# Development of a Modular Reconfigurable Machine for Reconfigurable Manufacturing Systems 

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## Abstract

The Reconfigurable Manufacturing Systems (RMSs) paradigm has been formulated to encapsulate methodologies that enable manufacturing systems to effectively cope with changes in markets and products. RMSs are systems which are envisioned to be capable of a rapid change in manufacturing layouts, process configurations, machines and control components to provide a quick response to changes in the master production schedule. This research was initiated due to the necessity for new forms of production machinery to be design for RMSs, which can aid manufacturers in the adjustment of system capacity and functionality at lower costs.

This thesis presents the development of Modular Reconfigurable Machines (MRMs), as a novel machining solution within the scope of RMSs. MRMs are characterized by modular mechanical structures that enable the flexibility of the machine to be adjusted in response to changes in products. The concept of adjustable flexibility implies that the flexibility of the machines may be balanced to exactly match the requirements of the system when changes in production plans occur. Product changes are managed by a variation of machining processes and Degrees of Freedom (DOF) on a platform. The modular nature of these machines permits this to be done easily and cost effectively. MRMs therefore possess an advantage over traditional machining systems, where an adjustment of system functionality would require the procurement of new machinery. Manufacturers will also have the option to purchase machines with flexibility that may be increased as needed, instead of investing in highly flexible and expensive CNC systems, with features that are often excessive and unused.

Main points of this research included the development of mechanical modules for assembly into complete machines. The number and types modules used in an assembly could be changed to provide the kinematic and process optimization of the mechanical hardware according to production requirements. In conjunction to the mechanical development, a suitable Mechatronic control system will be presented. The focus of control development was the facilitation of seamless system integration between modular mechanical hardware and the controller at both hardware and software levels. The control system is modular and distributed and characterised by a "plug-in" approach to control scalability. This is complimented by a software architecture that has been developed with a focus on hardware abstraction for the management of a reconfigurable mechanical and electronic architecture.

A static and dynamic analysis of the MRM system is performed for a selected mechanical configuration. The performance of the mechanical and control system is also evaluated for static and dynamic positioning accuracy for different modes of motion control. The implications for MRMs are then analysed, which include system functionality and capacity scaling, manufacturing expansion flexibility and system life spans. The research was concluded with an analysis of the challenges and problems that must be addressed before MRMs become industrially acceptable machines.

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## List of Acronyms and Abbreviations

| AC | Alternating Current |
| :---: | :---: |
| Acc | Accuracy, Acceleration |
| ADC | Analogue to Digital Converter |
| API | Application Programming Interface |
| ASCII | American Standard Code for Information Interchange |
| BLU | Basic Length Unit |
| CAD | Computer Aided Design |
| CAM | Computer Aided Manufacturing |
| CAN | Controller Area Network |
| CAPP | Computer Aided Part Programming (Also Computer Aided Process Planning) |
| COTS | Commercial Off-The-Shelf |
| CNC | Computer Numerically Controlled |
| CR | Control Resolution |
| DC | Direct Current |
| Dec | Deceleration |
| DMS | Dedicated Manufacturing System |
| DMT | Dedicated Machine Tool |
| DOF | Degrees of Freedom |
| DSP | Digital Signal Processor |
| EDM | Electric Discharge Machining |
| FIFO | First-In-First-Out |
| FMS | Flexible Manufacturing System |
| HTM | Homogenous Transformation Matrix |
| I2C | Inter Integrated Circuit (Read as: „"* squared „C') |
| ICR | Input Capture Register |
| IDE | Integrated Development Environment |
| I/O | Input/ Output |
| ITM | Improved Tustin Method |
| MIPS | Million Instructions Per Second |
| MRM | Modular Reconfigurable Machine |
| NC | Numerical Control |
| NCK | Numerical Control Kernel |
| NURBS | Non-Uniform Rotational Basis Spline |
| OAC | Open Architecture Control |

## List of Acronyms and Abbreviations

| OCR | Output Compare Register |
| :--- | :--- |
| OS | Operating System |
| PC | Personal Computer |
| PID | Proportional-Integral-Derivative |
| PREMADE | PRogram for REconfigurable MAchine DEsign |
| PROFIBUS | PRocess Feld BUS |
| PWM | Pulse Width Modulation |
| Ref | Reference |
| Rep | Repeatability |
| RMS | Reconfigurable Manufacturing System |
| RMT | Reconfigurable Machine Tool |
| SERCOS | SErial Real-time COmmunication System |
| SMMEs | SMall and Medium Enterprises |
| TCP/IP | Transmission Control Protocol/ Internet Protocol |
| TIPO | Time for InterPOlation (Interpolation Cycle Time) |
| TWI | Two Wire Interface |
| USART | Universal Synchronous and Asynchronous serial Receiver and Transmitter |
| USB | Universal Serial Bus |

## Nomenclature

| A | area, approach allowance |
| :---: | :---: |
| $A_{c}$ | clamped area |
| $A_{t}$ | tensile stress area |
| $a_{x}$ | acceleration |
| $b$ | mechanical damping coefficient |
| $C_{p}$ | cutting coefficient |
| c | damping coefficient |
| $D_{o}$ | original diameter, outer diameter |
| $d$ | diameter, nominal diameter of a bolt, depth of cut |
| $d_{c}$ | diameter of collar or bearing |
| $d_{m}$ | mean/nominal diameter of a power screw |
| E | modulus of elasticity, position error |
| $E_{C}$ | concatenation error |
| $E_{m}$ | mechanical position error |
| $E_{O}$ | edge offset error |
| $E_{p}$ | position control error, tracking error |
| $E_{i+1 \leftarrow i}$ | error matrix |
| EH | chord height error |
| ER | radial error |
| $e$ | error |
| $F$ | force |
| $F_{e}$ | external bolt force |
| $F_{c}$ | normal clamping force between interfaces |
| $F_{i}$ | initial bolt tension |
| $F_{o}$ | magnitude of a harmonic force |
| $f$ | coefficient of friction, frequency |
| $f_{c}$ | collar coefficient of friction |
| $f_{r}$ | linear feed rate |
| ${ }^{i+1} f_{i+1}$ | link-wise force |
| $g$ | gravity, grip length |
| I | moment of inertia |
| $J$ | moment of inertia of a rotating shaft |
| K | cutting coefficient, electromotive constant |
| $K_{d}$ | derivative gain |
| $K_{i}$ | integrator gain |
| $K_{p}$ | proportional gain |
| $K_{p p}$ | proportional position control gain |
| $K_{t}$ | cutting coefficient |
| $k$ | stiffness, interpolation number |
| $k_{b}$, | bolt stiffness |
| $k_{c}$ | interface stiffness |
| $k_{i}$ | bolt tightening constant |
| $L$ | length, thread lead, motor inductance |
| $\Delta L$ | increment in length |
| M | magnitude of acceleration |
| $M_{M}$ | maximum position |
| $M_{m}$ | minimum position |
| $M_{n}$ | module homogenous transformation matrix |
| $M_{t}$ | drill turning moment |
| ${ }^{i+1}{ }_{i} M_{n}$ | module homogenous transformation matrix |
| $m$ | mass, cutting coefficient |
| $N$ | rotational speed, number of configurations, number of iterations, reduction ratio |

## Nomenclature

| $n$ | number of enhancement modules, number of measurements |
| :---: | :---: |
| ${ }^{i+1} n_{i+1}$ | link-wise torque |
| $P$ | thread pitch, load |
| $P_{A}$ | angular pitch of a screw |
| $P_{T}$ | translational pitch of a screw |
| ${ }^{i+1}{ }_{i} P$ | position matrix |
| $p$ | number of encoder pulses |
| $R$ | radius, electrical resistance |
| Ref | reference value |
| $\operatorname{Res}_{x}$ | residual length |
| $R_{M R}$ | material removal rate |
| ${ }^{i+1}{ }_{i} R$ | rotation matrix |
| $r$ | number of enhancement modules selected at a time, frequency ratio |
| $S$ | tool feed per revolution, sum of axial increments |
| $\stackrel{\rightharpoonup}{\text { \$ }}$ | a screw |
| $\stackrel{\rightharpoonup}{S}$ | unit vector |
| $S_{p}$ | proof strength |
| $S_{\text {shear }}$ | shear strength |
| $s$ | standard deviation |
| $T$ | time constant, iteration time |
| $T_{m}$ | machining time |
| $T_{\text {step }}$ | step time |
| work ${ }_{\text {tool }}$ T | machine homogenous transformation matrix |
| $t$ | time, thread height, thickness |
| $u$ | output of position controller |
| $V$ | linear speed |
| $V_{\text {nom }}$ | nominal voltage |
| $V_{\text {ref }}$ | reference voltage |
| W | load on power screw |
| $\dot{W}$ | power |
| X | amplitude of harmonic response |
| $\Delta X$ | axial increment on X-axis |
| $\Delta X_{o}$ | axial increment on axis after Acc/Dec control |
| $x$ | distance on X -axis, cutting coefficient |
| $x_{e}$ | end position |
| $x_{s}$ | start position |
| $\bar{x}$ | mean/ average value |
| $\Delta Y$ | axial increment on Y-axis |
| $y$ | distance on Y-axis, cutting coefficient |
| ${ }^{i} \hat{Z}_{i}$ | joint axis unit vector |
| $z$ | distance on Z -axis |
| $\alpha$ | X-Y-Z Euler Angle, angular increment for ITM interpolator |
| $\alpha_{n}$ | thread angle |
| $\beta$ | X-Y-Z Euler Angle |
| $\gamma$ | X-Y-Z Euler Angle |
| $\delta$ | deflection |
| $\varepsilon$ | skewness error |
| $\theta$ | drill point angle, angular position |
| $\delta$ | damping factor |
| $\tau_{i}$ | actuation force or torque |

## Nomenclature

| $\varphi$ | phase angle |
| :--- | :--- |
| $\omega$ | angular frequency |
| $\omega_{d}$ | damped frequency |
| $\omega_{n}$ | natural frequency |

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## 1. Introduction

### 1.1 Manufacturing Challenges

The rationale for this research originates in the need to address manufacturing challenges that have emerged as a result of global economic competition in recent years. The ability of a manufacturer to monopolise a market is dependant on product innovation and the ability to respond rapidly and efficiently to market demands. Computer Aided Design (CAD) packages are an indispensable tool for product innovation. The advancements in CAD packages have considerably reduced product development times in the past decade [1]. The heightened rate of product development has resulted in products being introduced into markets in shorter periods of time. A consequence of this trend is the shortening production life of consumer goods. The challenge arising from a frequently changing product portfolio is the cost effective initialisation of new manufacturing configurations.

Frequent changes in market characteristics are induced by advancements in technology and erratic consumer trends. The necessity to favourably influence consumer behaviour has forced manufacturers to seek and exploit niches in global markets. The concept of product design by the customer has emerged as an inevitable consequence of increasing consumer awareness [2]. The manufacturing of products to customer specifications possesses the ability to fragment global markets and create niches for further exploitation. The challenge arising in product customisation is the need for increased process variation, dynamic production scheduling and the fabrication of these items at mass production rates.

The challenges arising from global economic competition may be translated into requirements for the design of future manufacturing systems. Lang et al [3] have identified four requirements for a manufacturing enterprise to effectively achieve the objectives of profitability and increased market share in a competitive environment. In brief, these requirements are:
(i) Short manufacturing lead time: Short lead time requires the quick initialization of manufacturing systems. Early product introduction increases the likelihood for obtaining and retaining a larger market share.
(ii) Increased product variety and product customization: Increased product variety and product customization increases the appeal of goods to consumers with varied preferences.
(iii) Mass production rates for low product volumes: The fragmentation of markets by product customization results in the demand for specific variants in small quantities. Improved production rates increase the likelihood of monopolizing resultant niche markets that may be shared by global competitors.
(iv) High quality products at lower prices: Globalization has resulted in a multiplicity of manufacturers offering consumers similar, high quality goods. The negative effects of market saturation may be avoided by an enterprise that is capable of producing personalized products at competitive prices.

The cost effective initialization of manufacturing systems that meet the outlined requirements has required the reengineering of manufacturing paradigms. Dedicated Manufacturing Systems (DMSs) and Flexible Manufacturing Systems (FMSs) have been identified as incapable of meeting the challenges of modern manufacturing [1].

The inadequacy in these systems has been primarily attributed to the structure of these systems and the types of production machinery employed in each. The reconfigurable manufacturing paradigm has been proposed by Koren et al [1], to encapsulate new methodologies for the design of manufacturing systems and equipment that will provide solutions to the challenges arising. Systems that will be developed according to this paradigm are called Reconfigurable Manufacturing Systems (RMSs).

RMSs are systems that are intended to provide a rapid response to dynamic changes in production requirements, through the reconfiguration of hardware and software resources. Mehrabi et al [4] have endeavoured to identify enabling technologies that must be developed for RMSs. These technologies include open architecture software systems, reconfigurable production equipment, scalable control systems and simulation and sensor systems for fault diagnosis. This research focused on the development of suitable production equipment for reconfigurable manufacturing environments.

### 1.2 Motivation for the Study

The conceptualization of the reconfigurable manufacturing paradigm has prompted the reengineering of production machinery. The inadequacies of DMSs and FMSs in meeting the demands of modern manufacturing have been traced, in part, to the production machines employed in each system. DMSs and FMSs employ machines that possess fixed mechanical architectures and exhibit closed proprietary control systems that are generally expensive or impossible to upgrade. RMSs require production machines with extensible and customizable mechanical hardware. The extensibility of a machines mechanical hardware is necessary to allow an expansion of the production envelope trough the process of reconfiguration. The customization of the mechanical hardware further implies that the machine, although flexible, will not possess excessive functionality. The notion of customized flexibility is essential in reducing the capital investment in manufacturing infrastructure.

RMS machines require scalable and open control systems. The scalability of a machines control system is necessary to facilitate the reconfiguration of the mechanical hardware. Existing Dedicated Machine Tools (DMTs) and Computer Numerically Controlled (CNC) machines posses unalterable monolithic control systems that generally do not provide the facility for the integration of additional actuation and control features on a platform. The implementation of user specific actuators, sensors and control algorithms, on commercially available processing platforms, possesses the potential to optimize the performance of a manufacturing system. Performance benefits include a reduction in machine cycle times, reductions in tool breakage, a reduction in rework and improvements in product quality. The creation of manufacturer specific features on a machine is currently only available on custom built hardware. The implementation of custom built hardware in a manufacturing system is uneconomical and not feasible if systems are to be initialized rapidly. The reengineering of commercially available machines is necessary to facilitate the implementation of user specific features within bounds that are acceptable to machine building companies.

Production scalability is a desired characteristic for RMSs. The scalability of production streams through the redistribution of hardware resources is an attractive, cost effective solution to scalability in systems producing a variety of products.

The concept of scalability through hardware redistribution involves the movement of resources between different production streams, as the capacity requirement of each stream varies. Hardware sharing between streams will ensure more complete use of system resources, and a potential reduction in capital investment. The ability of machines to facilitate production scalability has thus far been limited or impossible.

Regarding DMTs, production scalability is achieved through the purchasing of additional machines and the duplication of production lines. In a system employing DMTs, the redistribution of machining resources between distinctly different production streams is generally impossible. CNC machines, on the contrary, possess the ability to aid in the scalability of production streams. CNC machines are flexible in a manner that parts produced by one stream are capable of being produced by the machines employed in a second production stream. The limitation with a CNC machine being redistributed as a machining resource to another production stream is that the parts being created in that stream fall must fall within its production envelope. RMSs require machines with extensible production envelopes to enable advanced scalability with existing hardware resources.

### 1.3 Project Objectives

The objectives of this research were to:

- Research and establish a list of the essential characteristics that RMSs must display
- Research and establish criteria and design principles for reconfigurable machines
- Research, design and construct a mechanically reconfigurable machine for RMSs
- Research, design and implement a suitable control system. This must include the development of the electronic hardware, the programming of machine control algorithms and the creation of a Graphical User Interface (GUI) for human interaction
- Analyse the performance of the prototype machine and evaluate its applicability to RMSs


### 1.4 Scientific Contribution of the Dissertation

This research presents the development of a Modular Reconfigurable Machine (MRM) for RMSs. MRMs are machines that have been designed to be functionally modular in their mechanical and control architectures. A prototype has been designed for material removal operations. The novel modular design of the mechanical architecture permits the reconfiguration of the machines kinematic chain and processing functions in accordance to changing production requirements. The mechanical reconfiguration of the platform was achieved by the addition and removal of modular units of hardware from its structure. According to the literature survey, reconfigurable machines of this nature have not been previously developed by industrial machine builders or academia. The MRM possessed a modular, scalable Mechatronic control system which lays in direct contrast to traditional monolithic numerical control systems. The control system is lean, and low cost, being created with the intention of illustrating a unique style of control implementation for modular, numerically controlled machines. Although open architecture control has been highlighted as an essential feature for reconfigurable machines, the creation of a fully comprehensive open architecture controller was beyond the scope of this research.

The scientific contribution of this research is the enhancement of manufacturing system functionality through the reconfigurability offered by MRMs. The modular nature of MRMs further aids in the scalability of system production capacity through the synergistic redistribution of hardware. Machine modules may be considered as a resource, instead of entire machines and these modules that may be distributed between production streams as necessary. The movement of modules between streams provides a unique and elegant solution to system scalability (i.e. system production capacity scaling).

The MRM presented in this dissertation has been developed to perform material removal processes. It should be noted that the design methods presented in subsequent chapters may be extrapolated to create reconfigurable machines for other types of processing operations. Such machines may include Numerically Controlled (NC) robots, chip mounters and assembly machines with modular end effectors or other modular components.

### 1.5 Research Publications

- J. Padayachee, G. Bright; Modular Reconfigurable Machines for Reconfigurable Manufacturing Systems; $24^{\text {th }}$ ISPE International Conference on CAD/CAM, Robotics and Factories of the Future; 29-31 July 2008; Koriyama; Japan
- J. Padayachee, I. Masekamela, G. Bright, C. Kumile, N.S. Tlale; Modular Reconfigurable Machines Incorporating Open Architecture Control; 15th International Conference on Mechatronics and Machine Vision in Practice (M2VIP'08); 2-4 December 2008; Auckland; New Zealand
- J. Padayachee, G. Bright; Modular Reconfigurable Machining Systems for Reconfigurable Manufacturing Environments; 2nd Robotics and Mechatronics Symposium (RobMech 2008); 10-11 November 2008; Bloemfontein; South Africa; Pages 6-11
- J. Padayachee, G. Bright, I Masekamela; Modular Reconfigurable Machine Tools: Design, Control and Evaluation, South African Journal of Industrial Engineering; Volume 20, Number 2; November 2009 ; Pages 127-143
- J. Padayachee, G. Bright; Design of Reconfigurable Machine Tools for Reconfigurable Manufacturing; 3rd Mechatronics and Robotics Symposium; (RobMech 2009); 9 November 2009; Pretoria; South Africa
- J. Padayachee, G. Bright; The Development of a Mechatronic Control System for Modular Reconfigurable Machine Tools; Australasian Conference on Robotics and Automation (ACRA 2009); 2-4 December 2009; Sydney; Australia
- J. Padayachee, S. Davrajh, J. Collins, G. Bright; The Development of Reconfigurable Manufacturing Equipment for Product Mass Customization; International Conference on Competitive Manufacturing (COMA ’10); 3-5 February 2010; Stellenbosch; South Africa; Pages 291-296
- J. Padayachee, G. Bright; The Design of a Reconfigurable Control System for NC Machines with Augmented Flexibility; $25^{\text {th }}$ ISPE International Conference on CAD/CAM, Robotics and Factories of the Future; 14-16 July 2010; Pretoria; South Africa


### 1.6 Outline of Dissertation

Chapter One: Introduces the reader to the background of the project, the motivation for the research and the resultant scientific contributions. The objectives of the project are also presented.

Chapter Two: Analyses the inadequacies of existing manufacturing paradigms. The concept of reconfigurable manufacturing is presented and an analysis of the benefits of RMSs is conducted. Enabling technologies for RMSs are identified including the characteristics they must display.

Chapter Three: Analyses the merits and inadequacies of existing types of production machinery. Other developments are presented on the design of reconfigurable machines and useful advancements are identified.

Chapter Four: Presents the concept of MRMs, the criteria they must display and the principles used in their design. Engineering specifications for the development of a prototype library of modules are presented in this chapter.

Chapter Five: Presents the mechanical design and modelling of MRMs. Mechanical assemblies for different MRM configurations are presented. The static and dynamic analysis of a selected assembly is also included.

Chapter Six: Presents the electronic hardware system that was developed for the actuation and control of the MRM assemblies.

Chapter Seven: Presents the software system that was developed for execution of user programs on MRM platforms.

Chapter Eight: Addresses the assembly and calibration of MRM systems. Results are presented for the performance of the tool positioning systems in MRMs under different modes of motion control.

Chapter Nine: Summarizes the performance of the system. The implications of MRMs for reconfigurable manufacturing are presented and problems in MRMs are also identified.

Chapter Ten: Concludes this dissertation with a discussion of the advantages and disadvantages of MRMs, including problems that will require future research.

### 1.7 Chapter Summary

This chapter introduced the reader to the challenges in modern manufacturing that have provided the motivation for this research. The scientific contributions of the research were discussed and the objectives of the project were outlined. References have also been provided to conference papers and journal publications that have emerged from the work presented in this dissertation.

## 2. Reconfigurable Manufacturing Systems

### 2.1 A Review of Dedicated Manufacturing Systems

Dedicated Manufacturing Systems are historically the first manufacturing system paradigm, introduced at the beginning of the 1900's [5]. These systems are designed for the production of a single item or a bounded group of products. The dedicated nature of these systems implies a lower capital investment in system initialization, as compared to more flexible systems. These systems employ transfer line technology, dedicated machinery and fixed automation for optimized, robustly system performance. DMSs are capable of producing a high volume of units rapidly and cost effectively while maintaining high standards of quality [6]. However, achieving significant product variety is impossible due to the inflexible nature of the Dedicated Machine Tools employed in DMSs.

The lack of system scalability is a problem in DMSs. The capacity of a dedicated system may be scaled up by duplicating production lines when the demand for products exceeds the current capacity of a system. This is a very costly approach to system scalability and is not feasible as the minimum step size in system capacity is limited to the capacity of the line being duplicated [6]. Although DMSs are designed for high production capacities, these systems do not always operate at maximum capacity. When the demand for products is low DMSs possess excessive functionality and such systems are only economical when market demand for a specific product is high.

### 2.2 A Review of Flexible Manufacturing Systems

The Flexible Manufacturing paradigm was introduced in the 1970's to overcome the problem of inflexibility in manufacturing systems of the time [7]. Flexibility is viewed as the ability of a system to change and assume different positions or states in response to changing requirements rapidly and with minimal penalty in effort, cost or performance [8]. FMSs are systems with fixed hardware and fixed, but programmable software to manage changes in products and production schedules [9]. Such systems are designed for general flexibility, with CNC machines, robots and flexible material handling systems as their main elements [5].

At the machine level, CNC machines provide the framework for flexibility in FMSs. These machines are created with generic processing capabilities that enable the system to respond to reasonable changes in products and product families without an additional capital investment in new machinery. A generic number of axes and a generic spindle imply that CNC machines are not kinematically or dynamically optimized to any specific operation. The result is that CNC machines often possess unused functionality.

A survey on FMSs was conducted by Mehrabi et al [7] in the year 2002. The objective of the survey was to perform an assessment of the satisfaction of manufacturers and other related agencies with the performance of FMSs and associated technologies such as CNC machines. Industry respondents included machine tool builders, automotive, aerospace, robotics and mining companies in the United States.

The results revealed that two-thirds of the organizations that participated in the survey were dissatisfied with the performance of FMSs. The problems with FMSs according to the survey were:

- High system initialization costs
- Fifty percent of correspondents reported that their systems possessed excessive functionality
- The CNC machines in many cases possessed excessive features that were never used
- Fifty percent of correspondents reported excess tool magazine capacity
- Correspondents reported problems in operator training, system reliability and maintenance, software and communication, and the cost involved in increasing system capacity

Further research by Lin et al [10] has revealed that FMSs as a whole have low throughputs of customized parts and display significantly longer payback periods than DMSs. Based on the survey conducted by Mehrabi et al [7], manufacturing enterprises, government and trade organizations, research institutions and manufacturing system builders agreed that the reconfigurable manufacturing paradigm was the next logical advancement in the evolution of global manufacturing.

### 2.3 The Reconfigurable Manufacturing Paradigm

The reconfigurable manufacturing paradigm was conceptualized through an international collaboration between researchers in the United States and Europe. Participating universities included the University of Michigan, University of Stuttgart, Politechnico di Milano and Katholieke Universiteit Leuven [1]. The definition of a Reconfigurable Manufacturing System is as follows:

> " A Reconfigurable Manufacturing System (RMS) is a system that combines the advantages of DMSs and FMSs by designing it at the outset for rapid change in structure, as well as in its machines and controls, in order to quickly adjust production capacity and functionality in response to market or product changes."

RMSs are envisioned to possess intermediate functionality and production capacity between DMSs and FMSs; this will enable a RMS to display the best features of these two historic paradigms (see Figure 2.1). The intermediate positioning of RMS aims at a compromise between large production volumes and high product variety to achieve a reasonable output of an assortment of products.

The main objective of the RMS paradigm is to increase manufacturing system responsiveness to market and product changes. RMSs must therefore provide the functionality and capacity that is required, when it is necessary. A RMS may therefore display performance characteristics more likened to the extremities of either DMSs or FMSs, depending on system requirements at different times. The responsiveness of the system is achieved by the design of its elements for structural and software transformability. Production streams and processes are envisioned to be transformed by the reconfiguration of machines and the rearrangement of flow paths between machines.

At a machine level, rapid transformations are envisioned to be achieved by the changing of machine hardware components and the installation and reconfiguring of software.


Functionality (product variety)

Figure 2.1: Characteristics of Manufacturing Systems in Capacity- Functionality Coordinates [9]
RMSs extend further to incorporate features of lean manufacturing. Lean manufacturing is defined as an adaptation of mass production in which workers and work cells are made more flexible and efficient by adopting methods that reduce waste [11]. Lean manufacturing aims at a reduction of waste in production on a number of levels:

- Market: At the market level lean manufacturing aims to eliminate features in products that are unnecessary or unwanted by customers.
- Enterprise: At the enterprise level lean manufacturing aims to reduce waste due to over production and the holding of excessive inventory.
- System: At the system level lean manufacturing reduces waste due to production flaws and the waste of raw materials and consumables due to inefficient processes.

In general the objective of lean manufacturing is the reduction of any identifiable form of waste, thereby optimizing the efficiency of production and maximizing profits [11]. Figure 2.2 summarizes the economic goals of the dedicated, flexible and lean manufacturing paradigms. RMSs aim to achieve these goals in addition to enhancing system responsiveness to market demands, thereby granting manufacturers a competitive advantage.


Figure 2.2: The Economic Goals of Various Manufacturing Paradigms

### 2.4 Customized Flexibility in RMSs

RMSs are intended to be low cost systems that incorporate the high output of DMSs while combining the flexibility of FMSs. The low cost and high output of these systems are intended to be achieved by basing manufacturing system configurations on specific product families. Once the fabrication of a product family is complete, the system reconfigures to produce a different group of products. Galan et al [12] have established product families as the starting point in the configuring of a RMS and have endeavoured to provide a systematic approach for the subsequent formation of optimized part families. The efficiency of a configuration is dependent on the commonality of product/part features, the similarity in manufacturing processes and the market demand of each product.

The level of flexibility in a RMS must be tailored through reconfiguration, to the manufacturing requirements of each product family. Extensive studies on the various types of flexibility in a manufacturing system are presented by Sethi and Sethi [13] and Browne et al [14]. Flexibility may be broadly categorized into three groups: system hardware and software flexibility, system management and control flexibility and system expansion flexibility. The reduction in cost of system infrastructure is primarily concerned with the limitation of hardware and software flexibility. Hardware and software expenses form a substantial component of the capital investment in the initialization of a system. Unused (excessive) features are representative of capital that yields a zero return to an investor.

Through each reconfiguration cycle the following types of flexibility must be customized to ensure that the system does not possess unnecessary functionality [13, 14]:

- Machine Flexibility: The number of processing operations and axes displayed by a machine.
- Material Handling Flexibility: The total number of paths between machines.
- Volume Flexibility: The ability to vary production volumes.
- Process Flexibility: The set of part types that can be produced by current process configurations.

The limitation of these four types of flexibility is also intended as a means of customizing and optimizing each reconfigured state, enabling greater production volumes than FMSs. The ability of the system to then assume new machine characteristics as well as new material handling, volume and process flexibility characteristics through reconfiguration, is dependent on the expansion flexibility of the system.

### 2.5 Scalable Production Capacity in RMSs

Cost effective and rapid capacity scaling is essential in providing a profitable response to increases in product demand. Figure 2.3 illustrates the cost versus capacity characteristics of DMSs and FMSs and the idealized trend that RMSs are expected to exhibit. The DMS trend indicates a large minimum step size in capacity scaling, and the cost of increasing the production rate is high. An additional investment in capacity for DMS is only profitable for a long term, sustained increase in product demand.

The FMS characteristic indicates a smaller minimum step in capacity scaling, however the overall cost of increasing a FMSs capacity is higher. The higher cost is due to the large price difference between CNC machines and the DMTs employed in DMSs. The cost of flexible material handling systems is also higher than that of the fixed transfer lines employed in DMSs. The capacity gain in a FMS is also low compared to capital invested. This trend is due to low production volumes capable by CNC machines and as mentioned, these machines exhibit a longer pay-back period than DMTs.


Figure 2.3: Manufacturing System Cost versus Capacity [1]

The RMS cost versus capacity characteristic is prescribed to exhibit features of both DMSs and FMSs. RMSs are predicted to display a small minimum step size in capacity scaling. A smaller step size implies a greater responsiveness to moderate increases in product demand, and the risk involved with capital investments are lower. The gain in capacity for an individual step is envisioned to be high to provide a more profitable response to increased market demand. The frequency of capital investment in infrastructure is also expected to be low as machines for RMS are to be designed for easy modification and reuse.

### 2.6 Reconfigurability and Expansion Flexibility in RMSs

Expansion flexibility is the ease with which a system's capacity or functionality may be augmented through physical changes in the system [13, 14]. Rapidly adjustable capacity and functionality are the desired features for RMSs as this will enable these systems to cope with changes in markets and products, quickly and efficiently. It should be noted that under the context of RMSs, the understanding of expansion flexibility is consistent with that of reconfigurability [15]. The expansion flexibility of an RMS is prescribed to be maintained by the design of its hardware and control systems for easy rearrangement and rapid changes in their internal structures. If RMS machines, material handling systems, assembly robots and quality control systems are not designed for easy reconfigurability, the reconfiguration process will be lengthy and impractical [1]. Presently design methods and reconfiguration methodologies are under development, and enabling technologies for RMSs are not commercially available.

### 2.7 Manufacturing System Life Cycle

The lifespan of a manufacturing operation is determined by the expansion flexibility of the systems employed in view of product or market changes, before the system as a whole becomes unresponsive, redundant and outdated. The lifecycle of a system is the cycle of system expansion/reconfiguration as production requirements evolve over a period of time. The period for which a manufacturing configuration is suitable, is generally inconsistent and is strongly related to changes in market demand and progression in consumer goods technologies.


Figure 2.4: Manufacturing Systems Lifecycle, Initial Design, Redesign and Reconfiguration [15]

ElMaraghy [15] modelled the lifecycle of a manufacturing system as outlined in Figure 2.4. This model illustrates the initial design of a manufacturing system based on production requirements and constraints at the time of initialization. The initial system design is analysed, simulated, implemented and maintained until new manufacturing requirements emerge. The system is then redesigned and reconfigured cyclically as necessary. The process of reconfiguration is intended to extend the lifespan and utility of a manufacturing system. The lifespan of a RMS is envisioned to be significantly longer than a DMS, and the cost of extending its lifespan much lower than FMSs. This is to be achieved by the design of RMSs and their enabling technologies for expansion flexibility.

### 2.8 Essential Characteristics of RMSs

RMSs are systems where machine components, mechanisms, machines, cells, conveyors and other material handling systems can be added or removed in different configurations as required [7]. To display such reconfigurability RMSs must possess the following characteristics: modularity, convertibility, integrability, customization and diagnosability. Koren et al [1] and Mehrabi [9] discuss these terms as they relate to RMSs as follows:

Modularity: Requires the design of system components; mechanical and electronic control hardware as well as software to be modular or support modularity.

Convertibility: Requires the design of the system for a rapid conversion to produce the new products. Design for rapid conversion aims at reducing system down time and ramp-up time. Conversion entails the retooling of machines, the reorientation of machine axes, the integration of additional mechanical and control hardware into platforms and the loading of programs to produce the next family of parts.

Customization: Requires systems to be the initialized with only the necessary functionality and capacity needed for production. Customization requires that the machines used in production be kinematically and functionally matched to their applications.

Integrability: Requires the design of system components to be easily integrated into the system as required. Design for integrability facilitates the upgrading of system components as new technology emerges. The process of integration is greatly facilitated by the use of standardized components, interfaces and communication protocols in hardware and software systems.

Diagnosability: Requires system and machine design that incorporates diagnostics that will facilitate the quick identification of sources of problems within the system. Tools for the diagnosis of quality and reliability problems become indispensable if system ramp-up time is to be minimized.

The characteristics of modularity, convertibility, customization, integrability, and diagnosability are qualities that enable reconfigurability/expansion flexibility in machines, work cells and systems at large. These characteristics are recommended to be applied at all levels of a RMS (system, process, machine, software and control) to ensure a fully reconfigurable system.

### 2.9 Enabling Technologies for RMSs

RMSs require the development of enabling technologies that will bring to realization the idealized aims and predicted advantages of the paradigm. The goals of previous manufacturing paradigms have dictated the features of the technologies associated with those systems and cannot be implemented in RMSs without further improvement. Technologies that require development for RMSs are reconfigurable: machining systems, fixturing systems, assembly systems, quality control system and material handling.

This research is concerned with the development of a reconfigurable machining system and advancements in the field of reconfigurable machine tools are discussed in detail in Chapter 3. A brief summary of global research efforts on other technologies for RMSs are summarized in Table 2.1. This list is by no means exhaustive and intended only to highlight some important areas of research in RMS.

Table 2.1: Global Research in Enabling Technologies for RMS

| Field of Research | Publication | Authors |
| :---: | :---: | :---: |
| Reconfigurable Quality Control | Design Requirements of Quality Control Systems for Reconfigurable Cellular Manufacturing Environments | S. Davrajh, G. Bright [16] |
|  | Integration of Reconfigurable Inspection with Stream of Variations Methodology | J. Barhak, D. Djurdjanovic, P. Spicer, R. Katz [17] |
|  | Reconfigurable Inspection Machine for Machining Production Lines | R.Katz, M.G. Zutek, Y. Koren [18] |
| Reconfigurable Material Handling | Reconfigurable Materials Handling Control Architecture for Mass Customization Manufacturing | A.J. Walker, L.J. Butler, N. Hassan, G. Bright [19] |
| Reconfigurable Assembly | A Reconfigurable Assembly Cell for Mechanical Products | F. Giusti, M. Santochi, A. Arioti [20] |
|  | Modular Reconfigurable Flexible Final Assembly Systems | J. Heilala, P. Voho [21] |
|  | Reconfigurable Dual Robot Assembly System, Design ,, Developments and Future Directions | S.J. Hseih [22] |
| Reconfigurable Robotics | Theory and Application of Reconfigurable Robotic Systems | I. M Chen [23] |
|  | Design Fundamentals of <br> Reconfigurable Robotic Gripper <br> Systems   | R Kolluru, K.P. Valavanis, S.A. Smith, N. Tsourveloudis [24] |
| Reconfigurable Manufacturing Cells | Rapid Response Manufacturing Through Reconfigurable Robotic Work Cells | I.M. Chen [25] |
|  | Reconfiguration of Manufacturing Cell Control Systems and Reuse of their Components | R.P. Monfared, R.H. Weston [26] |
| Software and Control of RMSs | Process Control and Configuration of a Reconfigurable Production System using a Multi-Agent Software System | J.J. van Rensburg, H. Vermaak [17] |
|  | Control Architecture for Reconfigurable Manufacturing Systems | L. Ferrarini, C. Veber, A. Luder, J. Peschke, A. Kalogeras, J. Gialelis, J. Rode, D. Wunsch, V. Chapurlat [28] |

### 2.10 Chapter Summary

This chapter summarized the merits and problems of existing manufacturing paradigms. The concept of reconfigurable manufacturing was introduced and a definition of RMSs was provided. Matters pertaining to system flexibility, capacity, expansion flexibility and system life cycles were discussed in the context of RMSs. Enabling technologies for RMSs were identified and essential characteristics for the design of reconfigurable manufacturing equipment were presented.

## 3. Automated Production Machines

### 3.1. Dedicated Machine Tools

The design of a production machine is dependent on the flexibility and performance required from it. There are two customary design schemes for production machines. The first scheme initiates machine design based on the knowledge of the part, or product that is to be produced on that machine. The second scheme initiates machine design based on generic processing operations without prior knowledge of the manufacturing functions it will ultimately perform.

Dedicated Machine Tools (DMTs) are those machines that have been designed based on prior knowledge of a part or product. These machines are characteristic of DMSs, being created for the purpose of producing a known part rapidly and efficiently [1]. The design scheme for DMTs restricts the kinematic flexibility, spindle size, range of tooling and fixturing of the machine to the exact capability required to produce a given part. DMTs also possess fixed automation that is restricted in functionality to the control of specific operations. DMTs are often created in-house by manufacturers. Commercial alternatives for the purchase of DMTs are generally restricted, due to the specific nature of the equipment. The creation of DMTs is also widely initiated through the consultation of manufacturers with machine building companies.

The restrictive nature of DMT design results in machines that are optimized for a specific process. The advantages of an optimized, lean design are: the production of high quality goods, high production volumes, less raw material wastage and rework, rapid system ramp-up and relatively low cost of machines. Manufacturing enterprises such as The Boeing Company in Washington, USA favour the implementation of DMTs over more flexible machine tools due to the robust performance and cost savings derived from a dedicated design [29].

A DMT is the optimal machine, purely in consideration of robust performance with regard to manufacturing a specific part. Nonetheless the disadvantages of DMTs become evident in consideration of dynamic manufacturing environments. The greatest inhibiting factor for the implementation of DMTs in RMSs is the inability of these machines to effectively cope with changes in products. DMTs cannot be cost effectively converted when parts or products change and are therefore only economical for the long term production of specific items [30]. DMTs may be implemented in RMSs, but in limited numbers for the manufacturing of standardized components that are not expected to change through multiple product iterations.

### 3.2. Computer Numerically Controlled Machines

The concept of Numerical Control (NC) originated after World War II, when in 1947 the United States Air Force developed a method for moving two axes by using punch cards including coordinate data to manufacture aircraft parts [31]. In 1952, a three axis milling machine, the world"s first official NC production machine was developed at the servo laboratory, at Massachusetts Institute of Technology. Early NC machines were hardwired and performed functions according to the configuration of connected elements by electrical wiring. The advent of digital computing led to the integration of microprocessor technology in NC machines since the 1980"s and these machines are now known as Computer Numerically Controlled (CNC) machines.

In present times CNC technology has been applied to the development of a variety of machines. CNC machines are generally multi-purpose machines, being design to perform wide range operations. These machine tools can be classified as "cutting machines" and "non-cutting machines" [31]. Cutting machines perform material removal and common processing operations are: milling, drilling, turning, engraving, flame cutting and Electric Discharge Machining (EDM). Non-cutting machine tools include CNC presses and bending machines. The scope of CNC technology extends to robotic systems, welding and painting machines, semi-conductor handlers and chip mounting machines. Figure 3.1 illustrates three types of machines based on CNC technology.


Figure 3.1: Production Machines Based on CNC Technology [32, 33, 34]
a. The Haas vertical CNC mill - Material removal with a cutting tool [32]
b. A wire EDM - Material cutting via electric discharge [33]
c. Robotic CNCs - Non cutting CNCs [34]

CNCs are characteristic of FMSs, enabling these systems to produce a variety of products [1]. The automotive, maritime, aerospace and tool manufacturing industries are among the many industries that implement CNCs. These machines are also commonplace in engineering workshops and Small and Medium Enterprises (SMMEs) that service the specific needs of larger industries such as power generation and chemical processing plants.

With regard to material removal, CNCs possess a generic number of axes and a generic spindle. The flexible mechanical architecture of CNCs ensures a broad machining envelope, facilitating the ,absorption" of changes in parts or products. The generic nature of these machines additionally limits the possibility of redundancy and allows the integration of CNCs into multiple manufacturing configurations. Further advantages of this technology include: reduced operator involvement and the machining of complex contours.

The comprehensive flexibility of CNCs results in these machines being generally expensive with low production rates achieved on a platform. The flexibility of the machines in most manufacturing implementations may be excessive and although being designed for general flexibility these machines may nonetheless lack the functionality needed for a specific operation. The fixed mechanical architecture of both CNCs and DMTs neither permit any mechanical alterations to the machine, nor facilitates the integration of new hardware and additional sensors onto the platform.

CNC machines are primarily programmed in G-Code (ISO 6983), with advancements such as Computer Aided Part Programming (CAPP) and Computer Aided Manufacturing (CAM) software emerging in recent years for easier program generation. The software architectures of the machines are fixed, but the machine is end user programmable [35]. The proprietary nature of such control systems does not afford the end user access to the controller and upgrades or enhancements to the system are either impossible or very costly [4].

The inability to access the lower levels of the controller hinders the application of more efficient algorithms, the integration of new sensors and restricts the machine in being interfaced with a higher control system. Researchers in both academia and industry have concluded that traditional, closed CNC machine tools do not provide the functionality, flexibility or cost effectiveness necessary to match the demands of modern manufacturing [8].

### 3.3. Reconfigurable Machine Tools: The Arch Type RMT

The development of reconfigurable machinery has been motivated by the inadequacies in DMTs and CNCs, these are: poor expansion flexibility, rigid mechanical and control architectures and excessive or limited functionality. The philosophy of reconfigurable machine design has yet to converge on a single set of principles. Internationally, perspectives on the design of reconfigurable machines follow three strains of thought:
(i) Reconfigurable Machines are to be designed with intermediate flexibility between CNCs and DMTs: the part family approach to machine design.
(ii) The flexibility of reconfigurable machines must exceed that of CNC machines: the design for a wider range of generic operations.
(iii) It is not meaningful to distinguish reconfigurable machines from CNC machines: implement CNC machines in RMSs.
a.

b.


Figure 3.2: The Arch Type Reconfigurable Machine Tool [36]
a. The Arch Type RMT
b. Reconfigurable position of the Z-axis. The angle of inclination can be changed from $-15^{\circ}$ to $60^{\circ}$

The philosophy of Reconfigurable Machine design for intermediate flexibility between CNCs and DMTs was first proposed by researchers at the University of Michigan. This philosophy was applied to the creation of the worlds first Reconfigurable Machine Tool (RMT), the Arch Type RMT (see Figure 3.2.a). The objective of creating the Arch Type RMT was to illustrate the principle of constructing machine tools around part families. The machine was not restricted to a single part as in the case of a DMT, nor did the machine possess general-purpose flexibility as in CNC machines.

The flexibility of the machine was restricted by designing it around a family of V6 and V8 engine blocks [37]. The machine could perform milling operations on discreet inclined planes. Figure 3.2.b illustrates the reconfiguration of the machine by reorienting the machine spindle in $15^{\circ}$ steps through a range from $15^{\circ}$ degrees below the line of the work table to $60^{\circ}$ above the line of the work table. The discreet reorientation of the machine spindle reduced the number of active DOF during machine operation, simplifying the machine control system. Benefits demonstrated by this method of machine design are:

- lean design by a part family approach to flexibility,
- the realisation of design simplicity by use of non-orthogonal machine axes,
- a lean mechanical and control design by discreet reorientation of machine axes,
- the potential for high production volumes by mechanically optimised machine configurations.

The literature survey has indicated that the Arch Type RMT has been the only significant attempt at the development of a serial reconfigurable machine tool to date.

### 3.4 Reconfigurable Machine Tools: Design Methods

### 3.4.1 Virtual Modularity in RMT Design

Shinno and Ito [38, 39, 40] developed a methodology whereby the structural configuration of machine tools may be generated from simple geometric objects. This introduced the notion of structurally generating machinery from elementary modular subsystems. The structural synthesis of machines from simple virtual modules has been conducted by Chen and Yan [41]. Researchers at the University of Michigan further extrapolated this methodology for the fabrication of a virtual library of precompiled mechanical modules from which multiple types of machine tools could be assembled $[42,43]$. The structural synthesis of machines from a precompiled library of modules has been identified as an important advancement in facilitating the rapid design of machines.

The concept of modular design of machine tools has been discussed in academia since the 1980 "s. It has thus far been successfully used for the virtual synthesis of machine tools. The methodology has however, not been practically adopted for the creation of machines that are physically modular.

### 3.4.2 Kinematic Optimization of RMTs

Landers et al [30] and Moon and Kota [42, 44] have developed a mathematical framework for the synthesis of a kinematically viable machine tool from a library of mechanical building blocks. The methodology is intended to yield optimized and kinematically exact solutions in reference to the part being produced.


Figure 3.3: RMT Kinematic Design Methodology [30]

The sequence of steps in this methodology is illustrated in Figure 3.3. The first step in the methodology is the use of a screw theory based mathematical representation to obtain a task matrix from process plans and CAD drawings. The motion of any rigid body may be represented by a screw, which is comprised of a rotation about an axis and a translation about that axis. In this method discreet tool trajectories are represented by a screw. The general format of a screw is given by equation 3.1:

$$
\begin{equation*}
\stackrel{\rightharpoonup}{\$}=\left[M_{M} M_{m} M_{c}\right]\left(P_{A}+\varepsilon P_{T}\right)\left\{\vec{S}+\varepsilon \vec{S}_{o}\right\} \tag{3.1}
\end{equation*}
$$

$M_{M}, M_{m}$ and $M_{c}$ represent the maximum, minimum and current positions of the tool in the trajectory. The term $\left(P_{A}+\varepsilon P_{T}\right)$ represents the pitch of the motion and lastly the term $\left\{\vec{S}+\varepsilon \vec{S}_{o}\right\}$ represents the direction of motion. The complete set of screws, used to describe the desired operation is then condensed into a Homogenous Transformation Matrix (HTM). Elements of the task transformation matrix are represented by templates in a Function Structure Graph as illustrated in Figure 3.4. The graph gives the overall topology of the required machine tool, and suitable library modules are assigned to appropriate place holders or templates on the graph.


