Russian Mathematics 2015 vol.59 N7, pages 31-43

Method of penalization for the state equation for an elliptical optimal control problem

Lapin A., Zalyalov D. Kazan Federal University, 420008, Kremlevskaya 18, Kazan, Russia

Abstract

© 2015, Allerton Press, Inc. We solve by finite difference method an optimal control problem of a system governed by a linear elliptic equation with pointwise control constraints and non-local state constraints. A discrete optimal control problem is approximated by a minimization problem with penalized state equation. We derive the error estimates for the distance between the exact and regularized solutions. We also prove the rate of convergence of block Gauss-Seidel iterative solution method for the penalized problem. We present and analyze the results of the numerical experiments.

http://dx.doi.org/10.3103/S1066369X1507004X

Keywords

constraint saddle point problem, finite difference approximation, iterative methods, optimal control