

A deep learning approach to non-linearity in wearable stretch sensors

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2 ABSTRACT

3

4 There is a growing need for flexible stretch sensors to monitor real time stress and strain in
5 wearable technology. However, developing stretch sensors with linear responses is difficult due
6 to viscoelastic and strain rate dependent effects. Instead of trying to engineer the perfect linear
7 sensor we take a deep learning approach which can cope with non-linearity and yet still deliver
8 reliable results. We present a general method for calibrating highly hysteretic resistive stretch
9 sensors. We show results for textile and elastomeric stretch sensors however we believe the
10 method is directly applicable to any physical choice of sensor material and fabrication, and easily
11 adaptable to other sensing methods, such as those based on capacitance. Our algorithm does
12 not require any a priori knowledge of the physical attributes or geometry of the sensor to be
13 calibrated, which is a key advantage as stretchable sensors are generally applicable to highly
14 complex geometries with integrated electronics requiring bespoke manufacture. The method
15 involves three-stages. The first stage requires a calibration step in which the strain of the sensor
16 material is measured using a webcam while the electrical response is measured via a set of
17 arduino-based electronics. During this data collection stage, the strain is applied manually by
18 pulling the sensor over a range of strains and strain rates corresponding to the realistic in-use
19 strain and strain rates. The correlated data between electrical resistance and measured strain
20 and strain rate are stored. In the second stage the data is passed to a Long Short Term Memory
21 Neural Network (LSTM) which is trained using part of the data set. The ability of the LSTM to
22 predict the strain state given a stream of unseen electrical resistance data is then assessed
23 and the maximum errors established. In the third stage the sensor is removed from the webcam
24 calibration set-up and embedded in the wearable application where the live stream of electrical
25 resistance is the only measure of strain - this corresponds to the proposed use case. Highly
26 accurate stretch topology mapping is achieved for the three commercially available flexible sensor
27 materials tested.

28 **Keywords:** sensors, real-time, flexible, deep learning, Long Short Term Memory Neural Network

INTRODUCTION

29 Measuring real time stress and strain in wearable technology is a key requirement because this information
30 is required to monitor the recovery of a shoulder operation through the wearing of a therapeutic garment, or
31 the stretch of a hamstring of an athlete during training, or to protect the vulnerable skin of those who wear
32 prosthetics or orthotics (de la Fuente et al., 2000; Howe and Sherwood, 2009). On the face of it measuring
33 stretch should be relatively easy, especially because basic stretch sensors have been around for a long time.
34 However the non-linearity and strain rate dependent hysteresis of high strain flexible sensors have proved
35 difficult issues to solve (Amjadi et al., 2016; Noh, 2016; Seshadri et al., 2016).

36 In this paper we recognise that developing stretch sensors with linear responses is difficult and that
37 viscoelastic effects and strain rate effects are often unavoidable. Instead of trying to engineer the perfect
38 linear sensor we take a different approach. We present a deep learning method that can learn the peculiarities
39 of the non-linearity of cheap and easy-to-make sensors, while still giving reliable and robust strain data.
40 This way we can offset the disadvantages of some types of sensors, while maintaining their advantageous
41 simplicity in other areas. The method is entirely general and we believe it can be used with any flexible
42 stretch sensor.

43 We take a three-stage approach to developing a wearable sensor. The first stage involves a calibration
44 step in where the strain of a sensor is measured using a webcam while the electrical response is measured
45 via a set of arduino-based electronics. This data collection stage is designed to heed clinical advice that
46 strains applied manually, over a range of strains and strain rates, mimics the real use cases of wearables
47 which will always involve highly varying strain rates. This is the reason we did not use mechanically driven
48 stretching methods for data collection. The correlated data between electrical resistance, measured strain
49 and strain rate are stored, see Figure 1.

50 In the second stage, the data is passed to a Long Short Term Memory Neural Network (LSTM) which
51 is trained using part of the data set. The ability of the LSTM to predict the strain state given a stream of
52 unseen electrical resistance data is then assessed, see Figure 1.

53 In the third stage, the sensor is removed from the webcam calibration set-up and embedded in the
54 wearable technology where the live stream of electrical resistance is the only measure of strain - this
55 corresponds to the proposed use case. We are currently developing the approach to deal with stress and
56 pressure sensors, as well as 2D shear sensors but as proof of principle we have focused on 1D stretch
57 sensors in this paper. Nevertheless there are numerous applications where the measurement of linear 1D
58 stretch is desired, but not currently available to practitioners. For example in the fitting of orthotic and
59 prosthetic liners where the information on the expansion and expansion rate greatly affect comfort and
60 skin health, as shown in Figure 1. Here, In these cases multiple 1D sensors can combine to give important
61 information. More commonly, simple body tracking is required, such as the tracking of position of the arm,
62 this could be done with a linear stretch sensor placed on the elbow, as if the material used is sufficiently
63 thin, then change in resistance due to bending is negligible.

64 We used this procedure to investigate three different commercially available flexible sensor materials,
65 Medtex P130+B and Technitex P130+B both from Statex Produktions & Vertriebs GmbH, and Adafruit
66 Conductive Rubber Adafruit Industries. We show that in each case our deep learning approach provides
67 robust strain information with smaller errors than other methods.

BACKGROUND

68 There is a large body of research carried out to produce new flexible sensors, these fall broadly into two
69 categories, resistive and capacitive sensors.

70 Capacitive Strain Sensing

71 Capacitive stretch sensors are typically fabricated by sandwiching a dielectric between two electrode
72 layers, all of which need to be stretchable. The impedance is measured by analysing the response variable
73 signal frequency, and from this the capacitance is estimated without needing to have any information about
74 the resistance change in the conductive electrode layers. The advantage of capacitive flexible sensors is their
75 linearity and high sensitivity. However they tend to have low gauge factors and because of their layered
76 structure are more complex to fabricate. Nevertheless capacitive sensors have been successfully made
77 using conductive silicone for measuring pressure and shear stresses simultaneously at the stump-socket
78 interface of lower-limb amputees (Laszczak et al., 2015, 2016). Conductive fabrics have been used by
79 Tairyach et al. (Andreas Tairyach, 2017) to create multiple capacitive stretch sensors requiring only one
80 channel for measurement; Atalay et al. (Atalay et al., 2017) used conductive stretch fabric as the electrodes
81 sandwiching a silicone dielectric for a customizable strain sensor for human motion tracking; Kappel et al.
82 (Kappel et al., 2012) developed a strain sensor based on a dielectric electro-active polymer (DEAP) that acts
83 as an elastic capacitive material, strainable in one direction for measuring in-shoe navicular drop during
84 gait; Zens et al. (Zens et al., 2015) used a complex layering of non-conductive PDMS and conductive
85 PDMS made using carbon black particles as a novel approach to dynamic knee laxity measurement (Zens
86 et al., 2015); Fassler et al. (Fassler and Majidi, 2013) produced soft-matter capacitors and inductors from
87 microchannels of liquid-phase gallium–indium–tin alloy (galinstan) embedded in Ecoflex® 00-30.

88 Resistive Strain Sensing

89 The advantage of resistive flexible sensors are their relative simplicity and stability for large strain in
90 excess of 100%, however they tend to be highly non-linear and hysteretic, the two most common complex
91 behaviours being relaxation time and the resistance spikes associated with fast changes in strain rate
92 (Tiwana et al., 2012). There are two major mechanisms by which piezoresistive behaviour useful for stretch
93 sensing is achieved. These are: (1) by doping an elastomer matrix with a conductive filler of some kind
94 - this is primarily a nanoscale effect; and (2) by constructing a conductive pathway which undergoes a
95 significant geometrical change under stretch that the resistance also changes - this is primarily a macroscale
96 effect.

97 For the first type, a polymer with low Young's modulus, such as PDMS, rubber or silicone is used as a
98 matrix and a conductive filler such as metal nanoparticles or carbon allotropes. When the ratio of filler to
99 matrix content is above the percolation threshold, the composite material will conduct electricity. When the
100 material is stretched, this increases the gaps of insulating matrix between adjacent conductive particles
101 reducing the number of possible electron tunneling pathways, thus increasing the electrical resistance.
102 There many ways to fabricate such as materials, for example Boland et al. (Boland et al., 2014) describe a
103 simple method to infuse liquid-exfoliated graphene into natural rubber to create conducting composites,
104 displaying 10^4 -fold increases in resistance and working at strains exceeding 800%; Ferreira et al. (Ferreira
105 et al., 2017) report a carbon nanotube (CNT) and PVDF composite capable of measuring the interface
106 pressure within prosthetic stump/sockets; Watthanawisuth et al. (Watthanawisuth et al., 2015) report a
107 novel sensor using a 3D-Graphene foam amalgam with PDMS; Lee et al. (Lee et al., 2015) report a sensor
108 from highly stretchable conductive fiber composed of silver nanowires (AgNWs) and silver nanoparticles

109 (AgNPs) embedded in a styrene–butadiene–styrene (SBS) elastomeric matrix capable of 900% strain;
 110 Larimi et al achieved 350% strain with a low cost sensor fabricated by infusing graphene nano-flakes into
 111 a rubber-like adhesive pad (Larimia et al., 2018). This is similar to the commercially available Adafruit
 112 Conductive Rubber sensor Adafruit Industries we tested in this work.

