

1 **A Theoretical Model for the Formation of Ring Moat Dome Structures:**
2 **Products of Second Boiling in Lunar Basaltic Lava Flows**

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18 **Keywords:**

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21 Lava flow inflation

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25 **Abstract:**

26 Newly documented Ring Moat Dome Structures (RMDSs), low mounds typically
27 several hundred meters across with a median height of ~3.5 m and surrounded by
28 moats, occur in the lunar maria. They appear to have formed synchronously with the
29 surrounding mare basalt deposits. It has been hypothesized that they formed on the
30 surfaces of lava flows by the extrusion of magmatic foams generated in the flow
31 interiors as the last stage of the eruption and flow emplacement process. We develop
32 a theoretical model for the emplacement and cooling of mare basalts in which the
33 molten cores of cooling flows are inflated during the late stages of eruptions by
34 injection of additional hot lava containing dissolved volatiles. Crystallization of this
35 lava causes second boiling (an increase in vapor pressure to the point of
36 supersaturation due to crystallization of the melt), generating copious quantities of
37 vesicles (magmatic foam layers) at the top and bottom of the central core of the flow.
38 Flow inflation of many meters is predicted to accompany the formation of the foam
39 layers, flexing the cooled upper crustal layer, and forming fractures that permit
40 extrusions of the magmatic foams onto the surface to form domes, with subsidence of
41 the subjacent and surrounding surface forming the moats. By modelling the evolution
42 of the internal flow structure we predict the properties of RMDSs and the conditions
43 in which they are most likely to form. We outline several tests of this hypothesis.

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45

46 1. Introduction:

47 The volcanic origin of the lunar maria has been known confidently for more than
48 fifty years (see reviews in Head, 1976; Hiesinger and Head, 2006; Spudis, 2016), but
49 new very high-resolution image and altimetry data from the Lunar Reconnaissance
50 Orbiter (LRO) have continued to reveal surprises, including the wide-spread
51 occurrence of features originally detected by Schultz (1976) and Schultz et al. (1976),
52 and now called Ring Moat Dome Structures (RMDSs) (Zhang et al., 2017). More
53 than two thousand of these features were recently documented in numerous maria
54 (Figure 1) (Zhang et al., 2017). Theories proposed for their origin, summarized in
55 Zhang et al. (2017), include emplacement of domes of more viscous magma,
56 extrusions into impact craters billions of years after mare emplacement, squeeze-ups
57 or hornitos formed synchronously with lava flow emplacement, and extrusion of
58 magmatic foams (i.e., lavas with greater than ~70% vesicularity, Mangan and
59 Cashman, 1996) that developed below a cooling lava flow surface.

60

61 The availability of LRO imaging (Robinson et al., 2010) and topographic (Smith
62 et al., 2010) data, together with a better understanding of the ways in which magma is
63 transferred from the lunar mantle to the surface (Wilson and Head, 2017a; Head and
64 Wilson, 2017), and improvements in the analysis of patterns of gas release from lunar
65 magmas (Rutherford et al., 2017; Wilson and Head, 2018a) have prompted
66 recognition of the importance of the formation and extrusion of magmatic foams in
67 shaping lunar volcanic features (Qiao et al., 2017, 2018a, 2018b; Wilson and Head,
68 2017b, 2018b). Foam formation without extrusion can be a source of inflation of
69 lunar lavas (Garry et al., 2012; Elder et al., 2017) and a study of an inflated terrestrial
70 lava has shown that neglect of the consequences of this can be a major source of error
71 in deducing lava eruption characteristics from final deposit morphology observed by
72 remote sensing (Kolzenburg et al., 2018). We use these various developments to
73 assess the potential environment of RMDS formation, describing the basic
74 characteristics of these features that must be accounted for by any theory of their
75 origin. We then develop a model of the dynamics of mare lava flow emplacement and
76 use this to explore in detail the hypothesis that RMDS formation involves the
77 production of magmatic foams and their extrusion through a chilled upper lava flow
78 boundary layer. We conclude with predictions of the internal structures of RMDSs
79 and propose tests that can be undertaken with future observations of the global
80 distribution and characteristics of RMDSs.

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83 2. Characteristics of Ring Moat Dome Structures:

84 Following the initial recognition of these features (Schultz et al., 1976; Schultz,
85 1976), Zhang et al. (2017) used new LRO Lunar Reconnaissance Orbiter Camera
86 (LROC) data to analyze and characterize the distribution and morphology of RMDSs,
87 and digital terrain models (DTMs) to document their morphometry (Zhang et al.,
88 2017, 2018a, 2018b). RMDSs are generally circular in shape (Figure 1), have a
89 dome-like morphology with a surrounding moat, and are often concentrated in
90 clusters (Zhang et al., 2017). RMDSs have only been found in certain mare regions
91 (Figure 2b) and have a mineralogy similar to that of the surrounding lava, suggesting
92 no major compositional difference between the RMDSs and the surrounding maria
93 (Zhang et al., 2017). Detailed morphometric measurements (Figure 2c) using DTMs
94 showed that of the 512 RMDSs measured, the mound diameters range from 68-645 m

95 (median 192 m), the mound heights range from 0.38 m to 13.4 m (median 3.41 m),
 96 the height-to-diameter ratios are small (0.01–0.04) and the slopes are very gentle
 97 (1.5–5°), increasing toward the mound margins (Zhang et al. 2017). Theories of
 98 RMDS origin must be able to account for these major characteristics of size, shape,
 99 morphology and morphometry, clustering, and mineralogical similarity to the adjacent
 100 maria in which they are located. We therefore begin by assessing the mechanisms by
 101 which the underlying lava flows were emplaced.

102

103

104 **3. Emplacement of mare lava flows:**

105 Mafic eruptions on the Earth and Moon differ in that the source depths of lunar
 106 basalts are an order of magnitude greater than is typical on Earth (Hess, 2000; Grove
 107 and Krawczynski, 2009). The characteristics of large mare lava flows can be modeled
 108 in terms of the processes that must occur when giant dikes rise from the deep mantle
 109 and interact with the crust (Wilson and Head, 1983; 2017a; Head and Wilson, 1992).
 110 The low viscosity of lunar basalts (Murase and McBirney, 1970), coupled with the
 111 great widths of dikes of the size needed to explain the erupted volumes of large mare
 112 flows (Head and Wilson, 2018; Wilson and Head, 2017a), implies very high rise
 113 speeds for the dikes as they approach the surface. The high initial rise speed of a
 114 dike, coupled with its deceleration as it progressively loses buoyancy on penetrating
 115 the crust and is eventually forced to decrease in width due to compressive tectonic
 116 forces, leads to a predictable pattern of magma discharge rate as a function of time
 117 (Wilson and Head, 2018a). Typical examples of dikes producing long (up to several
 118 hundred km), large-volume (200-400 km³) flows (Head and Wilson, 2017) involve
 119 initial dense rock equivalent volume fluxes, F , of $\sim 10^6$ m³ s⁻¹ decreasing over the
 120 course of a few days to 10^5 m³ s⁻¹ and then decreasing more slowly over some tens of
 121 days to $\sim 10^4$ m³ s⁻¹ (Wilson and Head, 2017a). The lava flows leaving the vent are
 122 initially turbulent and remain so until F decreases below $\sim 3 \times 10^4$ m³ s⁻¹. Calculations
 123 of the dynamics of emplacement of such flows (Wilson and Head, 2018b) can be used
 124 to predict the initial thickness, D_f , and mean speed, U_f , of the flow as a function of
 125 total volume flux F and the flow width W_f . Figure 3 shows these variations for a flow
 126 erupted onto the present-day mean surface slope of SW Mare Imbrium, 0.086 degrees.
 127 F is predicted to decrease by ~ 2 orders of magnitude with time whereas W_f decreases
 128 much less, typically by a factor of ~ 3 from ~ 15 km to ~ 5 km. A curve is shown on
 129 each part of Figure 3 indicating how D_f and U_f at the vent would change with time
 130 during a specific eruption: the label "A" in Figure 3 marks the values at the start of the
 131 eruption and the label "B" marks values at the end.

132

133 As a flow advances, it loses heat at all of its margins; however, as long as it
 134 remains turbulent, heat loss is dominated by radiation at the upper flow surface (Head
 135 and Wilson, 2018). The temperature decrease causes crystallization, with latent heat
 136 release helping to offset heat losses. The presence of the resulting solids in the flow
 137 increases the bulk viscosity and introduces a yield strength. The consequent non-
 138 Newtonian rheology can be modeled as that of a Bingham plastic (Wilson and Head,
 139 2018b), requiring evaluation of both a Reynolds number and a Hedström number to
 140 characterize the motion. Turbulence continues as long as the Reynolds number
 141 remains greater than a critical value that is itself a function of the Hedström number
 142 (Skelland, 1967). Once turbulence has vanished, the flow quickly develops a cool
 143 upper surface, and heat loss from that surface becomes limited by conduction through
 144 the growing crust. As a consequence of the previous turbulence, the lava between the

145 growing thermal boundary layers is essentially isothermal, so that the temperature and
 146 rheology of the lava in the core of the flow now change very much more slowly. It is
 147 easy to show by evaluating the Grätz number, a measure of the extent of the
 148 penetration of cooling into the laminar flow (Pinkerton and Wilson, 1994), that flows
 149 of the scale of the large mare lavas ultimately stop for a combination of reasons, not
 150 only as a result of cooling (Wilson and Head, 2017a; Head and Wilson, 2018). As the
 151 flow advances, the thicknesses of the cooling upper and lower thermal boundary
 152 layers increase. However, the upper part of the lava in the central channel flows as a
 153 rigid unsheared plug as a result of the presence of the yield strength, and we find that
 154 the plug thickness is in all cases greater than the thickness of the upper thermal
 155 boundary layer. The flow stops advancing when the growing lower cooling layer and
 156 the thickening plug meet, so that no part of the lava can undergo shearing. For a
 157 typical mare basalt, the core of the flow, between the upper and lower thermal
 158 boundary layers, will have cooled through 30% of the interval between its liquidus
 159 and solidus, will contain 30% crystals, will have a bulk viscosity of 12 Pa s, and a
 160 yield strength of 175 Pa.

161

162 Although there is some reduction in advance speed and increase in thickness of
 163 the front of a flow as it moves away from the vent, this is partly compensated by the
 164 fact that the eruption rate is decreasing with time, and as a consequence the distal
 165 parts of the large lunar mare lava flow deposits are expected to have thicknesses
 166 comparable to the thicknesses that the lava forming them had on leaving the vent.
 167 The consequence of this is that the flow thicknesses at the points labeled "A" and "B"
 168 in Figure 3 can be regarded, to a good approximation, as being the flow thickness in
 169 the proximal, D_p , and distal, D_d , parts, respectively, of a given lava flow deposit. For
 170 this example, by the time the lava at the $D_d = 14$ m high flow front, erupted from an
 171 initially 15 km long fissure, has reached its furthest extent from the vent, the vent will
 172 be erupting a stream of lava approximately $D_p = 4$ m in thickness from a 3 km long
 173 fissure.

174

175

176 **4. Characteristics of mare lava flows:**

177 In order to understand the possible subsequent development of large mare lava
 178 flow fields produced under the conditions shown in Figure 3 it is necessary to define
 179 the internal structure of the lava in the various parts of such a field (Head and Wilson,
 180 2018). Lunar magmas are erupted into a vacuum, and the presence of even very small
 181 amounts of volatiles can ensure that explosive activity occurs (Wilson and Head,
 182 1981). Based on direct analysis of returned pyroclast samples and high-pressure
 183 laboratory experiments on samples with the same composition, lunar magma volatiles
 184 are found to be dominated by up to ~1000 ppm CO released mainly at depths between
 185 500 and 50 km with an admixture of at least several hundred ppm H₂O and sulfur
 186 species released at depth less than 500 m (Rutherford et al., 2017). The expansion of
 187 gas bubbles nucleating with initial diameters of ~10 μ m causes close packing to occur
 188 when the bubbles have grown to a few hundred microns, and the magma is then
 189 fragmented into sub-mm size pyroclastic droplets to emerge from the vent in a
 190 hawaiian-style fire fountain or curtain-of-fire eruption fed by a lava volume flux of
 191 $\sim 10^6$ m³ s⁻¹ (Wilson and Head, 2017a). The combination of small droplet size and
 192 large droplet numbers in the fountains causes them to be optically dense, i.e., other
 193 than at the very outermost edges of the fountain, droplets obscure one another's ability
 194 to radiate heat. As a result, droplets fall to the ground at magmatic temperatures and

195 coalesce into a lava lake that feeds lava flows. After they leave the immediate
 196 vicinity of the vent, these droplets are exposed to a hard vacuum. Also, the time they
 197 spend in flight is greater than it would be on Earth for a given eruption speed by a
 198 factor of ~ 6 because of the low acceleration due to gravity on the Moon. As a result,
 199 the droplets should very efficiently lose almost all of their residual volatiles. The lava
 200 flows generated from the earliest phase of an eruption are therefore expected to have
 201 an extremely low vesicularity, and it is these flows that form the distal parts of the
 202 resulting flow field.

203

204 By the end of an eruption the magma volatile inventory will not have changed
 205 significantly, but the erupted volume flux F will have decreased dramatically to $\sim 10^4$
 206 $\text{m}^3 \text{s}^{-1}$. The simulations of lunar fire fountains given by Wilson and Head (2017a)
 207 show that, despite this reduction in F , if a stable fire fountain exists it will still be
 208 retaining almost all of its heat and feeding hot, vesicle-free flows. However, the
 209 reduction in F with time implies a reduction in the rise speed, U_d , of the magma rising
 210 through the dike feeding the eruption, and this has important consequences for the
 211 eruption style. Gas bubbles nucleating in rising magma grow from their initial
 212 diameters of $\sim 10 \mu\text{m}$ as volatiles in the surrounding liquid diffuse into them, and also
 213 expand due to the decreasing pressure. As the bubbles grow in size their buoyancy-
 214 driven rise speed through the magmatic liquid increases, but as long as that speed is
 215 much less than the rise speed of the magma itself through the dike, bubbles are
 216 effectively uniformly distributed in the magma.

217

218 If the magma rise speed U_d becomes small enough this is no longer true; larger,
 219 earlier-nucleated bubbles can overtake later-formed, smaller bubbles and coalescence
 220 can occur, leading to an increase in rise speed of the new, even larger bubbles. In the
 221 extreme case of very small values of U_d , giant bubbles called slugs form, filling the
 222 conduit apart from a thin veneer against the walls, and absorbing almost all of the
 223 smaller bubbles in the liquid (Suckale et al., 2010; Pering and McGonigle, 2018). The
 224 lava lake around the vent is now no longer fed by pyroclastic droplets falling from
 225 above but instead is punctured by slugs emerging from depth and throwing off clots of
 226 magma as they burst through the lake surface in strombolian explosions (Blackburn et
 227 al., 1976). Wilson and Head (1981) showed that the transition between intermittent
 228 strombolian and relatively steady hawaiian explosive activity on the Moon would
 229 have occurred at magma rise speeds between $\sim 0.1 \text{ m s}^{-1}$, low enough to encourage gas
 230 bubble coalescence, and 0.5 m s^{-1} , fast enough to inhibit coalescence. The speed U_d is
 231 related to the magma volume flux F via the product $F = U_d W L$ where W and L are
 232 the horizontal width and length, respectively, of the feeding dike. For the Moon,
 233 Head and Wilson (2017) estimate typical values of $\sim 10 \pm 5 \text{ km}$ for L and $9 \pm 4 \text{ m}$ for
 234 W . As a result, all eruptions with F greater than $10^5 \text{ m}^3 \text{ s}^{-1}$ are expected to be
 235 hawaiian, and all with F less than $\sim 3 \times 10^3 \text{ m}^3 \text{ s}^{-1}$ are expected to be strombolian. The
 236 transition between these eruption styles for fissure lengths in the 5-15 km range
 237 occurs for values of F between $\sim 4 \times 10^4$ and $2 \times 10^4 \text{ m}^3 \text{ s}^{-1}$. Thus, at some stage late
 238 in a typical eruption, when F has decreased to less than $\sim 10^4 \text{ m}^3 \text{ s}^{-1}$, the activity will
 239 have become strombolian.

