

## PAPER

# Increase of Recognizable Label Number with Optical Passive Waveguide Circuits for Recognition of Encoded 4- and 8-Bit BPSK Labels

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**SUMMARY** Optical label processing is expected to reduce power consumption in label switching network nodes. Previously, we proposed passive waveguide circuits for the recognition of BPSK labels with a theoretically infinite contrast ratio. The recognizable label number was limited to four and eight for 4-bit and 8-bit BPSK labels, respectively. In this paper, we propose methods to increase the recognizable label number. The proposed circuits can recognize eight and sixteen labels of 4-bit BPSK codes with a contrast ratio of 4.00 and 2.78, respectively. As 8-bit BPSK codes, 64, 128, and 256 labels can be recognized with a contrast ratio of 4.00, 2.78, and 1.65, respectively. In recognition of all encoded labels, that is, 16 and 256 labels for 4-bit and 8-bit BPSK labels, a reference signal is employed to identify the sign of the optical output signals. The effect of phase deviation and loss along the optical waveguides of the devices is also discussed.

**key words:** code recognition, optical waveguide circuits, optical BPSK code

## 1. Introduction

Optical encoded labels have been employed to carry information in label-routed photonic networks [1], [2]. Optical processing for labels which are not converted to electrical signals is expected to reduce electrical power consumption in network nodes. Binary phase-shift-keying (BPSK) codes are one of the basic formats for the optical labels as well as for optical payload. Optical correlator-based systems have been investigated to recognize matched labels, which include systems consisting of fiber Bragg grating [3], taps and delay lines [2], and combination of a grating and spatial filters [4]–[6]. Multiple labels that correspond to a partial set of binary codes have also been recognized with waveguide-type circuits consisting of arrayed waveguide gratings (AWGs) [7], [8] and cascaded interferometers [9], [10].

We have proposed a passive waveguide circuit to recognize all BPSK coded labels [11], [12]. The device consists of a tree-structure connection of asymmetric X-junction couplers [13]. The number of the output ports for  $N$ -bit labels is  $2^N$ . The contrast ratio, which is expressed as the ratio of

the largest intensity at the desired output port corresponding to the incident label to the secondly largest intensity among other ports, is 2.78 and 1.65 for  $N = 4$  and 8, respectively [12]. We also proposed another recognition circuit for a partial set of the binary codes, which provides an infinite contrast ratio [14]. In this paper, we investigate the increase in the number of recognizable labels with waveguide circuits based on the latter circuit. A basic idea to increase the number of recognizable 4-bit BPSK labels was also briefly discussed in [14]. In this paper, we discuss systematically how to increase the number of available labels for 4- and 8-bit binary codes and find optimum circuit parameters. It is shown that the number of recognizable labels can be increased at the expense of decreasing the contrast ratio. However, the decrease of the contrast ratio can be suppressed by limiting employed labels to a set of classified labels. Therefore, the obtained results will give useful information to design a set of labels which meet requirement for a minimum contrast ratio at the output.

We also clarify the effect of phase deviation along waveguides and propagation loss variation between waveguides, which gives allowable fabrication error for the optical waveguide device only consisting of optical passive elements.

The remainder of this paper is organized as follows: Sect. 2 gives brief description of the basic optical waveguide circuits for the recognition of 4-bit and 8-bit labels. In Sect. 3, we discuss methods to increase the recognizable labels by extending the circuits for 4-bit labels. In Sect. 4, we apply similar methods to 8-bit labels. The results are discussed in comparison with tree-structure waveguide circuits [12] in Sect. 5. In Sect. 6, conclusions are presented.

## 2. Basic Waveguide Circuits for 4- and 8-Bit Label Recognition

A basic waveguide circuit for the recognition of four 4-bit BPSK labels is shown in Fig. 1 [14]. The device consists of four asymmetric X-junction couplers,  $X_i$ ,  $i = 1, \dots, 4$ , and interconnecting waveguides. The phases  $\phi_i$  and the transmission coefficients  $\beta_i$ ,  $i = 1, \dots, 4$ , mean the phase deviations due to model fabrication error and the attenuations due to propagation loss or scattering in the waveguides, respectively. Note that, in ideal devices, these phase deviations

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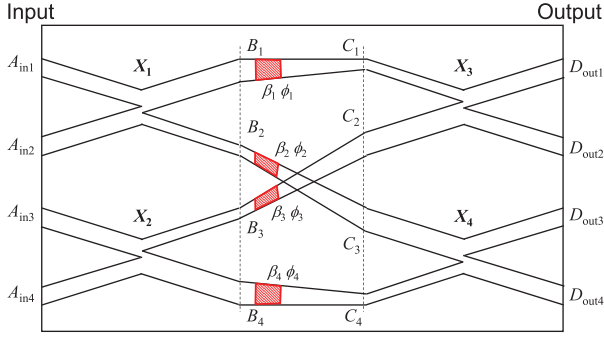
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**Fig. 1** A basic optical waveguide circuit for the recognition of the 4-bit BPSK labels.

$\phi_i$  are 0 and  $\beta_i$  are equal to one. An optical 4-bit label is supposed to have been converted from a serial pulse train to parallel pulses with a preprocessor. The parallel pulses are input in the input ports at the same time. We denote  $\beta_i e^{j\phi_i}$  as  $\alpha_i$ . The output optical fields  $D_{out j}$ ,  $j = 1, \dots, 4$ , are related to the input fields  $A_{in i}$ ,  $i = 1, \dots, 4$ , as [14]

$$\begin{pmatrix} D_{out1} \\ D_{out2} \\ D_{out3} \\ D_{out4} \end{pmatrix} = \frac{1}{2} \begin{pmatrix} \alpha_1 & \alpha_1 & \alpha_3 & -\alpha_3 \\ -\alpha_1 & -\alpha_1 & \alpha_3 & -\alpha_3 \\ -\alpha_2 & \alpha_2 & -\alpha_4 & -\alpha_4 \\ -\alpha_2 & \alpha_2 & \alpha_4 & \alpha_4 \end{pmatrix} \begin{pmatrix} A_{in1} \\ A_{in2} \\ A_{in3} \\ A_{in4} \end{pmatrix}. \quad (1)$$

We consider four BPSK labels  $A_i^{(1)}$ ,  $i = 1, \dots, 4$ , as defined by

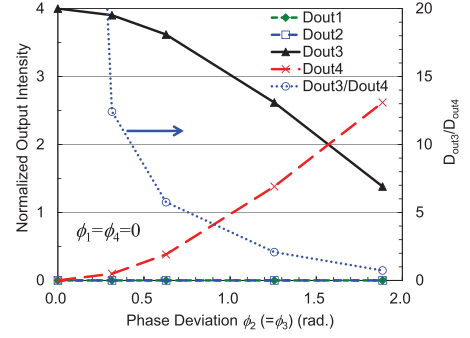
$$\begin{pmatrix} A_1^{(1)} & A_2^{(1)} & A_3^{(1)} & A_4^{(1)} \end{pmatrix} = \begin{pmatrix} A_1 & A_2 & A_3 & A_4 \end{pmatrix} = \begin{pmatrix} 1 & -1 & 1 & 1 \\ -1 & 1 & 1 & 1 \\ 1 & 1 & 1 & -1 \\ 1 & 1 & -1 & 1 \end{pmatrix}, \quad (2)$$

where  $A_i$  is a column vector of optical field and the superscript (1) denotes the 4-bit labels. The output fields  $D_i^{(1)}$  for  $A_i^{(1)}$  is obtained from Eqs. (1) and (2) as

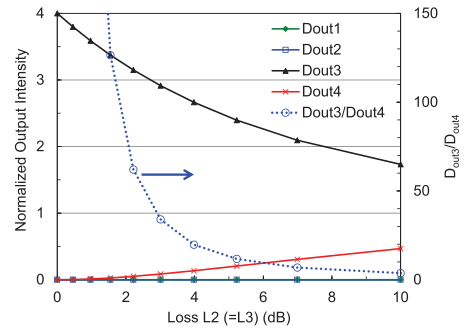
$$\begin{pmatrix} D_1^{(1)} & D_2^{(1)} & D_3^{(1)} & D_4^{(1)} \end{pmatrix} = \begin{pmatrix} 0 & 0 & \alpha_1 + \alpha_3 & \alpha_1 - \alpha_3 \\ 0 & 0 & -\alpha_1 + \alpha_3 & -\alpha_1 - \alpha_3 \\ -\alpha_2 - \alpha_4 & \alpha_2 - \alpha_4 & 0 & 0 \\ -\alpha_2 + \alpha_4 & \alpha_2 + \alpha_4 & 0 & 0 \end{pmatrix}. \quad (3)$$

Although each input label has an output with an infinite contrast ratio for the ideal case of  $\alpha_i = 1$ , the number of the recognizable labels is limited to four.

