

# 3D REGULARIZED SPEED-MAP RECONSTRUCTION IN ULTRASOUND TRANSMISSION TOMOGRAPHY



<sup>1</sup>Brno University of Technology, Czech Republic

Radovan Jiřík<sup>1</sup>, Igor Peterlík<sup>1</sup>, Jiří Jan<sup>1</sup>, Nicole Ruiter<sup>2</sup>, Michael Zapf<sup>2</sup>

<sup>2</sup>Forschungszentrum Karlsruhe, Germany

**Aim**

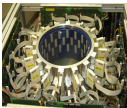
- for breast cancer diagnostics
- sound-speed closely related to the pathological tissue state
- stand-alone imaging application or for correction of reflectivity imaging algorithm

**Challenge**

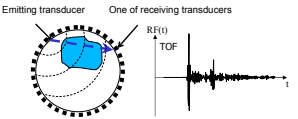
- Classical approach
  - 2D ring of transducers
  - large (high) transducers – high SNR
  - dense distribution of transducers
  - only 2D information
  - filtered backprojection (similarly to CT)
- Presented approach
  - 3D distribution of transducers
  - small transducers – low SNR
  - sparse distribution of transducers
  - complete 3D information at once
  - regularized algebraic reconstruction

**Data acquisition**

- tank filled with water
- transducers on surface
- each time one transducer in the emitter mode, all other transducers record the received RF signals
- all combinations of sending and receiving elements
- unfocused wave
- 6 motor positions



**Algebraic sound-speed reconstruction**



Contributions of voxels on the path:  $TOF = \sum_i T_i$      $T_i = d_i \cdot \frac{1}{c_i}$      $TOF = \sum_i d_i \cdot s_i$

TOF    time-of-flight – time span between emitting and receiving of the first pulse  
 $T_i$     time-of-flight through i-th voxel  
 $d_i$     path length through i-th voxel  
 $c_i$     sound-speed in i-th voxel  
 $s_i$     time-of-flight per unit distance in i-th voxel (unknowns)

Path 1:  $TOF_1 = \sum_{j=1}^N d_{1,j} \cdot s_j$

Path 2:  $TOF_2 = \sum_{j=1}^N d_{2,j} \cdot s_j$

...

Path K:  $TOF_K = \sum_{j=1}^N d_{K,j} \cdot s_j$

... overdetermined system of linear equations:  $Rf = p$

**Regularization**

Why:

- errors in transmission pulse detection, hence also in TOF (wave front aberration, noise)
- some equations can be left out as outliers (wave front aberration, noise) => smaller degree of equation-set overdetermination
- sparse transducer distribution (technical limitations)

Solution formulation:

- incorporation of the spatial context in the reconstruction
- edge preserving regularization:

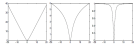
$$f = \arg \min_f \|J_1(f) + \lambda^2 J_2(f)\|$$

$$J_1(f) = \frac{1}{2} \|p - Rf\|^2$$

$$J_2(f) = \sum_k \phi(|D_x f|_k / \delta) + \sum_k \phi(|D_y f|_k / \delta) + \sum_k \phi(|D_z f|_k / \delta)$$

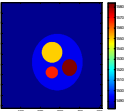
$J_1(f)$     least-squares term  
 $J_2(f)$     regularization term  
 $D_x f, D_y f, D_z f$     differences between neighboring voxels  
 $\delta, \lambda$     regularization parameters  
 $\phi$     potential (penalization) function:

Possible potential functions:

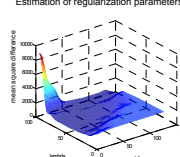


**Results on synthetic data**

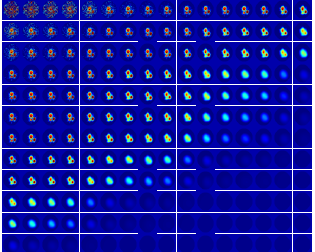
Synthetic phantom:



Estimation of regularization parameters:

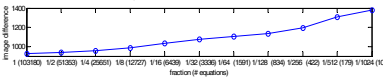
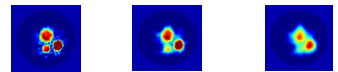


Corresponding reconstructed images:



**Results on synthetic data**

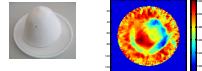
Robustness with respect to degree of equation-set overdetermination:

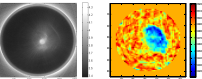
all equations    1/16 of equations    1/256 of equations

**Results on recorded phantom data**

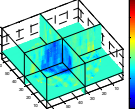
breast phantom:    backprojection FDK alg. result:



reference reflectivity img.:    regularized alg. result:



3D reconstruction example:



**Conclusions**

- algebraic reconstruction for sparse distribution of transducers is possible with regularization
- regularization parameters – compromise between edge preserving and spatial consistency
- optimal regularization parameters found for simulation (with SNR same as in reality – 11dB)
- optimal regularization parameters – valley, not steep
- image reconstruction still reasonable with a low fraction of complete equation set => wide space for selection "good" equations (RF signals)
- phantom measurements gave clear breast delineation
- regularized reconstruction provided better breast delineation than FDK filtered backprojection
- need for better evaluation
  - need for measurements on sound-speed phantom
  - known ground-truth sound-speed values
  - need for more realistic simulation used for system generation
- part of volume processed so far due to memory limitations
- need for distributed equation solver

**Acknowledgement**

We are grateful for support from

- Czech Ministry of Education, Youth and Sports (Research Center DAR, proj. no. 1M679855601)
- Joint programs of the German Academic Exchange Service and Czech Academy of Science,
- MetaCentrum for offering the computational resources