240

241 The lava flows emplaced during strombolian activity on the Moon will have
 242 distinctive characteristics. Recall that these flows are fed by the outflow from the
 243 vent lava lake of magma that has been smeared against the walls of the dike by rising
 244 gas slugs and has then risen into the base of the lava lake. Experiments by Llewellyn

245 et al. (2012) show that typically 84% of the initial volatiles would have been removed
246 from this magma, so that initial volatile contents as large as 1000 and 2000 ppm
247 would have been reduced to 160 and 320 ppm, respectively. This lake- and flow-
248 feeding liquid will contain mainly small bubbles of the gas species that exsolved at
249 low pressures in the upper ~500 m of the dike after the last passage of a slug and have
250 grown as they approach and enter the lake. Since water is the main volatile released
251 at less than 500 m depth (Rutherford et al., 2017) we use its physical properties in the
252 illustrations that follow. In general, the pressure, P_b , in the bubbles will be controlled
253 by the surface tension, σ , of the gas-liquid interface and will be of order $(2 \sigma / \phi)$
254 where ϕ is the bubble diameter and $\sigma = \sim 0.37 \text{ J m}^{-2}$ (Mangan and Cashman, 1996).
255 For bubbles nucleating with $\phi = 10 \text{ }\mu\text{m}$, $P_b = 74 \text{ kPa}$. If these bubbles nucleate at 500
256 m depth and rise to within 0.1 m of the surface they will have grown to $\sim 170 \text{ }\mu\text{m}$ and
257 will have internal pressures of $\sim 4 \text{ kPa}$; at 1 cm depth the diameters are $\sim 370 \text{ }\mu\text{m}$ and
258 the pressures $\sim 2 \text{ kPa}$.

259

260 It can readily be shown that for the up to ~ 1000 ppm mainly water contents of
261 lunar magmas, bubbles within a few meters of the surface will, if stable, constitute an
262 extremely vesicular foam (Wilson and Head, 2017b). At the surface of the lake, gas
263 bubbles may explode into the overlying vacuum. In theory, bubbles in contact with a
264 vacuum should have expanded to an infinite size so that the pressure within them is
265 zero, and the only reason for their collapse is the drainage of liquid through the thin
266 films between the bubbles. In practice the system is complex because the surface of
267 the lake will be radiating heat to the vacuum and so the liquid films will rapidly
268 solidify, adding a mechanical strength to the system. Fielder et al. (1967) exposed
269 liquid basalts to low pressures and found that gas bubbles ceased to expand and
270 formed a $>90\%$ vesicular foam of sub-mm sized bubbles when the ambient pressure
271 fell below 3 kPa; while this appears to be generally in agreement with the above
272 discussion, the pre-melting volatile (presumably mostly water) contents of these
273 basalts were not measured, and radiative cooling may have influenced the behavior of
274 the small samples used.

275

276 As a result, in modeling foam lavas of this kind, Wilson and Head (2018b)
277 adopted the conservative assumption that a wave of instability would spread down
278 into a lava lake containing foams of this kind until the accumulated debris of broken
279 bubble walls and collapsed interstitial liquid films reached a great enough thickness
280 that its weight exerted a high enough pressure to reduce the vesicularity to 65%, a
281 value commonly observed in pumiceous pyroclasts and similar to the value 0.69
282 suggested by Jaupart and Vergnolle (1989). Assuming a porosity of 30% for the
283 debris layer material, debris layer thicknesses of ~ 0.5 , 1.7 and 3.5 m were found for
284 initial magma water contents of 100, 200 and 300 ppm. Beneath the debris layer, the
285 vesicularity of the foam is controlled by the overlying pressure, both as regards its
286 effect on the volume of bubbles and on the exsolution of volatiles: a high enough
287 pressure will ensure that none of the water is exsolved. Figure 4 shows the resulting
288 vesicularity as a function of depth for the above three water contents in a flow with
289 the 4 m thickness expected near the end of a mare basalt eruption. The implications
290 of this figure are that if the residual water content of the magma is sufficiently small,
291 most of it remains in solution in the lower part of the lava flow. Thus, in Figure 4a,
292 for 100 ppm remaining, 90% of the flow retains dissolved water; in Figure 4b, for 200
293 ppm remaining, a little less than half of the flow does so; and in Figure 4c, for 300
294 ppm volatiles remaining, none of the flow retains water and the flow consists only of

295 a debris layer overlying a very vesicular layer. Figure 4b defines the depth to the top
 296 of the lava layer still containing dissolved water, D_t , and the thickness of that layer,
 297 D_w , for use in Section 5.1, and indicates the progressive changes with increasing
 298 depth within the flow.

299
 300

301 **5. Proposed RMDS formation mechanism:**

302 *5.1. Flow inflation:*

303 The presence towards the end of the eruption of a stationary mare lava flow
 304 field of volatile-poor, non-vesicular lava in the distal part of the field and the
 305 availability of lava still containing dissolved water being erupted into the proximal
 306 part of the field strongly suggests a mechanism for producing RMDSs. The process is
 307 closely related to the behavior inferred for many lava fields on Earth (Aubele et al.,
 308 1988; Hon et al., 1994; Self et al., 1996, 1998; Thordarson and Self, 1998): the
 309 relatively rapid emplacement of long flows, followed by the injection of later
 310 magmatic liquid into these stationary flows causing an initial phase of inflation.
 311 Subsequently, and on a time scale of weeks after all lava motion has ceased,
 312 continued cooling of the now composite flow interior causes crystallization. Volatiles
 313 still present in the injected lava behave incompatibly and are not incorporated into the
 314 crystals, and so become increasingly concentrated in the residual liquid phase, rapidly
 315 becoming supersaturated and causing second boiling, i.e. rapid additional gas release,
 316 producing very vesicular foam layers within the flow and leading to segregation
 317 structures. Second boiling has been invoked to explain some of the internal
 318 morphology of various types of lava flows on Earth (Morey, 1922; Sisson and Bacon,
 319 1999; Beresford et al., 2002), including flood-basalts (Self et al., 1996). The process
 320 will be more dramatic on the Moon where low acceleration due to gravity and absence
 321 of atmospheric pressure encourage release of greater amounts of volatiles and greater
 322 expansion of them after release. We propose that it is the escape of the internally-
 323 formed foam layers onto the surface of the flow that forms the RMDSs. The key
 324 requirement is not just the inflation of the initial flow deposits, it is the presence of
 325 still-dissolved volatiles in the lava that is being injected to cause the inflation (see
 326 Figure 5 for details), and the forced exsolution of these volatiles as the lava cools.

327

328 We take as our starting point the flow field development represented by Figure
 329 3. Vesicle-free distal flows $D_d = 14$ m thick produced by the high erupted volume
 330 flux early in the eruption are connected to proximal flows $D_p = 4$ m thick generated
 331 just after the change to laminar motion in the lava leaving the fissure vent produces
 332 flows having structural profiles like those in Figure 4. Although there is continuity
 333 between the hot interiors of the lava at all distances from the vent, we do not think
 334 that it is likely that all of the proximal lava will be involved in the inflation of the
 335 distal flows. The fragmental layer at the top of the proximal flows is likely to be
 336 easily sheared, but the <65% vesicular layer immediately beneath it will have a higher
 337 viscosity than the vesicle-free lava at the base which still contains dissolved water. It
 338 therefore seems likely that only the vesicle-free and therefore very low viscosity lava
 339 from the lower parts of the proximal flows will be injected into the interiors of distal
 340 flows to cause inflation and contribute water to cause second boiling. Comparison of
 341 the three parts of Figure 4 shows that the larger the amount of water retained, the
 342 smaller the vertical extent of the part of the flow that contains it, until, for a large
 343 enough volatile content, there is no very low-viscosity, vesicle-free, water-retaining
 344 lower layer available for causing an injection of the kind postulated.

345

346 Table 1 shows the consequences of the injection process for the range of values
 347 of residual dissolved volatile contents, n_{res} , in the lower parts of 4 m thick proximal
 348 lavas that can readily be injected into the 14 m thick distal part of the flow field
 349 (Figure 5). For this range of residual water contents, values are given for the depth,
 350 D_t , to the top of the water-retaining lower layer, the thickness of the water-retaining
 351 layer, D_w , and the thickness of the inflated distal lava flow after this injection. The
 352 intrusion process takes place after the eruption rate at the vent has become less than
 353 $\sim 3 \times 10^4 \text{ m}^3 \text{ s}^{-1}$, which Wilson and Head (2018b) show occurs after a time, τ , of 10-
 354 100 days. The distal flow will have been cooling during this period and will have
 355 developed thermal boundary layers at its upper and lower surfaces (Figure 5a), each
 356 having a thickness λ of $\sim 2.3 (\kappa \tau)^{1/2}$ (Turcotte and Schubert, 2002) where κ is the
 357 thermal diffusivity of the lava, $\sim 10^{-6} \text{ m}^2 \text{ s}^{-1}$, and using $\tau = 20$ days, $\lambda = \sim 3$ m. Thus,
 358 only the central ($14 - 2 \times 3 =$) 8 m of the distal flow will still be at close to magmatic
 359 temperature and it is with this lava that the injected lava mixes. Column 4 of the table
 360 gives the result of adding the 14 m total thickness of the distal flow to the thickness of
 361 the injected proximal lava in column 3 to give the new thickness of the inflated flow,
 362 D_i (Figure 5b). Column 5 shows the result of sharing the residual volatile content n_{res}
 363 of the injected lava with the 8 m thick flow core to produce a mean volatile content,
 364 n_m , in the inflated core. Note that, due to the vertical structure of the proximal flows
 365 shown in Figure 4, the dissolved volatile content of the core after the injection is a
 366 maximum for a residual volatile content of ~ 175 ppm, and is zero if n_{res} is greater than
 367 ~ 280 ppm.

368

369 *5.2. Flow cooling:*

370

Following cessation of eruptive activity at the vent, this mixture of old and new
 371 lava (Figure 5b) now continues to cool with no further significant horizontal
 372 movement. Waves of cooling continue to propagate into the lava from all of its
 373 boundaries. The great length and width of the flow relative to its thickness means that
 374 this can be treated as a one-dimensional problem with a planar cooling front
 375 propagating down from above and up from below. As crystallization induced by this
 376 cooling progresses, dissolved water is concentrated into the residual liquid, and this
 377 quickly becomes supersaturated so that second boiling takes place and gas bubbles
 378 nucleate in two expanding layers, one just below the upper cooling front and the other
 379 just above the lower cooling front (Figure 5c). We assume that the fraction of the
 380 residual water that is released is directly proportional to the degree of crystallization,
 381 i.e. to the volume fraction of crystals in the magma, v_c , and that the process is efficient
 382 because of the presence of the crystals as nucleation sites. The water nucleates small
 383 ($\sim 10 \mu\text{m}$) bubbles, the presence of which causes vertical expansion of the region they
 384 occupy to form a vesicular layer. The density of the water vapor and the bulk density
 385 and vesicle volume fraction at any point in the vesicular layer that is produced can be
 386 found from the local magma temperature, T , and pressure, P , the latter being the
 387 weight of the overlying flow material, i.e. the lithostatic pressure:

388

389

$$P = g \rho D \quad (1)$$

390

391 where g is the acceleration due to gravity, ρ is the density of the magmatic liquid,
 392 close to 3000 kg m^{-3} for all lunar basalts, and D is the depth of the point being
 393 considered below the surface of the flow before any inflation has taken place. This is
 394 a good approximation to the pressure because, although gas release causing inflation

395 increases the depth of a point below the surface, it does not, due to the small masses
 396 of gas involved, add significantly to the overlying total mass and hence weight and
 397 pressure. The local bulk density, β , of the vesicular lava is

$$398 \quad \beta = [(n Q T) / (m P) + (1 - n) / \rho]^{-1} \quad (2)$$

400

401 where n is the mass fraction of water released, Q is the universal gas constant, 8.314
 402 kJ kmol⁻¹ K⁻¹, T is taken as 1700 K, and m is the molecular weight of water, 18.02 kg
 403 kmol⁻¹. The vesicularity, v_b , i.e. the bubble volume fraction, of the lava is

404

$$405 \quad v_b = n Q T \rho / [n Q T \rho + (1 - n) m P] \quad (3)$$

406

407 With an assumption about the specific composition of the basaltic liquid, the
 408 bulk viscosity of the vesicular lava, η_b , can be evaluated from the temperature-
 409 dependent viscosity of the liquid alone, η_l , the fractional volume occupied by the
 410 crystals that have already formed, v_c , and the fractional volume occupied by the gas
 411 bubbles, v_b . A suitable formulation shown to be applicable to terrestrial basalts
 412 (Harris and Allen, 2008) when the gas bubbles are smaller than the crystals, as is
 413 likely to be the case here, is that of Phan-Thien and Pham (1997):

414

$$415 \quad \eta_b = \eta_l \{1 - [v_b / (1 - v_c)]\}^{-5/2} (1 - v_c)^{-1} \quad (4)$$

416

417 where a power law of the kind shown by Hulme (1973) to be suitable for lunar
 418 basalts, when fitted to the viscosity data for a low-Ti mare basalt analyzed by
 419 Williams et al. (2000), gives

420

$$421 \quad \eta_l = (1582.21 / T)^{11.5826} \quad (5)$$

422

423 High-titanium basalts have a viscosity about a factor of two smaller (Williams et al.,
 424 2000). This slightly delays the change from turbulent to laminar flow mentioned in
 425 Section 3.

426

427 The remaining quantity required to solve the above equations is the temperature
 428 in the cooling flow, which varies with both depth and time. We are now dealing with
 429 a static flow that has developed a crust, the upper surface of which is maintained at a
 430 temperature very close to the lunar ambient by radiative exchange with its
 431 surroundings, and cooling is taking place by conduction to the surface and into the
 432 substrate (Figure 5c). We have approximated this process using an analytical model
 433 given by Carslaw and Jaeger (1959) for a layer of material of thickness D_i with an
 434 initial internal temperature T_i emplaced on a substrate at temperature T_s with the
 435 surface temperature abruptly set to T_s and maintained there. In our case T_i is the
 436 eruption temperature of the lava, taken to be the liquidus of the above low-Ti mare
 437 basalt, 1713 K, T_s is the ambient lunar surface temperature assumed to average 200 K
 438 over the day-night cycle, and D_i is the thickness of the distal flow after injection of the
 439 proximal lava but before any second boiling, obtained from Table 1. Defining $\delta = T -$
 440 T_s and $\Delta = T_i - T_s$, the solution for the temperature T as a function of depth D and time
 441 t is

442

$$443 \quad \delta = 0.5 \Delta \{2 \operatorname{erf} [D / K] - \operatorname{erf} [(D - D_i) / K] - \operatorname{erf} [(D + D_i) / K]\} \quad (6)$$

444

445 where $K = 2 (\kappa t)^{1/2}$. This treatment is an approximation for several reasons. It
 446 assumes that the substrate has the same thermal properties as the hot layer, but this is
 447 reasonable for new lava flows overlying older ones in the maria, especially as the
 448 thickness of regolith developed on earlier flows (at rates of $\sim 5 \text{ mm Ma}^{-1}$, Hörz et al.,
 449 1991) will generally be no more than a few percent of the thickness of a new flow. It
 450 ignores the thermal effects of latent heat release during crystallization and also
 451 ignores the fact that the presence of gas bubbles will modify the thermal diffusivity.
 452 The likely effect is that the model underestimates the time taken for the flow to reach
 453 a given configuration, but as we are more concerned with the physical consequences
 454 of vesiculation rather than the exact time at which they occur, this is acceptable.