Figure 3.4: An Example of a Function Structure Graph [42]

It is recommended for RMT design that mechanical modules are combined into a library and parameterised according to individual HTMs [44]. The individual HTMs of the modules assigned to the Function Structure Graph are then concatenated according to equation 3.2 to yield a feasible machine transformation matrix:

$$
\begin{equation*}
\underset{\text { tool }}{\text { work }} T=M_{1} M_{2} M_{3} \ldots M_{n} \tag{3.2}
\end{equation*}
$$

If the resultant machine transformation matrix is in the image of the task transformation matrix then the current selection of modules is kinematically viable. This method is capable of yielding multiple, kinematically viable module sets for the construction of a machine tool. A library of modules may include a range of kinematically equivalent units; in this instance the optimal machine configuration is obtained by examining different module combinations while considering factors such as: mechanical stiffness, actuator speeds and torque.

### 3.4.3 Software Aids in Virtual RMT Synthesis

The rapid development of machine tools is necessary for shortening the production lead time on newly developed products. Software systems intended to shorten the machine design process have been developed at the University of Michigan (USA) and Fraunhofer Institute for Machine Tools and Forming Technology (Germany). The software package developed by the Fraunhofer Institute is called VRAx, which was created to give German machine tool companies a competitive advantage over their Japanese, South Korean and Chinese counterparts [45]. The VRAx system was not created with the intention of developing RMTs; however it does feature related design techniques. The software possessed the ability to create and store common machine components in a database. These components can be accessed at a later stage and used to create multiple types of machinery rapidly in a virtual environment. The concept employed in this software is a direct parallel to that of virtual modular machine design.


Figure 3.5: Screen shots of PREMADE (PRogram for REconfigurable MAchine DEsign) [37]

The University of Michigan developed a software package called PREMADE (PRogram for REconfigurable MAchine DEsign). The PREMADE package was designed specifically for the development of RMTs and contained a library of virtual mechanical modules for the rapid design of machines [37]. The software package incorporated the mathematical methodology developed by Moon and Kota [42, 44] and was capable of generating feasible machine designs based on the input of relevant part data.

Figure 3.5 illustrates a screen shot of the software. It should be noted that neither the VRAx system nor PREMADE have been made commercially available.

### 3.5 Open Architecture Control

Mehrabi et al [4] have emphasized the importance of Open Architecture Control (OAC) in machine control systems for RMSs. OAC aims at the easy implementation and integration of user-specific controls by means of open interfaces and configuration methods in a vendor neutral, standardized environment [46]. OACs are designed for PC-based control hardware. The advent of faster processors for Personal Computers (PCs) and a reduction in their prices have increased the use of PC-based controllers for machining systems. PC-based controllers are flexible, open and can be easily integrated into multiple manufacturing configurations [47].


Figure 3.6: Components of Open Control Systems [46]
Figure 3.6 illustrates essential components that an OAC must possess and the interaction between these components. OACs provide lower level access to control components and facilitate the integration of third party software by means of standardized internal and external interfaces. Standardized external interfaces are divided into programming interfaces and communication interfaces. For machine tools G-Code (ISO 6983) forms the programming interface, creating an internationally standardized method of machine programming.

Standardized communication interfaces with superior control systems entail provision for Ethernet and TCP/IP for machine integration into a factory wide control network. Communication networks such as CAN, PROFIBUS and SERCOS are used to communicate with subordinate peripheral devices such as Digital Signal Processor (DSP) boards and microcontrollers that are used for low-level processing and I/O operations. The use of standardized communication methods overcomes the problems associated with proprietary communication methods and physical connectors when hardware upgrades or repairs become necessary.

The creation of an internal interface for an OAC is concerned with the provision of an Application Programming Interface (API) for operator and machine related control functions. An API would serve to completely shield the application software from the hardware platform, thus facilitating the easy installation, and modification of third party application software. Further advantages include software portability, scalability and interoperability [48].

Since the $1990^{\circ}$ s, organizations like Open Systems Architecture for Controls within Automation systems (OSACA), Open Modular Architectures Controllers (OMAC) and academic institutions like University of Michigan, University of British Columbia have drawn standards and developed open architecture controllers for machine tools [49]. Most controllers of this nature are implemented on PC"s supporting a real-time Operating System (OS). Although several controllers have been successfully implemented, much work is still needed in improving the openness and real-time performance.

### 3.6 Chapter Summary

This chapter presented a review of DMTs and CNC machines. The advantages and disadvantages of these established types of machine tools were discussed and their inadequacies formed the motivation for the development of reconfigurable machines. The Arch Type RMT was presented, including other international research developments in the field of RMS machinery. OAC systems were recommended for inclusion in reconfigurable machines and the benefits of such systems were discussed.

## 4. Modular Reconfigurable Machines

### 4.1 Design Approach

This research proposes the development of Modular Reconfigurable Machines (MRMs) as a new solution in the design of automated production machines for RMSs. The design of a MRM prototype required the application of the Mechatronic engineering approach. Mechatronics may be defined as the synergistic integration of mechanical engineering, with electronics and computer control in the design and manufacturing of industrial products or processes [50]. This is one of many definitions of Mechatronic engineering that aim to describe the synergistic interaction of several elements in multidisciplinary engineering. The core disciplines of Mechatronic engineering are illustrated in Figure 4.1. A typical Mechatronic system consists of mechanical hardware, actuators, sensors, controllers, signal conditioning, digital hardware, interface devices and power sources [51]. MRMs, like other automated production machines, are Mechatronic systems as they consist of all of the typifying elements.


Figure 4.1: Graphical Representation of Mechatronic Engineering [52]
Mechatronic Engineering as a design approach promotes the study of the relationships between mechanical, control, electrical and digital subsystems at the earliest stages of the design process. The cross disciplinary examination of interacting systems is essential for development of lean, robust and cost effective designs. The Mechatronic approach involves a concurrent engineering stance to the development of various subsystems as opposed to the traditional sequential method of first developing the mechanical system, then the electrical system and finally the digital system [51]. In this design approach the concurrent engineering principles are applied as early as the conceptual design phase, in order to optimise the final product. Figure 4.2 illustrates the stages involved in the design of a typical Mechatronic system.


Figure 4.2: Sequence of Operations - Mechatronic Design Process (Adapted from [53], [54])

### 4.2 Design Concept

### 4.2.1 Design Perspective

The design of reconfigurable machinery has yet to converge on a single set of principles. The primary division in design philosophies is based on views of machine flexibility. The matter arising is if a reconfigurable machine should assume an intermediate level of flexibility between DMTs and CNC machines, or should it be designed to exceed the flexibility of typical CNCs. The Arch Type RMT is the only prototype machine that has been developed for RMSs to date. This machine was developed with intermediate flexibility between DMTs and CNCs, having been designed around a family of V6 and V8 engine blocks.

In a dynamic manufacturing environment problems may be encountered with designs that are either highly customized or excessively generic. With regard to machine design around a part family, the manufacturer bears the risk of machinery becoming redundant if drastic changes in products are expected. In the case of the Arch Type RMT, designs on automotive engines are not expected to change drastically over a short period of time, and the design of the machine around a part family was acceptable. In many other industries such as industries based on trend driven consumer products, product lifecycles are short and improvements in technology are rapid. Machines employed in the manufacturing of consumer goods with short production lives must be adaptable to dynamic changes in product portfolios and cannot be strictly designed around a part family. Conversely machines may be designed to possess comprehensive inbuilt flexibility, potentially exceeding that of current CNC machines; however such machines would be expensive, complex and will inevitably possess unused features in different manufacturing implementations. To avoid the problems associated with rigidly customized or excessively generic designs, the concept of Modular Reconfigurable Machines (MRMs) has been developed.

MRMs are oriented towards customized flexibility as in the case of the Arch Type RMT; nonetheless the flexibility of the machine may be extended through the process of reconfiguration. It is envisioned that through design for reconfigurability the machining envelope of a MRM could ultimately exceed that of similar CNC machines, although at each configured state the machine will possess only the functionality required for the operation at hand. The concept of customized, yet extensible flexibility in MRMs is realized by a modular design approach. MRMs are machines that are defined to be fully modular in their mechanical and control architectures. Although the idea of modular machines has been pre-existent, no fully modular machine has been developed by industry or academia.

### 4.2.2 Adopted Principles for MRM Design

The principle of machine design from a library of precompiled modules is indispensable in the synthesis of MRMs. This concept is essential for the rapid development of production machinery to capitalize on market opportunities. The concept of developing machines from a library of modules has been previously exploited in virtual machine tool design environments such as PREMADE and VRAx, as discussed in Section 3.4. The idea has nonetheless, never been extrapolated for the fabrication of a physical library of machine modules. Neither have machine tool builders developed individual automated modules for the synthesis of complete machining systems, with the possibility of after market reconfiguration. The main differences between the MRM library of modules and those developed elsewhere [37] are:

- the library exists at a physical level,
- modules within the library are intended for the complete synthesis of modular machine structures,
- modules are intended to be assembled and disassembled in a "building block" fashion,
- modules are intended to be mechanically autonomous and
- modules are intended to enable the after market reconfiguration of machinery.

The complete library of mechanical modules may be considered as the general solution to machining systems for reconfigurable manufacturing. Through the modular, interchangeable capability of the modules, customized solutions may be extracted from the general solution and the property of customized flexibility is present in this approach. The mathematical methodology for module selection developed by Moon and Kota, as discussed in [42, 44] may be implemented to extract the desired machining solution from the generic solution i.e. the identification of the necessary modules for the synthesis of a machine that is exactly matched to the application.

### 4.2.3 Conceptualization of MRMs: Virtual Mock-Up

The concept of MRMs was first tested in the virtual environment provided by the Autodesk Inventor 11 software package. Within this environment a conceptual library of mechanical modules was created for the synthesis of machinery (see Figure 4.3). The conceptual library was first created to clarify the concept of modular machine design and explore decisions on module connectivity and module functions. Modules within the library were categorized according to three classes: Process, Motion and Accessory Modules.

## Process Modules

Process modules are those modules within the library that provide a single manufacturing process.


Figure 4.3: A Conceptual Library of MRM modules [55]
The focus of MRM development in this research has been on material removal processes, and modules in the conceptual library were created for milling, drilling and boring processes. Process modules are envisioned to be the end effectors of a platform and a reconfiguration of the processing functionality is to be achieved by the interchange of MRM cutting heads. Figure 4.4 illustrates the concept where by a 3 -axis milling machine is reconfigured into a 3 -axis line boring machine by the substitution of a single module. Reconfigurability of this nature has not been illustrated by previous RMT designs.


Figure 4.4: The Reconfiguration of a 3-Axis Boring Machine to a 3-Axis Milling Machine [55]

## Motion Modules

Motion modules are units that contribute to the axes of a machine and are responsible for the DOF available to the cutting tool. One motion module corresponds to one axis of a machine. In total six types of motion modules were conceptualised enabling translations along the three axes of a conventional Cartesian system ( $\mathrm{X}, \mathrm{Y}, \mathrm{Z}$ ) and rotations about those axes ( $\mathrm{A}, \mathrm{B}, \mathrm{C}$ ). Although six types of motion modules are intended to be made available only the necessary combination for a specified operation will be integrated into the machining platform.

Figure 4.5 illustrates the kinematic reconfiguration of a 3 -axis milling machine into a 4 -axis milling machine through the integration of an additional motion module.


Figure 4.5: The Reconfiguration of a 3-Axis Milling Machine to a 4-Axis Milling Machine [55]

## Accessory Modules

Accessory modules are units of hardware that are not directly responsible for the material removal process; however these units enable a machine to perform the required operation more efficiently. Such modules include cutting fluid supply and work-clamping modules, steady rests, flow rests etc. In certain instances a machine may not be able to perform an operation without a critical accessory module, e.g. a work table module.

### 4.2.4 Digital Electronic Control

The concept of a mechanically modular machine required a similar approach to the conceptualization of a suitable electronic control system. Mechanical modules are to possess dedicated electronic control modules that map to the mechanical hardware on a 1:1 basis. The creation of a monolithic control system for MRMs would not suffice due to the scalable nature of the mechanical hardware. The electronic control system is therefore specified to be modular and scalable to exactly match the physical characteristics of a MRM platform.


Figure 4.6: Reconfigurable Software and Modular Electronic Control Systems for MRMs
MRMs are also specified to possess OAC systems, implemented on PC-based hardware. OAC is essential for software scalability in correlation to changes in the mechanical and electrical architectures of the machine tool. It is recommended that the MRM host control software be created in C++ to promote a modular programming approach. The architectural style of C++ presents an advantage in the object oriented nature of the programming language. The ability of an object to hide its representation from other client software makes it possible to change the software implementation without affecting the client. This is an essential feature for MRM software, as the system is expected to reconfigure with every reconfiguration of the physical hardware.

As the architecture of the machine changes software modules are envisioned to be added or removed from the host control system. Ideally, software modules are envisioned to be integrated as „Plug-Ins", with a single Plug-In corresponding to a single mechanical module. It should be noted that the creation of a fully functional OAC system with modular software is a momentous task and was beyond the scope of this research.

### 4.3 Design Specifications

A prototype library of MRM modules was to be designed for assembly into machines which display reconfigurability in their processing functions and degrees of freedom. Table 4.1 summarizes the engineering specifications that were prescribed for the development of the library of modules. The specifications also extend to the resultant machines that are assembled from the modules. The allocation of engineering specifications to different entities of the machine tool was strongly influenced by restrictions in development costs for the prototype system. Many of the performance specifications were therefore intentionally set lower than the specifications of industrially available machines.

Table 4.1: Design Specifications for a Prototype Library of MRM Modules

| General |  |
| :---: | :---: |
| Processing functions | Drilling and Turning |
| Machinable Materials | Wax and Plastic |
| Drilling - degrees of freedom | 3-6 |
| Turning - degrees of freedom | 2-3 |
| Motion Modules (Modular Axes) |  |
| Linear Axes |  |
| Maximum speed of at least | $100 \mathrm{~mm} / \mathrm{min}$ |
| Worst Accuracy | 1 mm |
| Worst Repeatability | $\pm 0.5 \mathrm{~mm}$ |
| Rotary Axes |  |
| Maximum speed of at least | $1 \mathrm{rev} / \mathrm{min}$ |
| Worst Accuracy | $1.5^{\circ}$ |
| Worst Repeatability | $\pm 1^{\circ}$ |
| Process Modules (Modular Cutting Heads) |  |
| Drilling capacity | $1 \mathrm{~mm}-10 \mathrm{~mm}$ |
| Turning capacity | 100 mm billet |
| Drilling Assemblies |  |
| Work table size | 100 mm by 100 mm |
| Maximum part size | $100 \mathrm{~mm} \times 100 \mathrm{~mm} \times 100 \mathrm{~mm}$ |
| Turning Assemblies |  |
| Maximum part length of at least | 400 mm |
| Maximum swing over bed of at least | 300 mm |
| Electrical Specifications |  |
| Operating voltage | 220 volt, AC |
| Digital electronics power supply | 12 volt, DC |
| Software Specifications |  |
| Software programming languages | C/C++ |
| Machine operating system | Linux |
| Machine programming language | Simplified G-Code |

### 4.4 Chapter Summary

This chapter presented the Mechatronic design approach for the development of reconfigurable machine tools. The chapter proceeded with a discussion on design perspectives for reconfigurable machines and the principles adopted for MRM design. A library of modules and machines were presented in a virtual mock-up, to illustrate the concept and features of MRMs. Engineering design specifications were presented for the development of a prototype library of modules and the machines that will emerge from their assembly.

## 5. Mechanical Design and Modelling

### 5.1 Mechanical Modules

The development of a MRM system began with the creation of a library of mechanical modules for assembly into complete machine tools. These modules, as discussed in Chapter 4, were intended to possess the ability to be assembled in different configurations to give rise to machines with varying architectural and functional features. During the process of developing a library of modules for MRMs, the possibility of using Commercial Off-The-Shelf (COTS) hardware was considered. Companies in South Africa and abroad offer automated solutions such as linear axes, rotary axes and other types of actuation mechanisms for the development of Mechatronic systems. Researchers such as Mpofu et al [56] have undertaken the task of examining the potential use of COTS hardware for the development of production machinery. Some of the outcomes of their research were:

- no company, local or international, was found to offer a complete set of modules for the development of reconfigurable machines,
- COTS modules did not possess standardized interfaces and the integration of modules from multiple manufacturers would require the use of numerous adaptor plates,
- COTS modules displayed non-standardized motors, supply voltage requirements and proprietary control protocols.

The use of commercially available axes units of hardware was minimal in this design due to the non-standardized nature of those systems. Commercially available units of hardware, which are of a more elementary nature such as spindles, tool holders and chucks were used in the creation of certain modules.

### 5.2 Mechanical Integrity and Design Objectives

The construction of a machine from modules presents an inherent design compromise in the mechanical integrity of a machining structure to enable advanced reconfigurability. The dimensional accuracy and strength of a modular structure is expected to be diminished in comparison to a similar integral cast structure. Modular machine tools were therefore expected from the outset to display reduced performance with regard to conventional CNC machines with integrated cast iron structures.

During the design process for MRM modules, the following factors were identified as essential to the construction of a viable machine tool: adequate strength and rigidity, adequate vibration damping, sufficient power/torque/speed and accurate control of motion. Due to budget constraints in the development of a prototype platform, the negative effect of modularization on these factors could not be diminished to the fullest extent by optimum material and component selection or by the implementation of ideal manufacturing processes. The primary objective of the design has been to explore the functional flexibility achievable in machine tools by a mechanically modular architecture. In view of mechanical integrity, the platform presented in subsequent sections has been designed to machine plastics, wax and other soft materials only.

### 5.3 Generic Architecture of MRM Modules

MRM modules were designed to be physically autonomous units. Module autonomy implies that all components of the drive and sensory infrastructure are to be contained within the body of the module. The functional modularity of an MRM platform has been divided such that one module contributes to one degree of functionality to a platform. A single module performing a dedicated function limited the number of electro-mechanical actuators within a module to one. Electromechanical actuation within modules was provided by either permanent magnet DC motors or AC induction motors, depending on the modules function. MRM modules therefore operated with 12 V DC power, except certain cutting heads that required 220 V AC power for an induction motor.

MRM modules contained in-built power transmission mechanisms such as belt drive systems, gear boxes and power screws for speed reduction and torque amplification. It was compulsory that these mechanisms be contained within the framework of an individual module to simplify the assembly and reconfiguration of modular machines. The provision of standardized mechanical interfaces on the body of the module permitted the interconnectivity of modules and the transmission of torque and forces from module to module.


Figure 5.1: General Architecture of an MRM Module
Electric power was supplied to the modules via standardized electric connections, which enabled modules to be quickly plugged into the power grid. MRM motion modules (modular axes) contained linear encoders for position feedback and limit switches to prevent collisions between internal mechanical components.

Process modules contained accelerometers for vibration sensory feedback. Feedback from sensors was achieved by the provision of a standardized control interface/connection on the modules. Although prototype modules contained a limited variety of sensors, future industrial implementations may include thermal sensors for the activation of heat extraction and strain gauges for the early detection of mechanical failure. Due to the prototypical nature of the existing platform motors were generally low powered and module heating was negligible. For industrial grade modules it is recommended that heat extraction be incorporated into the architecture.

MRM modules did not contain any embedded digital hardware. The choice not to embed digital hardware within a module was based on ease of accessibility to control circuitry for upgrades and repairs. Furthermore heat, dirt and noise generated within the module would have detrimentally affected the performance and lifespan of an internal digital system. The interfacing of modules with externally located control circuitry was achieved through the standardized control interface. Figure 5.1 illustrates the general architecture of an MRM module. Details of the internal elements and their implementation in specific modules are discussed in proceeding sections.

### 5.4 Mechanical Interfacing

### 5.4.1 Bolted Interfaces

MRM modules are connected together by means of a series of standardized mechanical interfaces. These interfaces enable torque and force propagation throughout the machine structure. For a robust solution these interfaces are required to be mechanically simple, easy to align and possess sufficient strength to support tensile and shear forces during machining. MRM modules were manually integrated into platforms, and bolted interface plates were selected as the method of interfacing.


Figure 5.2: Examples of MRM Module Interfaces
a. Single interface found on the base module
b. Double interface found on the column module

The application of standardized interfaces at multiple levels of the machines architecture was essential to ensure the interchangeability of modules. The library of modules employed a series of different interfaces, as the torques experienced at different levels of the machine may vary drastically. Torque is increasingly amplified at modules further away from the cutting tool, with the largest torques and forces being experienced by the base module.

An example of an MRM module interface is illustrated in Figure 5.2.a. This example consists of a single pattern of isometric threaded holes that will enable a bolted connection with an adjacent module. The interface of Figure 5.2.b contains two symmetrical patterns, which extended the range of modules that could be connected to this interface. A maximum of two connection patterns were used per interface. The full series of interfaces that were used in the design are contained in Appendix A.

### 5.4.2 Interface Failure

Interface integrity is of primary concern in the design of modular machines. The creation of a machine structure from modular elements as opposed to an integral cast structure presents a design trade off in the mechanical performance. The mechanical integrity of the machine is dependent on the performance of the interfaces. Bolted interfaces present three modes of failure that must be avoided during the operation of a machine, these are: joint separation, failure by thread stripping and failure by shear.

## Joint Separation and Thread Stripping

Joint separation is the separation of two bolted interface plates under the action of an external tension force $F_{e}$. Joint separation itself is not a form of fracture; however it does affect the accuracy and repeatability of the machine. During joint separation, the normal clamping force $F_{c}$, which two interfaces exert on each other, is zero. The minimum external tension force per bolt $F_{e}$ that will lead to separation is given by equation 5.1. Equations $5.2-4$ give the bolt stiffness $k_{b}$, interface plate stiffness $k_{c}$ (bolt threaded into interface plate) and clamped area $A_{c}$, required to calculate this force. $E$ is the modulus of elasticity of the material, $A_{t}$ is the tensile stressed area and $L$ is the length of either the bolt or the interface.

$$
\begin{gather*}
F_{e}=\frac{k_{b}+k_{c}}{k_{c}} F_{i}  \tag{5.1}\\
k_{b}=\frac{A_{t} E}{L_{\text {bolt }}}  \tag{5.2}\\
k_{c}=\frac{A_{c} E}{L_{\text {int }}}  \tag{5.3}\\
A_{c}=d^{2}+0.68 d g+0.065 g^{2} \tag{5.4}
\end{gather*}
$$

The initial bolt tension $F_{i}$ is usually based on the constant $k_{i}$ being specified in a range of 0.75 to 1.0. When a stronger bolt is threaded into a weaker material $k_{i}$ must be reduced accordingly. Equation 5.5 relates the initial bolt tension to proof strength $S_{p}$ for a preselected value of $k_{i}$.

$$
\begin{equation*}
F_{i}=k_{i} A_{t} S_{p} \tag{5.5}
\end{equation*}
$$

## Thread Stripping

Thread stripping, unlike joint separation is a catastrophic mode of failure. In this design the interface material was usually weaker than the bolt material, due to aluminium modules being fastened extensively with steel bolts.

The tensile force required to shear the thread on a interface is given by equation 5.6 , where $t$ is the height of the thread on the interface plate, $d$ is the nominal diameter of the thread and $S_{\text {shear }}$ is the shear strength of the interface material.

$$
\begin{equation*}
F_{e}=\pi d(0.75 t) S_{\text {shear }} \tag{5.6}
\end{equation*}
$$

## Failure by Shear

Interface failure by shear occurs as a result of excessive direct shear and torsional forces on a bolted structure. Due to geometric positioning, the effective shear force among bolts in the same interface is usually unequal. For a MRM the shear force on a bolt in a particular interface is dependent on:

- The number of modules on a platform
- The type of processing function
- The profile of the cutting tool and the direction tool feed

The number of possible loading configurations that could lead to interface failure by shear is numerous. Interface failure occurs when the shear stress exceeds the ultimate shear strength on a single bolt. The force at shear failure of an individual bolt is given by equation 5.7:

$$
\begin{equation*}
F=A S_{\text {shear }} \tag{5.7}
\end{equation*}
$$

## Interface Loading

Five interfaces were used in the library of modules. The minimum external force for joint separation, thread stripping and shear failure for each of these interfaces is presented in Table 5.1 (see Appendix A for calculations).

Table 5.1: Minimum Loads for Interface Failure

| Interface Type | Recommended <br> Assembly <br> Torque (Nm) | Total Joint <br> Separation <br> Force (N) | Total Thread <br> Stripping Force <br> (N) | Maximum <br> Shear Force per <br> Bolt (N) |
| :--- | :--- | :--- | :---: | :---: |
| One | 39.76 | 285352 | 293144 | 38000 |
| Two A \& B | 16.38 | 153024 | 183217 | 21375 |
| Three | 16.38 | 153024 | 183217 | 21375 |
| Four | 62.64 | 156868 | 320536 | 40448 |
| Five | 31.62 | 104672 | 256429 | 25886 |

### 5.5 MRM Motion Modules (Modular Axes)

### 5.5.1 Modular Degrees of Freedom

Machining DOF was modularized according to the adopted design approach. The design of the modular kinematic chain was achieved by the following steps:
(i) determine the maximum number of DOF per operation,
(ii) allocate modular DOF to cutting tool,
(iii) allocate modular DOF to the work table/ work clamping system,
(iv) relate allocated DOF to an absolute coordinate system on the work table/ work clamping system.


Figure 5.3: Cartesian Reference Coordinate Systems
a. Right hand coordinate system
b. Fixture of an absolute coordinate system to the work table (Red: X-axis, Green: Y-axis, Blue: Z-axis)

The prototype library of MRM modules was created with sufficient hardware to enable drilling and turning operations, with the possibility of enabling more processes with the creation of more modules. During the creation of the MRM module library it was established that a maximum of three DOF would be utilized in the turning configuration while a maximum of six DOF would be utilized in the drilling configuration. A conventional right hand Cartesian coordinate system as depicted in Figure 5.3.a was used to classify the axes that were to be created for the module library. The coordinate system is fixed to an absolute point of reference on the desired machine tool during the conceptualization phase. An absolute point of reference would be on a work holding/clamping element such as the work table depicted in Figure 5.3.b. Imposing an absolute coordinate system is necessary for classifying axes, procedural machine programming and position control.

In material removal operations it is preferable that less DOF be allocated to the machine spindle, in favour of greater stability during operation [57]. In turning operations the work piece rotates in the chuck of the cutting head, while the cutting tool traverses across the material. Based on design for machining stability all DOF were allocated to the tool post in the turning configuration. In drilling operations the tool rotates in the spindle of the cutting head, and the forces during drilling are expected to be much lower than in turning. The drilling configuration therefore possessed an equal distribution of DOF between the work table and the cutting head. Table 5.2 summarizes the allocation of modular DOF in the kinematic architecture of the desired drilling and turning configurations.

Table 5.2: Allocation of DOF for Drilling and Turning Configurations

| Degree of Freedom | Drilling | Turning |
| :---: | :---: | :---: |
| Linear X-Axis | Cutting Head | Tool Post |
| Linear Y-Axis | Work Table | Tool Post |
| Linear Z-Axis | Cutting Head | - |
| Rotary A-Axis | Cutting Head | - |
| Rotary B-Axis | Work Table | - |
| Rotary C-Axis | Work Table | Tool Post |

### 5.5.2 Generalized Kinematic Modelling

Each mechanical module possessed two active standardized mechanical interfaces (a module may possess more than two interfaces, however only two are used in any configuration). The first stage in the kinematic modelling of a MRM is the placement of localized coordinate systems at the centre of both interfaces of a module as depicted in Figure 5.4. This permits each module to be kinematically described by a Homogenous Transformation Matrix (HTM) $M_{n}$ that relates the two coordinate systems placed on either interface.


Figure 5.4: Placement of Localized Reference Frames on a Module
The Denavit -Hartenberg (D-H) method [58] of fixing a reference frame to links in a kinematic chain is applicable, however this method is not always convenient. The D-H method is best suited for application to serial robots and may result in unnecessarily complex transformation matrices when applied to different kinematic arrangements.

As an alternative to the D-H method, the following sets of guidelines were developed to fix local reference frames to modules:
(i) The placement of the local coordinate system on an interface must be such that it will coincide with the coordinate system of an adjacent interface once assembled.
(ii) The axis of actuation must be labelled according to the motion the modules provides with regard to the global reference frame. For example if a module has been identified as the global X-axis, then the two local X-axes must be parallel to the global X-axis.
(iii) No rotations of local reference frames are permitted between the two interfaces of a module unless the module is a rotary axis.
(iv) Frame 1 is always assigned to the tool holder or tool post. The kinematic chain terminates with link ,n" n " being assigned to the material clamp/ work table.

The HTM for any module is obtained from equation 5.8. The rotation component of the transformation matrix is constructed according to the X-Y-Z Euler angle convention [58], where angles $\gamma, \beta$ and $\alpha$ represent the respective rotations of the reference frame ,ie about the $\mathrm{X}, \mathrm{Y}$ and Z axes of the reference frame , $\mathrm{i}+1^{\text {ce, }}$, in the given order. The position component of the HTM represent the $\mathrm{X}, \mathrm{Y}, \mathrm{Z}$ offsets of the reference frame i with regard to frame $\mathrm{i}+1$.

$$
{ }_{i}^{i+1} M_{n}=\left[\begin{array}{cccc}
c \alpha c \beta & c \alpha s \beta s \gamma-s \alpha c \gamma & c \alpha s \beta c \gamma+s \alpha s \gamma & x  \tag{5.8}\\
s \alpha c \beta & s \alpha s \beta s \gamma+c \alpha c \gamma & s \alpha s \beta c \gamma-c \alpha s \gamma & y \\
-s \beta & c \beta s \gamma & c \beta c \gamma & z \\
0 & 0 & 0 & 1
\end{array}\right]
$$

Module transformation matrices are concatenated in order of assembly from the cutting tool to the work holder, yielding a final matrix that describes the position of the tool holding module relative to the global reference on the work holding module. The forward kinematic model for any MRM is given by equation 5.9:

$$
\begin{equation*}
{ }_{\text {Tool }}^{\text {ork }} T=M_{n} M_{n-1} M_{n-2} \ldots M_{1} \tag{5.9}
\end{equation*}
$$

### 5.5.3 Axis Drive Systems

## Drive System Alternatives

Machine axes on automated production machines are conventionally powered by:

- hydraulic drive systems,
- electric servo motors,
- pneumatic drive systems.

When selecting an appropriate actuator for MRM motion modules factors such as cost, positioning accuracy, speed, ease of control, actuator heating, required maintenance and ease of implementation were considered. Table 5.3 presents a selection matrix that weighs the relative importance of each factor; and evaluates the performance of each alternative against these factors to yield the optimal choice.

Table 5.3: Actuator Selection Matrix ( $\mathrm{R}=$ Rating (10), $\mathrm{S}=$ Weighted Score (100))

| Factor | Weighting | Hydraulic |  | Electric Servo |  | Pneumatic |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | R | S | R | S | R | S |
| Cost | 9 | 7 | 63 | 7 | 63 | 5 | 45 |
| Positioning Accuracy | 10 | 7 | 70 | 9 | 90 | 4 | 40 |
| Speed | 7 | 5 | 35 | 9 | 63 | 9 | 63 |
| Ease of Control | 7 | 5 | 35 | 8 | 56 | 5 | 35 |
| Actuator Heating | 7 | 7 | 49 | 5 | 35 | 7 | 49 |
| Required Maintenance | 7 | 5 | 35 | 8 | 56 | 7 | 49 |
| Ease of Implementation | 7 | 6 | 42 | 9 | 63 | 6 | 42 |
| Weighted Total |  | 329 |  | 426 |  | 323 |  |

According to the selection matrix, an electric servo drive system has been identified as the optimal choice. This was implemented accordingly.

## Drive System Implementation

MRM motion modules each contained a 12 volt, 100 watt permanent magnet DC motor for actuation. A HEDS-5540 incremental (optical) encoder was attached to the output shaft of each motor for speed and position measurement; this formed the servo drive system illustrated in Figure 5.5. The choice of servo drive system was based primarily on cost and for industrial implementations DC servomotors with fully integrated absolute encoders are recommended. The encoders used in this system were capable of resolutions of up to 1024 pulses per revolution with a two channel quadrature output; alternatively one channel of the encoder could be used providing a resolution of 512 pulses per revolution. Further details on the HEDS-5540 can be found in Section 6.6.


Figure 5.5: Servo Drive System Consisting of a 12 volt DC Motor and an Incremental Encoder

Figures 5.6 and 5.7 illustrate the performance characteristics of the motor with regard to torque, speed and current. When unloaded the maximum shaft speed of the motor is in the proximity of $60 \mathrm{rev} / \mathrm{min}$. During normal operation the motor was capable of a torque of 12 Nm at $20 \mathrm{rev} / \mathrm{min}$. The motor stalls on a resisting torque of 20 Nm while drawing a current of 18 amps .


Figure 5.6: Torque vs Speed Characteristic of Axis Drive Motor


Figure 5.7: Torque vs Current Characteristic of Axis Drive Motor

### 5.5.4 Linear Axes

## Actuation of Linear Axes

Linear axes in conventional machine tools are driven by power screw mechanisms coupled to servo motors [57]. The Acme lead screw or re-circulating ball screws are ideal for machine tool slide applications. These screws provide good positioning accuracy, low friction and require less drive power than other screw profiles. During the development of a library of modules an ISO Metric screw profile was selected for linear modules. Although this thread profile is less optimal than Acme or re-circulating ball screws, the cost was significantly lower. Figure 5.8 illustrates the thread profile of a conventional ISO Metric screw.


Figure 5.8: ISO Metric Screw Profile [59]
The total torque required to drive a power screw in a direction opposing an applied load $W$ ("raising the load") is calculated by equation 5.10 ; where $d_{m}$ is the mean diameter of the screw. For a single start ISO Metric thread, the lead $L$ is equal to the pitch $P$; and the angle $\alpha_{n}$ is equal to $30^{\circ}$. The coefficient of friction between the screw and the corresponding nut is $f$. The torque required to overcome collar/bearing friction is calculated by the second expression in equation 5.10, where $d_{c}$ is the collar diameter and $f_{c}$ is the coefficient of friction of the collar. The total torque required to drive a power screw in the same direction as the applied load ("lowering the load") is calculated by equation 5.11 . The linear speed $V$, power $\dot{W}$ and efficiency of a power screw are calculated by equations $5.12,5.13$ and 5.14 respectively. $N$ is the rotational speed of the screw in rev/min.

$$
\begin{gather*}
T=\frac{W d_{m}}{2} \frac{f \pi d_{m}+L \cos \alpha_{n}}{\pi d_{m} \cos \alpha_{n}-f L}+\frac{W f_{c} d_{c}}{2}  \tag{5.10}\\
T=\frac{W d_{m}}{2} \frac{f \pi d_{m}-L \cos \alpha_{n}}{\pi d_{m} \cos \alpha_{n}+f L}+\frac{W f_{c} d_{c}}{2}  \tag{5.11}\\
V=N L  \tag{5.12}\\
\dot{W}=\frac{\pi N}{30} T  \tag{5.13}\\
\text { Efficiency }=\frac{W L}{2 \pi T} \tag{5.14}
\end{gather*}
$$

## Base Module (X - Axis)

The MRM base module is a central module to all MRM configurations. This module forms the foundational structure of the machine, upon which other modules are added. The body of the module is cast iron, which provided the strength and mass necessary to support the rest of the machine structure while providing vibration damping.


Figure 5.9: MRM Base Module (X-axis)
The drive mechanism consisted of a steel ,,dove tail" slide mechanism driven by an ISO Metric M20x2.5 power screw. Steel was selected as the slide material, as it would provide the necessary strength and durability against wear. The power screw is of high tensile steel and it turns in a nut that was manufactured out of brass. The screw is supported by a deep groove ball bearing on one end and is coupled to the motor on the opposite end. Figure 5.10 illustrates the drive mechanism of the module and Table 5.4 summarizes the module"s specifications. The module code for all MRM modules is as follows "MRM-Type-Range-Moving Interface-Static Interface". Calculations for the loading specifications may be found in Appendix C. 3 and C.4. The maximum normal (vertical) load on the slide has been specified as not applicable as the prior failure of other MRM modules in all configurations is expected prior to the failure of the slide under a normal load. Engineering drawings for the base module are located in Appendix G; these drawings are a sample of the drawings that were generated during this research, the CAD drawings of other modules are located on the supplementary DVD.


Figure 5.10: Drive Mechanism of the Base Module

The MRM base module is designated as the X -axis in both drilling and turning configurations. The HTMs for this module in the drilling and turning configurations are given by equations 5.15 and 5.16 respectively; the limits are with reference to local frame , $i+1^{\text {"c. Refer to Appendix B. } 1 \text { for }}$ calculations and illustrative diagrams.

$$
\begin{align*}
{ }_{i}^{i+1} M_{\text {Base-Drilling }} & =\left[\begin{array}{lllc}
1 & 0 & 0 & x \\
0 & 1 & 0 & 2.5 \\
0 & 0 & 1 & 215 \\
0 & 0 & 0 & 1
\end{array}\right] \quad(257.5 \leq x \leq 757.5)  \tag{5.15}\\
{ }_{i}^{i+1} M_{\text {Base-Turning }} & =\left[\begin{array}{cccc}
1 & 0 & 0 & x \\
0 & 1 & 0 & 2.5 \\
0 & 0 & 1 & 19 \\
0 & 0 & 0 & 1
\end{array}\right] \quad(192.5 \leq x \leq 692.5 .5) \tag{5.16}
\end{align*}
$$

Table 5.4: Specifications of the Base Module

| Module Data | MRM Base Module |
| :--- | :--- |
| Module Code (B = Base) | MRM-B01-500-T1-T4/5 |
| Module Control Resolution (refer to section 8.8) | $4.883 \times 10^{-3} \mathrm{~mm}$ |
| Module Range | 500 mm |
| Moving Interface | Type one |
| Static Interface(s) | Type four and five |
| Max Speed | $145 \mathrm{~mm} / \mathrm{min}$ |
| Max Actuation Load | 930 N |
| Max Normal Load on Moving Interface | $\mathrm{N} / \mathrm{A}$ |

## Work Table Slide Module (Y-Axis)

The "work table slide" module supports the worktable in the drilling configuration. This module is also of a foundational nature upon which further enhancement modules may be added. The module was created with a steel framework to provide adequate strength in the module. This system was intended to provide sufficient support during drilling operations, for other machining operations such as milling, a heavier cast iron structure with a dove tail slide is recommended.


Figure 5.11: MRM Work Table Slide Module (Y-axis)

The drive mechanism of this module consisted of a steel slide driven by an ISO Metric M24x3 power screw. The screw was of high tensile steel and possesses a large diameter for added rigidity. The power screw is supported by two deep groove ball bearings at either end, and runs in a brass nut that is housed in the slide. Two 20 mm silver steel (BS-1407) rods from the support and guide mechanism for the slide as illustrated in Figure 5.12. Table 5.5 summarizes the module"s specifications. Calculations for the loading specifications may be found in Appendix C. 3 and C. 4 .


Figure 5.12: Drive mechanism of the Work Table Slide Module

Table 5.5: Specifications of the Work Table Slide Module

| Module Data | Work Table Slide Module |
| :--- | :--- |
| Module Code (WTS = Work Table Slide) | MRM - WTS01-300-T3-T5 |
| Module Control Resolution | $5.869 \times 10^{-3} \mathrm{~mm}$ |
| Module Range | 300 mm |
| Moving Interface | Type 3 |
| Static Interface(s) | Type 5 |
| Max Speed | $174 \mathrm{~mm} / \mathrm{min}$ |
| Max Actuation Load | 930 N |
| Max Normal Load on Moving Interface | 460 N |

The work table slide module is designated as the Y-axis in the drilling configuration. The HTM for this module is given by equation 5.17 ; the limits are with reference to local frame „ $1+1$ ". Refer to Appendix B. 2 for calculations and illustrative diagrams.

$$
{ }_{i}^{i+1} M_{\text {WT Slide }}=\left[\begin{array}{cccc}
1 & 0 & 0 & 155  \tag{5.17}\\
0 & 1 & 0 & y \\
0 & 0 & 1 & -111 \\
0 & 0 & 0 & 1
\end{array}\right] \quad(-150 \leq y \leq 150)
$$

## Column Module (Z- Axis)

The column module supports the cutting head in the drilling configuration. The module was created mainly out of aluminium (295-T4) for weight saving, with four silver steel rods forming the support and guide mechanism for the slide (see Figure 5.13b).

Silver steel is a $1 \%$ carbon tool steel [60] that was specifically selected for its high strength to create a stable, light weight support structure for the drill cutting head. The modules weight was limited for easy, manual assembly. The drive mechanism of the module consisted of a centrally located ISO Metric M24x3 power screw. The screw is of high tensile steel and runs in a brass nut as illustrated in Figure 5.13.c. The screw is supported by thrust bearings at the top and bottom ends of the column. Table 5.6 summarizes the module"s specifications.


Figure 5.13 MRM Column Module (Z-axis)
a. Column Module - Front view
b. Column Module - Displaying support structure
c. Column Module - Displaying drive mechanism

Table 5.6: Specifications of the Column Module

| Module Data | Column Module |
| :--- | :--- |
| Module Code (C=Column) | MRM-C01-562-T2A/2B-T1 |
| Module Control Resolution | $5.869 \times 10^{-3} \mathrm{~mm}$ |
| Module Range | 600 mm |
| Moving Interfaces | Type Two A and B |
| Static Interface | Type One |
| Max Speed | $174 \mathrm{~mm} / \mathrm{min}$ |
| Max Actuation Load | 2952 N |
| Max Normal Load on Moving Interface | 300 N |

The column module is designated as the Z-axis in the drilling configuration. The HTM for this module is given by equation 5.18 ; the limits are with reference to local frame „ $\mathrm{i}+1^{\text {"c. Refer to }}$ Appendix B. 3 for calculations and illustrative diagrams. Calculations for the loading specifications may be found in Appendix C. 3 and C.4.

$$
{ }_{i} M_{\text {Column }}=\left[\begin{array}{cccc}
1 & 0 & 0 & -54.5  \tag{5.18}\\
0 & 1 & 0 & 0 \\
0 & 0 & 1 & Z \\
0 & 0 & 0 & 1
\end{array}\right] \quad(85 \leq z \leq 647)
$$

Cross Slide Module (Y-Axis and C-Axis)


Figure 5.14: Cross Slide Module and Tool Post (Y and C axes)
a. MRM Cross Slide Module - Rear view
b. MRM Cross Slide Module - Illustrative side view

The cross slide module contains a tool post and is responsible for feeding the tool into a rotating work piece in the turning configuration. The module was a COTS unit of hardware that was retrofitted with a servo drive motor. The body of the module is steel and the servo drive system is supported by an aluminium bracket. The steel body is ideal for vibration damping and the support of high machining forces. The drive mechanism consisted of the tool post being driven by a $12 \times 2$ metric trapezoidal power screw.


Figure 5.15: MRM Automated Work Clamp

The cross slide module possessed two additional features. The first feature was the ability of the module to be transformed into an automated device for work clamping. This display of reconfigurability is achieved by the design of the tool post to be modular and removable from the base of the module. Figure 5.15 illustrates the reconfigured module with the tool post removed.

The second feature was the ability of the module to rotate about its axis. This effectively created a rotational axis (C-axis). The rotary indexing feature of this module is manually manipulated; the rotation is illustrated in Figure 5.16.b. Table 5.7 summarizes the module"s specifications. Calculations for the loading specifications may be found in Appendix C. 3 and C.4.

## a.


b.


Figure 5.16: Cross Slide Module Displaying Additional Rotary Axis
a. Cross slide module at home position
b. Cross slide module orientated at $45^{\circ}$ to the home position

Table 5.7: Specifications of the Cross Slide Module

| Module Data | Cross Slide Module |
| :--- | :--- |
| Module Code (CS= Cross Slide) | MRM-CS01-115-T0-T1 |
| Module Control Resolution | $3.906 \times 10^{-3} \mathrm{~mm}$ |
| Module Range (Y axis) | 115 mm |
| Module Range (C axis) | $360^{\circ}$ |
| Static Interface | Type One |
| Max Speed | $116 \mathrm{~mm} / \mathrm{min}$ |
| Max Actuation Load | 250 N |
| Max Load on Tool (vertical and horizontal) | 2500 N |

This module provides both the Y and C axes in the turning configuration. The HTM for this module is given by equation 5.19 ; the limits are with reference to local frame, $\mathfrak{i}+1$.". Refer to Appendix B. 4 for calculations and illustrative diagrams.

$$
{ }_{i}^{i+1} M_{\text {Cross Slide }}=\left[\begin{array}{cccc}
c \alpha & -s \alpha & 0 & 0  \tag{5.19}\\
s \alpha & c \alpha & 0 & y \\
0 & 0 & 1 & 168 \\
0 & 0 & 0 & 1
\end{array}\right] \quad\left(-90 \leq y \leq 25 ;-360^{\circ} \leq \alpha \leq 360^{\circ}\right)
$$

## Idealized Performance of Linear Axes

Performance characteristics of the servo drive system implemented in the MRM axes were presented in Section 5.5.3. By manipulating the performance characteristics of the drive motor a corresponding idealized performance characteristic may be developed for the performance of a module under the action of a resisting load. Rearranging equation 5.10 yields the force that a power screw mechanism is capable of acting against for a given input torque:

$$
\begin{equation*}
W=T\left[\frac{d_{m}}{2} \frac{f \pi d_{m}+L \cos \alpha_{n}}{\pi d_{m} \cos \alpha_{n}-f L}+\frac{f_{c} d_{c}}{2}\right]^{-1} \tag{5.20}
\end{equation*}
$$

Equation 5.20 and the motor performance data have been used to generate Figures 5.17 and 5.18. These figures represent the ideal performance of the linear motion modules with regard to actuation force and speed (Figure 5.17) and the electric current requirements of the modules under corresponding loads (Figure 5.18). These figures have been generated purely from the actuation characteristics of the associated motor and equation 5.20; the forces presented do not necessarily represent the maximum forces sustainable by the modules. Refer to Appendix C. 1 for calculations.


