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Wayne D. Shepperd

H.T. Mowrer

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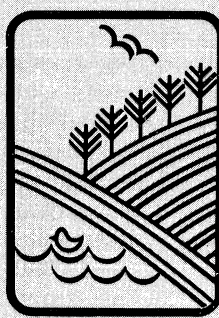
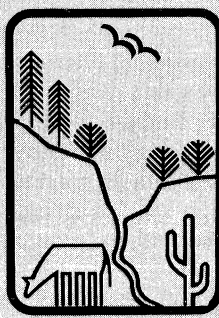
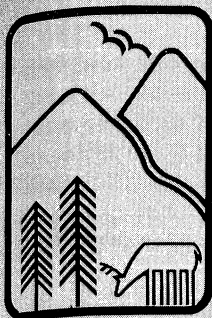
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USDA Forest Service

Rocky Mountain Forest and
Range Experiment Station

Whole Stand Volume Tables for Quaking Aspen in the Rocky Mountains

Wayne D. Shepperd and H. Todd Mowrer¹

Linear regression equations were developed to predict stand volumes for aspen given average stand basal area and average stand height. Tables constructed from these equations allow easy field estimation of gross merchantable cubic and board foot Scribner Rules per acre, and cubic meters per hectare using simple prism cruise data.

Keywords: *Populus tremuloides*, stand volume estimates, point-sampling

Introduction

Until recently, reliable, easy to use volume tables for quaking aspen (*Populus tremuloides* Michx.) in the central Rocky Mountains were not available. Foresters were limited to using crude tables derived in the early 1900's (Baker 1925), or tables which required field estimation of merchantable height (Peterson 1961). Edminster et al. (1981) simplified estimation of stem volumes by developing simple linear equations for aspen. The equations do not require estimation of merchantable height and provide volume/basal area ratio tables (Dilworth and Bell 1974) useful to estimate stem volumes from a diameter class cruise tally.

The tables and methodology presented here allow the direct estimation of gross stand volume per acre or hectare from average stand basal area and average stand height. The tables were developed from stand summaries computed with Edminster et al.'s (1981) equations and are applicable to even-aged aspen in Colorado and southern Wyoming. The merchantability limits for cubic, board feet Scribner, and metric tables are stems greater than 5 inches, 7 inches, and 10 cm, respectively.

¹The authors are Silviculturist and Associate Mensurationist, respectively, at the Rocky Mountain Forest and Range Experiment Station's headquarters in Fort Collins, in cooperation with Colorado State University.

Methodology

Data from two independent studies were used. A yield study contributed individual stem data from 100 fixed area plots containing from 100 to 150 trees each. A classification study contributed 70 stands point sampled with a Basal Area Factor (BAF) 10 or 20 prism, and 23 stands sampled using fixed area plots containing from 20 to 30 stems each. Stand volumes for all 193 stands were estimated by calculating individual stem volumes using Edminster et al.'s (1981) equations and then summing on a per area basis. These volumes then served as the dependent variable in a least squares regression analysis, with the weighted average height of all stems included in the volume computation as the independent variable. Because minimum diameter for the independent variable coincided with minimum merchantability standards, the resultant equations can be used to estimate stand volumes by including only those stems meeting the merchantability criteria in the determination of average basal area and height.

Regressions were run independently on both data sets for gross merchantable cubic feet per acre to a 4-inch top, board feet per acre Scribner Rule to a 6-inch top, and gross merchantable cubic meters per hectare. In all cases, equations from the two data sets were quite similar. Volume estimates were predicted for average

stand basal areas and heights of one data set using equations developed from the other data set. In all cases, there appeared to be reasonable agreement over the range of data between these estimates and the "actual" stand volumes estimated by Edminster et al.'s (1981) individual stem equations.

Next, the models derived from the two data sets for each volume table were tested for equality of coefficients by the method suggested by Graybill (1976). Good agreement between the two data sets was obtained for all volume equations with significance levels of 0.79, 0.22, and 0.48 for the cubic, board feet, and metric equations, respectively. Both data sets then were combined, and regressions were recomputed to derive the final equations used to construct the tables.