455

456 We again adopt our nominal model of the basal part of a 4 m thick proximal
 457 flow providing lava to be injected into a 14 m thick distal flow (Figure 5a, 5b) and
 458 assume that the residual volatile content of the proximal lava is 100 ppm water. Table
 459 1 then shows that 3.42 m thickness of lava is injected, initially inflating the distal flow
 460 to a thickness of 17.42 m (Figure 5b). The mixing of the injected lava with the 8 m
 461 thick hot but volatile-free core of the distal flow reduces the effective water content of
 462 the molten lava to 30 ppm. The distal flow has already undergone enough cooling
 463 during the 20 days between its emplacement and the injection event to produce a 3 m
 464 layer of solid lava at its top and base. The subsequent development of the internal
 465 structure of the resulting combined flow body is now calculated as a function of time
 466 as further cooling takes place (Figure 5c-e). After each time increment, the amount of
 467 crystallization in the molten interior at a series of depths is calculated as a function of
 468 the local temperature, and the corresponding mass fraction of water exsolved is found.
 469 The local temperature and pressure are used to find the density of the gas, and the gas
 470 density and mass fraction together define the local bulk density of the lava. Finally,
 471 the volume fractions of crystals and gas bubbles determine the bulk liquid viscosity.

472

473 Figures 6a-6e show the variations of the key parameters with depth below the
 474 surface of the flow, (i) just before, (ii) just after, and at time intervals of (iii) 20, (iv)
 475 30 and (v) 55 days after the injection event. The initially 14 m thick flow (Figure 5a)
 476 is inflated to a total thickness of 17.42 m by the injection of the as-yet unvesiculated
 477 but volatile-bearing lava (Figure 5b), and is then inflated to total thicknesses of 19.14,
 478 24.56 (Figure 5c) and 33.76 m (Figure 5d) after 20, 30 and 55 days, respectively, due
 479 to the volume of foam generated by gas released as the injected lava cools. The
 480 successive parts of Figure 6 show, as a function of depth below the flow surface, D ,
 481 the temperature, T , crystal volume fraction, v_c , gas bubble volume fraction, v_b , bulk
 482 density, β and, where liquid is still present, the bulk viscosity, η_b , of the remaining
 483 crystal- and bubble-rich liquid lava. At both 20 and 30 days there is still a small
 484 region in the core of the flow where the temperature is still at the liquidus, but it is
 485 shrinking in extent. Both above and below this hot core, zones containing gas bubbles
 486 are present. The pressure due to the weight of the overlying material is less in the
 487 upper vesicular layer than in the lower layer, and so the vesicularity is greater in the
 488 upper layer than in the lower one (Figures 5c, 6). By 55 days all parts of the interior
 489 are below the liquidus and therefore contain some proportion of gas bubbles. The
 490 total vertical expansion of the flow due to the presence of the gas bubbles formed
 491 during the cooling process is $(33.76 - 17.42 =) 16.34 \text{ m}$. Furthermore, despite the
 492 presence of the bubbles and crystals, the inherently low viscosity of lunar basalt
 493 means that almost all of this lava has a bulk viscosity less than $\sim 30 \text{ Pa s}$, with much of

494 it less than 3 Pa s, making it potentially very mobile. We adopt $\eta_b = 10$ Pa s as a
 495 conservative representative value in the subsequent calculations.

496

497 *5.3. Subsequent flow evolution:*

498 Vesicularity (i.e. gas bubble volume fraction) profiles like those shown in
 499 Figures 6c and 6d have been observed in many mafic lava flows on Earth at a variety
 500 of scales, from flows only a few meters thick at Surtsey (Sigmarsson et al., 2009) to
 501 flow units at least 20 m thick in the Columbia River flood basalt sequence (Hartley
 502 and Thordarson, 2009). Terrestrial flows with continuously vesicular regions in their
 503 centers appear to be very rare (but see Reidel, 2005, for a possible example), but this
 504 may be because gas bubbles have migrated out of the hottest central parts of these
 505 flows to be trapped in solidification fronts (Thordarson and Self, 1998; Hartley and
 506 Thordarson, 2009). Indeed, a common feature of all of these flows is the presence of
 507 segregation features, especially vesicle pipes, in which vesicle-rich liquid from the
 508 lower vesicular zone moves up through the core of the flow (Goff, 1996; Hartley and
 509 Thordarson, 2009). In some flows, unusually large "megavesicles" are seen at the
 510 bases of the upper vesicular zones (Sigmarsson et al., 2009). These comparisons
 511 strongly suggest that segregation structures will have formed in the lunar flows as gas
 512 bubbles migrate from the lower to the upper part of the flow core as shown in Figure
 513 5e. The bulk density profile in Figure 6e shows that after 55 days the lava in the
 514 lower vesicular zone has attained its greatest buoyancy, thus encouraging its upward
 515 migration. Since the central core of the flow is the hottest part of the system and has
 516 the lowest bulk viscosity, it is entirely possible the rather than gas bubbles migrating
 517 out of the lower vesicular zone a Rayleigh-Taylor instability may drive the entire
 518 mass of foam upward. The centers of the upper and lower vesicular zones after 30 and
 519 40 days are at depths of ~ 4 and ~ 17 m, where the pressures due to the overlying lava
 520 are ~ 16 and 80 kPa, respectively. If vesicular lava migrates from the lower to the
 521 upper zone (Figure 5e), the pressure it experiences will decrease by a factor of $(80/16$
 522 $\Rightarrow) 5$ and the sizes of the gas bubbles it contains will have expanded by a factor of $(5^{1/3}$
 523 $\Rightarrow) 1.71$. The significant differences between conditions in lava flows on the Moon
 524 and the Earth can be highlighted by noting that on Earth the pressures at the above 4
 525 and 17 m depths in a flow would be 198.7 and 593.9 kPa, accounting for the greater
 526 value of g and the Earth's atmospheric pressure of 100 kPa. The pressure reduction
 527 ratio would therefore be only $(\sim 593.9/198.7 \Rightarrow) 2.989$ and the bubble expansion factor
 528 $(2.989^{1/3} \Rightarrow) 1.44$, significantly smaller than in the lunar case. The greater expansion
 529 of all bubbles added to the upper vesicular zone from the lower zone increases the
 530 inflation of the entire flow slightly but more importantly makes the vesicular lava in
 531 the upper zone even more buoyant than it was before. Combined with the low
 532 viscosity of the vesicular layer, these conditions strongly encourage escape of the
 533 vesicular lava through any fractures that form in the ~ 3 meter thick cooled crust of the
 534 flow (Figure 5e). We now explore the factors potentially influencing this process.

535

536 *5.4. Crack formation:*

537 The calculations above have been made for a uniformly thick distal flow
 538 assuming that the injection of proximal lava takes place everywhere within it, leading
 539 to uniform inflation. In practice, lava flows on the Moon are typically emplaced onto
 540 a previously emplaced lava flow with an irregularly impact-cratered surface.
 541 Rosenberg et al. (2011) describe a method of characterizing topographic roughness of
 542 planetary surfaces. The procedure uses digital altimetry data to calculate the RMS
 543 deviation of the slope as a function of the baseline length scale at which the slope is

544 measured and to plot the logarithm of this quantity as a function of the logarithm of
 545 the baseline length. Most lunar highland surfaces produce a straight line on such a
 546 plot implying a single fractal law governing the change in roughness with scale, the
 547 consequence of impact cratering of the ancient anorthositic crust. However, the
 548 younger lunar mare surfaces have more complicated plots, characterized as bilinear
 549 or, most commonly, complex, with a distinct break in slope at a scale length in the
 550 range ~200 m to ~700 m, indicating a change at this spatial wavelength from
 551 topography dominated by small-scale impact gardening to that controlled by the
 552 emplacement mechanisms of individual mare lava flows. We assume therefore that
 553 broad-scale variations in the thickness of new flows will occur mainly on these 200-
 554 700 m scales driven by the presence of earlier volcanically-controlled, rather than
 555 impact-controlled, topography. Inflation will be greater where flows are thicker,
 556 causing differential stresses and a non-random spatial distribution of fractures through
 557 which extrusions can take place. Furthermore, field experience of the patterns of
 558 inflation of compound pahoehoe flow systems on Earth shows that the interiors of the
 559 flows are clearly not laterally homogeneous, and that preferred, and meandering,
 560 pathways develop within them (Vye-Brown et al., 2013; Khalaf and Hamed, 2016;
 561 Rader et al., 2017). The same is likely to be true of inflating flows on the Moon.

562
 563 The local slopes, α , of lunar mare surfaces have been analyzed by Kreslavsky et
 564 al. (2013); these show that at length scales, L , of 200-700 m they are of order 10^{-2} to 6
 565 $\times 10^{-3}$ (Kreslavsky, pers. comm., 2018). We have seen that inflation can double the
 566 total thickness of a flow. So, if two parts of a flow field are separated by the above
 567 typical length scales of $L = 200-700$ m and the above slopes exist between them, the
 568 flow in the lower elevation region is thicker than that in the shallower region by ~2 to
 569 ~4 meters, respectively. Initially both parts of the flow field can be assumed to have
 570 their surfaces at the same, equipotential, level. However, after inflation by a factor of
 571 2, the surface of the thicker part of the flow will have risen by an amount of 4 to 8
 572 meters and will stand 2 to 4 meters above the originally shallower part of the flow.
 573 Thus, the cooled crust of the flow will have been flexed by this amount.

574
 575 When flexing leads to fracture formation, fractures in the upper crust of a flow
 576 will likely have geometries similar to those of tumuli and similar features seen on the
 577 surfaces of inflating lava flows on Earth (Walker, 1991; Duraiswami et al., 2001;
 578 Duncan et al., 2004) and illustrated in the upper part of Figure 7. In one dimension
 579 the width, W , of a fracture can be estimated from the lower part of Figure 7. The
 580 relationships are $c = 0.5 L$, $0.5 W = c - b$, $c^2 = a^2 + b^2$, and $a / c = \alpha$ which, since α is
 581 small, combine to give

$$582 \quad 583 \quad W = (L / 2) \alpha^2 \quad (7)$$

584
 585 and so for L in the range 200-700 m, W is in the range 10 to 13 mm. These crack
 586 openings correspond to vertical uplift of the sides of the crack by 1 to 2 m.

587
 588 The opening of cracks is likely to begin as an episodic process. Slow cooling of
 589 the flow core produces steady inflation over a period of tens of days. At some point a
 590 crack forms in the lava crust. This exposes the top of the upper layer of vesicular lava
 591 foam to the external vacuum, and the bubbles in the top layer explode, allowing a
 592 mixture of released gas and chilling bubble wall glass shards to be ejected through the
 593 crack (Figure 8a). A wave of explosive decompression travels down into the foam

594 layer (Jaupart and Vergnolle, 1989), and an acoustic wave also travels away from the
 595 crack into the foam as a result of the pressure reduction at the base of the crack.
 596 These waves will have similar speeds, of order tens of m s^{-1} (Kieffer, 1977). The
 597 foam layer lava responds to the acoustic wave by accelerating toward the crack, but it
 598 is easy to show that the decompression wave will travel away from the crack very
 599 much faster than the vesicular magma can flow toward it. Disaggregated foam in the
 600 form of gas and liquid droplets (with sizes of $\sim 10\text{-}20\ \mu\text{m}$, the same order as the gas
 601 bubble size) will exit explosively through the crack leaving a potential space, so that
 602 the overlying crust is unsupported, and in extreme cases large-scale collapse of the
 603 crust into the space vacated by the entire foam layer could occur (Figure 8b). Large-
 604 scale collapse may be linked to the formation of some types of the Irregular Mare
 605 Patches seen on mare surfaces (Braden et al., 2014; Qiao et al., 2017, 2018a, 2018b)
 606 but is not consistent with the morphologies of RMDSs.

607
 608 We therefore infer that the RMDSs might form by a relatively slow inflation
 609 process, where small cracks form and discharge small amounts of disaggregated
 610 foam, and that this foam debris (some cooled bubble wall shards but mostly hot
 611 magma droplets) seals the cracks fast enough that sagging of the lava crust does not
 612 reach the stage of wholesale collapse. During this process, these cracking events
 613 produce a layer of debris over each crack site (Figure 8c), which we assume is
 614 confined to the highest part of the updomed crust as this is where stress is
 615 concentrated. Debris will collect extremely close to the cracks, because each jet of
 616 gas and entrained clasts will be heavily collimated by the crack sides, and as debris
 617 accumulates it will form an angle of rest cone. As the cone grows, the pressure at its
 618 base due to its weight increases, progressively reducing the violence of foam
 619 disaggregation when the crack is reactivated. When the cone gets sufficiently large,
 620 the pressure at its base will be equal to the pressure at the base of the lava crust, and
 621 so subsequent crack activation will not involve explosive activity (Figure 8c).
 622 Instead, foam will simply rise slowly through the crack and invade the base of the
 623 debris cone. We saw above that the pressure at the top of the foam under a 3 m thick
 624 flow crust was $\sim 14\ \text{kPa}$. If the expelled debris packs with 30% void space, the
 625 minimum cone height required to suppress explosive activity is 4.1 m, and an angle of
 626 rest cone with this height has a basal diameter of 14.2 m and a volume of $219\ \text{m}^3$
 627 (Figure 8c). With the smallest scale length for mare surface topographic
 628 irregularities, 200 m, the radius of a typical updomed region would be $c = \sim 100\ \text{m}$
 629 (see Figure 7), and so the volume of foam with vesicularity of $\sim 50\%$ in a 3 m thick
 630 upper foam layer available to feed the intermittent explosive events would be $(\pi \times$
 631 $100^2 \times 3) \sim 3.14 \times 10^4\ \text{m}^3$. Adjusting for the vesicularities of the foam and the
 632 debris mound, only 0.7% of the upper foam layer would need to be ejected to
 633 suppress explosive activity and start the process of inflation of the debris cone by
 634 injection of foam at its base. This difference in volume by two orders of magnitude
 635 suggests that the initial debris mound would be pushed aside and either buried or
 636 overridden by the subsequently extruded foam (Figure 5e).

637 638 5.5. *Foam extrusion:*

639 This process of intermittent enlargement of the mound of extruded material on
 640 the flow surface would continue until there was some major change in the inflation
 641 rate of the lava flow itself. Such a change can be anticipated in the form of the
 642 generation of instabilities in the lower foam layer causing mini-diapirs feeding vesicle
 643 pipes to form and transport foam from the lower to the upper layer. We showed

644 earlier that gas bubbles migrating from the lower to the upper zone would expand by a
 645 volume factor of ~5. Using Figure 6d, the lower vesicular zone extends between
 646 depths of 14 and 22 m and has an average vesicularity of 50%. Thus a 4 m vertical
 647 extent consists of liquid lava and a 4 m vertical extent consists of gas. If half of this
 648 mixture is transferred to the lower pressure of the upper layer, the 2 m of gas in it
 649 expands to a 10 m vertical extent and the 2 m of liquid is unchanged, so the total
 650 vertical extent is 12 m. However, this mixture came from a region with a vertical
 651 extent of 4 m, so the net inflation, I , caused by the upward foam transfer is (12 - 4 =)
 652 8 meters. This is considerably greater than the 1 to 2 m uplift due to the uneven
 653 topography found above; using the equivalent geometry, it would lead to crack widths
 654 in the range 640 and 183 mm for $c = 100$ and 350 m, respectively, ~50 times greater
 655 than the earlier values.

