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STRUCTURAL BEHAVIOUR OF HARDWOOD VENEER-BASED CIRCULAR HOLLOW

SECTIONS OF DIFFERENT COMPACTNESS

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Abstract: This paper presents the capacity and structural behaviour of hardwood veneer-based circular hollow sections (CHS) tested in bending, shear and compression. The sections were manufactured from early to mid-rotation (juvenile) Gympie messmate (*Eucalyptus cloeziana*) plantation thinned logs. In total twenty-one 167 mm Outside Diameter (OD) × 1.2 m long CHS were manufactured in seven sets of three nominally identical sections. Two different wall thicknesses were investigated to produce nine compact and twelve more slender cross-sections. The sections were also manufactured in three different structural grades. A sudden failure mode was observed in the compression zone of the slender sections tested in bending. In compression, the compact sections showed a ductile behaviour, while the slender sections showed a more brittle behaviour, with the sections bursting into longitudinal strips. While a relationship was observed between the bending and compressive capacities, and the structural grade, no such relationship was noticed for the shear capacity. Comparison to steel and concrete sections of similar outside diameter proved that the timber sections are the most efficient in terms of bending and compressive capacity to linear weight ratio. The timber sections fall behind their steel and concrete counterparts in terms of shear efficiency, however they still have enough shear capacity for representative structural applications.

1. INTRODUCTION

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To develop a market for low-value, small diameter, early to mid-rotation (juvenile) hardwood 27 28 plantation logs, veneer-based hollow sections are currently being developed in Australia [1-3], see 29 Figure 1. These sections have the potential to be used in structural applications [1, 3] and are seen, 30 for instance, as a potential solution for utility poles [1] and the main frame of buildings. They have 31 the advantage of having an efficient cross-sectional shape, are sustainable [4-6], and able to be man-32 ufactured in usable lengths [2] and cross-sectional sizes that are no longer available in sawn timber. 33 In the literature, various hollow timber structural solutions have been investigated. They include 34 (i) spirally winded veneer-based Circular Hollow Section (CHS) [7-9], (ii) fibre-reinforced moulded 35 wooden tubes [10-14], (iii) octagonal tubes from composite wood flakes panels [15], (iv) nonagon tubes from knot free pine wood strips [16], (v) "wood rings" reinforced with glass epoxy [17] and 36 (vi) LVL type CHS for temporary geotechnical soil nailing systems [18]. Commercially, veneer-37 38 based hollow timber solutions are also available, either limited to small diameter cross-sections (up 39 100 mm) [19] or short lengths (up to 1,000 mm) [20]. 40 To confidently use the new sections in structural applications, research is still needed to fully understand their structural behaviour, failure modes and reliability. In particular, bending tests per-42 formed on 145 mm Outside Diameter (OD) × 15 mm (wall thickness) Laminated Veneer Lumber 43 (LVL) type CHS showed that the sections can experience a sudden failure in the compression zone, 44 with the sections opening up [1]. While this failure mode has been observed in hollow trees [21], it is not typical of solid timber beams which usually reach a maximum bending moment due to tensile 45 46 rupture [22]. The sudden compressive failure mode is likely attributed to the semi-compactness of 47 the cross-section in [1] which led to local buckling and cross-section ovalisation (Brazier effect [23]). 48 The relationship between the cross-sectional slenderness and structural behaviour requires further 49 attention.

Consequently, the structural behaviour and failure modes of veneer-based timber CHS of various cross-sectional slenderness are experimentally investigated in bending, shear and compression in this paper. In total twelve 167 mm (OD) × 12.5 mm (wall thickness), referred to as "slender", and nine 167 mm (OD) × 25 mm (wall thickness), referred to as "compact", 1.2 m long CHS were manufactured from early to mid-rotation (juvenile) Gympie messmate (*Eucalyptus cloeziana*) plantation thinned logs. The veneer grain was orientated in the same direction and along the member longitudinal axis for all sections except for one type of the slender sections. For this section, cross-banded veneers were used in this case to potentially increase the section local buckling capacity. To study the effect of the timber elastic stiffness on the new products' structural behaviour, the CHS were manufactured in three different structural grades. The grades were solely based on the veneers' Modulus of Elasticity (MOE).

The paper initially introduces the investigated cross-sections and the associated manufacturing process. Secondly, the test set-ups for all investigated loading cases are presented. Thirdly, the structural behaviour, capacities and failure modes of the slender and compact sections are analysed and discussed. Finally, the performance of the studied sections is compared to similar steel and concrete counterparts.

2. INVESTIGATED CROSS-SECTIONS

2.1 General

In total, twenty-one nominal 167 mm (OD) \times 1.2 m long veneer-based CHS were manufactured from two half cross-sections following the process described later in Section 2.2. Randomly selected nominal 1.2 m (Long) \times 1.2 m (Wide) \times 2.5 mm (Thick) Gympie messmate rotary peeled veneer sheets were delivered and then cut parallel to the grain direction (i.e. perpendicular to the length of the veneer ribbon) into four 300 mm wide strips. The longitudinal dynamic MOE of each veneer sheet

