structures with a more general shape. We also refine the exploration of parameters. The objective is to achieve higher light-extraction efficiencies by an optimal choice of parameters. The height h(x) of the structures considered for the surface texturation of GaN is given the general expression

$$h(x) = \begin{cases} H \times \left[1 - \frac{(c.P - x)^{\alpha_{left}}}{(c.P)^{\alpha_{left}}} \right] & when \quad 0 \le x \le c.P \\ H \times \left[1 - \frac{(x - c.P)^{\alpha_{right}}}{(P - c.P)^{\alpha_{right}}} \right] & when \quad c.P \le x \le P \end{cases}$$

$$(4)$$

where *P* and *H* refer as previously to the period and the height of these structures. The parameter $c \in [0,1]$ determines the position of the apex of these structures. For c=0, 0.5 and 1, the apex is respectively on the left, in the middle and on the right of the base period *P*. The coefficients α_{left} and α_{right} determine the concavity of the left and right edges. Straight edges are achieved when $\alpha_{left}=\alpha_{right}=1$. Values of α_{left} or α_{right} higher than 1 will result in concave edges that extend beyond the reference triangular shape achieved when $\alpha_{left}=\alpha_{right}=1$. Values of $\alpha_{left}=\alpha_{right}=1$. Values of $\alpha_{left}=\alpha_{right}=1$.

The "factory-roof" structures considered in the work of Bay et al.¹² correspond to c=1, $\alpha_{left}=1$ and $\alpha_{right}=1$. We extend this study by considering periodic structures with a period *P* between 1 and 15 µm (step ≤ 0.1 µm), a height *H* between 1 and 15 µm (step ≤ 0.1 µm), a relative center position *c* between 0.5 and 1 (step ≤ 0.01), and α_{left} and α_{right} coefficients between 0.2 and 5 (step ≤ 0.01). The results achieved by the genetic algorithm are summarized in Table 1.

Table 1. Parameters relevant to our model of surface texturation for a GaN LED and resulting light-extraction efficiencies. The four lines correspond to different optimizations of these parameters (the parameters optimized in each study are underlined).

P (μm)	Η (μm)	с	α_{left}	α_{right}	3	η	Source
<u>5</u>	<u>6</u>	1	1	1	2.763	5.7%	Ref. 12
<u>6.98</u>	4.97	0.508	<u>1.074</u>	1.055	2.763	7.1%	GA
<u>3.20</u>	2.13	1	1	1	6.325	7.3%	GA
<u>3.42</u>	2.63	0.603	1.205	<u>0.933</u>	<u>6.340</u>	11.0%	GA

The results presented in Table 1 show that it is possible using the genetic algorithm to obtain parameters that increase substantially the light-extraction efficiency η of GaN light-emitting diodes. The solution found by the GA when considering *P*, *H*, *c*, α_{left} and α_{right} as adjustable parameters enables a light-extraction efficiency η of 7.1%. This represents a relative increase of 92% compared to the η value of 3.7% achieved for a flat GaN. These results were achieved by giving the photoresist a dielectric constant ε of 2.763 (manufacturer's value for photoresist AZ 9245®).¹⁷ We can extend this study and consider the dielectric constant ε as an additional adjustable parameter. This should guide future experimental work by suggesting materials to use for the surface texturation. We considered for this study ε values between 1.2 and 6.35 (step \leq 0.01). The results achieved when considering *P*, *H* and ε as adjustable parameters are presented in the third line of Table 1. We achieve in this case a light-extraction efficiency of 7.3% (relative increase of 97% compared to the flat GaN). By considering finally *P*, *H*, *c*, α_{left} , α_{right} and ε as adjustable parameters, we achieved a light-extraction efficiency of 11.0% (fourth line of Table 1). This corresponds to a relative increase of 197% compared to the flat GaN. The structure associated with this last result is represented in Fig. 1. The solutions found by the GA, when ε is considered as an adjustable parameter, suggest that the material used for the surface texturation should have essentially the same dielectric constant as the GaN. It seems also that the optimal shapes are essentially symmetric with respect to the center of the period.

When searching for optimal values of *P*, *H*, *c*, α_{left} , α_{right} and ε , the number of bits required for the representation of these six parameters was 49 (we used the parameter representation given in Eq. 1 as a strict enforcement of the parameter granularity was not necessary). This corresponds to the length of a DNA. The number of possibilities to explore for the six parameters considered in this optimization was therefore 2^{49} = 562,949,953,421,312. The genetic algorithm managed to find the optimum given in the fourth line of Table 1 after only 1687 evaluations of the fitness.

