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Low temperature formation of copper rich silicides

Erzsébet Dodony^{a, b, *}, György Z. Radnóczy^a, István Dódonyc^c

^a Hungarian Academy of Sciences, Center for Energy Research, Institute of Technical Physics and Material Sciences, Thin Film Physics Laboratory, H-1121, Budapest, Konkoly-Thege M. út 29-33, Hungary

^b Department of Material Physics, Eötvös Loránd University, Pázmány Péter Sétány 1/A, Budapest, H-1117, Hungary

^c Department of Mineralogy, Eötvös Loránd University, Pázmány Péter Sétány 1/C, Budapest, H-1117, Hungary

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ABSTRACT

The reactions of copper and amorphous silicon were studied by in-situ transmission electron microscopy up to 500 °C. Only the $\text{Cu}_7\text{Si}_{24}$ - η phase and the $\text{Cu}_{82}\text{Si}_{18}$ - δ phase formed at this temperature. The crystal structure of the dominating $\text{Cu}_7\text{Si}_{24}$ changed, by the elapsed time after heating. The Cu–Si ordering resulted in different supercells, built up by topologically identical subcells with different site occupancies and arrangement. Two modulated crystal structures were solved based on diffraction data and HRTEM images.

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1. Introduction

Copper silicides are being intensively studied, because of their wide range of applications in many fields. Cu_3Si (also denoted by $\text{Cu}_7\text{Si}_{24}$, Cu_{3+x}Si , $\text{Cu}_3\text{Si}_{1-x}$) is a key ingredient in ultrapure silicon synthesis (99.99999%) suitable for photovoltaic and electric devices [1]. It is used as contact material in microelectronics and as catalyst in production of semiconductor and carbon nanowires. The thrift of the solar cell production depends on refining metallurgical grade silicon to solar grade silicon [2] and on the lowering of the crystallization temperature of amorphous-Si (*a*-Si) to crystalline-Si (*c*-Si) in thin layers. The copper rich silicide phases have a great impact on several technical applications, e.g. in Li-ion batteries [3]. In spite of the impact of copper-silicides, their phases and structural relations are still not detailed properly.

In the focus of experimental works and thermodynamic calculations is the phase diagram of the copper-silicon system. The most cited phase diagram of the system is the 1986 work of Olesinski and Abbaschian [4]. Cui and Jung [5] gave a comprehensive overview in the field of the Cu–Si system; one can find the relevant literature therein. The phases at the copper rich side of the phase diagram is

the object of our study and it is shown in Fig. 1 (after Cui and Jung [5]). There are many differences between the widely cited phase diagram of Olesinski and Abbaschian and the recent results [5], showing us an uncertainty of the Cu – Si phase diagram. A good example for this uncertainty is the work of P. Riani et al. [6] who studied the stability of the $\text{Cu}_{79}\text{Si}_{21-\epsilon}$ phase.

Many studies have been published on the crystal structures of the copper silicide phases since 1935. Fagerberg and Westgren [7] studied alloys with the structure of β -Mn and found $\text{Cu}_{82}\text{Si}_{18}$ structure to be this type. The first structure model for the $\text{Cu}_3\text{Si}_{1-x}$, so called η -phase ($\text{Cu}_7\text{Si}_{24}$ in Fig. 1) was given in 1978 by Solberg [8], who proposed a structure model for the high temperature η -phase with trigonal symmetry. Additionally, he obtained superstructures – denoted as η' and η'' – stable at room temperature. This was in use until Mattern et al. [9 and 10] determined the structure model of η -phase shown in Fig. 2. Later, Wen and Spaepen [11] interpreted their findings on the copper containing precipitates in silicon crystals the same way as Mattern et al.

They proposed rhombohedral symmetries for η' and η'' polymorphs as result of long period antiphase boundaries. Corrêa et al. [12] measured the Cu_{3+x}Si polymorphs by X-ray powder diffraction using copper radiation and established six modifications in this narrow compositional range, although they found all modifications having the similar unit cell. Palatinus et al. [13] using their SUPERFLIP software [14] implemented in JANA2006 [15] interpreted their data on η phases having incommensurate structure.

* Corresponding author. Hungarian Academy of Sciences, Center for Energy Research, Institute of Technical Physics and Material Sciences, Thin Film Physics Laboratory, H-1121, Budapest, Konkoly-Thege M. út 29-33, Hungary.

E-mail address: erzsebet.dodony@energia.mta.hu (E. Dodony).

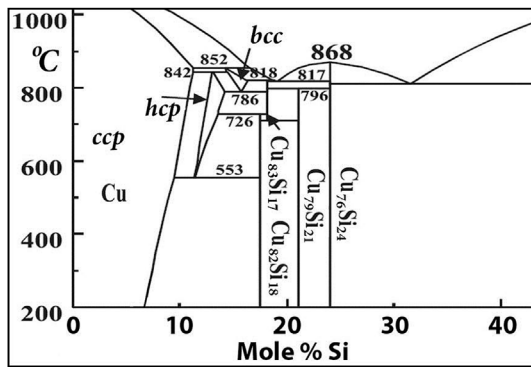


Fig. 1. Phase diagram of the Cu – Si system (after [5]).