- was then measured using a non-destructive resonance method [24]. To do so, the second cut strip per veneer sheet was simply supported on rubber bands and impacted with a hammer in its longitudinal direction. The sample natural frequency was recorded using a microphone and analysed using the software BING® (Beam Identification by Non-destructive Grading) [25]. Figure 2 shows a photo of
- the set-up. Before assessing the dynamic MOE, the veneers were conditioned in a temperature con-
- 79 trolled room set at 22°C.
- Based on their measured MOE, the delivered veneer sheets were divided into three stacks of equal
- 81 number of veneers. This classified the veneers into three grades referred to as "Grade 1" for the lower
- MOE (13 GPa < MOE \leq 19 GPa), "Grade 2" for the intermediate MOE (19 GPa < MOE \leq 21 GPa)
- and "Grade 3" for the higher MOE (21 GPa \leq MOE \leq 25 GPa).
- The twenty-one CHS were manufactured in seven sets of three nominal identical samples. Per set,
- 85 the half cross-sections of the three nominally identical CHS were manufactured from the same veneer
- sheets which were glued in the exact same order. Precisely, for each veneer sheet, three 300 mm wide
- 87 strips out of four were used in the CHS manufacturing process. The remaining strip was used to
- determine the material properties of the half cross-sections as detailed in Sections 2.2 and 3.2. The
- 89 seven sets consisted of:
- Three sets of nominal 167 mm (OD) × 12.5 mm (5-ply) slender CHS manufactured from Grade 1
- 91 (Set "S_G1"), Grade 2 (Set "S_G2") and Grade 3 (Set "S_G3") veneers. In these sets, the veneers'
- grain is orientated in the same direction and along the longitudinal axis of the section.
- One set of nominal 167 mm (OD) × 13 mm slender CHS. To potentially increase the section local
- buckling capacity, a cross-banded configuration was used. Four 2.5 mm thick Gympie messmate
- hardwood Grade 2 veneers were orientated along the longitudinal axis of the section and three 1
- 96 mm thick cross-banded softwood Hoop pine (Araucaria cunninghamii) veneers were inserted be-
- tween the hardwood veneers to form a 7-ply configuration. This set is referred to as "S G2_Cross".

- Three sets of nominal 167 mm (OD) × 25 mm (10-ply) compact CHS manufactured from Grade 1

 (Set "C_G1"), Grade 2 (Set "C_G2") and Grade 3 (Set "C_G3") veneers. In these sets, the veneers'

 grain is orientated in the same direction and along the longitudinal axis of the section.
- 101 An examples of a compact and slender CHS is shown in Figure 1 (a).
- Note that while the wall the slender sections is quite thin, fire protection may be achieved by gluing sacrificial low MOE veneers to the outside of the sections, therefore protecting the load carrying part of the CHS.

2.2 Manufacturing process

The manufacturing process detailed in [18, 26] and used to manufacture the samples tested in [1, 2] has been improved in this study. A similar process to the one described in [18, 27] has been followed. After assessing the dynamic MOE of the veneers, the veneers were moved out of the temperature controlled room and stored in an indoor environment (structure laboratory) until gluing. To form the half cross-sections, resorcinol formaldehyde structural adhesive was applied to the veneer strips at ambient temperature and humidity. The veneer stacks were then inserted into a 167 mm Internal Diameter (ID) CHS PVC pipe and cold-pressed for 24 hours by a fire hose inserted into the PVC pipe and pressurised at 1.2 MPa with water. Figure 3 illustrates the manufacturing process.

As rotary peeled veneers have the natural tendency to curl about their loose side (i.e. the one in contact with the blade of the peeling lathe), the loose side of a veneer was always glued herein to the tight side of the next veneer. The tight and loose veneer sides therefore formed the outside and inner faces of the manufactured hollow cross-sections, respectively. The two half cross-sections forming a complete CHS were then butt jointed together using structural epoxy resin (Figure 1 (b)) due to its good gap properties which can compensate for non-strict parallelism of the two half cross-sections.

For alignment, the glue-line incorporated biscuit joints every 400 mm.

Additionally, to determine the mechanical properties of the material of the timber sections, two $500 \text{ mm} \times 300 \text{ mm}$ flat panels were also manufactured for each half-section. The panels were manufactured from the same veneer sheets used to produce the half cross-sections and were glued in the exact same layering order.

3. TESTING METHODOLOGY

3.1 General

Per manufactured set, one section was tested in bending, one in shear and one in compression. The following sub-sections introduce the material testing methodology and the test set-ups of the CHS for each one of the investigated loading cases.

Before testing, all samples were conditioned in the same temperature controlled room as the veneers when the dynamic MOE was assessed, for a minimum period of one month. The temperature in the room was set at 22°C. For all scenarios, excluding the CHS tested in compression, pieces were cut and weighed immediately after testing from selected test samples to determine the timber moisture content at the time of testing. The oven-dry methodology in the Australian and New Zealand standard AS/NZS 1080.1 [28] was followed.

3.2 Material properties

138 3.2.1 Tension tests

From the first flat panel of each half cross-section, a maximum of five nominal 10 mm wide \times 100 mm long (gauge length) coupon (dog bone) samples were CNC cut. The samples were similar to the ones recommended by the ASTM D3500–14 [29] and were used to estimate the tensile strength of each half cross-section. The ends of the samples were clamped in the jaws of a 500 kN capacity MTS universal testing machine and tested in tension at a constant strain rate to reach failure in 3-6 mins.

The tensile strength σ_{tens} of each coupon was calculated as,

$$\sigma_{tens} = \frac{F_{\text{max}}}{W_t t_t} \tag{1}$$

where F_{max} is the maximum recorded force, W_t and t_t are the measured width and thickness of the coupons, respectively.

148 3.2.2 Compression tests

The second flat panel of each half cross-section was used to determine the compressive strength of the material. To avoid buckling of the samples corresponding to the slender CHS, the 12.5 mm thick panels were cut in two and glued together using resorcinol formaldehyde structural adhesive to form nominal 25 mm thick panels. The panels corresponding to the compact CHS were left untouched. Up to four 80 mm (Wide) \times 150 mm (Long) rectangular samples were cut per panel for material testing.

The samples were tested in compression in a 500 kN capacity MTS universal testing machine at a constant strain rate to reach the peak stress in 3-5 mins. Specifically, the samples were positioned between a fixed bottom platen and an upper platen mounted on a spherical seat, which could rotate, so as to provide full contact between the platens and the specimens. Note that before testing, the ends of the samples were cut with a high quality fine cut circular saw blade to ensure a uniform contact pressure between the platens and the samples.