113 For the second type of piezoresistive sensor, a geometrical change is achieved in a conductive material.
 114 This can be a simple change as in a highly conductive liquid in a fluidic channel whose length increases
 115 and cross-sectional area decreases, or it can be a much more complex change, such as the change in the
 116 conductive pathways of a stretchable fabric. In the latter case, as the textile is stretched and relaxed, different
 117 parts of the weave come into contact with each other, making discrete pathway changes on the scale of the
 118 weft and weave. There many ways to fabricate such as materials, for example Chossat et al. (Chossat et al.,
 119 2015) describe a complex microchannel network with a room temperature ionic liquid (RTIL); Menguc
 120 et al. (Mengüç et al., 2014) made Ga-In based fluidic strain sensors, but refined their design with the use
 121 of discretized stiffness gradients to improve mechanical durability; Michaud et al.(Michaud et al., 2015).
 122 combine thin gold films on silicone which display large reversible change in electrical resistance upon
 123 stretching, with eutectic liquid metal conductors to maintain bulk metal conductivity, even upon extensive
 124 elongation; Smart fabric sensors (Castano and Flatau, 2014); and smart textiles (Nejad et al., 2017) similar
 125 to the commercially available Medtex P130+B and Techniktex P130+B Statex Produktions & Vertriebs
 126 GmbH we tested in this work.

METHODS

127 Dynamic Electrical Resistance Measurement of the Stretch Sensors

128 The electrical resistance of each strain sensor was measured using an analogue signal processing (ASP)
 129 circuit which consists of a voltage divider, operational amplifier, filtering and an ADC as shown in Figure 2.
 130 After digitalisation, the signal undergoes digital signal processing (DSP) which consists of an oversampling
 131 routine onboard the Arduino, serial communication via USB to laptop, where it goes through a 5th Order
 132 Butterworth filter. This creates a data stream of filtered resistance and its gradient. These values are the
 133 inputs to the neural network described in the LSTM section. The values of the resistors and capacitors
 134 used in the ASP were calculated to optimise the dynamic range, and reduce noise. These calculations are
 135 explained in the following sections.

136 ASP: Optimising Dynamic Range

137 The opposing resistor, R_s from Figure 2, for the voltage divider is chosen using the maximum and
 138 minimum resistance measured by a standard multimeter (these are not necessarily at the max and min
 139 stretch). R_s was then calculated using equation 1:

$$R_s = \sqrt{R_{max} \times R_{min}} \quad (1)$$

140 ASP: Gain and Offset

141 The analogue conditioning circuit is an inverting op amp configuration using an MCP3208 Chip. The
 142 inversion is irrelevant to the analysis of the signal in this application, but has advantages compared to the
 143 non-inverting configuration. In particular, the noise contribution is amplified equally with the signal, which
 144 is not true for the non-inverting case, in which it is amplified to a greater degree (Carter, 2002). R_1 , R_2 , R_3
 145 and R_4 from Figure 2 were calculated using equations 2 and 3. Initial values for R_2 and R_3 must be of the

146 same order of magnitude, and are chosen so to minimise the input resistance to the ADC, which must be
 147 kept below 1000Ω for the MCP3208. So that

$$R_1 = \frac{R_2}{|m|} \quad (2)$$

$$R_4 = \frac{bR_3R_1}{5(R_2 + R_1) - bR_1} \quad (3)$$

148 where $m = \frac{-5}{V_{rag}}$, $b = mV_{low}$. V_{rag} is the voltage range of the stretch sensor and optimised voltage
 149 divider measured through the ADC, and V_{low} is the lowest value in this range, with the assumption that m
 150 is negative, and b is positive. A more detailed description of this method can be found in Carter (2002).

151 ASP: Filtering

152 Frequencies higher than the sampling rate appear as lower frequencies when sampled, which can result in
 153 a variety of possible distortions to a voltage signal. To avoid such aliasing, frequencies contained in the
 154 signal must be below the Nyquist frequency, which is defined as half the sampling rate. This was achieved
 155 by implementing a second order unity gain Sallen-key low-pass filter, for which equation 4 dictated the
 156 choice of resistors and capacitors to achieve the required cut-off frequency.

$$f_{cut-off} = \frac{1}{2\pi\sqrt{R_5R_6C_1C_2}} \quad (4)$$

157 For the unity gain op amp used this was simplified as $R_5 = R_6 = 470\Omega$, and $C_1 = C_2 = 0.01\mu F$.

158 DSP: Oversampling

159 Oversampling was undertaken onboard the Arduino, so as not to take CPU power away from the laptop,
 160 slowing the intensive neural network processing. A useful property of the inverse relationship between
 161 sample rate and resolution, is that it holds true even above the physical resolution of the ADC, however
 162 the sample rate is reduced by averaging over multiple real samples, here we averaged over N_s samples,
 163 to maintain the required sample rate. This achieves a n bit increase with $N_s = 2^{2n}$. A reduction in noise
 164 power also resulted from this by a factor of $\frac{1}{N_s}$. In this work we use $N_s = 25$.

165 The frame rate of the camera is orders of magnitude lower than the sample rate of the ASP, so it governs
 166 the size of the data set we could produce, namely 30 frames per second. All digital processes had to be
 167 achieved within the $\frac{1}{30}$ of a second frame window, and for this reason the oversampling was performed
 168 on board the Arduino, as this could be performed in parallel to computations on the computer CPU. The
 169 resistance was filtered using the SciPy package, Version 0.19.1 was used for this study. The filters used were
 170 the `signal.butter()` and `signal.filtfilt()` functions. The gradient was measured using the `gradient()` function in
 171 the NumPy package, Version 1.15.0 was used for this study.

172 Measuring Strain in Real-Time

173 To measure real-time strain and resistance, each stretch sensor was positioned under a webcam connected
 174 to a laptop, see Figure 3. We used a standard Logitech C270 camera with a frame rate of 30 frames per
 175 second. For each experiment the webcam was positioned 50cm above the flexible sensor using a clamp

176 stand. The flexible sensor was connected electrically to the ASP circuit and red dot labels were placed on
 177 the electrode clamps of the flexible sensor. The flexible sensor was then stretched and unstretched manually
 178 at a range of strain rates (from 0 to 1 sec^{-1}). The computer vision package OpenCV (Version 3.3.0 was
 179 used for this study) running on the laptop was used to collect the images from the camera and automatically
 180 detect the red dots and their coordinates, which were used to compute the real-time strain. The strain was
 181 correlated with the resistance measurements to produce a data set as input for the LSTM.

182 Long Short Term Memory Neural Network (LSTM)

183 Long Short Term Memory networks are a special kind of Recurrent Neural Network (RNN) introduced
 184 by Hochreiter and Jürgen Schmidhuber (1997), which are capable of learning long-term dependencies,
 185 and have advantages over traditional RNNs, such as avoiding the vanishing gradient problem. Traditional
 186 RNNs map input sequences to outputs using the following recurrence equations:

$$h_t = g(W_{xh}x_t + U_{hh}h_{t-1} + b_h) \quad (5)$$

$$z_t = g(W_{hz}h_t + b_z) \quad (6)$$

187 where g is an element-wise non-linearity, e.g. sigmoid function or hyperbolic tangent, x_t is the input
 188 matrix at time t . h_t is the hidden state matrix which from equation 5 is a function of the input at the same
 189 time step (x_t), modified by a specific weight matrix W_{xh} , and the previous hidden state h_{t-1} modified by
 190 its own weight matrix U_{hh} . In equation 6 the output matrix z_t is determined by a similar process to give an
 191 output prediction.
 192

193 The weighted matrices act as filters to determine the importance of various inputs, and their elements
 194 along with the biases b_h and b_z are the parameters in the ‘deep learning’. The ‘deep’ indicates that there
 195 are multiple separate layers with additional hidden states like h_t whose role is to modify the output layer,
 196 see Figure 4. LSTMs build on this RNN framework by including memory cells comprising of three types
 197 of gates: (i) a Forget Gate, which conditionally decides what information to throw away; (ii) an Input
 198 Gate which conditionally decides which values from the input to update to the memory state; and (iii) an
 199 Output Gate, which conditionally decides what to output based on input and the memory state, see Figure
 200 5. Each cell is like a mini-state machine where the gates of the cells have weights that are learned during
 201 the training procedure. These cells are described mathematically by the following equations:

$$i_t = \sigma(W_{ix}x_t + U_{ih}h_{t-1} + b_i) \quad (7)$$

$$f_t = \sigma(W_{fx}x_t + U_{fh}h_{t-1} + b_f) \quad (8)$$

$$o_t = \sigma(W_{ox}x_t + U_{oh}h_{t-1} + b_o) \quad (9)$$

$$c_t = f_t \odot c_{t-1} + i_t \odot \tanh(W_{cx}x_t + U_{ch}h_{t-1} - 1 + b_c) \quad (10)$$

$$h_t = o_t \odot \tanh(c_t) \quad (11)$$

202 where \odot is the Hadamard product and i_t is the input gate (state at time t), f_t is the forget gate, o_t is the
 203 output gate, c_t is the cell state, and h_t is the hidden state analogous to that from the simpler RNN example.

204 A pictorial representation of this LSTM unit can be seen in Figure 5, where as in the simple RNN, the cell
205 is given the input matrix x_t and the previous time step's hidden state h_{t-1} . Here however, they are passed
206 through the three gates, each with separate modifying weight matrices, serving their separate functions,
207 before outputting the hidden state h_t . A more detailed description of LSTM architecture can be found in
208 Jozefowicz et al. (2015).

209

210 Our network architecture comprises 3 layers of 270 LSTM cells followed by a single linear layer which
211 maps the final recurrent layer to a single output via further weighted & biased matrix multiplication. The
212 architecture of this structure is shown in Figure 4 showing the input nodes, the layers of LSTM cells (each
213 one as shown in Figure 5), the output matrix, and the output node. The network size was set by comparing
214 varied architectures that were able to complete within 1/30 of a second (along with the other processing
215 requirements). This means that once the vision tracking is removed from the system, the sampling rate can
216 be set to match the 30 fps of the original data collection, preserving the accuracy of the predictions without
217 any time lag.

218 The weights and biases of the 4 network layers are trained by gradient descent using Adaptive Moment
219 Estimation that computes adaptive learning rates for each parameter (Kingma and Ba, 2014). The loss
220 function used in this method is assessed by calculating the root mean squared error (RMSE) of the set of
221 batch predictions vs the actual strain measurements tracked with the webcam.