656

657 Sudden uplift and production of a wide crack in the lava crust allows foam from
 658 the newly enriched upper foam layer to extrude into the existing debris mound and
 659 greatly enlarge it. The lava crust must subside at a speed that leads to a volume loss
 660 from the underlying foam layer that just balances the volume extrusion rate onto the
 661 surface. To model this process we assume the crack geometry shown in plan view in
 662 the upper left part of Figure 7, with two cracks crossing at right angles producing four
 663 crack segments. Other geometries would yield similar crack openings. Vesicular
 664 foams generally have a non-Newtonian rheology. Dollet and Raufast (2014, their
 665 Figure 5) provide data on the control of surface tension on foam rheology showing
 666 that a monodisperse foam should have a yield strength, τ_y , given by

667

$$668 \quad \tau_y = K (\sigma / \phi) \quad (8).$$

669

670 where σ is the surface tension of the liquid-gas interface, $\sim 0.37 \text{ J m}^{-2}$ for water in
 671 basalt (Mangan and Cashman, 1996) and ϕ is the typical bubble radius. The constant
 672 K varies with the vesicularity of the foam, which Figure 6 shows is typically ~50%,
 673 for which K is very close to 10^{-3} (Dollet and Raufast, 2014). Given that the bubbles in
 674 the injected lava flow will have nucleated with a radius of $\sim 10 \mu\text{m}$, and that even
 675 those added to the upper layer from the lower layer will have expanded by less than a
 676 factor of 1.7, we adopt $\phi = 15 \mu\text{m}$ so that $\tau_y = \sim 25 \text{ Pa}$. If a material with a yield
 677 strength rises through a parallel-sided channel, the flow consists of a zone of shearing
 678 fluid on either side of a central plug of width Y given by

679

$$680 \quad Y = (2 \tau_y) / [g (\rho_o - \rho_f)] \quad (9)$$

681

682 where ρ_o is the density of the overburden and ρ_f is the density of the foam. The
 683 overburden at the crack site (Figure 8c) consists of about a 4 m thickness of loose
 684 debris with a porosity likely to be ~30%, implying a density of 2100 kg m^{-3} , and a 3 m
 685 thickness of non-vesicular lava with density 3000 kg m^{-3} , making the average
 686 overburden density close to 2500 kg m^{-3} . The density of the 50% vesicular foam is
 687 1500 kg m^{-3} . With $\tau_y = \sim 25 \text{ Pa}$ this implies $Y = \sim 30 \text{ mm}$. A foam with this yield
 688 strength cannot rise at all in a crack that is less than 30 mm wide. This 30 mm
 689 estimate is between ~5 and 16% of the 640 to 183 mm maximum crack widths
 690 derived above for $c = 100$ and 350 m, respectively. Using the upper part of Figure 7,
 691 this implies that the length, X , of the part of the crack through which foam can rise

692 will be between 95 and 84% of the corresponding value of c , i.e., $X = 95$ m for $c =$
 693 100 m and $X = 294$ m for $c = 350$ m.

694

695 As Figure 7 shows, the width of the crack decreases from W at the widest point
 696 to Y at the last point at which foam can rise through the crack. Let the local width of
 697 the crack be w at a point distant x from the last active point (Figure 7) and let q be the
 698 ratio of the width of the central plug to the local width of the crack:

699

$$700 \quad q = Y / w \quad (10).$$

701

702 In terms of this parameter, the speed, U_{plug} of the central plug rising through the crack
 703 is given by Skelland (1967) as

704

$$705 \quad U_{\text{plug}} = [(1 - q^2) w^2 g (\rho_o - \rho_f)] / (8 \eta_b) \quad (11),$$

706

707 and the mean velocity of the foam, U_F , including both sheared fluid and plug is

708

$$709 \quad U_F = [(2 + q) / 3] U_{\text{plug}} \quad (12)$$

710

711 The local volume flux of foam, F_i , escaping through each increment dx of the active
 712 crack is $(U_F w dx)$ and the total flux in each half crack is found by integrating this
 713 numerically in a spreadsheet program using $dx = 0.1 X$. Table 2 shows how the
 714 various parameters vary with x for both the $X = 90$ m and 245 m crack lengths, and for
 715 an intermediate case with $L = 450$ m, $c = 225$ m, $W = 0.285$ m and $X = 200$ m. The
 716 total volume fluxes, F_i , of foam released through a single crack are ~ 109 , 21.7 and 8.9
 717 $\text{m}^3 \text{s}^{-1}$, respectively, and the totals from all four crack segments are ~ 438 , 86.8 and
 718 $35.6 \text{m}^3 \text{s}^{-1}$, respectively. We now use these eruption rates to calculate the properties
 719 of the surface features that they produce.

720

721 The foam rising through the cracks intrudes into the base of the debris mound
 722 that has already accumulated and so there should be little change in its $\sim 50\%$
 723 vesicularity as long as it remains debris-covered. Where foam is erupted with no
 724 debris cover, which is most likely to occur at the narrow ends of the cracks, explosive
 725 decompression and debris formation will occur just as in the earlier phase of the
 726 activity until the foam is stabilized. The foam discharge rate is greatest at the widest
 727 part of each crack near the center of the uplifted area. The foam will spread both
 728 down-slope, approximately radially from the center of uplift, and also laterally away
 729 from the crack, at right-angles to the maximum slope, in the same way as any lava
 730 flow that exhibits a yield strength (Hulme, 1974). Let the flow that develops from a
 731 particular location on the crack where the volume flux being erupted is F_i have levees
 732 each of width W_i and maximum thickness D_i and a central channel of width W_c and
 733 maximum thickness D_c . Then Hulme (1974) showed that

734

$$735 \quad D_i = \tau_y / (\rho g \sin \alpha) \quad (13),$$

736

$$737 \quad W_i = \tau_y / (2 \rho g \sin^2 \alpha) \quad (14),$$

738

$$739 \quad D_c = [(W_i \tau_y) / (\rho g)]^{1/2} \quad (15),$$

740

741 where W_i is the total width of the flow,

742

743

$$W_t = W_c + 2 W_1 \quad (16).$$

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Wilson and Head (1983) found that the relationship between the central channel width W_c and the erupted volume flux F_1 could be simplified from Hulme's original more complex relationship using the good approximations

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$$W_c = [(24 F_1 \eta_p) / (\tau_y \sin^2 \alpha)]^{1/3} \quad , \quad W_c / (2 W_1) \leq 1 \quad (17a),$$

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751

$$W_c = [(24 F_1 \eta_p)^4 \rho_f g] / (\tau_y^5 \sin^6 \alpha)^{1/11} \quad , \quad W_c / (2 W_1) \geq 1 \quad (17b).$$

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The above system of equations has been solved for the three topographic scale lengths, $L = 200, 450$ and 700 m, used earlier and for the estimated initial inflation, I , of 8 m. The values are given for the total volume flux, F_t , and so apply towards the lower end of the crack nearest to the original lava flow surface level. As foam is extruded onto the surface of the lava flow, the underlying structure of the flow must change. Our initial assumption was that the upraised surface slab of lava crust subsided back towards the horizontal as shown in Figure 9. However, as Figure 7 makes clear, this would necessarily reduce the width of each crack at every point along its length, making the escape of foam with a yield strength ever more difficult. To explore this, the above equations were also solved with $I = 4$ m and 2 m to track the subsidence of the crustal slabs. Table 3 shows the results. First, all of the foam flows are less than one meter thick. Second, although at the top of the upraised crustal slabs the embryonic flows from the four individual crack segments inevitably overlap and combine, in no case do they continue to do so as they descend the slope. Instead of forming a single mound they diverge into four separate flow lobes: this is shown by the fact that in all of the cases in Table 3 the total width of all four flows, ($4 W_t$), is less than the circumference of the circular region occupied by the cracks, ($2 \pi c$), i.e., $W_t < (\pi / 2) c$; the values of $[(\pi / 2) c]$ are given in the table for comparison with the values of W_t . Finally, as I decreases to less than ~ 3 m, the cracks become so narrow in the cases of $L = 450$ and 700 m that foam can no longer be extruded. It is clear, therefore, that a response to foam extrusion in which the upraised crustal slabs simply rotate back towards the horizontal as in Figure 9 does not lead to significant extrusion of foam on the scale or with the geometry needed to explain the RMDSSs.

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An alternative response to foam extrusion is shown in Figure 10. In this scenario foam rises diapirically from the lower foam layer and supports the uptilted blocks of lava crust (Figure 10a) as they subside by a few meters nearly vertically, without rotating as they sink (Figure 10b). As they subside, foam extrudes through the cracks radiating from the center of the uplift which, because of the lack of crustal block rotation, now have a nearly constant width throughout the extrusion event (Figure 10c). The extrusion rate is greatest where the cracks are widest, and the foams from the four cracks immediately coalesce into a single body of fluid essentially emanating from a point source. There is now no progressive reduction in the extrusion rate, which remains essentially constant at its initial high value until the foam supply is exhausted. There is also no longer the bias against the formation of the larger mounds that was found with the previous geometry. The issue now becomes that of modelling the growth of a body of fluid having Bingham plastic rheology extruded from a point source. This problem was treated by Blake (1990), who found that the height H of the resulting mound was related to its radius R by

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793

$$H = [(3.1 \tau_y R) / (\rho g)]^{1/2} \quad (18)$$

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841

In our case the fluid density is that of the foam, ρ_f , and presumably R must be similar to our parameter c . We estimated $\tau_y = 25$ Pa earlier, and so for c in the range 100-225 m, H should lie in the range 1.8 to 2.7 m. This height is measured above a presumed pre-existing flat surface in the case of Blake's (1990) model and so in our case it should logically be measured relative to the pre-existing surface level. Zhang et al. (2018a, b) have obtained the heights of 532 RMDs, but their heights are measured relative to the base of the moat. Our model predicts (see Figure 10) that the depth of the moat produced by subsidence of the low end of the tilted crustal slab should be of the same order as the thickness of the upper foam layer, about 3 m, and so our equivalents to the heights of Zhang et al. (2018a, b) for c in the range 100-225 m would be 4.8 to 5.7 m. The average values found by Zhang et al. (2018a, b) for these dome heights are 3.5 to 6.0 m. Given the considerable scatter in the measurements and the numerous assumptions in our model, we consider this to be entirely satisfactory agreement, supporting our proposal that the geometry of Figure 10 describes the system. Note that very little foam extrudes through the cracks in the crustal slabs underlying the moats because much of the foam originally in those regions will have migrated inward to feed the central uplift.

Table 2 shows the foam volume fluxes expected for single cracks in the 4-crack configuration of Figure 7. For $c = 100$ and 225 m these are 109 and 21.7 m³ s⁻¹, respectively. The corresponding total volume fluxes from all four cracks are therefore 436 and 87 m³ s⁻¹. Zhang et al. (2018a, b) find that the typical volumes of RMDs mounds with radii 100 and 225 m are ~30,000 and 70,000 m³, respectively. This implies that the time intervals needed to emplace the mounds with these sizes are about 70 seconds in the first case and ~13 minutes in the second. These volume fluxes are the maxima that would apply with the cracks at their greatest extent. In practice a finite time is needed for a crack to expand to its greatest width, and the crack would begin to close after most of the foam was extruded. Even so, we see no reason to expect the time scales for mound formation to be more than a factor of two or three greater than the values given here.

5.6. Implications of dome heights:

Figure 2a shows that dome height tends to increase with dome diameter, but that the maximum dome height appears to be restricted to a value of ~14 m. In Figure 10 we have shown what we consider to be the most likely situation in which a large fraction of the locally-available foam is erupted onto the surface to form a mound, possibly with a contribution from foam migrating laterally from the surrounding flow to augment the local supply. If this is the case, then the height of the top of the mound above the bottom of its moat is an approximate indicator of the total vertical extent of foam in the flow before foam release onto the surface. For our nominal model shown in Figure 6, the total uplift of the flow due to gas release alone was 16.34 m. The equivalent vertical uplifts for other values of the residual gas in the injected lava are shown in Figure 11. Recall that in Section 5.1 we showed in Table 1 the expected water mass fraction n_m in the core of the distal flow as a function of the water content in the magma leaving the lava pond at the vent, n_{res} with n_m having a maximum when n_{res} was ~175 ppm. This is now reflected exactly in Figure 11, with the uplift due to gas exsolution showing a maximum of ~22 m when n_{res} is 175 ppm.

842 This leads to the striking implication that, at least for flows of the scale modeled here,
843 no RMDs should have a height greater than ~22 m, probably somewhat less since it is
844 unlikely that all of the available foam is extruded from a flow. This is clearly
845 supported by the observed dome heights being restricted to less than ~14 m.
846 Furthermore, the fact that domes with heights in the range 4-10 m are common
847 implies that residual water contents in lavas leaving vent lava ponds were commonly
848 in the range 25-250 ppm. Where foam extrusion occurs under other circumstances,
849 for example from fractures in the crusts of lava lakes at the summits of small shield
850 volcanoes, as at Ina (Qiao et al., 2017), conditions are likely to be different because
851 more foam accumulation might occur. Even so, the mounds inferred to be foam
852 extrusions on the floor of Ina typically have heights of 10-15 m with only a few
853 approaching 20 m (Qiao et al., 2017).

854

855 **6. Summary and discussion:**

856 We have presented above a theoretical model for the formation and evolution of
857 Ring Moat Dome Structures (RMDs) that is based on the expected dynamics of
858 lunar lava flows (Wilson and Head, 2018a; Head and Wilson, 2018) and is formulated
859 to attempt to account for the major characteristics of these newly documented features
860 (Zhang et al., 2017; 2018a,b). In this model, a mare basalt lava flow is emplaced
861 from a fissure vent. In the early stages of the eruption, the flow leaving the vent
862 contains extremely few dissolved volatiles and almost no exsolved gas bubbles due to
863 the efficient loss of volatiles in pyroclastic hawaiian fire fountain activity at the vent.
864 As it travels away from the vent area, the lava flow surface and base cool
865 progressively, producing a distal flow with upper and lower solidified boundary layers
866 and a molten core (Figure 5a). In the latter stage of the eruption at the vent, the
867 magma rise speed decreases as the dike begins to close, and volatile bubbles can
868 coalesce, favoring strombolian activity which removes much, but not all, of the
869 volatiles from the magma. Magma containing ~25-250 ppm of residual dissolved
870 volatiles from this latter phase of the eruption is injected into the previously emplaced
871 molten core of volatile-poor magma, causing flow inflation, substantially uplifting the
872 surface of the flow (Figure 5b).

873

874 As the flow ceases to advance, crystallization of the lava causes supersaturation
875 of residual dissolved volatiles in the injected core of the flow. The gas exsolved in
876 this second boiling generates copious quantities of vesicles at the top and bottom of
877 the central core of the flow, resulting in production of foam layers; additional flow
878 inflation of many meters is predicted to accompany the formation of the foam layers
879 (Figures 5c, 5d). This additional inflation flexes the cooled upper crustal layer, and
880 forms fractures that permit the buoyancy-driven extrusion of the magmatic foams
881 onto the surface (Figure 5e). Magmatic foam extrudes through the cracks and forms
882 circular mounds on the surface, i.e., the domes. Subsidence of the subjacent and
883 surrounding surface, in response to the foam displacement, forms the ring moats
884 around the mounds. The low viscosity of lunar basalts compared with terrestrial
885 basalts, coupled with predicted high effusion rates in typical lunar eruptions and the
886 absence of a lunar atmosphere, facilitates these processes in all flows with lengths
887 greater than ~50 km and thicknesses greater than ~10 m. Although second boiling
888 and inflation are common features of many large basaltic flows on Earth, the
889 formation of extremely vesicular foams, again the consequence of the low gravity and
890 absence of atmosphere, is unique to the Moon and allows not only the upward flexing

891 and fracture of lava flow surfaces but also the formation of the distinctive RMDS
892 mounds by extrusion of the foam (Figures 5e, 10).