Similar to Eq. (1), the compressive strength σ_{comp} of each sample was calculated as,

$$\sigma_{comp} = \frac{F_{\text{max}}}{W_c t_c} \tag{2}$$

where F_{max} is the maximum recorded force, W_c and t_c are the measured width and thickness of the samples, respectively.

3.3 Bending tests

3.3.1 Test set-up

To measure the bending strength and stiffness of the timber CHS, the sections were tested in a similar manner to the one reported in [2]. A pair of four reinforced quarter steel tubes, 240 mm long, were designed and manufactured to rigidly clamp each end of the CHS, as shown in Figure 4. Each steel clamp was bolted to a steel Rectangular Hollow Section (RHS) to form a 2,360 mm long beam. To avoid local crushing of the timber CHS and fully transfer the moment from the steel RHS to the timber with minimum stress concentration, two part epoxy resin was poured at the steel-timber connection (i) in the inside of the timber CHS filled with plywood and (ii) on the outside of the timber CHS to match the inside diameter of the four quarter steel tubes. On top of the friction forces applied by the clamps to the timber, screws connecting the steel to the timber were also added to further prevent sliding of the timber sections in the clamps. The overall test set-up is shown in Figure 5.

The sections were then tested in a 500 kN capacity MTS universal testing machine, with the load being applied to the steel RHS, as shown in Figure 5. The tests were run in displacement control and reached failure in 3-4 minutes for the slender sections and 5-6 minutes for the compact sections. For all tests, the butt joints between two half-sections lied in the horizontal plane.

Three Laser Displacement Sensors (LDS) recorded the vertical displacement at the bottom fibre of the timber sections for simplicity in the test set-up. Additionally, two 30 mm strain gauges (SG) recorded the mid-span longitudinal strain at the top (compression) and bottom (tension) fibres of the timber CHS. A third 30 mm strain gauge recorded the mid-span tangential stress to better apprehend the cross-sectional deformation. Locations and numbering of all LDS and strain gauges are given in Figure 5 (b). The 300 mm distance between LDS was chosen so the edge LDS are away for the clamping ends while placing the LDS the further away from each other.

3.3.2 Evaluations

The applied moment M to the hollow timber sections is calculated as,

$$M = \frac{\left(F + F_{w}\right)L_{1}}{2} \tag{3}$$

where F is the total applied load, $F_w = 2.37$ kN is the gravity load applied by the steel rig (including the steel CHS and measured at the points of application of the load) and $L_I = 455$ mm is given in Figure 5 (b). The bending capacity M_b is defined as the maximum applied moment M and the bending strength f_b is obtained from the well-known equation,

$$f_b = \frac{M_b}{Z} \tag{4}$$

- where Z is the section modulus calculated from the measured cross-sectional dimensions, assuming a perfect composite action between the two half cross-sections.
- The relative displacement δ of the timber sections is calculated from the displacements δ_1 , δ_2 and δ_3 recorded by the LDS number 1, 2 and 3, respectively, as,

$$\delta = \delta_1 - \frac{\delta_2 + \delta_3}{2} \tag{5}$$

The static MOE E_s parallel to the grain of the timber sections is calculated from the bending stiffness E_sI_s defined as,

$$E_{s}I_{s} = \frac{k_{t}d^{2}}{2} \tag{6}$$

where I_s is the second moment of area of the CHS (calculated from measured dimensions), d is given in Figure 5 (b) and k_t is the stiffness of the linear part of the experimental moment-displacement curve $(M-\delta)$, calculated by performing a linear regression between 5 kN.m and 20 kN.m for the compact sections and 2.5 kN.m and 15 kN.m for the slender ones. Note that Eq. (6) assumes that the relative displacement δ is measured at the neutral axis. Yet, using the relative displacement measured in this study at the bottom fibre of the section provides accurate results, with a maximum error in determining E_sI_s of less than 0.5%.

212 **3.4 Shear tests**

213 *3.4.1 Test set-up*

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To estimate the shear strength of the timber CHS, the sections were tested in three point bending, similarly to the tests performed in [1]. The sections were simply supported with a distance L = 500 mm between two consecutive loads, as shown in the schematic test set-up in Figure 6. To avoid local crushing of the sections, two part epoxy resin (combined with plywood) was poured inside the CHS at the load application point and supports. The butt joints between two half cross-sections lied in the horizontal plane. For each set, the half cross-section which was in compression in the bending test (Section 3.3) was also in compression in the shear test. The tests were performed in a 500 kN capacity MTS universal testing machine in displacement control and reached failure in 6-8 minutes for all sections but for S_G3 which was tested at a higher strain rate and reached failure in 2 minutes.

- 223 3.4.2 Evaluations
- The shear strength f_s of the hollow timber sections is calculated using the shear area of a CHS as
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$$f_{s} = \frac{F_{\text{max}}}{\frac{3}{2} A \left(\frac{R_{o}^{2} + R_{i}^{2}}{R_{o}^{2} + R_{o} R_{i} + R_{i}^{2}} \right)}$$
 (7)

- where F_{max} is the total maximum applied load, A is the measured CHS cross-sectional area, and R_o
- and R_i are the measured CHS external and internal radii, respectively. The shear capacity V_s is calcu-
- lated as $F_{max}/2$.
- 230 3.5 Compressive tests
- 231 *3.5.1 Test set-up*
- To measure the compressive strength and stiffness of the timber CHS, the sections were tested in compression in a 10 MN capacity MTS universal testing machine. The sections were positioned be-
- tween a fixed bottom platen and an upper platen mounted on a spherical seat, which could rotate. The

samples were mechanically sanded flat in a milling machine before testing to ensure a uniform contact pressure between the platens and the CHS. The tests were performed in displacement control and reached failure in 3-4 minutes for the slender sections and 5-6 minutes for the compact sections. The test set-up is shown in Figure 7.