We now consider the effect of phase deviation  $\phi_i$  with  $\beta_i = 1$ . Figure 2 shows the output intensities as a function of  $\phi_2 (= \phi_3)$ , whereas  $\phi_1 = \phi_4 = 0$  is assumed. Since the asymmetric X-junction coupler discriminates a phase difference  $\pi$  between the two inputs, the outputs from  $D_{out1}$  and  $D_{out2}$  are reversed at  $\phi_2 = \phi_3 = \pi$ . The ratio of  $D_{out3}/D_{out4}$  is also plotted to evaluate the contrast ratio. It is found that the deviation at the output intensities is kept below 2.5 % of



**Fig. 2** The output intensities as a function of the phase deviation  $\phi_2 (= \phi_3)$  for the 4-bit basic module.



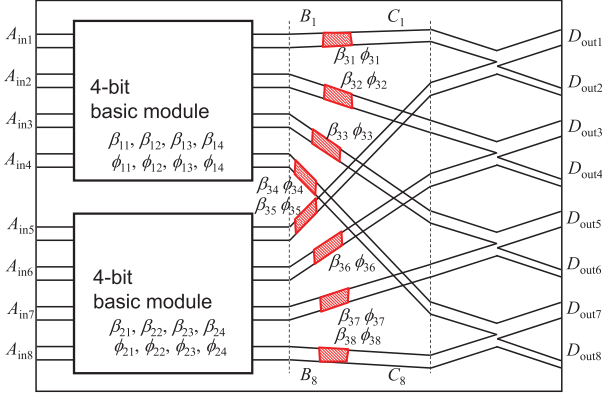
**Fig. 3** The output intensities as a function of waveguide loss  $L_2 (= L_3)$  for the 4-bit basic module, where the other losses and the phase deviation is assumed to be 0.

the maximum output when the phase deviation is less than  $0.1\pi$  rad, resulting in a contrast ratio larger than 12.4.

Next, we consider the effect of waveguide loss. Since the crossed waveguides are expected to have larger scattering loss, we evaluate the output as a function of  $L_2 (= L_3)$ , whereas  $L_1 = L_4 = 0$ . Here, we define  $L_i = -10 \log_{10} \beta_i$ . Figure 3 shows the calculated results. Loss of  $L_2 = L_3 = 2.2$  dB, which corresponds to 0.77 of  $\beta_2$  and  $\beta_3$ , induces a decrease of 21.3 % and an increase relative to  $D_{out3}$  and  $D_{out4}$ , respectively. The contrast ratio decreases from infinity to 62.0.

In addition to scattering and crosstalk at the crossed waveguides, the asymmetric X-junction coupler may induce scattering. Although the coupling performance of the asymmetric X-junction coupler does not have large dependence on the waveguide widths and the crossed angle, edge roughness of the waveguide at the junction induces scattering. Such fabrication error and roughness induce imbalance splitting, resulting in the degradation of the output contrast ratio.

The basic waveguide circuit for the 4-bit label recognition can be scaled to the 8-bit label recognition as shown in Fig. 4 [14]. The circuit consists of two 4-bit basic modules shown in Fig. 1 and four asymmetric X-junction couplers at the outputs. The transmission coefficients,  $\beta_{1i}$  and  $\beta_{2i}$ , and the phase deviations,  $\phi_{1i}$  and  $\phi_{2i}$ , correspond to  $\beta_i$  and  $\phi_i$  in the basic module of Fig. 1, respectively. The output



**Fig. 4** A basic optical waveguide circuit for the recognition of the 8-bit BPSK labels.

fields  $D_{out\ j}$ ,  $j = 1, \dots, 8$  are related to the input fields  $A_{in\ i}$ ,  $i = 1, \dots, 8$ , as

$$\begin{pmatrix} D_{out1} \\ D_{out2} \\ \vdots \\ D_{out8} \end{pmatrix} = T_8 \begin{pmatrix} A_{in1} \\ A_{in2} \\ \vdots \\ A_{in8} \end{pmatrix}, \quad (4)$$

where

$$T_8 = \frac{1}{2\sqrt{2}} \begin{pmatrix} \alpha_{31}\alpha_{11} & \alpha_{31}\alpha_{11} & \alpha_{31}\alpha_{13} & -\alpha_{31}\alpha_{13} & & & & \\ -\alpha_{31}\alpha_{11} & -\alpha_{31}\alpha_{11} & -\alpha_{31}\alpha_{13} & \alpha_{31}\alpha_{13} & & & & \\ -\alpha_{32}\alpha_{11} & -\alpha_{32}\alpha_{11} & \alpha_{32}\alpha_{13} & -\alpha_{32}\alpha_{13} & & & & \\ \alpha_{32}\alpha_{11} & \alpha_{32}\alpha_{11} & -\alpha_{32}\alpha_{13} & \alpha_{32}\alpha_{13} & & & & \\ -\alpha_{33}\alpha_{12} & \alpha_{33}\alpha_{12} & -\alpha_{33}\alpha_{14} & -\alpha_{33}\alpha_{14} & & & & \\ \alpha_{33}\alpha_{12} & -\alpha_{33}\alpha_{12} & \alpha_{33}\alpha_{14} & \alpha_{33}\alpha_{14} & & & & \\ -\alpha_{34}\alpha_{12} & \alpha_{34}\alpha_{12} & \alpha_{34}\alpha_{14} & \alpha_{34}\alpha_{14} & & & & \\ \alpha_{34}\alpha_{12} & -\alpha_{34}\alpha_{12} & -\alpha_{34}\alpha_{14} & -\alpha_{34}\alpha_{14} & & & & \\ \alpha_{35}\alpha_{21} & \alpha_{35}\alpha_{21} & \alpha_{35}\alpha_{23} & -\alpha_{35}\alpha_{23} & & & & \\ \alpha_{35}\alpha_{21} & \alpha_{35}\alpha_{21} & \alpha_{35}\alpha_{23} & -\alpha_{35}\alpha_{23} & & & & \\ -\alpha_{36}\alpha_{21} & -\alpha_{36}\alpha_{21} & \alpha_{36}\alpha_{23} & -\alpha_{36}\alpha_{23} & & & & \\ -\alpha_{36}\alpha_{21} & -\alpha_{36}\alpha_{21} & \alpha_{36}\alpha_{23} & -\alpha_{36}\alpha_{23} & & & & \\ -\alpha_{37}\alpha_{22} & \alpha_{37}\alpha_{22} & -\alpha_{37}\alpha_{24} & -\alpha_{37}\alpha_{24} & & & & \\ -\alpha_{37}\alpha_{22} & \alpha_{37}\alpha_{22} & -\alpha_{37}\alpha_{24} & -\alpha_{37}\alpha_{24} & & & & \\ -\alpha_{38}\alpha_{22} & \alpha_{38}\alpha_{22} & \alpha_{38}\alpha_{24} & \alpha_{38}\alpha_{24} & & & & \\ -\alpha_{38}\alpha_{22} & \alpha_{38}\alpha_{22} & \alpha_{38}\alpha_{24} & \alpha_{38}\alpha_{24} & & & & \end{pmatrix}, \quad (5)$$

where  $\alpha_{ij} = \beta_{ij}e^{j\phi_{ij}}$ .