893

894 The above model (see Figure 12 for a synthesis) has a number of implications
895 that can be regarded as predictions to be tested using future morphological
896 observations derived from high-resolution remote sensing and physical observations
897 made in situ. The material forming the RMDS mounds is predicted to be a basaltic
898 lava foam with ~50-60% vesicularity overlain by a layer of shattered foam which is a
899 mixture of glass shards and chilled droplets loosely packed with ~30% void space.
900 The mound formation process consists essentially of the redistribution of a given
901 volume of vesicular lava from the interior of a lava flow onto its surface, and although
902 there is clearly some change in the bulk density of this material as some of it explodes
903 into the overlying vacuum, changing from coherent foam to a loose layer of
904 fragments, the overall volume change should not be large, and so the volumes of each
905 mound and its surrounding moat should be similar. Since the second boiling that
906 leads to mound formation occurs within a stationary flow as it cools, the resulting
907 RMDS is predicted to be un-deformed by shearing due to any lateral flow movement,
908 as appears to be the case based on the first survey of RMDSs (Zhang et al., 2017).
909 Extrusion of the foam from cracks radiating from the highest point of uplift of the
910 underlying ~3 meter thick lava flow crust should generally lead to mounds with a
911 near-circular shape because the morphology is controlled by the non-Newtonian
912 rheology of the foam rather than by the underlying topography. However, the
913 topography of flow surfaces can have height excursions of order meters at horizontal
914 scales of tens of meters (Kreslavsky et al., 2017), for example due to a flow
915 encountering impact craters on these scales during its emplacement, and in such cases
916 extruded foam might collect in depressions or be diverted around high points, leading
917 to more irregular RMDSs. Further sources of RMDS irregularity include (1) uneven
918 surface topography due to multiple stages of flow inflation and lava crust bending,
919 flexing and fracturing (Figures 5, 6); (2) the presence of crater-like depressions
920 formed by foam collapse, gas venting and subsidence of cooled crust (Figure 8); and
921 (3) sequential emplacement of RMDSs such that the formation of one feature
922 scavengers foam from nearby parts of the flow and induces stresses that initiate a
923 subsequent RMDS nearby. Predictable consequences of these processes include (1)
924 somewhat linear chains of RMDS domes guided by fractures in distal flows due to
925 pre-eruption topography or by pathways used by magma during late stage inflation
926 and second boiling; and (2) asymmetric dome profiles due to preferential foam flow
927 into depressions.

928

929 We have derived the results presented above in terms of a nominal mare basalt
930 eruption scenario in which the distal parts of lava flow fields have thicknesses of ~14
931 m and the proximal parts thicknesses of ~ 4 m. Other patterns of variation of eruption
932 rate with time are possible, though the trends of high to low discharge rate and
933 consequent changes in morphology of the active part of the flow field seem inevitable
934 (Wilson and Head, 2017a, 2018a). The penetration of cooling fronts into lava flows is
935 controlled almost entirely by the thermal properties of the lava, such that the
936 thicknesses of the cooled crusts at the top and base of a flow are similar functions of
937 time until the two cooling fronts meet near the middle of the flow. Since this is the
938 critical period for foam creation by second boiling, the time scale for the onset of
939 RMDS formation, several tens of days after an eruption starts, is likely to be
940 independent of the actual flow thickness as long as this is greater than about 10

941 meters. Flows much thinner than this would probably not produce RMDSs at all
942 because almost all of their interiors would have cooled well below the liquidus before
943 conditions at the vent were suitable to cause late-stage lava injection into them.
944 Thicker flows would be at least as likely to form RMDSs as those modeled here, and
945 would probably be more likely to do so, and to produce mounds with greater heights,
946 because increased flow thickness causes the pressure in the lower foam layer to be
947 greater. As a result, the amount of expansion of the lower foam as it rises to join the
948 upper foam layer is also greater, and the stress exerted on the overlying crust to form
949 cracks is greater. The horizontal sizes of the RMDSs should not depend strongly on
950 flow thickness, however, because we predict that these parameters are controlled
951 mostly by horizontal irregularities in the topography onto which the flow is emplaced.
952 Thus we would expect only a weak correlation between dome width and dome height,
953 with considerable scatter in both parameters, as is observed (Zhang et al., 2018a, their
954 Figure 1).

955
956 Our model (see Figure 12 for a synthesis) implies that, immediately after their
957 formation (Figure 13a), RMDSs should consist of a highly fragmental layer overlying
958 a foam layer in turn overlying a very low vesicularity lava flow crust, each layer being
959 ~2-3 m in thickness. This physical structure has implications for subsequent RMDS
960 development under impact bombardment. The fragmental layer, consisting of the
961 shattered walls of sub-mm sized bubbles, has very similar properties to those of
962 mature mare regolith. Small-scale impacts into this material will simply re-distribute
963 it on a sub-cm scale (Figure 13b). Somewhat larger impactors able to create a cavity
964 more than 1-2 m deep and thus encounter the foam will produce anomalously shaped
965 craters relative to the impactor size because of the efficient energy-absorbing aerogel-
966 like response of this very vesicular material (Durda et al., 2003; Kadono and
967 Fujiwara, 2005; Qiao et al., 2017, 2018a, 2018b). Projectile kinetic energy
968 partitioning into the foam layer favors crushing of foam vesicles rather than the brittle
969 fracturing and ejection typical of impacts into coherent basalt bedrock. This may lead
970 to unusual crater shapes. Such cratering events occurring at this early time are
971 predicted to form pit craters on the dome/foam surfaces and normal craters on the
972 adjacent surface of the solid upper flow layer. Impacts large enough to penetrate
973 through the foam layer will encounter the uptilted bedrock slab, and produce flat-
974 bottomed craters with blocky floors and ejecta (Figure 13b). Impacts that occur on
975 the boundary between the dome and the moat are predicted to have very unusual
976 characteristics. The part of the crater forming on the rim and inner margin of the
977 moat should be characterized by a substrate formed of the upper cooled solid basalt
978 layer (see Figure 10), and should have a morphology similar to that of fresh blocky
979 craters in basaltic substrates. The part of the crater forming on the dome itself will
980 have a very different morphology, characterized by crushing of the foam substrate,
981 probably a higher than usual depth-diameter ratio, few to no boulders, and
982 enlargement of the rim by mass wasting of the crushed foam from the relatively
983 steeper sides of the dome edge onto the crater floor. This type of configuration might
984 be misinterpreted to mean that the mound foam flowed into the floor of a fresh crater,
985 partially filling it. This would erroneously suggest a very young age for the foam
986 emplacement event, significantly after the emplacement of the surrounding maria.
987 Finally, after hundreds of millions to several billion years (Figure 13c), these initial
988 dome substrate stratigraphic units (Figure 13a) will be largely obliterated and
989 admixed by the development of an impact-generated regolith that could easily exceed
990 the ~4-6 m thickness of the initial layers (Figure 13a) overlying the solid basalt lava

991 crust. In these latter stages, morphologies of craters superposed on domes should be
 992 very similar to those of craters developed on adjacent, non-RMDS mare surfaces.
 993 These evolutionary responses of superposed craters to regolith development may also
 994 influence the impact crater size-frequency distributions, and thus inferred ages, of
 995 RMDS features relative to non-RMDS maria. In situ examples of mature RMDS
 996 regolith soils are predicted to have a much greater abundance of shattered walls of
 997 sub-mm bubbles and fine foam fragments than typical non-RMDS regolith (Head and
 998 Wilson, 2019).

999

1000 Such a marked contrast in the physical properties of the dome and surrounding
 1001 moat and flow materials may also help to account of the preservation of the
 1002 topographically subtle moat for several billion years. Degradation of surface
 1003 topography on mare flows is dominated by the processes of subsequent impact
 1004 cratering and the resultant vertical gardening and lateral transport of ejecta to subdue
 1005 adjacent topography. In this case, on the dome side of the moat, lateral transport is
 1006 minimized in the earlier stages of regolith development due to the deep penetration of
 1007 the projectile into the foam, and the dominance of substrate crushing rather than
 1008 lateral transport and subduing of adjacent topography.

1009

1010 Our proposed model of lava flow injection, inflation, and second boiling is
 1011 consistent with many of the observed characteristics of Ring Moat Dome Structures
 1012 (RMDSs) as follows (Figure 12): 1) the generally circular shape and dome-like
 1013 morphology interpreted as uplift and then subsidence accompanying foam extrusion.
 1014 2) The presence of a surrounding moat interpreted as subsidence of the outer rigid
 1015 layer caused by foam evacuation from the subsurface. 3) The relatively large
 1016 diameter/height ratio due to the low viscosity and low yield strength of the foam,
 1017 consistent with expected foam properties. 4) The occurrence of RMDSs in clusters
 1018 interpreted as inflation and second boiling taking place in a sheet-like rather than a
 1019 channel-like configuration; occasional channel-like patterns might be manifested by
 1020 more linear mounds. 5) The non-uniform distribution of RMDSs in mare regions
 1021 because regions of volatile-rich flow inflation and foam extrusion are required, and
 1022 these regions make up only a part of the total initial flow area, and are likely to occur
 1023 preferentially in the proximal part of the flow field. 6) The similarity of RMDS
 1024 mineralogy to that of the surrounding lava because both have the same source. 7) The
 1025 common mound diameter range of ~100-500 m, consistent with the wavelength of
 1026 surface undulations triggering foam migration in inflated flows. 8) The extreme rarity
 1027 of overlapping mounds due to each mound potentially scavenging foam from the
 1028 surrounding foam layer below the flexing lava crust. 9) The apparent young age of
 1029 the domes due to the aerogel-like properties of the foams and the anomalously high
 1030 depth-diameter ratio that this induces in impact craters. 10) The association of some
 1031 RMDSs with irregular mare patches (IMPs) when both types of feature form close to
 1032 the volcanic vent feeding the flows.

1033

1034 This model makes the following predictions that can be further tested with
 1035 additional analyses of the characteristics and distribution of Ring Moat Dome
 1036 Structures (RMDS) as follows:

1037 1) RMDS will not form in typical mare flows unless the flows have been
 1038 inflated by late-stage volatile-rich cores, and thus have undergone second boiling of
 1039 volatile-rich lava; the presence of RMDSs will be a direct indicator of areas of flow
 1040 inflation.

1041 2) Lava flows with thicknesses less than a few meters will not produce RMDSs
1042 due to the small volume of foam produced relative to the cooling boundary layer
1043 thickness, though the flows may undergo a small amount of inflation.

1044 3) Initial fresh impact craters less than ~30 m in diameter forming on RMDSs
1045 before extensive regolith has developed should have unusual characteristics (Figure
1046 13b), lacking coarse ejecta (e.g., boulders) since they excavated only vesicular foam
1047 or low-strength fragmental debris. Following regolith development, differences in
1048 superposed crater morphology between RMDS domes and adjacent mare surfaces
1049 should be much less extreme (Figure 13c). Mature RMDS regolith soils are predicted
1050 to have a much greater abundance of shattered walls of sub-mm bubbles and fine
1051 foam fragments than typical non-RMDS regolith (Head and Wilson, 2019).

1052 4) The presence of vesicular/low density material and the absence of coarse
1053 crater ejecta should cause RMDSs to give distinctive low-strength returns at RADAR
1054 wavelengths penetrating a few meters and should also produce thermal anomalies.

1056 7. Conclusions:

1057 We have utilized the newly documented characteristics of Ring Moat Dome
1058 Structures (RMDSs) (Zhang et al., 2017; 2018a, b) together with a theoretical model
1059 for the emplacement and cooling of mare basalts (Wilson and Head, 2017a; 2018,
1060 Head and Wilson, 2018) to develop a theoretical model accounting for RMDS
1061 characteristics (Figure 12). RMDSs are low mounds that occur in the lunar maria and
1062 appear to form synchronously with the surrounding mare basalt deposits. We interpret
1063 them to be due to inflation of the molten cores of cooling flows during the late stages
1064 of eruptions by injection of additional hot lava containing dissolved volatiles.
1065 Subsequent crystallization of this lava causes second boiling gas exsolution,
1066 generating copious quantities of vesicles at the top and bottom of the central core of
1067 the flow, forming magmatic foam layers that can accumulate into a single layer below
1068 the upper cooled crust of the flow. Flow inflation of many meters accompanies the
1069 formation of the foam layers, flexing the cooled upper crustal layer, and forming
1070 fractures. These cracks permit the buoyancy-driven extrusion of the magmatic foam
1071 onto the surface. Subsidence of the subjacent and surrounding surface occurs to form
1072 the moat. We have outlined several ways that this model can be tested by further
1073 observations of the morphology, morphometry and distribution of RMDSs. Finally,
1074 we leave as a subject for further work the detailed analysis of the morphological
1075 development of proximal lava flows with internal structures like those shown in
1076 Figure 4 when they are not injected into distal flow units. However, we suggest that
1077 there are foreseeable consequences of the cooling of such flows following their
1078 eruption. The examples in Figures 4(a) and (b), with total water contents up to ~200
1079 ppm, contain significant dissolved water that will be released during second boiling,
1080 causing extreme inflation as foam is formed. We suggest that subsequent large-scale
1081 collapse of the foam is a possible mechanism for the production of some of the
1082 Irregular Mare Patches (IMPs) documented by Braden et al. (2014) and by Qiao et al.
1083 (2017, 2018a, 2018b).

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1098

1099 Table 1. Parameters relating to the injection of lava erupted late in an eruption into
 1100 the core of a 14 m thick stagnant lava flow emplaced in the early stages of the same
 1101 eruption. The early stage lava lost most of its volatiles in a fire fountain at the vent
 1102 and is very vesicle-poor. The late stage lava is 4 m thick and consists of three layers:
 1103 a fragmental upper layer overlies a very vesicular layer which in turn overlies a
 1104 vesicle-free basal layer still containing a mass fraction n_{res} in ppm of volatiles
 1105 dominated by H₂O. The top of the basal layer is at a depth D_t below the top surface of
 1106 the 4 m layer and the basal layer has a thickness D_w . Injection of this volatile-bearing
 1107 lava into the core of the 14 m thick distal flow inflates the distal flow to a new total
 1108 thickness D_i . After mixing between the injected lava and the original core lava, the
 1109 core has a dissolved water content of n_m , available to be released as gas bubbles when
 1110 cooling and crystallization causes second boiling to occur.