This technique and the resulting volume tables do not estimate actual stand volumes, but instead estimate the volumes which would be obtained from an individual stem cruise using Edminster et al.'s (1981) equations. Therefore, the statistics presented with these tables do not account for any error of estimation associated with Edminster et al.'s (1981) equations. The "smoothing" effect caused by this approach should be offset in general cruising applications by the greater sample intensities made possible with whole stand tables and their ease of use. Users requiring a higher degree of accuracy should continue to utilize individual stem cruising to estimate stand volumes.

Using the Tables

An estimate of average stand basal area and height can be obtained several ways. However, the quickest and easiest method would be a series of BAF variable radius points placed throughout the stand at which the cruiser counts "in" trees and multiplies by BAF to obtain a basal area estimate. A minimum sampling intensity of at least one point per acre using BAF of 10 or 20 is recommended for most aspen stands in the Rocky Mountains. Include only stems larger than 5 inches (10 cm) d.b.h. for cubic volume estimates, and only those larger than 7 inches d.b.h. for Scribner estimates. Additional diameter measurements or tallies are not needed. A stand height estimate should be taken at each point, and should be averaged to provide a height input for the tables. Metric basal area estimates can be obtained directly using a metric prism or wedge with a BAF of 2.5 to 5, or converted from English basal area estimates using:

$$\text{Square meters/ha} = \text{square feet/acre} * 0.229568.$$

The average stand basal areas and heights can then be used with the appropriate table to directly estimate stand volumes. No further computation or summaries are necessary. Procedures for converting these tables to hand-held calculator programs are available (Shepperd 1980). However, the valid application of any program written will be restricted to the range of data presented in the tables.

The growth characteristics of aspen in the Rocky Mountains make whole stand volume tables particularly useful to field situations where the volume of a large area encompassing a number of clones is being estimated. Because a clone is a genetic individual instead of a single tree, many more sample points per unit area are needed to adequately sample the natural genetic diversity within a stand. The cost of conventional individual tree cruises often prohibit sampling to these intensities. However, the ease of application of these whole stand volume tables allow the gathering of data from numerous sample points throughout a stand and will more adequately measure stocking variability resulting from clonal or microsite variation, provided that an appropriate sampling intensity is used.

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Table 1.—Aspen stand volume table in gross merchantable cunits per acre for even-aged aspen in Colorado and southern Wyoming. Includes stems greater than 5.0 inches d.b.h. to a 4-inch top d.i.b. Stump height 1 foot.