Two diametrically opposed 30 mm strain gauges, glued parallel to the column axis, each located in the middle of a half cross-section and 150 mm from the bottom end of the sections, recorded the longitudinal deformation. Strain gauges numbering is given in Figure 7.

242 3.5.2 Evaluations

The compressive stress σ of the hollow timber sections is calculated as,

$$\sigma = \frac{F}{A} \tag{8}$$

where F is the applied load and A is the measured CHS cross-sectional area. The compressive capacity R_c and strength f_c are defined as the maximum applied force and compressive stress, respectively. The static MOE E_s is calculated by performing a linear regression on the linear part of the stress-strain curve $(\sigma$ - ε) between 5 MPa and 40 MPa. The strain ε is calculated as the average of strains ε_1 and ε_2 from strain gauges 1 and 2, respectively.

4. RESULTS AND DISCUSSION

4.1 Material properties

Table 1 gives the tensile and compressive strengths of the material of each half cross-section of each investigated set. As the veneer MOE increases with the grade, so typically does the measured material strength [31]. For the LVL samples, the compressive strength ranges from 58.6 MPa (S_G1) to 77.9 MPa (C_G3 and S_G3), and the tensile one from 96.3 MPa (C_G1) to 135.8 (C_G3). Due to the nature of the brittle tensile failure mode compared to the ductile compressive failure mode of

timber samples, the Coefficients of Variation (CoV) of the tensile test results are typically higher than the ones of the compressive test results. The average oven dry moisture content at the time of testing of the tension and compression samples is reported in Table 2.

4.2 Bending tests

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4.2.1 Capacities and failure modes

The bending capacities M_b and strengths f_b for all CHS tested in bending are reported in Table 3, along with the measured static MOE E_s (Eq. (6)) and observed failure modes. Two of the slender sections (S_G1 and S_G3) failed in buckling of the compression fibre, with the section opening up, as shown in Figure 8 (a). Slender S_G2 and compact C_G1 sections failed in tensile rupture, as shown in Figure 8 (b). The cross-banded CHS (C_G2_Cross) prematurely failed in the butt joint between the two half cross-sections, as shown in Figure 8 (c). This weak zone was only observed for all testing configurations in C_G2_Cross, as later reported in Sections 3.4 and 0. In all other sections and sections tested in [1, 2], failure never developed in the butt joint. For compact sections C_G2 and C G3, the steel clamps did not provide sufficient restraints and the sections ultimately slid at the steel-timber connections, leading to shear failure, as shown in Figure 8 (d). However, the maximum bending stresses reached for these two sections are higher than the bending strengths f_b of all other tested sections. It is therefore very likely that the maximum recorded moments are within a few percent of the bending capacities M_b of the sections. Noting that these maximum recorded moments represent lower bound values of M_b , their values are conservatively taken for M_b herein for both C_G2 and C_G3 sections. For all sections, the bending strength typically increases with the veneer MOE (or grade). The compact sections reached on average a bending strength f_b 18% higher than the one of the slender sections of the same grade. This result is attributed to different material strengths between sections (Table 1) and possibly to the section compactness. Indeed, when buckling develops in the compression zone of the slender sections, it would result in a loss in stiffness of the section wall, consequently inducing a shift of the neutral axis and a higher stress in the tension zone. The sections would eventually fail in the compression zone (S_G1 and SG_G3) or tension zone (S_G2), whichever zone is the weakest. Such phenomenon would not occur for compact sections for which the compressive zone only experiences plasticity without buckling, as typically observed in timber beams [22]. A similar tensile failure mode to the one experienced in timber beams would be therefore expected.

More investigations are needed to (i) fully comprehend the mechanisms involved in the observed failure modes of the slender sections, (ii) validate the hypothesis in the above paragraph and (iii) quantify the influence of the cross-sectional geometry, timber compressive and tensile strengths on the full section capacity. Numerical models, similar to the one developed in [1], can be used to predict the capacity of compact sections.

Note that the cross-banded section (S_G2_Cross) has a bending strength f_b and static MOE E_s 9% and 55%, respectively, lower than the ones of the slender section of the same grade (S_G2). Cross-banded veneer-based CHS would gain further structural optimisation, such as number and thickness of the cross bands.

4.2.2 Behaviour

Figure 9 plots the Moment-Displacement curves (M- δ) of all investigated sections. While a large non-linear behaviour is observed for the compact sections, it is limited for the slender sections, except for the cross-banded one. As outlined in Figure 9, when failure occurred the moment suddenly dropped for all sections. This observed drop for the two slender sections failing in buckling of the compression zone (S_G1 and S_G3) is due to the sections opening up.

Figure 10 (a) shows the readings of the two strain gauges glued in the section longitudinal axis (SG 1 and SG 3). Timber elements loaded in tension typically exhibit a linear behaviour until fracture suddenly occurs at the maximum tensile strength, and the strain recorded on the tension zone (SG 3)

is consequently almost linear. Plasticity occurred on the compression side (SG 1) at an applied moment of about 20-25 kN.m and 12-15 kN.m for the compact and slender sections, respectively. This corresponds to bending stresses of about 60 MPa to 75 MPa, i.e. of the same order of magnitude of the material compressive strengths reported in Table 1. Due to the buckling of the compression zone for S_G1 and S_G3 , reading of Strain gauge 2 reached a plateau for these sections at about 12,000 to $16,000~\mu\epsilon$.

The transverse strain recorded by SG 2 is plotted in Figure 10 (b). The figure mainly indicates that the transverse strain significantly increased when plasticity damage occurred in the compression zone.

The strain reversal experienced for S_G1 and S_G3 is likely attributed to the buckling and ovalisation of the cross-sections.

The average oven dry moisture content at the time of testing of the sections tested in bending is reported in Table 2.