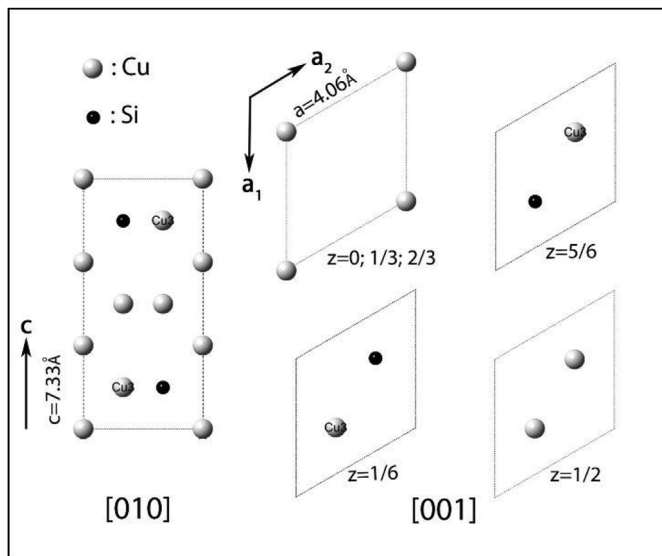


Fig. 2. Structure model of $\text{Cu}_{3+x}\text{Si}-\eta$ in [010] projection and cross sections along z direction in [001] projection as described by Mattern et al. and Wen and Spaepen [9,10 and 11].

However, these long period and incommensurate structures were not confirmed as separate thermodynamic phases [4]. The Cu–Si phases in the ICSD2017 data base [16] are listed in Table 1.

We performed in-situ transmission electron microscopic (TEM) experiments on phase formations of Cu – Si upon heating. We measured the cooled down samples after the heat treatment at room temperature using TEM. Selected area electron-diffraction patterns (SAED) served as basis of phase identifications, whereas high resolution images revealed the Cu/Si ordering. The experimental diffraction patterns and high resolution images, confirmed the atomic positions of $\text{Cu}_{76}\text{Si}_{24}$ [11] basic structure of Mattern et al.

Table 1
The known crystal structures in the Cu – Si system.

Composition	Sign in Fig. 1	Reference	ICSD#.	Prefix
$\text{Cu}_{15}\text{Si}_4$	$\text{Cu}_{79}\text{Si}_{21}$	Mukherjee et al. (1969) [26]	629165	ϵ
$\text{Cu}_{3.17}\text{Si}$	$\text{Cu}_{76}\text{Si}_{24}$	Wen and Spaepen (2007) [11] Mattern et al. (2001, 2007) [9,10]	160694	η and η''
$\text{Cu}_{0.83}\text{Si}_{1.7}$	$\text{Cu}_{82}\text{Si}_{18}$	Fagerberg and Westgren (1935) [7]	52285	δ
$\text{Cu}_{0.875}\text{Si}_{1.125}$	hcp	Foley and Raynor (1961) [27]	108407	κ
Cu	bcc	Xie et al. (2011) [28]	183263	β
		Jona and Marcus (2001) [29]	248435	β'

[9,10] and Wen & Spaepen [11], with different site occupancies.

2. Material and methods

2.1. Sample preparation

The applied starting materials were copper TEM grids (SPI, #200) covered by 10 nm thick amorphous silicon ($a\text{-Si}$) film. The silicon films were magnetron sputtered on a turntable under argon atmosphere of 3×10^{-3} mbar (300 W, 672 V, 0.454 A without bias) to NaCl substrate and transferred to the Cu grid through water baths.

A side-entry Philips PW 6599 heating stage attached with a Pt/PtRh thermocouple powered by a Philips PW 6363/00 regulating unit was used in a Philips CM20 microscope. The precision of the temperature measurement of the sample holder in this setup is $\pm 15^\circ\text{C}$ at the location of the thermocouple. The temperature was increased from room temperature to 350°C in 6 min and subsequently by 50°C increment with waiting time in between the steps, to 500°C . At this temperature, solid state reaction began between the contacted $a\text{-Si}$ thin film and Cu grid. The temperature was held at this temperature for 48 min, while the reactions carried on leaving copper-silicide phases behind. The heating was turned off, when the area covered with $a\text{-Si}$ in the inspected grid window seemed almost fully reacted leaving a small area of unreacted $a\text{-Si}$ in the middle and samples were let to cool down to room temperature in vacuum.

2.2. Applied methods

During the heating we followed the progress of copper silicide phase formation based on their appearance in bright field imaging using a Philips CM20 microscope.

The ex-situ observations were carried out in Philips CM20 and JEOL JEM 3010 type transmission electron microscopes (TEMs) equipped with double-tilt sample holders. Images and SAED patterns were recorded on imaging plates (CM20) and with 2x2k 2 bytes CCD camera (JEOL 3010). The symmetry and lattice parameters identify reaction products were measured on their SAED patterns. Sample thickness was deduced from SAED patterns also, using the measurable resolution maxima values after Cowley [17]. The high resolution (HRTEM) images were acquired using the JEOL TEM.

We used selected area electron diffraction (SAED) patterns for phase identification. The high-resolution images helped to determine structural relations between coexisting phases. The strong electron-matter interaction requires to handle multiple scattering in the function of sample thickness for evaluation of experimental SAED and HRTEM data [18]. Knowing optical parameters of the applied microscope (accelerating voltage, spherical aberration and stability) and its experimental settings (defocus value, aperture size, beam divergence) provide a reliable basis for comparison of experimental and simulated data. The beam divergence can be

determined from the size of reflections acquired at the same conditions as the corresponding HRTEM image or by examining the dampening function of the HRTEM images. The parameter was previously determined for the used microscopes. The defocus value could be obtained on the Fourier transform of an HRTEM image from the contrast transfer function's first crossover position [18]. Both the SAED patterns and HRTEM images were compared to their corresponding simulated counterparts calculated by Cerius² 4.0 software (Molecular Simulation Institute, Inc.). CRISP (Calidris, Version 2.1a) and Digital Micrograph 2.30.542.0 software packages served for image processing, simulations and quantification of diffraction data. In CRISP Fourier filtering was done by inverse Fourier transform using phases and amplitudes at the local maxima of the Fourier transform performed on an HRTEM image (lattice averaging [18]).