Figure 5.17: Graph of Actuation Force vs Speed for Linear Axes


Figure 5.18: Graph of Actuation Force vs Current for Linear Axes

### 5.5.5 Rotary Axes

## Cutting Head Rotary Module (A-Axis)

The "cutting head rotary" module was designed for use in the drilling configuration. The module is an optional rotary axis that is capable of orientating the cutting head in different planes. The frame of the module was created entirely out of aluminium to minimize weight, while providing sufficient strength during drilling. Weight minimization was necessary due to limitations imposed by the actuation torque that was available from module motors.


Figure 5.19: The Cutting Head Rotary Module (A-axis)
a. Cutting Head Rotary Module - Front view
b. Cutting Head Rotary Module - Illustrative isometric view

The actuation mechanism of this module consisted of a stepped interface plate rotating in a groove on the front face of the module. The groove provides support for the interface during operation and ensures smooth rotation. The interface plate is directly coupled to the drive motor as illustrated in Figure 5.20.b.


Figure 5.20: Drive Mechanism of the Cutting Head Rotary Module
a. Grooved front face
b. Direct coupling of motor to interface

The DC motor that has been implemented in all axes contains an internal worm gearbox that amplifies the output torque from the armature shaft. The second benefit derived from the internal gearbox is that it behaves as a braking mechanism. The gear component of the box cannot be rotated by an applied load and can only be rotated by the worm mechanism attached to the armature shaft. The direct coupled solution provided a basic, cost effective solution, however for industrial implementations it is recommended that the interface be coupled to the motor via a secondary gearbox. Table 5.8 summarizes the specifications of this module. Calculations for the loading specifications may be found in Appendix C. 3 and C.4.

Table 5.8: Specifications of the Cutting Head Rotary Module

| Module Data | Cutting Head Rotary Module |
| :--- | :--- |
| Module Code (CHR = Cutting Head Rotary) | MRM-CHR01-360-T2A-T2B |
| Module Control Resolution | $0.703^{\circ}$ |
| Module Range | $\pm 360^{\circ}$ |
| Moving Interfaces | Type Two A |
| Static Interface | Type Two B |
| Max Speed | 70 rev/min |
| Stall Torque | $20 \mathrm{~N} . \mathrm{m}$ |
| Max Allowable Torque On Moving Interface | $12 \mathrm{~N} . \mathrm{m}$ |
| Max Normal Load on Moving Interface | 250 N |

This module has been designated as the A -axis, as it provides rotary motion about the X -axis in the drilling configuration. The HTM for this module is given by equation 5.21 ; the limits are with reference to local frame „ $1+1^{\prime \prime}$. Refer to Appendix B. 5 for calculations and illustrative diagrams.

$$
{ }_{i}^{i+1} M_{\text {CH Rotary }}=\left[\begin{array}{cccc}
1 & 0 & 0 & -138  \tag{5.21}\\
0 & c \gamma & -s \gamma & 0 \\
0 & s \gamma & c \gamma & 0 \\
0 & 0 & 0 & 1
\end{array}\right] \quad\left(-360^{\circ} \leq \gamma \leq 360^{\circ}\right)
$$

Tilt Table Module (B-Axis)


Figure 5.21: The Tilt Table Module (B-axis)

The tilt table module illustrated in Figure 5.21 was designed for use in the drilling configuration. The module is capable of having a work table attached to its upper interface and provides an optional rotary axis. The table tilts the work part relative to the cutting tool to provide different planes of machining. The module was designed entirely out of aluminium, to create a strong light weight mechanism that is easy to reconfigure and easily moved by the drive motors of other modules in the kinematic chain.


Figure 5.22: Drive Mechanism of the Tilt Table Module
The drive mechanism of the module consisted of the upper interface plate being moved by a leaver arm as illustrated in Figure 5.22. The lever arm is coupled to a drive shaft, which is in turn coupled to the motor. The drive shaft fits into the lever arm and the connection is secured by a shear pin. The shaft is also supported at both ends by two deep groove ball bearings. The rotary motion of the upper interface is guided by two stepped arches at either end of the plate; these arches also support the load placed on this interface, protecting the drive shaft from bending. The DC motor that has been implemented in this axis contained an internal worm gearbox (as in all the other axes). The internal gearbox behaves as a braking mechanism, permitting motion to occur only by the actuation of motor. It should be noted that this mechanism is a direct drive mechanism as there is no torque conversion between the motor and the interface tilting mechanism. Table 5.9 summarizes the specifications of this module. Calculations for the loading specifications may be found in Appendix C. 3 and C.4.

Table 5.9: Specifications of the Tilt Table Module

| Module Data | Tilt Table Module |
| :--- | :--- |
| Module Code (TT = Tilt Table) | MRM-TT01-90-T3-T3 |
| Module Control Resolution | $0.703^{\circ}$ |
| Module Range | $\pm 90^{\circ}$ to the horizontal |
| Moving Interface | Type Three |
| Static Interface | Type Three |
| Maximum Speed | $70 \mathrm{rev} / \mathrm{min}$ |
| Stall Torque | $20 \mathrm{~N} . \mathrm{m}$ |
| Maximum Allowable Torque On Moving Interface | $12 \mathrm{~N} . \mathrm{m}$ |
| Max Normal Load on Moving Interface | 240 N |

The module is designed for attachment to the work table slide module and provides rotary motion about the Y -axis in the drilling configuration; it has therefore been designated as the B -axis of that system. The HTM for this module is given by equation 5.22 ; the limits are with reference to local frame , $\mathfrak{i}+1^{\text {ce. }}$. Refer to Appendix B. 6 for calculations and illustrative diagrams.

$$
{ }_{i}^{i+1} M_{\text {Tilt Table }}=\left[\begin{array}{cccc}
c \beta & 0 & s \beta & -50 s \beta  \tag{5.22}\\
0 & 1 & 0 & 0 \\
-s \beta & 0 & c \beta & -50 c \beta-95 \\
0 & 0 & 0 & 1
\end{array}\right] \quad\left(-45^{\circ} \leq \beta \leq 45^{\circ}\right)
$$

## Rotary Table Module (C-Axis)



Figure 5.23: Rotary Table Module (C-axis)
The rotary table module illustrated in Figure 5.23 was designed for use in the drilling configuration. The module is capable of having a work table or other modules attached to its upper interface. This module was also designed entirely out of aluminium, to create a strong, light weight mechanism that is easy to reconfigure and easily moved by the drive mechanisms of other modules.


Figure 5.24: Rotary Table Drive Mechanism

The drive mechanism consisted of the upper interface being rotated via a reduction worm gearbox. This interface is supported by a thrust bearing at its base. The worm gearbox is coupled to the drive motor by a 12 mm steel shaft. The worm gearbox in the module and the internal worm gearbox belonging to the motor both prevent the mechanism from being moved by the load, permitting motion to occur only under the control of the motor. Table 5.10 summarizes the specifications of this module. Calculations for the loading specifications may be found in Appendix C. 3 and C.4.

Table 5.10: Specifications of the Rotary Table Module

| Module Data | Rotary Table Module |
| :--- | :--- |
| Module Code (RT = Rotary Table) | MRM-RT01-360-T3-T3 |
| Module Control Resolution | $0.0125^{\circ}$ |
| Module Range | $\pm 360^{\circ}$ |
| Moving Interfaces | Type Three |
| Static Interface | Type Three |
| Maximum Speed | 1.25 rev/min |
| Stall Torque | N/A - Prior failure of gearbox |
| Maximum Allowable Torque on Moving Interface | $20 \mathrm{~N} . \mathrm{m}$ |
| Max Normal Load on Moving Interface | 250 N |

The module provides rotary motion about the Z-axis in the drilling configuration; it has therefore been designated as the C -axis of that system. The HTM for this module is given by equation 5.23 ; the limits are with reference to local frame , ,i+1". Refer to Appendix B. 7 for calculations and illustrative diagrams

$$
{ }_{i}^{i+1} M_{\text {Rot Table }}=\left[\begin{array}{cccc}
c \alpha & -s \alpha & 0 & 0  \tag{5.23}\\
s \alpha & c \alpha & 0 & 0 \\
0 & 0 & 1 & -152 \\
0 & 0 & 0 & 1
\end{array}\right] \quad\left(-180^{\circ} \leq \alpha \leq 180\right)
$$

## Idealized Performance of Rotary Axes

The cutting head rotary module and the tilt table module both possessed direct drive mechanisms with no torque conversion between the motor and the driven interface. Ideally (no friction) these modules should display the torque and speed characteristics of the drive motor due to the direct coupling. On the contrary the rotary table module possessed a mechanism where the rotating interface was driven via a secondary worm gearbox. Equations 5.24 and 5.25 relate the speed and torque of the input shaft to the output shaft of a single stage reduction gearbox.

$$
\begin{align*}
\omega_{\text {output }} & =\omega_{\text {input }} \frac{N_{\text {worm }}}{N_{\text {gear }}}  \tag{5.24}\\
T_{\text {output }} & =T_{\text {input }} \frac{\omega_{\text {input }}}{\omega_{\text {output }}} \tag{5.25}
\end{align*}
$$

These equations have been used in conjunction with the motor performance data to generate Table 5.11. This table displays the performance characteristic of actuation torque versus speed for the MRM rotary modules.

These values have been generated purely from the actuation characteristics of the associated motor and the relationships presented in equations 5.24 and 5.25 . The torques presented do not necessarily represent the maximum loads sustainable by the modules. Refer to Appendix C. 2 for calculations.

Table 5.11: Actuation Characteristics of MRM Rotary Axes

| Actuation <br> Current <br> $(\mathbf{a m p s})$ | A-Axis <br> Speed <br> $(\mathbf{r e v} / \mathbf{m i n})$ | A-Axis <br> Torque <br> $(\mathbf{N} . \mathrm{m})$ | B-Axis <br> Speed <br> $(\mathbf{r e v} / \mathbf{m i n})$ | B-Axis <br> Torque <br> $(\mathbf{N} . m)$ | C-Axis <br> Speed <br> $(\mathbf{r e v} / \mathrm{min})$ | C-Axis <br> Torque <br> $(\mathbf{N} . \mathbf{m})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3.4 | 58 | 1 | 58 | 1 | 1.036 | 56 |
| 7.5 | 40 | 5 | 40 | 5 | 0.714 | 280 |
| 12 | 20 | 12 | 20 | 12 | 0.357 | 672 |
| 18 | Stall | 20 | Stall | 20 | Stall | 1120 |

### 5.6 MRM Process Modules (Modular Cutting Heads)

Drilling Head


Figure 5.25: MRM Drilling Module

The MRM drilling module illustrated in Figure 5.25 forms the cutting head in the MRM drilling configuration. The module consists of a motor and spindle unit fitted into an aluminium housing. The module is specified to operate at 12 volts and provides 80 watts of power at the spindle. The motor and planetary gearbox arrangement, illustrated in Figure 5.26, is specified to provide a maximum spindle speed of $580 \mathrm{rev} / \mathrm{min}$. The internal planetary gearbox possesses a back-torque limiter (slip clutch) that connects the gearbox to spindle. The slip clutch prevents the motor from stalling which could potentially damage the motor. Table 5.12 summarizes the specifications of this module.

Table 5.12: Specifications for the Drilling Module

| Module Data | Drilling Module |
| :--- | :--- |
| Module Code (DH = Drilling Head) | MRM-DH01-12-T0-T2A |
| Drill Range | $0.5 \mathrm{~mm}-12 \mathrm{~mm}$ |
| Static Interface | Type Two A |
| Power | 80 watts |
| Maximum Speed | 580 rev/min (Unloaded) |
| Torque Settings | 16 |



Figure 5.26: MRM Drilling Module Internal Mechanism

The HTM for the kinematic description of this module is given by equation 5.26. Refer to Appendix B. 8 for calculations and illustrative diagrams.

$$
{ }_{i}^{i+1} M_{\text {Drill Head }}=\left[\begin{array}{cccc}
1 & 0 & 0 & -75  \tag{5.26}\\
0 & 1 & 0 & 0 \\
0 & 0 & 1 & -81.5 \\
0 & 0 & 0 & 1
\end{array}\right]
$$

## Turning Head



Figure 5.27: MRM Turning Module
a. Turning Module - Displaying chuck
b. Turning Module - Displaying belt drive mechanism
c. Turning Module - Displaying belt tensioning mechanism

The MRM module illustrated in Figure 5.27 is the cutting head in the turning configuration. The modular cutting head consists of a head stock driven by a single phase 220 volt, 0.55 kW AC induction motor. The motor drives the spindle/chuck mechanism via a vee-belt drive system as illustrated in Figure 5.27.b. The motor provides a maximum output speed of $1400 \mathrm{rev} / \mathrm{min}$ which is manipulated by the belt drive mechanism to provide three speed settings. The speed and torque characteristics of this module are summarized in Table 5.13. The belt position is adjusted by the manipulation of a slide tensioning mechanism illustrated in Figure 5.27.c. The slide tensioning mechanism consists of four bolts that when loosened permit the motor mounting plate to slide allowing the belt to be tensioned or slackened. The headstock mechanism consists of a 3-Jaw chuck, with a maximum diametric capacity of 120 mm . Table 5.14 summarizes the specifications of this module.

Table 5.13: Actuation Characteristics of Turning Module

| Motor Power <br> (W) | Motor Speed <br> $($ rev/min) | Motor <br> Torque <br> $(\mathbf{N} . \mathbf{m})$ | Reduction <br> Ratio | Spindle <br> Speed <br> $(\mathbf{r e v} / \mathrm{min})$ | Spindle <br> Torque <br> $(\mathbf{N} . \mathrm{m})$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 550 | 1400 | 3.75 | $30: 133$ | 315.79 | 16.63 |
| 550 | 1400 | 3.75 | $50: 111$ | 630.63 | 8.33 |
| 550 | 1400 | 3.75 | $67: 89$ | 1053.93 | 4.98 |

Table 5.14: Specifications of the Turning Module

| Module Data | Tilt Table Module |
| :--- | :--- |
| Module Code (TH = Turning Head) | MRM-TH01-120-T0-T4 |
| Swing Over Bed | 420 mm diameter |
| Spindle Hole | 24 mm |
| Chuck Capacity | 120 mm |
| Static Interface | Type Four |
| Power | 0.55 kW |
| Maximum Actuation Speed | $1054 \mathrm{rev} / \mathrm{min}$ |
| Maximum Actuation Torque | $16.63 \mathrm{~N} . \mathrm{m}$ |

The HTM for the kinematic description of this module is given by equation 5.27. Refer to Appendix B. 9 for calculations and illustrative diagrams.

$$
{ }_{i}^{i+1} M_{\text {Turning Head }}=\left[\begin{array}{cccc}
1 & 0 & 0 & -192.5  \tag{5.27}\\
0 & 1 & 0 & 0 \\
0 & 0 & 1 & -212.5 \\
0 & 0 & 0 & 1
\end{array}\right]
$$

### 5.7 MRM Accessory Modules

## Manufactured Accessory Modules

Two accessory modules were created for the MRM platform. The first module is the modular work table illustrated in Figure 5.28.a. The work table was constructed completely out of aluminium to create a light weight module that is comfortably moved by the drive motors of other modules.
a.

b.


Figure 5.28: Manufactured Accessory Modules
a. Modular Worktable
b. Modular Range Extension Arm

The work table was designed to be modular to enable it to be transferred between other automated modules. The work table can be transferred between the work table slide module, the tilt table module and the rotary table module. The second advantage of a modular work table is that it may be interchanged with other work tables. Manufacturers may therefore implement customized worktables that contain features and fixturing devices that are optimized in their functionality as compared to generic work clamps. This possesses the potential to shorten the work setup time on a machine. Table 5.15 summarizes the specifications of this module.

Table 5.15: Specifications of the Work Table Module

| Module Data | Tilt Table Module |
| :--- | :--- |
| Module Code (WT = Work Table) | MRM-WT01-160-T0-T3 |
| Dimensions | $160 \mathrm{~mm} \times 160 \mathrm{~mm}$ (Table Area) |
| Static Interface | Type Three |

The kinematic description of this module is given by equation 5.28. Refer to Appendix B. 10 for calculations and illustrative diagrams.

$$
{ }_{i}^{i+1} M_{\text {Work Table }}=\left[\begin{array}{cccc}
1 & 0 & 0 & 0  \tag{5.28}\\
0 & 1 & 0 & 0 \\
0 & 0 & 1 & -24.5 \\
0 & 0 & 0 & 1
\end{array}\right]
$$

The second accessory module that was created was the range extension arm illustrated in Figure 5.28.b. The arm was created for incorporation into the drilling configuration, partially to compensate for the length the base module (discussed later) and increases the extent of movement of the drilling head by 350 mm . Modular extensions to a machines range should be used with caution as the added physical length amplifies torques within the machine structure. Increased torques can lead to deflections in the machine structure, thereby increasing the first and second order errors in the geometric positioning of the tool. Table 5.16 summarizes the specifications of this module. The kinematic description of this module is given by equation 5.29 . Refer to Appendix B. 11 for calculations and illustrative diagrams.

Table 5.16: Specifications for Modular Range Extension Arm

| Module Data | Tilt Table Module |
| :--- | :--- |
| Module Code (REA=Range Ext Arm) | MRM-REA-370-T0-T2A |
| Dimensions | 370 mm extension |
| Static Interface | Type Two A |

$$
{ }_{i}^{i+1} M_{\text {Extension Arm }}=\left[\begin{array}{cccc}
1 & 0 & 0 & -370  \tag{5.29}\\
0 & 1 & 0 & 0 \\
0 & 0 & 1 & 0 \\
0 & 0 & 0 & 1
\end{array}\right]
$$

## COTS Accessory Modules



Figure 5.29: COTS Accessory Modules
a. A Modular Steady Rest
b. A Modular Tailstock

Two COTS accessories were incorporated into MRM platforms. The first module is the Steady Rest depicted in Figure 5.29.a. The second COTS module that was incorporated into the MRM is the Tailstock illustrated in Figure 5.29.b. These accessories, which may be considered as commercially available modules, were used in the turning configuration for the support of long work pieces during machining. The modules aid in minimizing the eccentricity of rotating shafts/ billets that would otherwise result in tool breakage or geometric errors on the machined product. The incorporation of COTS hardware into the MRM platform highlights the potential for the extension of the accessory category in the MRM library.

To facilitate the integration of COTS accessories due consideration must be undertaken to ensure that interfacing elements comply with current standards in the machine building industry. The modular Steady Rest and Tailstock both interface with the MRM base module which possesses a standardized ,,dove taile slide on which both accessory modules connect.

### 5.8 Mechanical Assembly and Reconfiguration

### 5.8.1 Assembling a Kinematically Viable Machine Tool (An Example)



Figure 5.30: An Example Part
The methodology employed in the creation of kinematically viable machine tools was discussed in Section 3.4.2. The first stage in the methodology is to obtain a task matrix from mechanical drawings of the part/parts the machine will be required to produce. The task matrix is obtained by placing reference frames along key points of the tools required trajectory. The first reference frame is placed at the start of the tools trajectory as illustrated in the example of Figure 5.30. The task matrix for this example is given by equations 5.31 (HTM used directly).

$$
\begin{gather*}
{ }_{4}^{1} T={ }_{2}^{1} T_{3}^{2} T_{4}^{3} T=\left[\begin{array}{llll}
1 & 0 & 0 & 0 \\
0 & 1 & 0 & y_{1} \\
0 & 0 & 1 & z_{1} \\
0 & 0 & 0 & 1
\end{array}\right]\left[\begin{array}{cccc}
c \beta & 0 & s \beta & x_{3} c \beta+x_{2} \\
0 & 1 & 0 & 0 \\
-s \beta & 0 & c \beta & -x_{3} s \beta+z_{2} \\
0 & 0 & 0 & 1
\end{array}\right]\left[\begin{array}{cccc}
1 & 0 & 0 & 0 \\
0 & 1 & 0 & y_{2} \\
0 & 0 & 1 & z_{3} \\
0 & 0 & 0 & 1
\end{array}\right]  \tag{5.30}\\
{ }_{4}^{1} T=\left[\begin{array}{cccc}
c \beta & 0 & s \beta & z_{3} s \beta+x_{3} c \beta+x_{2} \\
0 & 1 & 0 & y_{2}+y_{1} \\
-s \beta & 0 & c \beta & z_{3} c \beta-x_{3} s \beta+z_{2}+z_{1} \\
0 & 0 & 0 & 1
\end{array}\right] \tag{5.31}
\end{gather*}
$$

The symbols $x, y, z$ represent the respective translations with regard to the various local reference frames and $\beta$ represents a rotation about a local $y$ axis. The $z$ symbol appears in the homogenous transformation matrices, representing the motion of a drill in and out of the respective holes (not indicated on diagram). Once a task matrix has been obtained, essential motions are identified; these essential motions are represented in a function structure graph as illustrated in Figure 5.31. The function structure graph provides a template for the allocation of modules to a machine tool. This structure usually consists of two branches stemming from the machine base; these branches represent the allocation of DOF to the cutting tool and the work clamping/support system.

The methodology outlined above yielded the MRM configuration illustrated in Figure 5.32. The machine consisted of the base module forming the X -axis, the work table slide module forming the Y -axis, the column forming the Z -axis and the tilt table module forming the B -axis. The kinematic description of this configuration is achieved by mutiplying the HTM"s of individual modules, from tool holding module to work holding module. The HTM for this MRM configuration is given by equation 5.32.


Figure 5.31: Identification of Necessary Motions and Allocation of Modules to Machine Tool


Figure 5.32: A Kinematically Viable Machine Tool for the Production of the Example Part
A comparison between the task matrix (eqation 5.31) and the machine transformation matrix (equation 5.32) shows a driect match in the rotational component of the HTM. A comparison between the translation components does not yield a direct match. However the variables $x, y$ and $z$ and $\beta$ are present in corresponding terms indicating that the machine is kinematically viable in terms of the types of motions it is able to provide to the cutting head.

$$
\underset{\text { Worktable }}{\text { Drill }} T=\left[\begin{array}{cccc}
c \beta & 0 & s \beta & -344.5 c \beta-27.5 s \beta+z s \beta+x c \beta  \tag{5.32}\\
0 & 1 & 0 & 2.5+y \\
-s \beta & 0 & c \beta & 344.5 s \beta-119.5-27.5 c \beta+z c \beta-x s \beta \\
0 & 0 & 0 & 1
\end{array}\right]
$$

It should be noted that this method does not yield unique MRM configurations. Depending on the set up of local reference frames when generating a task matrix, different MRM configurations may be generated that are also kinematically viable. An example of this is the MRM configuration illustrated in Figure 5.33, which replaces the tilt table modue with the cutting head rotary module to enable drilling on the inclinded surface of the example part. The HTM for this alternate MRM configuration is:

$$
\underset{\text { Worktable }}{\text { Drill }} T=\left[\begin{array}{cccc}
1 & 0 & 0 & -482.5+x  \tag{5.33}\\
0 & c \gamma & -s \gamma & 2.5+81.5 s \gamma+y \\
0 & s \gamma & c \gamma & 79.5-81.5 c \gamma+z \\
0 & 0 & 0 & 1
\end{array}\right]
$$

When multiple kineamtically viable configurations are possible, the configuration that provides the most appropriate mechanical properties, axis ranges, speeds and torques is selected.


Figure 5.33: A Second Kinematically Viable Machine Tool for the Production of the Example Part

### 5.8.2 Machine Reconfiguration



Figure 5.34: Reconfiguration of Machining DOF by Addition of Modules
a. Three DOF configuration ( $\mathrm{X}, \mathrm{Y}$ and Z axes)
b. Four DOF configuration ( $\mathrm{X}, \mathrm{Y}, \mathrm{Z}$ and C axes)
c. Six DOF configuration (X,Y,Z, A, B and C axes)

MRM platforms possess the ability to provide a change in processing operations and DOF by the addition or removal of modules from the machine base. The ability to vary a machine"s DOF implies that a manufacturing enterprise may begin operation with machines possessing a minimum level of functionality. As the enterprise becomes more profitable and the product portfolio evolves, the machines in the system may be enhanced by the integration of additional DOF into a base platform. This capability is illustrated in Figure 5.34, where a three DOF machine is upgraded to a four and ultimately a six DOF system (additional modules highlighted in yellow circles).

In a manufacturing operation a change of parts/ part families may occur. Depending on the geometric features of the new part family it may be necessary that different processing operations may be required while previous processes capabilities of the system become irrelevant. In this instance the cutting head of the MRM may be changed to enable a new process, as illustrated in the concept of Figure 4.4. If the kinematic structure of the machine tool does not support a change in cutting heads the MRM structure may be decomposed into its modular elements. The elements may then be used in the construction of new types of machinery. This more extensive form of reconfiguration is illustrated in Figure 5.35 where the drilling machine structure is decomposed and a turning structure is assembled using modules from the decomposed drill and other modules from the MRM library.


Figure 5.35: Decomposition of Drilling Structure and Assembly of Turning Structure

### 5.8.3 Module Combinations

MRM modules may be combined in multiple configurations to yield different types of machinery with varying kinematic capabilities. For a specific processing function, the number of unique kinematic combinations, achievable is calculated by equation 5.34 where the number „one" in the formula represents the basic platform; $n$ represents the total number of enhancement modules that may be added to the platform and $r$ represents the number of enhancement modules selected at a time.

$$
\begin{equation*}
N=1+\sum_{r=1}^{n} \frac{n!}{r!(n-r)!} \tag{5.34}
\end{equation*}
$$

The basic configuration of the MRM drilling platform consisted of $\mathrm{X}, \mathrm{Y}$ and Z axes. This platform could be enhanced with three rotary axes to increase its DOF. Note that the range extension arm was not considered as an enhancement as it was essential to all drilling configurations. The total number of unique kinematic configurations for the drilling process is calculated as follows:

$$
N=1+\frac{3!}{1!(3-1)!}+\frac{3!}{2!(3-2)!}+\frac{3!}{3!(3-3)!}=1+3+3+1=8
$$

The MRM drilling platform possessed eight unique configurations ( $1 \times 3 \mathrm{DOF}, 3 \times 4 \mathrm{DOF}, 3 \times 5$ DOF and $1 \times 6 \mathrm{DOF}$ ). The turning platform, under the current library of modules was only enabled to display one configuration. The current library of eleven modules was therefore able to yield nine kinematically and functionally different machine configurations. The details of these nine configurations are given in Appendix D.

### 5.9 Cutting Conditions

### 5.9.1 Cutting Conditions in Turning



Figure 5.36: A Typical Turning Operation [61]
In machining operations NC programmers are required to select cutting conditions when developing part programs. The common conditions that an operator would be required to select are the depth of cut $d(\mathrm{~mm})$, the linear feed rate of the tool $f_{r}(\mathrm{~mm} / \mathrm{min})$ and the rotational speed of the machine spindle $N(\mathrm{rev} / \mathrm{min})$. The direction of the tool feed and the depth of cut for a typical turning operation are illustrated in Figure 5.36. The appropriate selection of cutting conditions is necessary to optimize the time required for machining while maintaining the surface integrity and geometric tolerances of machined parts. For a turning operation, the time $T_{m}(\mathrm{~min})$ required for a linear cut of length $L(\mathrm{~mm})$ between two points on a cylindrical part is determined by equation 5.35. The total time required for a turning operation is the summation of the times required for individual linear cuts.

$$
\begin{equation*}
T_{m}=\frac{L}{f_{r}} \tag{5.35}
\end{equation*}
$$

The material removal rate $R_{M R}\left(\mathrm{~mm}^{3} / \mathrm{min}\right)$ for a turning operation is calculated by equation 5.36 , where $V$ is the tangential velocity ( $\mathrm{m} / \mathrm{s}$ ) of the surface being machined (original surface). The tangential velocity of the original surface is calculated by equation 5.37 where $D_{0}$ is the diameter $(\mathrm{m})$ of this surface as illustrated in Figure 5.36.

$$
\begin{gather*}
R_{M R}=V \cdot f \cdot d  \tag{5.36}\\
V=\pi \cdot N \cdot D_{o} \tag{5.37}
\end{gather*}
$$

### 5.9.2 Cutting Conditions in Drilling



Figure 5.37: Typical Drilling Operations [61]
a. Drilling of a through hole
b. Drilling of a blind hole

In drilling operations the depth of cut $d$, coincides with the linear tool feed direction. The depth of cut, tool feed rate and spindle speed are specified in NC programs as in turning operations. Drilling operations may be performed to achieve either through holes or blind holes as illustrated in Figure 5.37. Based on the programmed feed rate $f_{r}(\mathrm{~mm} / \mathrm{min})$ and the thickness of the work material $t(\mathrm{~mm})$, the time required to machine a through hole is calculated by equation 5.38.

$$
\begin{equation*}
T_{m}=\frac{t+A}{f_{r}} \tag{5.38}
\end{equation*}
$$

The approach allowance $A(\mathrm{~mm})$, accounts for the additional length of the drill before it terminates at a point. The approach allowance is calculated by equation 5.39 , where $D$ is the drill diameter ( mm ) and $\theta$ is the drill point angle in degrees.

$$
\begin{equation*}
A=0.5 D \tan \left(90-\frac{\theta}{2}\right) \tag{5.39}
\end{equation*}
$$

The time required for the drilling of a blind hole is calculated by equation 5.40, and the material removal rate $R_{M R}\left(\mathrm{~mm}^{3} / \mathrm{min}\right)$ for both through and blind hole applications is calculated by equation 5.41.

$$
\begin{gather*}
T_{m}=\frac{d}{f_{r}}  \tag{5.40}\\
R_{M R}=\frac{\pi D^{2} f_{r}}{4} \tag{5.41}
\end{gather*}
$$

### 5.10 Forces and Torques in Machining

### 5.10.1 Forces in Turning

Forces in machining are largely determined by empirical relationships that are based on experiments. In turning operations the resultant force during the cutting process can be resolved into three elementary components:

- $P_{x}$ : the force acting against the direction of the tool feed
- $P_{y}$ : the force acting perpendicular to the tool feed in the horizontal plane
- $P_{z}$ : the force in the vertical plane simultaneously acting perpendicular to $\mathrm{P}_{\mathrm{x}}$ and $\mathrm{P}_{z}$

Basu and Pal [62] present the empirical relationship of equation 5.42 for determining $P_{z}$; where $C_{p}$ is a coefficient based on the work material, $d$ is the depth of cut ( mm ), $S$ is the tool feed ( $\mathrm{mm} / \mathrm{rev}$ ) and $K$ is a coefficient based on the tool geometry, coolant and work material. The coefficients $x$ and $y$ are based on the type of material being cut.

$$
\begin{equation*}
P_{z}=C_{p} \cdot d^{x} \cdot S^{y} \cdot K \tag{5.42}
\end{equation*}
$$

The coefficients are determined from tables that have been compiled from extensive experimental testing. The forces $P_{y}$ and $P_{x}$ are also empirically related to $P_{z}$ depending on the type of material being machined and other physical parameters of the cutting process:

$$
\begin{equation*}
\frac{P_{x}}{P_{z}} \approx 0.3 \text { to } 0.2 \quad \frac{P_{y}}{P_{z}} \approx 0.2 \text { to } 0.1 \tag{5.43}
\end{equation*}
$$

### 5.10.2 Forces and Torques in Drilling

Forces in drilling are determined empirically as in turning operations. Basu and Pal [62] present the empirical relationship of equation 5.44 , for determining the thrust force on a drilling tool; where $P$ is the thrust force ( kg ), $K$ is a constant that depends on the work material and geometric parameters of a drill, $S$ is the tool feed ( $\mathrm{mm} / \mathrm{rev}$ ) and $m$ is a constant depending on the material being machined. The constants are determined from tables developed from experiments.

$$
\begin{equation*}
P=K \cdot D \cdot S^{m} \tag{5.44}
\end{equation*}
$$

The turning moment on a drill is given by equation 5.45 ; where $M_{t}$ is the turning moment (kg.mm), and $K_{t}, x$ and $y$ are empirical constants.

$$
\begin{equation*}
M_{t}=K_{t} \cdot D^{x} S^{y} \tag{5.45}
\end{equation*}
$$

Tables for determining the cutting coefficients and constants are widely available for steel and other common metals. During this research such tables were not located for plastics and waxes. Drilling configurations were therefore designed around a drilling thrust force of 50 N , while turning configurations were designed on $P_{x}=P_{y}=P_{z}=50 \mathrm{~N}$.

### 5.10.3 Force and Torque Propagation

The knowledge of the force and torque exerted on a cutting tool may be used to determine the force and torque propagation throughout a machining structure. The link-wise torque and force propagation is given by:

$$
\begin{align*}
& { }^{i+1} f_{i+1}={ }^{i+1}{ }_{i} R{ }^{i} f_{i}  \tag{5.46}\\
& { }^{i+1} n_{i+1}={ }^{i+1} R{ }_{i} n_{i}+{ }_{i}^{i+1} P \quad \times{ }^{i+1} f_{i+1} \tag{5.47}
\end{align*}
$$

Where $f_{i+l}$ and $n_{i+l}$ are the force and torque exerted on link $\mathrm{i}+1$ by link i . The position $(P)$ and rotation $(R)$ matrices are derived directly from the HTM"s of individual modules. For an expected cutting force the joint actuation torques and forces are obtainable. The actuation torque required by a rotary axis is determined by equation 5.48 while the actuation force for a linear axis is calculated by equation 5.49 , where ${ }^{i} \hat{Z}_{i}$ is the joint axis unit vector.

$$
\begin{align*}
\tau_{i} & ={ }^{i} n_{i}^{T}{ }^{i} \hat{Z}_{i}  \tag{5.48}\\
\tau_{i} & ={ }^{i} f_{i}^{T}{ }^{i} \hat{Z}_{i} \tag{5.49}
\end{align*}
$$

### 5.11 Mechanical Error Modelling

### 5.11.1. First Order Errors

The ability of a MRM to accurately position a cutting tool relative to a work piece is an essential criterion in evaluating the feasibility of implementing this technology. Tool positioning errors are comprised of first and second order components [63]. First order errors result in dimensional inaccuracies in machined components. These errors are attributed to three factors:
(i) Geometric positioning errors between adjacent interfaces.
(ii) Static errors: deflections due to forces on modules, excluding impulse forces.
(iii) Thermal expansion/contraction errors (not considered in this research).
(iv) Mechanical backlash between mating components (discussed in Section 8.8).

## Geometric Positioning/ Assembly Errors

a.

b.

c.


Figure 5.38: MRM Assembly Errors for Interfacing Module Pairs
a. Concatenation error
b. Edge offset error
c. Skewness error

Geometric positioning errors are introduced into an MRM structure during module assembly/ reconfiguration. Although the geometric errors may be very small for properly designed interfaces and connectors with reasonable design tolerances, the accumulation of these minute errors across a significant number of connected modules may be noteworthy.

The first step in the modelling of the accumulated assembly error in an MRM is the identification of the three types of assembly errors illustrated in Figure 5.38. The first error, called the concatenation error $E_{C}$ is defined by equation 5.50 , where $L_{I}$ is the length of an integrated structure, and $L_{M}$ is the length of a similar structure having been created out of two modules instead of one integral piece.

$$
\begin{equation*}
E_{C}=L_{M}-L_{I} \tag{5.50}
\end{equation*}
$$

The second type of error is an edge offset errors $E_{O_{1}}$ or $E_{O_{2}}$ if more than one edge is offset. The third error called "Skewness" defined by the angle $\varepsilon$, is a measure of the rotation of module two about the geometric centre of module interfaces one and two.

The second step in the modelling of the accumulated assembly error is the relation of modulewise assembly errors to the reference frames placed on the interfaces of adjacent modules. According to the kinematic modelling method established in Section 5.5.2 the reference frames placed on the mating interfaces should perfectly coincide. The errors $E_{C}, E_{O 1}, E_{O 2}$ and $\varepsilon$ represent the error in aligning these frames. The error may be kinematically represented by the HTM of equation 5.51 which implements the X-Y-Z Euler angle convention. The mapping of errors $E_{C}$, $E_{O 1}, E_{O 2}$ and $\varepsilon$ to Euler parameters $x, y, z$ and $\alpha, \beta, \gamma$ is dependent on the orientation of reference frame $\mathrm{i}+1$. Errors must be methodically mapped to corresponding axes on frame $\mathrm{i}+1$ for the successful pairing of errors with Euler parameters.

$$
E_{i+1 \leftarrow i}=\left[\begin{array}{cccc}
c \alpha c \beta & c \alpha s \beta s \gamma-s \alpha c \gamma & c \alpha s \beta c \gamma+s \alpha s \gamma & x  \tag{5.51}\\
s \alpha c \beta & s \alpha s \beta s \gamma+c \alpha c \gamma & s \alpha s \beta c \gamma-c \alpha s \gamma & y \\
-s \beta & c \beta s \gamma & c \beta c \gamma & z \\
0 & 0 & 0 & 1
\end{array}\right]
$$

The total system transformation matrix, including assembly errors is calculated by equation 5.9. Accounting for assembly errors is essential during machine calibration, as it is possible for these errors to be compensated for by the machine controller as opposed to the reassembly of the machine tool. The total system transformation matrix, including assembly errors is given by equation 5.52 .

$$
\begin{equation*}
W_{\text {Tool }}^{W_{\text {ool }}} T E=M_{1} E_{1 \leftarrow 2} M_{2} E_{2 \leftarrow 3} \ldots M_{n-1} E_{n-1 \leftarrow n} \tag{5.52}
\end{equation*}
$$

## Static Deflections

Static deflections are caused by operational forces being transmitted throughout the machine structure. These errors contribute to the total first order error and result in geometric inaccuracies in machined parts. The geometric effect of static deflections can be mathematically accounted for in individual modules by altering the HTM that describes the spatial relationship, and orientation of the interface reference frames with regard to each other. Deflections may either cause or contribute to: (i) a linear offset in reference frames or (ii) a rotation of one reference frame relative to the other.


Figure 5.39: Effect of Static Deflections on Kinematic Models
a. A static deflection causing an offset and rotation of frame 2
b. A static deflection causing a deflection of frame 2

Figure 5.39 illustrates the effect of static deflections on the relative position and orientation of reference frames with regard to each other. Static deflections may be determined by established analytical methods or Finite Element Analysis. Once determined, the linear offsets and angles of rotations may be related to Euler parameters $(x, y, z)$ and $(\gamma, \beta, \alpha)$. The new $x, y$ and $z$ Euler parameters will describe the origin of frame $2^{c e}$ with reference to frame 1 ; while the angles $\gamma, \alpha$ and $\beta$ will describe the orientation of frame $2^{c e}$ relative to frame 1 . These parameters are then substituted into equation 5.8 to obtain a new HTM for the module $M_{n}^{\prime}$. The total system transformation matrix, including assembly errors and static deflections is therefore given by:

$$
\begin{equation*}
\underset{\text { Tool }}{\text { Work }} T E_{\text {total }}=M_{1}^{\prime} E_{1 \leftarrow 2} M_{2}^{\prime} E_{2 \leftarrow 3} \ldots M_{n-1}^{\prime} E_{n-1 \leftarrow n} \tag{5.53}
\end{equation*}
$$

The position error vector that characterises the entire first order error in a machine tool is calculated by equation 5.54. The position vector of the tool tip is with relation to the closest reference frame on an associated tool holding module:

$$
\underset{\text { Tool }}{\text { Work table }} P E_{\text {total }}=\underset{\text { Tool }}{\text { Worktable }} T E_{\text {total }}\left[\begin{array}{l}
x_{\text {tool tip }}  \tag{5.54}\\
y_{\text {tool tip }} \\
x_{\text {tool tip }}
\end{array}\right]-\underset{\text { Tool }}{\text { Worktable }} T\left[\begin{array}{l}
x_{\text {tool tip }} \\
y_{\text {tool tip }} \\
z_{\text {tool tip }}
\end{array}\right]
$$

### 5.11.2 Second Order Errors

Second order errors are a result of vibrations induced by the impact of a cutting tool"s teeth with the work surface, regenerative chatter and other vibrations within a machine. These errors are classified as dynamic - $E(t)$ - and generally affect the surface integrity of a machined component, machine tool wear, and tool breakage. The magnitude of a second order error depends on module stiffness and damping properties, as well the mass distribution in the machine. These errors are specific to the physical attributes of individual mechanical assemblies, and are difficult to model in a generic manner [63].

### 5.12 Mechanical Analysis of Drilling Subassembly



Figure 5.40: Drilling Arm and Column Assembly
MRM modules possess the ability to be assembled in multiple configurations and a total of nine unique configurations were achievable with the current library of modules. Loading calculations for individual modules are located in Appendix C. 3 and C.4. Due to the extensive number of modular assembly configurations, only an analysis of the weakest configuration is presented in this section. The subassembly with the least rigidity consists of the drilling head, the range extension arm, the cutting head rotary module and the column module. This subassembly is illustrated in figure 5.40.


Figure 5.41: Drilling Arm and Column Assembly Represented as Springs in Series
a. The vertical and horizontal stiffness"s of modules modelled as springs in series
b. The thrust force on the drill when the drilling head is vertically orientated
c. The thrust force on the drill when the drilling head is horizontally orientated

In order that a static and dynamic analysis could be performed on the system, the vertical and horizontal stiffness"s of individual modules have been modelled as springs in series, as illustrated in Figure 5.41.a. For simplicity the vertical and horizontal subsystems have been decoupled. This simplification will provide a reasonable approximation of the mechanical vibration except at frequencies close to resonance in each mode. The analysis considers the effect of a harmonic thrust force on the drilling head when it is vertically orientated and then horizontally orientated. These scenarios are illustrated in Figures 5.41.b and 5.41.c respectively.

Table 5.17: Module Stiffness's (Refer to Appendix C.5)

|  | Range Extension <br> Arm (1) | Cutting Head Rotary <br> Module (2) | Column Module <br> $\mathbf{( 3 )}$ |
| :---: | :---: | :---: | :---: |
| $\mathbf{K}_{\mathbf{V}}\left(\mathbf{N} \cdot \mathbf{m}^{-1}\right)$ | $1.592 \times 10^{6}$ | $95.908 \times 10^{6}$ | $1.949 \times 10^{6}$ |
| $\mathbf{K}_{\mathbf{H}}\left(\mathbf{N} \cdot \mathbf{m}^{-1}\right)$ | $1.592 \times 10^{6}$ | $153.222 \times 10^{6}$ | $2.597 \times 10^{4}$ |

Table 5.17 contains the calculated stiffness of the related modules; these calculations are presented Appendix C.5. The stiffness of the column in particular, strictly corresponds to the column slide being in a position of 600 mm above its base. For springs in series the spring rates combine reciprocally; the total vertical and horizontal stiffness of the system are therefore:

$$
\begin{gathered}
K_{V \text { total }}=\left[\frac{1}{1.592 \times 10^{6}}+\frac{1}{95.908 \times 10^{6}}+\frac{1}{1.949 \times 10^{6}}\right]^{-1}=8.683 \times 10^{5} \mathrm{~N} . \mathrm{m}^{-1} \\
K_{H \text { total }}=\left[\frac{1}{1.592 \times 10^{6}}+\frac{1}{153.222 \times 10^{6}}+\frac{1}{2.594 \times 10^{4}}\right]^{-1}=2.552 \times 10^{4} \mathrm{~N} . \mathrm{m}^{-1}
\end{gathered}
$$

## Static Analysis



Figure 5.42: Graph of Static Deflection vs Drill Thrust Force for Vertical Drilling
Equation 5.55 presents Hooke"s Law which relates the deflection of a spring to its stiffness and the force exerted on it. By manipulating Hooke"s Law the deflection of the drilling head under the action of a static force may be obtained. The deflection of the drilling head is presented in Figures 5.42 and 5.43 , for static vertical and horizontal forces.

$$
\begin{equation*}
\delta=\frac{F}{K} \tag{5.55}
\end{equation*}
$$



Figure 5.43: Graph of Static Deflection vs Drill Thrust Force for Horizontal Drilling

A vertical thrust force of 50 N leads to a total deflection of 0.058 mm in the vertical plane. The drilling subassembly displayed less rigidity in the horizontal plane and a total deflection of 1.959 mm is expected for a drill thrust force of 50 N . The static deflections due to the thrust force largely affect the accuracy of the depth of holes drilled by the MRM. The reduced rigidity is due to 15 mm sliver steel guide rods that have been used as supporting members in the MRM column module, as opposed a more rigid yet costly dove tail slide system.

## Dynamic Analysis at Multiple Frequencies



Figure 5.44: Spring-Mass-Damper Systems
a. Spring-Mass-Damper model of drilling assembly - vertical harmonic force
b. Spring-Mass-Damper model of drilling assembly - horizontal harmonic force

The performance of the drilling subassembly under dynamic loading conditions was investigated. The system was modelled as a Spring-Mass-Damper system, and separate investigations were conducted for vertical and horizontal harmonic loading; this is illustrated in Figures 5.44.a and 5.44.b respectively.