4.3 Shear tests

Table 4 gives the experimental shear capacities V_s and strengths f_s for all investigated sections. All sections failed in the timber except S_G2_Cross which failed in the butt joint between the two half cross-sections. The two observed failure modes are shown in Figure 11. All sections reached a similar shear strength of 10 MPa, +/- 7%, indicating that contrary to the bending tests, the grade does not influence the shear capacity. Note that despite S_G2_Cross failing in the butt joint, it still reached a strength of 10.4 MPa. Further optimisation of the cross bands layering may improve the shear capacity of the CHS.

In terms of shear capacities, the slender sections sustained shear forces up to 32 kN and the compact ones up to 60.8 kN.

The average oven dry moisture content at the time of testing of the sections tested in shear is reported in Table 2.

4.4 Compressive tests

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The compressive stress-strain curves $(\sigma - \varepsilon)$ of all sections are plotted in Figure 12. Two different types of curves are observed resulting in two different failure modes. The compact sections showed a large non-linear plastic behaviour, with the load reaching a plateau before gradually decreasing. A portion of the section wall ultimately locally buckled in a compression type failure mode, as shown in Figure 13 (a). This led to a sudden drop of the load with the section remaining in one single piece. For the slender sections, a plastic behaviour usually started to develop but premature failure (i.e. before the load reached a plateau as for the compact sections) suddenly occurred with the sections bursting into (i) two half cross-sections, with the failure occurring in the butt joint, for S G2 Cross and (ii) six to seven strips for all remaining slender sections. The latter failure mode is shown in Figure 13 (b) and was also observed in [13, 32] for formed wood profiles. The slender sections could therefore not reach their potential full capacity and exhibited a failure mode which should be avoided in structures. The compressive capacities R_c and strength f_c for all tested sections are reported in Table 5. The ratios of f_c to the average material compressive strength σ_{comp} of the two half cross-sections (reported in Table 1) are also given in the table. Similar to the bending tests, the compressive strength increases with the veneer MOE (grade). Interestingly, both slender and compact sections reached a capacity higher, up to 20%, than the one of the average measured compressive strength of the material. This observation is in contradiction with the length effect [33, 34] encountered in timber structures for which the larger the tested volume, the lesser the capacity. The circular shape of the section may delay the compression failure of the cell walls when compared to the results reported in Section 4.1 and performed on flat panels. Further investigations are needed to validate and understand the observed phenomena.

The compressive capacity is high for both section types and reached about 400-500 kN for the slender sections to about 800-1,000 kN for the compact ones. For the compact sections, the capacity is in the range of the design load which may be encountered in the columns of mid-rise timber buildings.

Also given in Table 5 are the static MOE E_s of the sections measured from the linear part of the stress-strain curves (σ - ε) and the ratios of E_s measured from the bending tests to the one measured from the compressive tests. The values of E_s measured from the two types of tests are consistent with an average difference between the two values of 4%.

4.5 Comparisons

The structural efficiency of the compact sections is compared herein to the one of steel and reinforced concrete circular sections of similar (i) diameter and (ii) compressive short-term capacity to the middle grade section C_G2 reported in Table 5. In a first instance only the short-term capacities of the timber section is compared to the ultimate capacities of the steel and concrete counterparts, which are calculated based on relevant Australian standards and without the use of the capacity factor (resistance factor). Effect on long-term loading on the structural efficiency is discussed in a second instance.

4.5.1 Comparison to steel CHS

A 168.3 (OD) \times 4.8 (wall thickness) CHS, commercialised by the Australian manufacturer Onesteel [35], is selected for the structural steel section. Its yield stress is 350 MPa. Based on the Australian and New-Zeeland standard AS4100 [36], the steel section has ultimate bending, shear and compressive section capacities of $M_b = 44.8$ kN.m, $V_s = 311.2$ kN and $R_c = 864.5$ kN, respectively. Its compressive capacity is within 4% of the one of C_G2. Table 6 compares the ultimate capacities, ultimate capacity to linear weight ratios, bending and axial stiffness of the steel and timber sections. Densities of 805 kg/m³ for early to mid-rotation Gympie messmate veneers [37] and 7,850 kg/m³ for steel are used in Table 6. MOE of 200 GPa is also used for the steel in the Table.

Results show that the timber CHS has a short-term bending capacity M_b comparable to and only 13% lower than the one of the steel CHS. Yet, the timber CHS is nearly twice more efficient in terms of ultimate capacity to linear weight ratio. A similar conclusion applies to the compressive capacity to linear weight ratio, with the timber section being more than twice more efficient than the steel CHS. However, the steel CHS is stiffer than the timber profile, with the bending and axial stiffness being 2.7 and 2.1 times higher, respectively.

Regarding the shear, the timber CHS performs poorly when compared to the steel profile. The shear capacity V_s and shear to linear weight ratio of the steel CHS are 5.1 and 2.4 times higher, respectively, than the ones of the timber sections. However, for the sizes of timber beams typically encountered in structural applications, i.e. with a span to depth ratio of 20 [38], the shear capacity of the timber section would be high enough. A simply supported, 3.5 m long, 167×25 timber CHS loaded with a UDL which fails at an ultimate bending moment of 39.1 kN.m (C_G2 in Table 3), would experience a maximum shear force of 44.7 kN. This shear force is 26% lower than the shear capacity recorded for C_G2 in Table 4.

For long-term loading, the Australian standard AS1720.1 [39] uses a duration of load factor of 0.57. Therefore, using the same 168.3×4.8 steel CHS and comparing it to the timber CHS, but under long-term loading, the timber section becomes 1.08 and 1.28 times more efficient that the steel CHS in term of bending capacity to linear weight ratio and compressive capacity to linear weight ratio, respectively. In terms of shear capacity to linear weight ratio, the timber CHS now becomes 4.16 times less efficient than the steel CHS.