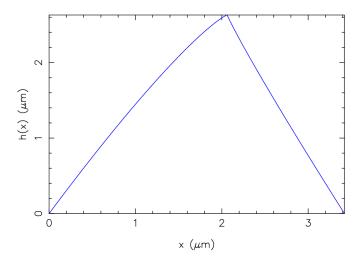


Figure 1. Representation of the structure achieved when searching for optimal values of *P*, *H*, *c*, α_{left} , α_{right} and ε with the objective of maximizing the light-extraction efficiency of GaN light-emitting diodes. The parameters associated with this representation are given in the fourth line of Table 1. The light-extraction efficiency achieved with this structure is 11.0%.

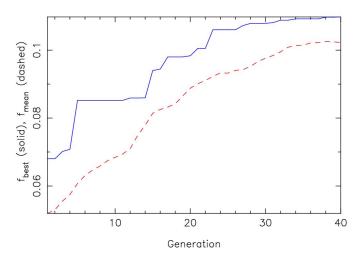


Figure 2. Best fitness (solid) and mean fitness (dashed) in the population when searching for optimal values of *P*, *H*, *c*, α_{left} , α_{right} and ε with the objective of maximizing the light-extraction efficiency of GaN light-emitting diodes.

4. OPTIMIZATION OF A SOLAR THERMAL COLLECTOR

The second application we consider deals with the optimization of a solar thermal collector. This application is essentially an extension of the work presented by Gaouyat et al. in Refs 18 and 19. In this previous work, an aluminium substrate with NiCrO_x and anti-reflection (AR) coatings was studied with the objective of developing high-performance solar thermal collectors. The NiCrO_x ceramic-metal composite (cermet) was chosen because of its high durability and attractive absorption/emission selectivity.²⁰ The applicability of this material to the development of solar thermal collectors was presented with details in Ref. 19.

In order for a solar thermal collector to be efficient, one must maximize the solar absorption α , while minimizing the thermal emissivity ε in the infrared.¹⁸⁻¹⁹ α represents the fraction of the solar spectrum that is effectively absorbed by the system. ε represents the fraction of the spectrum of a blackbody heated at 373 K that will escape the system (equivalent of thermal losses). These quantities are defined by

$$\alpha = \int_{0}^{\infty} [1 - R(\lambda)] B_{s}(\lambda) d\lambda / \int_{0}^{\infty} B_{s}(\lambda) d\lambda$$
(5)

and

$$\mathcal{E} = \int_{0}^{\infty} [1 - R(\lambda)] B_a(\lambda) d\lambda / \int_{0}^{\infty} B_a(\lambda) d\lambda$$
(6)

where $B_s(\lambda)$ is the solar irradiance spectrum (Air Mass 1.5), $B_a(\lambda)$ is the irradiance spectrum of a blackbody heated at 373 K and $R(\lambda)$ is the reflectance of the system for a radiation of wavelength λ having a normal incidence.

Values of α =91.2% and ϵ =1.5% were achieved in previous work by considering a bi-layer stack of NiCrO_x/AR deposited on a flat Al substrate.¹⁹ We seek at improving these results by keeping the same Al/NiCrO_x/AR configuration. The Al substrate will be shaped like a "waffle" (see Fig. 3). This idea was inspired by the work of Shimizu on structured W substrates for high-temperature solar absorbers.²¹ We use finally SnO₂ as material for the anti-reflection coating. The geometrical parameters that characterize the Al substrate are hence the period *P*, the height *H* of the Al, the ratio *f* between the width of the holes on the front side of the Al and the period, and finally the ratio *r* between the width of the holes on the back side of the Al and that on the front side. Conformal coatings of NiCrO_x (thickness *t*₁) and SnO₂ (thickness *t*₂) are then added to this waffle-shaped Al structure.

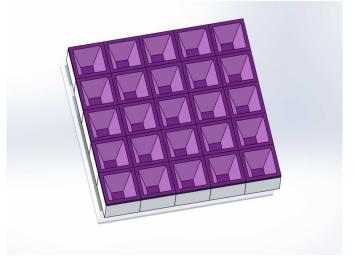


Figure 3. Waffle-shaped Al substrate with conformal coatings of $NiCrO_x$ and SnO_2 . This structure is considered for the development of high-performance solar thermal collectors.

The optical properties of this waffle-shaped Al/NiCrO_x/SnO₂ system can be simulated by using again a Rigorous Coupled-Waves Analysis within the transfer-matrix methodology for the calculation of $R(\lambda)$.¹³⁻¹⁴ The optical properties of the different materials were taken from the literature and UV-visible and IR ellipsometric measurements.^{18,22-23} The parameters considered for this optimization problem are *P*, *H*, *f*, *r*, *t*₁ and *t*₂. There are two objective functions to maximize: $f_1=\alpha$ and $f_2=1-\varepsilon$. We must therefore use a multi-objective genetic algorithm.