For a damped system under the action of a harmonic force, the motion is described by equation 5.56; where $m$ is the mass of the drill module ( kg ), $c$ is the damping coefficient $(\mathrm{N} . \mathrm{s} / \mathrm{m}), k$ is the stiffness of the system $(\mathrm{N} / \mathrm{m}), F_{0}$ is the magnitude of the harmonic force $(\mathrm{N})$ and $\omega$ is the frequency of the harmonic force ( $\mathrm{rad} / \mathrm{s}$ ).

$$
\begin{equation*}
m \ddot{x}+c \dot{x}+k x=F_{0} \cos \omega t \tag{5.56}
\end{equation*}
$$

The complete solution to this differential equation for an underdamped system is given by equation 5.57 , where $X$ is the amplitude of the response (m), $\varphi$ is the phase angle (deg), $\delta$ is the damping factor and $\omega_{d}$ is the frequency of damped vibrations ( $\mathrm{rad} / \mathrm{s}$ ).

$$
\begin{gather*}
x(t)=X_{0} e^{-\zeta \omega_{n} t} \cos \left(\omega_{d} t-\phi_{0}\right)+X \cos (\omega t-\phi)  \tag{5.57}\\
\omega_{d}=\sqrt{1-\zeta^{2}} \omega_{n}  \tag{5.58}\\
\omega_{n}=\sqrt{\frac{k}{m}}  \tag{5.59}\\
\zeta=\frac{C}{C_{c}}=\frac{C}{2 \sqrt{k m}}  \tag{5.60}\\
r=\frac{\omega}{\omega_{n}} \tag{5.61}
\end{gather*}
$$

The relative performance of a system under a dynamic load with regard to its static loading characteristics is most effectively analysed by obtaining a ratio of the amplitude of the dynamic response to the amplitude of the static response of the system; under the action of force $F_{0}$ at different frequencies. The amplitude ratio $M$ is calculated by equation 5.62 ; where $r$ is the frequency ratio.

$$
\begin{gather*}
M=\frac{X}{\delta_{s t}}=\frac{1}{\left\{\left[1-\left(\frac{\omega}{\omega_{n}}\right)^{2}\right]^{2}+\left[2 \zeta \frac{\omega}{\omega_{n}}\right]^{2}\right\}^{0.5}}=\frac{1}{\sqrt{\left(1-r^{2}\right)^{2}+(2 \zeta r)^{2}}}  \tag{5.62}\\
\delta_{s t}=\frac{F_{o}}{k} \tag{5.63}
\end{gather*}
$$

The phase angle between the response and the excitation is calculated by equation 5.64.

$$
\begin{equation*}
\phi=\tan ^{-1}\left\{\frac{2 \zeta \frac{\omega}{\omega_{n}}}{1-\left(\frac{\omega}{\omega_{n}}\right)^{2}}\right\}=\tan ^{-1}\left(\frac{2 \zeta r}{1-r^{2}}\right) \tag{5.64}
\end{equation*}
$$

Table 5.18: Physical Characteristics of Drilling Assembly in Horizontal and Vertical Directions

|  | $\mathrm{K}(\mathbf{N} / \mathrm{m})$ | $\mathrm{C}(\mathbf{N} . \mathrm{s} / \mathrm{m})$ | $\mathrm{m}(\mathrm{kg})$ | $\omega_{\mathrm{n}}(\mathrm{rad} / \mathrm{s})$ | $\zeta$ | $\omega_{\mathrm{d}}(\mathrm{rad} / \mathrm{s})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Vertical | $8.683 \times 10^{5}$ | 5 | 2.1 | 643.02 | 0.0019 | 643.02 |
| Horizontal | $2.552 \times 10^{4}$ | 5 | 2.1 | 110.24 | 0.0108 | 110.23 |

Table 5.18 presents physical characteristics of the drilling subassembly, where the stiffnesses correspond to the column slide being in a position of 600 mm above its base. Information on the damping characteristics of drill subassembly was not available. The damping coefficients of the system have therefore been set at the conservatively small but finite value of 5 N.s.m ${ }^{-1}$ in both vertical and horizontal cases.


Figure 5.45: Graph of Amplitude Ratio vs Excitation Frequency - Vertical Excitation Force


Figure 5.46: Graph of Amplitude Ratio vs Excitation Frequency - Horizontal Excitation Force

The physical characteristics of the system were used in conjunction with equation 5.62 to generate plots of the amplitude ratio at multiple frequencies, for both vertical and horizontal planes (see Figures 5.45 and 5.46). Equation 5.64 was used to generate plots of phase angle versus frequency for the subassembly (see Figures 5.47 and 5.48 ). The natural frequency of the drilling subassembly for a vertical excitation force is 102.23 Hz , while the natural frequency in the horizontal direction is 17.55 Hz . Excitation at the natural frequency is accompanied by a peak in amplitude ratio as seen in Figures 5.45 and 5.46. If the excitation were to occur twice per drill revolution, the respective resonant drilling speeds would be $3067 \mathrm{rev} / \mathrm{min}$ and $527 \mathrm{rev} / \mathrm{min}$.


Figure 5.47: Graph of Phase Angle vs Excitation Frequency - Vertical Excitation Force


Figure 5.48: Graph of Phase Angle vs Excitation Frequency - Horizontal Excitation Force

Figures 5.47 and 5.48 present the phase angle of the system response at various excitation frequencies. In both vertical and horizontal cases the excitation and the system response are approximately in phase for frequency ratios less than one. For frequencies greater than the natural frequencies of the system the response leads the excitation by approximately $180^{\circ}$. These characteristics are due to the (approximated) small damping capacity of the system.

## Simulation Performed at 20 Hz

A simulation was performed to investigate the performance of the drilling subassembly under the action of a 50 N force at 20 Hz . The solving of equation 5.57 for these conditions is presented in Appendix C.6. Table 5.19 presents the results of the solution.

Table 5.19: Vibration Characteristics of Drilling Assembly in Horizontal and Vertical Directions

|  | $\mathbf{X}_{\mathbf{0}}(\mathbf{m})$ | $\varphi_{\mathbf{0}}(\mathbf{d e g})$ | $\mathbf{X}(\mathbf{m})$ | $\varphi(\mathrm{deg})$ | $\omega_{\mathrm{n}}(\mathrm{rad} / \mathrm{s})$ | $\zeta$ | $\omega(\mathrm{rad} / \mathbf{s})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Vertical | $8.360 \times 10^{-5}$ | 0.1141 | $5.987 \times 10^{-5}$ | 0.0442 | 643.02 | 0.0019 | 125.66 |
| Horizontal | $6.474 \times 10^{-3}$ | 175.29 | $6.473 \times 10^{-3}$ | 175.33 | 110.24 | 0.0108 | 125.66 |

Equation 5.57 was simulated for five seconds at a refresh rate of 5 ms ; the results of the simulation are presented in Figures 5.49 and 5.50. The graphs display the displacement of the MRM cutting head with regard to time under the action of the excitation force. Theoretical displacements in excess of 10 mm were demonstrated for horizontal excitation (not practically verified). This is due to the excitation frequency being in close proximity to the natural frequency of the system. The dynamic deflections due to the harmonic excitation are expected to adversely affect the accuracy of the depth of holes drilled by the MRM.


Figure 5.49: Graph of Displacement vs Time - Vertical Excitation Force (50 N)


Figure 5.50: Graph of Displacement vs Time - Horizontal Excitation Force (50 N)

### 5.13. Chapter Summary

This chapter presented the mechanical systems of individual modules; including specifications on their mechanical performance, interconnectivity, speeds, torques and power. An example was presented on the assembly of a kinematically viable machine tool and illustrations were provided on the reconfigurability of the prototype system. The mathematical models governing cutting forces and other cutting conditions were presented in brief. An error modelling technique was also presented for MRMs which accounts for assembly errors and static deflections (first order errors). Finally an analysis of a drilling subassembly was presented. This analysis included a static and dynamic analysis of the systems performance in maintaining positional accuracy under the action of cutting forces.

## 6. MRM Electronic System

### 6.1 Electronic System: Design Considerations

The design of an electronic hardware system for the control of MRM modules required the application of the Mechatronic design approach. The focus of the Mechatronic design approach is subsystem design for seamless system integration and balance between the capabilities of the mechanical, electronic and software systems. The following characteristics were identified as essential in the electronic design to support system integration and the mechanical reconfigurability of MRMs:

- Physical modularity: the electronic hardware must be modular in parallel to the mechanical hardware to facilitate easy reconfiguration.
- Scalability: the electronic system must be scalable to provide an increase in digital processing capacity when mechanical modules are added to a machine.
- Customization: the electronic hardware on a platform must be customizable in terms of its ability to enable actuation in different MRM configurations. The number of digital controllers and power amplification units in the electronic system must be exactly matched to the number of actuators present on a platform at all times.
- Integrability: modular units of electronic hardware must display "plug-in" capabilities to facilitate quick integration into a platform.
- Diagnosability: the electronic control system must facilitate the integration of sensors into a platform and provide feedback to the machine operator.


### 6.2 MRM Electronic Control System



Figure 6.1: MRM Electronic Control System

The electronic control architecture illustrated in Figure 6.1 was selected for implementation in MRMs. At the head of the control system is a Personal Computer (PC). The advent of faster processors for PCs and a general reduction in their prices have increased the use of PC-based controllers in CNC machines. PC based controllers are generally flexible, open and can be easily integrated into multiple manufacturing configurations [47]. A PC was also selected for implementation due to already existing hardware and software support for Universal Serial Bus (USB) and Ethernet communication. Although Ethernet communication was not implemented in this design, it has been identified as an important supporting feature for MRM integration into factory wide networks.

The electronic hardware is divided into two subsystems that are controlled by the host PC; these are the spindle control system and the servo control system. The desktop PC communicates with both subsystems via USB. The USB 2.0 protocol was implemented due to existing software support, data transfer rates of up to $12 \mathrm{Mb} / \mathrm{s}$ and the possibility of port expansion [64]. Further advantages of implementing the USB 2.0 standard include its low cost of implementation and its plug-and-play feature.

The host PC communicates directly with a spindle control module via USB. At any instant there is only one spindle control module attached to the PC and the USB standard provided an acceptable solution. Communication with servo control modules does not occur directly via USB. The variable number of axes that may be implemented on an MRM created the necessity for a network orientated approach for communication with these control modules. Servo instructions are first obtained from the host PC via USB, the servo communication module formats these instructions according to the Inter-Integrated Circuit Communication (I2C) protocol. These instructions are then placed onto an I2C network (bus) for transmission to servo control modules.

The I2C protocol was selected based on wide support for the protocol in microcontrollers. The I2C bus is a multi-master bus, implying that any device connected to the bus can initiate a transfer of data. The protocols 7 -bit address format permits up to 128 servo control modules to be implemented on the network, bounded otherwise by a bus capacitance limit of 400 pF . Data on the bus can be transferred at rates up to 400 kbits/s [65]; providing sufficient bandwidth for the communication of servo control instructions. It should be noted that any mechanical module requiring servo control may be connected to the I2C network, provided that the data packet protocols discussed in Chapter 7 are strictly adhered to. This will allow auxiliary modules other than the machines axes (motion modules) to be connected and controlled via this network.

### 6.3 Spindle Control Modules

## Power Supply

The function of a spindle control module is to control the actuation of MRM cutting heads, as well as provide diagnostic feedback on the cutting process. Spindle control modules map to process modules on a $1: 1$ basis. A spindle control module is supplied by 12 V DC power, with a low current and high current supply. The low current 12 V supply is internally regulated to 5 V , and powers the internal digital electronics of the control module. The regulated power also provides a source of power to sensors.

The high current 12 V supply, is used to power an internal relay switch from which motors may draw electricity. The separation of the power supply into a low and high current side was to ensure that the digital electronics are not deprived of power by the motors that are driven by the spindle control module. The total power requirement of a spindle control module is 144 watts, or 24 watts if the onboard relay switch system is unused (see Section 6.7).


Figure 6.2: Spindle Control Module

## USB Communication

The spindle control module receives instructions and provides feedback to the host PC via USB. The module consists of a bi-directional USB to USART converter that is based on a FT232RL chip. The chip is USB 2.0 full speed compatible and requires no USB specific firmware programming; the USB protocol is handled entirely by this device [66]. Serial data that has been received by the FT232RL chip is transmitted via USART to the ATmega 32L control board for manipulation.

## ATmega 32L Control Board

The main spindle control board was based on the ATmega 32L microcontroller, which operated at 4 MHz . The ATmega 32L is a high performance, low power 8-bit RISC chip.

The range of features on this chip is significant, allowing it to be used in both spindle and servo control modules. Features of the ATmega 32L include (but are not limited to):

- 131 Instructions - most single-clock cycle execution
- Up to 16 MIPS throughput at 16 MHz
- $32 \times 8$ general purpose working registers
- 32 K Bytes or flash program memory
- 1024 Bytes of EEPROM
- 2 K Bytes internal SRAM
- 8-channel, 10-bit ADC
- Two 8-bit timer/counters
- One 16 -bit timer/counter
- Four channel PWM
- Byte Oriented Two Wire Serial Interface
- Programmable serial USART
- External and internal interrupts

A diagram of the ATmega 32L board is located in Appendix E.2.

## Sensor Monitoring and A/D Conversion

The Analogue to Digital Conversion (ADC) facility on the ATmega 32L control boards was used to extract sensor data from the MRM cutting heads. The sensor used for vibration monitoring is the ADXL204 dual-axis accelerometer, discussed in Section 6.6.1. Two of the eight available channels were used on the chip for the measurement of vibrations in both vertical and horizontal directions. Sensor signals were decoded with 10 -bit ADC. The vibration data is continuously fed back to the host PC via USB, for process monitoring by the machine operator.

## Relay Switches and Actuation

Digital speed control was omitted in process modules (modular cutting heads), with spindle speed and torque ratios being manipulated only by the mechanical mechanisms discussed in Section 5.6. Process modules were controlled on a simple on/off basis, with the motors being activated by relay switches. The relay switches were in turn activated by 5 V DC signals applied by two output terminals on the ATmega 32L control board. Two terminals were used to provide forward and reverse functionality on the spindle:

- Terminal One (off), Terminal Two (off): Spindle stopped
- Terminal One (on), Terminal Two (off): Rotate spindle forward/clockwise
- Terminal One (on), Terminal Two (on): Rotate spindle in reverse/anticlockwise

Spindle control modules contained onboard relay switches that are capable of supplying 12 V DC power at a maximum of 10 amps to modular cutting heads. In the instance that a module possessed an AC induction motor an AC power box had to be used in conjunction with the spindle control module, this is presented in Section 6.7.

### 6.4 The Servo Communication Module



Figure 6.3: Servo Communication Module

## Power Supply

The function of a servo communication module is to obtain servo instructions via USB and transmit it via an I2C network to servo control modules. The module is powered by a low current 12 V DC power supply. The 12 V supply is internally regulated to 5 V , and powers an ATmega 32L control board and the I2C bus. An MRM platform requires only one servo communication module to begin operation; however if the data transfer requirements of the system exceeds $400 \mathrm{kbits} / \mathrm{s}$ more may be plugged into the system. The total power requirement of a servo communication module is 24 watts.

## USB and I2C Communication

The module contains an FT232RL chip and an ATmega 32L chip (presented in Section 6.3). The FT232RL device enabled bi-directional serial communication between the USB port on the host PC and the USART hardware on the ATmega 32L. ATmega 32L was operated at 4 MHz and performed the function of obtaining serial data, and placing it into a First-In-First-Out (FIFO) queue for transmission on the I2C network. The Two Wire Interface (TWI) on the ATmega 32L was used for I2C communication. The chip contained internal hardware for arbitration detection, status monitoring and control. Complete details of the I2C module on this chip may be found in [67]. The connection points for I2C slave devices are present on the module as illustrated in Figure 6.3. A diagram of the ATmega 32L board is located in Appendix E.2.


Figure 6.4: I2C Bus Electrical Connection [65]
The I2C bus consisted of a clock (SCL) and data (SDA) line that was connected to each device in the network. To ensure proper operation, $2.7 \mathrm{k} \Omega$ pull-up resistors $\left(R_{p}\right)$ were connected between the clock and data lines and a 5 V source $\left(\mathrm{V}_{\mathrm{DD}}\right)$. Figure 6.4 illustrates the electrical integration of devices with the I2C bus.

### 6.5 Servo Control Modules



Figure 6.5: Servo Control Module

## Power Supply

The function of a servo control module is to perform position and speed control on motion modules (machine axes) according to the instructions received on the I2C network. Servo control modules map to motion modules on a $1: 1$ basis. The module is supplied by 12 V DC power, with a low current and high current supply. The low current supply is internally regulated to 5 V for use by ATmega 32L and ATmega 8L microcontrollers. The servo control module also provides regulated power to the sensors on an associated mechanical module. The high current 12 V supply, is used to power an onboard H-Bridge motor driver. The H-Bridge in turn supplies pulse width modulated electric power to a servo drive motor. The total power requirement of a servo control module is 174 watts.

## ATmega 32L and ATmega 8L Control Boards

Servo control modules contained an ATmega 8L and an ATmega 32L chip. The features of the ATmega 32L were discussed in Section 6.3; features of the ATmega 8L [68] include (but are not limited to):

- 130 Instructions - most single-clock cycle execution
- Up to 16 MIPS throughput at 16 MHz
- $32 \times 8$ general purpose working registers
- 32 K Bytes or flash program memory
- 512 Bytes of EEPROM
- 1 K Byte internal SRAM
- Two 8-bit timer/counters
- One 16-bit timer/counter
- Programmable serial USART
- External and internal interrupts

The ATmega 32L microcontroller performs the functions of receiving servo instructions, initializing the appropriate servo control routine and finally reporting the status of the operation to the host PC (via the servo communication module). The chip communicates with the second onboard chip, the ATmega 8L, via USART. The ATmega 8L performs the function of encoder monitoring. Diagrams of the ATmega 32L and ATmega 8L boards are located in Appendix E.2.

## Pulse Counting on the ATmega 8L Board

The ATmega 8L chip counts the electric pulses from the output channels of optical encoders. Pulse counting occurs on an external interrupt basis, which is the reason why a dedicated chip has been used for this purpose. The ATmega 8L determines the number of pulses detected in a 100 ms interval. The pulse count data is transmitted to the ATmega 32L, which determines the speed and position of an axis based on the information. The transmission is triggered by an internal interrupt that is generated by the 16 -bit timer/counter on the ATmega 8L.

## Wave Generation on the ATmega 32L Board

The 16 -bit timer/counter unit on the ATmega 32L chip was used to generate a Pulse Width Modulation (PWM) signal. The PWM signal is the control signal that is generated by a software servo control routine that is executed on the ATmega 32L board. The PWM channel on the ATmega 32L is connected to an onboard H -Bridge motor driver to enable speed control.

A second output terminal on the ATmega 32L board was also connected to the motor driver to switch the direction of motor actuation (refer to diagrams in Appendix E.2).

## Onboard H-Bridge

The H-Bridge motor driver, indicated in Figure 6.5, performed PWM on a 12 volt power source. The unit is capable of supplying up to 10 amps continuously to servo drive motors. At the maximum current rating of 10 amp , a constant load of 9 Nm can be sustained at the output shaft of the motors. In linear axes the motors could theoretically maintain a constant actuation force of up to 1500 N at a current of 10 amp .

## Collision Detection on the ATmega 32L Board

The external interrupt pins on the ATmega 32L were connected to limit switches for collision detection. When a collision occurs a limit switch closes a circuit which applies a 5 V signal to an interrupt pin. The interrupt software routine ends the servo control routine and the operation of the motor. An appropriate status message is then transmitted to the host PC via the servo communication module.

### 6.6 Sensors

### 6.6.1 Process Modules

a.

b.


Figure 6.6: ADXL 204 dual axis accelerometer [69]
a. ADXL 204 sensor and circuit board
b. ADXL 204 function block diagram

MRM process modules each contained the ADXL dual axis accelerometer illustrated in Figure 6.6.a. The accelerometer was used to measure the vibrations generated by the cutting process and hence introduce the characteristic of diagnosability into the system. The mechanical vibrations generated during the interaction of the tool with the work piece can provide diagnostic data for the analyses of the stability of machining operations. The data obtained from an accelerometer can also be used to detect the phenomenon of regenerative chatter (second order vibrations). Regenerative chatter causes volatility in the cutting process which leads to the degradation of machined parts and possibly tool breakage.

The ADXL 204 IC is capable of measuring accelerations up to $17 \mathrm{~m} / \mathrm{s}^{2}$ with a bandwidth of 0.5 Hz up to 2.5 kHz . The bandwidth may be manipulated by changing the capacitors $\mathrm{C}_{\mathrm{Y}}$ and $\mathrm{C}_{\mathrm{X}}$ labelled in Figure 6.6.b. This option is available to narrow the bandwidth and increases the resolution. The commercial board of Figure 6.6.a has factory installed capacitors of 100 nF , setting the bandwidth to 50 Hz and resolution to 2 mg ( g = gravity). The current setting enabled vibrations to be measured at spindle speeds up to $3000 \mathrm{rev} / \mathrm{min}$ on the basis of a single excitation per revolution. Other significant features of the ADXL 204 included a low current requirement of $700 \mu \mathrm{~A}$ when operated at 5 volt. The sensor unit can withstand temperatures of $-40^{\circ} \mathrm{C}$ to $125^{\circ} \mathrm{C}$ and has a shock survival of 3500 g . Further details on the ADXL 204 may be found in [69].

The ADXL 204 interfaces with the servo control module via two of the eight ADC channels present on the ATmega 32L chip (see Section 6.3). The $X_{\text {out }}$ and $Y_{\text {out }}$ channels indicated in Figure 6.6.b, output a signal between 0 to 5 volt for ADC. The nominal voltage on the device is 2.5 volt, which is the voltage when the device is sensing zero acceleration along an axis. Voltages less than 2.5 volt indicate acceleration in the negative direction of an axis while voltages greater than 2.5 volt indicate a positive acceleration. The 10 -bit ADC on the ATmega 32L allowed a measurement resolution of 47 mg .

### 6.6.2 Motion Modules

## Optical Encoders

a.

b.


Figure 6.7: The HEDS-5540 Optical Encoder [70]
a. HEDS-5540 optical encoder
b. HEDS-5540 function block diagram

The HEDS-5540 optical encoder was integrated into MRM motion modules to create a servo drive system (see Section 5.5.3). The function block diagram for this device is illustrated in Figure 6.7.b; indicated on this diagram is the pin configuration for the unit. The HEDS-5540 is capable of producing two square waves in quadrature using channels A and $\mathrm{B}(\mathrm{CH} \mathrm{A}$ and CH B$)$, with a third indexing pulse generated once per revolution on channel I (CH I).

The HEDS-5540 is capable of a resolution of 512 pulses per revolution on a single channel, or 1024 pulses per revolution in quadrature. Further features on the HEDS-5540 include a maximum velocity rating of 30000 rpm and acceleration of $250000 \mathrm{rad} / \mathrm{s}^{2}$. The encoders were also suitably rated at a maximum vibration of 20 g at 1000 Hz , and a maximum temperature of $100{ }^{\circ} \mathrm{C}$ [70].

Although the encoders possess three channels, only one channel ( $\mathrm{CH} A$ ) was used in the MRM design. The device was selected based on cost rather than its level of functionality and proved more cost effective than other single channel encoders. The direction of motion on an axis is predetermined by servo control modules and the decoding of a quadrature signal was not necessary. Channel , $A^{\text {ce }}$ producing 512 pulses per revolution enabled resolutions of up to $0.70^{\circ}$ on rotary axes and 0.003 mm on linear axes. The channel is connected directly to the interrupt terminal on an associated servo control module. The device is also operated on 5 volt DC and derives its power from the regulated power supply unit on servo control modules.

## Limit Switches



Figure 6.8: Limit Switch on Column Module

Limit switches were used in the MRM design for contact sensing in motion modules. These sensors were necessary to prevent damage to the modules through collisions between the internal mechanical components. A single module would usually contain two switches at either end of its axis. The limit switches were connected in a ,normally opence configuration, and would close a circuit when contact is made between a moving component and the switch. The sensors are connected to an interrupt terminal on servo control modules and a 5 volt interrupt signal is generated when the circuit is closed. The interrupt software routine then ceases the generation of a PWM signal to the H -Bridge motor drivers, which in turn stops the operation of the motor.

### 6.7 The AC Power Box

a.

b.


Figure 6.9: Electrical System of the AC Power Box
a. AC Power Box
b. AC Power Box - Schematic of electrical system

Modular cutting heads containing AC induction motors required the use on an AC power box in conjunction with the spindle control module for actuation. The electrical system in this instance bypasses the DC relay switch present on the spindle control module. This relay switch is only capable of supplying 12 V DC power to cutting heads with DC motors (the drilling head specifically). The AC control box, illustrated in Figure 6.9., consists of an alternating current contactor (K), a pilot light (HL), an AC relay switch (S1), an emergency button (S2) and a shift switch (S3).

The pilot light was a safety feature of this system, used to indicate that the electrical components of the system were powered. The second safety feature was the emergency switch, which once pressed, shuts down the operation of the motor.


Figure 6.10: AC Relay Switch

The modular turning head was the only module from the current MRM library that contained an AC induction motor. The motor is a single phase, 220 volt, 0.55 kW induction motor. The motor is specified to use 20 amps and it was necessary that an AC contactor be used in the safe actuation of the motor. The AC contactor consisted of a low current circuit that is activated and deactivated by the emergency stop button and the AC relay switch. When switches S1, S2 and S3 are "closed" and the low current circuit is active, an electromagnetic system within the contactor activates the high current circuit allowing power to be supplied to the shift switch. If the shift switch has been preset, the motor will begin rotating in the preset direction. Figure 6.11 outlines the sequence of control in the actuation of the motor.


Figure 6.11: Sequence of Control in Motor Actuation

The AC relay switch was included in the design to enable the digital on/off control of process modules. The switch is activated by a 5 V signal from the spindle control module, interfaced via an optoisolator. The integrated optoisolator, shown in Figure 6.10, protects the digital circuitry of the spindle control module from the AC currents that exist in the circuitry of the relay switch. Due to cost restrictions a manual shift switch was used to preset the direction of a motor"s rotation and hence the direction of the spindle rotation. The shift switch indicated in Figure 6.9.b has forward and reverse settings or alternatively can be set to zero to deactivate the system. This switch need only be set once prior to the digital actuation of motors via the AC relay switch. The system may then continue to be controlled digitally until a change in spindle direction is necessary.

### 6.8 Power Supply System



Figure 6.12: Flow of AC and DC Power in a MRM

The MRM electrical system is powered by 220 volt AC at 50 Hz . The total power requirement of an MRM system is dependent on the number of control modules, communication modules and AC power boxes present in the system. The host PC operates directly on AC, including those MRM process modules that contain AC induction motors. Those components of the system that required 12 volt DC power are supplied by AC to DC converters; 20 amp converters were used to meet to high current electrical requirements of the system, while 8 amp "PC power supplies" were used to meet the low current requirements of the system. The hybrid use of AC to DC converters was due to restrictions on costs when developing the system. Figure 6.13 shows the AC to DC converters that were used.

Process modules are operated on AC or DC power depending on the type of motor the module contains. Motion modules (MRM Axes) are powered exclusively by 12 volt DC, as all motion modules contain DC servo drives. The power to these modules is supplied and controlled via an associated servo control module. Sensors and microcontrollers in the system that required 5 volt DC power for operation, derived their power form appropriate DC regulators present on either servo or spindle control boards.


Figure 6.13: AC to DC Converters

### 6.9 System Integration and Reconfiguration



Figure 6.14: Power and Control Interface between Mechanical and Electronic Modules
Mechanical modules interface with spindle and servo control modules via an eight wire interface: four sensor signal wires, two sensor power wires and two motor power wires. Mechanical modules with AC induction motors contain three additional wires for motor power. The two generic "interfaces" that are formed by these combinations of wires provide a consistent means of connecting mechanical modules to electronic control modules.


Figure 6.15: Electronic System Assembly
Figure 6.15 illustrates the assembly of the MRM control hardware where spindle and servo control modules are housed in Perspex alongside the mechanical platform. The electronic system is reconfigurable on four levels which ultimately support the mechanical reconfigurability of a MRM.

## Level One - Software

The software on spindle and servo control modules may be changed if the module is used to control a different mechanical module. This enables the modules to be reused with minor adaptations. The change in software may be achieved by removing and reprogramming the associated ATmega 32L and 8L chips. Alternatively the chips may be simply swapped for chips containing the correct control programs. These chips are designed to be modular and fit into dip sockets for easy installation and removal.

## Level Two - Processing Capacity

MRMs possess the ability to increase their functionality by the integration of additional motion modules into a platform. As the number of motion modules increases the digital processing capacity of the system must be increased. This is always necessary as servo control modules map to motion modules on a 1:1 basis. Additional servo control modules may be added to the electronic system by plugging them into the I2C network, and connecting them to the 12 V power supply system.

## Level Three - Communication Bandwidth

Through the process of reconfiguration additional motion modules may be added to the I2C network. If many modules are added to the network, the $400 \mathrm{kbit} / \mathrm{s}$ bandwidth of a standard network may be insufficient to cater for the data requirements of all the modules. In this instance additional servo communication modules may be added in parallel to the first by plugging them into the USB ports of the host PC. The upgrade is completed by connecting the modules into the 12 V DC supply system. Additional servo control modules may then be plugged into the I2C networks on the new servo communication modules.

## Level Four - Power Supply

The power requirements of an MRM system varies as the number of controllers and actuators present in a system are changed through reconfiguration. In the instance that the power demand of the system cannot be met by the present supply system, additional power sources may be added in parallel. Although modular power supply systems were not developed for the present MRM library of modules, it is recommended that in future implementations, standardized modular power supply units be created for these systems. These power supply units should be designed as "plug-in" units, intended for rapidly assembly in parallel to each other.

### 6.10 Chapter Summary

This chapter began with a list of desirable characteristics for the MRM control system, such that its design supports system integration and the mechanical reconfigurability if MRMs. The chapter proceeded with a presentation of the entire MRM electronic control system. This was followed by the presentation of constituent control modules, communication modules, sensors and actuation units such as AC power boxes. The four levels of reconfigurability and the integration of the electrical/electronic system with mechanical modules was also discussed.

## 7. MRM Software System

### 7.1 Software Design Considerations

The MRM software system was designed with due consideration of the five key characteristics that MRMs must display, these are: modularity, convertibility, customization, integrability and diagnosability. The software system either displays these characteristics directly or provides the support needed for the electronic and mechanical systems to fulfil the required characteristics. The translation of these characteristics into software design requirements was as follows:

- Modularity: the MRM software must support the integration of modular electronic hardware into the system.
- Convertibility: the software system must support the control of mechanical hardware that is periodically converted for the manufacturing of new products. This specifically entails the ability to program different MRM configurations.
- Customization: the software must display the ability to customize its control configuration to match a machines hardware configuration. This includes the activation/deactivation of specific control commands based on the mechanical modules present in a platform.
- Integrability: the software system must be designed for the seamless integration of the MRM host PC with distributed control drives containing embedded programs. Integrability is supported by the implementation of well defined communication and control protocols.
- Diagnosability: MRM software routines must be implemented for the extraction of sensor data. This also entails the interpretation and formatting of the data for display through the MRM GUI. A status and error reporting system must be built into the GUI.

The MRM software system, in addition to displaying these five characteristics, is recommended to display controller openness and real time control. Controller openness and real time performance are achieved by the development of an open architecture control system, on an operating system with a real time software kernel. The development of a real time open architecture controller for the MRM was beyond the scope of this research.

### 7.2 Machine Operating System and Development Environment

At the head of the MRM software system was a desktop PC supporting a LINUX operating system. The LINUX operating system was implemented due to the openness of the software thus enhancing the manipulability of the operating system. The host control system was developed and implemented on the Fedora 7 derivative of LINUX.

The development environment that was used in the creation of the host software was Qt Designer by Trolltech ASA [71]. Qt Designer is a C++ Integrated Development Environment (IDE). Qt supports the development of advanced GUI applications, including applications that require Ethernet communication. The Qt application Programming Interface (API) contains approximately 400 classes and 6000 functions, providing an extensive set of building blocks for the development of applications.

The ATmega 8L and ATmega 32L microcontrollers which were implemented on servo control modules, spindle control modules and servo communication modules were programmed in C. The software was created using a package called CodeVision AVR, which is a C compiler, IDE and in-system programmer for the AVR family of microcontrollers [72].

### 7.3 Software Reference Architecture



Figure 7.1: MRM Software Reference Architecture

The MRM software system is based on the multi-tier architecture illustrated in Figure 7.1. The reference architecture outlines the necessary software routines and the interaction between these routines for the functional objectives of the software system to be achieved. The primary objectives of the software system are to enable digital control over MRM actuators, provide reconfigurable control settings and provide diagnostic feedback to the user.

At the highest tier of the software system are the functions that are associated with the humanmachine interface. These functions include user programming, process monitoring and reconfiguration.

User programs and input configurations are cross referenced and validated by other functions to prevent erroneous user inputs. Validated user commands are then relayed to lower functions in the system that manipulate user instructions for use by servo and spindle control modules.

The focus of the control implementation was on hardware abstraction. Hardware abstraction facilitated the reconfiguration of the mechanical and electronic system and minimized the level of reconfiguration required in the software system. Hardware abstraction was achieved on the host PC by creating well defined control protocols for the management of subordinate hardware units. The hardware abstraction was further supported by concentrating generic software functions on the host PC, while module specific functions were concentrated on distributed control drives. Software functions which are designed to be generic (not module specific) included text interpretation, code validation, error compensation, adaptive control and interpolation. Software functions that were specific to individual mechanical modules included position control, speed control, collision detection and sensor monitoring.

The adaptive control and error compensation functions are outlined in red (in Figure 7.1) as these functions have been identified as essential in MRMs; however the implementation of this in software was out of the scope of this research. The individual software routines that constitute the MRM software architecture are to be discussed in further detail in the proceeding sections of Chapter 7. Figure 7.1 should be referred to during the discussions as guide to the context of software entities in the overall architecture.

### 7.4 MRM Graphic User Interface



Figure 7.2: MRM User Interface

The first stage in the development of the MRM software system was the development of a GUI. The MRM GUI provides a text window for the entry of user programs. Users enter programs in the text window according to a limited version of conventional NC or G code (ISO 6983). The GUI provides control buttons that enable the user's control program/code to be validated and saved. Alternatively a previous program may be executed the from the machine "s code database file (code.dat - discussed later). Drop down menus have been built into the GUI that allow the machines current control configuration to be selected.

Once a user has selected the machine es current control configuration and has entered a valid NC program, the execution of the program is initialized by the „Execute ${ }^{\text {ec }}$ button. A progress bar in the GUI indicates the progress of the user"s program as a percentage. A status info box provides the user with reports on the current operation and a warning info box alerts the user with regard to problems that arise during the machines operation. The feedback of information to the user fulfils the diagnosability requirement of the system.

Provision has been made on the machine GUI for the feedback of process data from sensors to the user. In particular a visual and numerical display of the vibration measured from MRM cutting heads is available for user examination via the machine GUI. Mechanical vibration has been chosen as the process variable for diagnostics as these vibrations are the primary indicators of the stability of the machining process. For an industrial implementation the range of diagnostic tools on the MRM may be extended to force and temperature monitoring systems.

### 7.5 User Programming

a.


## b.



Figure 7.3: Numerical Control Syntax [31]
a. A block of NC code
b. The format of an NC word

The MRM is programmed by the user with a modified and limited set of traditional NC commands (ISO 6983). A part program using this syntax consists of code blocks, individual blocks consist of several ,,words", and each word consists of an address and a number [31]. Figure 7.3.a illustrates a typical block of NC code and Figure 7.3.b illustrates the format of a typical NC word.

The MRM software was created to recognize a single line of code as a block, without the necessity of using the customary EOB (End of Block) syntax. This limited the length of a block of code to a single line. The MRM GUI may be expanded in size for longer lines/blocks of NC code. Table 7.1 summarizes the addresses and the related functions that were made available for creating control programs for the MRM. For additional information on NC programming please refer to [31].

Table 7.1: NC Commands for MRM Programming

| Function | Address | Units |
| :---: | :---: | :---: |
| Line Number |  |  |
| Block Number | N |  |
| Preparatory Functions |  |  |
| Rapid Positioning | G00 |  |
| Linear Interpolation | G01 |  |
| Circular Interpolation (CW) | G02 |  |
| Circular Interpolation (CCW) | G03 |  |
| Coordinate System Origin Setting | G10 |  |
| Absolute Distance Mode | G90 |  |
| Incremental Distance Mode | G91 |  |
| Axis Words |  |  |
| X - Primary Linear Axis | X | mm |
| Y - Primary Linear Axis | Y | mm |
| Z - Primary Linear Axis | Z | mm |
| U - Secondary Linear Axis (Parallel to X) | U | mm |
| V - Secondary Linear Axis (Parallel to Y) | V | mm |
| W - Secondary Linear Axis (Parallel to Z) | W | mm |
| A - Angular Axis About X | A | deg |
| B - Angular Axis About Y | B | deg |
| C - Angular Axis About Z | C | deg |
| Miscellaneous Words |  |  |
| Program Stop | M00 |  |
| Program End | M02 |  |
| Turn Spindle CW | M03 |  |
| Turn Spindle CCW | M04 |  |
| Stop Spindle Rotation | M05 |  |
| Other Words |  |  |
| Spindle Speed (Manually Manipulated) | S | 0 or 1 |
| Feed Rate | F | $\mathrm{mm} / \mathrm{min}$ |
| X - Axis Offset for Arcs | I | mm |
| Y - Axis Offset for Arcs | J | mm |
| Z - Axis Offset for Arcs | K | mm |
| Arc Radius | R | mm |

### 7.6 Reconfiguration of the NC Command Set

MRM reconfiguration at a software level involved the activation/ deactivation of commands in view of a machines modular configuration. All MRM configurations contained the base module and a cutting head; the $S$ word address and the $X$ word address were therefore always active. In addition to this all M and G words addresses (Excluding G02 and G03) were active in every configuration as these words are non-specific with regard to a particular module.

Through the process of mechanical reconfiguration the number and types of motion modules changed on a MRM platform. The process of software reconfiguration therefore targeted the activation/deactivation of commands which related directly to an individual axis or commands which were used to control the synchronized motion of two axes.

For simplicity all MRM kinematic configurations were represented in a drop down menu for selection by the operator. The selection of a specific kinematic configuration activated the word addresses associated with that configuration. Table 7.2 summarizes the activation/ deactivation of MRM functions through software reconfiguration, and their associated word addresses.

Table 7.2: MRM Software Reconfiguration - Activation/ Deactivation of Functions

| Functions/ Words | Address | Activation |
| :--- | :--- | :--- |
| Block Number | N | Always active |
| Preparatory Functions | G00, G01, G10, G90, G91 | Always active |
| Miscellaneous Words | M00, M02, M03, M04 M05 | Always active |
| Other Words | S, F | Always active |
| X - Primary Linear Axis | X | Always active |
| Y or Z - Primary Linear Axes | X, Y, Z | Active when selected |
| A, B or C - Primary Angular Axes | A, B, C | Active when selected |
| U, V, W - Secondary Linear Axes | U, V, W | Active when selected |
| Circular Interpolation (CW) | G02, G03 | +2 active linear axes |
| X, Y or Z - Axis Offset for Arcs | I, J, K | Relevant linear axes are active |
| Arc Radius | R | +2 active linear axes |

### 7.7 Reconfiguration of Driver Module Addresses

The physical addition/removal of spindle driver modules and servo communication modules during reconfiguration required the initialization of module addresses to re-establish communication via USB and I2C. USB communication was initialized by entering the addresses of the servo and spindle ports in text format in the MRM user interface. An example of a USB port address on a Linux operating system would be "/dev/ttyUSB0". USB port speeds were configured through a drop down menu on the GUI from which common data transfer speeds were selected.

The addressing of servo driver modules and their corresponding axes was a simpler process. The I2C addresses of individual axes corresponded on a 1:1 basis with their program word addresses. To illustrate this principle consider an axis which is controlled using the word address „X". The corresponding I2C address of this axis will also be the character 'X', which according to the ASCII standard is reduced to the hexadecimal number 0x58. The number 0x58 is therefore the address of the X -axis on the I2C network. The process of reconfiguring the MRM command set by drop down menus therefore served a dual purpose. Enabling an axis word address further enabled the corresponding axis to be addressed over the I2C network.

### 7.8 NC interpretation and Validation

MRM programs are entered into the code editor on the machine GUI in text format. All programs must first be interpreted and saved prior to execution; this is done by the activation of the "Interpret and Save" button on the user interface. Text interpretation involved the allocation of individual NC words to appropriate variables in the software. During the process of text interpretation the user"s program is subjected to two stages of filtering. The first stage filters the program for the use of incorrect syntax. The second stage compares the user program to the MRMs current modular configuration.

The drop menus used to initialize the machine "s modular axes configuration creates a function reference model against which NC functions in the user"s program are compared. Functions used by the machine operator that are inconsistent and incompatible with the machines modular configuration are rejected and an error message is issued through the GUI.

Valid user programs that have successfully passed through the two stages of filtering are stored in a database file called "code.dat". Code that has been stored is ready to be executed using the "Execute" button on the user interface. If the "Execute" button is activated without a program entered in the code editor the MRM software will execute old code that has been previously stored in the code database file. This file is overwritten each time the user saves a new program, and is cleared by the activation of the "Reset" button. Only a limited level of functionality was enabled with regard to code storage and retrieval due to the prototypical nature of the platform.

### 7.9 Execution of User Programs

The clicking of the "Execute" button on the MRM user interface begins the execution of the user"s program (sample code located in Appendix I). The validated program is retrieved from the code database file (code.dat) and loaded into the host PC"s dynamic memory by the "Load Program" software routine. If the software is unable to read the code database file or if the file is empty, error messages are generated in the warning text box on the GUI. User programs are loaded a block at a time, and if a block had been successfully loaded, control is passed onto the "Function Selection" software routine; this is illustrated in Figure 7.4.

The Function Selection software routine is the main software entity that manages the active control routines being executed on the MRM platform. Control routines are dictated by the M and $G$ word addressed in the user program, while other word addresses dictate information on tool feed rates, spindle speeds and distances. The function selection software routine first executes all M word instructions. M word addresses contain instructions relating to the general control of the machine, these instructions include: program stop/start/end, direction of spindle rotation and other miscellaneous functions. Each instruction requires additional dedicated software subroutines for its execution. Once an M word has been used to activate a mechanical module, that module will continue operation until another M word has been used to deactivate it. For example, if a spindle has been switched on and instructed to rotate clockwise, it will continue to do so without the M word instruction being repeated in every block of user code. Upon the completion of the M word instructions in a block of code, the execution of $G$ word instructions begins.

G word addresses are primarily concerned with control of the machines axes. These instructions include the initialization of reference coordinate systems, absolute or incremental programming and the mode of motion control (point to point, linear interpolation, circular interpolation). Each of these software routines require additional dedicated software subroutines for their execution. Once a $G$ word has been used, the control routines that are related to that $G$ word maintain precedence until overruled by other G words in subsequent blocks of code. G words do not need to be repeated in every line of code. For example, if absolute coordinate programming has been selected, this mode of control will maintain precedence without the $G$ word instruction being. Once all M and G word instructions have been completed for a block of code, control is passed onto the "Status Update" software routine.

The Status Update routine updates the progress bar on the machine GUI. The progress is indicated as a percentage of the number of code blocks that have been executed with regard to the total number of blocks in the user 's program. The status box is also updated with information for the machine operator, relating to the current state of the machining process. If all the blocks of code in the program have been executed the software returns control to the operating system until the user activates another function on the user interface.


Figure 7.4: Sequence of Operations for Execution of User Programs

### 7.10 M Word Software Routines



Figure 7.5: Sequence of Events in the Execution of $M$ Word Instructions
Table 7.3: Hexadecimal Values of General Instruction Byte for Various M and G Words

| Spindle Control Modules |  |  |
| :---: | :---: | :---: |
| M or G Word | Instruction | General Instruction Byte Value (HIEX) |
| M00 | Program Stop | 0x01 |
| M02 | Program End | 0x02 |
| M03 | Turn Spindle Clockwise | 0x03 |
| M04 | Turn Spindle Anticlockwise | 0x04 |
| M05 | Spindle Stop | 0x05 |
| M or G Word | Instruction | Servo Control Modules |
| M00 | Program Stop | General Instruction Byte Value (HEX) |
| M02 | Program End | 0x01 |

M Word instructions that were enabled in the MRM software system included: Program Stop, Program End, Turn Spindle CW/CCW and Spindle Stop. The execution of these functions involved switching operations on the MRM, as no digital speed control was enabled on the cutting heads. The communication of these instructions to spindle and servo control modules occurred via the respective USB ports and feedback on the completion of these instructions also received via USB on an interrupt basis. Section 7.14 presents the control and data communication protocols for servo and spindle control modules. A single byte was required to transfer M word instructions to both types of control modules. This byte is the "General Instruction" byte in the respective control protocols. Table 7.3 displays the hexadecimal values of the "General Instruction" byte for the various instructions.

### 7.11 G Word Software Routines

## Coordinate Systems and Absolute Programming

The G10 instruction was built into the MRM software however its use in this instance differed from the ISO 6983 convention. MRMs being modular and reconfigurable present a unique challenge in establishing the position of the machine spindle relative to the work table after reconfiguration. The challenge of establishing the position of the machine spindle is solved by issuing the G10 command, causing each individual axis to move to its home position after the machine has been assembled. The position of the spindle relative to the absolute reference coordinate system on the work table is then known by the substitution of the various home locations for individual axes into the machine transformation matrix.

Example: consider the three axis drilling configuration presented in Appendix D.1. The home positions of the various axes are: $x=257.5 \mathrm{~mm}, y=0 \mathrm{~mm}$ and $z=647 \mathrm{~mm}$
$\underset{\text { Worktable }}{\text { Drill }} T=\left[\begin{array}{cccc}1 & 0 & 0 & -344.5+x \\ 0 & 1 & 0 & 2.5+y \\ 0 & 0 & 1 & -2+z \\ 0 & 0 & 0 & 1\end{array}\right]=\left[\begin{array}{cccc}1 & 0 & 0 & -344.5+257.5 \\ 0 & 1 & 0 & 2.5+0 \\ 0 & 0 & 1 & -2+685 \\ 0 & 0 & 0 & 1\end{array}\right]=\left[\begin{array}{cccc}1 & 0 & 0 & -87 \\ 0 & 1 & 0 & 2.5 \\ 0 & 0 & 1 & 683 \\ 0 & 0 & 0 & 1\end{array}\right]$
Therefore upon the issuing of the G10 command the position of the drilling spindle relative to the coordinate system on the work table is $\mathrm{P}(x, y, z)=(-87 \mathrm{~mm}, 2.5 \mathrm{~mm}, 645 \mathrm{~mm})$.

To enable absolute programming the position of the spindle relative to the work table must be manually entered by the machine operator into the position database file (Position.dat); after the G10 command has been issued. The position database file maintains a record of the position of the machine spindle relative to the work table and is updated by the software for each movement of the machines axes thereafter. The G10 command need only be issued once after reconfiguration, or when a recalibration of the machine is required. This command is issued in the "General Instruction" byte in the servo control instruction (see Section 7.14).

Table 7.3 (continued): Hexadecimal Values of General Instruction Byte for Various M and G Words

|  | Servo Control Modules |  |
| :---: | :---: | :---: |
| M or G Word | Instruction | General Instruction Byte Value (HEX) |
| G10 | Return Axis to Home Position | 0x0A |

## Modes of Motion Control

MRM platforms possess the ability to be programmed in either absolute or incremental coordinates (G90 and G91). The motion of the machines axes could be controlled in rapid point to point motions (G00) or constant speed motions (G01, G02, G03). Figure 7.6 illustrates the sequence of operations for the processing of a G Word instruction. Instructions such as G90 and G91 do not require any motion of the machine axes and are activated to control the behaviour of other G Word instructions. Instructions G00 and G10 are associated with rapid motions of the machines axes, and do not require interpolation before the transmission of commands to servo control modules.