3. Results and discussion

The initial stage of reaction between the copper grid and *a*-Si is represented by Fig. 3. All of our experimental data are combination of signals from the reaction products between the copper grid and the 10 nm thick *a*-Si layer and the unreacted amorphous silicon layer (*a*-Si) underneath. We know after Re et al. [19] that overlapping an amorphous layer reduces aesthetic quality of both

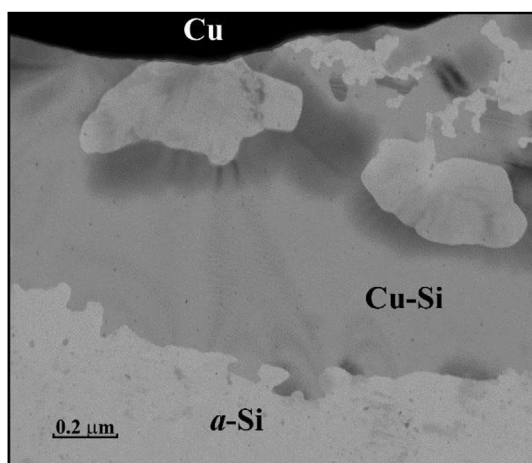


Fig. 3. Image of the reaction products between copper grid bars and amorphous silicon (*a*-Si) in a Philips CM20 microscope film after the 8th minute at 500 °C.

HRTEM images and SAED patterns, however structural data can still be retrieved from these. The thickness measured on SAED patterns (using the formula of Cowley [17]) usually varied in between 60 Å and 80 Å. For instance, if the η -phase is 80 Å thick, then it only consumes an 18 Å thick layer of *a*-Si. The amorphous part blurs significantly the HRTEM images of the tarnishing crystalline phases [19]. The background intensities in the SAED patterns are clouded by the *a*-Si as it is shown below in the upper left corner of Fig. 4a.

3.1. The $\text{Cu}_{82}\text{Si}_{18}$ - δ phase

The beta-manganese analog copper rich silicide (δ) phase [7] is a minor component of the reaction products of *a*-Si and the supporting Cu-grid. Fig. 5 and Fig. 6 demonstrate the defect free crystal structure of $\text{Cu}_{82}\text{Si}_{18}$ by its SAED and HRTEM images. The weak satellite reflections seen near the reflections of the tetragonal net, originate from misoriented grains of the same phase close to the selected area. The $P4_1\bar{3}2$ space group of $\text{Cu}_{82}\text{Si}_{18}$ only allows $h = 4n$ type reflections for $h00$. The $h \neq 4n$ type reflections in the observed SAED patterns and Fourier-transforms of HRTEM images are due to dynamical scattering.

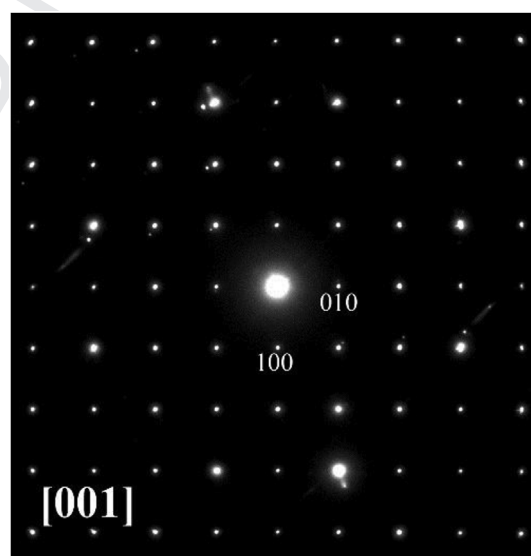


Fig. 5. SAED pattern of a δ -phase crystallite ($\text{Cu}_{82}\text{Si}_{18}$).

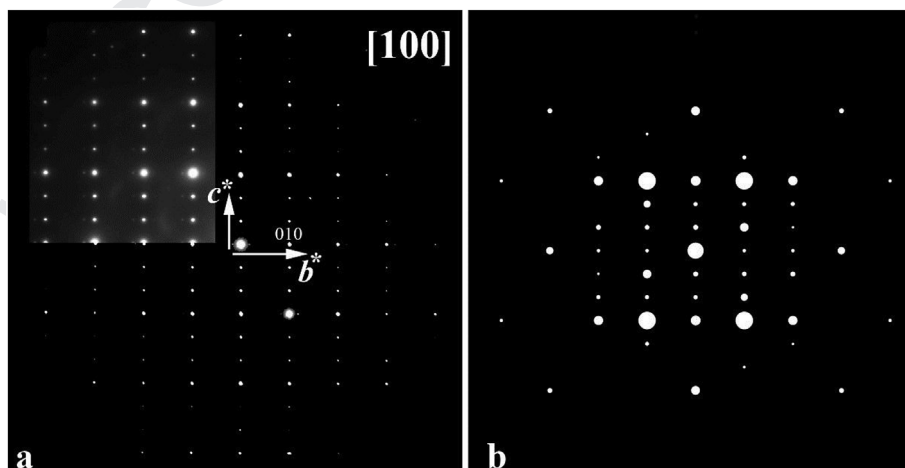


Fig. 4. Experimental (a) and simulated (b) SAED pattern (Wen and Spaepen's data) of $\text{Cu}_{76}\text{Si}_{24}$ - η . Their different intensity distributions are evident.

