

# Forschungszentrum Karlsruhe in der Helmholtz-Gemeinschaft

## Tunneling transport through molecules and coupled quantum dots

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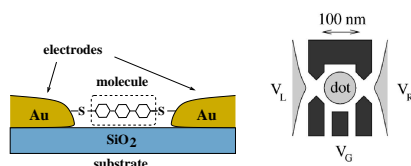
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### I. Motivation

- Quantum dots and molecules as potential building blocks for future nanoelectronic devices
- Problem: **coupling** of molecule to electrodes **unknown** and not easily controllable in nanoscopic devices.
- Combined measurement of **current and shot noise** provides additional information about couplings, interaction, etc.

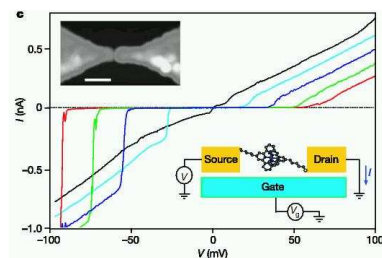
### II. Physical Realization



l.h.s.: deposition of molecule between two fixed electrodes (Reed et al., Science **278**, 252 (1997))

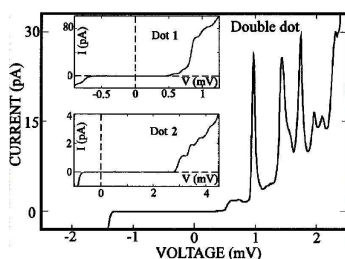
r.h.s.: schematic picture of a lateral quantum dot structure

### III. Experiments



J. Park, A.N. Pasupathy, et al., Nature **417**, 722 (2002)

- electrodes probed via electron beam lithography and electromigration
- molecule is a Co ion bonded to ligands → coupling to the electrodes can be controlled

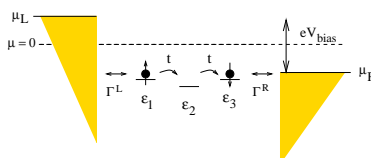


van der Wiel et al., Rev. Mod. Phys. **75**, 1 (2003)

- lateral coupled quantum dots ("artificial molecules")
- single-electron phenomena such as Coulomb blockade observed

### IV. Model

Sketch of couplings for three coupled quantum dots



- $\hat{H} = \hat{H}_L + \hat{H}_R + \hat{H}_{\text{dots}} + \hat{H}_{T,L} + \hat{H}_{T,R}$  with:

$$\hat{H}_r = \sum_{k\sigma} \epsilon_{k\sigma} a_{k\sigma}^\dagger a_{k\sigma},$$

$$\hat{H}_{T,r} = \sum_{i\sigma} (t_i^r a_{i\sigma}^\dagger c_{i\sigma} + h.c.),$$

$$\hat{H}_{\text{dots}} = \sum_{i\sigma} \epsilon_i n_{i\sigma} - t \sum_{\langle ij \rangle > \sigma} (c_{i\sigma}^\dagger c_{j\sigma} + h.c.)$$

$$+ U \sum_i n_{i\uparrow} n_{i\downarrow} + U_{mn} \sum_{\langle ij \rangle > \sigma\sigma'} n_{i\sigma} n_{j\sigma'}$$

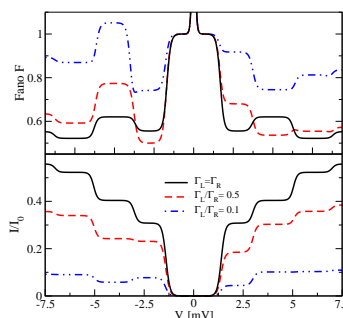
- $\hat{H}_L, \hat{H}_R$ : left and right electrode with non-interacting electrons ( $r = L, R$ ).
- $\hat{H}_{\text{dots}}$ : molecule or dot term with  $i$  (spin-dependent) molecular sites ( $n_{i\sigma} = c_{i\sigma}^\dagger c_{i\sigma}$ ).
- $\hat{H}_{T,L}, \hat{H}_{T,R}$ : tunneling between the dot system and electrodes.
- Energies**: level energies ( $\epsilon_i$ ), intra-dot ( $U$ ) and inter-dot ( $U_{mn}$ ) Coulomb repulsion, kinetic (hopping) energy ( $t$ )
- coupling strength  $\Gamma_i^r = 2\pi |t_i^r|^2 \rho_e$  with  $t_i^r$  being the tunneling amplitude and  $\rho_e$  is DOS

### V. Numerical Results

#### A. Two coupled quantum dots

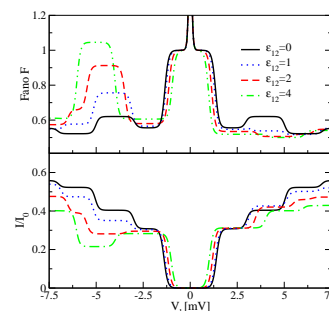
Fano factor  $F = \frac{S}{2I}$  for symmetric bias voltage and  $\epsilon_1 = \epsilon_2 = -5.5, t = 2, U = 10, U_{mn} = 5, k_B T = 0.05$  (all units in meV). Step positions determined by energy parameters and plateau heights by couplings  $\Gamma_L, \Gamma_R$ . The total coupling scale is set to  $\Gamma_R = 0.05 k_B T$ .

Asymmetric coupling  $\Gamma_L \neq \Gamma_R$



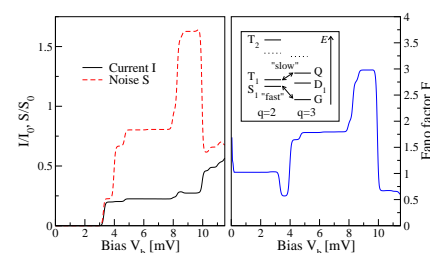
For strong asymmetries **super-Poissonian** Noise ( $F > 1$ ) and **negative differential conductance** (NDC) develop at the same bias (energy) positions

Strong **level detuning**, in particular  $\epsilon_{12} = \epsilon_1 - \epsilon_2 > t$ , leads to **super-Poissonian** noise and **NDC**



#### B. Three coupled quantum dots

Strong **non-local Coulomb interactions**  $U_{mn} > t$  Current and Noise for symmetric coupling  $\Gamma_R = \Gamma_L$  with parameters  $\epsilon_i = -10, t = 2, U = 10, U_{mn} = 5, k_B T = 0.025$  (units in meV) and more complex many body wavefunctions (Singlets S, Doublets D, Triplets T, Quadruplets Q)

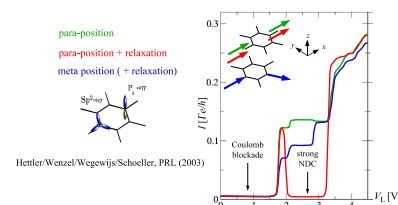


**Super-Poissonian** noise and Fano factors without simultaneous suppression of the current

→ competition of "fast" and "slow" transport channels leads to strongly enhanced noise  
→ effect depends on the ratio  $\frac{U_{mn}}{t}$  and is entirely due to **internal electronic level structure**

#### C. Towards a description of Molecules

Six site model for aromatic molecules like **benzene** rings including **relaxation processes** of photons



Transport highly sensitive to different coupling positions (para and meta position)

In the case of paraposition **strong NDC** is observed  
→ occupation of a **blocking state** of the molecule

#### References:

Thielmann et al., Phys. Rev. Lett. **95**, 146806 (2005), Aghassi et al., Phys. Rev. B **73**, 195323 (2006), Aghassi et al. cond-mat/0505345 (to be published in Appl. Phys. Lett.)