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1 **Statistical model specification and power: recommendations on the use of test-qualified pooling in**
2 **analysis of experimental data**

3

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7 **Abstract**

8 A common approach to the analysis of experimental data across much of the biological sciences is
9 test-qualified pooling. Here non-significant terms are dropped from a statistical model, effectively
10 pooling the variation associated with each removed term with the error term used to test
11 hypotheses (or estimate effect sizes). This pooling is only carried out if statistical testing on the basis
12 of applying that data to a previous more complicated model provides motivation for this model-
13 simplification; hence the pooling is test-qualified. In pooling, the researcher increases the degrees of
14 freedom of the error term with the aim of increasing statistical power to test their hypotheses of
15 interest. Despite this approach being widely adopted and explicitly recommended by some of the
16 most widely-cited statistical textbooks aimed at biologists, here we argue that (except in highly
17 specialised circumstances that we can identify) the hoped-for improvement in statistical power will
18 be small or non-existent, and there is likely to be much reduced reliability of the statistical
19 procedures through deviation of type I error rates from nominal levels. We thus call for greatly
20 reduced use of test-qualified pooling across experimental biology, more careful justification of any
21 use that continues, and a different philosophy for initial selection of statistical models in the light of
22 this change in procedure.

23 **Key words:** experimental design, pseudoreplication, model simplification

24 **Introduction**

25 A common approach to the analysis of experimental data across disparate parts of the biological
26 sciences is test-qualified pooling. A common manifestation of this approach can be summarised as
27 follows: the researcher fits their data to a model that they select on the basis of the design of their
28 study and the hypotheses they are interested in testing. After examining the significance of terms in
29 the model that are not specifically related to the hypothesis currently under investigation, the
30 researcher then removes non-significant terms from the model, and re-fits their data to this
31 simplified model. That is, some terms were included in the original model not because they allow an
32 interesting hypothesis to be tested but because (on the basis of the specifics of the experimental
33 design allied to previous knowledge of the system) they were expected to explain substantial
34 portions of the variation. If the data generated in this particular experiment do not suggest that one
35 or more of these terms are strongly influential then they are dropped from the model, and further
36 analysis is performed based on a simplified model. Such a simplification process is often seen as
37 attractive in making presentation of results more compact, in highlighting more influential variables,
38 and/or in increasing statistical power for exploring the significance of remaining terms. By
39 simplifying the model in this way, the researcher is effectively *pooling* the variation associated with
40 each removed term with the error term that will ultimately be used to test their hypotheses. This
41 pooling is only carried out if statistical testing on the basis of applying that data to a previous more
42 complicated model provides motivation for this approach, hence the pooling is *test-qualified*. In
43 pooling, the researcher increases the degrees of freedom of the error term with the aim of
44 increasing statistical power to test their hypotheses of interest. Despite this approach being widely
45 adopted and explicitly recommended by some works on data analysis (e.g. [1]), other influential
46 authors explicitly warned against this practice (e.g. [2]). Here we want to offer some resolution of
47 this apparent conflict in the literature, in order to help authors, reviewers, editors and readers
48 evaluate the consequences of pooling in different circumstances. Note that although we couch this
49 discussion in terms of null-hypothesis statistical testing, the arguments transfer naturally to

50 approaches based on estimation of effect size; our discussion is however focussed on the analysis of
51 data from planned experiments rather than from purely observational studies. The costs and
52 benefits of test-qualified pooling are more clear-cut for planned experiments where potential
53 confounding factors can often be eliminated or controlled for by careful experimental design,
54 removing the need to deal with these factors statistically. Also, planned experiments generally are of
55 what is termed a “confirmatory” nature, where the study specifically aims to test one or more
56 hypotheses known from the outset. Observational studies more often have an “exploratory”
57 motivation involving measuring a broad range of variables and then seeking to rank them in terms of
58 potential importance and influence. We return to these issues in the *Discussion*.