4.5.2 Comparison to reinforced concrete plain circular section

A 167 mm diameter plain reinforced concrete column, with a concrete compressive strength f'_c = 40 MPa and a steel yield stress f_y = 500 MPa, was designed to standard practices and the Australian Standard AS3600 [40]. While it is understood that a 167 mm diameter concrete columns would usually not be used in practice, it still forms a comparative solution to the performance of the timber section. The concrete section is shown in Figure 14, has four N12 longitudinal reinforcing bars and an R10 helix with a pitch of 150 mm. Based on the requirements in [40], a minimum concrete cover of 20 mm is used with a minimum of 2% reinforcing steel by gross cross-sectional area. The AS3600 [40] gives ultimate bending, shear and compressive capacities of M_b = 11.9 kN.m, V_s = 92 kN and R_c = 946.4 kN, respectively, for the concrete section. The compressive capacity of this column is therefore within 6% of the one of C_G2.

Table 6 compares the ultimate capacities, ultimate capacity to linear weight ratios, bending and axial stiffness of the concrete and timber sections. The density of concrete for the calculations presented is 2,400 kg/m³ and the MOE is 32,8 GPa, in accordance to [40].

The ultimate bending capacity of the concrete section is significantly lower (3.3 times lower) than the short-term bending capacity of the timber section. This results in the timber section being 22 times more efficient than the concrete one in terms of bending capacity to linear weight ratio. On the other hand, the bending stiffness of the concrete section is twice higher than the proposed timber section and nearly as stiff as the steel section. Note that the small diameter of the concrete column results in the steel being placed close to the neutral axis and therefore an inefficiency in resisting bending moments is introduced. It is anticipated that for columns of larger diameter, the efficiency of the concrete column for these comparisons would improve.

In terms of shear, the shear capacity of the reinforced concrete section is 1.5 higher than the short-term shear capacity of the timber section, yet the concrete solution is 3.9 less efficient than the timber one in terms of shear capacity to linear weight ratio.

The concrete section is also the least efficient option in terms of compressive capacity to linear weight ratio. It is 5.6 times and 2.5 less efficient than its timber and steel counterparts, respectively. Nevertheless, it outperformed both the steel (1.5 times higher) and timber (3 times higher) solutions in terms of compressive stiffness.

Regarding long-term loading and considering a duration of load factor of 0.57 [39] on the results in Table 6, the concrete section becomes 12.5, 2.2 and 3.2 times less efficient in terms of bending, shear and compressive capacity to linear weight ratios, respectively, when compared to the long-term loading capacities of the timber section.

5. CONCLUSION

This paper presented the bending, shear and compression capacities, and structural behaviour, of hardwood veneer-based CHS manufactured from early to mid-rotation (juvenile) Gympie messmate plantation thinned logs. Twelve 167 mm (OD) × 12.5 mm (wall thickness), referred to as "slender", and nine 167 mm (OD) × 25 mm (wall thickness), referred to as "compact", 1.2 m long CHS were produced in seven sets of three nominally identical sections. The sections were tested in bending, shear and compression. A sudden failure mode was observed in the compression zone of the slender sections tested in bending, while the compact sections failed in the tension zone. The section had shear capacities of the same order of magnitude, within 7% of each other. In compression, the compact sections showed a ductile behaviour, while the slender sections catastrophically failed, with the sections bursting into six to seven longitudinal strips. The section compressive strength was observed to be consistently higher than the compressive strength of the material determined from tests performed of flat samples. Comparison to steel and concrete sections of similar outside diameter proved that the timber sections were the most efficient in terms of bending and compressive capacity to linear weight ratio. However, while the timber sections fell behind their steel and concrete counterparts in

- 448 terms of shear efficiency, they still showed enough shear capacity for structural applications. The
- optimisation of the cross-banded layering may improve the shear capacity without significantly im-
- pacting the critical structural performances of the CHS.

452

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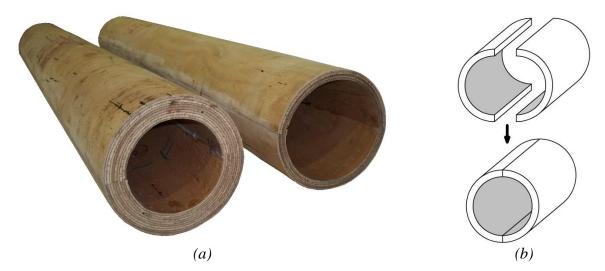


Figure 1: (a) circular hollow section currently developed in Australia (shown for compact and slender 167 mm (OD) Gympie messmate) and (b) principle of half cross-sections butt joined together to form a complete CHS

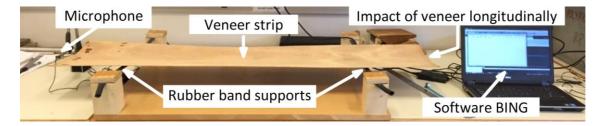


Figure 2: Set-up to assess the longitudinal MOE

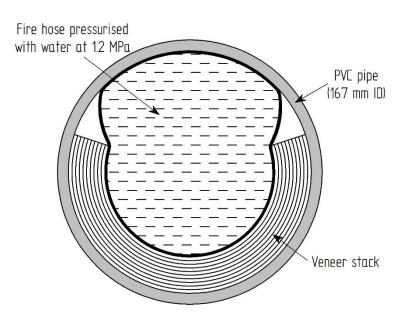


Figure 3: Manufacturing process of the half cross-sections

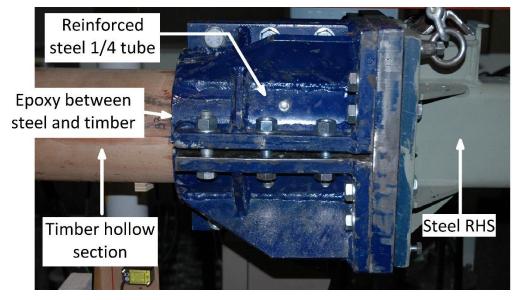


Figure 4: Clamps to connect timber CHS to test rig

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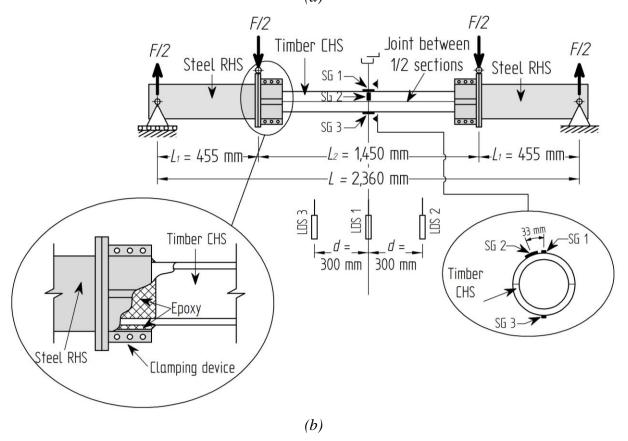