Figure 7.6: Sequence of Events in the Execution of G Word Instructions

Instructions G01, G02 and G03 observe the required feed rate as dictated by the user program. These instructions require the execution of an appropriate interpolation algorithm, to divide the required distance of travel into small linear segments across which a position control algorithm is applied. The smaller segmented target distances are transmitted to the servo control modules for the execution after acceleration and deceleration control is applied.

Servo control instructions are transmitted to control modules via USB, as shown in Figure7.6. Once these low level instructions have been generated by the MRM software, control is transferred to the serial communication software routine that transmits servo instructions and receives feedback on its successful or unsuccessful execution. Feedback is received via USB on an interrupt basis. If the execution of servo instructions is unsuccessful, control is transferred to the function selection subroutine which generates an error message for the machine operator. If the instructions have been successfully transmitted, the serial communication routine updates the position of the axes in the position database file (Position.dat), and continues with the transmission of further servo instructions until all the necessary instructions have been completed.

### 7.12 Interpolation

A Sampled-Data interpolator was selected for implementation in MRMs. The Reference Word algorithm incorporating the Improved Tustin Method (ITM) was the favoured combination. The ITM is generally preferred for software orientated numerical control designs where floating point arithmetic is possible. The ITM exhibits high accuracy and a relatively low number of iterations in comparison to Euler and Taylor methods [31]. The ITM/Reference Word algorithm involved the linear segmentation of both linear and non linear trajectories.

## Linear Interpolation



Figure 7.7: Linear Interpolation [31]
a. Total linear path divided into interpolation points $P_{i}$
b. Axial increments in X and Y axes for individual interpolation time steps

The G01 command required the process of interpolation to achieve a linear trajectory of the cutting tool. Figure 7.7.a illustrates the principle of interpolation, where a linear trajectory is divided into segments. The division of a trajectory into segments improves the accuracy of the position control. Individual segments may be resolved into axial increments for each axis that is active in the trajectory. Figure 7.7.b illustrates the axial increments for each interpolation cycle time. These increments generate a discreet ramp input to the position control algorithms running on servo drive modules. For a trajectory requiring the synchronized motion of two axes the length of the linear path is calculated by equation 7.1.

$$
\begin{equation*}
L=\sqrt{\left(x_{e}-x_{s}\right)^{2}+\left(y_{e}-y_{s}\right)^{2}} \tag{7.1}
\end{equation*}
$$

The length to be travelled per interpolation cycle is calculated by equation 7.2 , where $T_{i p o}$ is the interpolation cycle time (s) and $f$ is the combined feed rate of the two axes ( $\mathrm{mm} / \mathrm{min}$ ):

$$
\begin{equation*}
\Delta L=\frac{f \cdot T_{i p o}}{60} \tag{7.2}
\end{equation*}
$$

The axial increments per cycle are calculated by equation 7.3 and the total number of iterations $N$, required to complete the trajectory is calculated by equation 7.4 :

$$
\begin{gather*}
\Delta X=\Delta L \frac{x_{e}-x_{s}}{L}  \tag{7.3}\\
\Delta Y=\Delta L \frac{y_{e}-y_{s}}{L} \\
N=\frac{L}{\Delta L} \tag{7.4}
\end{gather*}
$$

The calculation of the total number of iterations often results in a residual length for each axis, as the number $N$ has to be in the format of an integer.

$$
\begin{align*}
\operatorname{Res}_{x} & =\left(x_{e}-x_{s}\right)-N \cdot \Delta X  \tag{7.5}\\
\operatorname{Res}_{y} & =\left(y_{e}-y_{s}\right)-N . \Delta Y
\end{align*}
$$

The residual length is a form of truncation error, and is compensated for by distributing it evenly among each interpolation cycle. The final axial increments per interpolation cycle are given by equation 7.6:

$$
\begin{align*}
& \Delta X_{\text {final }}=\Delta X+\frac{R e s_{x}}{N}  \tag{7.6}\\
& \Delta Y_{\text {final }}=\Delta Y+\frac{R e s_{y}}{N}
\end{align*}
$$

The axial increments are stored in a database file called "FIFOtemp.dat". This is a temporary storage location for the data before acceleration/deceleration control is performed.

## Circular Interpolation

The G02 and G03 commands require the process of circular interpolation to achieve a tool trajectory along an arc of radius $R(\mathrm{~mm})$. The circular trajectory is achieved by dividing the arc into multiple linear segments. The linear axial increments per interpolation cycle time, for a trajectory along an arc of radius $R$, are given by equation 7.7:

$$
\begin{align*}
\Delta X & =x(i+1)-x(i)  \tag{7.7}\\
\Delta Y & =y(i+1)-y(i)
\end{align*}
$$

The calculation of the appropriate linear increments is dependent on the current position of a machines tool tip after each interpolation cycle. This is given by equation 7.8 where $R(i)$ is the radius of the interpolated arc from the previous interpolation cycle.


Figure 7.8: Circular Interpolation [31]
a. Interpolation of an arc
b. Radial Error and Chord Height Error

$$
\begin{align*}
& x(i+1)=R(i) \cos (\theta(i+1))  \tag{7.8}\\
& y(i+1)=R(i) \sin (\theta(i+1)) \\
& R(i)=\sqrt{x(i)^{2}+y(i)^{2}} \tag{7.9}
\end{align*}
$$

The angular position of the tool tip is calculated by equation 7.10, where $\alpha$ is the angular increment in tool position, for each interpolation cycle. In the Improved Tustin Method $\alpha$ is calculated by equation 7.11 and the number of required iterations by equation 7.12.

$$
\begin{align*}
& \theta(i+i)=\theta(i)+\alpha  \tag{7.10}\\
& \alpha=\sqrt{\frac{16}{R-1}} \cong \frac{4}{R}  \tag{7.11}\\
& N=\frac{\theta}{4} \sqrt{R} \tag{7.12}
\end{align*}
$$

The required feed rates for the individual axes to achieve the synchronized circular motion are given by equation 7.13:

$$
\begin{align*}
& f_{x}=f \frac{x(i+1)-x(i)}{\sqrt{(x(i+1)-x(i))^{2}+(y(i+1)-y(i))}}  \tag{7.13}\\
& f_{y}=f \frac{y(i+1)-y(i)}{\sqrt{(x(i+1)-x(i))^{2}+(y(i+1)-y(i))}}
\end{align*}
$$

Once an arc has been linearized into multiple segments with individual feed rate requirements, further linear interpolation must be performed to obtain a final set of axial increments for transmission to servo control modules.

When approximating a circle by multiple linear segments two types of errors occur, these are chord height errors EH and radial errors ER (see Figure 7.8.b). These errors are calculated using equations 7.14 and 7.15:

$$
\begin{gather*}
E R(i)=R(i)-R=\sqrt{x(i)^{2}+y(i)^{2}-R}  \tag{7.14}\\
E H(i)=R-R(i) \cos \left(\frac{\alpha}{2}\right) \tag{7.15}
\end{gather*}
$$

### 7.13 After Interpolation Acc/Dec Control



Figure 7.9: Axial Increments Before and After Acc/Dec Control [31]
a. Axial increments before Acc/Dec control
b. Axial increments after Acc/Dec control
c. Only deceleration control performed

The process of acceleration and deceleration (Acc/Dec) control must be preformed after interpolation to ensure the smooth motion of the axes. The interpolation algorithms presented in the previous section provide a steady reference of axial increments to position control algorithms as illustrated in Figure 7.9.a. The position control algorithm runs on servo control modules. A fixed reference of axial increments creates the problem of excessive acceleration at the beginning of a trajectory and causes an overshoot of the target position at the end. Acc/Dec control is performed by ramping up and ramping down the reference input to the position control algorithm, as illustrated in Figure 7.9.b.

The MRM system contained low powered motors. The execution of acceleration control was therefore omitted from the software as excessive accelerations were not a concern for this system. After interpolation the focus of the control system was exclusively on deceleration control to prevent overshoot in the target position that may be caused by inertia. The output from deceleration control only is illustrated in Figure 7.9.c. Deceleration control is performed by obtaining the sum $S$ of the position increments for the final $j$ interpolation cycles. This sum is then spread out over $n$ additional interpolation cycles in a linearly receding pattern.

The sum is obtained by equation 7.16 where $k_{\text {final }}$ is the last interpolation cycle number in the original set of axial increments:

$$
\begin{equation*}
S=\sum_{a=0}^{j-1} \Delta X\left(k_{\text {final }}-a\right) \tag{7.16}
\end{equation*}
$$

The sum of the final $j$ increments is used to calculate a declaration constant $D$ that provides the linear decrement in the reference position. Equation 7.17 was used to calculate the deceleration constant for a steady original reference of $\Delta \mathrm{X}$.

$$
\begin{equation*}
D=\frac{S-\Delta X \times(j+n)}{0.5(j+n)^{2}} \tag{7.17}
\end{equation*}
$$

The new set of reference positions including linear deceleration control is calculated by 7.18. Note that deceleration control is only applied from interpolation cycle time numbers $\left(k_{\text {final }}-j+1\right)$ to $\left(k_{\text {final }}+n\right)$, where $k_{\text {final }}+n$ is the new number of interpolation cycles required to complete the motion of the axes.

$$
\begin{equation*}
\Delta X_{o}(k)=\Delta X+0.5 D\left(i^{2}-(i-1)^{2}\right) \quad(0 \leq i \leq j+n) \tag{7.18}
\end{equation*}
$$

The final sets of axial increments are stored in a database file called "FIFO.dat". After Acc/Dec control has been performed, control is passed onto the serial communication software routine. This software routine then transmits the axial increments stored in FIFO.dat, as part of the instruction set to servo control modules.

## Example

Table 7.4: Deceleration Control Performed After Interpolation

| Before Deceleration Control |  | After Deceleration Control |  |  |
| :---: | :---: | :---: | :---: | :---: |
| $k$ | $\Delta \mathbf{X}(\mathrm{~mm})$ | $\mathbf{k}$ | $\mathbf{i}$ | $\Delta \mathbf{X}_{\mathbf{0}}(\mathbf{m m})$ |
| 1 | 4 | 1 | 0 | 4 |
| 2 | 4 | 2 | 0 | 4 |
| 3 | 4 | 3 | 0 | 4 |
| 4 | 4 | 4 | 0 | 4 |
| 5 | 4 | 5 | 1 | 3.75 |
| 6 | 4 | 6 | 2 | 3.25 |
| 7 | 4 | 7 | 3 | 2.75 |
| 8 | 4 | 8 | 4 | 2.25 |
|  | 0 | 9 | 5 | 1.75 |
|  | 0 | 10 | 6 | 1.25 |
|  | 0 | 11 | 7 | 0.75 |
|  | 0 | 12 | 8 | 0.25 |
| Total | $\mathbf{3 2} \mathbf{~ m m}$ |  |  | $\mathbf{3 2} \mathbf{~ m m}$ |

As an example, consider the set of original axial increments presented in Table 7.4. For deceleration control it is decided that the sum of the final four increments are to be distributed over an additional four interpolation cycles. This brings the total number of interpolation cycles for the trajectory up to twelve. Deceleration control begins on the fifth cycle and ends on the twelfth, linearly ramping down the axial increments from 4 mm down to 0.25 mm per cycle.
$S=\sum_{a=0}^{j-1} \Delta X\left(k_{f \text { final }}-a\right)=\sum_{a=0}^{4-1} \Delta X(8-a)=\Delta X(8)+\Delta X(7)+\Delta X(6)+\Delta X(5)=16$
$D=\frac{S-\Delta X \times(j+n)}{0.5(j+n)^{2}}=\frac{16-4 \times(4+4)}{0.5(4+4)^{2}}=-0.5$
Deceleration begins at cycle number: $k=k_{\text {final }}-j+1=8-4+1=5$
Deceleration and trajectory ends at cycle number: $k=k_{\text {final }}+n=8+4=12$

### 7.14 Control Protocols and Data Communication

The use of standard instruction and feedback protocols for the control of MRMs created the flexibility for mechanical and electronic control modules to be easily connected and controlled by the system. Motion modules (modular axes) were controlled using a ten byte instruction protocol. The first byte of the instruction packet is the servo control module address to which the subsequent data bytes must be routed. The second byte is used to transmit general instructions to the control module. The final pair of four bytes are instructions on the distance and the interpolation cycle time for the execution of the position control algorithm. Distances and interpolation cycle times are stored in the „C"c float data type, enabling a range of values in decimals from $\pm$ ( $3.4 \times 10^{-38}$ to $3.4 \times 10^{38}$ ).

A seven byte protocol was used for the feedback of information from servo control modules to the host PC. The first byte was used to address the data to the servo communication module. This was necessary as the I2C bus is a multi-master bus and the transmission of feedback to the host PC required the servo communication module to enter into slave receiving mode with a corresponding servo control module as the master. The six successive data bytes that are received by the servo communication module are then transmitted to the host PC via USB. The second byte is the address of the servo control module that is providing the feedback. This address acts as an identification number for the module.

The third byte is general feedback provided by the module. The type of feedback responses include: Instruction Complete, No Actuation and Collision at Axis Limit. The final four bytes are used to transmit the final position of the axis back to the host PC; this is used to update the position database file. Table 7.5 summarises the instruction and feed back protocols for servo control modules. The details of the "General Instruction" and "General Feedback" bytes are contained in Table 7.3 and Table E.3.1 (in Appendix E.3).

Modular cutting heads were controlled by spindle control modules, based on a single instruction byte received from the host PC. Five bytes were used for feedback to the main control program.

Spindle modules are connected directly to the host PC via USB, and required a much more compact control protocols than motion modules. Feedback values from process modules are returned in the „, $\mathrm{C}^{\text {ce }}$ float data type. Table 7.6 summarizes the instruction and feed back protocols that were used in conjunction with spindle control modules to manage the MRM cutting heads. The details of the of the "General Instruction" and "General Feedback" bytes are contained in Table 7.3 and Table E.3.1 (in Appendix E.3).

Table 7.5: Instruction and Feedback Protocols for Servo Control Modules

| Transmission of Instructions |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Sequence | Purpose | Data Size |  |  |
| $\mathbf{1}$ | Servo Control Module"s I2C Address | 1 Byte |  |  |
| $\mathbf{2}$ | General Instructions | 1 Byte |  |  |
| $\mathbf{3}$ | Axial Increment | 4 Bytes |  |  |
| $\mathbf{4}$ | Interpolation Cycle Time | 4 Bytes |  |  |
| Feedback |  |  |  |  |
| Sequence | Purpose | Data Size |  |  |
| $\mathbf{1}$ | Servo Communication Module"s I2C Address | 1 Byte |  |  |
| $\mathbf{2}$ | Servo Control Module"s I2C Address | 1 Byte |  |  |
| $\mathbf{3}$ | General Feedback | 1 Byte |  |  |
| $\mathbf{4}$ | Feedback Value | 4 Bytes |  |  |

Table 7.6: Instruction and Feedback Protocols for Spindle Control Modules

| Transmission of Instructions |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Sequence | Purpose | Data Size |  |  |
| $\mathbf{1}$ | General Instructions | 1 Byte |  |  |
| Feedback |  |  |  | Data Size |
| Sequence | Purpose | 1 Byte |  |  |
| $\mathbf{1}$ | General Feedback | 4 Bytes |  |  |
| $\mathbf{2}$ | Feedback Value |  |  |  |

### 7.15 Servo Communication Module: Software Routines

The servo communication module is responsible for the transmission of data between the host PC and servo control modules. Figure 7.10 places the software functions of the servo communication module into the context of the control system. The diagram also illustrates the sequence of operations performed by the servo communication module for the transmission of data. The servo communication module has four modes of operation: instruction receive mode, instruction transmit mode, feedback receive mode and feedback transmit mode.

## Instruction Receive Mode

At the beginning of the execution of a new series of instructions the servo communication module is in receive mode. In this mode the main ATmega 32 chip waits for the issue of servo control instructions from the host PC. These instructions are received by the USART receiver interrupt service routine. The USART data register is eight bits and instructions are received a single byte a time. The service routine obtains the servo control instructions and places them into a character buffer. The first byte of every ten bytes received is the address of a servo control module. These addresses are registered as active by the software.

The hexadecimal number 0xFF was reserved as a flag to indicate that all instructions have been loaded. If the first byte of an anticipated ten byte sequence is found equal to $0 x F F$, the software routine ceases to buffer data and the servo communication module switches from instruction receive to instruction transmit mode.


Figure 7.10: Sequence of Operations for the Transmission of Servo Instructions and Feedback

## Instruction Transmit Mode

In instruction transmit mode, the software transmits the buffered servo instruction data to the respective servo control modules over the I2C bus. The transmission is initialized by the issue of a START condition on the bus. Next a seven bit slave address is transmitted and one „write" bit, indicating that a transmission of data is to occur. The servo control module that has been addressed issues an acknowledgement on the bus. The servo communication module will then continue to transmit all nine remaining instruction bytes to the servo control module. Upon completion a STOP condition is issued on the bus, and the process is repeated until all servo control modules have received their respective instructions. Once all instructions have been transferred the servo communication module issues a general call on the I2C bus. The binary address $0 b 0000000$ is reserved for the general call, to which all modules respond, irrespective of their individual addresses. The general call is issued to begin the synchronized execution of instructions by the various servo control modules. Once the general call has been issued the servo communication module switches to the feedback receive mode.

## Feedback Receive Mode

In feedback receive mode the servo communication module receives feedback from the servo control modules. Individual servo control modules transmit their respective feedback data packets to the communication module over the I2C bus. The first byte of the packet is the servo communication module"s address and a write bit. The direct addressing of the communication module is necessary to prevent other servo control modules on the bus from receiving the data. Once communication has been established the remaining six bytes of feedback are transmitted. The I2C hardware units on the ATmega 32 chips contain inbuilt bus arbitration, allowing servo control modules to transmit feedback data one at a time without interference from other modules.

The second byte received by the servo communication module is the address of the transmitter. This is cross referenced against the register of active addresses. The feedback data is stored in a character buffer and when feedback has been received from all active addresses the module switches to feedback transmit mode.

## Feedback Transmit Mode

In feedback transmit mode all buffered feedback from servo control modules is transmitted to the host PC via USART and USB for analysis. Once all data is transmitted the servo communication module is switched back to instruction receive mode. The module is then ready to repeat the processes for the next set of instructions. If feedback has not been received by the host PC for a period equal to two interpolation cycle times an error report is displayed on the machine GUI.

### 7.16 Servo Control Modules: Software Routines

The software system on servo control modules is concerned with the execution of position control instructions that have been received from the host PC. A position control instruction is composed of an axial increment and a time for the motion to be achieved. The cycle of periodically updating these instructions is known as an interpolation cycle, and the time specified for the increment to be achieved corresponds to the interpolation cycle time. Operations associated with position control include:

- the receiving and interpretation of instructions,
- the periodic execution of the position control algorithm,
- the monitoring of encoder feedback,
- the generation of a PWM signal to H-bridge motor drivers based on the output of the position control algorithm and
- collision detection.


## Position Control



Figure 7.11: Cascade Structure for Closed Loop Servo Control
The position control of an axis is achieved by the cascaded control system of Figure 7.11. The outer loop is the position control loop while the inner loop is the speed control loop. Speed control is therefore inherent in achieving position control, and the feed rates prescribed through user programs are preserved. The efficiency of the cascaded structure for closed loop servo control depends primarily on the speed and stability of the inner control loop. A slow response on the inner loop reduces machining accuracy around circles and corners, where a rapid change in the position reference is expected.

The transfer function for a typical axis $P(s)$, is given by equation 7.19 where $K$ is an electromotive constant, $J$ is the moment of inertia of the mechanical system about the axis of the motor, $b$ is a damping coefficient of the mechanical system, $L$ is the motor inductance and $R$ is the electrical resistance [73]. The values of these constants for the DC motors used in the MRM platform were unknown, but were not necessary for the control of the system.

$$
\begin{equation*}
P(s)=\frac{K}{(J s+b)(L s+R)+K^{2}} \tag{7.19}
\end{equation*}
$$

The position control loop in the system contained a proportional controller $K_{p p}$ while a PID controller was implemented on the inner speed control loop. The transfer function of the PID controller is defined by equation 7.20 , where $K_{p}, K_{i}$ and $K_{d}$ are the gains of the controller (coarse tuned by the Ziegler-Nichols method and fine tuned by trial).

$$
\begin{equation*}
G(s)=K_{p}+\frac{1}{s} K_{i}+s K_{d} \tag{7.20}
\end{equation*}
$$

The controller was reduced to a discrete format for implementation in software. The z-transform of the controller was obtained by determining the z -transforms of the individual terms:

$$
\begin{gather*}
K_{p} \Rightarrow K_{p}  \tag{7.21}\\
\frac{K_{i}}{s} \Rightarrow \frac{K_{i} T}{1-z^{-1}}  \tag{7.22}\\
K_{d} s \Rightarrow \frac{K_{d}\left(1-z^{-1}\right)}{T} \tag{7.23}
\end{gather*}
$$

The transfer function of the controller in the discrete time domain is given by equation 7.24 , where $T$ is the sampling time for the control loop:

$$
\begin{equation*}
G(z)=K_{p}+\frac{K_{i} T}{1-z^{-1}}+\frac{K_{d}\left(1-z^{-1}\right)}{T} \tag{7.24}
\end{equation*}
$$

The transfer function may be written in the more convenient form of equation 7.25 , where the constants $K_{0}, K_{l}$ and $K_{2}$ are calculated by equations 7.26-28.

$$
\begin{gather*}
G(z)=\frac{K_{0}+K_{1} z^{-1}+K_{2} z^{-2}}{1-z^{-1}}  \tag{7.25}\\
K_{0}=K_{p}+K_{i} T+\frac{K_{d}}{T}  \tag{7.26}\\
K_{1}=-K_{p}-\frac{2 K_{d}}{T}  \tag{7.27}\\
K_{2}=\frac{K_{d}}{T} \tag{7.28}
\end{gather*}
$$

The error $e$ is the input to the PID controller and $u$ is the output, therefore:

$$
\begin{equation*}
G(z)=\frac{u}{e}=\frac{K_{0}+K_{1} z^{-1}+K_{2} z^{-2}}{1-z^{-1}} \tag{7.29}
\end{equation*}
$$

By manipulating equation 7.29:

$$
u(n)-u(n-1)=K_{0} e(n)+K_{1} e(n-1)+K_{2} e(n-2)
$$

The output for the PID controller at the $\mathrm{n}^{\text {th }}$ iteration is therefore calculated by equation 7.30 :

$$
\begin{equation*}
u(n)=u(n-1)+K_{0} e(n)+K_{1} e(n-1)+K_{2} e(n-2) \tag{7.30}
\end{equation*}
$$

By substituting the constants $K_{0}, K_{1}$ and $K_{2}$ into equation 7.30 the output of the controller is then given by equation 7.31:

$$
\begin{align*}
u(n)= & u(n-1)+K_{p}(e(n)-e(n-1))+K_{i} T e(n) \\
& +\frac{K_{d}}{T}(e(n)-2 e(n-1)+e(n-2)) \tag{7.31}
\end{align*}
$$

Equation 7.31 is recursive, where the output of the controller $u(n)$ is dependent on the output of the previous iteration $u(n-1)$. Based on the condition that $u(0)=0$ and $e(0)=0$, equation 7.31 is further reduced:

$$
\begin{equation*}
u(n)=K_{p} e(n)+K_{i} T \sum_{i=1}^{n} e(i)+\frac{K_{d}}{T}(e(n)-e(n-1)) \tag{7.32}
\end{equation*}
$$

Equation 7.32 was implemented on servo control modules for position control. The output $u(n)$ was used to set the duty cycle of PWM signals to motor drivers, which ultimately regulates the speed of the motors. The variable $e(n)$, which is the input to the PID controller is calculated by equation 7.33 :

$$
\begin{equation*}
e(n)=K_{p p} \cdot E(n)-\frac{\Delta X_{m}(n-1)}{T} \tag{7.33}
\end{equation*}
$$

$E(n)$ is the error in the existing position of an axis with regard to the reference position that is specified in position control instructions. This is calculated by equation 7.34, where $i$ is the iteration number and $\Delta X_{m}$ is the axial increment that was measured for that iteration.

$$
\begin{equation*}
E(n)=R e f-\sum_{i=1}^{n-1} \Delta X_{m}(i) \tag{7.34}
\end{equation*}
$$

The reference input Ref, to the position control algorithm is dependent on the type of motion required. Rapid motions are used to move a machine axis from one point to another quickly, without the observance of a target feed rate. In this instance the reference is provided by the step function of equation 7.35 . For interpolated motions the program feed rate is observed and the reference is provided by the discrete ramp function of equation 7.36. Figure 7.12 illustrates both step and discrete ramp references as functions of time.

$$
\begin{gather*}
\text { Ref }=0 \quad\left(t<T_{\text {step }}\right)  \tag{7.35}\\
\text { Ref }=\Delta X_{\text {ideal }} \quad\left(t \geq T_{\text {step }}\right) \\
\operatorname{Ref}=\sum_{i=1}^{n} \Delta X_{o}(i) \tag{7.36}
\end{gather*}
$$



Figure 7.12: Reference to Position Control Loop

## Signal Sampling

The ATmega 8L chip on servo control modules was responsible for the monitoring of feedback from position encoders. Encoder pulses were counted on an external interrupt basis and each interrupt incremented the pulse count by one. For all MRM axes, 512 pulses corresponded to one full revolution of a motor shaft. Equation 3.37 and 3.38 relate the pulse count to linear and angular increments respectively, where $L$ is the pitch of a power screw (mm) and $N$ is a reduction ratio.

$$
\begin{gather*}
\Delta X_{m}=L \frac{\text { count }}{512}  \tag{7.37}\\
\Delta \theta_{m}=360 \mathrm{~N} \frac{\text { count }}{512} \tag{7.38}
\end{gather*}
$$

Pulse counts were transmitted from the ATmega 8L chip to the ATmega 32L chip every 100 ms for position calculations. The position control algorithm was therefore executed every 100 ms upon the receiving the data. The transmission was driven by a 16-bit timer counter on the ATmega 8L chip that triggered software interrupt. The software interrupt transmitted the updated pulse count via USART.

## PWM Signal Generation

The output of the position control algorithm $u(n)$ was used to regulate the duty cycle of the PWM signal to H-Bridge motor drivers, thus enabling the control of motor speed and ultimately axis position. Phase and frequency correct PWM was executed on the ATmega 32L chip, by using the 16-bit timer/counter unit. The Input Capture Register (ICR) was used to set the TOP value, which defines the frequency of the PWM signal. The frequency of the PWM is calculated by equation 7.39, where $N$ is a pre-scalar and $f_{\text {clk_ } / / O}$ is the operating frequency of the chip [67].

$$
\begin{equation*}
f_{P W M}=\frac{f_{c l k_{l} / O}}{2 \cdot N . T O P} \tag{7.39}
\end{equation*}
$$

The operating frequency of the chip was 4 MHz , which was pre-scaled by eight. The TOP value on the ATmega 32 chip was set to 10000 resulting in a PWM frequency of 25 Hz . The Output Compare Register (OCR1A) was used to set the duty cycle of the PWM according to equation 7.40. The equation relates the integer value of the register to $u(n)$, and $K$ is a scaling factor. The duty cycle is then given as a percentage by equation 7.41.

$$
\begin{gather*}
\text { OCR1A }=K . u(n)  \tag{7.40}\\
\text { Duty Cycle }=\frac{O C R 1 A}{T O P} \times 100 \% \tag{7.41}
\end{gather*}
$$

## Collision Detection

Collision detection was enabled for individual axes, but not for the system at large. Individual axes contained limit switched that were connected to the external interrupt pins of the ATmega 32 L chip. When a collision occurs at the end of an axis range, the limit switch generates a signal on an interrupt pin, initializing the external interrupt service routine. This routine stops the generation of the PWM signal, transmits an error message to the host PC and returns the servo control module to an inactive state ready for the receipt of further instructions.

### 7.17 Spindle Control Modules: Software Routines

## Switching Operations

Spindle control modules activated and deactivated the motors of the MRM cutting heads via relay switches. The software routine associated with the switching operation was uncomplicated as digital speed control was omitted from the system. Two pins on the ATmega 32L microcontroller were used to activate either clockwise or anticlockwise spindle rotation. The states of the pins were varied in software by setting the related port registers to suitable values using appropriate bitwise operations.

## ADC and Vibration Monitoring

Spindle control modules were responsible for monitoring the vibrations in MRM process modules during machining operations. The vibration data would ideally be used in adaptive control to alter spindle speeds and tool feed rates to reduce the vibrations to acceptable levels. The creation of adaptive control routines was out of the scope of this research and vibration data was collected only for display on the user interface. A practical analysis of mechanical vibrations in MRMs was also out of the scope of this research (theoretical analysis in Section 5.12). The inclusion of a vibration monitoring system was only to reinforce the principle of diagnosability in MRMs.

The output channels of the ADXL204 dual-axis accelerometer were connected to the Analogue to Digital Converter (ADC) terminals of the local ATmega 32L microcontroller board. Only the axis and channel of interest was connected by manually configuring the electrical connections to the microcontroller. The reading of an ADC port was initialized by a 16-bit timer on the chip, and measurements were obtained at a frequency of 100 Hz . The ADC hardware converted the analogue input voltage to a 10-bit value through successive approximation [67]. The acceleration $a$ of an axis was calculated by equation 7.42 , where $g$ is gravity, $n$ is the number of bits dedicated to the $\mathrm{ADC}, \quad V_{\text {ref }}$ is the ADC reference voltage and $V_{\text {nom }}$ is the nominal voltage of the accelerometer.

$$
\begin{equation*}
a=g\left(V_{\text {ref }} \frac{A D C_{-} \text {Ouput }}{n^{2}}-V_{\text {nom }}\right) \tag{7.42}
\end{equation*}
$$

The accelerations on an axis were converted into an absolute value $M$. The maximum magnitude registered in a one second cycle was then transmitted to the host PC for update on the user display.

The transmission was triggered by the same software interrupt the initializes the reading of the ADC ports (maximum magnitude per 100 readings $=$ maximum magnitude registered in one second). The data was transferred to the host PC via USART and USB.

Appendix F. 5 contains a sample graph of accelerometer measurements obtained from the drilling head, when the spindle was unloaded and allowed to rotate at maximum speed (approximately $580 \mathrm{rev} / \mathrm{min}$ ).

### 7.18 Chapter Summary

This chapter presented the software system that was created for MRMs. The focus of the software implementation was on hardware abstraction to minimize the reconfigurability required at a software level. Hardware abstraction was achieved by the definition of control and communication protocols and the appropriate distribution of generic and module specific software functions between the host PC and distributed control drives. Matters of user programming and reconfiguration were addressed and a complete overview of the software system was provided. The algorithms that were implemented on the host PC and control drives were also presented.

## 8. System Assembly and Performance

### 8.1 System Assembly and Reconfiguration: An Overview



Figure 8.1: A Complete Overview of the MRM Assembly/Reconfiguration Procedure
The assembly of an MRM platform begins with a description of the product that is to be machined. Section 5.8.1 presented a methodology based on the research of Moon and Kota [42], whereby information on the desired tool trajectory is used to identify the essential mechanical modules for the assembly of a kinematically viable machine tool. Once the modules have been identified they are assembled by means if a series of standardized bolted interfaces.

All MRM platforms contain one process module (cutting head), and require a single spindle control module to manage its operation. The spindle control module is connected to the cutting head by means of the standard power and control interfaces: an eight wire connection for DC modules, and an eleven wire connection for AC modules. The spindle control module is then connected to the power supply system and finally to the host PC via USB.


Figure 8.2: Mechanical and Electronic Assemblies
a. Assembled mechanical system showing power and control connections to modules
b. Assembled electronic control system
c. Servo communication module showing connections to I2C network
d. Spindle control module showing incoming eight wire connection form drilling head

Each axis in a MRM requires a servo control module to manage its operation and only the exact number needed should be present on a platform. Servo control modules connect to their respective mechanical modules by means of an eight wire power and control connection. Once connected, servo control modules are then connected to the DC power supply system. Servo control modules are finally plugged into the I2C bus, with the physical connection points being present on an associated servo communication module. All MRM configurations contain at least one servo communication module. The communication module is connected to the power supply system, and interfaced with the host PC via USB, during assembly. Figure 8.2 illustrates aspects of the mechanical and electronic assembly.


Figure 8.3: Initialization of Machine Configuration on Host PC
After the complete assembly of the mechanical and electrical systems the user is required to reconfigure the active NC command set. This is achieved by selecting the axes configurations from drop down menus on the machine GUI illustrated in Figure 8.3. Thereafter the USB addresses of the servo and spindle ports are set and an interpolation cycle time is specified for the machine. Prior to user programming the G10 command must be entered in the code window and executed. This command causes all axes to move to their respective home positions. The position of the machine spindle relative to the work table is then calculated and manually entered into the position database file, thus enabling absolute programming. This completes the assembly of the platform. During MRM reconfiguration, the procedure is the same as the assembly procedure outlined in Figure 8.1; however individual stages that are not necessary may be omitted. A new MRM configuration must always be initialized in software before operation.

### 8.2 Pairing of Mechanical and Control Modules

Servo and spindle control modules match to mechanical modules on a $1: 1$ basis. During MRM assembly, control modules are paired with mechanical modules and those pairs must be maintained throughout successive reconfigurations. Although generic servo and spindle control programs were implemented on distributed control drives, these programs require module specific information to complete their respective functions. For example a servo control module would contain information on the mechanical ratios (gear ratios, screw pitch, etc) of a module as well as PID tuning constants. The ATmega 32L microcontrollers on servo and spindle control modules are programmed with module specific information and if a control module is to be used to manage a different unit of mechanical hardware, the microcontroller must be swapped or reprogrammed with the correct data.

### 8.3 Machine Calibration

MRMs are reconfigured by the addition and removal of mechanical modules from a platform. To ensure a swift system ramp-up after reconfiguration, techniques must be employed for process debugging and optimization. For tool positioning errors, a kinematic calibration of the machine tool is required.

Machine Calibration typically requires the following steps:
(i) Modelling: mathematical model that describes the machines geometry and motion.
(ii) Measurement: of the tool position in the workspace.
(iii) Identification: understanding the relationship between axial positions and the tool position.
(iv) Compensation: implementing the modified control program to ensure accurate task completion.

The mathematical model of a machines geometry and motion is encapsulated in its homogenous transformation matrix. The measurement of the tool or spindle position in the workspace is achieved by traditional laser measurement techniques that are already used in CNC calibration procedures. The discrepancy between the measured tool position and the ideal tool position may be resolved into a set of linear and angular offsets. These offsets are related to individual axes and the true position of an axis is reprogrammed on its associated servo control module.

### 8.4 System Performance Criteria and Errors

The performance of a machine tool is primarily evaluated with regard to spindle power and the accuracy, repeatability, maximum torque and maximum speed of its axes. The power, torque, speeds and other loading specifications for MRM modules were presented in Chapter 5. This chapter focuses on the performance of the MRM positioning systems for dynamic accuracy, as well as static accuracy and repeatability. An MRM positioning system consists of:

- the host PC which provides position instructions,
- the servo communication module which facilitates the transmission of instructions and enables the synchronized execution of these instructions,
- servo control modules which execute the position control algorithm and
- mechanical axes (motion modules), which position the cutting tool relative to the work part.

The accuracy and repeatability of a machine tool is dependant on the first order mechanical errors and control errors that are introduced during the positioning of the cutting tool. First order mechanical errors are a result of static deflections in the machine structure, errors that have been introduced due to the inaccurate assembly of the machine, backlash between mechanical components and thermal errors. Second order mechanical errors are a result of the dynamic interaction of the cutting tool with the work piece and generally affect the surface finish of a machined part.

Control errors are composed of truncation errors, linearization and tracking errors. Truncation errors are introduced by the limitation of measurement systems and rounding off during calculations. On MRMs truncation errors were introduced by the necessity to reduce axial increments to discrete pulse counts to be achieved by individual axes. Pulse counts are an integer value and the remainder is truncated. The truncation errors on MRMs were therefore limited in size to the increment associated with a single pulse count. This increment is often referred to as the Basic Length Unit (BLU) of an axis.

Linearization errors are a result of the linear approximation of curves. The chord height error and radial error are two particular errors that are characteristic of circular interpolation. The chord height error is an inherent error in the circular interpolation algorithm and its value is an indication of the maximum deviation of the reference path generated by the interpolator, as compared to the ideal tool path. The radial error is in indication of the difference in radii between the measured tool path and an ideal arc. The radial error is also an inherent error in the linear approximation; however when it is computed at the start and end positions of a linear segment it is reflective of a truncation error.

Tracking errors are errors between a reference trajectory and the actual axis/tool trajectory. These errors are a result of the incorrect tuning of the control algorithm, inertia in the mechanical system, uneven friction in slides and irregular loading. These errors are particularly prominent during the acceleration and deceleration of an axis. The effect of tracking errors is overshoot in the target position and a general discrepancy between the ideal and actual position of the cutting tool at time $t$.

The final significant factor with regard to machine performance is the ability of the positioning system to maintain calibration. A drift in machine calibration occurs due to backlash between mechanical components and the cumulative effect of uncertainty in position measurements. This uncertainty is inherent in measurement systems as the smallest measurable increment in position is limited to one BLU. Calibration errors are characterized by high repeatability and poor accuracy in the positioning system.

### 8.5 Control Performance: Interpolated Motion

Interpolated motions are motions where reference to the speed control algorithm is incremented by $\Delta X$ or $\Delta \theta$ in each interpolation cycle, resulting in a discrete ramped input to the position control algorithm. The objective of this mode of control is to achieve the user prescribed feed rate for the cutting tool. The performance of individual axes for interpolated motions was investigated.

Statistical tools that were used in the analysis included an evaluation of the average value of a set of measurements and the standard deviation. The average and standard deviation of a set of measurements are calculated by equations 8.1 and 8.2 respectively, where $x$ is a generic variable, $n$ is the number of measurements and $s$ is the standard deviation.

$$
\begin{gather*}
\bar{x}=\frac{1}{n} \sum_{i=1}^{n} x_{i}  \tag{8.1}\\
s=\sqrt{\frac{1}{n-1} \sum_{i=1}^{n}\left(x_{i}-\bar{x}\right)^{2}} \tag{8.2}
\end{gather*}
$$

## Linear Axes (Dynamic Analysis)



Figure 8.4: Graph of Position vs Time: Base Module (+X Direction)


Figure 8.5: Graph of Speed vs Time: Base Module (+X Direction)


Figure 8.6: Graph of Position Error vs Time: Base Module (+X Direction)

The dynamic performance of the linear axes was investigated for interpolated motion. The graphs presented in Figures 8.4-6 demonstrate the performance of the base module. The interpolation was performed for a distance of 100 mm at an axis feed rate of $100 \mathrm{~mm} / \mathrm{min}$. This feed rate was selected for testing as it is the original upper speed specification for linear modules (see Section 4.3). Furthermore it is at higher end of the axis speed range (not the highest speed) and errors are prominent in the accelerated and decelerated regions of the trajectory. Figure 8.4 illustrates the measured position of the axis with regard to time. Figure 8.5 illustrates the measured speed of the axis with regard to time. The speed of the axis oscillated about the reference speed of 100 $\mathrm{mm} / \mathrm{min}$. The average speed of the trajectory was $100.15 \mathrm{~mm} / \mathrm{min}$ with a standard deviation of $10.31 \mathrm{~mm} / \mathrm{min}$.

An uneven friction characteristic displayed by the module drive mechanism is the primary cause of the oscillations. The number of oscillations in the curve of Figure 8.5 is equal to the number of power screw revolutions that were required to complete the movement, confirming that the origin is in the mechanical system and not instability in the control system. Figure 8.6 illustrates the position error of the axis (tracking error) with regard to time, where the position error $E_{p}$, at interpolation cycle $i$, is defined by equation 8.3. The highest position errors occurred in the accelerated and decelerated regions of the trajectory. These errors were 0.58 mm and -0.41 mm respectively.

$$
\begin{equation*}
E_{p}(i)=\sum_{i=1}^{n} \Delta X_{o}(i)-\sum_{i=1}^{n} \Delta X_{m}(i) \tag{8.3}
\end{equation*}
$$

The test data that was used to generate Figures 8.4-6 is located in Appendix F.6. The performance graphs of other linear axes are also located in Appendix F. Please not that only a sample of the test data collected during testing is located in this appendix due to the extensive amount of data that was collected; the test data for other axes is located on the supplementary DVD.

Table 8.1: Speed Control Performance of Linear Modules for Interpolated Motion

| Module | Program Speed <br> $(\mathrm{mm} / \mathrm{min})$ | Distance <br> $(\mathbf{m m})$ | Average Speed <br> $(\mathrm{mm} / \mathrm{min})$ | Avg Speed <br> Prog <br> Speed | Std Dev: Speed <br> $(\mathrm{mm} / \mathrm{min})$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Base | 100 | +100 | 100.15 | $100.15 \%$ | 10.31 |
|  | 100 | -100 | 97.89 | $97.89 \%$ | 14.16 |
|  | 25 | +100 | 23.40 | $93.60 \%$ | 4.38 |
|  | 25 | -100 | 23.42 | $93.68 \%$ | 2.63 |
|  | 100 | +100 | 96.66 | $96.66 \%$ | 21.26 |
|  | 100 | -100 | 96.01 | $96.01 \%$ | 22.45 |
| Column Slide | 25 | +100 | 24.49 | $97.96 \%$ | 4.87 |
|  | 25 | -100 | 24.61 | $98.44 \%$ | 3.82 |
|  | 100 | +100 | 96.49 | $96.49 \%$ | 18.54 |
|  | 100 | -100 | 94.47 | $94.47 \%$ | 16.94 |
|  | 25 | +100 | 24.61 | $98.44 \%$ | 4.21 |
| Cross Slide | 25 | -100 | 24.63 | $98.82 \%$ | 4.09 |
|  | 100 | +50 | 96.82 | $96.82 \%$ | 13.92 |
|  | 100 | -50 | 94.95 | $94.95 \%$ | 19.25 |
|  | 25 | +50 | 23.34 | $93.36 \%$ | 2.20 |

Tables 8.1 and 8.2 summarize the performance of all linear axes in the MRM module library for interpolated motion. Table 8.1 presents data on the performance of linear axes with regard to speed control for higher and lower speeds. The average speeds of the axes were computed for the specified distances. For speeds of $100 \mathrm{~mm} / \mathrm{min}$ the axes exhibited an average speed that was in a range of $94.47 \%$ to $100.15 \%$ of the program speed. At the slower speed of $25 \mathrm{~mm} / \mathrm{min}$ the axes exhibited an average speed of $92.88 \%$ to $98.82 \%$ of the program speed. Deviations from the user specified speeds are inevitable due to axis acceleration and deceleration. The execution of deceleration control on the MRM platform is an example of an intentional and controlled deviation from the user specified speed. Deviations from the program speed are also caused by the controller compensating for errors such that the target position is achieved in precedence to the prescribed feed rate.

All linear axes displayed an oscillation in speed during operation. The standard deviation represents the average amplitude of these oscillations with regard to the average speed. The standard deviation of the axes speeds is significantly higher at increased speeds. For a program speed of $100 \mathrm{~mm} / \mathrm{min}$ the standard deviation was in a range of $10.31 \mathrm{~mm} / \mathrm{min}$ to $22.45 \mathrm{~mm} / \mathrm{min}$, while for a program speed of $25 \mathrm{~mm} / \mathrm{min}$ the standard deviation of the axes speeds was in a range of $2.20 \mathrm{~mm} / \mathrm{min}$ to $5.87 \mathrm{~mm} / \mathrm{min}$. The oscillations exhibited in the speed and position error graphs for all linear axes was attributed to an uneven friction characteristic in the drive mechanisms (see Appendix F.1). The standard deviation may be reduced with the use of higher quality power screws in linear axes as opposed to the low cost ISO metric threaded bar that was used in the present design.

The motors used in the axes were generally underpowered and exhibited rise times in excess of 500 ms when accelerating to target speeds. The lower torques exhibited by the motors at higher speeds contributed to greater deviations from the program feed rate at these speeds.

Table 8.2: Position Control Performance of Linear Modules for Interpolated Motion

| Module | Program <br> Speed <br> $(\mathbf{m m} / \mathbf{m i n})$ | Distance <br> $(\mathbf{m m})$ | Max Pos <br> Error <br> $(\mathbf{m m} / \mathbf{m i n})$ | Avg Pos <br> Error <br> $(\mathbf{m m} / \mathbf{m i n})$ | Final Pos <br> Error <br> $(\mathbf{m m})$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 100 | +100 | 0.581 | 0.053 | -0.015 |
|  | 100 | -100 | 0.439 | 0.040 | -0.015 |
|  | 25 | +100 | 0.186 | 0.017 | -0.015 |
| Work Table | 25 | -100 | 0.112 | 0.011 | -0.020 |
| Slide | 100 | +100 | 0.527 | 0.082 | -0.023 |
|  | 100 | -100 | 0.527 | 0.089 | -0.018 |
|  | 25 | +100 | 0.158 | 0.033 | 0.000 |
| Column | 25 | -100 | 0.182 | 0.037 | -0.012 |
|  | 100 | +100 | 0.586 | 0.077 | -0.023 |
|  | 100 | -100 | 0.633 | 0.070 | -0.006 |
|  | 25 | +100 | 0.187 | 0.030 | -0.023 |
|  | 25 | -100 | 0.211 | 0.032 | -0.018 |
|  | 100 | +50 | 0.453 | 0.116 | -0.023 |
|  | 100 | -50 | 0.359 | 0.035 | -0.086 |
|  | 25 | +50 | 0.156 | 0.007 | -0.020 |

Table 8.2 presents data on the performance of position control for interpolated motion. The maximum position errors occurred consistently in the accelerated regions of individual trajectories. The maximum position errors for program speeds of $100 \mathrm{~mm} / \mathrm{min}$ were in a range from 0.0359 mm to 0.633 mm , while for program speeds of $25 \mathrm{~mm} / \mathrm{min}$ the maximum position errors for individual trajectories were in a range from 0.112 mm up to 0.211 mm .