1111	n_{res}	D_t	D_w	D_i	n_m
1112	10	0.02	3.98	17.98	3.3
1113	25	0.06	3.94	17.94	8.2
1114	50	0.18	3.82	17.82	16.1
1115	75	0.35	3.65	17.65	23.5
1116	100	0.58	3.42	17.42	30.0
1117	125	0.87	3.13	17.13	35.2
1118	150	1.22	2.78	16.78	38.7
1119	175	1.64	2.36	16.36	39.9
1120	200	2.12	1.88	15.88	38.1
1121	225	2.67	1.33	15.33	32.1
1122	250	3.28	0.72	14.72	20.6
1123	275	3.96	0.04	14.04	1.4
1124					
1125					
1126					

1127 Table 2. Parameters of foam extrusion through the cracks in the lava crust to form
 1128 surface foam flows for three horizontal scales of features. Values given as a function
 1129 of distance along active part of crack, x , in meters are: local crack width, w , in meters;
 1130 ratio of plug width to crack width, q ; mean speed of foam in crack, U_F , in m s^{-1} ;
 1131 Reynolds number, Re , of fluid in crack; and local volume flux of foam, F_1 , in $\text{m}^3 \text{s}^{-1}$.
 1132 The total volume flux from the crack is given at the bottom of the last column.
 1133

1134 (a) Crack with $c = 100 \text{ m}$, $X = 95.2 \text{ m}$, $W = 0.64 \text{ m}$

1135	x	w	q	U_F	Re	F_1
1136	9.52	0.09	0.34	0.12	1.6	0.10
1137	19.04	0.15	0.20	0.33	7.6	0.49
1138	28.56	0.21	0.14	0.65	20.8	1.32
1139	38.07	0.27	0.11	1.06	43.9	2.78
1140	47.59	0.34	0.09	1.58	79.6	5.05
1141	57.11	0.40	0.08	2.20	130.8	8.30
1142	66.63	0.46	0.07	2.91	200.2	12.70
1143	76.15	0.52	0.06	3.73	290.5	18.43
1144	85.67	0.58	0.05	4.65	404.5	25.67
1145	95.19	0.64	0.05	5.67	545.0	<u>34.58</u>
1146						109.43

1147

1148 (b) Crack with $c = 225 \text{ m}$, $X = 200.6 \text{ m}$, $W = 0.284 \text{ m}$

1149	x	w	q	U_F	Re	F_1
1150	20.06	0.06	0.55	0.04	0.32	0.04
1151	40.12	0.08	0.38	0.09	1.12	0.15
1152	60.18	0.11	0.29	0.16	2.60	0.35
1153	80.24	0.13	0.23	0.25	4.95	0.66
1154	100.30	0.16	0.20	0.35	8.38	1.12
1155	120.36	0.18	0.17	0.48	13.09	1.75
1156	140.42	0.21	0.15	0.62	19.26	2.58
1157	160.47	0.23	0.13	0.77	27.11	3.63
1158	180.53	0.26	0.12	0.95	36.82	4.92
1159	200.59	0.28	0.11	1.14	48.60	<u>6.50</u>
1160						21.70

1161

1162 (c) Crack with $c = 350 \text{ m}$, $X = 290.9 \text{ m}$, $W = 0.183 \text{ m}$

1163	x	w	q	U_F	Re	F_1
1164	29.09	0.05	0.67	0.02	0.1	0.03
1165	58.19	0.06	0.50	0.05	0.4	0.08
1166	87.28	0.08	0.40	0.08	0.9	0.18
1167	116.37	0.09	0.34	0.12	1.6	0.31
1168	145.47	0.11	0.29	0.16	2.6	0.50
1169	174.56	0.12	0.25	0.21	3.9	0.75
1170	203.65	0.14	0.22	0.27	5.5	1.07
1171	232.75	0.15	0.20	0.33	7.6	1.47
1172	261.84	0.17	0.18	0.40	10.1	1.95
1173	290.93	0.18	0.17	0.48	13.0	<u>2.53</u>
1174						8.89

1175

1176

1177 Table 3. Parameters of foam extrusion through cracks in the lava crust to form
 1178 surface foam flows for three horizontal scales of features. As the inflation I of the
 1179 lava surface decreases, values are given for the maximum thickness D_b and width W_b
 1180 of the levee on each side of the flow, the width W_c of the central channel, the total
 1181 flow width W_t , and the center-line thickness of the flow D_c . Values of $[(\pi/2) c]$ are
 1182 given for comparison with values of W_t . All values are in meters.
 1183

1184 Crack with $L = 200$ m, $c = 100$ m, $X = 95.2$ m, $(\pi/2) c = 157$ m

1185	I	D_b	W_b	W_c	W_t	D_c
1186	8	0.13	0.8	75.5	77.1	0.89
1187	4	0.26	3.2	24.2	30.6	0.56
1188	2	0.51	12.9	5.1	30.8	0.56

1189
1190

1191 Crack with $L = 450$ m, $c = 225$ m, $X = 200.6$ m, $(\pi/2) c = 353$ m

1192	I	D_b	W_b	W_c	W_t	D_c
1193	8	0.29	4.1	65.2	73.3	0.87
1194	4	0.58	16.3	19.9	52.4	0.73

1195
1196

1197 Crack with $L = 700$ m, $c = 350$ m, $X = 290.9$ m, $(\pi/2) c = 550$ m

1198	I	D_b	W_b	W_c	W_t	D_c
1199	8	0.45	9.8	60.0	79.7	0.91
1200	4	0.90	39.4	15.6	94.3	0.99

1201
1202
1203
1204

1205

1206 **Notation**

1207	D	depth below surface of lava flow
1208	D_1	thickness of lava in central channel of foam flow
1209	D_d	flow thickness in distal part of lava flow
1210	D_f	initial thickness of lava flow
1211	D_i	distal flow thickness between proximal lava injection and second boiling
1212	D_l	thickness of levee of foam flow
1213	D_p	flow thickness in proximal part of lava flow
1214	D_t	depth to top of part of flow still containing dissolved water
1215	D_w	thickness of layer of lava still containing dissolved water
1216	E	maximum uplift of lava flow surface due to foam concentration
1217	F	dense rock equivalent lava volume eruption rate from vent
1218	F_1	local volume flux of foam from an increment of crack length
1219	F_t	total volume flux of foam from one crack
1220	G	acceleration due to gravity
1221	H	height of dome constructed from Bingham plastic fluid
1222	I	amount of vertical flow inflation
1223	K	the parameter 2 (κt) ^{1/2}
1224	L	separation of two locations on flow
1225	P	pressure within lava flow
1226	P_b	pressure in gas bubble
1227	Q	universal gas constant
1228	R	radius of dome constructed from Bingham plastic fluid
1229	Re	Reynolds number of flowing fluid
1230	T	temperature within lava flow
1231	T_i	eruption temperature of lava
1232	T_s	average ambient lunar surface temperature
1233	U_f	mean speed of lava flow
1234	U_d	rise speed of the magma rising through the dike
1235	U_{plug}	speed of unsheared plug in flow of Bingham plastic
1236	U_F	mean speed of flowing Bingham plastic lava foam
1237	W	width of fracture in lava crust
1238	W_f	lava flow width
1239	W_l	width of levee on foam flow
1240	W_1	width of central channel of foam
1241	W_t	total width of foam flow
1242	X	length of crack within which lava is moving
1243	Y	width of central plug in lava in crack
1244	a	uplift of lava surface
1245	b	projection of c onto horizontal plane
1246	c	length of uplifted lava slab
1247	f	wall friction factor for turbulent fluid flow
1248	m	molecular weight of water
1249	n	mass fraction of water released from lava
1250	n_{res}	water content of lava in proximal flow
1251	q	ratio of plug width to local crack width
1252	t	time since start of cooling
1253	v_b	bubble volume fraction in lava
1254	v_c	volume fraction of crystals in magma

1255	w	local width of crack in lava crust
1256	x	distance along crack
1257	Δ	temperature difference ($T_i - T_s$)
1258	α	local slope of mare surface
1259	β	bulk density of vesicular lava
1260	δ	temperature difference ($T - T_s$)
1261	η_b	bulk viscosity of vesicular lava
1262	η_l	viscosity of magmatic liquid
1263	κ	thermal diffusivity of lava
1264	λ	cooled boundary layer thickness at both top and base of a lava flow
1265	ϕ	gas bubble diameter
1266	ρ	density of magmatic liquid
1267	ρ_o	density of overburden at crack site
1268	ρ_f	density of magmatic foam
1269	σ	surface tension of gas-liquid interface
1270	τ	time since lava left vent
1271	τ_y	yield strength of magmatic foam
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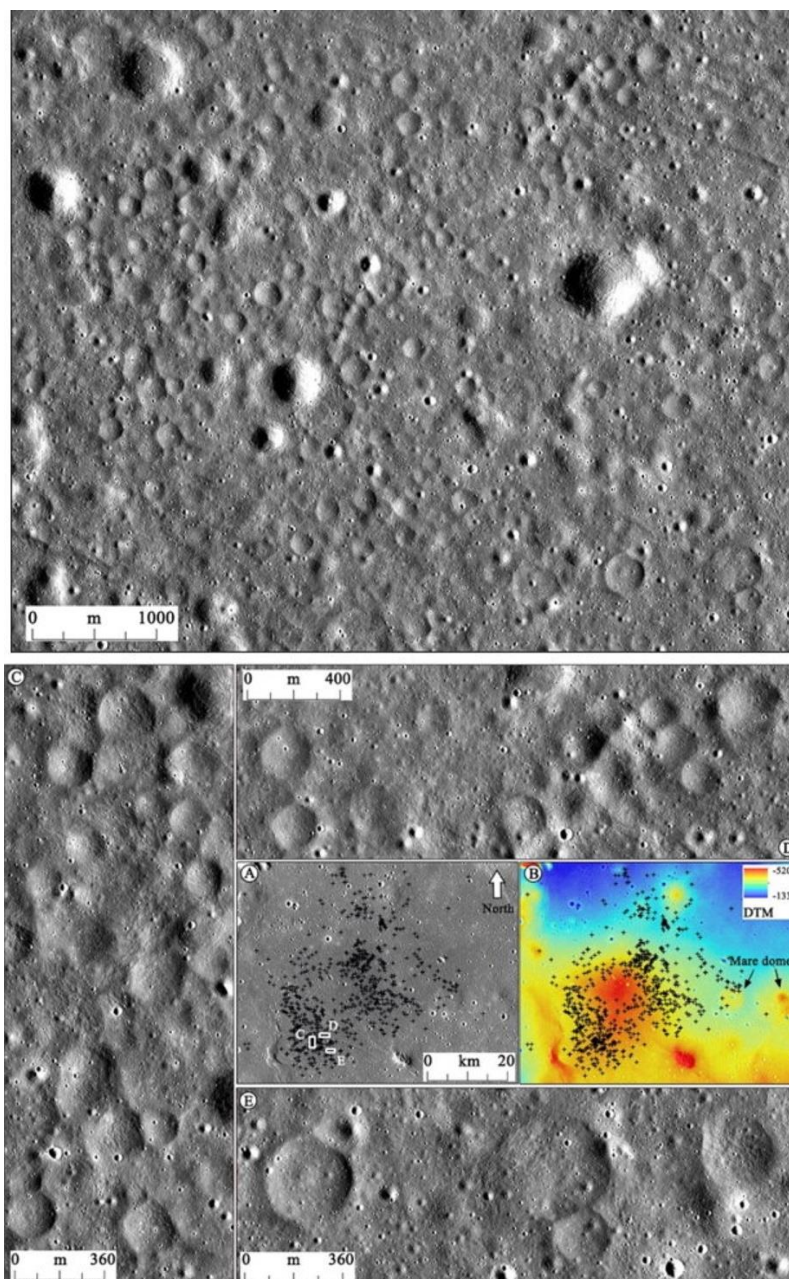
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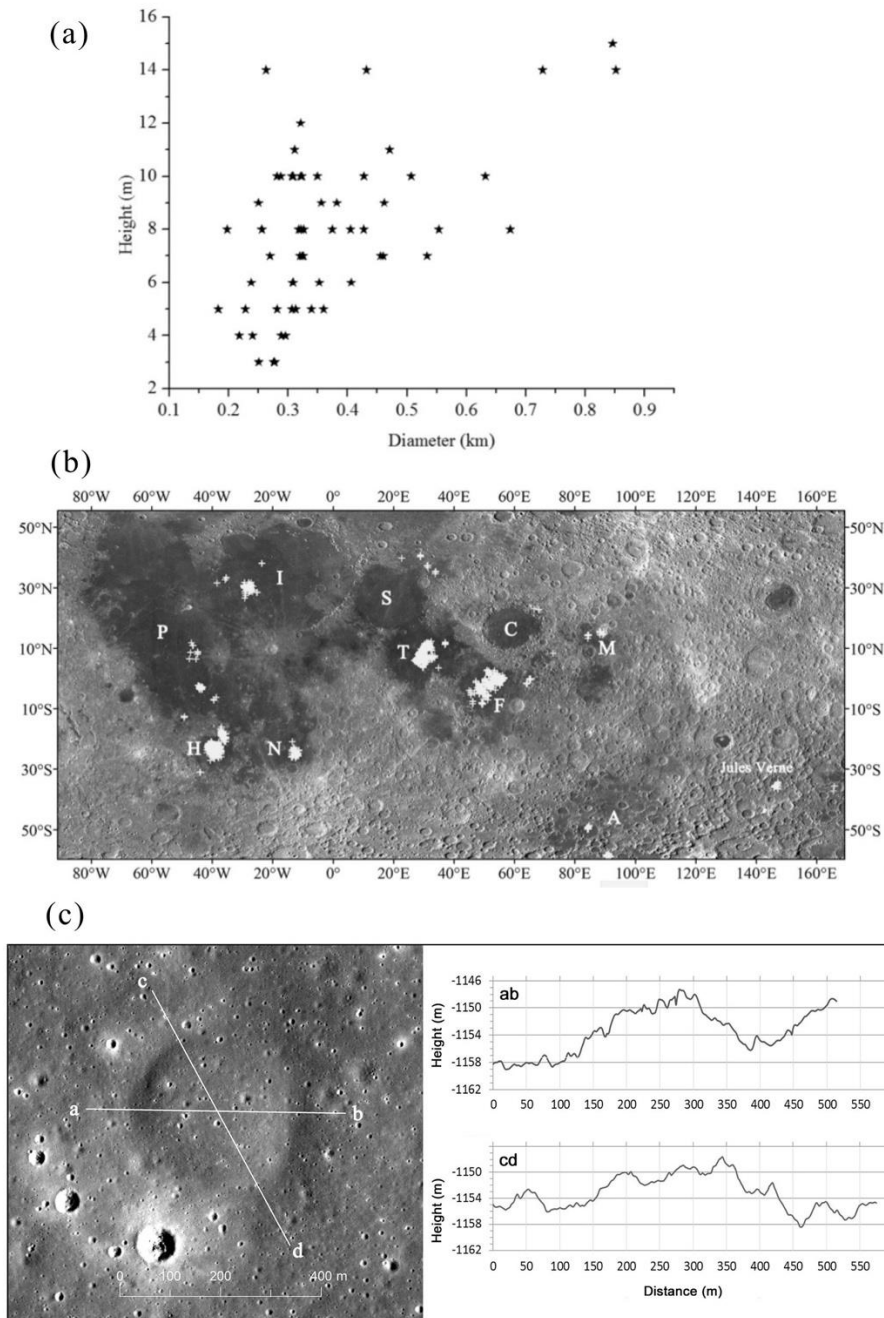
1575 **Figures and Captions:**
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1579 Figure 1. Ring Moat Dome Structures (RMDS). North is up in all images. The sun
 1580 illumination direction is from left to right. Top: LROC NAC mosaic (frames
 1581 M1096293859LE and RE) showing a dense distribution ($\sim 30.8^\circ\text{E}$, 10.3°N) of RMDSs
 1582 in Mare Tranquillitatis. Bottom: LROC WAC mosaic (A) and Kaguya TC-derived
 1583 DTM (B) of a ring moat dome structure (RMDS) terrain (Coordinates of the figure
 1584 center: $\sim 31.4^\circ\text{E}$, 11.0°N) in Mare Tranquillitatis. Enlarged views (C, D, and E) of
 1585 RMDSs in LROC NAC mosaic (frames M1096293859LE and RE) and their locations
 1586 (white boxes) are shown in Figure 1 bottom, A. Reproduced from Zhang et al.
 1587 (2017), with permission, © John Wiley and Sons/American Geophysical Union.
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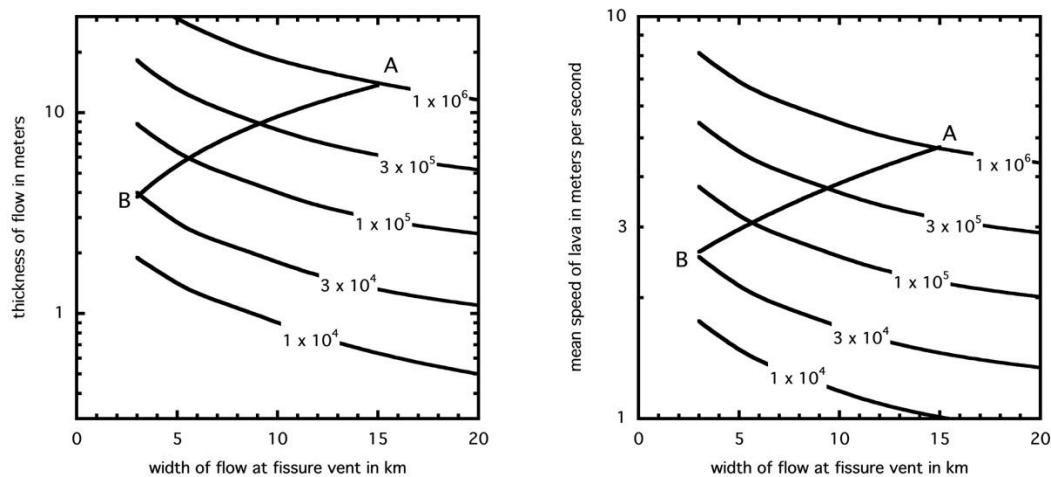
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1592 Figure 2. (a) Diameter versus height of 60 RMDs in Mare Tranquillitatis measured
 1593 from Kaguya-TC derived DTMs (Zhang et al. 2017). (b) LROC WAC mosaic
 1594 showing the distribution of about 2,600 RMDs (white crosses) identified in the lunar
 1595 maria. Imbrium (I), Serenitatis (S), Crisium (C), Tranquillitatis (T), Fecunditatis (F),
 1596 Humorum (H), Nubium (N), Marginis (M), Australe (A), and Oceanus Procellarum
 1597 (P) are labeled. Reproduced from Zhang et al. (2017), with permission, © John Wiley
 1598 and Sons/American Geophysical Union. (c) Cross-sectional profiles of an RMD that
 1599 is about 400 m in diameter located at 10.579°N, 30.689°E, LROC NAC image.