59 **Being clear what pooling is and why you might want to do it**

60 To clarify the issues we consider a specific example. You are interested in the effect of an
61 experimental treatment (a new humidification system) on the growth of individually-potted tomato
62 plants. Your experiment will be conducted in ten small greenhouses at your research station, and the
63 nature of the treatment means that it has to be applied to whole greenhouses. You install the
64 humidification system in five (randomly selected) greenhouses, leaving the other five as controls,
65 and you assay the growth of 40 tomato plants in each greenhouse. In this design the greenhouse is
66 the experimental unit, and any hypothesis test of the treatment should use an error based on the
67 variation amongst greenhouses rather than variation amongst the individual plants. In this case the
68 simplest means of analysis would be to calculate a mean growth rate across the 40 plants in each
69 greenhouse and carry out a one-way ANOVA using these 10 independent data points.

70 However, as a thought experiment, suppose that we somehow knew for a fact that growth
71 conditions (in the absence of our treatment manipulation) were absolutely identical amongst our
72 greenhouses. In this imaginary situation we might argue that, since greenhouse-to-greenhouse
73 variation is not confounded with any treatment effect we can use the growth measures from the
74 individual plants as independent data points in our analysis. This will result in a substantial increase

75 in our degree of freedom, and consequently our statistical power to detect treatment effects. Of
76 course in reality, we cannot usually know with certainty whether our greenhouses vary, and this has
77 led to the development of methods for test-qualified pooling. In this case, we would start by fitting
78 the nested model defined by the design of our study (with individual plants being nested within
79 greenhouse). This would include the treatment term, a nested term for the variation amongst
80 greenhouses in the same treatment group, and a second error term corresponding to the variation
81 amongst plants in the same greenhouse. The key to test-qualified pooling is that the set of data itself
82 influences the nature of the analyses performed on it. If initial analysis of the full model indicates
83 substantial variation amongst greenhouses, then the significance of the treatment term is tested
84 using the variation amongst greenhouses as its error term with 8 df. However, if there is no evidence
85 of substantial greenhouse-to-greenhouse variation in this initial analysis then the among-
86 greenhouse and the true error variations are pooled, and this combined error term with 398 df is
87 used then to provide a test of the treatment effect that is expected to benefit from higher statistical
88 power (see [3-5] for commonly-cited texts that recommend this approach). The justification that
89 advocates of test-qualified pooling give for this approach is that in the absence of any greenhouse
90 effect, the among-greenhouse and the within-greenhouse error terms are both estimating the same
91 thing, and so by combining them we get a better estimate than we would estimating the two
92 separately.

93 However pooling is not limited to nested designs. Continuing with tomatoes and greenhouses, you
94 now want to compare the effects of four different growing media in individually-potted tomato
95 plants rather than the effect of humidity. To gain a sufficient sample size for the experiment you
96 have to use three different greenhouses to keep all the plants, but because your treatments can now
97 be applied randomly to individual plants, you randomly allocate equal numbers of plants to each
98 treatment in each greenhouse leading to a randomised block design (with specific greenhouse
99 identity as the blocking factor, with three levels). The statistical model implied by this design would
100 include terms for both treatment applied to a plant and the specific greenhouse a plant was kept in,

101 as well as a treatment-by-greenhouse interaction and an amongst-plant error term based on the
102 variation amongst individual plants within the same treatment-greenhouse combination. Depending
103 on the exact hypothesis we wish to test, the appropriate error term for our treatment effect will be
104 either the interaction term, or the amongst-plant error term [6], but in either case, if the interaction
105 term is not significant, we might chose to pool its variation with the amongst-plant error term prior
106 to testing the treatment effect. Similarly, we might then decide that if the greenhouse term is also
107 non-significant, we would add that source of variation and its associated degrees of freedom to our
108 error pool. In either case, we would be carrying out test-qualified pooling.