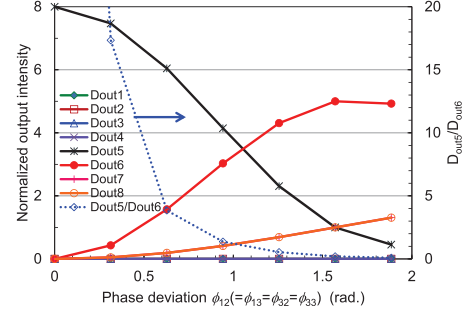
We consider eight BPSK labels  $A_i^{(2)}$ ,  $i = 1, \dots, 8$ , as defined by

$$\begin{pmatrix} A_1^{(2)} & A_2^{(2)} & A_3^{(2)} & A_4^{(2)} & A_5^{(2)} & A_6^{(2)} & A_7^{(2)} & A_8^{(2)} \\ A_1 & A_1 & A_2 & A_2 & A_3 & A_3 & A_4 & A_4 \\ A_1 & \bar{A}_1 & A_2 & \bar{A}_2 & A_3 & \bar{A}_3 & A_4 & \bar{A}_4 \end{pmatrix}, \quad (6)$$

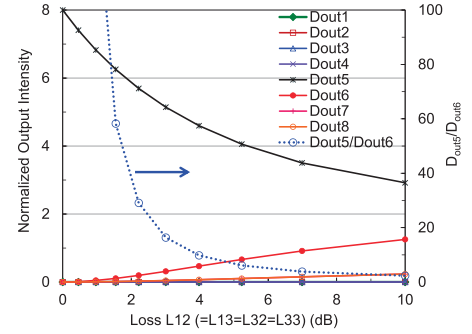
where  $\bar{A}_i = -A_i$  and the superscript (2) denotes the 8-bit labels.

The output  $D_i^{(2)}$  for  $A_i^{(2)}$  is obtained from Eqs.(4)–(6) [14]. Eight labels can be recognized with an infinite contrast ratio for the ideal case of  $\alpha_{ij} = 1$ .

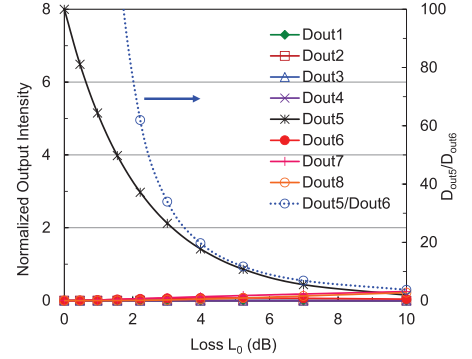
We now consider the effect of the phase deviation alone by setting  $\beta_{ij} = 1$ . To find the accumulated effect in the 4-bit



**Fig. 5** The output intensities as a function of the phase deviation  $\phi_{12}$  ( $= \phi_{13} = \phi_{32} = \phi_{33}$ ) for the 8-bit recognition circuit, where the other phases  $\phi_{ij}$  are assumed to be 0.



(a)



(b)

**Fig. 6** (a) The output intensities as a function of the waveguide loss  $L_{12}$  ( $= L_{13} = L_{32} = L_{33}$ ), where the other losses and the phase deviation are assumed to be 0. (b) The output intensities as a function of  $L_0$ , where  $L_{11} = L_{14} = L_{21} = L_{24} = L_{31} = L_{38} = 0$  dB,  $L_{12} = L_{13} = L_{22} = L_{23} = L_{32} = L_{37} = L_0$ ,  $L_{33} = L_{36} = 2L_0$ , and  $L_{34} = L_{35} = 3L_0$ , and the phase deviation is assumed to be 0.

basic module and in the connecting waveguides between  $B_i$  and  $C_i$ , we evaluated the output intensities as a function of  $\phi_{12}$  ( $= \phi_{13} = \phi_{32} = \phi_{33}$ ) as shown in Fig. 5, where the other phases  $\phi_{ij}$  are assumed to be 0. The ratio of  $D_{out5}/D_{out6}$  is also plotted to evaluate the contrast ratio. For example, the output from  $D_{out6}$  increases 5.4 % of the maximum output intensity when the phase deviation is  $0.1\pi$  rad, where, the contrast ratio decreases to 17.3. Now, we consider the effect of loss in two specific cases. First, we find the effect of  $\beta_{12}$ ,  $\beta_{13}$ ,  $\beta_{32}$ , and  $\beta_{33}$  on the outputs as a function of  $L_{12}$  ( $= L_{13} = L_{32} = L_{33}$ ) as shown in Fig. 6(a), where other  $L_{ij}$  are assumed to be 0. The loss of 2.2 dB in  $\beta_{12} = \beta_{13} =$

$\beta_{32} = \beta_{33}$  induces a decrease of 28.8 % and an increase relative to  $D_{out5}$  of 2.4 % at  $D_{out5}$  and  $D_{out6}$ , respectively. The contrast ratio decreases to 29.1. Next, we consider the case where the loss is assumed only at the crossed waveguides. We assume  $L_{11} = L_{14} = L_{21} = L_{24} = L_{31} = L_{38} = 0$  dB,  $L_{12} = L_{13} = L_{22} = L_{23} = L_{32} = L_{37} = L_0$ ,  $L_{33} = L_{36} = 2L_0$ , and  $L_{34} = L_{35} = 3L_0$  according to the number of crossed points. The output intensities as a function of  $L_0$  is shown in (b). The loss of 2.2 dB in  $L_0$  induces a decrease of 62.8 % and an increase relative to  $D_{out5}$  of 0.6 % at  $D_{out5}$  and  $D_{out6}$ , respectively. The contrast ratio decreases to 62.0. Although the output intensities decrease due to larger loss through the connecting waveguides, the contrast ratio is larger than the case shown in (a). This is caused by the assumed asymmetric losses in (a).

### 3. Increase of Recognizable 4-Bit Labels

In this section, we discuss methods to increase the number of recognizable labels by extending the circuits for 4-bit labels.

#### 3.1 Increase by Code Conversion

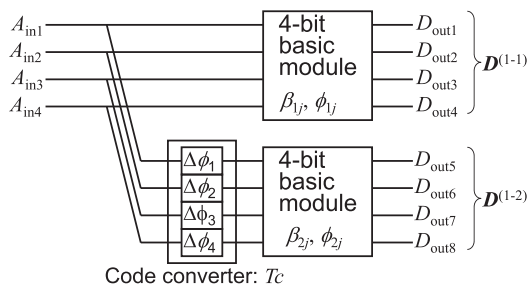
The basic idea to increase the number of recognizable labels is the extension of the circuit to accept other combination of label codes. Namely, we consider the codes having not only one but also zero or two “-1” components in each label of  $A_i$ . In order to accept such labels, a code converter circuit  $Tc$  is employed in front of the lower 4-bit basic module as shown in Fig. 7 [14]. In the code converter, constant phase shifts

$$\Delta\phi_i = \begin{cases} \pi & (i = 1) \\ 0 & (i = 2, 3, 4) \end{cases} \quad (7)$$

are applied to  $A_{in i}$  as  $A_{in i} e^{j\Delta\phi_i}$ ,  $i = 1, \dots, 4$ . Using this code converter, four labels  $A_5, A_6, A_7, A_8$  defined by

$$(A_5 \ A_6 \ A_7 \ A_8) = \begin{pmatrix} -1 & 1 & -1 & -1 \\ -1 & 1 & 1 & 1 \\ 1 & 1 & 1 & -1 \\ 1 & 1 & -1 & 1 \end{pmatrix} \quad (8)$$

are converted to  $A_1, A_2, A_3, A_4$ , respectively. Therefore,



**Fig. 7** A circuit to recognize eight 4-bit labels by employing code converter.

the outputs  $D_{out5}, \dots, D_{out8}$  from the lower 4-bit basic module for  $A_5, A_6, A_7$ , and  $A_8$  are the same as the outputs  $D_{out1}, \dots, D_{out4}$  for  $A_1, A_2, A_3$ , and  $A_4$ , respectively.