222 Dropout, Noise, Processing and Implementation

223 Dropout is a recently introduced regularization method as described by Srivastava et al. (2014), which
224 has been very successively applied to standard feed-forward neural networks, but with less success when
225 applied to recurrent networks. Dropout entails probabilistically excluding a given proportion of the input
226 and internal connections from activation and weight updates while training the network. Our approach
227 follows the method suggested by Zaremba et al. (2014) for applying it to LSTM networks, which in short,
228 only applies it to all non-recurrent connections in the cell structure.

229 LSTM networks produce better results on larger datasets and many training steps. In order to train them
230 effectively using small datasets, we create more data for it to use, by adding symmetric noise to the inputs
231 and continuing training. With this larger augmented dataset, a much greater number of useful training steps
232 are possible. It also serves as an effective regularisation method, reducing overfitting of the network, which
233 is a primary concern for all networks, particularly those with smaller datasets.

234 A Butterworth filter is used with a cut-off frequency dictated by the highest measured frequency present
235 in the vision data. This enables usable predictions to be achieved even when the neural network is not able
236 to reduce its loss function to a low enough value to produce stable outputs. In general, the raw network
237 output is noisy, however after filtering, shows excellent calibration correlation.

238 This method was implemented using the Tensorflow package, Version 1.8 was used for this study, on a
239 Toshiba Tecra laptop running an Arch based linux operating system.

240 Materials

241 We tested three commercially available stretch sensor materials with our method, these were Medtex
242 P130+B and Techniktex P130+B both from Statex Produktions & Vertriebs GmbH, and Adafruit Conductive
243 Rubber Adafruit Industries.

244 Medtex P130+B

245 Medtex P130+B is a commercially available stretch nylon, interweaved with silver, aimed at medical
246 dressings due to the anti-bacterial properties of silver. It is also used to construct stretchable conductive
247 circuits and basic stretch sensors. Compared to solid rubber-like materials, it has a much smaller relaxation
248 time than some material options, yet does display some additional complex resistive behaviour which
249 makes more precise use more difficult.

250 A 15cm sized strip of the Medtex P130+B fabric was cut and placed in metal clamps attached to the ASP
251 circuit. The maximum and minimum resistance values were measured as 41Ω and 153Ω . Using Equation
252 1, the optimum resistance value was found to be 79.2Ω , therefore a 75Ω resistor was used for R_s , as this
253 was the closest single standard value available. The sensor was then stretched to find the operating range
254 of this set-up, which was found to be $1.52V - 2.79V$, a span of $1.27V$. The required gain was calculated
255 to be $-3.94V/V$, with an off-set of $5.99V$. Using equations 2 and 3 the resistor values were calculated
256 to optimise the ASP circuit for this experiment and found to be: $R_1 = 130\Omega$, $R_2 = 510\Omega$, $R_3 = 510\Omega$,
257 $R_4 = 160\Omega$.

258 Techniktex P130+B

259 Techniktex P130+B is an advanced conductive fabric aimed at the wearable electronics market. It claims
260 to have homogeneous conductivity in all directions, and have more reliable and linear behaviour. It still
261 has an associated relaxation time, however it only increases resistance as it is stretched, unlike the Medtex
262 fabric.

263 A 15cm sized strip of the Techniktex fabric sample was cut and placed in metal clamps attached to
264 the ASP circuit. The maximum and minimum resistance values were measured as 16Ω and 28Ω . Using
265 Equation 1, the optimum resistance value was found to be 21.2Ω , therefore a 22Ω resistor was used, as this
266 was the closest single standard value available. The sensor was then stretched to find the operating range of
267 this set-up, which was $1.95V - 2.45V$, a span of $0.5V$. The required gain was calculated to be $-10V/V$,
268 with an off-set of $11V$. Using equations 2 and 3 the resistor values were calculated to optimise the ASP
269 circuit for this experiment and found to be: $R_1 = 51\Omega$, $R_2 = 510\Omega$, $R_3 = 510\Omega$, $R_4 = 120\Omega$.

270 Adafruit Conductive Rubber

271 The Adafruit conductive rubber comes in an 3mm diameter extruded cord, a 15cm sized length was
272 placed in metal clamps attached to the ASP circuit. The maximum and minimum resistance values were
273 measured as $1.18k\Omega$ and $2.6k\Omega$. Using Equation 1, the optimum resistance value was found to be $1.75k\Omega$,
274 therefore a $22k\Omega$ resistor was used, as this was the closest single standard value available. The sensor was
275 then stretched to find the operating range of this set-up, which was $2V - 2.6V$, a span of $0.6V$. The required
276 gain was calculated to be $-8.3V/V$, with an off-set of 16.7 . Using equations 2 and 3 the resistor values
277 were calculated to optimise the ASP circuit for this experiment and found to be: $R_1 = 62\Omega$, $R_2 = 510\Omega$,
278 $R_3 = 510\Omega$, $R_4 = 330\Omega$.

RESULTS

279 For each of the three stretch sensors the same experimental method was carried out. This comprised of
280 collecting data by manually pulling and releasing the sensors in a manner consistent with real usage ie. over
281 a period of many minutes and with a range of strain rates. For each material some of the correlated sets of
282 measured strain from the webcam and measured electrical resistance were used to train the neural network.

283 Subsequently the neural network was used to predict the strain when only supplied with unseen electrical
284 resistance data which was then compared with the unseen measured strain and the errors computed. The
285 results are as follows.

286 **Medtex P130+B**

287 The sensor was manually stretched and relaxed for ~ 15 minutes under the webcam, producing ~ 27500
288 correlations of measured sensor length vs measured electrical resistance. The data was pre-processed to
289 produce a set of filtered resistance and unfiltered resistance gradients, matched against values of strain. The
290 complex nature of this data can be seen in Figure 6(a) where three stretch and relax cycles for the sensor
291 with three different strain rates (depicted in red, blue and green) produced very different functional forms
292 (the grey line shows all the data). Figure 6(b) shows the measured strain correlated with the measured
293 electrical resistance showing that the strain rates were different in each case and varied in a realistic i.e.
294 non-linear manner. The strain rates are quantified in Figure 6(c) which shows the characteristic spikes
295 which are typical of such flexible stretch sensors. The rate of change of resistance for each case is shown in
296 Figure 6(d) which was used as an input for the LSTM neural network.

297 This dataset was used to train our LSTM architecture for ~ 17 hours following an automated training
298 schedule. The correlation between measured strain and resistance of the training data set can be seen in
299 Figure 7(a). Figure 7(b) shows the correlation between measured and predicted strain in the final trained
300 network. The Mean Absolute Error (MAE) between prediction and measured was 11.38% total strain,
301 and the error distribution can be seen in Figure 7(c). The correlation was calculated using the Pearson
302 Product-Moment Correlation.

303 Figure 8 (a) shows some of the unseen test data that correlates measured resistance with measured strain.
304 Using only unseen resistance data and the resistance gradient data as inputs for the trained LSTM resulted
305 in predicted strains of the flexible sensor with an MAE of 19.29% strain. Figure 8(b) shows the comparison
306 between predicted and measured. The error distribution can be seen in Figure 8(c), which did show some
307 errors up to 65%. The correlation of predicted vs. actual for the test set was 0.80, and increase of 0.23
308 compared to the correlation of raw resistance vs actual, which was 0.67. This shows a significant increase
309 in linearity of the system.

310 **Techniktex P130+B**

311 The sensor was manually stretched and relaxed for ~ 15 minutes under the webcam, producing ~ 27500
312 data points of correlations of measured sensor length vs measured electrical resistance. As with the Medtex
313 P130+B fabric, the complex nature of this data can be seen in can be seen in Figure 9(a) where three
314 stretch and relax cycles for the sensor with three different rates (depicted in red, blue and green) produced
315 very different functional forms. Figure 9(b) shows the output of the webcam correlated with the measured
316 electrical resistance in each case showing that the rates were different in each case as quantified in Figure
317 9(c). The rate of change of resistance for each case is shown in Figure 9(d) which was used as an input for
318 the LSTM neural network.

319 This dataset was used to train our LSTM architecture for around 17 hours following an automated training
320 schedule. The correlation between measured and resistance of the training data set can be seen in Figure
321 10(a). The resulting strain predictions can be seen in Figure 10(b), where the Mean Absolute Error (MAE)
322 was 6.64% total, and the error distribution can be seen in Figure 10(c).

323 Figure 11 (a) shows the unseen test data that correlates measured resistance with measured. Using only
324 the resistance data and the resistance gradient data as inputs for the trained LSTM resulted in predicted

	Medtex P130+B	Techniktex P130+B+B	Adafruit Rubber
Linear Regression Model			
<i>Training Set Prediction Error (MAE%)</i>	19.3	17.5	28.6
<i>Test Set Prediction Error (MAE%)</i>	24.8	19.3	30.6
5th Deg Polynomial Regression Model			
<i>Training Set Prediction Error (MAE%)</i>	18.9	17.2	27.0
<i>Test Set Prediction Error (MAE%)</i>	25.0	19.2	28.9
Deep Feedforward Neural Network			
<i>Training Set Prediction Error (MAE%)</i>	23.2	20.1	28.3
<i>Test Set Prediction Error (MAE%)</i>	25.1	21.3	32.1
Recurrent Neural Network			
<i>Training Set Prediction Error (MAE%)</i>	16.4	11.8	17.1
<i>Test Set Prediction Error (MAE%)</i>	22.1	14.2	18.3
LSTM Neural Network			
<i>Training Set Prediction Error (MAE%)</i>	11.4	6.64	13.8
<i>Test Set Prediction Error (MAE%)</i>	19.3	10.8	14.5

Table 1. Table of Results comparing different methods for calculating strain from the measured resistance value.