The magnitude of the maximum position errors at the higher speed are attributed to the slow acceleration exhibited by the drive motors. These errors may be reduced by the implementation of higher powered, geared servo motors. The average position errors for individual trajectories were computed as an average of the magnitude (absolute value) of individual position errors during a trajectory. At the higher speed the average position errors for individual trajectories were in a range from 0.035 mm up to 0.116 mm . For the lower speed these errors were in a range from 0.007 mm up to 0.037 mm .

The errors in the final position of the axes at the end of an interpolation were in similar ranges for both lower and higher speeds. These errors are negative indicating that an overshoot of the final target position has occurred. The errors in the final position for individual trajectories were in a range from 0.000 mm up to 0.086 mm . Note that all the errors that have been presented thus far have been determined from data that has been extracted from the control system, this data does not account for mechanical errors.

## Rotary Axes (Dynamic Analysis)



Figure 8.7: Graph of Angular Position vs Time: Rotary Table Module (+C/ $\boldsymbol{\alpha}$ Direction)
An investigation of the dynamic performance of rotary axes was performed for interpolated motion. Figures $8.7-9$ provide a sample of the performance curves for position control, speed control and position errors generated from the testing of rotary axes. These figures illustrate the performance of the rotary table module for an interpolation of $360^{\circ}$ at a target speed of $0.75 \mathrm{rev} / \mathrm{min}$. For this interpolation the rotary table achieved an average speed that was $93.73 \%$ of its program speed with a standard deviation of $0.086 \mathrm{rev} / \mathrm{min}$. The maximum error in angular position was $0.086^{\circ}$ which occurred in the deceleration phase of the trajectory as illustrated in Figure 8.9. Sample data and the performance graphs of other rotary modules are located in Appendix F2 and F6.


Figure 8.8: Graph of Speed vs Time: Rotary Table Module ( $+\mathbf{C} / \alpha$ Direction)


Figure 8.9: Graph of Angular Position Error vs Time: Rotary Table Module (+C/ $\alpha$ Direction)
Tables 8.3 and 8.4 summarize the results of individual performance tests on all rotary modules. It should be noted that the performance results provided are only for a single speed per module, as position errors have already been shown to increase with an increase in reference speed, particularly in the acceleration and deceleration regions of a trajectory.

Table 8.3: Speed Control Performance of Rotary Modules for Interpolated Motion

| Module | Program <br> Speed <br> (rev/min) | Angle <br> (Degrees) | Average <br> Speed <br> (rev/min) | Avg Speed <br> Prog <br> Speed | Std Dev: <br> Speed <br> (rev/min) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Cutting | 10 | +360 | 8.973 | $89.73 \%$ | 2.680 |
| Head Rotary | 10 | -360 | 9.109 | $91.09 \%$ | 2.516 |
| Tilt Table | 15 | +90 | 10.798 | $71.99 \%$ | 6.584 |
|  | 15 | -90 | 10.076 | $67.17 \%$ | 7.042 |
| Rotary Table | 0.75 | +360 | 0.703 | $93.73 \%$ | 0.086 |
|  | 0.75 | -360 | 0.700 | $93.33 \%$ | 0.093 |

The cutting head rotary module and the tilt table module both possessed direct drive mechanisms, while the rotary table module was driven via a reduction gearbox. A reduction gearbox was necessary in the rotary table module as the axis of motor shaft was perpendicular to the axis of rotation on the module's moving interface. An already available worm gearbox was used in the module to reduce development costs and the reduction ratio limited the maximum rotary speed of this module to $1.07 \mathrm{rev} / \mathrm{min}$. The tilt table module and the cutting head rotary module were both capable of speeds of $60 \mathrm{rev} / \mathrm{min}$, however program speeds of greater than $10 \mathrm{rev} / \mathrm{min}$ to $15 \mathrm{rev} / \mathrm{min}$ resulted in excessive position errors in interpolated motions. For a program speed of $10 \mathrm{rev} / \mathrm{min}$, the cutting head rotary module achieved an average speed in the region of $90 \%$ of its target speed. The standard deviations of $2.680 \mathrm{rev} / \mathrm{min}$ and $2.515 \mathrm{rev} / \mathrm{min}$ for clockwise and anticlockwise motion both indicate an uneven friction characteristic in the module's mechanical system.

The tilt table module displayed significantly greater standard deviations in its speed characteristics and only achieved average speeds in the region of $70 \%$ of the target speed. Both the cutting head rotary and tilt table modules displayed a "slip-stick" effect in the reaction of the axes to friction. The "slip-stick" effect in the axes indicated that the drive motors did not possess sufficient torque for a direct drive system. On the contrary the rotary table module displayed a low standard deviation in its speed, as this module possessed the advantage of torque amplification which resulted in a relatively smooth trajectory.

Table 8.4: Position Control Performance of Rotary Modules for Interpolated Motion

| Module | Program <br> Speed <br> (rev/min) | Angle <br> (Degrees) | Max Pos <br> Error <br> (Degrees) | Avg Pos <br> Error <br> (Degrees) | Final Pos <br> Error <br> (Degrees) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Cutting <br> Head Rotary | 10 | +360 | 14.766 | 5.698 | -0.703 |
| Tilt Table | 10 | -360 | 12.656 | 5.742 | -0.703 |
|  | 15 | +90 | 11.250 | 6.228 | -1.406 |
| Rotary Table | 15 | -90 | 12.656 | 6.797 | -0.703 |
|  | 0.75 | +360 | 0.942 | 0.062 | -0.083 |

The "slip-stick" effect in addition to the low acceleration of the drive motors resulted in large maximum and average position errors for the cutting head rotary module and the tilt table module. The lower operating speed and higher torque of the rotary table resulted in a drastic difference in the positioning accuracy of this axis as compared to the other modules. At increased program speeds the effect of poor acceleration is more pronounced in position accuracy. The cutting head rotary module and tilt table module both possessed direct drive mechanisms and which ultimately made them difficult to control at speeds lower than $5 \mathrm{rev} / \mathrm{min}$. The advantage of improved position control at low speeds was therefore not realized with these modules.

The cutting head rotary module and tilt table module displayed errors in the region of $-0.703^{\circ}$ to $1.406^{\circ}$ in their final positions. These errors are relatively small compared to the errors exhibited during the motion of the axes. This indicated that the system was still effective in stopping the axes once the required encoder pulse counts had been achieved.

### 8.6 Control Performance: Rapid Point to Point Motion Control

Tests were performed to determine the accuracy of individual axes for point to point motion control. In point to point motion control the axes are moved rapidly to target positions without observing a target feed rate. The objective is to move the axes to the programmed positions as quickly and as accurately as possible. The position control software on servo control modules limited the maximum reference input to the cascade control loop, resulting in axes displaying linearly incrementing position characteristics over larger movements in distance. Figures 8.10 and 8.11 illustrate the position control characteristics for the base module and cutting head rotary module. The sample characteristics illustrate a highly linear profile for the 40 second trajectory of the base module, while a s-shaped characteristic is displayed for the 1.8 second trajectory of the cutting head rotary module.


Figure 8.10: Graph of Position vs Time, Point to Point Control of Base Module (+X Direction)


Figure 8.11: Graph of Position vs Time, Point to Point Control of Cutting Head Rotary Module ( $+\mathbf{A} / \gamma$ Direction)
The position control software was designed to continue the execution of the control algorithm until a position equal to the target position was achieved or an overshoot of the target position had occurred. Position control errors were therefore always overshoot errors. The H-Bridges used to drive the motors could not provide a rapid change in the direction of motor rotation, and the position control loop was not used to compensate for the overshoot.

Figures 8.12 and 8.13 demonstrate the average and maximum position errors for rapid point to point motion motions in linear and rotary axes respectively. The position errors were calculated by equation 8.4 which determines the difference between the reference position provided by the control system and the position obtained from encoder measurements.

$$
\begin{equation*}
E_{p}\left(t_{\text {final }}\right)=\Delta x_{\text {ideal }}-\Delta x_{\text {measured }} \tag{8.4}
\end{equation*}
$$

The graphs have been generated from eight tests being performed on individual axes across various distances. Refer to Appendix F. 3 to locate the data from individual tests, note that this data has been obtained from the control system and does not account for mechanical errors.


Figure 8.12: Graph of Overshoot in Final Position for Point to Point Control of Linear Axes


Figure 8.13: Graph of Overshoot in Final Position for Point to Point Control of Rotary Axes

Tests were performed on linear axes across distances of 25 mm up to 100 mm . The distribution of the overshoot errors showed no specific trend with increases in distance. The overshoot of an axis depended primarily on the inconsistencies of localized friction characteristics close to the target position. The maximum overshoot recorded for a linear axis was 0.059 mm by the column module, while the base module displayed the highest average overshoot error of 0.018 mm . The smallest errors were displayed by the cross slide module, which displayed the smoothest motion from all linear modules due to higher quality in its manufacturing. The cross slide module was a retrofitted commercially acquired unit of hardware.

Tests on rotary axes were performed for rotations of $45^{\circ}$ up to $360^{\circ}$. The highest overshoot error of $1.406^{\circ}$ was registered by the cutting head rotary module; which also displayed the highest errors on average. The rotary table module possessed a reduction gearbox and operated at relatively low speeds, it therefore displayed the smallest overshoot errors on average.

### 8.7 Control Performance: Synchronized Motion

## Linear Paths (Dynamic Analysis)

An investigation was performed to determine the combined accuracy for the synchronized motion of two axes. The synchronization of axes was performed by the servo communication module, which issued a synchronized start to axes by means of a general I2C call. Figure 8.14 illustrates the resultant position error from the synchronized motion of the base module and work table slide module in a MRM drilling configuration. The axes were required to move the drill spindle across a linear trajectory of 100 mm at a combined feed rate of $100 \mathrm{~mm} / \mathrm{min}$ (G-code: F100 X70.71 Y70.71). The resultant error from the trajectory was calculated by equation 8.5 . The equation does not account for mechanical errors and only presents the error from the perspective of the control system (tracking error).

$$
\begin{equation*}
E_{r e s}(i)=\sqrt{\left(\sum_{i=1}^{n} \Delta X_{o}(i)\right)^{2}+\left(\sum_{i=1}^{n} \Delta Y_{o}(i)\right)^{2}}-\sqrt{\left(\sum_{i=1}^{n} \Delta X_{m}(i)\right)^{2}+\left(\sum_{i=1}^{n} \Delta Y_{m}(i)\right)^{2}} \tag{8.5}
\end{equation*}
$$

The maximum resultant error in the position of the drill spindle was 0.429 mm and the trajectory was completed with an average position error of 0.069 mm . The average was computed on the magnitude (absolute value) of the errors.


Figure 8.14: Graph of Position Error (Drill Spindle) vs Time, Resultant Position of $X$ and $Y$ Axes


Figure 8.15: Graph of Position Error (Tool Post) vs Time, Resultant Position of $X$ and $Y$ Axes
Figure 8.15 illustrates the resultant position error from the synchronized motion of the base module and cross slide module in the MRM turning configuration. The axes were required to move the tool post (and tool) across a linear trajectory of 50 mm at a combined feed rate of $100 \mathrm{~mm} / \mathrm{min}$ (G-code: F100 X35.36 Y35.36). The maximum resultant error exhibited for the synchronized motion of these axes was 0.382 mm and the average error was 0.045 mm .

## Circular Interpolation (Dynamic Analysis)



Figure 8.16: Arc Generated by Synchronized Motion of Base Module and Work Table Slide Module
The performance of the MRM control system was investigated for circular interpolation. A test was performed for the interpolation of an arc of radius 100 mm with a subtended angle of $90^{\circ}$. The test was performed with the base module as the X -axis and the work table slide module as the Y -axis in the 3-DOF drilling configuration. The arc began with the drill spindle at relative position ( $\mathrm{x}=100 \mathrm{~mm}, \mathrm{y}=0 \mathrm{~mm}$ ) and ended at position ( $\mathrm{x}=0 \mathrm{~mm}, \mathrm{y}=100 \mathrm{~mm}$ ). The arc was linearized according to the circular interpolation algorithm and the linear segments were further interpolated according to the linear interpolation algorithm. Figure 8.16 illustrates the resultant arc that was described by the drill spindle in free space (drill not engaged with work part).

Figure 8.17 illustrates the resultant position error of the drill spindle during the formation of the arc. The position error accounts for tracking errors in the control system and is calculated by equation 8.5 . The position error graph is characterized by multiple peaks in the error throughout the trajectory. These peaks occur due to a rapid change in reference input to the position controller at the end of each linear segment in the arc. The arc of Figure 8.16 contained four distinct linear segments resulting in four peaks in the position error characteristic. The magnitude of the errors is highly dependant on the dominant axis (axis required to cover the greater distance) in an individual linear segment and the consistency of the error curve varied throughout the trajectory. The largest error registered for the trajectory was 0.241 mm .

The linearization of an arc generates inherent errors, causing the radius of the arc to deviate from the prescribed radius. The errors are present in the reference to the position control algorithm resulting in the final control error being a composite of both reference and tracking errors.


Figure 8.17: Graph of Position Error vs Time, Generation of Arc by $X$ and $Y$ Axes


Figure 8.18: Graph of Radial Error vs Time, Generation of Arc by $X$ and $Y$ Axes

Figure 8.18 illustrates the radial errors in the arc with regard to time. The radial error is calculated by equation 7.14 ; where the equation was used to calculate the error after every iteration of the position control loop. The curve is characterized by four peaks, corresponding to the four linear segments that were used to approximate the arc. The maximum radial error occurs at the middle of each segment resulting in a peak and the error at this point is also referred to as the chord height error (see equation 7.15). Chord height errors as large as 2.850 mm registered in the reference to the controller and the largest total error (reference error + tracking error) in the trajectory was 2.961 mm . The poor accuracy of the interpolated arc was primarily attributed to the circular interpolation algorithm used. For improved accuracy, a moving average fine interpolator may be implemented after the ITM algorithm has performed basic circular interpolation. More advanced algorithms such as the NURBS interpolator may also be implemented for the accurate linearization of curved paths [31].

### 8.8 Accuracy and Repeatability of Axes

The performance of a machine may be evaluated on the ability of its axes to accurately position the cutting tool and to provide a repeatable measure of accuracy during its operation. Sections 8.5 and 8.7 concentrated on the dynamic performance of the control system specifically, where the investigations explored the ability of the system to track target positions with regard to time for various control instructions. An investigation into the errors in the reference input to the control algorithm was conducted for circular interpolation. The errors resulting from the synchronized motion of two axes were also presented. Thus far, all results presented have only considered the magnitude of errors from the perspective of the control system. These errors did not account for mechanical inaccuracies in the positioning system. The accuracy and repeatability figures calculated in this section will account for mechanical errors, control errors and the control resolution of axes.

## Control Resolution

The control resolution $C R$ is defined as the distance that separates two adjacent control points (two encoder pulses) in the motion of an axis [61]. This distance corresponds to the machine BLU which is the smallest measurable increment in distance that may be detected by the control system. The control resolutions of individual axes in the MRM library have been previously presented in Tables 5.4-10. The control resolutions were calculated by equation 8.6 , where $N$ is the number of encoder pulses generated per motor revolution and $\Delta x$ is the axial increment associated with a single revolution.

$$
\begin{equation*}
C R=\frac{\Delta x}{N} \tag{8.6}
\end{equation*}
$$

The control resolution represents a limitation in the exactness of position measurements by the control system. The position of an axis will often lie between two control points and the error in the measurement is generally dealt with by adding $0.5 C R$ to the position error determined by the control system [61].

## Mechanical Errors

Mechanical errors are a result of static deflections, backlash between gears and general play between mating components in the positioning system of an axis.

For the purpose of determining the accuracy and repeatability of MRM modules only the errors resulting from backlash and play between mechanical components was considered. The mechanical errors were determined by measuring the maximum erroneous encoder readings that were generated by the play between components. The final mechanical errors for individual axes were then calculated by equation 8.7 , where $p$ is the number of pulses output by the encoders. The truncation effect of the control resolution was not compensated for in this equation and is dealt with later. These calculated errors are presented in Table 8.5

$$
\begin{equation*}
\max \left(E_{m}\right)=p . C R \tag{8.7}
\end{equation*}
$$

Table 8.5: Mechanical Errors Due to Backlash and Play between Mating Components

| Linear Modules | p | $\mathbf{C R}(\mathrm{mm})$ | $\max \left(\mathrm{E}_{\mathrm{m}}\right)(\mathrm{mm})$ |
| :---: | :---: | :---: | :---: |
| Base | 1 | $4.883 \times 10^{-3}$ | $4.883 \times 10^{-3}$ |
| Work Table Slide | 1 | $5.869 \times 10^{-3}$ | $5.869 \times 10^{-3}$ |
| Column | 1 | $5.869 \times 10^{-3}$ | $5.869 \times 10^{-3}$ |
| Cross Slide | 1 | $3.906 \times 10^{-3}$ | $3.906 \times 10^{-3}$ |
| Rotary Modules | p | $\mathbf{C R}(\mathrm{deg})$ | $\max \left(\mathrm{E}_{\mathrm{m}}\right)(\mathrm{deg})$ |
| Cutting Head Rotary | 1 | 0.703 | 0.703 |
| Tilt Table | 1 | 0.703 | 0.703 |
| Rotary Table | 8 | 0.0125 | 0.1 |

## Accuracy

The accuracy of an axis is defined as the maximum possible error that may occur between the target position specified in a user program and the actual position finally achieved by the axis [61]. The accuracy of CNC systems is commonly determined by equation 8.8 where $s$ is the standard deviation of the error distribution. This equation assumes $100 \%$ accuracy in the ability of the system to position the axis exactly to a prescribed encoder pulse count. The equation also assumes a mean error of zero and that $99.74 \%$ of the mechanical errors are within three standard deviations of the final control position.

$$
\begin{equation*}
\text { Accuracy }=0.5 C R+3 s \tag{8.8}
\end{equation*}
$$

Appropriate equipment and sufficient information to determine the standard deviation of the mechanical error was unavailable. The calculation of accuracy for MRM modules was therefore based on equation 8.9 which calculates the worst instance of accuracy displayed by an axis; this equation is still in agreement to the accepted definition of accuracy in NC machines. The maximum position error $E_{p}$ is the error in the final position of the axis as measured by the control system.

$$
\begin{equation*}
\text { Accuracy }=0.5 C R+\max \left(E_{m}\right)+\max \left(E_{p}\right) \tag{8.9}
\end{equation*}
$$

The repeatability of a positioning system may be defined as the ability of the system to return to a previously programmed position [61]. The repeatability of CNC systems is commonly determined by equation 8.10 . However, for MRM axes the repeatability was calculated by equation 8.11 which determines the worst measure of repeatability displayed by each axis.

$$
\begin{gather*}
\text { Repeatability }= \pm 3 s  \tag{8.10}\\
\text { Repeatability }= \pm\left[\max \left(E_{m}\right)+\max \left(E_{p}\right)\right] \tag{8.11}
\end{gather*}
$$

The maximum position error $E_{p}$ as measured by the control system was determined from multiple tests on individual axes; the results of the individual tests are located in Appendix F.4. These tests were performed at controlled speeds (interpolated motion) for each axis. Table 8.6 presents the accuracy and repeatability data for individual axes. The worst accuracy displayed by linear axes was 0.038 mm and the worst repeatability was $\pm 0.035 \mathrm{~mm}$. These figures were displayed by the column module for the $+Z$ direction. The worst case of accuracy and repeatability for rotary axes was displayed by the cutting head rotary module in the -A direction; the accuracy was $3.164^{\circ}$ and the repeatability was $\pm 2.812^{\circ}$. Both the cutting head rotary and tilt table modules displayed poor accuracy and repeatability. The poor performance of these modules is attributed to the direct drive system (no secondary reduction gearbox) used in the modules. It should be noted that accuracy and repeatability figures do not provide any indication of the dynamic performance of an axis, but instead provide performance information with regard to the errors in final axis positions.

Table 8.6: Accuracy and Repeatability of MRM Modules

| Linear Modules | Test Conditions |  | $\begin{gathered} \mathrm{CR} \\ (\mathrm{~mm}) \end{gathered}$ | $\underset{(\mathrm{mm})}{\max \left(\mathrm{E}_{\mathrm{m}}\right)}$ | $\begin{gathered} \max \left(\mathrm{E}_{\mathrm{D}}\right) \\ (\mathrm{mm}) \\ \hline \end{gathered}$ | $\begin{gathered} \text { Acc } \\ (\mathrm{mm}) \end{gathered}$ | $\begin{aligned} & \text { Rep } \\ & (\mathrm{mm}) \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Distance (mm) | $\begin{gathered} \text { Speed } \\ (\mathrm{mm} / \mathrm{s}) \end{gathered}$ |  |  |  |  |  |
| Base | 100 | 100 | 0.005 | 0.005 | 0.020 | 0.027 | 0.024 |
|  | -100 | 100 | 0.005 | 0.005 | 0.015 | 0.022 | 0.020 |
| Work Table Slide | 100 | 100 | 0.006 | 0.006 | 0.023 | 0.032 | 0.029 |
|  | -100 | 100 | 0.006 | 0.006 | 0.023 | 0.032 | 0.029 |
| Column | 100 | 100 | 0.006 | 0.006 | 0.029 | 0.038 | 0.035 |
|  | -100 | 100 | 0.006 | 0.006 | 0.023 | 0.032 | 0.029 |
| Cross Slide | 50 | 50 | 0.004 | 0.004 | 0.012 | 0.018 | 0.016 |
|  | -50 | 100 | 0.004 | 0.004 | 0.012 | 0.018 | 0.016 |
| Rotary Modules | Angle (deg) | $\begin{gathered} \text { Speed } \\ (\mathrm{rev} / \mathrm{min}) \end{gathered}$ | $\begin{gathered} \text { CR } \\ (\mathrm{deg}) \end{gathered}$ | $\begin{gathered} \max \left(\mathrm{E}_{\mathrm{m}}\right) \\ (\mathrm{deg}) \end{gathered}$ | $\begin{gathered} \max \left(\mathrm{E}_{\mathrm{E}}\right) \\ (\mathrm{deg}) \end{gathered}$ | Acc (deg) | $\begin{gathered} \text { Rep } \\ (\mathrm{deg}) \end{gathered}$ |
| Cutting Head Rotary | 360 | 40 | 0.703 | 0.703 | 1.406 | 2.461 | 2.109 |
|  | -360 | 40 | 0.703 | 0.703 | 2.109 | 3.164 | 2.812 |
| Tilt Table | 90 | 30 | 0.703 | 0.703 | 1.406 | 2.461 | 2.109 |
|  | -90 | 30 | 0.703 | 0.703 | 1.406 | 2.461 | 2.109 |
| Rotary Table | 360 | 0.75 | 0.013 | 0.100 | 0.151 | 0.257 | 0.251 |
|  | -360 | 0.75 | 0.013 | 0.100 | 0.113 | 0.219 | 0.213 |

### 8.9 Chapter Summary

This chapter presented an overview of MRM assembly and reconfiguration. A calibration procedure for MRMs was also outlined. Investigations into the performance of position systems were presented. A positioning system consisted of the host PC, the servo communication module, servo control modules and MRM axes. Investigations were conducted into the static and dynamic positioning accuracy of individual modules and the synchronised motion of multiple axes. Tests were performed for rapid point to point motions, linear interpolated motions and circular interpolated motion. The accuracy and repeatability of individual axes was determined; which accounted for control errors, mechanical errors and the control resolution of modules.

## 9. Discussion

### 9.1 Performance Summary: Mechanical Systems

The primary objective of creating the MRM platform was to develop a new class of machine tools that are designed from the outset to display reconfigurability in their functionality. Development costs limited the design of the MRM library of modules to the machining of soft materials such as wax and plastic only. The power available at the machine spindle for drilling and turning was 80 watts and 550 watts respectively. The power available at each axis in the system was 100 watts. The power of the machine spindles and axes were sufficient for the drilling and turning of the specified materials.

All linear axes were capable of speeds of $100 \mathrm{~mm} / \mathrm{min}$ and all rotary axes were capable of a speed of $1 \mathrm{rev} / \mathrm{min}$, thus meeting the minimum design expectations of the system. The force requirement from the system for the drilling and turning of plastics and waxes was specified at 50 N . All MRM modules were capable of actuation loads in excess of 250 N and normal loads in excess of 240 N on their moving interfaces. These were usually conservative estimations that permitted deflections less than 0.20 mm in individual modules. All MRM configurations were capable of sustaining machining forces of 50 N . The assembly most inclined to large static deflections and vibrations was the drilling subassembly presented in Section 5.12. This particular configuration of modules included the drilling head, the range extension arm, the cutting head rotary module and the column module. For a vertical force of 50 N (N.B column slide 600 mm above its base) a total deflection of 0.058 mm in the position of the machine spindle was predicted by calculations. This subassembly displayed significantly less rigidity in the horizontal plane and a total deflection of 1.959 mm was estimated for a force of 50 N on the drilling head. Of all nine possible MRM configurations this was the worst anticipated deflection in the position of the cutting head/tool for the specified force. This particular configuration was still able to sustain the 50 N drilling force for rotations of $\pm 30^{\circ}$ in the position of the drilling head (from a vertical position), while still maintaining a deflection of less than 1 mm in the position of the cutting tool.

The dynamic performance of the mechanical system was investigated. The investigation was also performed on the drilling subassembly presented in Section 5.12; as this was the mechanically weakest assembly of all MRM module combinations tested. The system was found to have a resonant frequency of 100 Hz for a vertical excitation force and 15 Hz for a horizontal excitation force on the drilling head (N.B column slide 600 mm above its base). These frequencies correspond to drilling speeds of $6134 \mathrm{rev} / \mathrm{min}$ and $1054 \mathrm{rev} / \mathrm{min}$ if the excitation were to occur once per revolution. If the excitation were to occur twice per drill revolution, the respective resonant drilling speeds would be $3067 \mathrm{rev} / \mathrm{min}$ and $527 \mathrm{rev} / \mathrm{min}$. The drilling head has an unloaded speed of $580 \mathrm{rev} / \mathrm{min}$; however once loaded the speed of the drill is expected to be safely below the resonant speeds (only 80 watts available at spindle). For normal drilling operations (not vibration assisted drilling) vibrations along the axis of the drill are ideally not expected as there is a continuous engagement of the cutting edge of the tool with the work piece. In reality vibrations are induced by inconsistencies in the work piece and damaged tools. The MRM system therefore possesses sufficient mechanical integrity for the machining of wax and plastics which have a generally even consistency.

The performance of the MRM library of modules may be further improved. The column module contained a low cost sliding mechanism consisting of four silver steel rods. For the investigation of Section 5.12, the column module was the module with the least stiffness. In series, spring stiffness's are combined reciprocally and the low total stiffness resulted in the large deflection of 1.959 mm for a force of 50 N on the drilling head in the horizontal direction. The performance of this module under static and dynamic loading may be improved by the use of a traditional dove tail slide mechanism in place of the current system. The work table slide module is another module, which should ideally possess a dove tail slide mechanism in place of the existing steel rod sliding mechanism. Additional mechanical problems resulting from the modularization of production machines are discussed in Section 9.5.

### 9.2 Performance Summary: Positioning Systems

## Dynamic Performance: Interpolated Motion of Individual Axes

Positioning systems consist of the host PC, the servo communication module, servo control modules and the machine axes. An investigation into the dynamic performance of positioning systems was conducted in Section 8.5, for interpolated motion. For program speeds of $100 \mathrm{~mm} / \mathrm{min}$, linear axes displayed a maximum tracking error of 0.633 mm . This error is the discrepancy between a reference position and a measured position with regard to time. Rotary axes with reduction gearboxes (rotary table module) displayed a maximum tracking error of $0.942^{\circ}$ at a speed of $0.75 \mathrm{rev} / \mathrm{min}$. Rotary axes with direct drive mechanisms (tilt table and cutting head rotary module) were capable of higher speeds, and errors as large as $14.776^{\circ}$ were registered at speeds of $10 \mathrm{rev} / \mathrm{min}$. Dynamic tracking errors increased with an increase in operating speeds in both linear and rotary motion modules. The motors used in motion modules were generally under powered and exhibited poor acceleration when achieving target speeds. The highest dynamic errors were generally exhibited during the acceleration phase of interpolations as the drive motors did not possess sufficient power to effectively track the reference.

Across entire trajectories, linear axes displayed average dynamic errors as large as 0.116 mm and rotary axes displayed average dynamic errors as large as $6.797^{\circ}$. A significant contributing factor to the deviation of the measured position from the target position, in the steady region of axis trajectories, was uneven friction characteristics in module drive mechanisms and sliding systems. In both linear and rotary modules the uneven friction characteristics were attributed to the poor quality manufacturing of the mechanisms. The modules that were most affected be uneven friction were the tilt table module and the cutting head rotary module. The direct drive mechanisms in both these modules provided insufficient torque at test speeds to provide smooth operation in view of the uneven friction characteristics displayed by their sliding mechanisms. The modules were prone to the "slip-stick" effect caused by uneven friction, resulting in comparatively large dynamic errors after the acceleration phase of the trajectory. The internal gearboxes of the drive motors were inadequate and the performance of these modules would improve with a redesign that includes a secondary reduction gearbox.

## Static Performance: Point to Point Rapid Motion of Individual Axes

Point to point rapid motion is concerned with the rapid positioning of axes, without the observance of a target speed. The performance of positioning systems under this mode of motion control is not concerned with the dynamic positioning accuracy of the system, but rather the accuracy in the final static position of an axis after a trajectory.

Section 8.6 presented the results of tests performed on individual axes for point to point, rapid motions. The error in the final position of an axis was calculated by obtaining the difference between the reference position and the measured position at the end of a trajectory. The calculations did not consider the effect of mechanical play and backlash between mating components. The largest position error exhibited by a linear axis was 0.059 mm , which was displayed by the column module. The largest error exhibited by a rotary axis was $1.406^{\circ}$, which was displayed by the cutting head rotary module. Both these modules displayed the worst cases of uneven friction in their respective categories.

## Dynamic Performance for Synchronized Motions -Linear Paths

The performance of the MRM axes for synchronized motions was presented in Section 8.7. A test was performed for the synchronized motion of the base module and work table slide module in the 3-DOF drilling configuration. For a linear path and a resultant speed of $100 \mathrm{~mm} / \mathrm{min}$ ( $70.71 \mathrm{~mm} / \mathrm{min}$ per axis), the maximum dynamic position error from the combined motion was 0.429 mm ; which occurred during the acceleration of the two axes. The average position error for the drill spindle was 0.069 mm . A similar test was performed in the turning configuration, with the resultant motion of the tool post being provided by the base module and cross slide module. For a linear path and a resultant speed of $100 \mathrm{~mm} / \mathrm{min}$, the maximum dynamic position error was 0.382 mm and the average error was 0.045 mm .

## Dynamic Performance for Synchronized Motions -Circular Paths

A performance investigation was conducted on the 3-DOF drilling configuration for circular interpolated motion. The ideal arc to be followed by the drill spindle was of radius 100 mm and a subtended angle of $90^{\circ}$. The base module and the work table slide module were to provide a resultant feed rate of $100 \mathrm{~mm} / \mathrm{min}$ along the arc. The results of the test showed a maximum dynamic position (tracking) error of 0.241 mm . The trajectory was characterized by four peaks in the dynamic position error, corresponding to the end of the four linear segments that were used to approximate the arc. These peaks in error signify a rapid change in the reference to the position control loop and the slow response of the drive motors in tracking this change.

A reference word algorithm incorporating the Improved Tustin Method was used to perform the circular interpolation in software. The ITM algorithm was selected as it is known to provide better accuracy and require less iterations than Euler and Taylor methods [31]. The ITM algorithm resulted in chord height errors as large at 2.850 mm in the reference input to the control algorithm. The performance of the ITM with regard to circular interpolation was poor, as a fine interpolator was not included in the existing software system. The performance of the system may therefore be improved by the addition of a moving average fine interpolator to the software system. The comprehensiveness of the software may also be improved by the incorporation of the NURBS interpolator, which is used for the linear approximation of more complex curved paths.

## Accuracy and Repeatability

Accuracy and repeatability tests were performed for individual axes at controlled speeds (interpolated motion). Six tests were performed for each axis in either direction of motion and the results of the individual tests are presented in Appendix F.5. Section 8.8 presented the accuracy and repeatability figures for each axis; these figures accounted for mechanical and control errors, as well as possible errors in position measurements.

The worst accuracy displayed by linear axes was 0.038 mm and the worst repeatability was $\pm 0.035 \mathrm{~mm}$. These figures were displayed by the column module at a speed of $100 \mathrm{~mm} / \mathrm{min}$ in the $+Z$ direction. For rotary axes with reduction gearboxes the worst accuracy and repeatability figures were $0.257^{\circ}$ and $\pm 0.251^{\circ}$ respectively, displayed by the rotary table module for a speed of $0.75 \mathrm{rev} / \mathrm{min}$ in the +Y direction. Rotary axes without secondary reduction gearboxes displayed a worst case accuracy and repeatability of $3.164^{\circ}$ and $\pm 2.812^{\circ}$ respectively. These figures were displayed by the cutting head rotary module for a speed of $40 \mathrm{rev} / \mathrm{min}$ in the -A direction.

The modules with the worst relative performance in their respective categories were the cutting head rotary module, the tilt table module and the column module. All of these modules were prone to the negative effects of uneven friction characteristics in their drive and sliding mechanisms. The torque provided by the drive motors at the respective test speeds was also insufficient to smooth the motion of the axes. The only modules that failed to meet the required accuracy and repeatability specifications were the cutting head rotary module and the tilt table module. The combination of uneven friction characteristics, the slip-stick effect and the low power of the motors were the dominant contributors to this discrepancy. Appendix H contains the final specifications that were achieved by the various MRM modules and assemblies.

### 9.3 Comparative Analysis of the Properties of MRMs

The motivation for the design of MRMs was the inadequacies of other types of machine tools in their applicability to reconfigurable manufacturing. These inadequacies included poor expansion flexibility, rigid mechanical and control architectures and either excessive or limited functionality. The Arch Type RMT presented in Section 3.3 is the only known reconfigurable machining platform that has been built by either industry or academia to date. The machine was built on a party family approach to reconfigurability. The design of MRMs deviated from this approach due to the rigidity of the mechanical architecture and the risk of such machinery becoming redundant if drastic changes in products are expected.

Table 9.1: Comparative Analysis of DMTs, CNCs, RMTs and MRMs

| Characteristics | DMTs | CNCs | RMTs | MRMs |
| :---: | :---: | :---: | :---: | :---: |
| Design Orientation | Part | Generic | Part Family | Generic, Reconfigure to Part Family |
| Mechanical Hardware | Fixed Design | Fixed Design | Fixed Design | Modifiable Design |
| Control Hardware | Fixed Design | Fixed Design | Fixed Design | Scalable Design |
| Control Software | No software or Fixed Design | Fixed Designs or Open Architecture Control | Open Architecture Control | Open Architecture Control |
| Flexibility of Design | Part Design | Generic Design | Part Family Design | Generic design |
| Reconfigurability - <br> Machining Processes | Not Applicable | Retooling of spindle | Reorientation of Machine Spindle | Interchangeable <br> Cutting Heads |
|  |  |  | Retooling of Spindle | Reorientation of Machine Spindle |
|  |  |  |  | Retooling of Spindle |
| Reconfigurability - <br> Machine Axes | Not Applicable | Not Applicable | Reorientation of Machine Axes | Interchangeable <br> Machine Axes |
| Customization of Machine to Process | Very High | Low | High | Moderately High |
| Predicted Relative Cost | Low | High | Low - Moderate | Moderate |

MRMs were designed for the manufacturing of general products as in the case of CNC machines; however the modularity of the system permits its flexibility to be customized as in the case of DMTs and RMTs. A comparative analysis of MRMs is provided in Table 9.1, this comparison is between the properties of MRMs, DMTs, CNCs and RMTs. MRMs display a clear advantage over other types of machines in terms of the modifiable mechanical architecture, the scalable nature of the control system and the interchangeability of axes and cutting heads. The property of customizable and expandable flexibility in MRMs has resulted in the prediction of a relatively moderate cost in comparison to CNCs.

### 9.4 MRMs in Reconfigurable Manufacturing Systems

### 9.4.1 Reconfigurable Functionality in MRMs

The MRM library of modules consisted of twelve units of hardware that were ultimately used to create nine machines that displayed distinctly different combinations of cutting processes and kinematic abilities. In addition to the manufactured hardware, commercial off the shelf enhancements such as steady rests and tail stocks could be integrated with MRM platforms to provide additional levels of functionality. The full range of modules is documented in Appendix B. All MRM configurations created with the library of modules are documented in Appendix D.

MRMs address the necessity for reconfigurable functionality in RMSs by providing a variation in processing operations and DOF through the structural reconfiguration of a machining platform. A change in processing operations enables different part features to be produced while a change in DOF enables different tool paths. Reconfigurability of this nature holds three important implications:
(i) The flexibility of individual machines may be expanded, thus enabling RMSs to produce different part families with a minimum investment in additional hardware.
(ii) MRMs need only possessed the exact level of functionality required to complete an operation, any excess modules may be removed and distributed to other machines in the system.
(iii) Unused machines may be decomposed into modules and reassembled into other machines that are needed in the system.

### 9.4.2 Initial Capital Investment in Hardware

MRMs are machines that are able to display expandable machine flexibility. The implication is that manufacturers may begin the operation of a system with the minimal level of functionality required at the outset. As the product portfolio of the system evolves, the machines in the system may be enhanced with additional modules. From an economic perspective this means that manufacturing systems may be initialized at a minimum cost and the flexibility of the system may be gradually increased at a later stage as the system begins to pay back the initial capital investment. Moreover, the increase in flexibility is derived from the upgrading of existing machines as opposed to the purchasing of new machines, therefore promising cost savings in hardware investments.

### 9.4.3 Scalable System Capacity



Figure 9.1: Example Demand Characteristics: Part A (above), Part B (below) [74]

In manufacturing systems producing multiple product types, a redistributing of system resources between operations will often be required as the demand characteristics of the individual products vary over a period of time. Changes in demand characteristics are most profound when new products are launched into markets. Consider the example of Figure 9.1 which illustrates two parts belonging to two different products. Part A corresponds to Product A, which is being phased out of production. Part B corresponds to Product B, which is replacing the old product.


Figure 9.2: Reconfiguration of Production Stream Capacity by the Reconfiguration and Redistribution of MRMs

During the phase of introducing the new product the demand for the older product will decline while the demand for the new product will increase as illustrated. Part A requires a 3 -axis drilling machine for the machining of holes on its various flat surfaces while Part B requires a 4 -axis drilling machine to cater for the machining of additional holes on inclined surfaces. In the case presented a manufacturer would reallocate a portion of the system resources previously used in the production of A to the production of B based on the demand characteristic.

This is achieved by reconfiguring the 3 -axis drilling machines into 4 -axis drilling machines by the addition of modules to the platforms. The 4 -axis machines are then allocated to the production stream of product B. Figure 9.2 illustrates how the process of reconfiguration may used to vary the capacities of both production streams by the redistribution of system resources.

### 9.4.4 High Product Variety and Product Customization

MRMs are able to display expandable mechanical flexibility. An expansion in machine flexibility further implies an expansion in the process flexibility of the manufacturing system. Process flexibility is concerned with the set of part types that can be produced by current process configurations. MRMs will therefore enable systems to cope with a higher part variety over a period of time; this is presently a significant challenge in modern manufacturing.

MRMs possess the potential to aid in product customization, which was also identified as a significant challenge in modern manufacturing. Specific product configurations may require unique machine configurations for their production. In this instance an MRM may be suitably reconfigured to match a customized derivative of a product platform. This eliminates the need to purchase an unpopular machine for the customized product. This is a particularly unattractive scenario as the machine may only be used for a limited run of products. With MRMs the manufacturer need only invest in a specialized module to impart the required functionality to the system. The machine may then be reconfigured for other operations once a customized product feature is no longer required.

The modularity of MRMs may in future, grant manufacturers the platform to develop customized modules for their machines (as opposed to purchasing them). This will further enhance product customization and enable manufacturers to optimize MRMs to meet their specific requirements. A customized MRM is expected to be quicker to assemble than the building of customized machines. User customization will require the drafting and publication of open standards for the interfacing and control of MRM modules.

### 9.4.5 Expansion Flexibility and System Life Span

The expandable machine flexibility, process flexibility and the ability of MRMs to aid in capacity scaling imply high expansion flexibility for RMSs. DMSs are limited in their expansion flexibility due to the rigid nature of the systems, while FMSs would usually require the purchasing of new types of machines to alter the functionality available in the system. The lifespan of RMSs are therefore expected to be significantly longer than DMSs, and the cost of extending its lifespan much lower than FMSs, if MRM technology is refined and implemented.

### 9.4.6 MRMs and the Five Essential Characteristics of RMSs

The five essential characteristics of RMSs are modularity, convertibility, customization, integrability and diagnosability. These characteristics are to be enabled in RMSs by the technologies implemented in these systems. In MRMs these characteristics were imparted to the system at multiple levels. The Mechatronic engineering approach was applied to the design of MRMs and necessary features in the mechanical, electronic and software systems were identified as early as the conceptual design phase. The individual subsystems either display each of the five characteristics directly, or support other subsystems in displaying these characteristics.

Table 9.2 summarizes how features in the various subsystems of an MRM support the five essential characteristics of RMSs.

Table 9.2: MRMs and the Five Essential Characteristics of RMSs

|  | Mechanical System | Electronic System | Software System |
| :---: | :---: | :---: | :---: |
| Modularity | - Modularized axes and cutting heads. | - Modularized control hardware and networked axes. | - The concentration of generic software functions on the host PC and the location of module specific control functions on distributed control drives promoted mechanical and electronic modularity. |
| Convertibility | - Reconfiguration of modular assemblies to convert machines to produce new products. | - Modular control hardware supported the conversion of the mechanical platform. | - A fully comprehensive G-Code command set inbuilt to support a large variety of mechanical configurations. |
| Customization | - The functionality of the mechanical system could be customized by allowing only the necessary modules to be present on a platform. | - The electronic control system was modular and scalable, ensuring that only those modules necessary for the control of the current MRM configuration are present in the control system. | - The selection of active axis combinations by drop down menus customized the active G-Code command set. <br> - Commands that were inconsistent with the selected combination were rejected by the text interpreter. |
| Integrability | - Mechanical modules possessed a series of standard mechanical interfaces for integration with each other. <br> - $\quad$ Standardized 8 and 11 wire connections were used to provide a consistent power and control interface between mechanical and control modules. | - $\quad$ Standardized 8 and 11 wire connections for interfacing of control modules with the mechanical platform. <br> - The use of standardized communication protocols such as I2C supported the integration of control modules into networks. <br> - USB communication provided a standard means of interfacing distributed control dives with the host PC. | - The software system supported the USB communication protocol. <br> - The ability to configure USB port addresses for spindle and servo control further enhanced the integrability of hardware with the host PC. <br> - For modular axes the G-Code word addresses corresponded on a $1: 1$ basis with their I2C addresses, supporting the easy addressability of servo control modules. |
| Diagnosability | - All automated mechanical modules contained sensors. | - Limit switches for collision detection. <br> - Accelerometers for the measurement of vibrations. | - The MRM GUI contained a warning box, status box, progress bar and LCD for the display of diagnostic information to the user. |

### 9.5 Problems Associated with MRMs

### 9.5.1 Geometric Proportions of Machine Slides

The use of the range extension arm for drilling configurations increased the susceptibility of those MRM assemblies to static and dynamic deflections. The use of the range extension arm was necessary to compensate for the distance of the column module from the work table slide module. This distance was a result of the geometric proportions of the base module, which was also used for the turning configuration. The dimensions of the base module were suitable for turning configurations which require a long base, but particularly inappropriate for drilling configurations.

Imbalances in the geometric proportions of machines axes are a problem that will have to be addressed before MRM technology becomes practically implementable in industries. A particular range of axes lengths may be more suitable for some cutting processes than for others and the use of a generic set of axes will result in a general decline in the optimality of MRMs for specific processes. Imbalances in the dimensions of axes may be diminished by creating libraries of modules centered on cutting processes that are grouped together on the basis of geometric commonality in the typical parts they machine.

Turning operations are generally concerned with long cylindrical work parts while work parts in drilling are either non-prismatic or possess small length to diameter ratios. The work parts in drilling operations are clamped onto a rectangular work table and an example of a more complementary group of processes would be drilling, vertical milling and some boring operations (operations with a rotating boring bar). These processes may be combined to create a more suitable set of modules, where the dimensional imbalances in the final machine configurations are minimal. Moreover the machines may be reconfigured with a less drastic disassembly and reassembly process.

### 9.5.2 Mass Distribution in MRM Structures



Figure 9.3: Unfavourable Mass Distributions in MRMs
a. Overhanging mass in a 3-axis milling machine
b. Overhanging masses in a 3-axis drilling machine

MRM axes and cutting heads each possess a single drive motor. The motors are housed within the framework of individual modules and cannot be placed elsewhere due to the modularity of the machine structures. This results in an unfavorable mass distribution in machines with regard to deflections. Larger masses are found in overhanging positions as illustrated in Figure 9.3.a due to the necessity to locate the drive motor at the point of actuation. In CNCs and DMTs the drive motor for the machine spindle is usually located in a more stable position with greater mechanical support and power is transmitted from the motor to the spindle via a belt drive mechanism. Figure 9.3.b illustrates a scenario where an overhanging mass is introduced by the addition of a rotary axis to the system. In more conventional machining structures an axis of this nature would have been created as an integrated part of the machine column, minimizing the overhang. Lastly, Figure 9.3.b illustrates how an unfavorable mass distribution may be introduced in a machine structure as a result of the use of geometrically disproportional axes (as discussed in Section 9.4.1). Larger overhanging masses not only affect the static performance of the machine but also adversely affect the dynamic performance. For a given structural stiffness a larger mass closer to the cutting head reduces the natural resonant frequency of the system. MRMs are therefore susceptible to larger vibrations than CNCs or DMTs.

### 9.5.3 Module Weights, Stiffness and Actuation Power

MRM modules were created largely out of aluminum due to the low power of drive motors. This was a drawback that was introduced by restrictions in development costs. The light weights of the modules allowed the existing MRM system to be reconfigured manually within a maximum of one hour. As a consequence the use of aluminum reduced the stiffness of modules and their resonant frequencies, thus providing less rigidity to structures supporting the work piece and cutting tool. This reduced the performance of the system with regard to static and dynamic deflections.