The outputs ( $D_1^{(1-1)} \dots D_4^{(1-1)}$ ) from the upper 4-bit basic module for ( $A_1, \dots, A_4$ ) are given by replacing  $\alpha_i$  by  $\alpha_{1i}$  in Eq. (3). The outputs ( $D_1^{(1-2)} \dots D_4^{(1-2)}$ ) from the lower 4-bit basic module are derived as

$$\begin{pmatrix} D_1^{(1-2)} & D_2^{(1-2)} & D_3^{(1-2)} & D_4^{(1-2)} \end{pmatrix} = \begin{pmatrix} -\alpha_{21} & \alpha_{21} & \alpha_{23} & -\alpha_{23} \\ \alpha_{21} & -\alpha_{21} & \alpha_{23} & -\alpha_{23} \\ -\alpha_{24} & -\alpha_{24} & \alpha_{22} & \alpha_{22} \\ \alpha_{24} & \alpha_{24} & \alpha_{22} & \alpha_{22} \end{pmatrix}. \quad (9)$$

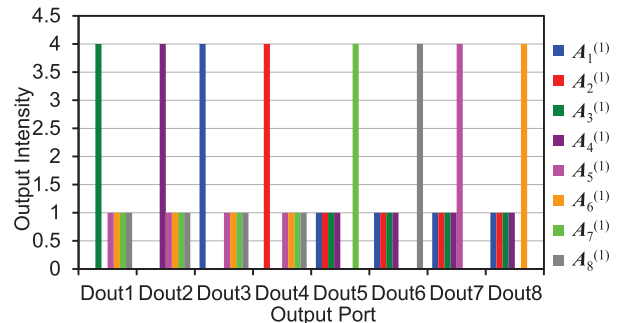
The outputs ( $D_5^{(1-1)} \dots D_8^{(1-1)}$ ) from the upper 4-bit basic module for ( $A_5, \dots, A_8$ ) are derived from Eqs. (1) and (8) as given by replacing  $\alpha_{2i}$  by  $\alpha_{1i}$  in Eq. (9). The outputs ( $D_5^{(1-2)} \dots D_8^{(1-2)}$ ) from the lower 4-bit basic module are given by replacing  $\alpha_i$  by  $\alpha_{2i}$  in Eq. (3).

The ideal output intensities for  $A_1, \dots, A_8$  with  $\alpha_{ij} = 1$  are plotted in Fig. 8. The contrast ratio at each output is calculated as  $(\pm 2.0)^2 / (\pm 1.0)^2 = 4.0$ . The decrease of the contrast ratio due to  $\alpha_{ij}$  is similar to that in the basic 4-bit module.

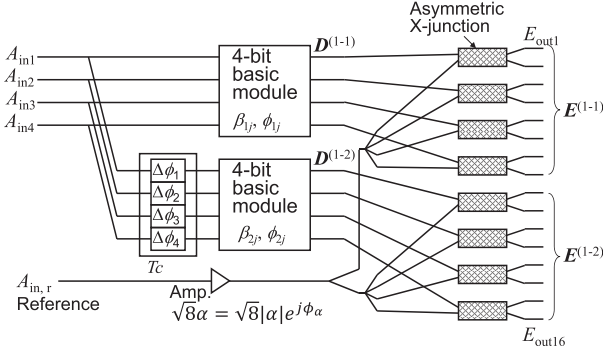
#### 3.2 Increase by Sign Identification

Since the number of the 4-bit binary codes is sixteen, only a half of the codes can be recognized in the circuit shown in Fig. 7. The rest codes are complement of  $A_i$ ,  $i = 1, \dots, 8$ , that is,  $\bar{A}_i$ . Although the output fields for  $A_i$  and  $\bar{A}_i$  are different in the sign, that is, the phase difference of  $\pi$ , they cannot be distinguished by their intensities.

To distinguish the sign of the output field, we introduce interference with a reference pulse  $A_{in,r}$  as shown in Fig. 9. The reference pulse is supposed to have been transmitted together with the label pulse train. The reference pulse  $A_{in,r}$  is amplified with the amplitude amplification coefficient  $\sqrt{8}\alpha$ , and is divided into eight pulses having amplitude  $\alpha A_{in,r}$ . Although, in our previous paper [14], the value of  $\alpha$  was assumed to be 1, we try to find an optimum value for  $\alpha$  in this paper. The output fields  $D^{(1-1)}$  and  $D^{(1-2)}$  of the basic modules are interfered with  $\alpha A_{in,r}$  through asymmetric X-junction couplers. For complete interference between the



**Fig. 8** Ideal output intensities for the eight 4-bit labels  $A_1, \dots, A_8$ .



**Fig. 9** A circuit to recognize the sixteen 4-bit labels by employing a code converter and interference with a reference pulse.

signals  $D^{(1-1)}$ ,  $D^{(1-2)}$ , and  $\alpha A_{in,r}$  to distinguish the sign, the phase relation is important. We define  $\alpha = |\alpha|e^{j\phi_\alpha}$ . The phase  $\phi_\alpha$  corresponds to the phase shift due to the fabrication error or an equivalent phase deviation in the reference signal  $A_{in,r}$ . The sixteen output fields  $E^{(1-1)}$  and  $E^{(1-2)}$  are related to the output fields  $D^{(1-1)}$  and  $D^{(1-2)}$ , and the reference  $\alpha A_{in,r}$  as

$$\begin{aligned} E^{(1-1)} &= (E_{out1}, \dots, E_{out8})^t \\ &= Tx_4(D_{out1}, \dots, D_{out4}, \alpha A_{in,r})^t, \end{aligned} \quad (10)$$

and

$$\begin{aligned} E^{(1-2)} &= (E_{out9}, \dots, E_{out16})^t \\ &= Tx_4(D_{out5}, \dots, D_{out8}, \alpha A_{in,r})^t, \end{aligned} \quad (11)$$

where

$$Tx_4 = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 & 0 & 0 & 0 & 1 \\ -1 & 0 & 0 & 0 & 1 \\ 0 & 1 & 0 & 0 & 1 \\ 0 & -1 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 & 1 \\ 0 & 0 & -1 & 0 & 1 \\ 0 & 0 & 0 & 1 & 1 \\ 0 & 0 & 0 & -1 & 1 \end{pmatrix}. \quad (12)$$

We assume  $A_{in,r} = 1$ . The output fields  $E^{(1-1)}$  and  $E^{(1-2)}$  for  $(A_1 \dots A_4)$  are given by

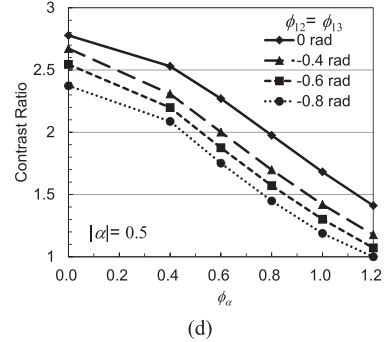
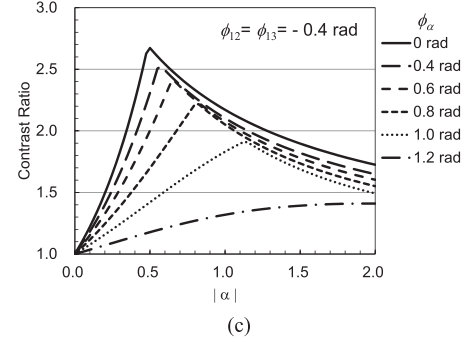
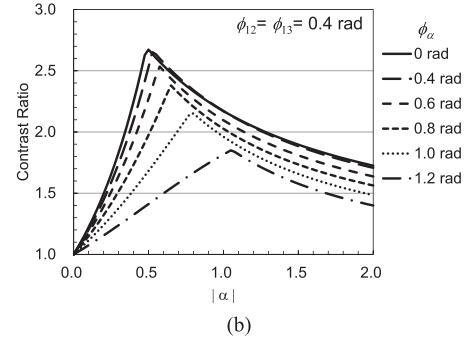
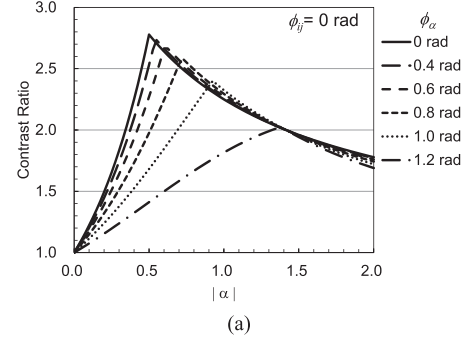
$$\begin{aligned} &(E_1^{(1-1)} \ E_2^{(1-1)} \ E_3^{(1-1)} \ E_4^{(1-1)}) \\ &= Tx_4 \begin{pmatrix} D_1^{(1-1)} & D_2^{(1-1)} & D_3^{(1-1)} & D_4^{(1-1)} \\ \alpha & \alpha & \alpha & \alpha \end{pmatrix}, \end{aligned} \quad (13)$$

where  $D_j^{(1-1)}$  are given by replacing  $\alpha_i$  by  $\alpha_{1i}$  in Eq. (3).

$$\begin{aligned} &(E_1^{(1-2)} \ E_2^{(1-2)} \ E_3^{(1-2)} \ E_4^{(1-2)}) \\ &= Tx_4 \begin{pmatrix} D_1^{(1-2)} & D_2^{(1-2)} & D_3^{(1-2)} & D_4^{(1-2)} \\ \alpha & \alpha & \alpha & \alpha \end{pmatrix}, \end{aligned} \quad (14)$$

where  $D_i^{(1-2)}$  are given by Eq. (9).

