

## Nondeterministic unitary OBDDs

Gainutdinova A., Yakarylmaz A.

Kazan Federal University, 420008, Kremlevskaya 18, Kazan, Russia

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### Abstract

© Springer International Publishing AG 2017. We investigate the width complexity of nondeterministic unitary OBDDs (NUOBDDs). Firstly, we present a generic lower bound on their widths based on the size of strong 1-fooling sets. Then, we present classically "cheap" functions that are "expensive" for NUOBDDs and vice versa by improving the previous gap. We also present a function for which neither classical nor unitary nondeterminism does help. Moreover, based on our results, we present a width hierarchy for NUOBDDs. Lastly, we provide the bounds on the widths of NUOBDDs for the basic Boolean operations negation, union, and intersection.

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