325 strain of the flexible sensor with an MAE of 10.75%. Figure 11(b) shows the comparison between predicted
 326 and measured. The error distribution can be seen in Figure 11(c), which did show some errors up to 50%.
 327 The correlation of predicted vs. actual for the test set was 0.94, an increase of 0.09 when compared to the
 328 correlation of raw resistance vs actual, which was 0.85.

329 **Adafruit Conductive Rubber**

330 The sensor was manually stretched and relaxed for ~15 minutes under the webcam, producing ~27500
 331 data points of vs resistance. This material behaved in a more regular manner than the other two materials
 332 when exposed to different rates as shown in Figure 12(a) where three stretch and relax cycles for the sensor
 333 with three different rates are depicted in red, blue and green. Figure 12(b) shows the output of the webcam
 334 which measured the that correlated with the measured electrical resistance in each case showing that the
 335 rates as quantified in Figure 12(c). The rate of change of resistance for each case is shown in Figure 12(d)
 336 which was used as an input for the LSTM neural network.

337 This dataset was used to train our LSTM architecture for around 13 hours following an automated training
 338 schedule until the error did not improve further. The correlation between measured and resistance of the
 339 training data set can be seen in Figure 12(a). The resulting predictions fitting the training data set can be
 340 seen in Figure 13(b), where the Mean Absolute Error (MAE) was 13.77% total , and the error distribution
 341 can be seen in Figure b 13(c).

342 Figure 14 (a) shows the unseen test data that correlates measured resistance with measured strain. Using
 343 only the resistance data and the resistance gradient data as inputs for the trained LSTM resulted in predicted
 344 strain of the flexible sensor with an MAE for the test set was 14.49 %. Figure 14(b) shows the comparison
 345 between predicted and measured. The error distribution can be seen in Figure 14(c), which did show some
 346 errors up to 40%. The correlation of predicted vs actual for the test set was 0.92, an increase of 0.32
 347 compared to the correlation of raw resistance vs actual, as the correlation was only 0.60 for this material - a
 348 highly significant increase.

	Medtex P130+B	Techniktex P130+B+B	Adafruit Rubber
No. of training examples	27500	27500	27500
No. of testing examples	5000	3200	5300
Raw Training Set Correlation	0.67	0.85	0.60
Training Set Prediction Correlation	0.95	0.98	0.93
Test Set Prediction Correlation	0.80	0.94	0.92
Training Set Prediction Error (MAE%)	11.38	6.64	13.77
Test Set Prediction Error (MAE%)	19.29	10.75	14.49

Table 2. Summary of results of the three commercially available stretch sensors used in this study.

349 Comparison with other Statistical Methods

350 To evaluate the effectiveness of our deep learning approach we tested four alternative methods for
 351 calculating strain from the sensor data. These were: a standard linear regression model (Schneider et al.,
 352 2010); a 5th degree polynomial regression model (Heiberger and Neuwirth, 2009); a deep feed-forward
 353 neural network (DNN) (Schmidhuber, 2015); and a traditional recurrent neural network (RNN) (Jain and
 354 Medsker, 2000). Both the network models have the same structure as our LSTM network, that of 3 layers of
 355 270 nodes. These were fitted to the training data from all three materials and tested on the unseen datasets,
 356 in the same manner as our LSTM method. The regression models were created using the SciPy package
 357 (Version 0.19.1), and the networks were created using the Keras package (Version 2.2.2).

358 We can see from Table 1 that the LSTM out-performs the simpler methods consistently for all three
 359 sensor types. The LSTM results show an average improvement of 10.0% error compared to the linear
 360 models, and an average improvement of 3.4% error on unseen test data compared to the simpler RNN. The
 361 linear and polynomial regression models perform poorly which is not surprising given the complexity of
 362 the non-linearity of the sensors. Although potentially capable of modelling much greater complexity, the
 363 DNN performs worse than the linear and polynomial regression methods, this is likely to be due to its
 364 single input/single output structure. As soon as some recurrence is added to the network architecture, as
 365 with the RNN and the LSTM, the results are greatly improved with a significant drop in error across all
 366 three materials, however generally a greater difference in error between the training data and the testing
 367 data is seen. This suggests that some overfitting is present, and that significant improvements can still be
 368 made in the future.

DISCUSSION

369 In general, wearable technology developers would prefer perfectly linear flexible sensors, however such
 370 sensors have historically been difficult to make hence our approach to use available commercial flexible
 371 sensors and use deep learning algorithms such as LSTMs to make them usable in wearable technology. To
 372 test our approach we used three commercially available flexible sensors all of which showed non-linearity
 373 and strain rate dependant electrical responses. The summary of our results in Table 2 shows that we can
 374 predict strain to between 10% and 20% error for three different sensor types. The origin of non-linearity and
 375 rate dependence in flexible sensors is different in each case, and hence they show very different behaviour.
 376 However there are some general principles which our selection of commercial sensors illustrate.

377 The fabric sensors have a macrostructure comprising of a warp and weft. In these sensors the conductive
 378 route through the material is via many different temporary mechanical connections which arise where
 379 the conductive fibres in the warp touch the weft and in doing so make another potential conductive path
 380 through the material. During stretch these local connections change both in number and area of contact, and

381 this changes the electrical resistance. The geometry of the fabric macrostructure during different stretch
382 does not scale linearly with extension and so it is not surprising that fabric sensors are non-linear in their
383 electrical response. Similarly on release their electrical properties are dependent on the way the individual
384 fibres unstretch and mechanically slide past each other. Although the topology of the warp and weft remains
385 in tact after stretch, at the microscale of the individual connective fibres, different mechanical connections
386 and adjacencies result once the fabric returns to its original length. Hence the return path of de-stressing
387 such a fabric is likely to be different. In addition the elastomer component of the fibres are viscoelastic and
388 so their mechanical response is highly sensitive to strain rate. The difference between the two fabrics arises
389 from thier intended use. Techniktex is designed with sensor applications in mind, having homogeneous
390 conductivity in all directions, and more reliable and linear behaviour. The Medtex is primarily aimed at
391 medical dressings, meaning that the homogeneity of the conductivity is not a major manufacturing concern.
392 All these factors taken together produce the highly non-linear and distinctly different behaviours seen in
393 our fabric sensors shown in Figure 6(a) and Figure 9(a).

394 The Adafruit conductive rubber sensor is comprised of a viscoelastic rubber material with carbon black
395 powder added. Here the electrical conduction arises from a percolation path of carbon particles in contact
396 with each other. During stretching the percolative path changes as particle contact changes. As with the
397 conductive fabrics the matrix elastomer is viscoelastic and so the combination of microscale contacts
398 changing with length with rate dependant restoration forces results in a high non-linear electrical response.
399 An interesting result arises with the conductive rubber as although the raw data has a much lower correlation
400 than the two fabrics, it achieves an impressive increase after training, although still with a larger overall
401 error than the Techniktex fabric. We speculate that this is due to the lack of macroscale structure (warp
402 and weft) in the rubber which allows the behaviour to be learnt much more affectively by the neural
403 network. This has some interesting implications for the inevitable use of deep learning with soft materials.
404 Previous to the very recent increase in use of learning algorithms, structure and complexity has been
405 focused on the physical geometries and structure, balanced against the human-limited ability to efficiently
406 produce applicable models. Now that the limits of applied models has changed, with a huge increase in
407 the complexity of non-human designed models of correlating input to output without the need for the
408 intermediary steps to be established in full, the way we approach our use of materials may change. If the
409 most powerful element in a system is its own learning capability, then physical design may begin to change
410 in accordance. We find here that comparable results are possible with the simplest of physical approaches
411 compared to a highly refined composite textile structure.

412 The training time of the LSTM on our system, which comprised of a simple low-spec PC, was of the
413 order of 10-20 hours, but this could be reduced significantly through software optimisation and the use
414 of faster machines. Nevertheless this amounts to a calibration process which only needs to be performed
415 once. The more stringent criterion for real use application requires the trained LSTM to give real time
416 high resolution values of stretch, and this requires a portable resistance measurement circuit and a portable
417 computation unit to run the LSTM, as illustrated in Figure 1. We estimate the requirement for these would
418 be entirely feasible.

419 There are many advantages of a deep learning approach to calibration that have not been applied here. A
420 major avenue which we will investigate in the future is ‘transfer learning’, where pre-trained models are
421 applied to new datasets, either for direct inference, or for reductions in training time. For our application,
422 this would be expected to be useful for different geometries of the same or similar materials. Another
423 advantage of using this approach concerns wear and damage of sensors. With additional new datasets,
424 an original trained system might be able to adjust itself to damage, thereby prolonging the usefulness

425 of sensors that generally require considerable manual construction. For instance (Graves et al., 2005)
426 have shown LSTM networks are able to re-train rapidly to adapt to new subsets of data achieving greater
427 accuracy than when trained from scratch.

CONCLUSION

428 We have developed a deep learning method for calibrating highly hysteretic resistive stretch sensors.
429 We show that technique gives reliable robust strain information for commercially available textile and
430 elastomeric stretch sensors and requires no specialist equipment. Our LSTM model is more accurate than
431 four other statistical models tested, as shown by consistent significantly lower errors on unseen datasets.
432 Our method is open source and does not require any a priori knowledge of the physical attributes or
433 geometry of the sensor to be calibrated, which is a key advantage as stretchable sensors are generally
434 applicable to highly complex geometries with integrated electronics requiring bespoke manufacture.

CONFLICT OF INTEREST STATEMENT

435 The authors declare that the research was conducted in the absence of any commercial or financial
436 relationships that could be construed as a potential conflict of interest.

AUTHOR CONTRIBUTIONS

437 BO, PS and MM conceived the project. BO carried out the work; building and testing the prototype sensors
438 and the deep learning software. RJ helped with the building and testing the prototype sensors. MM and BO
439 analysed the data and wrote the paper.