Figure 5: Bending test set-up, (a) overall picture and (b) schematic

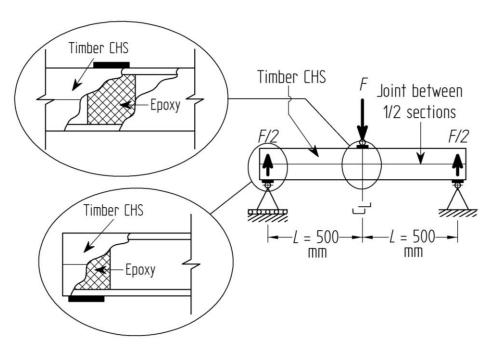


Figure 6: Shear test set-up

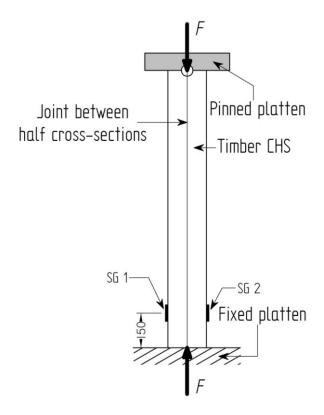


Figure 7: Compression test set-up



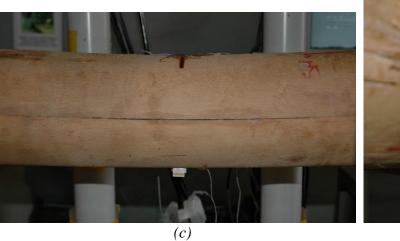




Figure 8: Bending tests failure modes (a) buckling of the compression zone (shown for S_G3), (b) Tensile rupture (shown for C_G1), (c) initial failure in the butt joint for C_G2_Cross and (d) premature failure at the steel-timber connections (shown for C_G2)

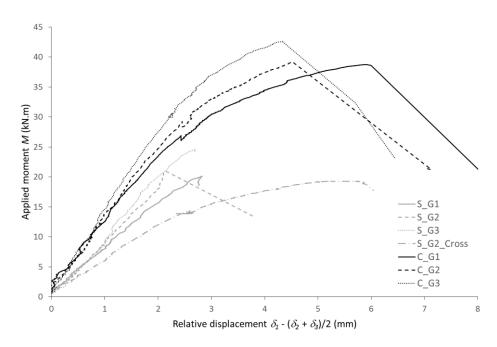


Figure 9: Bending tests, Moment-Displacement curves (M- δ) for all investigated sections

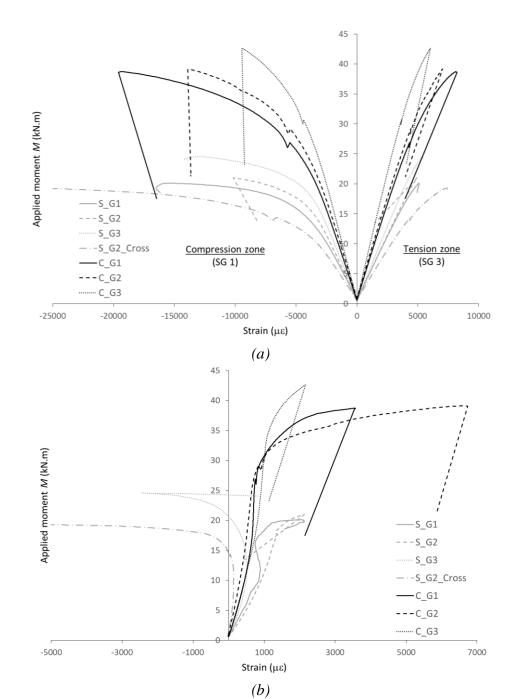


Figure 10: Bending tests, Strain gauge readings for all investigated sections (a) longitudinal strain gauges (SG 1 and SG 3) and (b) transverse strain gauge (SG 2)

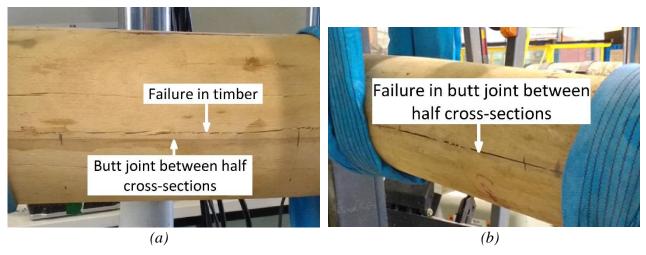


Figure 11: Shear tests failure modes (a) failure in the timber for all sections but C_G2_Cross (shown for S_G3) and (b) failure in the butt joint for C_G2_Cross

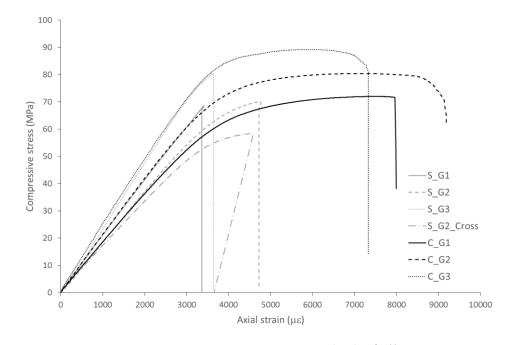


Figure 12: Compression tests, Stress-Strain curves $(\sigma - \varepsilon)$ of all investigated sections