For  $(A_5 \dots A_8)$ ,  $(E_5^{(1-1)} \dots E_8^{(1-1)})$  and  $(E_5^{(1-2)} \dots E_8^{(1-2)})$  are obtained from Eq. (14) with the replacement of  $\alpha_{2i}$  by  $\alpha_{1i}$



**Fig. 10** The contrast ratio as a function of  $|\alpha|$  for the sixteen 4-bit labels for the phases  $\phi_{ij}$  of  $\alpha_{ij}$  are 0 in (a), for  $\phi_{12} = \phi_{13} = 0.4$  rad. and other  $\phi_{ij} = 0$  in (b), and for  $\phi_{12} = \phi_{13} = -0.4$  rad. and other  $\phi_{ij} = 0$  in (c). The contrast ratio at  $|\alpha| = 0.5$  as a function of  $\phi_\alpha$  is summarized in (d).

and Eq. (13) with the replacement of  $\alpha_{1i}$  by  $\alpha_{2i}$ , respectively.

We define  $A_9, A_{10}, A_{11}, A_{12}$  as  $\bar{A}_1, \bar{A}_2, \bar{A}_3, \bar{A}_4$ , respectively. For these labels, the output fields  $(E_9^{(1-1)} \dots E_{12}^{(1-1)})$  and  $(E_9^{(1-2)} \dots E_{12}^{(1-2)})$  are given by replacing  $\alpha_{ji}$  by  $-\alpha_{ji}$  in Eqs. (13) and (14), respectively.

We also define  $A_{13}, A_{14}, A_{15}, A_{16}$  as  $\bar{A}_5, \bar{A}_6, \bar{A}_7, \bar{A}_8$ , respectively. For these labels,  $(E_{13}^{(1-1)} \dots E_{16}^{(1-1)})$  and

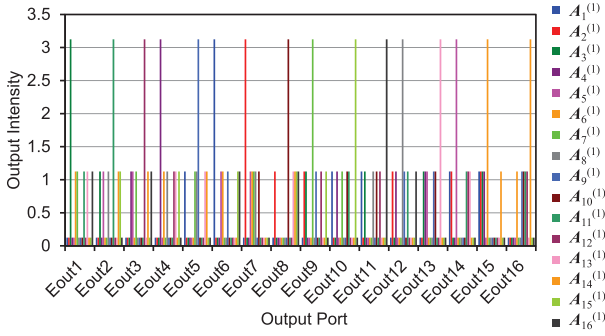


Fig. 11 Ideal output intensities at  $\alpha = 0.5$  for the sixteen 4-bit labels.

$(E_{13}^{(1-2)} \dots E_{16}^{(1-2)})$  are given by replacing  $\alpha_{2i}$  by  $-\alpha_{1i}$  in Eq. (14) and by replacing  $\alpha_{1i}$  by  $-\alpha_{2i}$  in Eq. (13), respectively.

The contrast ratio of the output intensities depends on the value  $\alpha$  as shown in Fig. 10, where the phase  $\phi_\alpha$  of  $\alpha$  is varied as a parameter. Three typical cases are shown for the phases  $\phi_{ij}$  of  $\alpha_{ij}$  are 0 in (a), for  $\phi_{12} = \phi_{13} = 0.4$  rad. and other  $\phi_{ij} = 0$  in (b), and for  $\phi_{12} = \phi_{13} = -0.4$  rad. and other  $\phi_{ij} = 0$  in (c). The contrast ratio at  $|\alpha| = 0.5$  as a function of  $\phi_\alpha$  is summarized in (d), where  $\phi_{ij}$  is varied from 0 to  $-0.8$  rad. The sign of  $\phi_{ij}$  is assumed to be different from that of  $\phi_\alpha$  to evaluate the worst phase-error combinations. If the required contrast ratio for the label recognition is 1.5, it is roughly estimated that the phase error of  $\phi_{ij}$  and  $\phi_\alpha$  has to be less than around 0.8 rad.

For the ideal case of  $\phi_\alpha = \phi_{ij} = 0$ , the maximum output intensity is  $[(2 + \alpha)/\sqrt{2}]^2$ . The second largest output intensity is the larger value between  $[(-2 + \alpha)/\sqrt{2}]^2$  and  $[(1 + \alpha)/\sqrt{2}]^2$ . Therefore, the maximum contrast ratio of  $[(2 + \alpha)/\sqrt{2}]^2 / \text{Max}([(-2 + \alpha)/\sqrt{2}]^2, [(1 + \alpha)/\sqrt{2}]^2) = 2.78$  is obtained when  $[(-2 + \alpha)/\sqrt{2}]^2 = [(1 + \alpha)/\sqrt{2}]^2$ , that is,  $\alpha = 0.5$ . The output intensities at  $\alpha = 0.5$  for all sixteen labels are plotted in Fig. 11.

## 4. Increase of Recognizable 8-Bit Labels

### 4.1 Increase by Code Conversion

In similar manner as the 4-bit label recognition, we consider a recognition circuit for a half of the 8-bit binary codes as shown in Fig. 12. The 8-bit basic module is the circuit shown in Fig. 4. A code converter  $Tc_k$  is placed in front of the  $k$ th 8-bit basic module, where  $k = 1, \dots, 16$ . Each code converter consists of parallel eight phase shifters with the phase shift amount of  $\Delta\phi_i, i = 1, \dots, 8$  as follows:

- For  $Tc_k, k = 1; \Delta\phi_i = 0 (i = 1, \dots, 8)$
- For  $Tc_k, k = 2, \dots, 9; \Delta\phi_{k-1} = \pi$  and  $\Delta\phi_i = 0 (i \neq k-1)$
- For  $Tc_k, k = 10, \dots, 16; \Delta\phi_1 = \pi, \Delta\phi_{k-8} = \pi$  and  $\Delta\phi_i = 0 (i \neq 1 \text{ or } i \neq k-8)$ .

Only one and two components of an incident code are inverted with  $Tc_k, k = 2, \dots, 9$ , and  $Tc_k, k = 10, \dots, 16$ , respectively. Using these converters and the 8-bit basic mod-

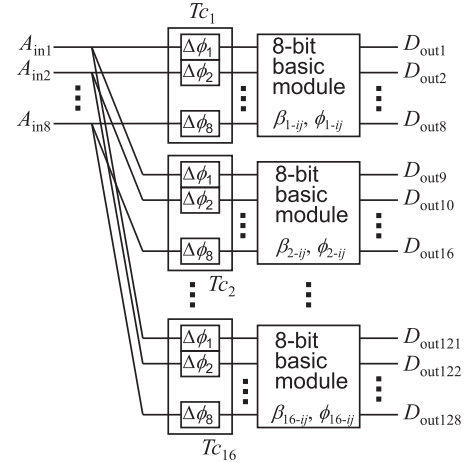


Fig. 12 A circuit to recognize the 128 8-bit labels by employing code converters.

ules, the 128 optical labels shown in Table 1 can be recognized. The decimal number for each label calculated by  $(A_{in1} + 1)/2 + (A_{in2} + 1)2^1/2 + \dots + (A_{in8} + 1)2^7/2$  is also given in this table to show that these labels are nonidentical with each other.