Basal area (ft ² /acre)	Average stand height (feet)																
	20	25	30	35	40	45	50	55	60	65	70	75	80	85	90	95	100
10																	
20																	
30	0	0	<u>1</u>	2	2	3	3	4									
40	1	<u>1</u>	<u>2</u>	3	<u>4</u>	5	5	6	7								
50	1	<u>2</u>	<u>3</u>	<u>4</u>	<u>5</u>	6	<u>7</u>	8	9								
60	2	<u>3</u>	<u>5</u>	<u>6</u>	<u>7</u>	<u>8</u>	9	11	12	13							
70	3	4	6	7	<u>9</u>	<u>10</u>	11	13	14	16	17						
80			7	<u>9</u>	<u>10</u>	12	13	15	17	18	20	20					
90			8	<u>10</u>	<u>12</u>	14	15	17	19	21	22	24					
100			9	11	<u>13</u>	<u>15</u>	<u>17</u>	<u>19</u>	<u>21</u>	<u>23</u>	<u>25</u>	27					
110				<u>13</u>	<u>15</u>	<u>17</u>	<u>19</u>	<u>22</u>	<u>24</u>	26	28	30	32				
120				14	17	<u>19</u>	<u>21</u>	<u>24</u>	<u>26</u>	28	31	33	36	38			
130				16	18	21	<u>23</u>	<u>26</u>	<u>28</u>	31	<u>34</u>	36	39	41			
140				17	20	22	<u>25</u>	<u>28</u>	31	34	<u>36</u>	39	<u>42</u>	45			
150				18	21	24	<u>27</u>	<u>30</u>	<u>33</u>	<u>36</u>	<u>39</u>	<u>42</u>	<u>45</u>	48			
160				20	23	26	<u>29</u>	<u>32</u>	<u>36</u>	<u>39</u>	<u>42</u>	<u>45</u>	48	51			
170				21	24	28	<u>31</u>	<u>35</u>	<u>38</u>	<u>41</u>	<u>45</u>	48	51	55	58		
180				22	<u>26</u>	30	<u>33</u>	<u>37</u>	<u>40</u>	<u>44</u>	<u>47</u>	<u>51</u>	<u>55</u>	<u>58</u>	62		
190				24	<u>28</u>	31	<u>35</u>	<u>39</u>	<u>43</u>	<u>46</u>	<u>50</u>	<u>54</u>	<u>58</u>	62	65	69	
200				25	29	33	<u>37</u>	<u>41</u>	<u>45</u>	49	<u>53</u>	57	<u>61</u>	65	<u>69</u>	73	
210					31	35	39	<u>43</u>	<u>47</u>	<u>52</u>	56	60	64	68	<u>72</u>	77	81
220					32	<u>37</u>	41	<u>46</u>	<u>50</u>	54	59	63	67	72	76	80	85
230					34	39	43	<u>48</u>	<u>52</u>	<u>57</u>	<u>61</u>	66	<u>70</u>	<u>75</u>	80	84	89
240					36	40	45	<u>50</u>	<u>55</u>	<u>59</u>	<u>64</u>	69	<u>74</u>	<u>78</u>	83	88	93
250					37	42	47	<u>52</u>	<u>57</u>	<u>62</u>	<u>67</u>	72	77	82	87	92	97
260					39	44	49	<u>54</u>	59	<u>65</u>	70	75	80	<u>85</u>	90	95	
270					40	46	<u>51</u>	<u>56</u>	<u>62</u>	<u>67</u>	72	78	83	<u>89</u>	94	99	
280					42	47	53	<u>59</u>	64	70	75	81	86	92	<u>97</u>	103	
290					44	49	55	61	67	72	78	84	90	95	101	107	
300					45	51	57	63	69	75	81	87	93	99	105	111	
310					47	53	59	65	71	77	84	90	96	102			
320					48	55	61	67	74	80	<u>86</u>	<u>93</u>	99	105			
330					50	56	63	70	76	83	<u>89</u>	96	102	109			