109 Another form of pooling can involve the initial test that triggers whether pooling is used or not being
110 entirely separate to the model testing the hypotheses of interest. To illustrate this, we return to the
111 experiment above comparing the effects of four different growing media on individually-potted
112 tomato plants. Imagine that, because of a change of supplier at your institute, you ended up using
113 two different but broadly similar types of pots to grow the tomatoes in. Plants are randomised to
114 pot type as well as to growth medium and greenhouse. You really do not expect type of pot to
115 influence growth rates, but just to be careful you first of all perform a t-test comparing growth rates
116 across the two types of pot. Your plan is that if (as you expect) this t-test reveals no evidence of a
117 difference, you report this and use this test as justification for pooling data across the two pot types
118 in your subsequent analyses. However if it does reveal evidence of a difference then you will either
119 add pot-type as a factor in subsequent analyses or carry out separate analyses for the two types of
120 pot. Again, there is the potential for pooling driven by the results of a pre-test, so this scenario is
121 another manifestation of test-qualified pooling.

122 **Why is test-qualified pooling controversial?**

123 The case against pooling was made most forcefully and explicitly in the biological literature by Stuart
124 Hurlbert primarily in relation to its use in nested designs [2]. Hurlbert coined the expression
125 *pseudoreplication* for the situation where authors treat data-points that are not independent as if

126 they were independent in their data analysis. His original paper on this [7] has been cited over 6000
127 times and has been hugely influential in the design of data collection and the analysis of data
128 spanning all of biology. Hurlbert considers the pooling of errors in a nested analysis to be a form of
129 pseudoreplication, a form that he calls *test-qualified sacrificial pseudoreplication*. He argues that
130 pooling biases p-values downwards and biases confidence intervals towards being too narrow. He
131 further argues that demanding a higher p-value than 0.05 in the initial test before pooling (a process
132 often called “sometimes pooling”) reduces but does not eliminate these problems. An analogous
133 argument can be made against pooling interaction terms with error terms when analysing
134 randomised block designs [6]. However, even in situations where pooling might not be regarded as
135 analogous to pseudoreplication (e.g. pooling an interaction between two fixed factors prior to
136 testing the main effects), type 1 error rates can be increased (as we will see below). Despite this,
137 pooling is still regularly practiced, and is recommended in influential statistics textbooks aimed at
138 biologists (e.g. [3-5]) and research papers on statistical methodology (e.g. [2,8]). In the next section
139 we argue that both philosophically and pragmatically there are strong arguments for siding with
140 Hurlbert.

141 **The philosophy and pragmatics of pooling**

142 The two main philosophical arguments against pooling are well articulated by Newman et al. [7], and
143 can be explained in the context of our greenhouses and growth media example. Firstly, if we use
144 pooling, then the way that we test for an effect of growth medium becomes conditional on the data,
145 but that conditionality is not acknowledged in the associated p-values. That is, whether we test the
146 effect of medium in a model with or without a *greenhouse* term will be determined by the data.
147 Philosophically, p-values are probabilities based on a very large number of notional replicates of
148 exactly the experiment under investigation. So imagine that we repeat the full experiment and
149 analysis of the resulting data again and again. In replicates of this experiment, if we adopt a test-
150 qualified pooling approach then sometimes the analysis will test the main hypothesis one way and

151 sometimes the other. For each form of the analysis, that particular analysis will be implemented only
152 for a specific subset of replicate experiments determined by the patterns of data in that replicate
153 experiment. Importantly, this is a biased sample of all the possible replicate experiments in terms of
154 properties of the sample. Yet the test is predicated on the assumption that it is applied to data from
155 an experiment drawn without bias from the population of all possible replicates of this experiment.
156 It is this mismatch that leads to lack of control of type I error and of confidence intervals. Secondly,
157 by pooling (no matter what critical value we compare the calculated p-value against) we are
158 accepting that the null hypothesis that there is no effect of *greenhouse* is true, and the whole
159 philosophy of null-hypothesis statistical testing is that the null hypothesis is never accepted as true,
160 rather we might either reject it or find that we do not have sufficient grounds to reject it. Thus, from
161 a purist philosophical perspective pooling should not be recommended.