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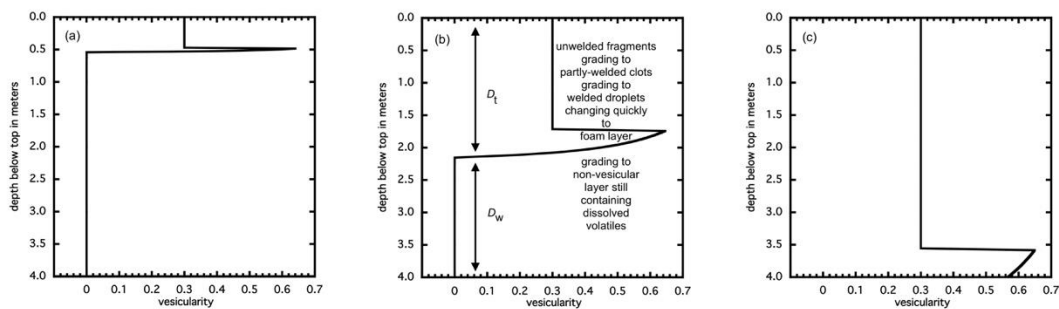
1605 Figure 3. Variation of (a) thickness and (b) mean flow speed of a lunar mare lava
 1606 flow as a function of the length along strike of the fissure feeding the flow and the
 1607 dense rock equivalent volume flux, F , being erupted - curves labelled in $\text{m}^3 \text{s}^{-1}$. Label
 1608 A indicates conditions in the early stage of the eruption and corresponds to lava that
 1609 forms the distal part of the resulting flow field; label B indicates conditions in the late
 1610 stage of the eruption and corresponds to lava forming the proximal deposits. Flows
 1611 are turbulent for all F greater than $\sim 3 \times 10^4 \text{ m}^3 \text{ s}^{-1}$ and remain so until F decreases
 1612 below this value. When F becomes less than $\sim 2 \times 10^4 \text{ m}^3 \text{ s}^{-1}$, the explosive activity at
 1613 the vent changes from hawaiian to strombolian. At all stages these flows contain a
 1614 non-zero volume fraction of solids and are treated as Bingham plastics, not
 1615 Newtonian fluids.

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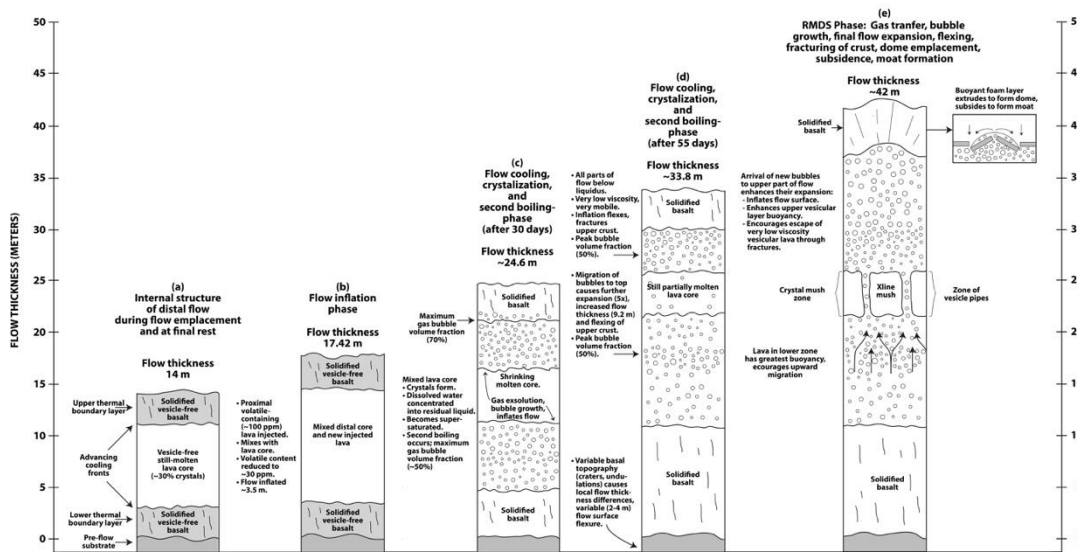
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1622 Figure 4. Variation of vesicularity with depth in 4 meter thick proximal lunar mare
 1623 lava flows. Parts (a), (b) and (c) correspond to total water contents in the erupted lava
 1624 of 100, 200 and 300 ppm, respectively. In parts (a) and (b) a layer of disaggregated
 1625 lava overlies a very vesicular layer, which in turn overlies a vesicle-free layer still
 1626 containing dissolved water. In part (c) no part of the flow retains any dissolved water.
 1627 The text within part (b) describes the successive changes that occur with depth in the
 1628 flow.

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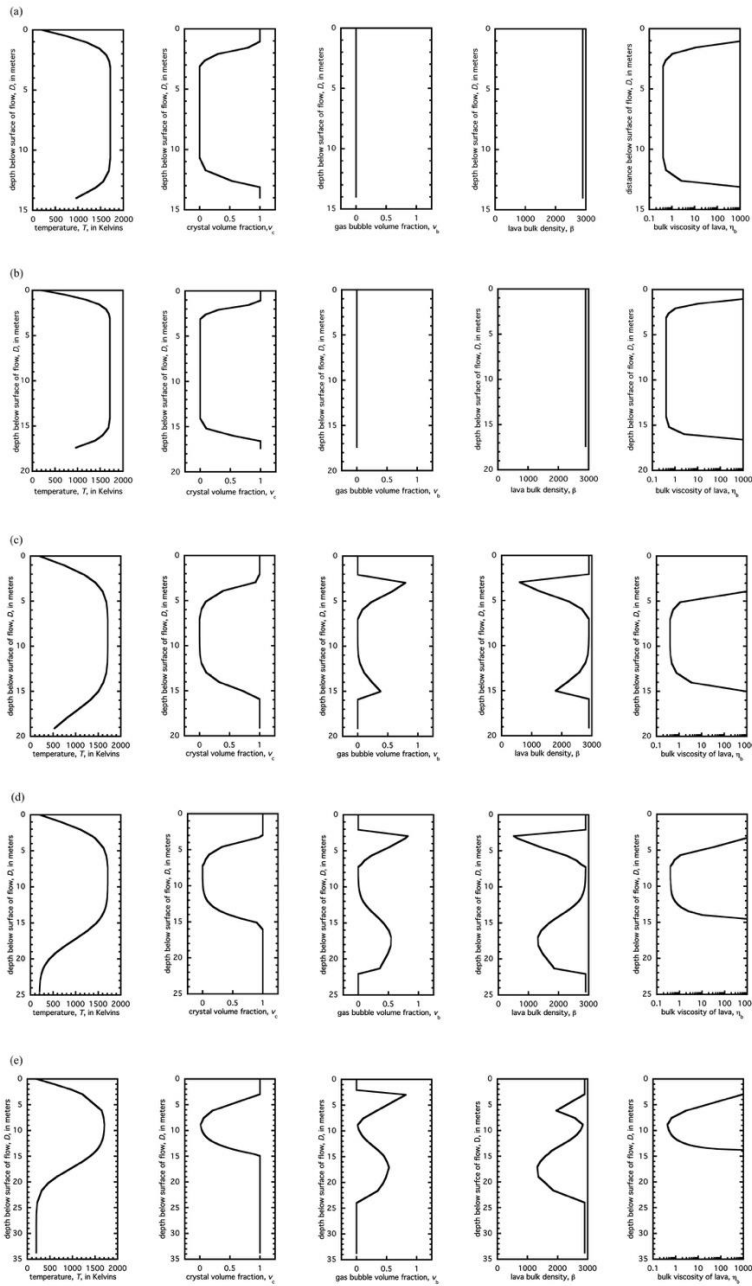
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Figure 5. Five stages in the internal structure of a distal flow during the final stages of flow emplacement, at final rest, and following further flow cooling and second boiling for the cases where late stage lava flows have $< \sim 280$ ppm volatile content (compare with Figure 6). (a) Internal structure of distal flow during flow emplacement and at final rest. (b) Flow inflation phase. (c) Flow cooling, crystallization and second boiling phase (after 30 days). (d) Flow cooling, crystallization and second boiling phase (after 55 days). (e) RMDS phase: gas transfer, bubble growth, final flow expansion, flexing, fracturing of crust, dome emplacement, subsidence, and moat formation.

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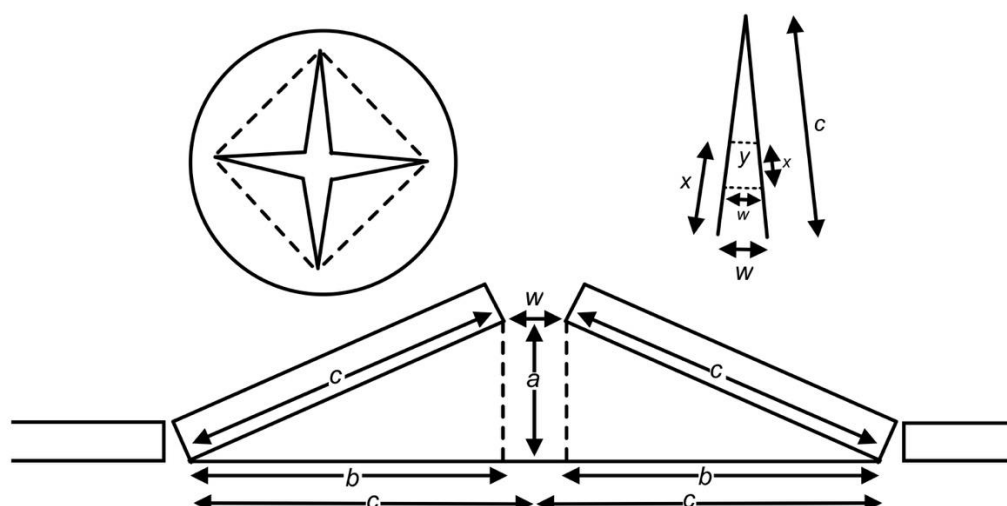
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Figure 6. Variation as a function of depth in a distal lunar mare lava flow of the temperature, crystal volume fraction, gas bubble volume fraction, bulk density, and bulk viscosity. Parts (a) and (b) represent conditions just before, and just after, respectively, proximal lava containing dissolved volatiles is injected into a distal, volatile-free flow. Parts (c), (d) and (e) correspond to time intervals of 20, 40 and 55 days, respectively, after the lower 3.42 meters of a proximal flow containing 100 ppm water is injected into a 14 m thick distal flow. Note the changing vertical scale due to the progressive inflation of the flow as increasing amounts of water are forced out of solution by second boiling due to the increasing crystal content as the interior of the flow cools.

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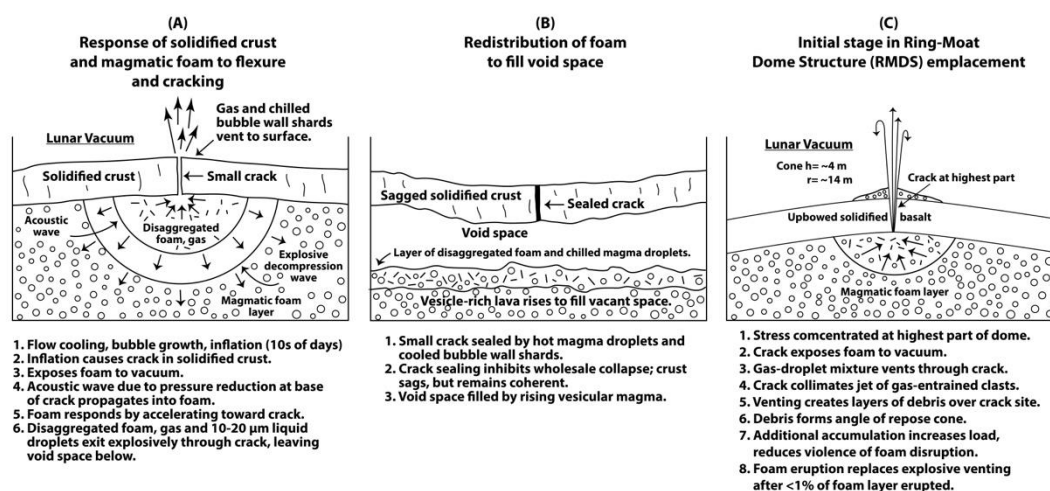
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Figure 7. Sketches of the geometry of the fracturing and uplift of a mare lava flow surface crust as foam becomes concentrated beneath the upper crust of the flow. For simplicity it is assumed that four orthogonal fractures form. Upper row: plan view; lower row: cross-section. Variables are defined and discussed in the text.



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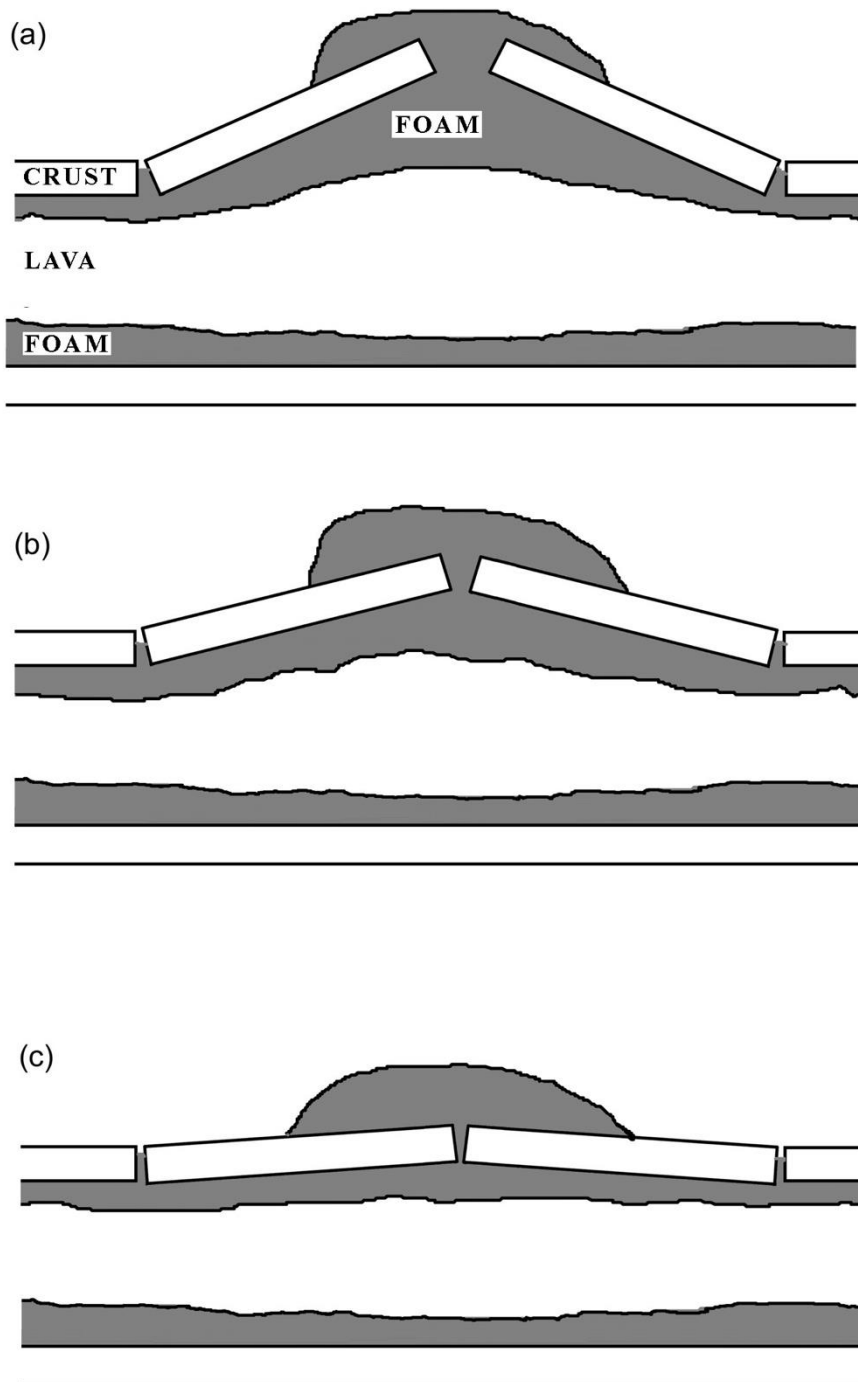
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Figure 8. Behavior of magmatic foam when cracks form in the solidified lava crust and the magmatic foam is exposed to the lunar surface vacuum. (A) Upper inflated flow configuration (see Figure 5e for context) and consequences when cracks form in the upper cooled upper flow boundary layer. (B) Initial venting of gas/foam and creation of potential void space filled by accumulating foam from lower in the flow. (C) Venting of foams to form ring-moat dome structures (RMDS).