Figure 13: Compression tests failure modes, (a) local buckling of the wall for the compact sections (shown for C_G1) and (b) sudden failure with the sections bursting into strips for the slender sections with no cross-banded veneers (shown for S_G2)

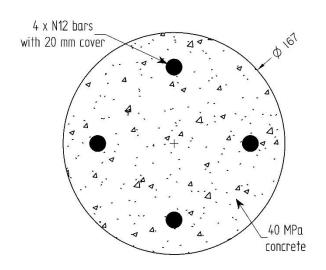


Figure 14: Concrete section used for comparison purposes

Table 1: Average compressive and tensile strengths of the material (numbers in brackets indicate the number of tests on which the average and Coefficient of Variation (CoV) are calculated)

	Half cross-section 1 ⁽¹⁾				Half cross-section 2 ⁽¹⁾			
Set	σ_{comp}	CoV	σ_{tens}	CoV	σ_{comp}	CoV	σ_{tens}	CoV
	(MPa)	(%)	(MPa)	(%)	(MPa)	(%)	(MPa)	(%)
S_G1	61.2 (3)	4.2	109.5 (5)	21.4	58.6 (3)	< 0.1	96.7 (3)	7.3
S_G2	65.5 (3)	5.3	101.0 (4)	31.1	69.2 (3)	3.5	119.1 (5)	11.4
S_G3	72.7 (3)	3.2	114.0 (5)	31.9	77.9 (3)	3.4	(2)	(2)
S_G2_Cross ⁽³⁾	54.0 (3)	0.5	94.4 (5)	5.3	59.9 (2)	12.3	88.9 (5)	15.7
C_G1	67.0 (2)	1.9	99.3 (5)	6.9	64.4 (4)	3.4	96.3 (5)	7.7
C_G2	67.8 (2)	7.2	117.2 (5)	8.7	66.7 (4)	1.6	134.0 (5)	11.8
C_G3	77.9 (2)	3.6	133.0 (5)	8.8	71.3 (3)	2.4	135.8 (5)	11.5

^{(1):} Half cross-section #1 in tension and half cross-section #2 in compression during the bending and shear tests

Table 2: Average measured moisture content (MC) for material testing and full cross-sections (numbers in brackets indicate the number of samples on which the average and Coefficient of Variation (CoV) are calculated)

Sample type	Test type	MC (%)	CoV (%)
Material testing	Compression	13.7 (10)	3.4
	Tension	11.3 (14)	5.7
Full cross-sections	Bending	13.7 (4)	4.2
	Shear	12.2 (4)	1.9

Table 3: Bending tests results

Set	Capacity Strength f _b		$MOE E_s$	Failure mode
	M_b	(MPa)	(MPa)	
	(kN.m)			
S_G1	20.1	96.9	20154	Compression (buckling) failure
S_G2	21.0	96.3	23252	Tension failure
S_G3	24.6	116.7	27883	Compression (buckling) failure
S_G2_Cross ⁽¹⁾	19.3	88.5	14947	Failure in joint between 1/2 cross-sections
C_G1	38.7	116.1	18590	Tension failure
C_G2	39.1	119.0	21666	Failure at support with steel clamps
C_G3	42.6	128.6	23331	Failure at support with steel clamps

 $^{^{(1)}}$: Strength f_b calculated using the gross measured cross-section which includes cross-banded veneers

^{(2):} Samples lost by the external company which CNC cut the samples

^{(3):} Strengths calculated using the gross measured cross-sectional area which includes cross-banded veneers

Table 4: Shear tests results

Set	Capacity V_s (kN)	Strength f_s (MPa)
S_G1	30.5	10.3
S_G2	29.5	9.5
S_G3	30.9	9.9
S_G2_Cross ⁽¹⁾	32.0	10.4
C_G1	53.9	9.5
C_G2	60.8	10.7
C_G3	58.5	10.6

⁽¹⁾: Strength f_s calculated using the gross measured cross-section which includes cross-banded veneers

 Table 5: Compression tests results

Set	Capacity	Capacity Strength f_c		Section strength f_c /	E_s (bending) /	
	R_c (kN)	(MPa)	(MPa)	material strength σ_{comp}	E_s (compression)	
S_G1	438.2	68.6	18824	1.15	1.07	
S_G2	451.4	70.0	20592	1.04	1.13	
S_G3	488.0	80.3	24709	1.07	1.13	
S_G2_Cross ⁽¹⁾	372.3	58.4	16343	1.02	0.91	
C_G1	784.0	72.0	17852	1.10	1.04	
C_G2	897.8	80.4	20849	1.20	1.04	
C_G3	992.4	89.3	24529	1.20	0.95	

^{(1):} Strength f_c calculated using the gross measured cross-section which includes cross-banded veneers

Table 6: Structural efficiency of circular timber, steel and reinforced concrete sections

	Bending			Shear		Compression		
Section	M_b	M_b / linear	Stiffness	V_s	V_s / linear	R_c	R_c / linear	Stiff-
	(kN.m)	weight	EI	(kN)	weight	(kN)	weight	ness EA
		(kN.m/kg)	$(kN.m^2)$		(kN/kg)		(kN/kg)	(kN)
Timber (C_G2)	39.1	4.4	6.15×10^2	60.8	6.8	897.8	100.0	2.37×10^{5}
Steel (168×4.8)	44.8	2.3	1.65×10^3	311.2	16.1	864.5	44.6	4.94×10^{5}
Concrete	11.9	0.2	1.22×10^3	92.0	1.8	946.4	18.0	7.18×10^5