162 We next ask if there is a pragmatic argument that says that pooling may have some less-than-ideal
163 properties, but pooling leads to relatively mild misbehaviours that are sometimes outweighed by the
164 (enhanced power) benefits of pooling. There is no underlying theory to give general and definitive
165 answers to the issue of pragmatics raised above; all we have to go on are a number of numerical
166 explorations of specific cases. However, the consensus in this literature is that (i) pooling can cause
167 actual type one error rates to be very different from the nominal value, and (ii) there is no consistent
168 and substantial increase in power to compensate. Walde-Tsadik & Afifi [9] explore the effect of
169 always pooling when one factor is associated with a p-value above 0.05, and also of “sometimes
170 pooling” when the required critical value was higher than 0.05 in two-way ANOVA random effects
171 models. They found that both procedures very rarely offered adequate control of type-1 error rate
172 and even less commonly lead to significant improvement in power to test for an effect of the other
173 factor. Hines [10] performed extensive simulations and concluded that for multifactorial ANOVA
174 “the conditions for pooling to be even potentially rewarding are more restrictive than might be
175 expected, and power improvements are generally lower”. Janky [11] performed a similar analysis of
176 split-plot designs and concluded that “pooling generally inflates Type I error and offers at best

177 insubstantial gain in power (and often power loss) relative to the nominal test.” Even when using a
178 conservative “sometimes pooling” value of $\alpha = 0.35$ to trigger pooling, Janky found the type I error
179 rate in subsequent tests on pooled data rose from the nominal 5% to generally somewhere between
180 7% and 11%. This study was interesting for highlighting that pooling actually led to a reduction of
181 power more often than it lead to a substantial gain in power; this occurs because the increase in
182 inherent variation caused by pooling dominates any effect of increased degrees of freedom devoted
183 to exploring remaining factors. Figure 1 shows examples of deviations in both directions from the
184 nominal 5% level for type I error rates generated by simulations of our whole-greenhouse-treatment
185 thought experiment. In exploring our model we found that small changes in parameter values could
186 lead to substantial change in the magnitude and direction of deviations from the nominal level. It is
187 difficult to make generalisations about the circumstances under which deviations will be strongest.
188 In common with the other studies discussed directly above, we found that the direction and
189 magnitude of deviations are driven by a complex interaction between structure of the experimental
190 design, aspects of the shape of the underlying “population” from which sample values are obtained,
191 and sample sizes. Also, as the highest line in Figure 1 illustrates, relationships with parameter values
192 can be non-monotonic.

193 **Discussion and Conclusion**

194 Use of test-qualified pooling is widely adopted, but its prevalence across biological sciences is
195 patchy. For example, it is much less commonplace in clinical trials; where often statistical analyses
196 have to be specified in pre-registration of trials, and thus scope for flexibility in data analysis is
197 reduced. Test-qualified pooling is also relatively uncommon in the agricultural sciences, where
198 particular designs and modes of analysis that avoid issues of pooling are traditional; and the
199 statistical software package *Genstat* is commonly used, which is particularly suited to forms of
200 analyses that avoid test-qualified pooling.

201 We do still consider that test-qualified pooling is over-used in biology. Simply, in “confirmatory
202 studies” based on designed experiments where we aim to test specific hypotheses (or estimate
203 specific effect sizes) we do not recommend pooling under any circumstances. The often-modest
204 expected increases in power from pooling do not make it an attractive option when its drawbacks
205 are taken into account. Apart from statistical power, the other attraction to pooling is simplification
206 of the presentation of results, but we feel that this will never be sufficient grounds for justifying the
207 process. We would only recommend pooling in such a study if the decision to consider test-qualified
208 pooling was made on the basis of a prior simulation study that aimed at evaluating the
209 consequences of pooling for Type I and Type II error rates. We have yet to see an example of a study
210 that provided such a justification for pooling.

211 As we mentioned in the *Introduction*, it is not as easy to offer clear and simple guidance on pooling
212 in purely observational studies, and studies where the researchers’ aims are more focussed on
213 exploration or prediction than on testing specific hypotheses. However, in such situations pooling
214 can be seen as a facet of *model selection* – which is an area of considerable activity in applied
215 statistics. A particularly useful introduction to the concepts involved is that of Chatfield [12]. He
216 makes the point that if the same data-set is used to both select the most appropriate model from a
217 suite of alternatives and also to fit that model, then the interpretation of the fitted model should be
218 quite different from circumstances where the form of the model is decided upon first and only then
219 is the data applied to fit that model. Where there is uncertainty as to the most appropriate model,
220 then there are methodological developments in *model averaging* that can acknowledge this ([13]
221 and [14] offer good introductions for the biologist). A failure to properly acknowledge model
222 uncertainty when the same data is used to select and fit the model can read to very unreliable
223 inferences ([12],[15],[16]).

