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## Spectra of high n and non-low n degrees

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## Abstract

We survey known results on spectra of structures and on spectra of relations on computable structures, asking when the set of all highn degrees can be such a spectrum, and likewise for the set of non-low n degrees. We then repeat these questions specifically for linear orders and for relations on the computable dense linear order  $\mathbb{Q}$ . New results include realizations of the set of non-low n Turing degrees as the spectrum of a relation on  $\mathbb{Q}$  for all  $n \ge 1$ , and a realization of the set of all non-low n Turing degrees as the spectrum of a linear order whenever  $n \ge 2$ . The state of current knowledge is summarized in a table in the concluding section.  $\mathbb{C}$  2010 The Author. Published by Oxford University Press. All rights reserved.

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## **Keywords**

Computability, computable model theory, linear order, relation, spectrum