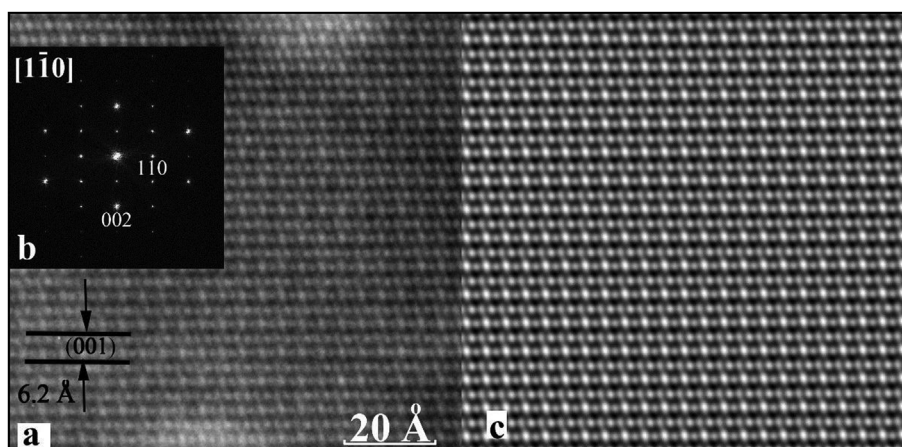


Fig. 6. Raw experimental HRTEM image of $\text{Cu}_{82}\text{Si}_{18}$ crystal (a), its Fourier-transform (b) and the Fourier-filtered experimental image (c).

3.2. The $\text{Cu}_{76}\text{Si}_{24}$ - η phase

The $\text{Cu}_{76}\text{Si}_{24}$ - η phase [9,10 and 11] (Fig. 2.) – also denoted by Cu_3Si , Cu_{3+x}Si , $\text{Cu}_3\text{Si}_{1-x}$ – is the dominant component of the reaction product between Cu grid and α -Si film as revealed by SAED patterns. The observed d_{hkl} values match well with the simulated

ones based on the Wen and Spaepen (2007) data as it is shown in Fig. 4. However, the experimental and simulated intensities deviate from each other. There is lack of the point symmetry relations in the experimental pattern of the η phase [9,10 and 11]; the calculated intensities of the $0kl$ and $0\bar{k}l$ are different. As a consequence, a revised structure model is needed to describe the Cu_3Si phase.

The lamellar texture of an area of $\text{Cu}_{76}\text{Si}_{24}$ in orientation close to $[100]$ is visible in Fig. 7. The HRTEM image on a selected lamella and its Fourier-transform in Figs.6ab is conform to the SAED pattern shown in Fig. 4a. The intense 010 maximum is evident in both figures. The noisy Fourier transform reflects the low contrast in the experimental HRTEM image.

We compared our experimental data to the corresponding simulated data, based on the Wen and Spaepen [10] structure model of the η -phase. The results showed poor match both for the SAED as well as for HRTEM images. The dynamical SAED simulations were performed in the *Cerius²* package (200 kV, sample thickness: 81 Å). Fig. 8 demonstrates a drastic difference in the

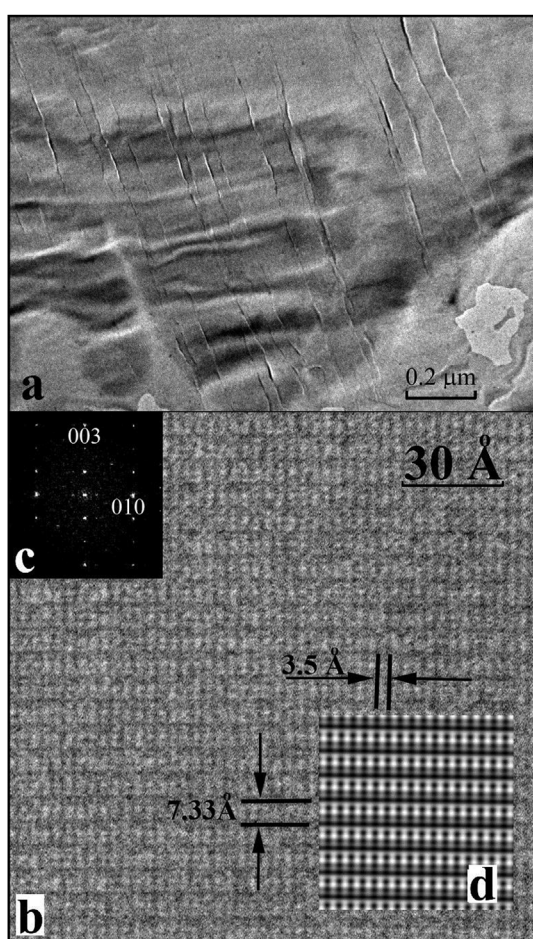


Fig. 7. (a) Bright field TEM image of a lamellar $\text{Cu}_{76}\text{Si}_{24}$ area close to the $[100]$ projection, (b) raw experimental HRTEM image of $\text{Cu}_{76}\text{Si}_{24}$, (c) its Fourier-transform and (d) the Fourier-filtered and symmetry imposed (pm plane group) experimental image.

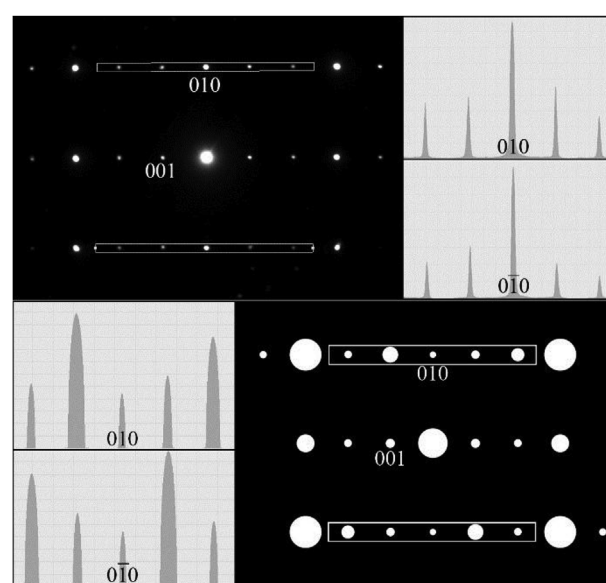


Fig. 8. Diffracted intensity distributions integrated by Digital Micrograph along the stripes for the experimental (in the upper half) and the corresponding calculated one (in the bottom half) using the Wen and Spaepen's data. Differences between the two sets are significant.