The output intensities for these labels are calculated by using Eqs. (4) and (5). Some typical parts of the ideal output intensities for labels  $(A_1^{(2)} \dots A_8^{(2)})$ ,  $(A_9^{(2)} \dots A_{16}^{(2)})$ , and  $(A_{17}^{(2)} \dots A_{24}^{(2)})$  are plotted in Fig. 13 (a), (b), and (c), respectively, where  $\alpha_{k-ij}$  are assumed to be 1. The contrast ratio for these 128 label recognition is  $[8/(2\sqrt{2})/(6/(2\sqrt{2}))]^2 = 1.78$ . If the system is separated into two groups, that is,  $(Tc_1, Tc_2, \dots, Tc_8)$  and  $(Tc_9, \dots, Tc_{16})$ , the contrast ratio for each group is  $[8/(2\sqrt{2})/(4/(2\sqrt{2}))]^2 = 4.0$ , where 64 labels are recognized in each system.

### 4.2 Increase by Sign Identification

To recognize all the 8-bit binary labels, we introduce interference with a reference pulse as shown in Fig. 14, where the  $k$ th code converter and the 8-bit basic module are illustrated. Since sixteen similar circuits for  $k = 1, \dots, 16$  are connected in parallel, the incident signals  $A_{in1}, \dots, A_{in8}$ , and  $A_{in,r}$  are divided into sixteen signals. However, for simplicity, the signals of amplitudes  $A_{in1}, \dots, A_{in8}$ , and  $A_{in,r}$  are assumed to be input into each parallel circuits.

The output fields  $E_{out16(k-1)+m}, m, k = 1, \dots, 16$ , are related to the output fields of 8-bit basic modules  $D_{out(k-1)+m}, m = 1, \dots, 8$ , and the reference signal  $A_{in,r}$  as

$$\begin{pmatrix} E_{out16(k-1)+1} \\ E_{out16(k-1)+2} \\ \vdots \\ E_{out16(k-1)+16} \end{pmatrix} = T_{x8} \begin{pmatrix} D_{out(k-1)+1} \\ \vdots \\ D_{out(k-1)+8} \\ A_{in,r} \end{pmatrix}, \quad (15)$$