The general idea of multi-objective genetic algorithms follows the description of Sec. II. We work in this case with an effective fitness that depends on the two components f_1 and f_2 of the objective function and on the *Pareto-classification* of the population with respect to these two components. The definition of this effective fitness is given with details in the Appendix. The multi-objective genetic algorithm seeks in this case at establishing a set of *Pareto-optimal* solutions. These solutions provide (f_1, f_2) values with a distinct advantage compared to the rest of the population. Amongst this set of Pareto-optimal solutions, individuals that are better for f_1 will be weaker for f_2 (but no individual in the whole population is better for both f_1 and f_2). Making finally a choice amongst this set of solutions depends on how we value the two components f_1 and f_2 of the objective function and on their practicability for an experimental device. We implemented elitism and kept records for solutions that were better for either f_1, f_2 or f_1+f_2 (solutions that maximize f_1+f_2 are generally those of interest for a solar collector).

For the optimization of the solar collector, we considered *P* values between 500 and 1500 nm (step of 5 nm) and *H* values between 500 and 2500 nm (step of 5 nm). These boundaries enable *P* and *H* to keep in the same range as the absorbed wavelengths. We take *f* values between 0.5 and 0.99 (step of 0.01) and *r* values between 0 and 0.99 (step of 0.01) in order to explore the full range of pyramidal shapes. Finally t_1 and t_2 are chosen between 50 nm and 100 nm (step of 5 nm) to be representative of layer thicknesses obtained by physical vapor deposition (PVD). The representation of these parameters relied on Eq. 2 in order for *H*, t_1 and t_2 to be always multiples of the same unit (5 nm). It was indeed easier in this case to achieve good spatial discretization of the system. The number of bits required for the DNA representation of these parameters was 38 and the number of possibilities to explore was 48,763,605,000. The number of evaluations of the fitness was however as small as 2377 for the results presented here.

Solutions providing good values for f_1 , f_2 or f_1+f_2 were quickly established by the GA so that a representation of the number of Pareto-optimal solutions is actually more illustrative for the progress achieved by the algorithm. Fig. 4 shows that the genetic algorithm progressively builds up an ensemble of Pareto-optimal solutions for the realization of a solar thermal collector. The solution that provides the maximal value of f_1+f_2 is given in the first line of Table 2. The next three lines provide selected Pareto-optimal solutions established by the GA.

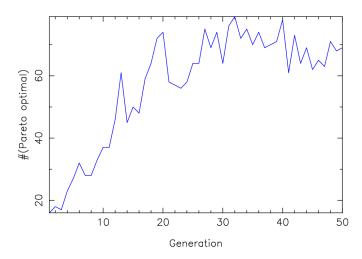


Figure 4. Number of Pareto-optimal solutions when searching for *P*, *H*, *f*, *r*, t_1 and t_2 with the objective of optimizing the parameters α and ε of a solar thermal collector.

Table 2. Parameters relevant to the optimization of the parameters α and ε of a solar thermal collector. The first line corresponds to the solution that maximizes f_1+f_2 , where $f_1 = \alpha$ and $f_2=1-\varepsilon$. The next three lines correspond to selected Pareto-optimal solutions established by the GA.

P (nm)	H (nm)	f	r	t ₁ (nm)	t ₂ (nm)	α	3	
1345	1960	0.96	0.45	50	50	97.8%	4.8%	f ₁ +f ₂ max
1435	1975	0.99	0.31	55	50	98.4%	5.8%	P-optimal
795	1590	0.90	0.28	50	50	96.1%	4.1%	P-optimal
560	545	0.95	0.28	50	50	95.2%	3.7%	P-optimal

The results presented in Table 2 compare very well with the values of α =91.2% and ϵ =1.5% achieved in previous work with a flat Al/NiCrO_x/AR configuration¹⁹ and with the record values of α =97% and ϵ =5% obtained on a 3-layers stack.²³ The three Pareto-optimal solutions given in Table 2 illustrate the fact that solutions with better α values have less attractive ϵ values. These solutions have t_1 and t_2 values around 50 nm. The choice of a particular solution for the

realization of a solar thermal collector will depend at this point on how we want to compromise between α and ε and on other practical considerations.