224 Despite the complexity of the literature on model selection and model uncertainty, we feel that we
225 can offer a general opinion on the utility of test-qualified pooling outside designed experiments. For

226 more exploratory studies where the intention is to identify factors that might be of interest, rather
227 than to test specific hypotheses, then test-qualified pooling might be more attractive; since
228 researchers may be willing to live with loss of control of type I error rates if this helps boost their
229 statistical power to flag up factors of interest. That is, they may be prepared to suffer higher rates of
230 false positives to boost their likelihood of detecting real effects. We expect that these power gains
231 may sometimes be considerable for nested-designs. However for other types of design the literature
232 discussed in the last section should serve as a caution that power gains from pooling may be small or
233 non-existent. Our view is that even in exploratory studies, test-qualified pooling cannot really be
234 recommended except perhaps where the design is nested and where the size of the experiment was
235 reduced from its ideal size by practical constraints or unforeseen adverse circumstances.

236 Where does this leave the experimenter in our tomato plant example who just wanted to be diligent
237 and reassure themselves and their readers that there was no effect due to two different types of
238 pots being used? They have to make a decision about how important this check is to them. If they
239 feel that it is worth investing a few degrees of freedom in, then they should include *type-of-pot* as a
240 factor in their analysis and pay a modest cost in reduced power to test the hypothesis (comparing
241 different growth media) that they are really interested in. Alternatively, they may decide that careful
242 experimental design and explanation of that experimental design should allay concerns about
243 differential effects of pot types sufficiently that there is no need for formal statistical testing. More
244 generally, we all have to accept that there are no free statistical analyses, and think hard about
245 which factors to include in any model. This is analogous to the decision to block on a given variable
246 in experimental design. It is only advantageous to block on variables that explain a substantial
247 fraction of variation between experimental units, otherwise the degrees of freedom lost in including
248 that blocking term are not compensated for by effective partitioning of variation into error and other
249 terms.

250 Sometimes we can make a strong enough case based on careful experimental design (especially use
251 of randomisation), biological intuition, and logical reasoning for why we can safely assume that some
252 potentially influential factors are in fact very unlikely to be important in our study, and so we omit
253 them from our statistical procedures. In fact, we do this all the time. In our example the researcher
254 felt no need to test whether which shelf on a greenhouse a pot was placed on had an effect, or what
255 side of the greenhouse, or how near to the door of the greenhouse it was. Sometimes we will feel
256 that we cannot make a sufficiently strong case this way, and we should then include that factor in
257 our model and explore its effects statistically. As so often in the design and analysis of scientific
258 studies, there are no black-and-white rules for which factors to include in your statistical model; we
259 need to think hard about it and justify our choices in terms of experimental design, understanding of
260 underlying biology and logical reasoning. This should be good news: model selection should be much
261 more about biology than about mathematics and probability theory – and biology is what we are
262 interested in.

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265 **Author contributions:** This article was conceived, developed and written equally by both authors.

266 **References**

267 [1] Schank, J. C., & Koehnle, T. J. (2009). Pseudoreplication is a pseudoproblem. *Journal of*
268 *Comparative Psychology*, 123(4), 421.

269 [2] Hurlbert, S. H. (2009). The ancient black art and transdisciplinary extent of
270 pseudoreplication. *Journal of Comparative Psychology*, 123(4), 434.

271 [3] Sokal, R. R., & Rohlf, F. J. (1995). *Biometry: the principals and practice of statistics in biological*
272 *research. WH Freeman and Company, New York.*

273 [4] Quinn, G. P., & Keough, M. J. (2002). *Experimental design and data analysis for biologists.*
274 Cambridge University Press.

