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## Convergence of integrable operators affiliated to a finite von Neumann algebra

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### Abstract

© 2016, Pleiades Publishing, Ltd. In the Banach space  $L_1(M, \tau)$  of operators integrable with respect to a tracial state  $\tau$  on a von Neumann algebra  $M$ , convergence is analyzed. A notion of dispersion of operators in  $L_2(M, \tau)$  is introduced, and its main properties are established. A convergence criterion in  $L_2(M, \tau)$  in terms of the dispersion is proposed. It is shown that the following conditions for  $X \in L_1(M, \tau)$  are equivalent: (i)  $\tau(X) = 0$ , and (ii)  $\|I + zX\| \geq 1$  for all  $z \in \mathbb{C}$ . A.R. Padmanabhan's result (1979) on a property of the norm of the space  $L_1(M, \tau)$  is complemented. The convergence in  $L_2(M, \tau)$  of the imaginary components of some bounded sequences of operators from  $M$  is established. Corollaries on the convergence of dispersions are obtained.

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