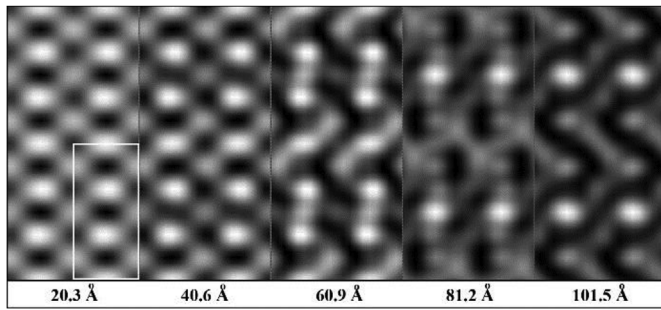


Fig. 9. Wen and Spaepen's data based simulated [100] HRTEM images in the function of the sample thickness. There was no observed HRTEM image showing satisfactory match with any simulated one.

Table 2

Occupancies and atomic coordinates for the modified Cu_3Si structure; space group: $P\bar{3}m1$, a_0 : 4.06 Å, c_0 : 7.33 Å.

#	Occupancy	x	y	z
1	Cu 1.000	0.0000	0.0000	0.0000
2	Cu 0.500	0.6667	0.3333	0.1667
3	Si 1.000	0.3333	0.6667	0.1667
4	Cu 1.000	0.0000	0.0000	0.3333
5	Cu 1.000	0.6667	0.3333	0.5000
6	Cu 1.000	0.3333	0.6667	0.5000
7	Cu 1.000	0.0000	0.0000	0.6667
8	Si 1.000	0.6667	0.3333	0.8333
9	Cu 0.500	0.3333	0.6667	0.8333

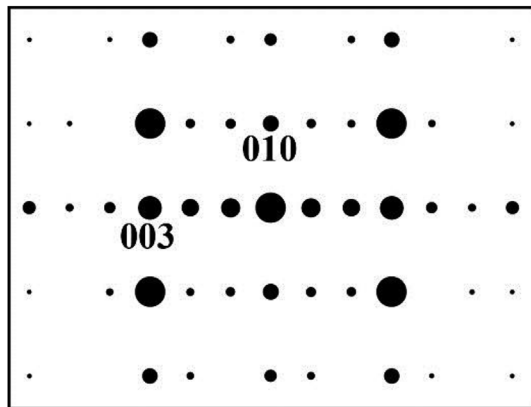


Fig. 10. Calculated [100] projected SAED pattern of the modified Wen and Spaepen's model with matching intensities as in the experimental pattern shown in Fig. 8.

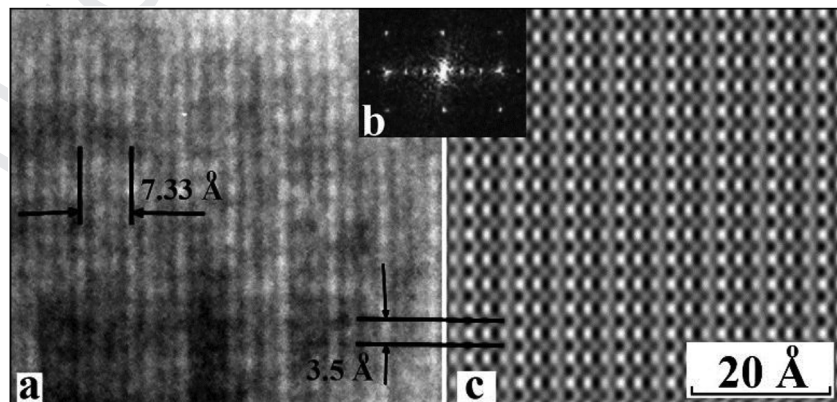


Fig. 11. Raw HRTEM image (a), its Fourier-transform (b) and PCD map (c) generated from (a) using electron crystallographic methods implemented in CRISP package.

intensity distributions of [100] projected crystal. The differences in intensity ratios are far above the tolerance that could be explained by sample thickness or misorientation, which was checked in Cerius² 4.0 software package.

HRTEM many-beam multi-slice calculations (300 kV; c_s : 0.6 mm; defocus spread 40 Å; extended Schertzer defocus Δf : -400 Å) were carried out as a function of sample thickness on the [100] projected Wen and Spaepen [10] structure model. The applied defocus value was measured as described in section 2.2 (practically, there was no astigmatism). The result is shown in Fig. 9. Surprisingly there is no experimental HRTEM image showing similar contrast to any of the simulated image, especially close to the real sample thickness. (The sample thickness was measured on SAED patterns, by applying the $t = 2d_{\text{res}}^2/\lambda$ formula [17,18].) Due to the poor match of the experimental and simulated data some serious doubts have arisen about the validity of the structure model used hitherto.

To resolve the problem, we built several structure models for unmodulated and stoichiometric $\eta\text{-Cu}_3\text{Si}$, varying site occupancies in the original [9,10 and 11] model (Fig. 2). Changes in values of the site occupation factors of the two Cu_3 (at 1/3, 2/3, 1/6 and 2/3, 1/3, 5/6 coordinates) to 0.5 and the rest to 1, result in a structural model (Table 2) satisfying appropriate matches to the experimental SAED pattern and HRTEM images. Electron crystallography software – CRISP [18] – served as a good tool to recover projected charge density (PCD) using HRTEM image and diffracted intensities in the corresponding SAED pattern. Fig. 10 shows a simulated [100] projected SAED pattern for 81 Å sample thickness using the new, modified Wen and Spaepen basic structure for Cu_3Si . Comparing to the experimental SAED pattern in Fig. 8a the fit is satisfactory. A PCD map (Fig. 11c) was generated from the raw experimental HRTEM image in Fig. 11a using electron crystallographic methods implemented in CRISP. We validated our modified Wen and Spaepen [10] structural model by comparing the simulated PCD map to the one recovered from the experimental data is shown in Fig. 11c; the result is presented in Fig. 12. The PCD map at 1.82 Å resolution (Fig. 12b) and the image – based on the experimental HRTEM image – in Figs. 11 and 12c fits well. Cu_3 and Si positions are marked by circle and square respectively in the insert in Fig. 12a.