- 275 [5] Zar, J. H. (1999). *Biostatistical analysis*. Pearson Education India.
- 276 [6] Newman, J. A., Bergelson, J., & Grafen, A. (1997). Blocking factors and hypothesis tests in
277 ecology: is your statistics text wrong?. *Ecology*, 78(5), 1312-1320.
- 278 [7] Hurlbert, S. H. (1984). Pseudoreplication and the design of ecological field experiments. *Ecological*
279 *monographs*, 54(2), 187-211.
- 280 [8] Crits-Christoph, P., Tu, X., & Gallop, R. (2003). Therapists as fixed versus random effects-some
281 statistical and conceptual issues: a comment on Siemer and Joormann (2003). *Psychological Methods*
282 8, 518-523.
- 283 [9] Wolde-Tsadiq, G., & Afifi, A. A. (1980). A comparison of the “sometimes pool”, “sometimes switch”
284 and “never pool” procedures in the two-way ANOVA random effects model. *Technometrics*, 22(3),
285 367-373.
- 286 [10] Hines, W. G. S. (1996). Pragmatics of pooling in ANOVA tables. *The American Statistician*, 50(2),
287 127-139.
- 288 [11] Janky, D. G. (2000). Sometimes pooling for analysis of variance hypothesis tests: A review and
289 study of a split-plot model. *The American Statistician*, 54(4), 269-279.
- 290 [12] Chatfield, C. (1995). Model uncertainty, data mining and statistical inference. *Journal of the Royal*
291 *Statistical Society, Series A*, 158, 419–466.
- 292 [13] Whittingham, M. J., Stephens, P. A., Bradbury, R. B. & Freckleton, R. P., (2006). Why do we still
293 use stepwise modelling in ecology and behaviour?. *Journal of Animal Ecology*, 75, 1182-1189.
- 294 [14] Richards, S. A., Whittingham, M. J. & Stephens, P. A., (2011). Model selection and model
295 averaging in behavioural ecology: the utility of the IT-AIC framework. *Behavioral Ecology and*
296 *Sociobiology*, 65, 77-89.
- 297 [15] Blanchet, F. G., Legendre, P. & Borcard, D., (2008). Forward selection of explanatory
298 variables. *Ecology*, 89, 2623-2632.

299 [16] Mundry, R. & Nunn, C. L., (2009). Stepwise model fitting and statistical inference: turning noise
300 into signal pollution. *The American Naturalist*, 173, 119-123.

301

302

303 **Figure legend**

304 Figure 1: To illustrate how the type 1 error rate can be affected by test qualified pooling we
305 examined simulated data sets for both 4 (broken line) and 10 (solid line) greenhouses. In both cases,
306 equal numbers of greenhouses were allocated to control or treatment conditions (but condition had
307 no effect on plant growth), and 40 plants were measured in each greenhouse. We also examined the
308 effect of two different alpha levels for the pooling decision (recommended in [3]: open circles = 0.25
309 and closed circles = 0.75), and several different levels of among-greenhouse variation (σ^2). Under
310 many different parameter combinations the actual type 1 error rate differs from the desired value of
311 0.05, sometimes substantially.

312 Plant growth rates were calculated as a baseline value (10) plus an individual deviation drawn from
313 $N(0,1)$ plus a greenhouse-deviation drawn from $N(0,\sigma)$ and the same for all plants in a given
314 greenhouse. We analysed each data set in two ways. First we carried out a nested analysis of
315 variance in which the treatment mean square was tested over the among-greenhouses within-
316 treatment mean square. The same analysis tested for variance among greenhouses by comparing
317 the among-greenhouses mean square to the amongst-plants error mean square. Second we carried
318 out an analysis in which data from all greenhouses was pooled. The decision as to which P value to
319 use for our actual hypothesis test for the effect of the treatment was based on the significance of
320 the among-greenhouse test at one of two alpha levels. If this test was significant at the appropriate
321 alpha level we used the P value from the nested model, otherwise we used the P value from the
322 second model. This process was repeated 100000. The proportion of these runs that gave a P value