340								72	78	<u>85</u>	<u>92</u>	99	105	112			
350									81	88	<u>95</u>	102	109	116			
360										90	<u>97</u>	105	112	119			
370										100	<u>108</u>	<u>115</u>	122				
380											111	118	126				
390											114	121	129				
400											117	124	132				
410											119	<u>128</u>	136				
420											122	131	139				
430											125	134	142				

$Cunits/acre = (0.39666673 * BAHT - 249.0846) / 100$

Where: BAHT = Average stand basal area in square feet/acre x average stand height in feet.

Standard error of estimate: 2.173 Cunits/acre.

Values underlined indicate extent of data.

Table 2.—Aspen stand volumes in thousand board feet, inside bark Scribner Rule, merchantable stems excluding stump and top, aspen in Colorado and southern Wyoming. Includes stems greater than 7 inches d.b.h. to a 6-inch d.i.b. Stump height 1 foot.

Basal area (ft ² /acre)	Average stand height (feet)															
	30	35	40	45	50	55	60	65	70	75	80	85	90	95	100	
20	0	0	0	0	0	0	1	1	1							
40	1	1	<u>1</u>	<u>1</u>	<u>2</u>	2	2	3	3	3						
60	1	2	<u>2</u>	<u>3</u>	<u>3</u>	<u>4</u>	<u>4</u>	<u>5</u>	5	6	6					
80		3	4	<u>4</u>	<u>5</u>	5	6	<u>7</u>	7	8	9	9				
100		4	5	<u>6</u>	<u>6</u>	<u>7</u>	8	<u>9</u>	10	11	11	12	13			
120			6	<u>7</u>	<u>8</u>	<u>9</u>	<u>10</u>	<u>11</u>	12	13	14	15	16			
140			7	<u>9</u>	<u>10</u>	<u>11</u>	<u>12</u>	<u>13</u>	<u>14</u>	<u>16</u>	<u>17</u>	18	19	21		
160			9	<u>10</u>	<u>11</u>	<u>13</u>	<u>14</u>	<u>15</u>	<u>17</u>	<u>18</u>	<u>20</u>	21	23	24	26	
180			10	<u>12</u>	<u>13</u>	<u>15</u>	<u>16</u>	<u>18</u>	<u>19</u>	<u>21</u>	<u>23</u>	<u>24</u>	26	28	29	
200				<u>13</u>	15	<u>16</u>	<u>18</u>	<u>20</u>	<u>22</u>	<u>24</u>	<u>26</u>	<u>27</u>	<u>29</u>	<u>31</u>	33	
220				15	16	<u>18</u>	<u>20</u>	<u>22</u>	<u>24</u>	<u>26</u>	<u>29</u>	<u>31</u>	33	35	37	
240					18	<u>20</u>	<u>23</u>	<u>25</u>	<u>27</u>	<u>29</u>	<u>32</u>	<u>34</u>	36	39	41	
260					20	<u>22</u>	<u>25</u>	<u>27</u>	<u>30</u>	<u>32</u>	35	<u>37</u>	40	43	46	
280					22	<u>24</u>	<u>27</u>	30	<u>32</u>	<u>35</u>	38	<u>41</u>	44	47	50	
300						26	29	32	<u>35</u>	<u>38</u>	41	44	<u>48</u>	51		
320						29	32	35	<u>38</u>	<u>41</u>	45	48	<u>52</u>	55		
340							34	37	41	<u>44</u>	48	52	<u>56</u>	59		
360								40	44	48	52	56	<u>60</u>	64		
380								43	47	51	55	59	<u>64</u>	68		
400										54	59	63	<u>68</u>	73		