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1 FIGURES

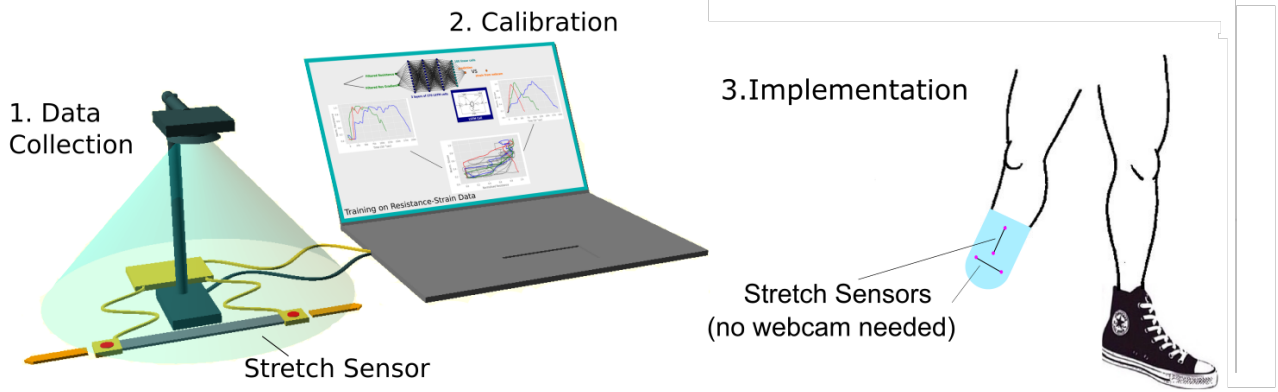


Figure 1. Overview of System showing our three-stage approach to developing a wearable sensor. The first stage involves a calibration step in which the sensor material is measured using a webcam while the electrical response is measured via a set of arduino-based electronics. In the second stage the data is passed to a Long Short Term Memory Neural Network which is trained using part of the data set. In the third stage the sensor is removed from the webcam calibration set-up and embedded in the wearable technology where the live stream of electrical resistance is the only measurement taken - this corresponds to the proposed use case.

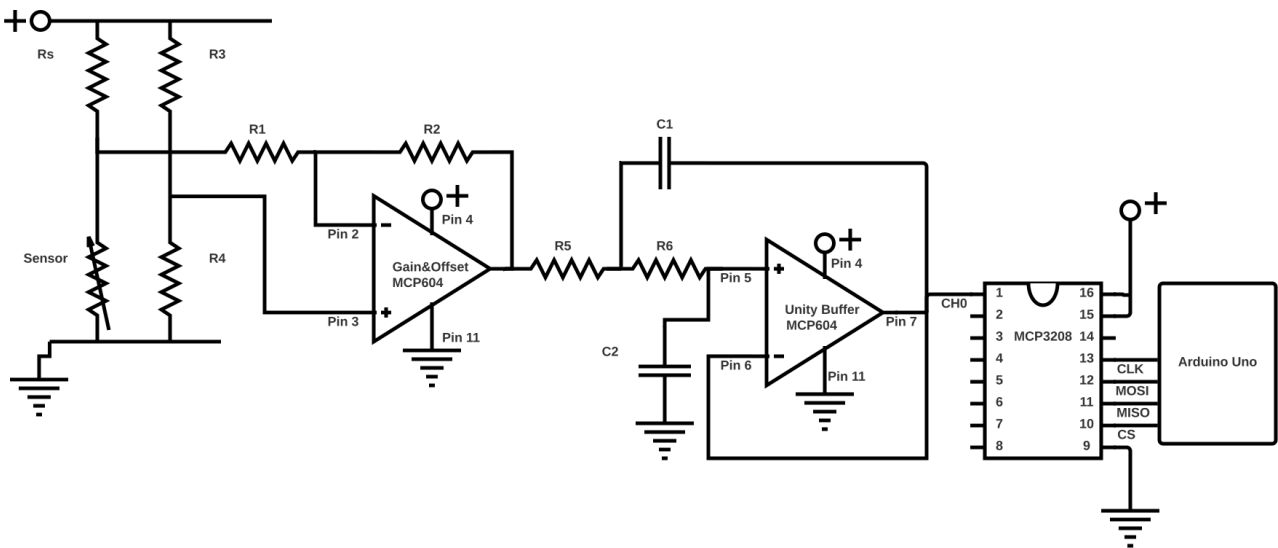


Figure 2. A diagram of the Analogue Signal Processing Circuit used in this work.

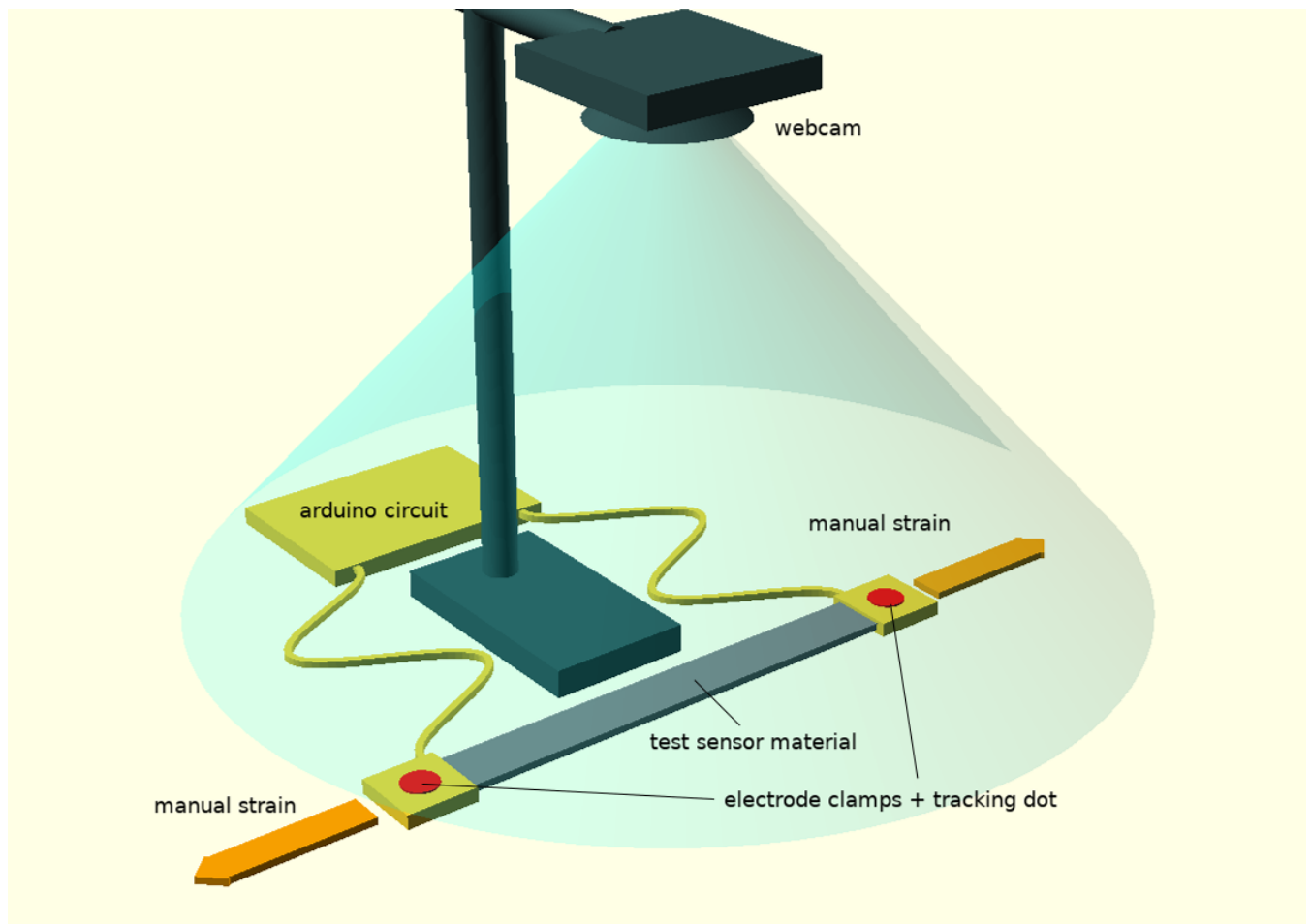


Figure 3. A diagram showing the experimental set-up for the calibration step in our process, which involves the use of a webcam to track dots in real-time on a flexible sensor to measure elongation, while arduino-based electronics is used to collect the correlated electrical data.

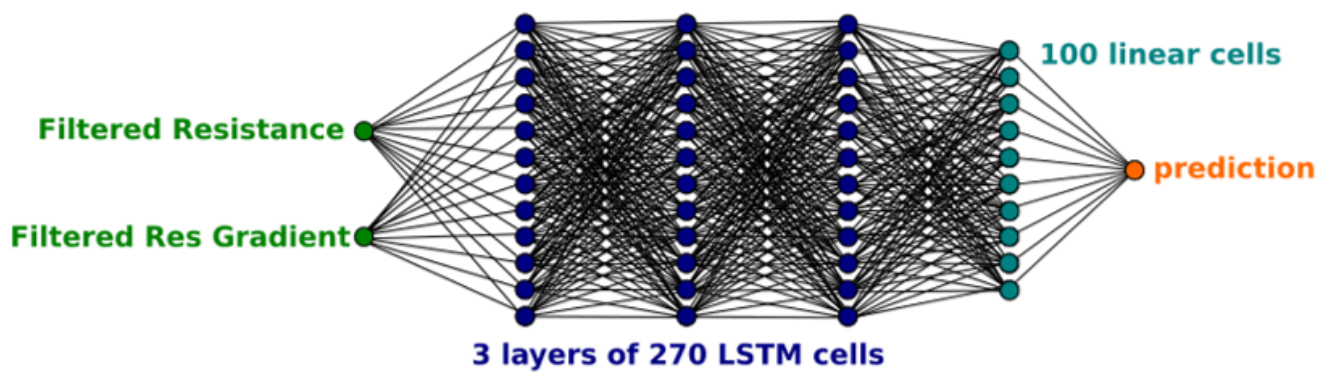


Figure 4. A diagram of the architecture of the neural network used.