Most of the $\text{Cu}_{76}\text{Si}_{24}$ grains have modulated structures in directions along and perpendicular to the [001] direction. An HRTEM image and its FFT in Fig. 13 show a doubled periodicity (14.66 Å) along the c axis. Fig. 14 shows the modulation along the a^* , the periodicity is four times of the basic $d_{010} \approx 3.5$ Å.

In previous works, it was stated that the modifications (so called η' , η'' , ... polymorphs) differ from each other not only by periodicities along the main crystallographic directions, but also in their

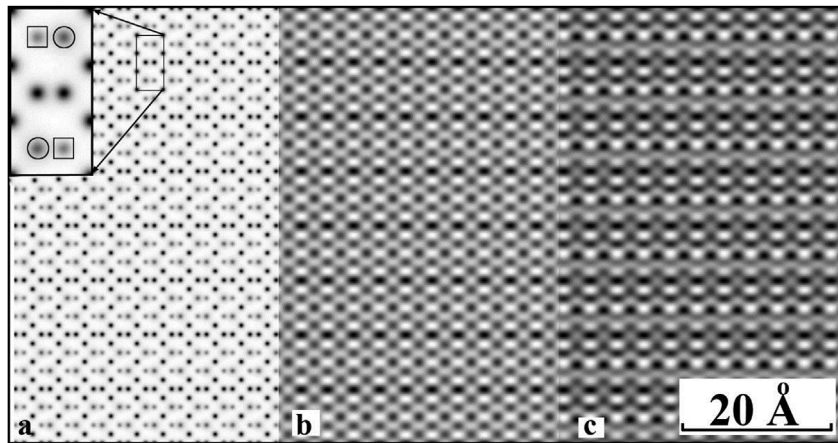


Fig. 12. PCD maps calculated for the modified Wen and Spaepen's model at 0.3 Å (a) and 1.81 Å resolution (b). The image in (c) is the same as in Fig. 11c showing appropriate match to image in (b). The insert in (a) indicates the unit cell where circles are at Cu positions with half occupation and squares are at Si sites.

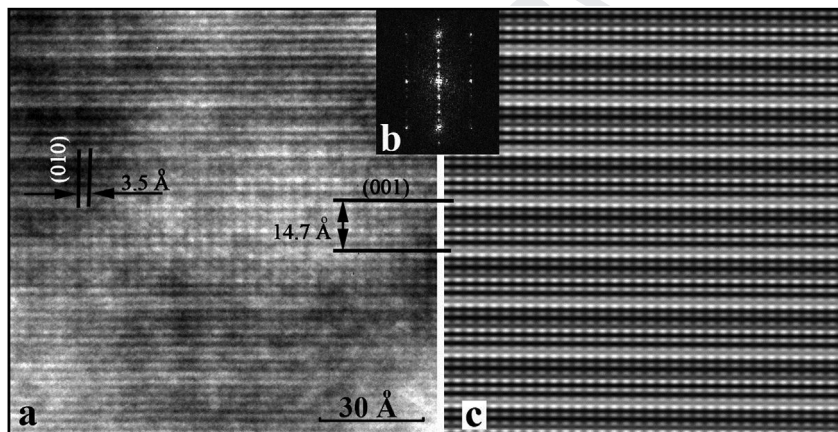


Fig. 13. Raw [100] projected experimental HRTEM image of modulated $\text{Cu}_{76}\text{Si}_{24}$ with doubled (14.7 Å) periodicity along the [001] (a), its Fourier-transform (b) and the projected charge density map (c) retrieved by the CRISP package (Calidris, Version 2.1a), using the experimental HRTEM image and amplitudes from the corresponding SAED patterns.

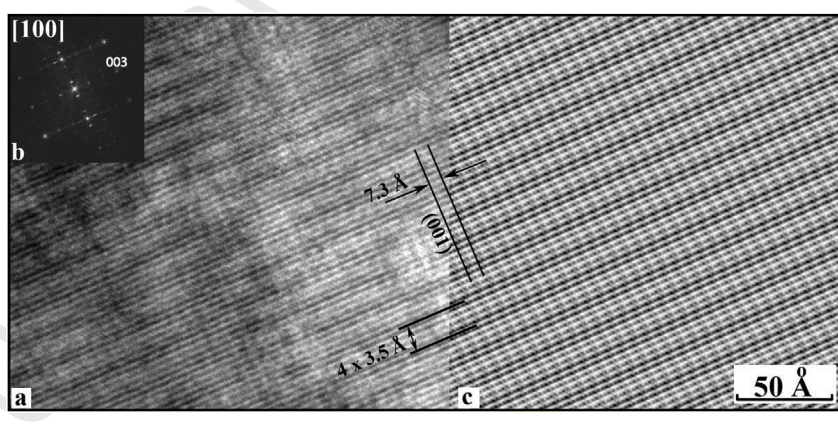


Fig. 14. Raw [100] projected experimental HRTEM image of modulated $\text{Cu}_{76}\text{Si}_{24}$ with four times of the (100) periodicity (= 14.0 Å) of the basic structure (a), its Fourier-transform (b) and the Fourier-filtered experimental image (c).

composition. The value of x is slightly increasing in the Cu_{3+x}Si formula in the η , η' , η'' order [20]. Samson and coworkers [21] observed silicon precipitations from the heat treated homogenous “ η ” phase with $\text{Cu}_{0.738}\text{Si}_{0.262}$ composition. They found the first transformation and silicon precipitation on heating, just below 500 °C, and interpreted as the $\eta \rightarrow \eta'$ reaction. In addition, repeated

diffraction patterns (after two days) on the same samples showed different peak positions and intensity values, which means that the structural state changes in time.