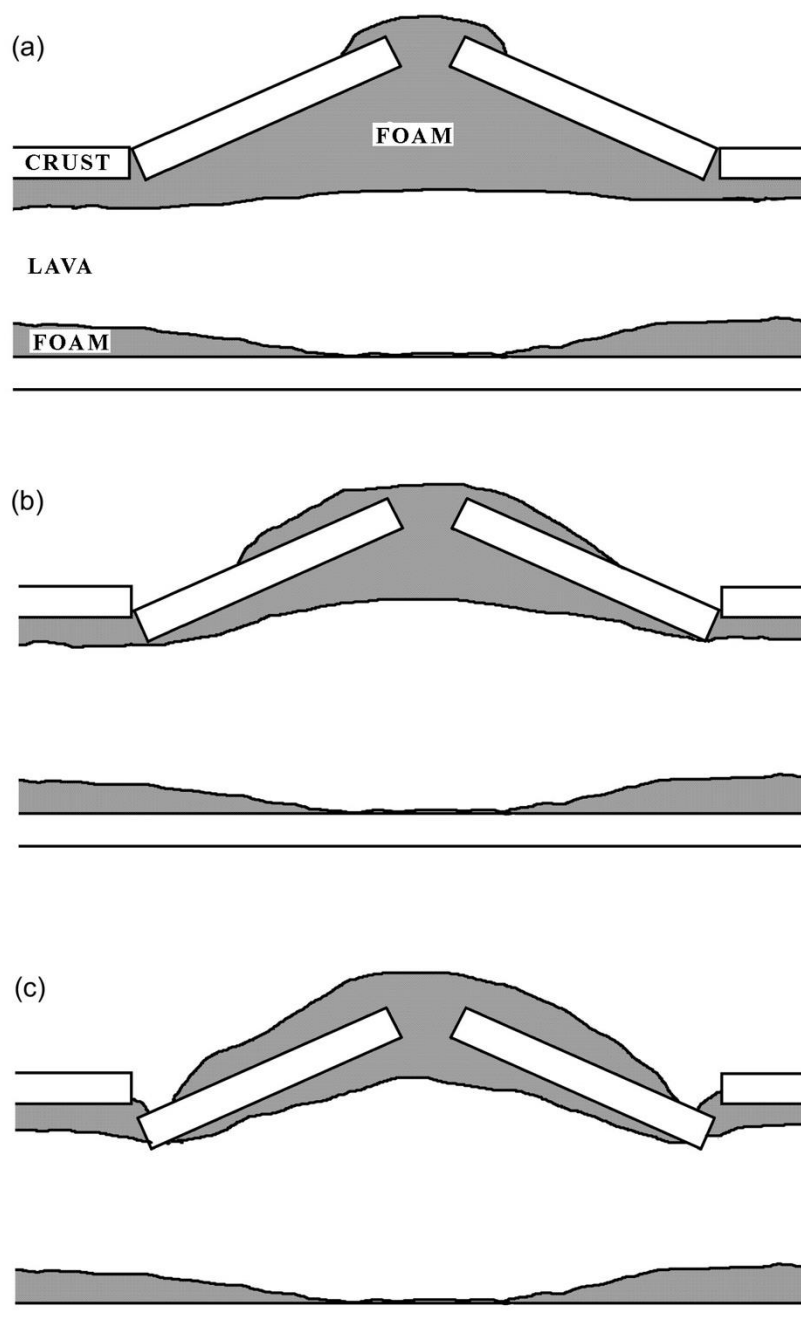
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Figure 9. A possible scenario for the progressive stages of collapse of the geometry of Figure 7 as foam is extruded through the cracks. This configuration would shut off the foam release too quickly and is not favored - see Figure 10. Vertical exaggeration ~20.

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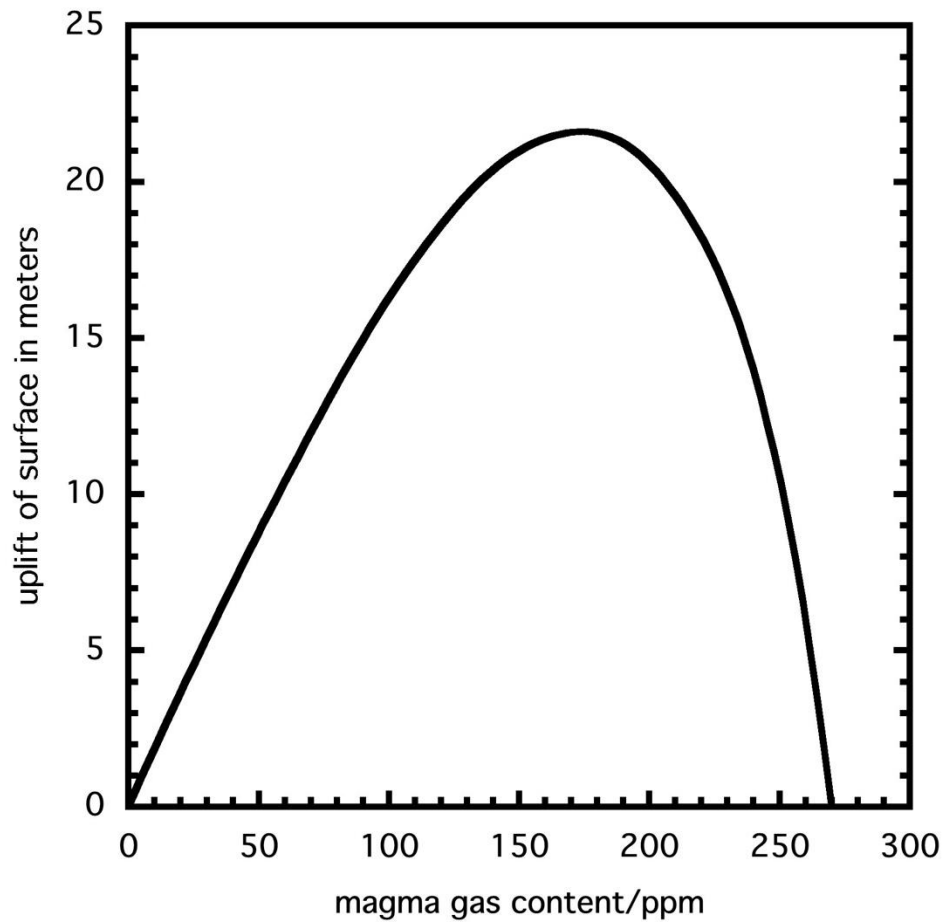
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1689 Figure 10. Preferred scenario for the progressive stages of RMDS foam emplacement
 1690 and moat formation on the basis of the general geometry shown in Figure 7. (a) Foam
 1691 (shown in grey) upwells from lower foam layer to upper foam layer, causing
 1692 upbowing and cracking of brittle crust, and begins extrusion through cracks in the
 1693 lava crust. (b) Subsidence of the crustal slabs maximizes both the rate and volume of
 1694 the foam released. (c) Note the progressive production of a moat at the edge of the
 1695 mound by this pattern of subsidence. See Figure 5 for the sequence of events leading
 1696 up to this final stage. Vertical exaggeration ~ 20 x.

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1701 Figure 11. Uplift of the surface of a stationary lava flow by gas released when cooling
1702 induces second boiling in lava injected into the stationary flow by continuing activity
1703 at the vent. The uplift is given as a function of the dissolved gas mass fraction in the
1704 injected lava.

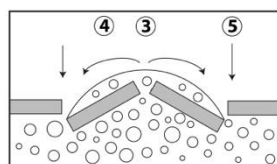
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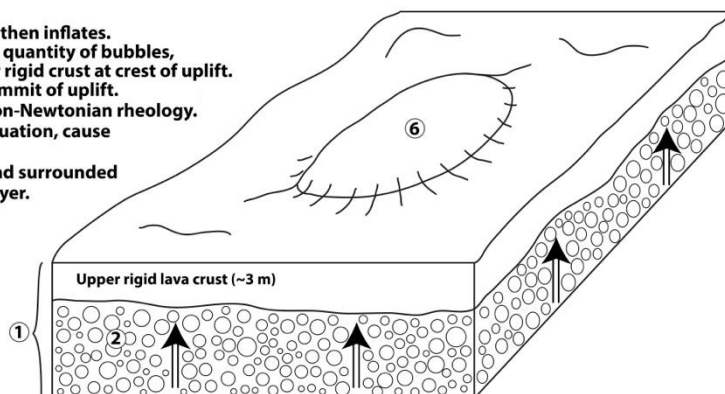
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Inflated flow - Second boiling: Proposed Model for Ring-Moat Dome Structures (RMDS)

- ① Flow (at least 10 m thick) halts, and then inflates.
- ② Second boiling produces significant quantity of bubbles, expands flow (arrows), cracks upper rigid crust at crest of uplift.
- ③ Foam extrudes through cracks at summit of uplift.
- ④ Mound shape controlled by foam non-Newtonian rheology.
- ⑤ Weight of foam, evolving foam evacuation, cause subsidence of rigid crust.
- ⑥ Final product is circular dome/mound surrounded by moat from subsidence of foam layer.



Buoyant foam layer forms, then extrudes to form dome, subsides to form moat



PREDICTED CHARACTERISTICS CONSISTENT WITH OBSERVATIONS:

- | | | |
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| <ol style="list-style-type: none"> 1. Flow halts before inflation, no shearing or no deformation of RMDS. 2. Dome composition ~same as surrounding, underlying flow. 3. Occur only on parts of flow: requires second boiling for inflation and extrusion. | <ol style="list-style-type: none"> 4. Dome diameters (100-500 m) consistent with estimated substrate topographic irregularities. 5. Rough flow surface topography can cause mound shape variations from circular to oval. 6. Occur in clusters due to second boiling region in flow. | <ol style="list-style-type: none"> 7. Dome height (typical < ~14 m) is constrained by maximum amount of gas available. 8. Diameters of RMDS not strongly dependent on flow thickness. 9. Sub-flow topographic variations may produce a range of RMDS sizes. |
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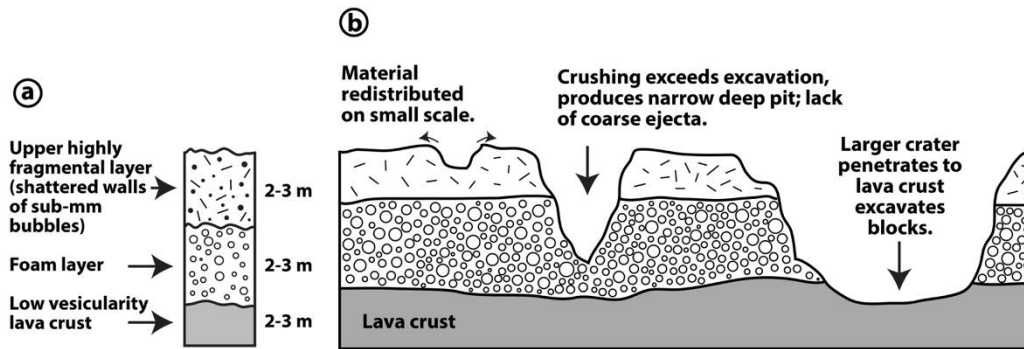
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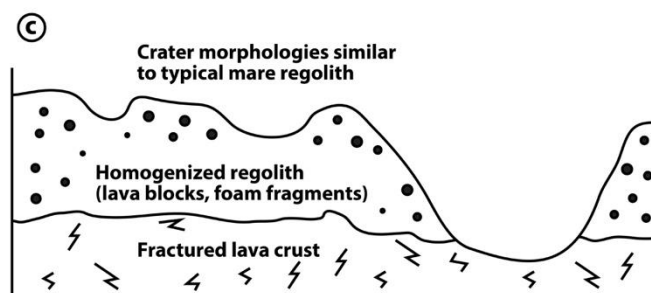
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Figure 12. Illustration of the proposed model for Ring Moat Dome Structure (RMDS) formation due to flow inflation and second boiling. Perspective and cross-sectional views illustrate the main steps following cessation of injection of lava with dissolved volatiles that inflates the core of the initially emplaced flow: flow cooling, second boiling, foam formation, flow inflation, rigid crust cracking and foam extrusion to form RMDS. Predicted RMDS characteristics that are consistent with observations (Zhang et al., 2017; 2018a) are listed. See Figure 5 for steps in flow emplacement leading up to these final stages of RMDS formation.



Initial post-dome emplacement cratering influenced by vertical target structure. Dome/mound surface: Coarse ejecta scarce, vesicular/low density material yields low-strength radar return, thermal anomalies. Initial differences smoothed out with impact regolith development.



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Figure 13. Cross-sectional views of an RMDS dome segment illustrating the change in physical properties as a function of time, and the response of these evolving target properties to the subsequent impact events that are building the regolith. (a) The initial vertical column consists of an upper part of an RMDS dome, illustrating the three predicted layers (1-shattered foam bubble walls; 2-foam layer; 3-uplifted solid lava crust). (b) Initial and early (~1-10 Ma) regolith development, in which small craters (left) simply redistribute the upper 2-3 m thick highly fragmental layer, larger craters (middle) penetrate into the 2-3 m thick foam layer and produce deeper, narrower craters due to crushing of foam, and even larger craters (right), penetrate to the solidified lava crust below and can excavate blocks of the uplifted solid lava crust (see Figures 10 and 12). (c) Later-stage regolith development (>10-1000 Ma) in which impacts superposed in the intervening period have tended to homogenize the initial differences in physical properties (a and b) and to produce a regolith and superposed crater morphologies that are very similar to those being developed on adjacent, non-RMDS maria. These evolutionary responses of superposed craters to regolith development may influence the impact crater size-frequency distribution, and thus inferred ages, of RMDS features relative to non-RMDS maria. In situ samples of mature RMDS regolith soils are predicted to have a much higher abundance of shattered walls of sub-mm bubbles and fine foam fragments than typical non-RMDS regolith (Head and Wilson, 2019).