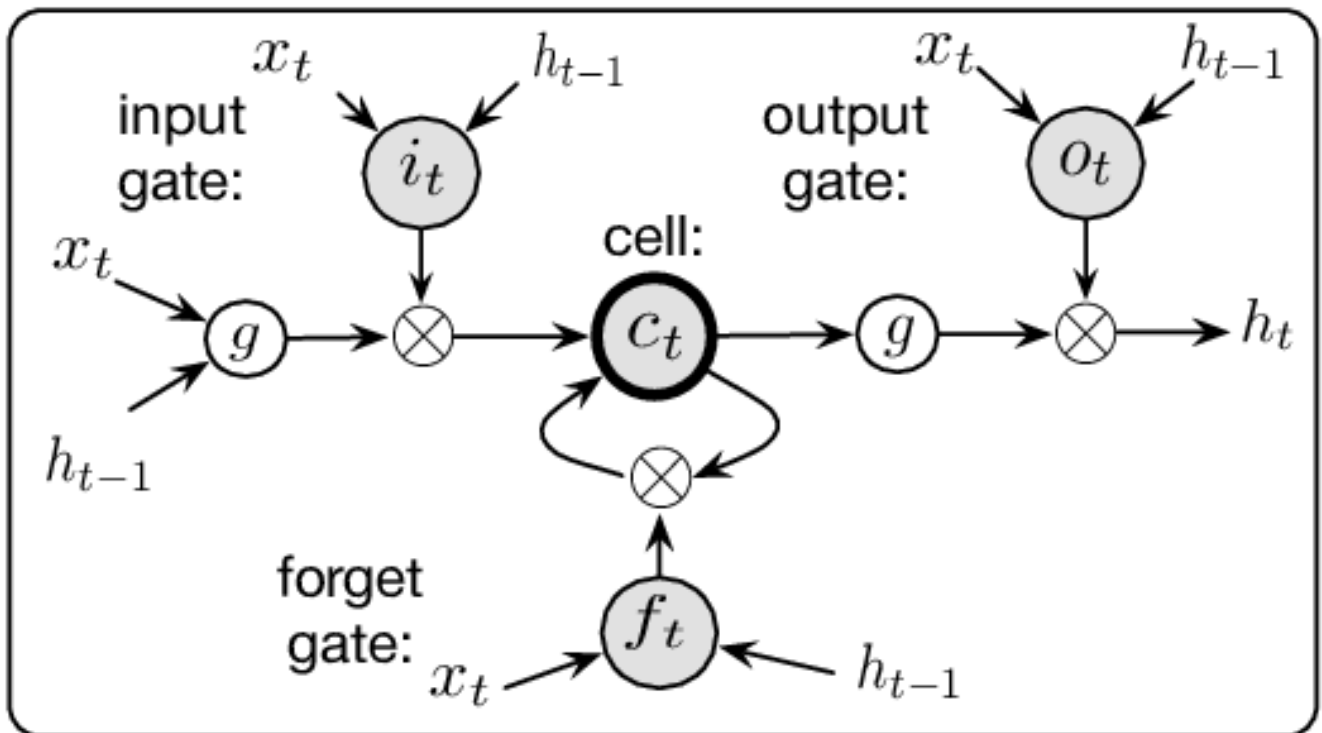


Figure 5. A pictorial representation of the LSTM cell used Chen and Wang (2017)

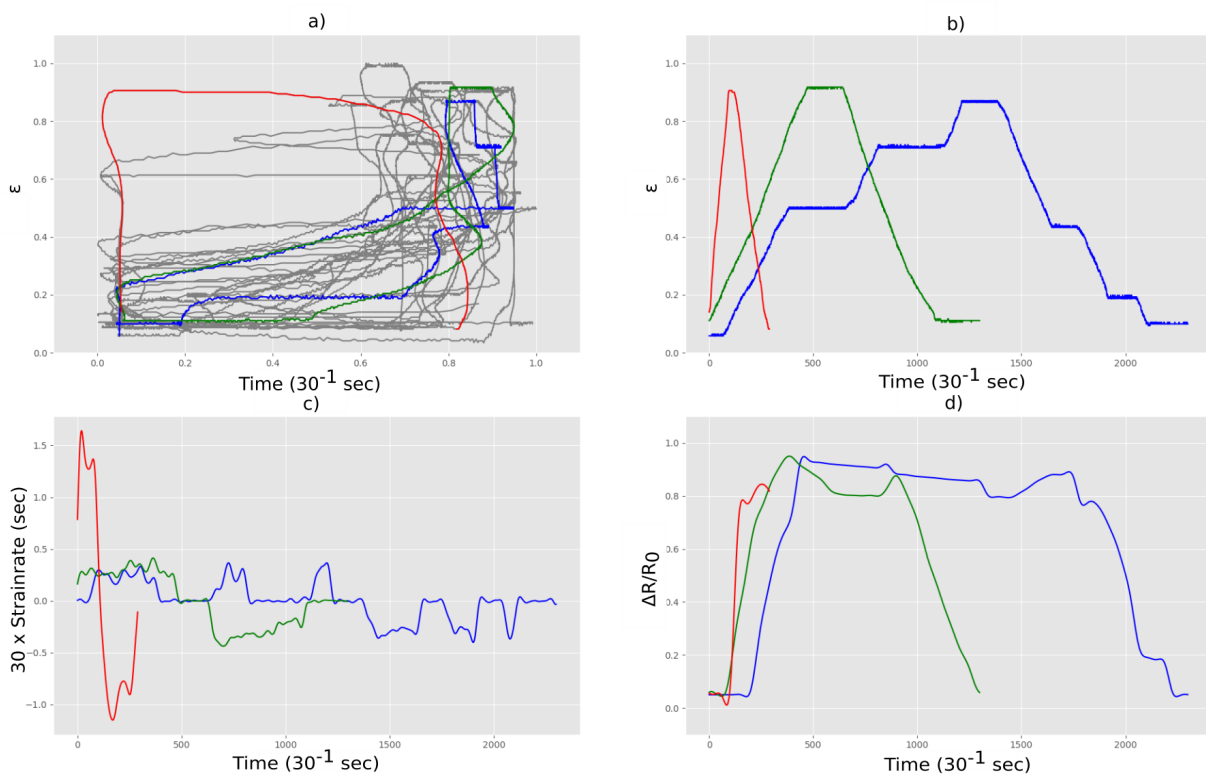


Figure 6. Strain & electrical resistance behaviour of the Medtex P130+B during stretching; (a) normalised strain versus normalised resistance; (b) normalised strain versus time; (c) strain rate versus time; (d) normalised resistance versus time

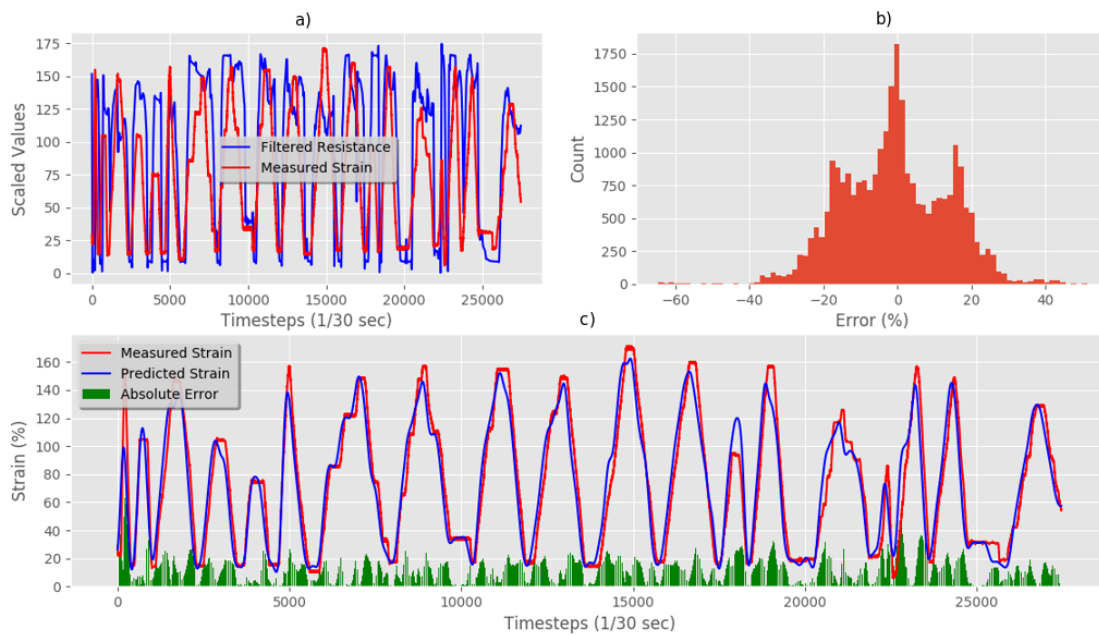


Figure 7. Medtex P130+B training data predictions and errors: (a) electrical resistance and correlated strain of training set versus time; (b) training set error distribution; (c) Measured strain versus predicted strain for training set.