In our experiment after the in-situ heating, the sample texture, and the real structure of crystals changed with the elapsed time (within a week). Fig. 15 gives a comparison of the freshly formed

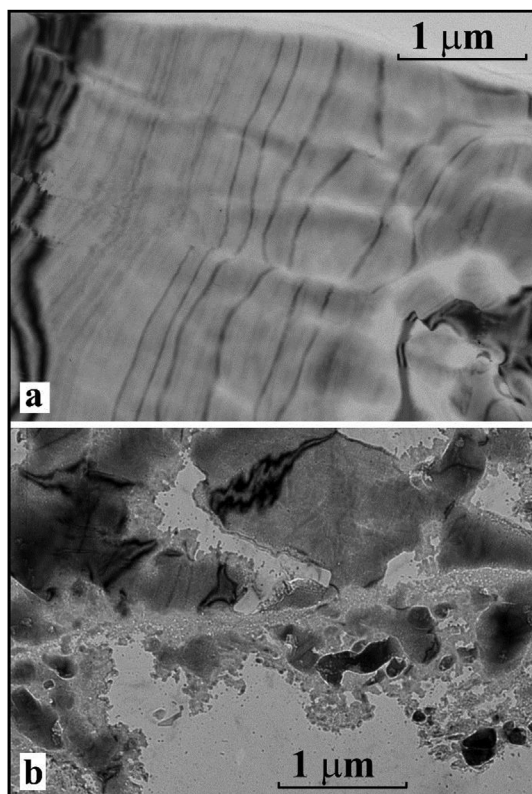


Fig. 15. Two typical bright field TEM images from the same sample. The image in (b) captured one week after (a).

Table 3
Occupancies and atomic coordinates for the 2xc modulated Cu_3Si .

#	Occupancy	x	y	z
1	Cu 1.000	0.0000	0.0000	0.0000
2	Cu 0.500 Si 0.500	0.6667	0.3333	0.0833
3	Cu 0.500 Si 0.500	0.3333	0.6667	0.0833
4	Cu 1.000	0.0000	0.0000	0.1667
5	Cu 0.500 Si 0.500	0.3333	0.6667	0.2500
6	Cu 0.500 Si 0.500	0.6667	0.3333	0.2500
7	Cu 1.000	0.0000	0.0000	0.3333
8	Cu 0.500 Si 0.250	0.3333	0.6667	0.4167
9	Cu 0.500 Si 0.250	0.6667	0.3333	0.4167
10	Cu 1.000	0.0000	0.0000	0.5000
11	Cu 0.500 Si 0.500	0.3333	0.6667	0.5833
12	Cu 0.500 Si 0.500	0.6667	0.3333	0.5833
13	Cu 1.000	0.0000	0.0000	0.6667
14	Cu 0.500 Si 0.250	0.3333	0.6667	0.7500
15	Cu 0.500 Si 0.250	0.6667	0.3333	0.7500
16	Cu 1.000	0.0000	0.0000	0.8333
17	Cu 0.500	0.3333	0.6667	0.9167
18	Cu 0.500	0.6667	0.3333	0.9167

texture and one week older. These rough changes may be caused by the extreme mobility of copper atoms in silicon. In crystalline silicon copper is by an order of magnitude the fastest element [2] with the diffusivity around $2.8 \times 10^{-7} \text{ cm}^2 \text{ s}^{-1}$ at room temperature. The high mobility of copper in silicon [22] led to modulated $\text{Cu}_{76}\text{Si}_{24}$ structures. The two superstructures which are detailed in Tables 3 and 4 are products of these time dependent changes. The volume ratio of modulated structures increases with the elapsed time at room temperature. Our results are in accordance with previous observations [21].

We were able to solve the modulated $\eta\text{-Cu}_3\text{Si}$ superstructure

Table 4
Occupancies and atomic coordinates for the 4xa modulated Cu_3Si .

#	Occupancy	x	y	z
1	Cu 1.000	0.0000	0.0000	0.0000
2	Cu 1.000	0.5000	0.0000	0.0000
3	Cu 1.000	0.2500	0.0000	0.0000
4	Cu 1.000	0.7500	0.0000	0.0000
5	Cu 0.500 Si 0.375	0.0833	0.6667	0.1667
6	Cu 0.500 Si 0.375	0.4167	0.3333	0.1667
7	Cu 0.500 Si 0.375	0.1667	0.3333	0.1667
8	Cu 0.500 Si 0.375	0.3333	0.6667	0.1667
9	Cu 0.500	0.5833	0.6667	0.1667
10	Cu 0.500	0.6667	0.3333	0.1667
11	Cu 0.500	0.9167	0.3333	0.1667
12	Cu 1.000	0.0000	0.0000	0.3333
13	Cu 1.000	0.2500	0.0000	0.3333
14	Cu 1.000	0.5000	0.0000	0.3333
15	Cu 1.000	0.7500	0.0000	0.3333
16	Cu 0.500 Si 0.500	0.0833	0.6667	0.5000
17	Cu 0.500 Si 0.500	0.4167	0.3333	0.5000
18	Cu 0.500 Si 0.500	0.1667	0.3333	0.5000
19	Cu 0.500 Si 0.500	0.3333	0.6667	0.5000
20	Si 0.500 Cu 0.250	0.8333	0.6667	0.5000
21	Si 0.500 Cu 0.250	0.9167	0.3333	0.5000
22	Si 0.500 Cu 0.250	0.5833	0.6667	0.5000
23	Si 0.500 Cu 0.250	0.6667	0.3333	0.5000
24	Cu 1.000	0.0000	0.0000	0.6667
25	Cu 1.000	0.7500	0.0000	0.6667
26	Cu 1.000	0.5000	0.0000	0.6667
27	Cu 0.500	0.1667	0.8333	0.6667
28	Cu 1.000	0.2500	0.0000	0.6667
29	Cu 0.750 Si 0.250	0.0833	0.6667	0.8333
30	Cu 0.750 Si 0.250	0.1667	0.3333	0.8333
31	Cu 0.750 Si 0.250	0.3333	0.6667	0.8333
32	Cu 0.750 Si 0.250	0.4167	0.3333	0.8333
33	Cu 0.500 Si 0.375	0.5833	0.6667	0.8333
34	Cu 0.500 Si 0.375	0.6667	0.3333	0.8333
35	Cu 0.500 Si 0.375	0.8333	0.6667	0.8333
36	Cu 0.500 Si 0.375	0.9167	0.3333	0.8333