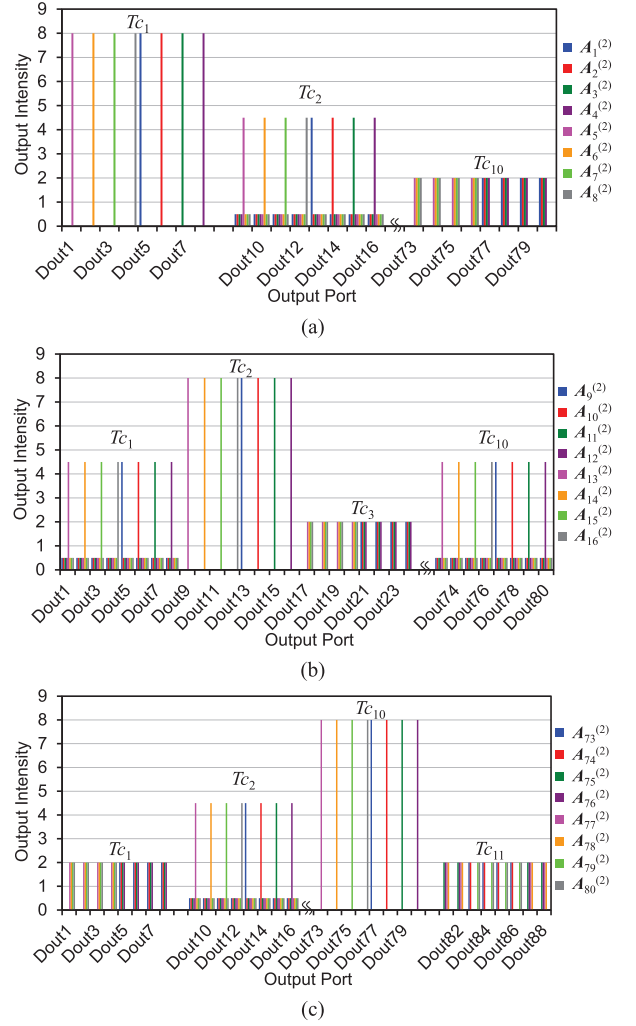
where

**Table 1** Recognizable 128 8-bit label by code conversion.

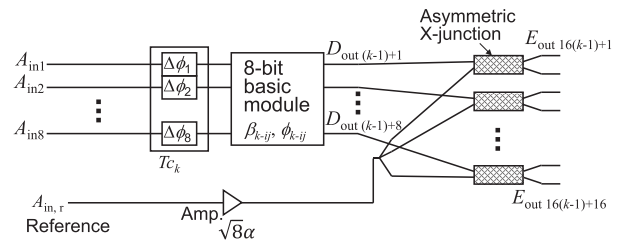
$T_{C1}$ :	$(A_1^{(2)} \dots A_8^{(2)}) = \begin{pmatrix} A_1 A_1 A_2 A_2 A_3 A_3 A_4 A_4 \\ A_1 \bar{A}_1 A_2 \bar{A}_2 A_3 \bar{A}_3 A_4 \bar{A}_4 \end{pmatrix}$ $\rightarrow (221 \ 45 \ 238 \ 30 \ 119 \ 135 \ 187 \ 75)$
$T_{C2}$ :	$(A_9^{(2)} \dots A_{16}^{(2)}) = \begin{pmatrix} A_5 A_5 A_6 A_6 A_7 A_7 A_8 A_8 \\ A_1 \bar{A}_1 A_2 \bar{A}_2 A_3 \bar{A}_3 A_4 \bar{A}_4 \end{pmatrix}$ $\rightarrow (220 \ 44 \ 239 \ 31 \ 118 \ 134 \ 186 \ 74)$
$T_{C3}$ :	$(A_{17}^{(2)} \dots A_{24}^{(2)}) = \begin{pmatrix} A_6 A_6 A_5 A_5 \bar{A}_8 \bar{A}_8 \bar{A}_7 \bar{A}_7 \\ A_1 \bar{A}_1 A_2 \bar{A}_2 A_3 \bar{A}_3 A_4 \bar{A}_4 \end{pmatrix}$ $\rightarrow (223 \ 47 \ 236 \ 28 \ 117 \ 133 \ 185 \ 73)$
$T_{C4}$ :	$(A_{25}^{(2)} \dots A_{32}^{(2)}) = \begin{pmatrix} \bar{A}_7 \bar{A}_7 A_8 A_8 \bar{A}_5 \bar{A}_5 A_6 A_6 \\ A_1 \bar{A}_1 A_2 \bar{A}_2 A_3 \bar{A}_3 A_4 \bar{A}_4 \end{pmatrix}$ $\rightarrow (217 \ 41 \ 234 \ 26 \ 115 \ 131 \ 191 \ 79)$
$T_{C5}$ :	$(A_{33}^{(2)} \dots A_{40}^{(2)}) = \begin{pmatrix} \bar{A}_8 \bar{A}_8 A_7 A_7 A_6 A_6 \bar{A}_5 \bar{A}_5 \\ A_1 \bar{A}_1 A_2 \bar{A}_2 A_3 \bar{A}_3 A_4 \bar{A}_4 \end{pmatrix}$ $\rightarrow (213 \ 37 \ 230 \ 22 \ 127 \ 143 \ 179 \ 67)$
$T_{C6}$ :	$(A_{41}^{(2)} \dots A_{48}^{(2)}) = \begin{pmatrix} A_1 A_1 A_2 A_2 A_3 A_3 A_4 A_4 \\ A_5 \bar{A}_5 A_6 \bar{A}_6 A_7 \bar{A}_7 A_8 \bar{A}_8 \end{pmatrix}$ $\rightarrow (205 \ 61 \ 254 \ 14 \ 103 \ 151 \ 171 \ 91)$
$T_{C7}$ :	$(A_{49}^{(2)} \dots A_{56}^{(2)}) = \begin{pmatrix} A_1 A_1 A_2 A_2 A_3 A_3 A_4 A_4 \\ A_6 \bar{A}_6 A_5 \bar{A}_5 \bar{A}_8 \bar{A}_8 \bar{A}_7 \bar{A}_7 \end{pmatrix}$ $\rightarrow (253 \ 13 \ 206 \ 62 \ 87 \ 167 \ 155 \ 107)$
$T_{C8}$ :	$(A_{57}^{(2)} \dots A_{64}^{(2)}) = \begin{pmatrix} A_1 A_1 A_2 A_2 A_3 A_3 A_4 A_4 \\ \bar{A}_7 \bar{A}_7 A_8 \bar{A}_8 \bar{A}_5 \bar{A}_5 A_6 A_6 \end{pmatrix}$ $\rightarrow (157 \ 109 \ 174 \ 94 \ 55 \ 199 \ 251 \ 11)$
$T_{C9}$ :	$(A_{65}^{(2)} \dots A_{72}^{(2)}) = \begin{pmatrix} A_1 A_1 A_2 A_2 A_3 A_3 A_4 A_4 \\ \bar{A}_8 \bar{A}_8 A_7 \bar{A}_7 A_6 \bar{A}_6 \bar{A}_5 \bar{A}_5 \end{pmatrix}$ $\rightarrow (93 \ 173 \ 110 \ 158 \ 247 \ 7 \ 59 \ 203)$
$T_{C10}$ :	$(A_{73}^{(2)} \dots A_{80}^{(2)}) = \begin{pmatrix} A_2 A_2 A_1 A_1 \bar{A}_4 \bar{A}_4 \bar{A}_3 \bar{A}_3 \\ A_1 \bar{A}_1 A_2 \bar{A}_2 A_3 \bar{A}_3 A_4 \bar{A}_4 \end{pmatrix}$ $\rightarrow (222 \ 46 \ 237 \ 29 \ 116 \ 132 \ 184 \ 72)$
$T_{C11}$ :	$(A_{81}^{(2)} \dots A_{88}^{(2)}) = \begin{pmatrix} \bar{A}_3 \bar{A}_3 A_4 A_4 \bar{A}_1 \bar{A}_1 A_2 A_2 \\ A_1 \bar{A}_1 A_2 \bar{A}_2 A_3 \bar{A}_3 A_4 \bar{A}_4 \end{pmatrix}$ $\rightarrow (216 \ 40 \ 235 \ 27 \ 114 \ 130 \ 190 \ 78)$
$T_{C12}$ :	$(A_{89}^{(2)} \dots A_{96}^{(2)}) = \begin{pmatrix} \bar{A}_4 \bar{A}_4 A_3 A_3 A_2 A_2 \bar{A}_1 \bar{A}_1 \\ A_1 \bar{A}_1 A_2 \bar{A}_2 A_3 \bar{A}_3 A_4 \bar{A}_4 \end{pmatrix}$ $\rightarrow (212 \ 36 \ 231 \ 23 \ 126 \ 142 \ 178 \ 66)$
$T_{C13}$ :	$(A_{97}^{(2)} \dots A_{104}^{(2)}) = \begin{pmatrix} A_5 A_5 A_6 A_6 A_7 A_7 A_8 A_8 \\ A_5 \bar{A}_5 A_6 \bar{A}_6 A_7 \bar{A}_7 A_8 \bar{A}_8 \end{pmatrix}$ $\rightarrow (204 \ 60 \ 255 \ 15 \ 102 \ 150 \ 170 \ 90)$
$T_{C14}$ :	$(A_{105}^{(2)} \dots A_{112}^{(2)}) = \begin{pmatrix} A_5 A_5 A_6 A_6 A_7 A_7 A_8 A_8 \\ A_6 \bar{A}_6 A_5 \bar{A}_5 \bar{A}_8 \bar{A}_8 \bar{A}_7 \bar{A}_7 \end{pmatrix}$ $\rightarrow (252 \ 12 \ 207 \ 63 \ 86 \ 166 \ 154 \ 106)$
$T_{C15}$ :	$(A_{113}^{(2)} \dots A_{120}^{(2)}) = \begin{pmatrix} A_5 A_5 A_6 A_6 A_7 A_7 A_8 A_8 \\ \bar{A}_7 \bar{A}_7 A_8 \bar{A}_8 \bar{A}_5 \bar{A}_5 A_6 A_6 \end{pmatrix}$ $\rightarrow (156 \ 108 \ 175 \ 95 \ 54 \ 198 \ 250 \ 10)$
$T_{C16}$ :	$(A_{121}^{(2)} \dots A_{128}^{(2)}) = \begin{pmatrix} A_5 A_5 A_6 A_6 A_7 A_7 A_8 A_8 \\ \bar{A}_8 \bar{A}_8 A_7 \bar{A}_7 A_6 \bar{A}_6 \bar{A}_5 \bar{A}_5 \end{pmatrix}$ $\rightarrow (92 \ 172 \ 111 \ 159 \ 246 \ 6 \ 58 \ 202)$

$$T_{X8} = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & -1 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & -1 & 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & -1 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 & -1 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & -1 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & -1 & 0 & 1 \end{pmatrix}. \quad (16)$$

First, we consider an ideal case of  $\alpha_{k-i} = 1$  and  $\phi_\alpha = 0$ .

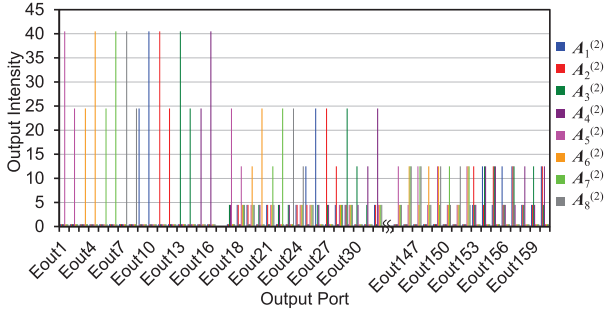


**Fig. 13** The output intensities at the partial output ports for the 128-bit labels with the circuits having code converters for (a)  $(A_1^{(2)}, \dots, A_8^{(2)})$ , (b)  $(A_9^{(2)}, \dots, A_{16}^{(2)})$ , and (c)  $(A_{73}^{(2)}, \dots, A_{80}^{(2)})$ .



**Fig. 14** A circuit to recognize the 256 8-bit labels by employing a code converter and interference with a reference pulse, where the  $k$ th partial circuit is illustrated.

The maximum output  $E_{outk}$  is  $(2\sqrt{2} + \alpha)/\sqrt{2}$ . The minimum value of the secondly largest output is  $|(-2\sqrt{2} + \alpha)/\sqrt{2}| = |(6 + 2\sqrt{2}\alpha)/4|$  when  $\alpha = \sqrt{2}/4 \approx 0.354$ . The maximum contrast ratio is found to be  $[(2\sqrt{2} + \alpha)/\sqrt{2}] / [(-2\sqrt{2} + \alpha)/\sqrt{2}]^2 \approx 1.653$  at  $\alpha \approx 0.354$ . The output intensities of  $E_{out1}, \dots, E_{out32}, E_{out145}, \dots, E_{out160}$  are plotted for labels  $A_1^{(2)}, \dots, A_8^{(2)}$  in Fig. 15. These characteristics are the same for the other labels. Thus, all binary 8-bit labels



**Fig. 15** The output intensities of  $E_{\text{out}1}, \dots, E_{\text{out}32}, E_{\text{out}33}, \dots, E_{\text{out}160}$  at  $\alpha = 0.354$  for the eight 8-bit labels  $A_1^{(2)}, \dots, A_8^{(2)}$ .