$MBF \text{ Scribner/acre} = -1232.6954 + 1.4756175 \cdot BAHT + 0.000012382661 \cdot BAHT \cdot BAHT$
 Where: BAHT = Average stand basal area in square feet/acre \times average stand height in feet.
 Standard error of estimate: 1.863 MBF/acre.
 Values underlined indicate extent of data.

Table 3.—Aspen stand volumes in gross merchantable cubic meters per hectare for even-aged aspen in Colorado and southern Wyoming. Includes stems greater than 10cm d.b.h, which have a minimum top d.i.b. of 10cm. Stump height 0.3m.

Basal area (m ² /ha)	Average stand height (meters)													
	6	8	10	12	14	16	18	20	22	24	26	28	30	32
2	0	0	0	0	2									
4	0	<u>3</u>	<u>6</u>	<u>9</u>	<u>13</u>									
6	5	<u>9</u>	<u>14</u>	19	23	28								
8	9	<u>16</u>	<u>22</u>	28	34	40								
10	14	<u>22</u>	<u>30</u>	<u>37</u>	45	53	61							
12	19	<u>28</u>	<u>37</u>	<u>47</u>	56	65	75	84						
14	23	<u>34</u>	<u>45</u>	<u>56</u>	67	78	<u>89</u>	99						
16	28	<u>40</u>	<u>53</u>	<u>65</u>	78	<u>90</u>	103	115						
18		<u>47</u>	<u>61</u>	<u>75</u>	<u>89</u>	103	116	130						
20		53	<u>68</u>	<u>84</u>	<u>99</u>	115	130	146	161					
22		59	<u>76</u>	<u>93</u>	<u>110</u>	127	144	161	179					
24		65	<u>84</u>	<u>103</u>	<u>121</u>	140	158	177	196	214				
26		71	<u>92</u>	<u>112</u>	<u>132</u>	<u>152</u>	172	<u>193</u>	213	233				
28		78	<u>99</u>	<u>121</u>	<u>143</u>	<u>165</u>	<u>186</u>	<u>208</u>	230	251				
30		84	<u>107</u>	<u>130</u>	<u>154</u>	<u>177</u>	<u>200</u>	<u>224</u>	<u>247</u>	270	293			
32		90	<u>115</u>	<u>140</u>	<u>165</u>	<u>189</u>	<u>214</u>	<u>239</u>	<u>264</u>	<u>289</u>	314	338		
34		96	<u>123</u>	<u>149</u>	<u>175</u>	<u>202</u>	<u>228</u>	<u>255</u>	<u>281</u>	<u>307</u>	334	360		
36		103	<u>130</u>	<u>158</u>	<u>186</u>	<u>214</u>	<u>242</u>	<u>270</u>	<u>298</u>	326	354	382	410	
38		109	<u>138</u>	<u>168</u>	<u>197</u>	<u>227</u>	<u>256</u>	<u>286</u>	<u>315</u>	345	374	404	433	
40			<u>146</u>	<u>177</u>	<u>208</u>	<u>239</u>	<u>270</u>	<u>301</u>	<u>332</u>	<u>363</u>	394	425	<u>456</u>	
42			<u>154</u>	<u>186</u>	<u>219</u>	<u>251</u>	<u>284</u>	<u>317</u>	<u>349</u>	<u>382</u>	<u>414</u>	447	480	
44			<u>161</u>	<u>196</u>	<u>230</u>	<u>264</u>	<u>298</u>	<u>332</u>	<u>366</u>	<u>400</u>	<u>435</u>	469	503	
46				<u>205</u>	<u>241</u>	<u>276</u>	<u>312</u>	<u>348</u>	<u>383</u>	<u>419</u>	<u>455</u>	<u>490</u>	<u>526</u>	
48				<u>214</u>	<u>251</u>	<u>289</u>	<u>326</u>	<u>363</u>	<u>400</u>	<u>438</u>	<u>475</u>	512	549	
50				<u>224</u>	<u>262</u>	<u>301</u>	<u>340</u>	<u>379</u>	<u>417</u>	<u>456</u>	<u>495</u>	534	573	
52					<u>273</u>	<u>314</u>	<u>354</u>	<u>394</u>	<u>435</u>	<u>475</u>	<u>515</u>	556	596	
54					<u>284</u>	<u>326</u>	<u>368</u>	<u>410</u>	<u>452</u>	<u>494</u>	<u>535</u>	577	619	
56					<u>295</u>	<u>338</u>	<u>382</u>	<u>425</u>	<u>469</u>	<u>512</u>	<u>556</u>	599	642	
58					<u>306</u>	<u>351</u>	<u>396</u>	<u>441</u>	<u>486</u>	531	576	621	666	
60					<u>317</u>	<u>363</u>	<u>410</u>	<u>456</u>	<u>503</u>	549	596	642	689	
62					<u>327</u>	<u>376</u>	<u>424</u>	<u>472</u>	<u>520</u>	568	<u>616</u>	664	712	
64						<u>388</u>	<u>438</u>	<u>487</u>	<u>537</u>	587	<u>636</u>	<u>686</u>	736	
66						<u>400</u>	<u>452</u>	<u>503</u>	<u>554</u>	605	<u>656</u>	<u>708</u>	<u>759</u>	
68						<u>413</u>	<u>466</u>	<u>518</u>	<u>571</u>	624	<u>677</u>	<u>729</u>	<u>782</u>	
70						<u>425</u>	<u>480</u>	<u>534</u>	<u>588</u>	<u>642</u>	697	<u>751</u>	<u>805</u>	
72						<u>438</u>	<u>494</u>	<u>549</u>	<u>605</u>	661	<u>717</u>	<u>773</u>	<u>829</u>	
74						<u>450</u>	<u>507</u>	<u>565</u>	<u>622</u>	<u>680</u>	737	<u>795</u>	<u>852</u>	
76						<u>462</u>	<u>521</u>	<u>580</u>	<u>639</u>	<u>698</u>	<u>757</u>	<u>816</u>	<u>875</u>	
78						<u>475</u>	<u>535</u>	<u>596</u>	<u>656</u>	<u>717</u>	<u>777</u>	<u>838</u>	<u>898</u>	
80						<u>487</u>	<u>549</u>	<u>611</u>	<u>674</u>	<u>736</u>	<u>798</u>	<u>860</u>	<u>922</u>	
82							<u>563</u>	<u>627</u>	<u>691</u>	<u>754</u>	<u>818</u>	<u>881</u>		
84							<u>577</u>	<u>642</u>	<u>708</u>	<u>773</u>	<u>838</u>	<u>903</u>		
86								<u>658</u>	<u>725</u>	<u>791</u>	<u>858</u>	<u>925</u>		
88									<u>742</u>	<u>810</u>	<u>878</u>			
90									<u>759</u>	<u>829</u>	<u>898</u>			
92									<u>776</u>	<u>847</u>	<u>919</u>			
94									<u>793</u>	<u>866</u>				
96									<u>810</u>	<u>885</u>				
98										<u>903</u>				
100										<u>922</u>				

$Cubic\ meters/hectare = 0.38791 * MBA * MHT - 9.21137$

Where: MBA = Average stand basal area in square meters/hectare and: MHT = Average stand height in meters.

Standard error of estimate: 1.47 cubic meters/hectare.

Values underlined indicate extent of data.