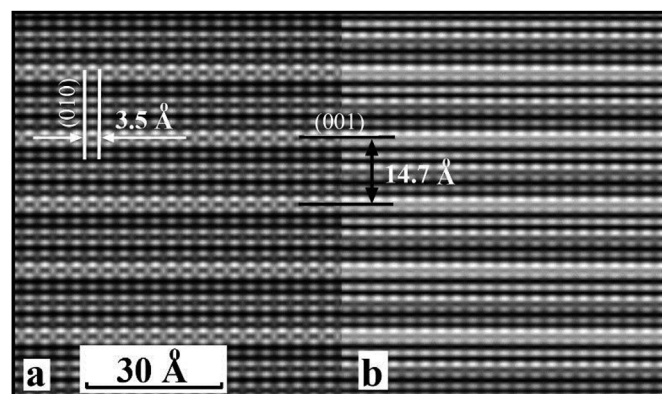


Fig. 16. Simulated HRTEM image (a) using experimental parameters, and structural data listed in Table 3 gives a good match with the filtered experimental HRTEM image (b).

varieties by tuning site occupancies at positions inside supercells built up by multiple unit cells. We measured modulations both along the **c** and **a** axes, respectively. The simulated HRTEM image in Fig. 16a using the experimental parameters (300 kV, 0.6 mm c_s , 0.3 mrad divergence, 2.08 Å resolution, 81 Å sample thickness and -300 Å defocus value) and the ordering values listed in Table 2 for doubled **c** modulation gave an excellent match with the filtered experimental HRTEM image in Fig. 16b (also in Fig. 13c). The period length of modulation along the **a** axis is typically $4x d_{(100)}$ (14 Å). We found satisfactory matches in between the Fourier-filtered

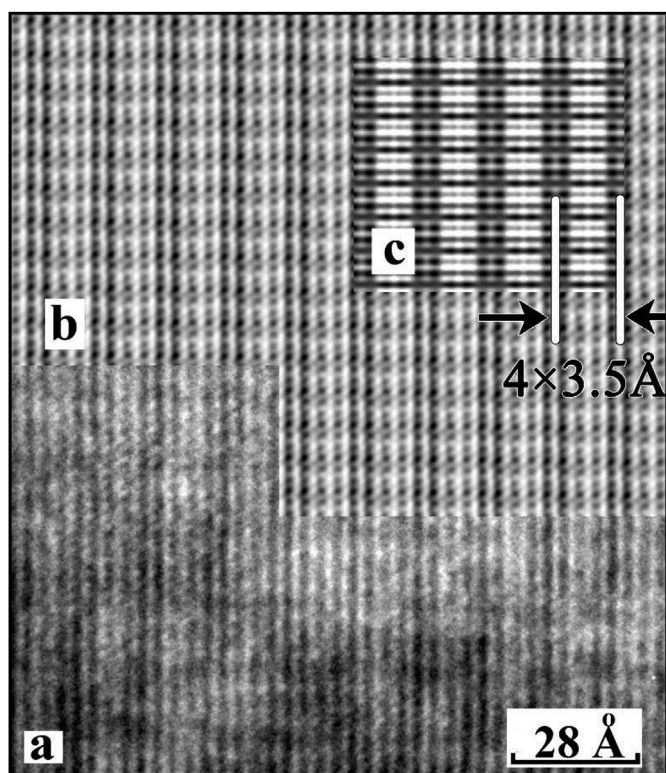


Fig. 17. Raw HRTEM image (a) and Fourier-filtered experimental HRTEM image (b) gives a good match with the simulated HRTEM image (c) using experimental parameters and structural data listed in Table 4.

experimental HRTEM (in Fig.17b) and a simulated (300 kV, 0.6 mm c_s , 0.6 mrad divergence, 2.08 Å resolution, 81 Å sample thickness and -400 Å (extended-Scherzer) defocus value) image, based on the atomic coordinates and site occupancies listed in Table 4.

4. Conclusion

We heat treated copper grids contacted with 10 nm thick amorphous Si layer at 500 °C and determined the phases and structures formed using transmission electron microscopy and electron crystallography. A new structural model was constructed for $\text{Cu}_3\text{Si} - \eta$ phase ($\text{Cu}_{76}\text{Si}_{24}$) in order to get a fit with the experimental HRTEM images and SAED patterns. The time dependent appearance of modulated superstructures was attributed to the extreme mobility of Cu atoms in Si. Two modulated Cu_3Si structures were solved by tuning the site occupancies in the supercell, to give satisfactory matches between the models and the experimental data.

In contrast to the majority of published papers on the phase relations [4–6,21–25], our experiment on copper-silicides was produced by heating copper and amorphous silicon, in high vacuum. It seems to be evident that no $\text{Cu}_{79}\text{Si}_{21}$ (ϵ) phase [26] formed up to 500 °C. Combined with the knowledge of the previously mentioned works like Riani et al.'s [6], this prompts the question whether a new comprehensive study of the Cu – Si phase diagram is needed.

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