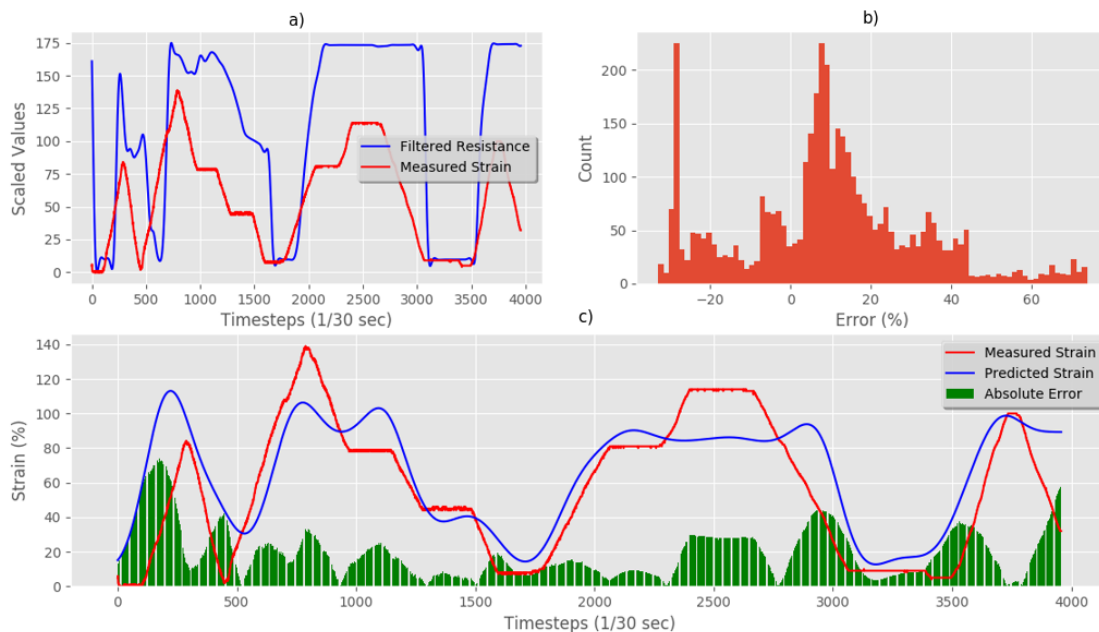


Figure 8. Medtex P130+B real-time test predictions and errors:(a) electrical resistance and correlated strain of unseen test set versus time; (b) unseen test set error distribution; (c) Measured strain versus predicted strain for unseen test set.

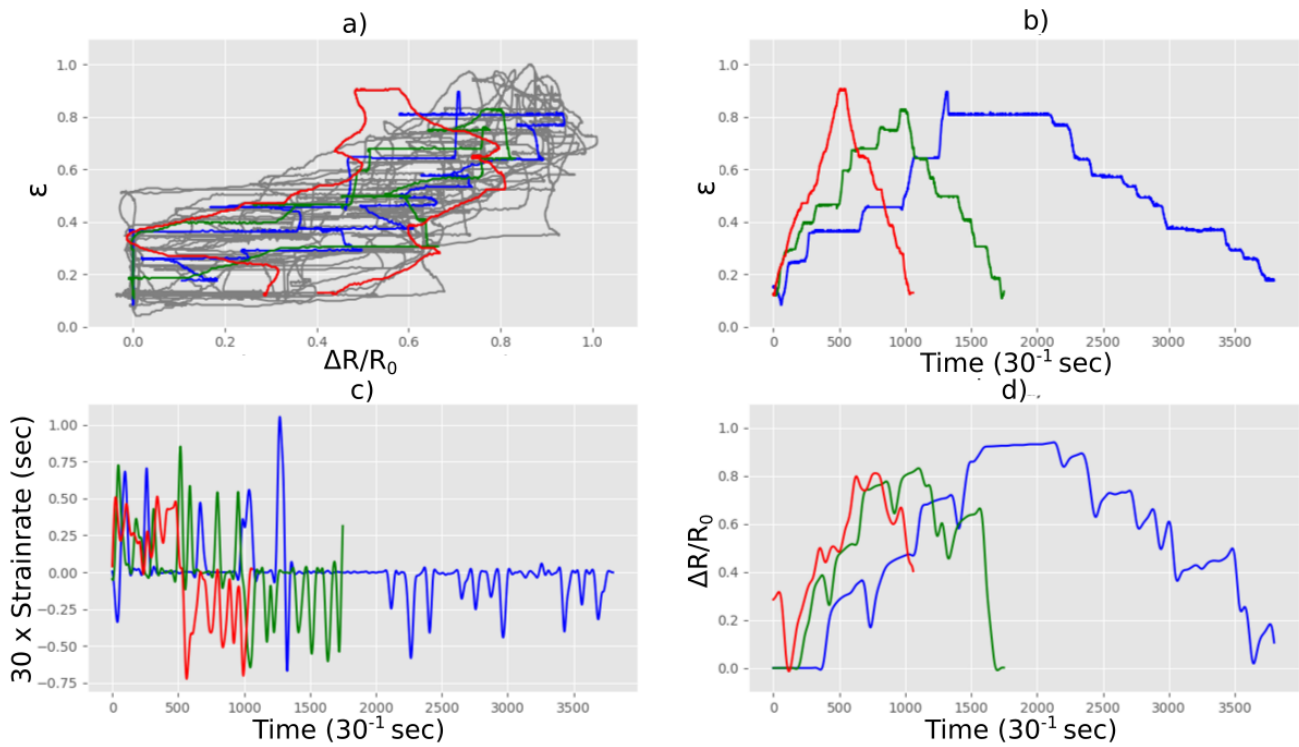


Figure 9. Strain & electrical resistance behaviour of the Techniktex P130+B during stretching; (a) normalised strain versus normalised resistance; (b) normalised strain versus time; (c) strain rate versus time; (d) normalised resistance versus time

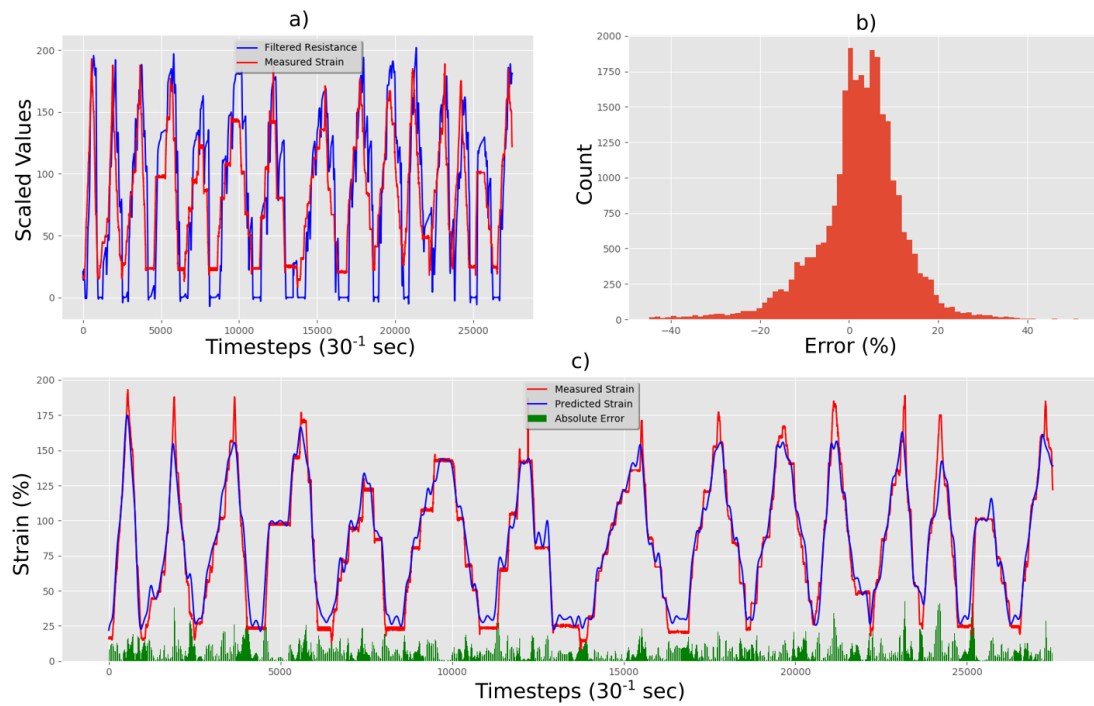


Figure 10. Technitex P130+B training data predictions and errors: (a) electrical resistance and correlated strain of training set versus time; (b) training set error distribution; (c) Measured strain versus predicted strain for training set.

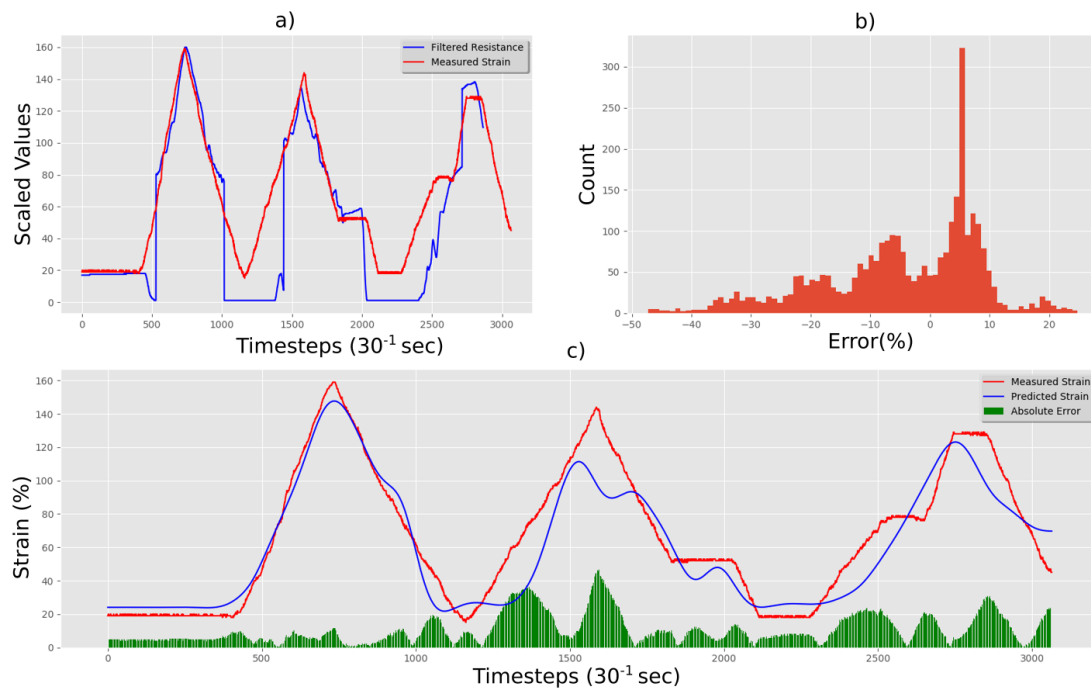


Figure 11. Techniktex P130+B real-time test predictions and errors:(a) electrical resistance and correlated strain of unseen test set versus time; (b) unseen test set error distribution; (c) Measured strain versus predicted strain for unseen test set.

