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# Recognition of a new permittivity function for glycerol by the use of the eigen-coordinates method

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## Abstract

Measurements of real and imaginary parts of the relative complex permittivity of glycerol were carried out in the frequency range 1 mHz–1 MHz at different temperatures between 188 and 263 K. The permittivity data have been analyzed thoroughly by a new data curve-fitting approach that involves the so-called eigen-coordinates method in conjunction with a separation procedure and the inverse permittivity formulas. A new single permittivity function, based on the so-called recap element picture for a self-similar (fractal) structure, has been recognized to describe well such data over the entire frequency range studied. The recognized dielectric function enabled us to infer an electrical equivalent-circuit network for the glycerol sample studied that involves a series combination of two recap elements, reflecting the existence of two different dielectric relaxation processes in glycerol. The temperature dependence of the relaxation times  $\tau_1(T)$  and  $\tau_2(T)$  entering into the identified permittivity function was found to obey nearly an Arrhenius behaviour with activation energies  $E_1 \approx 114$  kJ/mol and  $E_2 \approx 94$  kJ/mol. The recognized permittivity function can be justified by presuming that the processes represented by the recap elements characterized by the parameters  $(\nu_1, \tau_1, E_1)$  and  $(\nu_2, \tau_2, E_2)$  are linked to ‘donor-like’ and ‘acceptor-like’ charges formed from the infinite hydroxyl hydrogen bonds. © 2002 Elsevier Science B.V. All rights reserved.

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## 1. Introduction

In recent years, dielectric relaxation phenomena in glass-forming glycerol and similar hydrogen-bonded molecular materials received a lot of attention from both experimental and theoretical

aspects [1–9]. Most of the experimental studies show that the dielectric ac response of such glass-forming materials is hardly being explained by the ‘classical’ Debye dielectric function that gives the complex permittivity  $\varepsilon^*(\omega)$  as [10,11]. The loss-peak angular frequency  $\omega_p$  is generally temperature dependent and can be described by the Vogel–Fulcher–Tammann (VFT) formula [6,7, 11, 12]. Non-Debye ac response can classically be correlated with some distribution of relaxation times quantifiable in terms of purely empirical

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