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[Extended Abstract]

## Stability investigations of an elastic rotor supported by actively deformed journal bearings considering the associated spectral system

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### Introduction

Due to the non-linear fluid-solid interaction within journal bearings instability phenomena (often referred to as 'oil-whirl' and/or 'oil-whip') can be observed at higher revolution speeds, which can lead to unwanted oscillations of the corresponding rotor-dynamic system. To improve this behaviour, various methods which are based on the idea of non-circular bearing geometries have been proposed in literature. E.g. in [1] first approaches of a simple two-lobe bearing with an actively controlled change in geometry are investigated in order to suppress the above mentioned instability phenomena. In the present work a more elaborated model of a journal bearing with modifiable geometry is developed. Afterwards, this bearing is implemented in an elastic Jeffcott rotor and the associated spectral system is derived and analysed.

### 1. Modelling of the Jeffcott rotor in actively deformed journal bearings

#### 1.1 Geometry of the deformed bearing

As depicted in figure 1 the initially circular bearing of inner radius  $R_0$  is deformed by two oscillating vertical forces  $F(\tau) = \hat{F}(1 - \delta_F \cos((\Omega/\omega)\tau))$  with given dimensionless time  $\tau = \omega t$ . The bearing is modelled as thin, circular beam with middle radius  $R$  and Young's modulus  $E$ . The rectangular cross-section is characterized by its width  $B \ll R$  and its height  $A \ll R$ . It is assumed that the deformation is not influenced by the fluid pressure at all and that inertia terms can be neglected. Using the classical bending theory for curved beams (cf. [2]), the radial deflection  $w(\varphi, \tau)$  from the undeformed state can be calculated.

A normalisation on the initial bearing clearance  $C = R_0 - R_W = (R - A/2) - R_W$  leads to:

$$W(\varphi, \tau) = \frac{w(\varphi, \tau)}{C} = \frac{3R^3}{CBA^3} \frac{F(\tau)}{E} \begin{cases} \frac{4}{\pi} - \sin \varphi + (\varphi - \frac{1}{2}\pi) \cos \varphi & 0 \leq \varphi < \pi \\ \frac{4}{\pi} + \sin \varphi + (\frac{3}{2}\pi - \varphi) \cos \varphi & \pi \leq \varphi \leq 2\pi \end{cases} \quad (1)$$

#### 1.2 Pressure distribution

With the deflection from equation (1) and the depicted kinematic relations in figure 1 the non-dimensional pressure  $\Pi(\varphi, \bar{z})$  can be modelled according to the non-dimensional Reynolds equation:

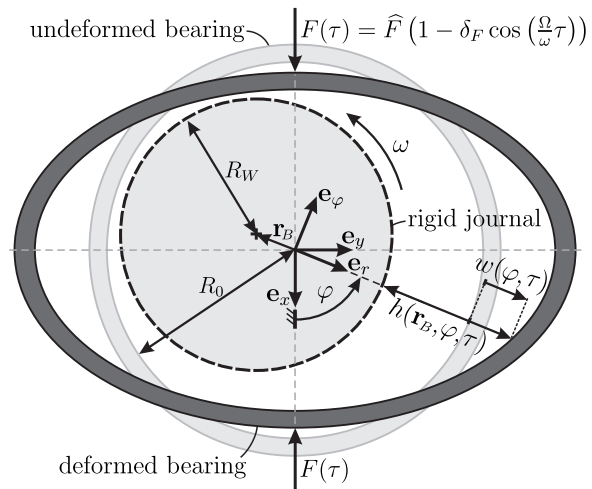


Figure 1. deformed journal bearing

$$\frac{\partial}{\partial \varphi} \left( \frac{\partial \Pi}{\partial \varphi} H^3 \right) + \gamma^2 \frac{\partial}{\partial \bar{z}} \left( \frac{\partial \Pi}{\partial \bar{z}} H^3 \right) = 6 \frac{\partial H}{\partial \varphi} + 12 \frac{\partial H}{\partial \tau} \quad \text{with} \quad H = \frac{h}{C} = 1 + W - X_B \cos \varphi - Y_B \sin \varphi, \quad (2)$$

with the boundary conditions  $\Pi(\bar{z} = \pm 1) = 0$ ,  $\Pi(\varphi = 0) = \Pi(\varphi = 2\pi)$  and  $\frac{\partial \Pi}{\partial \varphi}|_{\varphi=0} = \frac{\partial \Pi}{\partial \varphi}|_{\varphi=2\pi}$ . The normalised journal coordinates are given by  $r_{B/C} = X_B \mathbf{e}_x + Y_B \mathbf{e}_y$ . Assuming a rather short bearing ( $2R_0/B = \gamma \gg 1$ ) the Galerkin approach  $\Pi = (1 - \bar{z}^2)g(\varphi)$  is used to reduce the Reynolds equation (2) to a one-dimensional problem in  $\varphi \in [0, 2\pi]$ , which is solved by using a finite-difference scheme.

### 1.3 Bearing forces

With the semi-discrete pressure values  $\Pi_i(\bar{z}) = (1 - \bar{z}^2)g(\varphi_i)$  for  $i = 1 \dots N$  the non-dimensional bearing forces  $f_x$  and  $f_y$  are calculated. After integrating along the axial coordinate  $\bar{z}$  the circumferential integration in  $\varphi$  is performed by means of the trapezoidal rule whereby negative pressure values are neglected.

### 1.4 Equations of motion

Having derived the bearing forces, the equations of motion of the Jeffcott rotor (cf. [3]) are given by:

$$\begin{aligned} \bar{\omega}^2 X_R'' + \bar{d}_a \bar{\omega} X_R' + \frac{X_R - X_B}{\Gamma} = f, \quad \eta \bar{\omega}^2 X_B'' + \frac{X_B - X_R}{\Gamma} - \sigma \bar{\omega} f_x &= 0, \\ \bar{\omega}^2 Y_R'' + \bar{d}_a \bar{\omega} Y_R' + \frac{Y_R - Y_B}{\Gamma} = 0, \quad \eta \bar{\omega}^2 Y_B'' + \frac{Y_B - Y_R}{\Gamma} - \sigma \bar{\omega} f_y &= 0, \end{aligned} \quad (3)$$

with the dimensionless parameters  $\bar{d}_a$  for damping,  $\eta$  for the masses allocated at the bearing seats,  $\bar{\omega}$  for the revolution speed,  $\Gamma$  for the shaft compliance,  $\sigma$  for the bearing characteristic and  $f$  for a vertically acting external load.  $X_R$  and  $Y_R$  thereby describe the centre coordinates of the rotor and  $(\cdot)' = d/d\tau(\cdot)$  represents the derivative with respect to the non-dimensional time  $\tau$ .

### 1.5 Derivation of the spectral system

As the time-varying bearing deformation (1) enters the equations in (3) as a parameter, the system is exposed to parametric- and self-excitation, which can lead to quasi-periodic behaviour. Therefore, the associated spectral system is derived according to the suggested method of SCHILDER [4], such that quasi-periodic trajectories can be easily described and analysed.

## 2. Simulation results

With the previously mentioned spectral system a fast analysis of the dynamic behaviour by means of solution continuation algorithms is possible even for originally quasi-periodic behaviour.

The results reveal a high potential to decrease large rotor amplitudes by selecting an appropriate time-varying deformation function (1), i.e. it is possible to shift the beginning of the above mentioned instability phenomena to even higher revolution speeds.

## References

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