MRM modules may be created out of stiffer materials such as steel or cast iron. The consequence of this will be heavier modules which will be more difficult to assemble manually. For full scale industrial machines the use of lifting equipment will be required for the assembly and reconfiguration of MRMs. This increases the complexity, cost and time invested in the reconfiguration of an MRM platform. The upgrading of a platform by the integration of a heavier module will diminish the performance of the system, as the drive motors in lower modules such as a base module will have to have to cope with additional weight in the machining structure. This presents the potential for the power balance in the system to be negatively affected and some modules will be found to be underpowered in the new MRM configuration. The underpowered modules will ultimately provide poor dynamic performance during position control, resulting in inaccuracies in machined parts. Slower actuation speeds may also reduce the throughput (units/time) achievable on these machines resulting in a drop in productivity and profits for a manufacturer.

### 9.5.4 Power Supply Systems

MRM platforms may be upgraded by the integration of additional mechanical and control modules into an existing system. The increase in the number of actuators, sensors and electronic circuits in a platform ultimately increases the demand on the electrical power supply system. MRMs may be created with excess capacity to provide additional power when necessary; alternatively research may be conducted into the development of a scalable power supply system.

Both alternatives are not cost effective and may even result in MRMs being more expensive than highly flexible CNC systems. A power supply with excess capacity is uneconomical while a scalable power supply system would be expected to cost more because of the added complexity in the technology.

### 9.5.5 Problems Associated with Reconfigurations

The process of reconfiguration requires that an MRM be taken "offline" from the manufacturing system. This implies a loss in productivity for the system during the time that is taken for reconfiguration. If the machine is in series with other machines in a production stream, this implies a standstill in production for the entire stream. The cost savings derived by modular upgrades of machines may be outweighed by the financial losses associated with the loss in productivity in the system.

Modular machines are expected to be prone to assembly errors if the reconfiguration process is not performed with precision. In order to minimize assembly errors the reconfiguration process is expected to be slow and the accurate alignment of module interfaces is of utmost importance. An MRM will have to be recalibrated after every reconfiguration and the calibration may be performed by using traditional CNC laser calibration systems. The entire reconfiguration, calibration and ramp-up processes for the MRMs are expected to be lengthy for industrial grade machines. This reduces the attractiveness of MRMs as a machining solution.

### 9.6 Chapter Summary

This chapter presented summaries and discussions on the performance of the library of MRM modules and the systems that were assembled from them. The performance of mechanical systems and positioning systems were reviewed and design improvements were recommended. The applicability of MRMs in RMSs was discussed and important benefits of MRMs were highlighted. The chapter concluded with an analysis of the problems associated with MRMs.

## 10. Conclusion

This research was motivated by the need to develop new production technologies that will enable the objectives of rapidly scalable system capacity and adjustable functionality to be achieved in reconfigurable manufacturing. Modular reconfigurable machines were proposed in this research as a possible solution to the machining requirements of RMSs. The modular nature of these machines permits a change in machining functions and degrees of freedom on a platform, thus enabling adjustable functionality in RMSs. The modular nature of the machines further permits the reconfiguration and redistribution of hardware resources in a system, thus enabling the synergistic scaling of production capacities in manufacturing streams or cells within the system. The variable machining functionality and the ability to assist in scaling production capacities will enable MRMs to form part of the solution that addresses the primary challenges of coping with high product variety and product customization. The modularity of MRMs also creates the potential for the machines to be cost effectively used in the initialization of manufacturing configurations that are needed for the short term manufacturing of small product batches.

MRMs possess the expandable machine flexibility needed in RMSs, thus favoring their implementation above dedicated machine tools. MRMs also exhibit the features of convertibility and customization allowing a machine to be adjusted in its functionality to suit new product portfolios. MRMs therefore possess the potential to cost less than CNC machines, which have comprehensive inbuilt functionality and may have features that may never be used by a manufacturer. Although CNC machines are designed with high flexibility, a CNC may still not possess the functionality required by a manufacturer. In this instance a new CNC machine will have to be purchased or the job may have to be outsourced to another manufacturer who possesses suitable machines. The expandable flexibility in MRMs therefore creates a second advantage over CNC machines, as they may be upgraded as necessary. The expansion flexibility in MRMs increases the expansion flexibility of RMSs and the lifespan of a RMS is expected to be longer and more economical to extend than either DMSs or FMSs.

The MRM modules created during this research could be assembled into a drilling or turning center. The turning configuration displayed two automated axes and one manually adjustable axis. The drilling configuration was able to display a variation from three up to six automated DOF. The twelve modular units of hardware that formed the library of modules were used to create nine unique machine configurations in total. A high level of reconfigurability with limited hardware is therefore displayed in MRM technology.

A modular distributed control system was created for MRMs. The modularity of the system complimented the mechanical modularity and the computing capacity of the system was scalable. The number of mechanical modules controlled by the system could be increased with an increase in the number of distributed control drives connected to the system. The use of standard communication protocols such as USB and I2C promoted the modularity and easy reconfigurability of the control system. The concentration of generic software functions on the host PC and the location of module specific control functions on distributed control drives created a hardware abstraction that further promoted mechanical and electronic modularity. Theoretically the hardware abstraction supports the augmentation of a platform with mechanical and electronic control modules from multiple vendors by providing a consistent style of integration with the rest of the control system.

The facility for a manufacturer to augment his machine tools with modules from multiple vendors would ultimately result in a more competitive machine tool market. The potential to reconfigure and upgrade machine tools cost effectively, exists with MRMs a technology for future manufacturing.

The MRM software system on the host PC was created with full inbuilt functionality. The level of reconfigurability in the software system was limited to the selection of axes and the configuring of port addresses. Collision detection was only enabled locally between a mechanical module and a control module, and the host PC was only informed of collisions after a machining process had begun. For preemptive collision detections on the part of the host PC, a more extensive reconfiguration of the software system is required. A software system with full inbuilt functionality is also bound to be uneconomical if the technology is made commercially available. Further research must be conducted into the development of a modular open architecture control system for MRMs.

The MRM platform developed in this research was limited to the machining of wax and soft materials. The machine displayed a lack of stiffness in certain machine configurations and low powered motors resulted in a decreased performance compared to similar machines that are commercially available. Low cost sliding mechanisms, power screws and other low cost drive mechanisms limited the performance of the machine. The overall performance of the mechanical system was sufficient to achieve the objectives of the research and the performance of the present MRM platform may be significantly improved with additional monetary investments. Improvements that have been identified include the implementation of more suitable and higher quality mechanical components such as recirculating ball screws in linear axes; bevel and spur gearboxes in rotary axes and higher quality DC servo motors in all axes. The use of cast dove tail slide systems and bifurcated structures would also increase the stiffness of linear axes. Stiffer and heavier materials such as steel and cast iron would further increase the rigidity and vibration damping characteristics of individual modules. This would be complimented by an increase in the power capacities of all drive motors in modular axes.

Through the research performed on the existing library of modules, problems in MRMs have been identified. Some of these problems may be solved with improved design while others are an inherent and fundamental consequence of a modularized structure. Dimensional imbalances in machining structures are introduced when uncomplimentary machining processes are grouped together to create a set of modules. This problem was displayed by the current system where the use of a range extension arm was required to compensate for the uncomplimentary dimensions of the base module in drilling configurations. The range extension arm increased the susceptibility of the drilling configurations to large static and dynamic mechanical deflections. Imbalances in the dimensions of axes may be diminished by creating sets of modules centered on cutting processes that are grouped together on the basis of geometric commonality in the typical part shapes they machine (prismatic/non-prismatic, large length to breadth ratio/small length to breadth ratio, large length to diameter ratio/small length to diameter ratio, etc).

The second problem that has been identified in MRMs is an unfavorable mass distribution in the machine structure. The effect of this problem may be diminished to an extent by improved mechanical design; however the necessity to locate drive motors at the point of actuation creates a fundamental structural disadvantage with regard to the mass distribution.

The third problem that was identified is the potential to drastically upset the balance of the structural rigidity and mechanical power available in the system by the integration of additional mechanical modules. This is a fundamental problem and modules may have to be designed with generally high powered motors and high stiffness; which will ultimately reduce the economic viability of the technology. The fourth problem that was identified was the need to increase the electrical power supply to the system as the number of modules in the system increases. Power supplies may be either created with excess capacity or further research may be performed on the development of modular scalable power supplies. A modular power supply system would be expected to cost more than a standard power supply system of equivalent capacity. The economic viability of both solutions appears fundamentally poor at present.

The final problem that was identified is the complexity of the reconfiguration process for MRMs. Reconfigurations entail alterations to the mechanical, electronic, software and electrical power supply systems of a machine. The level of complexity will require the use of companies that possess lifting equipment, calibration equipment and trained personnel to complete the reconfigurations. The reconfiguration process is therefore expected to be costly and time consuming. MRMs have to be taken offline from a system to be reconfigured and the profit losses associated with the machine downtime further reduce the economic viability and practicality of the technology. It should be noted that the automated reconfiguration of a machine is an impractical solution to this problem. If a machine is to display automated transformability into different configurations this would imply that the machine would have to be created with full inbuilt functionality. This is a logical contradiction to the intentions of a modular structural design. In addition to containing full inbuilt functionality, an automated transforming machine would have to contain additional motors and mechanisms to enable the transformability. Such machines would be inherently expensive and therefore not applicable as reconfigurable technology in RMSs.

Further research must be conducted on solving the problems identified, before MRMs become industrially implementable and economically attractive machines. Novel solutions will have to be developed as many of the problems that were highlighted appear to be of a fundamental nature and plausible solutions are not easily identified. An investment into the further research of MRM technology is justified by the promising benefits of enhanced reconfigurability in system functionality and production capacity for RMSs.

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## Appendix A

## A. 1 Interface Type One



Figure A.1: Dimensional Specifications of Interface One

Table A.1.1: Physical Specifications and Data for Interface One

| Interface Name | Plate Material | Yield Strength <br> $\mathbf{S}_{\mathrm{y}}(\mathbf{M P a})$ | Ultimate Tensile <br> Strength <br> $\mathbf{S}_{\mathrm{U}}(\mathbf{M P a})$ | Shear Strength <br> $\mathbf{S}_{\text {shear }}($ MPa $)$ |
| :---: | :---: | :---: | :---: | :---: |
| One | Aluminum 295- <br> T 4 | 165 | 250 | 162 |
| Modulus of <br> Elasticity <br> E (GPa) | Plate Thickness <br> $\mathrm{h}(\mathrm{mm})$ | Interface <br> Thickness <br> $\mathbf{L}_{\text {Int }}(\mathrm{mm})$ | Thread Height <br> $\mathbf{t}(\mathrm{mm})$ | Grip Length <br> $\mathrm{g}(\mathrm{mm})$ |
| 72 | 12 | 24 | 12 | 24 |

Table A.1.2: Physical Specifications and Data for Interface Connectors - Interface One

| Interface Name | Bolt Size (Hexagon Socket Head) | SAE Class | Proof Strength $\mathrm{S}_{\mathrm{P}}$ (MPa) | Yield Strength $\mathrm{S}_{\mathrm{y}}$ (MPa) | Ultimate <br> Tensile Strength $\mathrm{S}_{\mathrm{U}}$ (MPa) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| One | M8x1.25 | 12.9 | 970 | 1100 | 1220 |
| Shear Strength $\mathrm{S}_{\text {shear }}$ (MPa) | Modulus of Elasticity E (GPa) | Stressed <br> Area $\mathbf{A}_{\mathrm{t}}$ <br> ( $\mathrm{mm}^{2}$ ) | Minor Diameter $d_{r}$ $(\mathrm{~mm})$ | Bolt Length $\mathrm{L}_{\text {bolt }}(\mathrm{mm})$ | Bolt <br> Tightening Factor k $_{i}$ |
| 756 | 207 | $36.6 \mathrm{~mm}^{2}$ | 6.47 | 25 | 0.7 |

## Thread Stripping

Thread stripping will first occur on the interface plate
$F_{e}=\pi d(0.75 t) S_{\text {shear }}=\pi \times 0.008 \times(0.75 \times 0.012) \times 162 \times 10^{6}=36643 \mathrm{~N}$
$F_{e \text { total }}=8 \times 36643=293144 N$

Joint Separation
$F_{i}=k_{i} A_{t} S_{p}=0.7 \times 36.6 \times 10^{-6} \times 970 \times 10^{6}=24851 \mathrm{~N}$
$A_{c}=d^{2}+0.68 d g+0.065 g^{2}$
$A_{c}=0.008^{2}+0.68 \times 0.008 \times 0.024+0.065 \times 0.024^{2}=2.32 \times 10^{-4} \mathrm{~m}^{2}$
$k_{b}=\frac{A_{t} E}{L_{\text {bolt }}}=\frac{36.6 \times 10^{-6} \times 207 \times 10^{9}}{0.025}=3.03 \times 10^{8} \mathrm{~N} . \mathrm{m}^{-1}$
$k_{c}=\frac{A_{c} E}{L_{\text {int }}}=\frac{2.32 \times 10^{-4} \times 72 \times 10^{9}}{0.024}=6.96 \times 10^{8} \mathrm{~N} . \mathrm{m}^{-1}$
$F_{e}=\frac{k_{b}+k_{c}}{k_{c}} F_{i}=\frac{3.03+6.96}{6.96} 24851=35669 \mathrm{~N}$
$F_{\text {e total }}=8 \times 35669=285352 \mathrm{~N}$

## Recommended Bolt Tightening Torque

$T=0.2 F_{i} d=0.2 \times 24851 \times 0.008=39.76 \mathrm{~N} . \mathrm{m}$

## Maximum Shear Force per Bolt

$F=A S_{\text {shear }}=\frac{\pi}{4} \times 0.008^{2} \times 756 \times 10^{6}=38000 \mathrm{~N}$

## A. 2 Interface Type Two



Figure A.2: Dimensional Specifications of Interface Two

Table A.2.1: Physical Specifications and Data for Interface Two

| Interface Name | Plate Material | Yield Strength <br> $\mathbf{S}_{\mathbf{y}}(\mathbf{M P a})$ | Ultimate Tensile <br> Strength <br> $\mathbf{S}_{\mathrm{U}}(\mathbf{M P a})$ | Shear Strength <br> $\mathbf{S}_{\text {shear }}(\mathbf{M P a})$ |
| :---: | :---: | :---: | :---: | :---: |
| Two | Aluminum 295- <br> T4 | 165 | 250 | 162 |
| Modulus of <br> Elasticity <br> E (GPa) | Plate Thickness <br> $\mathbf{h ( m m )}$ | Interface <br> Thickness <br> $\mathbf{L}_{\mathrm{lt}}(\mathbf{m m})$ | Thread Height <br> $\mathbf{t}(\mathbf{m m})$ | Grip Length <br> $\mathbf{g}(\mathbf{m m})$ |
| 72 | 10 | 20 | 10 | 20 |

Table A.2.2: Physical Specifications and Data for Interface Connectors - Interface Two

| Interface Name | Bolt Size <br> (Hexagon Socket Head) | SAE Class | Proof Strength $\mathrm{S}_{\mathrm{P}}$ (MPa) | Yield Strength $\mathrm{S}_{\mathrm{y}}$ (MPa) | Ultimate <br> Tensile Strength $\mathrm{S}_{\mathrm{U}}$ (MPa) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Two | M6x1 | 12.9 | 970 | 1100 | 1220 |
| Shear Strength $\mathrm{S}_{\text {shear }}$ (MPa) | Modulus of Elasticity E (GPa) | Stressed <br> Area $\mathbf{A}_{\mathrm{t}}$ $\left(\mathrm{mm}^{2}\right)$ | Minor Diameter $\mathbf{d}_{r}$ $(\mathrm{~mm})$ | Bolt Length $\mathrm{L}_{\text {bolt }}$ (mm) | Bolt Tightening Factor $\mathbf{k}_{\text {i }}$ |
| 756 | 207 | $20.1 \mathrm{~mm}^{2}$ | 4.77 | 20 | 0.7 |

Note: Interface $A=$ Inner Pattern; Interface $B=$ Outer Pattern

## Thread Stripping

Thread stripping will first occur on the interface plate
$F_{e}=\pi d(0.75 t) S_{\text {shear }}=\pi \times 0.006 \times(0.75 \times 0.01) \times 162 \times 10^{6}=22902 \mathrm{~N}$
$F_{e \text { total }}=8 \times 22902=183217 N$

## Joint Separation

$F_{i}=k_{i} A_{t} S_{p}=0.7 \times 20.1 \times 10^{-6} \times 970 \times 10^{6}=13648 \mathrm{~N}$
$A_{c}=d^{2}+0.68 d g+0.065 g^{2}$
$A_{c}=0.006^{2}+0.68 \times 0.006 \times 0.020+0.065 \times 0.020^{2}=1.44 \times 10^{-4} \mathrm{~m}^{2}$
$k_{b}=\frac{A_{t} E}{L_{\text {bolt }}}=\frac{20.1 \times 10^{-6} \times 207 \times 10^{9}}{0.02}=2.08 \times 10^{8} \mathrm{~N} . \mathrm{m}^{-1}$
$k_{c}=\frac{A_{c} E}{L_{i n t}}=\frac{1.44 \times 10^{-4} \times 72 \times 10^{9}}{0.02}=5.18 \times 10^{8} \mathrm{~N} . \mathrm{m}^{-1}$
$F_{e}=\frac{k_{b}+k_{c}}{k_{c}} F_{i}=\frac{2.08+5.18}{5.18} 13648=19128 \mathrm{~N}$
$F_{e \text { total }}=8 \times 19128=153024 \mathrm{~N}$

## Recommended Bolt Tightening Torque

$T=0.2 F_{i} d=0.2 \times 13648 \times 0.006=16.38 \mathrm{~N} . \mathrm{m}$

## Maximum Shear Force per Bolt

$$
F=A S_{\text {shear }}=\frac{\pi}{4} \times 0.006^{2} \times 756 \times 10^{6}=21375 \mathrm{~N}
$$

## A. 3 Interface Type Three



Figure A.3: Dimensional Specifications of Interface Three

Table A.3.1: Physical Specifications and Data for Interface Three

| Interface Name | Plate Material | Yield Strength <br> $\mathbf{S}_{\mathbf{y}}(\mathbf{M P a})$ | Ultimate Tensile <br> Strength <br> $\mathbf{S}_{\mathrm{U}}(\mathbf{M P a})$ | Shear Strength <br> $\mathbf{S}_{\text {shear }}(\mathbf{M P a})$ |
| :---: | :---: | :---: | :---: | :---: |
| Three | Aluminum 295- <br> T4 | 165 | 250 | 162 |
| Modulus of <br> Elasticity <br> E (GPa) | Plate Thickness <br> $\mathrm{h}(\mathrm{mm})$ | Interface <br> Thickness <br> $\mathrm{L}_{\mathrm{Int}}(\mathrm{mm})$ | Thread Height <br> $\mathrm{t}(\mathrm{mm})$ | Grip Length <br> $\mathrm{g}(\mathrm{mm})$ |
| 72 | 10 | 20 | 10 | 20 |

Table A.3.2: Physical Specifications and Data for Interface Connectors - Interface Three

| Interface |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Name | Bolt Size <br> (Hexagon <br> Socket Head) | SAE Class | Proof <br> Strength <br> $\mathbf{S}_{\mathrm{P}}(\mathrm{MPa})$ | Yield <br> Strength <br> $\mathbf{S}_{\mathrm{y}}(\mathrm{MPa})$ | Ultimate <br> Tensile <br> Strength <br> $\mathbf{S}_{\mathrm{U}}(\mathrm{MPa})$ |
| Three | M6x1 | 12.9 | 970 | 1100 | 1220 |
| Shear <br> Strength <br> $\mathbf{S}_{\text {shear }}(\mathrm{MPa})$ | Modulus of <br> Elasticity <br> $\mathrm{E}(\mathrm{GPa})$ | Stressed <br> Area $\mathbf{A}_{\mathrm{t}}$ <br> $\left(\mathrm{mm}^{2}\right)$ | Minor <br> Diameter $\mathbf{d}_{r}$ <br> $(\mathrm{~mm})$ | Bolt Length $_{\mathbf{L}_{\text {bolt }}(\mathrm{mm})}$ | Bolt <br> Tightening <br> Factor $\mathbf{k}_{\mathrm{i}}$ |
| 756 | 207 | $20.1 \mathrm{~mm}^{2}$ | 4.77 | 20 | 0.7 |

## Thread Stripping

Thread stripping will first occur on the interface plate
$F_{e}=\pi d(0.75 t) S_{\text {shear }}=\pi \times 0.006 \times(0.75 \times 0.01) \times 162 \times 10^{6}=22902 \mathrm{~N}$
$F_{\text {e total }}=8 \times 22902=183217 \mathrm{~N}$

## Joint Separation

$F_{i}=k_{i} A_{t} S_{p}=0.7 \times 20.1 \times 10^{-6} \times 970 \times 10^{6}=13648 \mathrm{~N}$
$A_{c}=d^{2}+0.68 d g+0.065 g^{2}$
$A_{c}=0.006^{2}+0.68 \times 0.006 \times 0.020+0.065 \times 0.020^{2}=1.44 \times 10^{-4} \mathrm{~m}^{2}$
$k_{b}=\frac{A_{t} E}{L_{\text {bolt }}}=\frac{20.1 \times 10^{-6} \times 207 \times 10^{9}}{0.02}=2.08 \times 10^{8} \mathrm{~N} . \mathrm{m}^{-1}$
$k_{c}=\frac{A_{c} E}{L_{\text {int }}}=\frac{1.44 \times 10^{-4} \times 72 \times 10^{9}}{0.02}=5.18 \times 10^{8} \mathrm{~N} . \mathrm{m}^{-1}$
$F_{e}=\frac{k_{b}+k_{c}}{k_{c}} F_{i}=\frac{2.08+5.18}{5.18} 13648=19128 \mathrm{~N}$
$F_{e ~ t o t a l}=8 \times 19128=153024 \mathrm{~N}$

## Recommended Bolt Tightening Torque

$T=0.2 F_{i} d=0.2 \times 13648 \times 0.006=16.38 \mathrm{~N} . \mathrm{m}$

## Maximum Shear Force per Bolt

$F=A S_{\text {shear }}=\frac{\pi}{4} \times 0.006^{2} \times 756 \times 10^{6}=21375 \mathrm{~N}$

## A. 4 Interface Type Four



Figure A.4: Dimensional Specifications of Interface Four

Table A.4.1: Physical Specifications and Data for Interface Four

| Interface Name | Plate Material | Yield Strength <br> $\mathbf{S}_{\mathbf{y}}(\mathbf{M P a})$ | Ultimate Tensile <br> Strength <br> $\mathbf{S}_{\mathrm{U}}(\mathbf{M P a})$ | Shear Strength <br> $\mathbf{S}_{\text {shear }}($ MPa $)$ |
| :---: | :---: | :---: | :---: | :---: |
| Four | Cast Iron ASTM <br> 20 | - | 152 | 179 |
| Modulus of <br> Elasticity <br> E (GPa) | Plate Thickness <br> $\mathrm{h}(\mathrm{mm})$ | Interface <br> Thickness <br> $\mathbf{L}_{\text {Int }}(\mathrm{mm})$ | Thread Height <br> $\mathbf{t ( m m )}$ | Grip Length <br> $\mathbf{g}(\mathrm{mm})$ |
| 97 | 19 | 38 | 19 | 38 |

Table A.4.2: Physical Specifications and Data for Interface Connectors - Interface Four

| Interface Name | Bolt Size <br> (Hexagon Socket Head) | SAE Class | Proof Strength $\mathrm{S}_{\mathrm{P}}$ (MPa) | Yield Strength $\mathrm{S}_{\mathrm{y}}$ (MPa) | Ultimate <br> Tensile <br> Strength $\mathrm{S}_{\mathrm{U}}(\mathrm{MPa})$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Four | M10x1.5 | 8.8 | 600 | 660 | 830 |
| $\begin{gathered} \text { Shear } \\ \text { Strength } \\ \mathrm{S}_{\text {shear }}(\mathrm{MPa}) \end{gathered}$ | Modulus of Elasticity E (GPa) | Stressed <br> Area $\mathbf{A}_{t}$ <br> ( $\mathrm{mm}^{2}$ ) | Minor Diameter $d_{r}$ $(\mathrm{~mm})$ | Bolt Length $\mathbf{L}_{\text {bolt }}(\mathrm{mm})$ | Bolt Tightening Factor $\mathrm{k}_{\mathrm{i}}$ |
| 515 | 207 | $58.0 \mathrm{~mm}^{2}$ | 8.16 | 40 | 0.9 |

## Thread Stripping

Thread stripping will first occur on the interface plate
$F_{e}=\pi d(0.75 t) S_{\text {shear }}=\pi \times 0.01 \times(0.75 \times 0.019) \times 179 \times 10^{6}=80134 \mathrm{~N}$
$F_{e \text { total }}=4 \times 80134=320536 N$

## Joint Separation

$F_{i}=k_{i} A_{t} S_{p}=0.9 \times 58.0 \times 10^{-6} \times 600 \times 10^{6}=31320 \mathrm{~N}$
$A_{c}=d^{2}+0.68 d g+0.065 g^{2}$
$A_{c}=0.01^{2}+0.68 \times 0.01 \times 0.038+0.065 \times 0.038^{2}=4.52 \times 10^{-4} \mathrm{~m}^{2}$
$k_{b}=\frac{A_{t} E}{L_{\text {bolt }}}=\frac{58.0 \times 10^{-6} \times 207 \times 10^{9}}{0.04}=3.00 \times 10^{8} \mathrm{~N} . \mathrm{m}^{-1}$
$k_{c}=\frac{A_{c} E}{L_{\text {int }}}=\frac{4.52 \times 10^{-4} \times 97 \times 10^{9}}{0.038}=11.54 \times 10^{8} \mathrm{~N} . \mathrm{m}^{-1}$
$F_{e}=\frac{k_{b}+k_{c}}{k_{c}} F_{i}=\frac{3.00+11.54}{11.54} 31320=39217 \mathrm{~N}$
$F_{e \text { total }}=4 \times 39217=156868 N$

## Recommended Bolt Tightening Torque

$T=0.2 F_{i} d=0.2 \times 31320 \times 0.01=62.64 \mathrm{~N} . \mathrm{m}$

## Maximum Shear Force per Bolt

$F=A S_{\text {shear }}=\frac{\pi}{4} \times 0.01^{2} \times 515 \times 10^{6}=40448 \mathrm{~N}$

## A. 5 Interface Type Five



Figure A.5: Dimensional Specifications of Interface Five

Table A.5.1: Physical Specifications and Data for Interface Five

| Interface Name | Plate Material | Yield Strength $\mathrm{S}_{\mathrm{y}}$ (MPa) | Ultimate Tensile <br> Strength <br> $\mathrm{S}_{\mathrm{U}}$ (MPa) | Shear Strength $\mathrm{S}_{\text {shear }}(\mathrm{MPa})$ |
| :---: | :---: | :---: | :---: | :---: |
| Four | $\begin{aligned} & \text { Cast Iron ASTM } \\ & 20 \\ & \hline \end{aligned}$ | - | 152 | 179 |
| Modulus of Elasticity E (GPa) | Plate Thickness h (mm) | Interface Thickness $\mathrm{L}_{\mathrm{Int}}$ (mm) | Thread Height t (mm) | Grip Length g (mm) |
| 97 | 6 | 25 | 19 | 25 |

Table A.5.2: Physical Specifications and Data for Interface Connectors - Interface Five

| Interface Name | Bolt Size <br> (Hexagon Socket Head) | SAE Class | Proof Strength $\mathrm{S}_{\mathrm{P}}(\mathrm{MPa})$ | Yield Strength <br> $\mathrm{S}_{\mathrm{y}}$ (MPa) | Ultimate Tensile Strength $\mathrm{S}_{\mathrm{U}}$ (MPa) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Four | M8x1.25 | 8.8 | 600 | 660 | 830 |
| $\begin{gathered} \text { Shear } \\ \text { Strength } \\ \mathrm{S}_{\text {strear }} \text { (MPa } \end{gathered}$ | Modulus of Elasticity E (GPa) | Stressed Area $\mathbf{A}_{\mathrm{t}}$ ( $\mathrm{mm}^{2}$ ) | $\begin{gathered} \text { Minor } \\ \text { Diameter } d_{r} \\ (\mathrm{~mm}) \end{gathered}$ | Bolt Length $\mathrm{L}_{\text {bolt }}(\mathrm{mm})$ | Bolt Tightening Factor $\mathrm{k}_{\mathrm{i}}$ |
| 515 | 207 | 36.6 mm ${ }^{2}$ | 6.47 | 25 | 0.9 |

## Thread Stripping

Thread stripping will first occur on the interface plate
$F_{e}=\pi d(0.75 t) S_{\text {shear }}=\pi \times 0.008 \times(0.75 \times 0.019) \times 179 \times 10^{6}=64107 N$
$F_{\text {e total }}=4 \times 64107=256429 \mathrm{~N}$

## Joint Separation

$F_{i}=k_{i} A_{t} S_{p}=0.9 \times 36.6 \times 10^{-6} \times 600 \times 10^{6}=19764 \mathrm{~N}$
$A_{c}=d^{2}+0.68 d g+0.065 g^{2}$
$A_{c}=0.008^{2}+0.68 \times 0.008 \times 0.025+0.065 \times 0.025^{2}=2.41 \times 10^{-4} \mathrm{~m}^{2}$
$k_{b}=\frac{A_{t} E}{L_{\text {bolt }}}=\frac{36.6 \times 10^{-6} \times 207 \times 10^{9}}{0.025}=3.03 \times 10^{8} \mathrm{~N} . \mathrm{m}^{-1}$
$k_{c}=\frac{A_{c} E}{L_{\text {int }}}=\frac{2.41 \times 10^{-4} \times 97 \times 10^{9}}{0.025}=9.35 \times 10^{8} \mathrm{~N} . \mathrm{m}^{-1}$
$F_{e}=\frac{k_{b}+k_{c}}{k_{c}} F_{i}=\frac{3.03+9.35}{9.35} 19764=26168 \mathrm{~N}$
$F_{\text {e total }}=4 \times 26168=104672 \mathrm{~N}$

Recommended Bolt Tightening Torque
$T=0.2 F_{i} d=0.2 \times 19764 \times 0.008=31.62 \mathrm{~N} . \mathrm{m}$

Maximum Shear Force per Bolt
$F=A S_{\text {shear }}=\frac{\pi}{4} \times 0.008^{2} \times 515 \times 10^{6}=25886 \mathrm{~N}$

## Appendix B

## B. 1 Base Module



Figure B.1: Base Module Displaying Local Reference Frames

Table B.1.1: Parameters Relating Frame ito i+1 on Base Module (Drilling)

| X-Y-Z Euler Angles | Degrees | X-Y-Z Offsets | mm |
| :--- | :--- | :--- | :--- |
| $\gamma$ | 0 | X | variable |
| $\beta$ | 0 | $y$ | -2.5 |
| $\alpha$ | 0 | Z | 215 |

$$
{ }_{i}^{i+1} M_{\text {Base-Drilling }}=\left[\begin{array}{cccc}
c 0 c 0 & c 0 s 0 s 0-s 0 c 0 & c 0 s 0 c 0+s 0 s 0 & x \\
s 0 c 0 & s 0 s 0 s 0+c 0 c 0 & s 0 s 0 c 0-c 0 s 0 & -2.5 \\
-s 0 & c 0 s 0 & c 0 c 0 & 215 \\
0 & 0 & 0 & 1
\end{array}\right]=\left[\begin{array}{cccc}
1 & 0 & 0 & x \\
0 & 1 & 0 & 2.5 \\
0 & 0 & 1 & 215 \\
0 & 0 & 0 & 1
\end{array}\right]
$$

Limits: $257.5 \leq x \leq 757.5$

Home: $x=257.5 \mathrm{~mm}$
Table B.1.2: Parameters Relating Frame ito i+1 on Base Module (Turning)

| X-Y-Z Euler Angles | Degrees | X-Y-Z Offsets | mm |
| :--- | :--- | :--- | :--- |
| $\gamma$ | 0 | $x$ | variable |
| $\beta$ | 0 | $y$ | -2.5 |
| $\alpha$ | 0 | $z$ | 19 |

$$
{ }_{i}^{i+1} M_{\text {Base-Turning }}=\left[\begin{array}{cccc}
c 0 c 0 & c 0 s 0 s 0-s 0 c 0 & c 0 s 0 c 0+s 0 s 0 & x \\
s 0 c 0 & s 0 s 0 s 0+c 0 c 0 & s 0 s 0 c 0-c 0 s 0 & -2.5 \\
-s 0 & c 0 s 0 & c 0 c 0 & 19 \\
0 & 0 & 0 & 1
\end{array}\right]=\left[\begin{array}{cccc}
1 & 0 & 0 & x \\
0 & 1 & 0 & 2.5 \\
0 & 0 & 1 & 19 \\
0 & 0 & 0 & 1
\end{array}\right]
$$

Limits: $192.5 \leq x \leq 692.5$
Home: $x=192.5 \mathrm{~mm}$

## B. 2 Work Table Slide Module



Figure B.2: Work Table Slide Module Displaying Local Reference Frames

Table B.2: Parameters Relating Frame i to i+1 on Work Table Slide Module

| X-Y-Z Euler Angles | Degrees | X-Y-Z Offsets | mm |
| :--- | :--- | :--- | :--- |
| $\gamma$ | 0 | x | 155 |
| $\beta$ | 0 | y | variable |
| $\alpha$ | 0 | z | -111 |

$$
\underset{i}{i+1} M_{\text {WT Slide }}=\left[\begin{array}{cccc}
c 0 c 0 & c 0 s 0 s 0-s 0 c 0 & c 0 s 0 c 0+s 0 s 0 & 155 \\
s 0 c 0 & s 0 s 0 s 0+c 0 c 0 & s 0 s 0 c 0-c 0 s 0 & y \\
-s 0 & c 0 s 0 & c 0 c 0 & -111 \\
0 & 0 & 0 & 1
\end{array}\right]=\left[\begin{array}{cccc}
1 & 0 & 0 & 155 \\
0 & 1 & 0 & y \\
0 & 0 & 1 & -111 \\
0 & 0 & 0 & 1
\end{array}\right]
$$

Limits: $-150 \leq y \leq 150$
Home: $y=0 \mathrm{~mm}$

## B. 3 Column Module



Figure B.3: Column Module Displaying Local Reference Frames

Table B.3: Parameters Relating Frame ito i+1 on Column Module

| X-Y-Z Euler Angles | Degrees | X-Y-Z Offsets | mm |
| :--- | :--- | :--- | :--- |
| $\gamma$ | 0 | x | -54.5 |
| $\beta$ | 0 | $y$ | 0 |
| $\alpha$ | 0 | $z$ | variable |

$$
{ }_{i}^{i+1} M_{\text {Column }}=\left[\begin{array}{cccc}
c 0 c 0 & c 0 s 0 s 0-s 0 c 0 & c 0 s 0 c 0+s 0 s 0 & -54.5 \\
s 0 c 0 & s 0 s 0 s 0+c 0 c 0 & s 0 s 0 c 0-c 0 s 0 & 0 \\
-s 0 & c 0 s 0 & c 0 c 0 & Z \\
0 & 0 & 0 & 1
\end{array}\right]=\left[\begin{array}{cccc}
1 & 0 & 0 & -54.5 \\
0 & 1 & 0 & 0 \\
0 & 0 & 1 & Z \\
0 & 0 & 0 & 1
\end{array}\right]
$$

Limits: $85 \leq z \leq 685$
Home: $z=685 \mathrm{~mm}$

## B. 4 Cross Slide Module



Figure B.4: Cross Slide Module Displaying Local Reference Frames
a. Reference frame i
b. Reference frame $i+1$

Table B.4: Parameters Relating Frame $\mathbf{i}$ to $\mathbf{i}+1$ on Cross Slide Module

| X-Y-Z Euler Angles | Degrees | X-Y-Z Offsets | mm |
| :--- | :--- | :--- | :--- |
| $\gamma$ | 0 | X | 0 |
| $\beta$ | 0 | y | variable |
| $\alpha$ | variable | Z | 168 |

$$
{ }_{i}^{i+1} M_{\text {Cross Slide }}=\left[\begin{array}{cccc}
c \alpha c 0 & c \alpha s 0 s 0-s \alpha c 0 & c \alpha s 0 c 0+s 0 s 0 & 0 \\
s \alpha c 0 & s \alpha s 0 s 0+c \alpha c 0 & s \alpha s 0 c 0-c \alpha s 0 & y \\
-s 0 & c 0 s 0 & c 0 c 0 & 168 \\
0 & 0 & 0 & 1
\end{array}\right]=\left[\begin{array}{cccc}
c \alpha & -s \alpha & 0 & 0 \\
s \alpha & c \alpha & 0 & y \\
0 & 0 & 1 & 168 \\
0 & 0 & 0 & 1
\end{array}\right]
$$

Limits: $-90 \leq y \leq 25$
Home: $y=0 \mathrm{~mm}$

## B. 5 Cutting Head Rotary Module



Figure B.5: Cross Slide Module Displaying Local Reference Frames
a. Reference frame i
b. Reference frame $i+1$

Table B.5: Parameters Relating Frame ito i+1 on Cutting Head Rotary Module

| X-Y-Z Euler Angles | Degrees | X-Y-Z Offsets | mm |
| :--- | :--- | :--- | :--- |
| $\gamma$ | variable | x | -138 |
| $\beta$ | 0 | y | 0 |
| $\alpha$ | 0 | z | 0 |

$$
{ }_{i}^{i+1} M_{\text {CH Rotary }}=\left[\begin{array}{cccc}
c 0 c 0 & c 0 s 0 s \gamma-s 0 c \gamma & c 0 s 0 c \gamma+s 0 s \gamma & -138 \\
s 0 c 0 & s 0 s 0 s \gamma+c 0 c \gamma & s 0 s 0 c \gamma-c 0 s \gamma & 0 \\
-s 0 & c 0 s \gamma & c 0 c \gamma & 0 \\
0 & 0 & 0 & 1
\end{array}\right]=\left[\begin{array}{cccc}
1 & 0 & 0 & -138 \\
0 & c \gamma & -s \gamma & 0 \\
0 & s \gamma & c \gamma & 0 \\
0 & 0 & 0 & 1
\end{array}\right]
$$

Limits: $-360^{\circ} \leq \gamma \leq 360^{\circ}$
Home: $\gamma=0^{\circ}$

## B. 6 Tilt Table Module



Figure B.6: Tilt Table Module Displaying Local Reference Frames

Table B.6.1: Parameters Relating Frame i to the Intermediate Frame on Tilt Table Module

| X-Y-Z Euler Angles | Degrees | X-Y-Z Offsets | mm |
| :--- | :--- | :--- | :--- |
| $\gamma$ | 0 | x | 0 |
| $\beta$ | variable | y | 0 |
| $\alpha$ | 0 | z | -50 |
| T |  |  |  |

Table B.6.2: Parameters Relating the Intermediate Frame to $\mathbf{i}+1$ on Tilt Table Module

| X-Y-Z Euler Angles | Degrees | X-Y-Z Offsets | mm |
| :--- | :--- | :--- | :--- |
| $\gamma$ | variable | X | -138 |
| $\beta$ | 0 | y | 0 |
| $\alpha$ | 0 | Z | 0 |

$$
{ }_{i}^{\text {int }} M=\left[\begin{array}{cccc}
c 0 c \beta & c 0 s \beta s 0-s 0 c 0 & c 0 s \beta c 0+s 0 s 0 & 0 \\
s 0 c \beta & s 0 s \beta s 0+c 0 c 0 & s 0 s \beta c 0-c 0 s 0 & 0 \\
-s \beta & c \beta s 0 & c \beta c 0 & -50 \\
0 & 0 & 0 & 1
\end{array}\right]=\left[\begin{array}{cccc}
c \beta & 0 & s \beta & -50 s \beta \\
0 & 1 & 0 & 0 \\
-s \beta & 0 & c \beta & -50 c \beta \\
0 & 0 & 0 & 1
\end{array}\right]
$$

$$
{ }_{\text {int }}^{i+1} M=\left[\begin{array}{cccc}
c 0 c 0 & c 0 s 0 s 0-s 0 c 0 & c 0 s 0 c 0+s 0 s 0 & 0 \\
s 0 c 0 & s 0 s 0 s 0+c 0 c 0 & s 0 s 0 c 0-c 0 s 0 & 0 \\
-s 0 & c 0 s 0 & c 0 c 0 & -95 \\
0 & 0 & 0 & 1
\end{array}\right]=\left[\begin{array}{cccc}
1 & 0 & 0 & 0 \\
0 & 1 & 0 & 0 \\
0 & 0 & 1 & -95 \\
0 & 0 & 0 & 1
\end{array}\right]
$$

$$
{ }_{i}^{i+1} M_{\text {Tilt Table }}=\left[\begin{array}{cccc}
1 & 0 & 0 & 0 \\
0 & 1 & 0 & 0 \\
0 & 0 & 1 & -95 \\
0 & 0 & 0 & 1
\end{array}\right]\left[\begin{array}{cccc}
c \beta & 0 & s \beta & -50 s \beta \\
0 & 1 & 0 & 0 \\
-s \beta & 0 & c \beta & -50 c \beta \\
0 & 0 & 0 & 1
\end{array}\right]=\left[\begin{array}{cccc}
c \beta & 0 & s \beta & -50 s \beta \\
0 & 1 & 0 & 0 \\
-s \beta & 0 & c \beta & -50 c \beta-95 \\
0 & 0 & 0 & 1
\end{array}\right]
$$

Limits: $-45^{\circ} \leq \beta \leq 45^{\circ}$
Home: $\beta=0^{\circ}$

## B. 7 Rotary Table Module



Figure B.7: Rotary Table Module Displaying Local Reference Frames
a. Reference frame i
b. Reference frame $i+1$

Table B.7: Parameters Relating Frame $\mathbf{i}$ to $\mathbf{i}+1$ on Rotary Table Module

| X-Y-Z Euler Angles | Degrees | X-Y-Z Offsets | mm |
| :--- | :--- | :--- | :--- |
| $\gamma$ | 0 | X | 0 |
| $\beta$ | 0 | y | 0 |
| $\alpha$ | variable | z | -152 |

$$
{ }_{i}^{i+1} M_{\text {Rot Table }}=\left[\begin{array}{cccc}
c \alpha c 0 & c \alpha s 0 s 0-s \alpha c 0 & c \alpha s 0 c 0+s \alpha s 0 & 0 \\
s \alpha c 0 & s \alpha s 0 s 0+c \alpha c 0 & s \alpha s 0 c 0-c \alpha s 0 & 0 \\
-s 0 & c 0 s 0 & c 0 c 0 & -152 \\
0 & 0 & 0 & 1
\end{array}\right]=\left[\begin{array}{ccc}
c \alpha & -s \alpha & 0 \\
s \alpha & c \alpha & 0 \\
0 & 0 & 1 \\
-152 \\
0 & 0 & 0
\end{array} 1\right]
$$

Limits: $-180^{\circ} \leq \alpha \leq 180^{\circ}$
Home: $\alpha=0^{\circ}$

## B. 8 Drilling Module



Figure B.8: Drilling Module Displaying Local Reference Frames

Table B.8: Parameters Relating Frame $i$ to $i+1$ on Drilling Module

| X-Y-Z Euler Angles | Degrees | X-Y-Z Offsets | mm |
| :--- | :--- | :--- | :--- |
| $\gamma$ | 0 | X | -75 |
| $\beta$ | 0 | y | 0 |
| $\alpha$ | 0 | Z | -81.5 |

$$
{ }_{i}^{i+1} M_{\text {Drill Head }}=\left[\begin{array}{cccc}
c 0 c 0 & c 0 s 0 s 0-s 0 c 0 & c 0 s 0 c 0+s 0 s 0 & -75 \\
s 0 c 0 & s 0 s 0 s 0+c 0 c 0 & s 0 s 0 c 0-c 0 s 0 & 0 \\
-s 0 & c 0 s 0 & c 0 c 0 & -81.5 \\
0 & 0 & 0 & 1
\end{array}\right]=\left[\begin{array}{cccc}
1 & 0 & 0 & -75 \\
0 & 1 & 0 & 0 \\
0 & 0 & 1 & -81.5 \\
0 & 0 & 0 & 1
\end{array}\right]
$$

## B. 9 Turning Module



Figure B.9: Turning Module Displaying Local Reference Frames

Table B. 9: Parameters Relating Frame ito i+1 on Turning Module

| X-Y-Z Euler Angles | Degrees |  | X-Y-Z Offsets | mm |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\gamma$ | 0 | x |  | -192.5 |  |  |
| $\beta$ | 0 | y |  | 0 |  |  |
| $\alpha$ | 0 |  | z | -212.5 |  |  |
| ${ }_{i}^{i+1} M_{\text {Turn Head }}=\left[\begin{array}{c}c 0 c 0 \\ s 0 c 0 \\ -s 0 \\ 0\end{array}\right.$ | $c 0 s 0 s 0-s 0 c 0$ $s 0 s 0 s 0+c 0 c 0$ $c 0 s 0$ 0 | $\begin{gathered} c 0 s 0 c 0+s 0 s 0 \\ s 0 s 0 c 0-c 0 s 0 \\ c 0 c 0 \\ 0 \end{gathered}$ | $\left.\begin{array}{c}-192.5 \\ 0 \\ -212.5 \\ 1\end{array}\right]=$ | $=\left[\begin{array}{l}1 \\ 0 \\ 0 \\ 0 \\ 0\end{array}\right.$ | $\begin{array}{lll}1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 0\end{array}$ | $\left.\begin{array}{c}-192.5 \\ 0 \\ -212.5 \\ 1\end{array}\right]$ |

## B. 10 Work Table Module



Figure B.10: Work Table Module Displaying Local Reference Frames

Table B.10: Parameters Relating Frame ito $\mathbf{i}+1$ on Work Table Module

| X-Y-Z Euler Angles | Degrees | X-Y-Z Offsets | mm |
| :--- | :--- | :--- | :--- |
| $\gamma$ | 0 | $x$ | 0 |
| $\beta$ | 0 | $y$ | 0 |
| $\alpha$ | 0 | Z | -24.5 |

$$
{ }_{i}^{i+1} M_{\text {Work Table }}=\left[\begin{array}{cccc}
c 0 c 0 & c 0 s 0 s 0-s 0 c 0 & c 0 s 0 c 0+s 0 s 0 & 0 \\
s 0 c 0 & s 0 s 0 s 0+c 0 c 0 & s 0 s 0 c 0-c 0 s 0 & 0 \\
-s 0 & c 0 s 0 & c 0 c 0 & -24.5 \\
0 & 0 & 0 & 1
\end{array}\right]=\left[\begin{array}{cccc}
1 & 0 & 0 & 0 \\
0 & 1 & 0 & 0 \\
0 & 0 & 1 & -24.5 \\
0 & 0 & 0 & 1
\end{array}\right]
$$