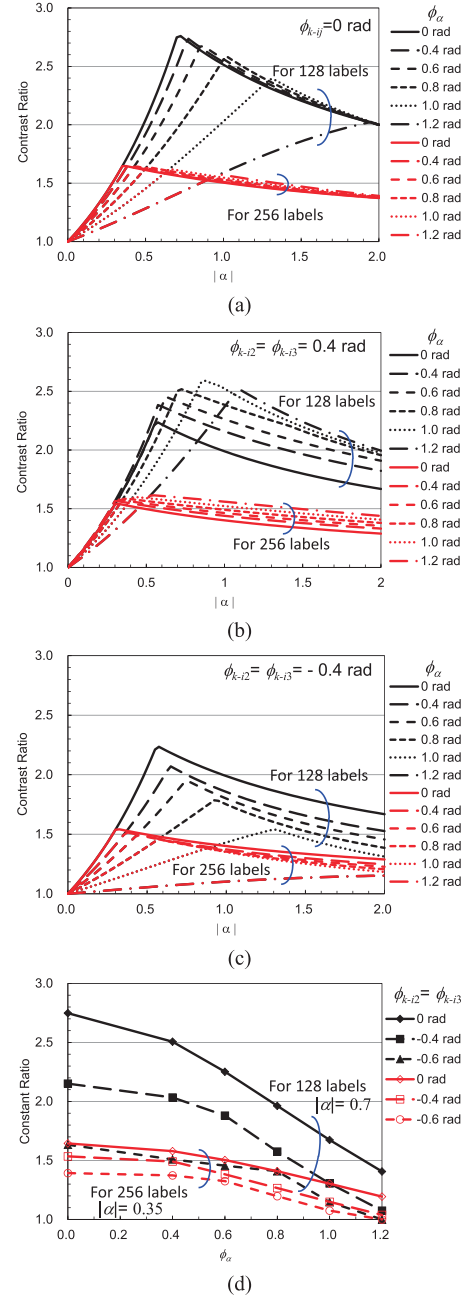
can be recognized with a contrast ratio of 1.653. If the labels are divided into two groups, namely, the labels for  $(Tc_1, Tc_{10}, \dots, Tc_{16})$  and for  $(Tc_2, \dots, Tc_9)$ , the minimum value of the second highest output can be  $|(-2\sqrt{2} + \alpha)/\sqrt{2}| = |(4 + 2\sqrt{2}\alpha)/4|$  when  $\alpha = 1/\sqrt{2} \approx 0.707$ . With this  $\alpha$ , the contrast ratio becomes  $[(2\sqrt{2} + \alpha)/\sqrt{2}] / [(-2\sqrt{2} + \alpha)/\sqrt{2}]^2 \approx 2.778$ .

Next, we consider the effect of phases  $\phi_\alpha$  and  $\phi_{k-ij}$ . The minimum contrast ratio for the 128 and 256 labels is plotted as a function of  $|\alpha|$  in Fig. 16 for the cases of  $\phi_{k-i2} = \phi_{k-i3} = 0, 0.4$ , and  $-0.4$  rad. in (a), (b), and (c), respectively, where  $\phi_\alpha$  is varied as a parameter. The contrast ratio at  $|\alpha| = 0.7$  and  $0.35$  for 128 and 256 labels, respectively, as a function of  $\phi_\alpha$  is summarized in (d). It is found that the contrast ratio decreases due to the phase deviation of  $\phi_\alpha$  and  $\phi_{k-ij}$  for a constant  $|\alpha|$ . If the constant ratio required for the label recognition is supposed to be 1.5, it is roughly estimated that the phase error of  $\phi_{k-ij}$  and  $\phi_\alpha$  has to be less than around  $0.5$  and  $0.4$  rad for 128 and 256 labels, respectively.

## 5. Discussion

The proposed circuits for the 4-bit BPSK labels can recognize 4, 8, and 16 labels with a contrast ratio of infinity, 4.00, and 2.78, respectively for the ideal cases of no phase shift. The circuits for the 8-bit labels can recognize 8, 64, 128, and 256 labels with a contrast ratio of infinity, 4.00, 2.78, and 1.65, respectively for the cases of no phase shift.

We compare these results with the tree-structure waveguide circuits with asymmetric X-junction couplers reported by Hiura *et al.* [12] designed for  $2^N$   $N$ -bit BPSK labels. The number of recognizable bits can be increased with the number of concatenating stage of the asymmetric X-junction couplers. Four, eight, and sixteen labels corresponding to 2-, 3-, and 4-bit BPSK labels can be recognized with a contrast ratio of 9.00, 4.00, and 2.78, respectively. Similarly, 64, 128, and 256 labels corresponding to 6-, 7-, and 8-bit BPSK labels can be recognized with a contrast ratio of 1.96, 1.78, and 1.65, respectively. These contrast ratios for 64, 128, and 256 labels are plotted in Fig. 17 compared with the circuits proposed in this paper. It is found that contrast ratios of this work are larger than or equal to that of the tree-structured circuits. Therefore, the circuits proposed in this

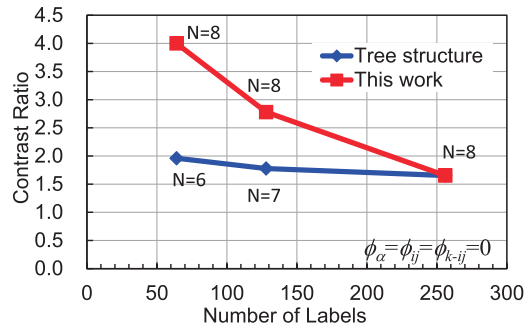


**Fig. 16** The contrast ratio as a function of  $\alpha$  for the 256 and the classified 128 8-bit labels for the cases of (a)  $\phi_{k-ij} = 0$ , (b)  $\phi_{k-ij} = 0.4$  rad., and (c)  $\phi_{k-ij} = -0.4$  rad. The contrast ratio at  $|\alpha| = 0.7$  and  $0.35$  for the 128 and 256 labels, respectively, as a function of  $\phi_\alpha$  is summarized in (d).

paper can relax the requirement such as a dynamic range of post-processing thresholding devices. When the recognizable label number is maximized, both circuits show the same contrast ratio because they only consist of passive elements.

We consider the influence of the incident optical intensity on the recognition performance. When the number of labels increase, the incident intensities to the optical circuits, e.g. 8-bit basic modules in Fig. 12, decrease due to power dividers for parallel processing. Since the optical cir-





**Fig. 17** The contrast ratio as a function of the number of recognizable labels with the tree-structure circuit proposed by Hiura *et al.* and the circuit of this work, where  $N$  is the number of bits.

circuits consist of passive waveguides and passive waveguide components, the S/N of the optical signal is expected to degrade only due to scattering and crosstalk in the waveguide components and does not depend on the incident power. However, when the output optical intensities decrease, the detected electric signals degrade due to additive noise at detectors and electronic amplifiers. Similar degradation is expected when the optical label intensities incident at the recognition circuits decrease.

Finally, we consider the scalability of the proposed circuits. It was reported that 32-bit labels were employed in the burst optical packet switching [15]. Since the 8-bit basic module consists of the two 4-bit basic modules, a 16-bit basic module can be composed with the two 8-bit basic modules. However, as shown in Fig. 17, the contrast ratio decreases with the employed number of labels. Therefore, from the viewpoint of the contrast ratio, the employed number of labels has to be limited for a given bit number. To increase further the number of labels without sacrificing the contrast ratio, a multi-stage recognition process can be considered. For instance, if the incident 32-bit labels are demultiplexed into four time-series of 8-bit labels prior to the recognition, the 8-bit basic module can be applied for each time slot. In this case, additional memory and post-processing functions with the help of electronic processing would be required to recognize all of the labels.

## 6. Conclusion

The optical passive waveguide circuits for the recognition of BPSK labels have been discussed. The proposed circuits can recognize eight and sixteen labels of the 4-bit BPSK labels with a contrast ratio of 4.00 and 2.78, respectively. The 8-bit BPSK labels, 64, 128, and 256 labels can be recognized with a contrast ratio of 4.00, 2.78, and 1.65, respectively. The number of recognizable labels can be increased to all binary encoded labels at the expense of reduction of the contrast ratio.

The decrease of the contrast ratio due to the phase deviation and the propagation loss through optical waveguides was also investigated. Although the effect of phase error is large, it can be reduced by introducing a phase adjusting

mechanism in the waveguide devices. Optical path-length adjusting waveguides as introduced in [14] are considered to be useful to simplify the phase adjustment. A systematic procedure for the phase adjustment for all the labels may be required when the number of labels increases.

Since the circuits consist of passive waveguide components, various materials such as silica glass and silicon can be employed.

## Acknowledgments

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