5. CONCLUSION

These applications prove that genetic algorithms constitute a smart approach to global optimization problems. Genetic algorithms involve indeed a collective exploration of the parameter space. This gives the algorithm the capacity to escape local optima. The algorithm is also more robust against the possible failure of an individual to evaluate the fitness and it can easily account for constrains in the parameter space. The population contributes in this exploration of parameters to a reservoir of information on the fitness. This database may be used to guide the exploration through additional heuristics. Genetic algorithms are finally especially suited to parallel programming techniques. High efficiency on super-calculators was indeed achieved by using a multi-agent programming model in order to parallelize the evaluation of the fitness. The applications presented in this work aimed at optimizing parameters that influence the efficiency of GaN light-emitting diodes and solar thermal collectors. The solutions found by the GA turned out to improve the efficiencies achieved in previous work and to be competitive with record values found in the literature. The multi-objective version of the genetic algorithm actually provides a whole set of solutions with distinct advantages. Making a choice amongst this set of solutions depends on how we value the different components of objective function and on practical considerations. Addressing these optimization problems by scanning on the different parameters considered would have been intractable because the number of possibilities to consider grows exponentially with the number of parameters (each evaluation of the fitness required up to 50 hours of CPU time for the optimization of the LED and up to 30 hours for the optimization of the solar collector). The genetic algorithm could however address these optimization problems by evaluating in parallel only a reduced number of possibilities. These results prove that genetic algorithms are a great value for addressing complex problems in physics.

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APPENDIX: EFFECTIVE FITNESS FOR A MULTI-OBJECTIVE GENETIC ALGORITHM

We define here the effective fitness that was used by the multi-objective genetic algorithm in Sec. IV. This effective fitness is used to establish a classification of the population. This is indeed required in the selection step of the algorithm. The effective fitness presented here is that used by Nicolay in previous work.²⁴ The idea is due originally to Deb.²⁵

Let us consider a population of n_{pop} individuals. We refer by *n* to the number of parameters x_i and by f_j to the different components of the objective function.

A solution \vec{x}_1 is <u>dominated</u> by the solution \vec{x}_2 if $f_j(\vec{x}_2) \ge f_j(\vec{x}_1) \forall j$ and $\exists j : f_j(\vec{x}_2) > f_j(\vec{x}_1)$.

<u>Pareto-optimal</u> solutions are solutions that are not dominated. These solutions will receive a <u>rank</u> of 1. Solutions will receive a rank of 2 if they are not dominated when discarding solutions of rank 1. Solutions of rank 3 are solutions that are not dominated if we discard solutions of rank 1 and 2. We can proceed in this way and attribute a rank to every individual in the population.

The effective fitness will be higher for individuals that have lower ranks. The genetic algorithm will tend in this way to develop solutions that are Pareto-optimal instead of solutions that improve a specific combination of the components f_j of the objective function. We seek also at establishing a set of Pareto-optimal solutions that presents a good dispersion. This prevents indeed early convergence of the GA to a given individual. We proceed therefore in the following way to define the effective fitness.

All individuals of rank 1 receive an effective fitness of n_{pop} . We then define a sharing function in order to reduce, amongst individuals of the same rank, the effective fitness of individuals that are too close. For individuals of the same rank, we define a <u>distance matrix</u> whose components d_{kl} are defined by

$$d_{k,l} = \sqrt{\sum_{i=1}^{n} \left(\frac{x_i[k] - x_i[l]}{x_i^{\max} - x_i^{\min}}\right)^2}$$
(7)

where $x_i[k]$ refers to the parameter x_i of an individual k, $x_i^{\max} = \max_{k \in [1, n_{pop}]} x_i[k]$ and $x_i^{\min} = \min_{k \in [1, n_{pop}]} x_i[k]$.

The <u>sharing function</u> between two individuals is then defined by $S_{k,l} = 1 - (d_{k,l} / \sigma_{share})^2$ if $d_{k,l} \le \sigma_{share}$ and 0 otherwise. Following Ref. 24-25, we take $\sigma_{share} = 0.5 / \sqrt[n]{10}$. We then define the <u>niche count</u> of a given individual by $m_k = \sum_l S_{k,l}$ where the sum is restricted to individuals of the same rank. The effective fitness of each individual is then

divided by its niche count. We penalize in this way individuals that are too close to other individuals within the same rank.

The effective fitness of all individuals of rank 2 is then initialized with a value of $0.99 \times f_{effect,min}$ [rank 1], where $f_{effect,min}$ [rank 1] refers to the minimal value of the effective fitness for the individuals of rank 1. We proceed then by computing the distance matrix $d_{k,l}$, the sharing function $S_{k,l}$ and finally the niche count m_k for all individuals of rank 2. The effective fitness of these individuals is then divided by their niche count.

We continue in this way until all individuals in the population have been attributed an effective fitness. Other definitions are possible for this effective fitness. They may be considered in future work.

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