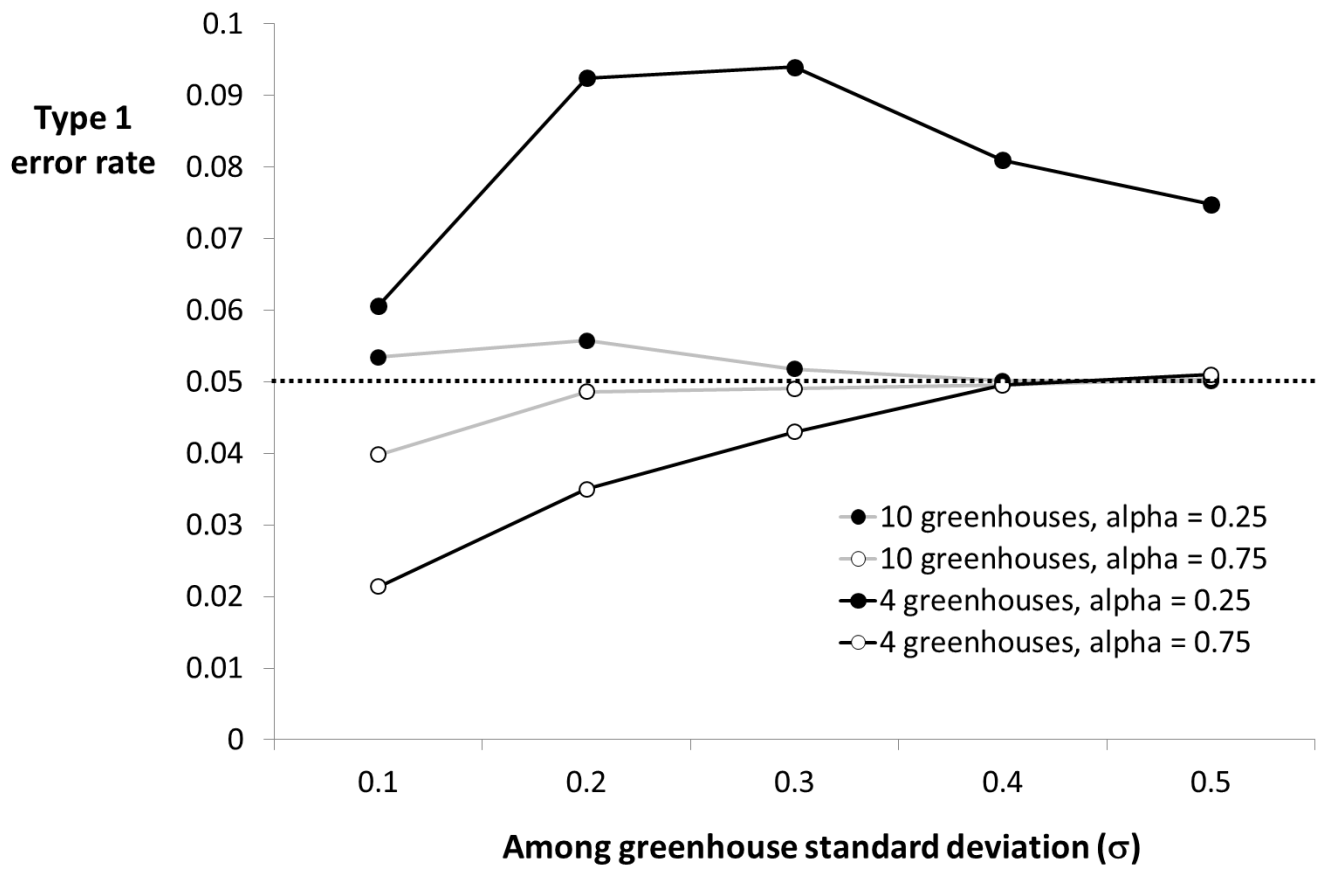
323 of less than 0.05 (i.e. a false positive at alpha = 0.05) is an estimate of the type 1 error rate. The
324 simulations were carried out in R, with the AOV function being used for the analyses.

325

326

327

328 **Figure 1:**



329