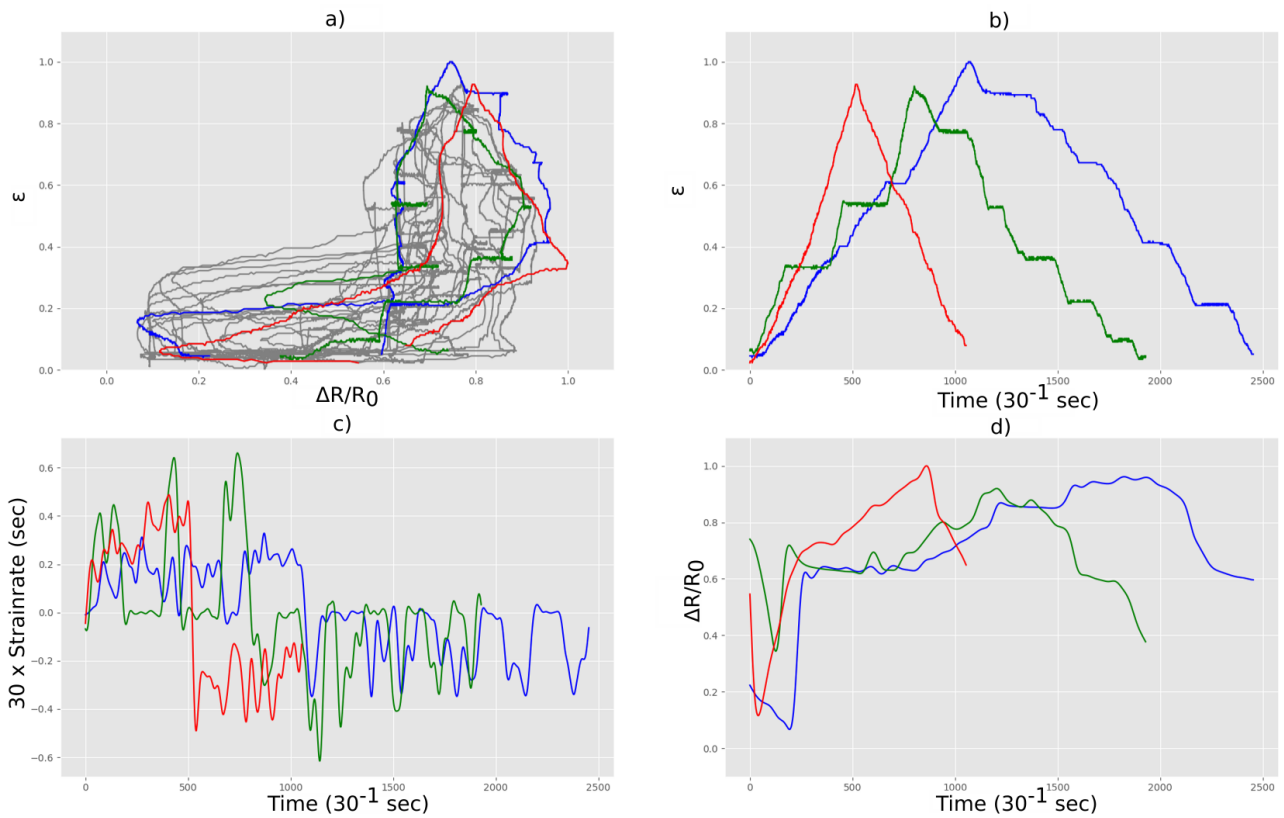


Figure 12. Strain & electrical resistance behaviour of the Adafruit carbon-black rubber during stretching; (a) normalised strain versus normalised resistance; (b) normalised strain versus time; (c) strain rate versus time; (d) normalised resistance versus time

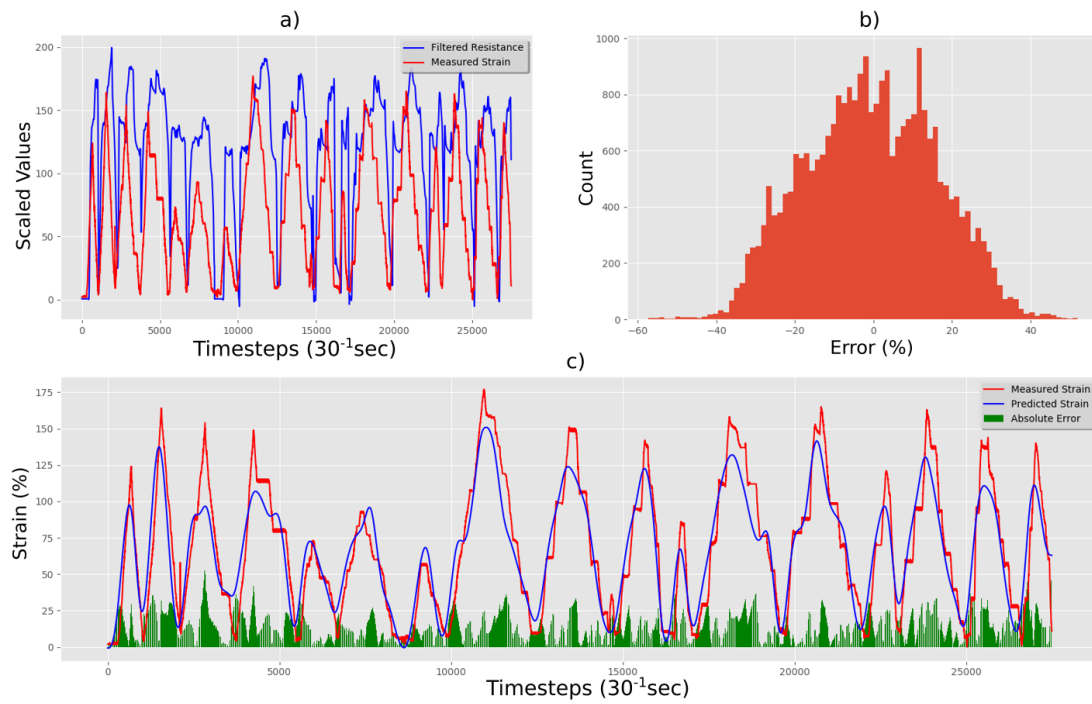


Figure 13. Adafruit carbon-black rubber training data predictions and errors: (a) electrical resistance and correlated strain of training set versus time; (b) training set error distribution; (c) Measured strain versus predicted strain for training set.

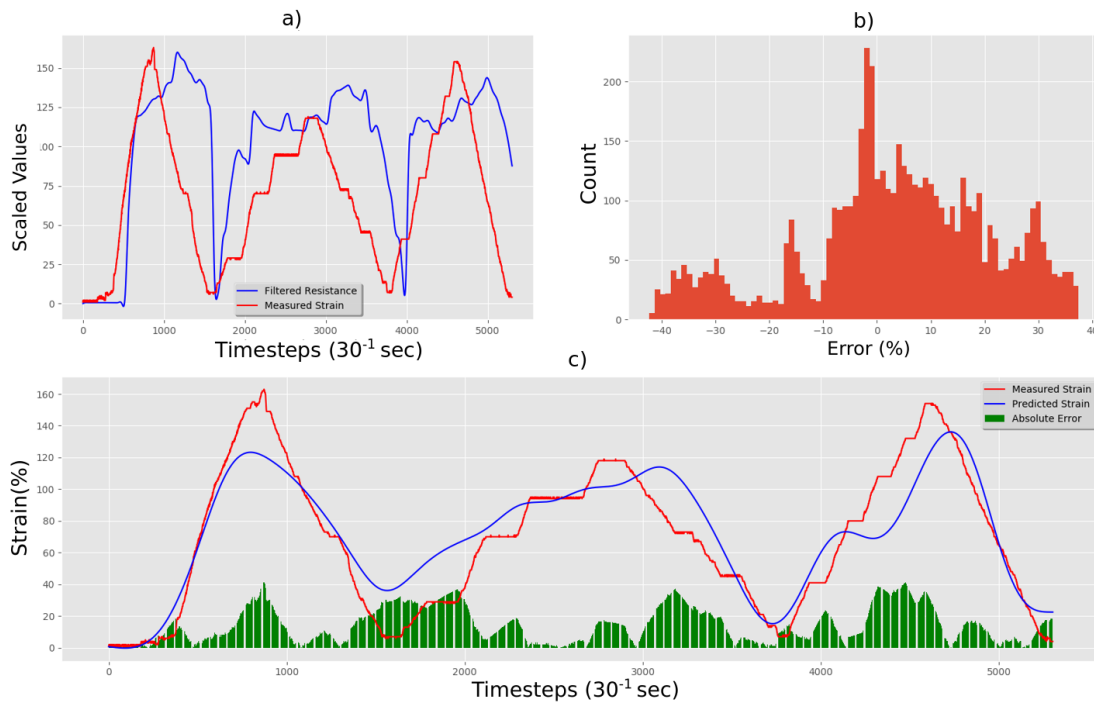


Figure 14. Adafuit carbon-black Rubber real-time test predictions and errors:(a) electrical resistance and correlated strain of unseen test set versus time; (b) unseen test set error distribution; (c) Measured strain versus predicted strain for unseen test set.