## B. 11 Range Extension Module (Arm)



Figure B.11: Range Extension Module (Arm) Displaying Local Reference Frames

Table B.11: Parameters Relating Frame $\mathbf{i}$ to $\mathbf{i}+1$ on Range Extension Module

| X-Y-Z Euler Angles | Degrees | X-Y-Z Offsets | mm |
| :--- | :--- | :--- | :--- |
| $\gamma$ | 0 | x | -370 |
| $\beta$ | 0 | y | 0 |
| $\alpha$ | 0 | z | 0 |

$$
{ }_{i}^{i+1} M_{\text {Extension Arm }}=\left[\begin{array}{cccc}
c 0 c 0 & c 0 s 0 s 0-s 0 c 0 & c 0 s 0 c 0+s 0 s 0 & -370 \\
s 0 c 0 & s 0 s 0 s 0+c 0 c 0 & s 0 s 0 c 0-c 0 s 0 & 0 \\
-s 0 & c 0 s 0 & c 0 c 0 & 0 \\
0 & 0 & 0 & 1
\end{array}\right]=\left[\begin{array}{cccc}
1 & 0 & 0 & -370 \\
0 & 1 & 0 & 0 \\
0 & 0 & 1 & 0 \\
0 & 0 & 0 & 1
\end{array}\right]
$$

## B.12 Cross Slide Interface Plate



Figure B.12: Cross Slide Interface Plate Displaying Local Reference Frames

Table B.12: Parameters Relating Frame $\mathbf{i}$ to $\mathbf{i}+1$ on Cross Slide Interface Plate


Limits: $0 \leq v \leq 80$

## Appendix C

## C. 1 Power Screw Calculations

## Base Module (X-Axis)

Table C.1.1: Power Screw Characteristics of MRM Base Module

| $\mathbf{d}_{\mathbf{m}}(\mathbf{m m})$ | $\mathbf{f}$ | $\mathbf{L}(\mathbf{m m})$ | $\boldsymbol{\alpha}$ (Degrees) | $\mathbf{f}_{\mathbf{c}}$ | $\mathbf{d}_{\mathbf{c}}(\mathbf{m m})$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 18.45 | 0.25 | 2.5 | 30 | 0.0015 | 17 |

Relationship between torque and linear load with direction of motion opposing direction of load:
$W=T\left[\frac{d_{m}}{2} \frac{f \pi d_{m}+L \cos \alpha_{n}}{\pi d_{m} \cos \alpha_{n}-f L}+\frac{f_{c} d_{c}}{2}\right]^{-1}$
$W=T\left[\frac{0.01845}{2} \frac{0.25 \times \pi \times 0.01845+0.0025 \times \cos 30}{\pi \times 0.01845 \times \cos 30-0.25 \times 0.0025}+\frac{2 \times 0.0015 \times 0.017}{2}\right]^{-1}$
$W=320.00 T$

Table C.1.2: Power Screw Actuation Characteristics of MRM Base Module

| Motor Speed <br> $($ rev/min) | Motor Current <br> $(\mathbf{a m p s})$ | Motor Torque <br> $(\mathbf{N} . \mathbf{m})$ | Actuation Speed <br> $(\mathbf{m m / m i n})$ | Actuation Force <br> $(\mathbf{N})$ |
| :---: | :---: | :---: | :---: | :---: |
| 58 | 3.4 | 1 | 145 | 320 |
| 40 | 7.5 | 5 | 100 | 1600 |
| 20 | 12 | 12 | 50 | 3840 |
| Stall | 18 | 20 | 0 | 6400 |

## Work Table Slide Module (Y-Axis)

Table C.1.3: Power Screw Characteristics of MRM Work Table Slide Module

| $\mathbf{d}_{\mathbf{m}}(\mathbf{m m})$ | $\mathbf{f}$ | $\mathbf{L}(\mathbf{m m})$ | $\boldsymbol{\alpha}$ (Degrees) | $\mathbf{f}_{\mathbf{c}}$ | $\mathbf{d}_{\mathbf{c}}(\mathbf{m m})$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 22.15 | 0.25 | 3 | 30 | 0.0015 | 17 |

Relationship between torque and linear load with direction of motion opposing direction of load:
$W=T\left[\frac{d_{m}}{2} \frac{f \pi d_{m}+L \cos \alpha_{n}}{\pi d_{m} \cos \alpha_{n}-f L}+\frac{f_{c} d_{c}}{2}\right]^{-1}$
$W=T\left[\frac{0.02215}{2} \frac{0.25 \times \pi \times 0.02215+0.003 \times \cos 30}{\pi \times 0.02215 \times \cos 30-0.25 \times 0.003}+\frac{2 \times 0.0015 \times 0.017}{2}\right]^{-1}$
$W=266.93 T$

Table C.1.4: Power Screw Actuation Characteristics of MRM Work Table Slide Module

| Motor Speed <br> $(\mathbf{r e v} / \mathbf{m i n})$ | Motor Current <br> $(\mathbf{a m p s})$ | Motor Torque <br> $(\mathbf{N} . \mathbf{m})$ | Actuation Speed <br> $(\mathbf{m m} / \mathbf{m i n})$ | Actuation Force <br> $(\mathbf{N})$ |
| :---: | :---: | :---: | :---: | :---: |
| 58 | 3.4 | 1 | 174 | 266.93 |
| 40 | 7.5 | 5 | 120 | 1334.65 |
| 20 | 12 | 12 | 60 | 3203.16 |
| Stall | 18 | 20 | 0 | 5338.60 |

## Column Module (Z-Axis)

Table C.1.5: Power Screw Characteristics of MRM Column Module

| $\mathbf{d}_{\mathbf{m}}(\mathbf{m m})$ | $\mathbf{f}$ | $\mathbf{L}(\mathbf{m m})$ | $\boldsymbol{\alpha}$ (Degrees) | $\mathbf{f}_{\mathbf{c}}$ | $\mathbf{d}_{\mathbf{c}}(\mathbf{m m})$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 22.15 | 0.25 | 3 | 30 | 0.0015 | 15 |

Relationship between torque and linear load with direction of motion opposing direction of load:
$W=T\left[\frac{d_{m}}{2} \frac{f \pi d_{m}+L \cos \alpha_{n}}{\pi d_{m} \cos \alpha_{n}-f L}+\frac{f_{c} d_{c}}{2}\right]^{-1}$
$W=T\left[\frac{0.02215}{2} \frac{0.25 \times \pi \times 0.02215+0.003 \times \cos 30}{\pi \times 0.02215 \times \cos 30-0.25 \times 0.003}+\frac{2 \times 0.0015 \times 0.015}{2}\right]^{-1}$
$W=267.14 T$

Table C.1.6: Power Screw Actuation Characteristics of MRM Column Module

| Motor Speed <br> $(\mathbf{r e v} / \mathbf{m i n})$ | Motor Current <br> $(\mathbf{a m p s})$ | Motor Torque <br> $(\mathbf{N} . \mathbf{m})$ | Actuation Speed <br> $(\mathbf{m m / m i n})$ | Actuation Force <br> $(\mathbf{N})$ |
| :---: | :---: | :---: | :---: | :---: |
| 58 | 3.4 | 1 | 174 | 267.14 |
| 40 | 7.5 | 5 | 120 | 1335.70 |
| 20 | 12 | 12 | 60 | 3205.68 |
| Stall | 18 | 20 | 0 | 5342.80 |

## Cross Slide Module (Y-Axis and C-Axis)

Table C.1.7: Power Screw Characteristics of MRM Cross Slide Module

| $\mathbf{d}_{\mathrm{m}}(\mathrm{mm})$ | $\mathbf{f}$ | $\mathbf{L}(\mathbf{m m})$ | $\boldsymbol{\alpha}$ (Degrees) | $\mathbf{f}_{\mathbf{c}}$ | $\mathbf{d}_{\mathbf{c}}(\mathbf{m m})$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 10.75 | 0.25 | 2 | 15 | N/A | N/A |

Relationship between torque and linear load with direction of motion opposing direction of load:
$W=T\left[\frac{d_{m}}{2} \frac{f \pi d_{m}+L \cos \alpha_{n}}{\pi d_{m} \cos \alpha_{n}-f L}+\frac{f_{c} d_{c}}{2}\right]^{-1}$
$W=T\left[\frac{0.01075}{2} \frac{0.25 \times \pi \times 0.01075+0.002 \times \cos 15}{\pi \times 0.01075 \times \cos 15-0.25 \times 0.002}+0\right]^{-1}$
$W=576.01 T$

Table C.1.8: Power Screw Actuation Characteristics of MRM Cross Slide Module

| Motor Speed <br> $($ rev/min) | Motor Current <br> $(\mathbf{a m p s})$ | Motor Torque <br> $(\mathbf{N} . \mathbf{m})$ | Actuation Speed <br> $(\mathbf{m m / m i n})$ | Actuation Force <br> $(\mathbf{N})$ |
| :---: | :---: | :---: | :---: | :---: |
| 58 | 3.4 | 1 | 116 | 576.01 |
| 40 | 7.5 | 5 | 80 | 288.05 |
| 20 | 12 | 12 | 40 | 692.12 |
| Stall | 18 | 20 | 0 | 11520.20 |

## C. 2 Actuation Characteristics of Rotary Axes

For the "Work Table Rotary "module:
$\omega_{\text {output }}=\omega_{\text {input }} \frac{N_{\text {worm }}}{N_{\text {gear }}}=\frac{\omega_{\text {input }}}{56}$
$T_{\text {output }}=T_{\text {input }} \frac{\omega_{\text {input }}}{\omega_{\text {output }}}=56 T_{\text {input }}$
All other rotary axes possessed direct drive systems.

Table C.2.1: Actuation Characteristics of MRM Rotary Axes

| Motor <br> Speed <br> $($ rev/min) | Motor <br> Current <br> (amps) | Motor <br> Torque <br> (N.m) | A-Axis <br> Torque <br> (N.m) | B-Axis <br> Torque <br> (N.m) | C-Axis <br> Speed <br> $($ rev/min) | C-Axis <br> Torque <br> (N.m) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 58 | 3.4 | 1 | 1 | 1 | 1.036 | 56 |
| 40 | 7.5 | 5 | 5 | 5 | 0.714 | 280 |
| 20 | 12 | 12 | 12 | 12 | 0.357 | 672 |
| Stall | 18 | 20 | 20 | 20 | Stall | 1120 |

## C. 3 Module Actuation Loading Calculations

## Module Actuation Loading and Torque/Force Amplification

The specification of the maximum load that a module can sustain along its axis of actuation is primarily constrained by the load that will cause the drive motor to stall during operation. The torque and force amplification created by power screws and gearboxes may lead to excessive deflections or mechanical fracture before the drive motor stalls. In these instances the maximum load specification must be reduced to below the stall load. The cutting head rotary module and the tilt table module both possessed direct drive mechanisms with no other torque amplification systems; the maximum load that these modules are specified to sustain has therefore been set equal to the stall torque of the motor ( $20 \mathrm{~N} . \mathrm{m}$ ). The rotary table module possessed a worm gearbox; this gearbox was the mechanical equivalent of the internal worm gearboxes possessed by the drive motors. The maximum load that the rotary table module can sustain was therefore also limited to 20 N.m of torque. The calculations presented in the following subsections relate exclusively to the load specifications for linear axes.

## Base Module (X-Axis)

Failure mode: Thread stripping calculation.

Table C.3.1: Physical Specifications of Power Screw Nut on Base Module

| Nut Material | Nut Height <br> $(\mathrm{mm})$ | Thread Specification | Shear Strength <br> $\mathbf{S}_{\text {shear }}($ MPa $)$ |
| :---: | :---: | :---: | :---: |
| Brass | 50 | $\mathrm{M} 20 \times 2.5$ | 206 |

$F_{e}=\pi d(0.75 t) S_{\text {shear }}=\pi \times 0.020 \times(0.75 \times 0.05) \times 206 \times 10^{6}=485.376 \mathrm{kN}$

Failure mode: Failure of shear pin in motor coupling.

Table C.3.2: Physical Specifications of Shear Pin and Shaft on Base Module

| Pin Material | Pin Diameter <br> $(\mathbf{m m})$ | Motor Shaft <br> Diameter $(\mathbf{m m})$ | Pin Shear Strength <br> $\mathbf{S}_{\text {shear }}($ MPa $)$ |
| :---: | :---: | :---: | :---: |
| Steel | 4 mm | 12 mm | 206 |

$A_{\text {Shear }}=2 \times \pi \frac{d^{2}}{4}=2 \times \pi \times \frac{0.004^{2}}{4}=25.133 \times 10^{-6} \mathrm{~m}^{2}$
$F_{\text {Shear }}=S_{\text {Shear }} \times A_{\text {Shear }}=206 \times 10^{6} \times 25.133 \times 10^{-6}=5177.398 \mathrm{~N}$
$T_{\text {Shear }}=F_{\text {Shear }} \times \frac{d_{\text {shaft }}}{2}=5177.398 \times \frac{0.012}{2}=31.064 \mathrm{~N} . \mathrm{m}$

This is greater than the motor stall torque; therefore the force related to this toque is too high to be used as a limit.

Failure mode: Shear failure of bolts on slide/ power screw attachment system.


Figure C.3.1: Slide - Power Screw Attachment Bracket

Table C.3.3: Physical Specifications of Bolts on Slide Attachment Bracket

| Bolt Size | SAE Class | Shear Strength S $_{\text {shear }}$ (MPa) |
| :---: | :---: | :---: |
| M6x1 | 12.9 | 756 |

$$
\begin{aligned}
& F_{\text {Shear }}=A S_{\text {shear }}=\frac{\pi}{4} \times 0.006^{2} \times 756 \times 10^{6}=21375 \mathrm{~N} \\
& F_{\text {Total }}=F_{\text {shear }} \times 4=85500 \mathrm{~N}
\end{aligned}
$$

Failure mode: Bearing failure under axial load.
Bearing: Deep Groove Ball Bearing SKF 61803
Static radial load rating: $C_{o}=930 \mathrm{~N}$
Axial load rating: $F_{\text {axial }}=0.5 C_{o}=465 \mathrm{~N}$
Two bearings: $F=930 \mathrm{~N}$

## Summary of Failure modes:

Table C.3.4: Summary of Failure Modes on Base Module

| Summary |  |
| :--- | :--- |
| Power Screw Thread Stripping | 485.376 kN |
| Motor Stall | 6400 N |
| Shear Pin on Motor Shaft | $\mathrm{F}_{\text {shear }}>\mathrm{F}_{\text {stall }}$ |
| Shear of Bolts on slide attachment | 85500 N |
| Bearing Failure | 930 N |

## Work Table Slide Module (Y-Axis)

Failure mode: Thread stripping calculation.

Table C.3.5: Physical Specifications of Power Screw Nut on Work Table Slide Module

| Nut Material | Nut Height <br> $(\mathrm{mm})$ | Thread Specification | Shear Strength <br> $\mathbf{S}_{\text {shear }}(\mathbf{M P a})$ |
| :---: | :---: | :---: | :---: |
| Brass | 50 | M24x3 | 206 |

$F_{e}=\pi d(0.75 t) S_{\text {shear }}=\pi \times 0.024 \times(0.75 \times 0.05) \times 206 \times 10^{6}=582.451 \mathrm{kN}$
Failure mode: Failure of shear pin on motor coupling; pin specifications and calculations same as in base module.
$F_{\text {Shear }}>F_{\text {Stall }}$
Failure mode: Bearing failure under axial load, bearing specification same as in base module.
$F=930 \mathrm{~N}$

## Summary of Failure modes:

Table C.3.6: Summary of Failure Modes on Work Table Slide Module

| Summary |  |
| :--- | :--- |
| Power Screw Thread Stripping | 582.451 kN |
| Motor Stall | 5338.6 N |
| Shear Pin on Motor Shaft | $\mathrm{F}_{\text {shear }}>\mathrm{F}_{\text {stall }}$ |
| Bearing Failure | 930 N |

## Column Module (Z- Axis)

Failure mode: Thread stripping calculation; thread specifications and calculations same as in work table slide module.
$F_{e}=582.451 k N$

Failure mode: Failure of shear pin on motor coupling; pin specifications and calculations same as in base module.
$F_{\text {Shear }}>F_{\text {Stall }}$

Failure mode: Thrust Bearing failure under axial load.
Bearing: Thrust Ball Bearing SKF 51102
Static axial load rating: $C_{o}=11200 \mathrm{~N}$
Dynamic axial load rating: $C=9360 \mathrm{~N}$

Failure mode: Deflection of column support rods and power screw.


Figure C.3.2: Loading on Support Rods and Power Screw for Pure Vertical Force on Sliding Interface

The loading scenario on the support rods and power screw is presented in Figure C.3.2 for a pure vertical force on the column es sliding interface. The axial stress on the screw and rods has been neglected as its effect on the deflection of the members is expected to be small. The primary loads that contribute to the deflection of the members are the moments generated by the force. The deflection of a beam under the action of a moment $M_{o}$ at a distance , $a^{\text {ec }}$ from its supported end is given by equation C.3.1. Figure C.3.3 illustrates the loading scenario for a single rod.

$$
\begin{equation*}
\delta_{B}=\frac{M_{o} a}{2 E I}(2 L-a) \tag{С.3.1}
\end{equation*}
$$



## Figure C.3.3: Loading on a Single Beam

For the loading scenario of Figure C.3.2:
$M_{\text {front rods }}=R \times F=0.02445 F$
$M_{\text {screw }}=R \times F=0.0545 F$
$M_{\text {back rods }}=R \times F=0.08445 F$
Manipulating equation C.3.1:

$$
\begin{equation*}
\delta_{B}=\frac{M_{o} a}{2 E I}(2 L-a)=\frac{F R a}{2 E I}(2 L-a)=F\left[\frac{R a}{2 E I}(2 L-a)\right] \tag{С.3.2}
\end{equation*}
$$

The stiffness of a beam at a distance " a " from the support is given by equation C.3.3:

$$
\begin{equation*}
K_{B}=\frac{F}{\delta_{B}}=\left[\frac{R a}{2 E I}(2 L-a)\right]^{-1} \tag{C.3.3}
\end{equation*}
$$

For springs in parallel:

$$
\begin{equation*}
K_{\text {Total }}=K_{1}+K_{2}+\cdots+K_{n} \tag{С.3.4}
\end{equation*}
$$

The total effective stiffness of the column in for the loading scenario of Figure C.3.2 is given by equation C.3.5:

$$
\begin{equation*}
K_{\text {Total }}=2 K_{1}+K_{2}+2 K_{3} \tag{С.3.5}
\end{equation*}
$$

Where:
$K_{1}=\left[\frac{0.02445 a}{2 E_{\text {rod }} I_{\text {rod }}}\left(2 L_{\text {rod }}-a\right)\right]^{-1}$
$K_{2}=\left[\frac{0.0545 a}{2 E_{\text {screw }} I_{\text {screw }}}\left(2 L_{\text {screw }}-a\right)\right]^{-1}$
$K_{3}=\left[\frac{0.08445 a}{2 E_{\text {rod }} I_{\text {rod }}}\left(2 L_{\text {rod }}-a\right)\right]^{-1}$

Table C.3.7: Physical Characteristics of Column Support Elements

|  | $\mathbf{d}(\mathbf{m m})$ | $\mathbf{E}(\mathbf{G P a})$ | $\mathbf{a}(\mathbf{m m})$ | $\mathbf{L}(\mathbf{m m})$ |
| :---: | :---: | :---: | :---: | :---: |
| Rods | 15.00 | 207 | 600 | 700 |
| Screw | 24.00 | 207 | 600 | 700 |

By the parallel axis theorem (distance between two axes $r=0.0425 \mathrm{~m}$ ):
$I_{\text {rod }}=\frac{\pi d^{4}}{64}+A r^{2}=\frac{\pi \times 0.015^{4}}{64}+\left(\frac{\pi 0.015^{2}}{4}\right) \times 0.0425^{2}=321.676 \times 10^{-9} \mathrm{~m}^{4}$
$I_{\text {screw }}=\frac{\pi d^{4}}{64}=\frac{\pi \times 0.024^{4}}{64}=16.286 \times 10^{-9} \mathrm{~m}^{4}$
$K_{1}=\left[\frac{0.02445 \times 0.6}{2 \times 207 \times 10^{9} \times 321.676 \times 10^{-9}}(2 \times 0.7-0.6)\right]^{-1}=11.347 \times 10^{6} \mathrm{~N} . \mathrm{m}^{-1}$
$K_{2}=\left[\frac{0.0545 \times 0.6}{2 \times 207 \times 10^{9} \times 16.286 \times 10^{-9}}(2 \times 0.7-0.6)\right]^{-1}=257.737 \times 10^{3} \mathrm{~N} . \mathrm{m}^{-1}$
$K_{3}=\left[\frac{0.08445 \times 0.6}{2 \times 207 \times 10^{9} \times 321.676 \times 10^{-9}}(2 \times 0.7-0.6)\right]^{-1}=3.285 \times 10^{6} \mathrm{~N} . \mathrm{m}^{-1}$
$K_{\text {Total }}=2 \times 11.347 \times 10^{6}+257.737 \times 10^{3}+2 \times 3.285 \times 10^{6}=29.522 \times 10^{6} \mathrm{~N} . \mathrm{m}^{-1}$

The maximum tolerable deflection for the column structure has been set at 0.1 mm . The force associated with this deflection is:
$F=K_{\text {Total }} \times \delta=29.522 \times 10^{6} \times 0.1 \times 10^{-3}=2952.20 \mathrm{~N}$

Failure mode: Buckling of column under compressive load. This calculation is limited to the critical load that would lead to buckling on the central power screw. The calculation ignores the support effects of the four guide rods, thus providing a conservative limit to the compressive forces that may be allowed in the module.
$P_{c r}=\frac{\pi^{2} E I}{L^{2}}=\frac{\pi^{2} \times 207 \times 10^{9} \times 16.286 \times 10^{-9}}{0.7^{2}}=21.614 \times 10^{6} \mathrm{~N}$

## Summary of Failure modes:

Table C.3.8: Summary of Failure Modes on Column Module

| Summary |  |
| :--- | :--- |
| Power Screw Thread Stripping | 582.451 kN |
| Motor Stall | 5342.8 N |
| Shear Pin on Motor Shaft | $\mathrm{F}_{\text {shear }}>\mathrm{F}_{\text {stall }}$ |
| Bearing Failure | 9360 N |
| Deflection of Column $(\mathbf{0 . 1 ~ m m})$ | 2952.2 N |
| Buckling of Column | 21.641 MN |

## Cross Slide Module (Y-Axis and C-Axis)

Failure mode: Thread stripping calculation.

Table C.3.9: Physical Specifications of Power Screw Nut on Cross Slide Module

| Nut Material | Nut Height <br> $(\mathrm{mm})$ | Thread Specification | Shear Strength <br> $\mathbf{S}_{\text {shear }}(\mathbf{M P a})$ |
| :---: | :---: | :---: | :---: |
| Brass | 20 | Trapezoidal 12x2 | 206 |

$F_{e}=\pi d(0.75 t) S_{\text {shear }}=\pi \times 0.012 \times(0.75 \times 0.02) \times 206 \times 10^{6}=116.490 \mathrm{kN}$

Failure mode: Failure of shear pin on motor coupling; pin specifications and calculations same as in base module.
$F_{\text {Shear }}>F_{\text {Stall }}$

Failure mode: Failure of motor gearbox due to an axial thrust force. The axial thrust forces on the motor shaft are sustained by a thin steel plate which forms the back cover of the worm gearbox. This cover keeps the worm and gear in mesh by restricting the movement of the gear shaft. Finite element analysis was performed on the plate to determine a tolerable maximum thrust force on the motor shaft. The force was applied as a point load at the central point of contact between the shaft and the plate. Fixed constraints were applied to the three fastening points on the plate. The results of the analysis resulted in the maximum force being set to 250 N , which has an associated deflection of 0.1221 mm . Further details of the analysis are found below.

Table C.3.10: Material Properties of Steel Plate

| Carbon Steel |  |
| :--- | :--- |
| Young's Modulus | $2 . \mathrm{e}+005 \mathrm{MPa}$ |
| Poisson's Ratio | 0.29 |
| Mass Density | $7.87 \mathrm{e}-006 \mathrm{~kg} / \mathrm{mm}^{3}$ |
| Tensile Yield Strength | 350.0 MPa |
| Tensile Ultimate Strength | 420.0 MPa |

Table C.3.11: Loading and Constraints Definition

| Load and Constraint Definitions |  |  |  |
| :---: | :---: | :---: | :---: |
| Name | Type | Magnitude | Vector |
| Force 1 | Surface Force | 250.0 N | 0.0 N 0.0 N 250.0 N |
| Fixed Constraint 1 | Edge Fixed Constraint | 0.0 mm | $\begin{aligned} & 0.0 \mathrm{~mm} \\ & 0.0 \mathrm{~mm} \\ & 0.0 \mathrm{~mm} \end{aligned}$ |

Table C.3.12: Structural Results

| Structural Results |  |  |
| :---: | :---: | :---: |
| Name | Minimum | Maximum |
| Equivalent Stress | 0.3424 MPa | 177.3 MPa |
| Maximum Principal Stress | $-9.362 \mathrm{MPa}$ | 182.6 MPa |
| Minimum Principal Stress | -189.6 MPa | 36.49 MPa |
| Deformation | 0.0 mm | 0.1221 mm |
| Safety Factor | 1.974 | N/A |

$$
\begin{aligned}
& \text { Type: Equivalent Stress } \\
& \text { Unit: MPa }
\end{aligned}
$$

$=$| 177.28 Max |
| :--- |
| 157.62 |
| 137.96 |
| 118.3 |
| 98.64 |
| 78.98 |
| 59.321 |
| 39.661 |
| 20.002 |
| 0.34241 Min |




Figure C.3.4: Equivalent Stress on Motor Plate


Figure C.3.5: Maximum Principle Stress on Motor Plate

| Deformation <br> Type: Deformation Unit: mm |
| :---: |
|  |  |
|  |  |
|  |
|  |
| 0.094991 |
| 0.081421 |
| 0.067851 |
| 0.054281 |
| 0.04071 |
| 0.02714 |
| 0.01357 |
| 0 Min |



Figure C.3.6: Deformation of Motor Plate

## Summary of Failure modes:

Table C.3.13: Summary of Failure Modes on Cross Slide Module

| Summary |  |
| :--- | :--- |
| Power Screw Thread Stripping | 116.490 kN |
| Motor Stall | 11520.2 N |
| Shear Pin on Motor Shaft | $\mathrm{F}_{\text {shear }}>\mathrm{F}_{\text {stall }}$ |
| Deflection of Motor Back Plate | 250 N |

## C. 4 Normal Loading Calculations

The calculations presented in this section were used to determine the maximum perpendicular/normal loads that a module can sustain on its moving interface. The loading for selected modules are as follows:

- For the work table rotary module and cutting head rotary module, the maximum load is limited by the maximum thrust load that can be sustained by the motor gearboxes. This force is 250 N , as calculated in section C. 3
- Not determined for the base module as prior failure of other MRM modules in all configurations are expected prior to the failure of the base module under the action of a normal load on its slide.


## Work Table Slide Module (Y-Axis)

Failure mode: Deflection of power screw and supporting rods under a normal load. The loading scenario is illustrated in Figure C.4.1.


Figure C.4.1: Loading on Work Table Slide Power Screw and Support Rods

For the loading scenario of Figure C.4.1:

$$
\begin{equation*}
\delta=\frac{P L^{3}}{48 E I} \tag{C4.1}
\end{equation*}
$$

Therefore:

$$
\begin{equation*}
K=\frac{P}{\delta}=\frac{48 E I}{L^{3}} \tag{C4.2}
\end{equation*}
$$

Table C.4.1: Physical Characteristics of Work Table Slide Support Elements

|  | d (mm) | E (GPa) | L (mm) |
| :---: | :---: | :---: | :---: |
| Rods | 20 | 207 | 410 |
| Screw | 24.00 | 207 | 410 |

$I_{\text {rod }}=\frac{\pi d^{4}}{64}=\frac{\pi \times 0.02^{4}}{64}=7.834 \times 10^{-9} \mathrm{~m}^{4}$
$I_{\text {screw }}=\frac{\pi d^{4}}{64}=\frac{\pi \times 0.024^{4}}{64}=16.286 \times 10^{-9} \mathrm{~m}^{4}$
$K_{\text {rod }}=\frac{48 E I}{L^{3}}=\frac{48 \times 207 \times 10^{9} \times 7.834 \times 10^{-9}}{0.41^{3}}=1.129 \times 10^{6} \mathrm{~N} . \mathrm{m}^{-1}$
$K_{\text {screw }}=\frac{48 E I}{L^{3}}=\frac{48 \times 207 \times 10^{9} \times 16.286 \times 10^{-9}}{0.41^{3}}=2.349 \times 10^{6} \mathrm{~N} . \mathrm{m}^{-1}$
$K_{\text {Total }}=2 \times 1.129 \times 10^{6}+2.349 \times 10^{6}=4.607 \times 10^{6}{\mathrm{~N} . \mathrm{m}^{-1}}$

The maximum tolerable deflection for the structure has been set as 0.1 mm . The force associated with this deflection is:
$F=K_{\text {Total }} \times \delta=455.6 \times 10^{3} \times 0.1 \times 10^{-3}=460.700 \mathrm{~N}$

## Column Module (Z-Axis)

Failure mode: Deflection of power screw and supporting rods under a normal load. The loading scenario is illustrated in Figure C.4.2


Figure C.4.2: Loading on Column Power Screw and Support Rods

For the loading scenario of Figure C.4.1:

$$
\begin{equation*}
\delta=\frac{P a^{2}}{6 E I}(3 L-a) \tag{C4.1}
\end{equation*}
$$

Therefore:

$$
\begin{equation*}
K=\frac{P}{\delta}=\frac{6 E I}{a^{2}(3 L-a)} \tag{C4.2}
\end{equation*}
$$

For physical properties of the module and relevant lengths refer to Table C.3.7
$I_{\text {rod }}=\frac{\pi d^{4}}{64}+A r^{2}=321.676 \times 10^{-9} \mathrm{~m}^{4}$
$I_{\text {screw }}=\frac{\pi d^{4}}{64}=16.286 \times 10^{-9} \mathrm{~m}^{4}$
$K_{\text {rod }}=\frac{6 E I}{a^{2}(3 L-a)}=\frac{6 \times 207 \times 10^{9} \times 321.676 \times 10^{-9}}{0.6^{2}(3 \times 0.7-0.6)}=7.399 \times 10^{5} \mathrm{~N} . \mathrm{m}^{-1}$
$K_{\text {screw }}=\frac{6 E I}{a^{2}(3 L-a)}=\frac{6 \times 207 \times 10^{9} \times 16.286 \times 10^{-9}}{0.6^{2}(3 \times 0.7-0.6)}=3.746 \times 10^{4} \mathrm{~N} . \mathrm{m}^{-1}$
$K_{\text {Total }}=4 \times 7.399 \times 10^{5}+3.746 \times 10^{4}=2.997 \times 10^{6} \mathrm{~N} . \mathrm{m}^{-1}$

The maximum tolerable deflection for the structure has been set as 0.1 mm . The force associated with this deflection is:
$F=K_{\text {Total }} \times \delta=2.997 \times 10^{6} \times 0.1 \times 10^{-3}=300.05 \mathrm{~N}$

## Cross slide Module (Y-Axis and C-Axis)

Failure Mode: Failure of motor gearbox by associated force.
The load restriction on the motor is a force of 250 N along the axis of the output shaft from its gearbox. This corresponds to $P_{y}=250 \mathrm{~N}$ (see Section 5.10.1). Based on the approximation of equation 5.4.3:
$\frac{P_{y}}{P_{z}} \approx 0.2$ to 0.1
The maximum allowable vertical load on a cutting tool that is associated with the cross slide module has been approximated as:
$P_{z}=\frac{P_{y}}{0.1}=\frac{250}{0.1}=2500 \mathrm{~N}$

## Tilt Table (B-Axis)

Failure Mode: Shearing of pin connecting drive shaft to leaver arm.

Table C.4.2: Physical Specifications of Shear Pin and Shaft in Tilt Table Module

| Pin Material | Pin Diameter <br> $(\mathrm{mm})$ | Drive Shaft <br> Diameter $(\mathrm{mm})$ | Pin Shear <br> Strength <br> $\mathbf{S}_{\text {shear }}(\mathrm{MPa})$ | Length of <br> Leaver Arm <br> $(\mathrm{mm})$ |
| :---: | :---: | :---: | :---: | :---: |
| Steel | 4 mm | 12 mm | 206 | 85 |

$A_{\text {Shear }}=2 \times \pi \frac{d^{2}}{4}=2 \times \pi \times \frac{0.004^{2}}{4}=25.133 \times 10^{-6} \mathrm{~m}^{2}$
$F_{\text {Shear }}=S_{\text {Shear }} \times A_{\text {Shear }}=206 \times 10^{6} \times 25.133 \times 10^{-6}=5177.398 \mathrm{~N}$
$T_{\text {Shear }}=F_{\text {Shear }} \times \frac{d_{\text {shaft }}}{2}=5177.398 \times \frac{0.015}{2}=38.830 \mathrm{~N} . \mathrm{m}$
$T_{\text {Shear }}>\left(T_{\text {Stall }}=20 \mathrm{~N} . \mathrm{M}\right)$

Mass associated if tilt table is tilted $90^{\circ}$ from a horizontal position:
$M=\frac{T}{g \times L}=\frac{20}{9.81 \times 0.085}=24 \mathrm{~kg}$
This mass has been selected for the maximum normal load, because if loaded while interface is horizontal (creating a normal load), and then moved by $90^{\circ}$ it will cause the drive motor to stall.

## C. 5 Stiffness Calculations for Drilling Assembly

The calculations in this section pertain to the drilling subassembly of Figure 5.40

## Range Extension Arm

Position and Rotation Matrices (see Appendix B.11):

$$
\begin{aligned}
& { }_{i}^{i+1} M_{\text {Drill Head }}=\left[\begin{array}{lllc}
1 & 0 & 0 & -75 \\
0 & 1 & 0 & 0 \\
0 & 0 & 1 & -81.5 \\
0 & 0 & 0 & 1
\end{array}\right] \\
& { }^{i+1} R=\left[\begin{array}{lll}
1 & 0 & 0 \\
0 & 1 & 0 \\
0 & 0 & 1
\end{array}\right] \\
& { }_{i}^{i+1} P=\left[\begin{array}{c}
-75 \\
0 \\
-81.5
\end{array}\right]
\end{aligned}
$$

Torque and Force Propagation

$$
\begin{aligned}
& { }^{i+1} f_{i+1}={ }_{i}^{i+1} R{ }^{i} f_{i}=\left[\begin{array}{lll}
1 & 0 & 0 \\
0 & 1 & 0 \\
0 & 0 & 1
\end{array}\right]\left[\begin{array}{l}
0 \\
0 \\
F_{t}
\end{array}\right]=\left[\begin{array}{l}
0 \\
0 \\
F_{t}
\end{array}\right] \\
& { }^{i+1} n_{i+1}={ }_{i}^{i+1} R \quad{ }^{i} n_{i}+{ }_{i}^{i+1} P \quad \times{ }^{i+1} f_{i+1}=\left[\begin{array}{lll}
1 & 0 & 0 \\
0 & 1 & 0 \\
0 & 0 & 1
\end{array}\right]\left[\begin{array}{l}
0 \\
0 \\
0
\end{array}\right]+\left[\begin{array}{c}
-75 \\
0 \\
-81.5
\end{array}\right] \times\left[\begin{array}{c}
0 \\
0 \\
F_{t}
\end{array}\right]=\left[\begin{array}{c}
0 \\
75 F_{t} \\
0
\end{array}\right]
\end{aligned}
$$

The loading scenario will therefore be a force of $\mathrm{F}_{\mathrm{t}}(\mathrm{N})$ and a torque of $75 \mathrm{~F}_{\mathrm{t}}(\mathrm{N} . \mathrm{mm})$ on the interface between the drilling head and the range extension arm.


Figure C.5.1: Loading on Range Extension Arm for both Vertical and Horizontal Scenarios

Table C.5.1: Physical Specifications of Range Extension Arm

| Material | E (GPa | $\mathbf{L}(\mathbf{m m})$ | $\mathbf{d}_{\mathbf{0}}(\mathbf{m m})$ | $\mathbf{d}_{\mathbf{i}}(\mathbf{m m})$ |
| :---: | :---: | :---: | :---: | :---: |
| Aluminum | 72 | 350 | 76.2 | 69.84 |

By superposition, the deflection due to the combined load is given:

$$
\begin{equation*}
\delta=\frac{P L^{3}}{3 E I}+\frac{M_{o} L^{2}}{2 E I} \tag{C.5.1}
\end{equation*}
$$

Therefore:

$$
\begin{gather*}
\delta=\frac{2 P L^{3}+3 M_{o} L^{2}}{6 E I} \\
\delta=\frac{2 F_{t} L^{3}+3 \times 0.075 F_{t} L^{2}}{6 E I} \\
\delta=\frac{F_{t}\left(2 L^{3}+0.225 L^{2}\right)}{6 E I} \\
K=\frac{F_{t}}{\delta}=\frac{6 E I}{2 L^{3}+0.225 L^{2}} \tag{С.5.2}
\end{gather*}
$$

Moments of inertia for machining arm (Cross section: thin circular ring)

$$
\begin{equation*}
I_{x}=I_{y}=\frac{\pi\left(d_{o}^{4}-d_{i}^{4}\right)}{64} \tag{C.5.3}
\end{equation*}
$$

Substituting dimensions from Table C.5.1

$$
\begin{aligned}
& I_{x}=I_{y}=\frac{\pi\left(d_{o}^{4}-d_{i}^{4}\right)}{64}=\frac{\pi\left(0.0762^{4}-0.06984^{4}\right)}{64}=487.119 \times 10^{-9} \mathrm{~m}^{4} \\
& K=\frac{6 E I}{2 L^{3}+0.225 L^{2}}=\frac{6 \times 72 \times 10^{9} \times 487.119 \times 10^{-9}}{2 \times 0.370^{3}+0.225 \times 0.370^{2}}=1.592900 \times 10^{6} \mathrm{~N} . \mathrm{m}^{-1} \\
& K_{H 1}=K_{V 1}=1.592 \times 10^{6} \mathrm{N.m}^{-1}
\end{aligned}
$$

## Cutting Head Rotary Module

Position and Rotation Matrices (see Appendix B.5):

$$
\begin{aligned}
& { }^{i+1}{ }_{i} M_{\text {Extension Arm }}=\left[\begin{array}{lllc}
1 & 0 & 0 & -370 \\
0 & 1 & 0 & 0 \\
0 & 0 & 1 & 0 \\
0 & 0 & 0 & 1
\end{array}\right] \\
& { }^{i+1} R=\left[\begin{array}{lll}
1 & 0 & 0 \\
0 & 1 & 0 \\
0 & 0 & 1
\end{array}\right] \\
& { }^{i+1} P=\left[\begin{array}{c}
-370 \\
0 \\
0
\end{array}\right]
\end{aligned}
$$

Torque and Force Propagation

$$
{ }^{i+1} f_{i+1}={ }_{i}^{i+1} R{ }^{i} f_{i}=\left[\begin{array}{ccc}
1 & 0 & 0 \\
0 & 1 & 0 \\
0 & 0 & 1
\end{array}\right]\left[\begin{array}{c}
0 \\
0 \\
F_{t}
\end{array}\right]=\left[\begin{array}{c}
0 \\
0 \\
F_{t}
\end{array}\right]
$$

$$
{ }^{i+1} n_{i+1}={ }_{i}^{i+1} R \text { i } n_{i}+{ }_{i}^{i+1} P \quad \times{ }^{i+1} f_{i+1}=\left[\begin{array}{lll}
1 & 0 & 0 \\
0 & 1 & 0 \\
0 & 0 & 1
\end{array}\right]\left[\begin{array}{c}
0 \\
75 F_{t} \\
0
\end{array}\right]+\left[\begin{array}{c}
-370 \\
0 \\
0
\end{array}\right] \times\left[\begin{array}{l}
0 \\
0 \\
F_{t}
\end{array}\right]=\left[\begin{array}{c}
0 \\
445 F_{t} \\
0
\end{array}\right]
$$

The loading scenario will therefore be a force of $\mathrm{F}_{\mathrm{t}}(\mathrm{N})$ and a torque of $445 \mathrm{~F}_{\mathrm{t}}(\mathrm{N} . \mathrm{mm})$ on the interface between the drilling head and the range extension arm. Refer to Figure C.5.1.

Table C.5.2: Physical Specifications of Cutting Head Rotary Module

| Material | $\mathbf{E}(\mathbf{G P a})$ | $\mathbf{L}(\mathbf{m m})$ | $\mathbf{h}_{\mathbf{0}}(\mathbf{m m})$ | $\mathbf{h}_{\mathbf{i}}(\mathbf{m m})$ | $\mathbf{b}_{\mathbf{0}}(\mathbf{m m})$ | $\mathbf{b}_{\mathbf{i}}(\mathbf{m m})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Aluminum | 72 | 110 | 108 | 100 | 116 | 96 |

By super position:

$$
\delta=\frac{2 P L^{3}+3 M_{o} L^{2}}{6 E I}
$$

Substituting loads:

$$
\begin{gather*}
\delta=\frac{2 P L^{3}+3 M_{o} L^{2}}{6 E I} \\
\delta=\frac{\left(2 F_{t} L^{3}+3 \times 0.445 F_{t} L^{2}\right)}{6 E I} \\
\delta=\frac{F_{t}\left(2 L^{3}+1.335 L^{2}\right)}{6 E I} \\
K=\frac{F_{t}}{\delta}=\frac{6 E I}{2 L^{3}+1.335 L^{2}} \tag{C.5.4}
\end{gather*}
$$

Moments of inertia for cutting head rotary module (Cross section: rectangular ring)

$$
\begin{align*}
& I_{x}=\frac{b_{o} h_{o}^{3}-b_{i} h_{i}^{3}}{12}  \tag{С.5.5}\\
& I_{y}=\frac{h_{o} b_{o}^{3}-h_{i} b_{i}^{3}}{12} \tag{C.5.6}
\end{align*}
$$

Substituting dimensions from Table C.5.2
$I_{x}=\frac{b_{o} h_{o}^{3}-b_{i} h_{i}^{3}}{12}=\frac{0.116 \times 0.108^{3}-0.096 \times 0.100^{3}}{12}=4.1772 \times 10^{-6} \mathrm{~m}^{4}$
$I_{y}=\frac{h_{o} b_{o}^{3}-h_{i} b_{i}^{3}}{12}=\frac{0.108 \times 0.116^{3}-0.100 \times 0.096^{3}}{12}=6.6753 \times 10^{-6} \mathrm{~m}^{4}$
$K_{V 2}=\frac{6 E I}{2 L^{3}+1.335 L^{2}}=\frac{6 \times 72 \times 10^{9} \times 4.1772 \times 10^{-6}}{2 \times 0.110^{3}+1.335 \times 0.110^{2}}=95.908 \times 10^{6} \mathrm{~N} . \mathrm{m}^{-1}$
$K_{H 2}=\frac{6 E I}{2 L^{3}+1.335 L^{2}}=\frac{6 \times 72 \times 10^{9} \times 6.6735 \times 10^{-6}}{2 \times 0.110^{3}+1.335 \times 0.110^{2}}=153.222 \times 10^{6} \mathrm{~N} . \mathrm{m}^{-1}$

## Column Module

Position and Rotation Matrices (see Appendix B.3):

$$
{ }_{i}^{i+1} M_{\text {CH Rotary }}=\left[\begin{array}{cccc}
1 & 0 & 0 & -138 \\
0 & c \gamma & -s \gamma & 0 \\
0 & s \gamma & c \gamma & 0 \\
0 & 0 & 0 & 1
\end{array}\right]
$$

$$
{ }_{i}^{i+1} R=\left[\begin{array}{ccc}
1 & 0 & 0 \\
0 & c \gamma & -s \gamma \\
0 & s \gamma & c \gamma
\end{array}\right]
$$

$$
{ }_{i}^{i+1} P=\left[\begin{array}{c}
-138 \\
0 \\
0
\end{array}\right]
$$

## Torque and Force Propagation

$$
\begin{gathered}
{ }^{i+1} f_{i+1}={ }_{i}^{i+1} R{ }^{i} f_{i}=\left[\begin{array}{ccc}
1 & 0 & 0 \\
0 & c \gamma & -s \gamma \\
0 & s \gamma & c \gamma
\end{array}\right]\left[\begin{array}{c}
0 \\
0 \\
F_{t}
\end{array}\right]=\left[\begin{array}{c}
0 \\
-F_{t} s \gamma \\
F_{t} c \gamma
\end{array}\right] \\
{ }^{i+1} n_{i+1}={ }_{i}^{i+1} R{ }^{i} n_{i}+{ }_{i}^{i+1} P \quad \times{ }^{i+1} f_{i+1}=\left[\begin{array}{ccc}
1 & 0 & 0 \\
0 & c \gamma & -s \gamma \\
0 & s \gamma & c \gamma
\end{array}\right]\left[\begin{array}{c}
0 \\
445 F_{t} \\
0
\end{array}\right]+\left[\begin{array}{c}
-138 \\
0 \\
0
\end{array}\right] \times\left[\begin{array}{c}
0 \\
-F_{t} s \gamma \\
F_{t} c \gamma
\end{array}\right] \\
=\left[\begin{array}{c}
0 \\
583 F_{t} c \gamma \\
583 F_{t} s \gamma
\end{array}\right]
\end{gathered}
$$

## Vertical Orientation

For a vertically orientated drilling head $\gamma=0$, therefore:

$$
\begin{aligned}
& { }^{i+1} f_{i+1}=\left[\begin{array}{c}
0 \\
0 \\
F_{t}
\end{array}\right] \\
& { }^{i+1} n_{i+1}=\left[\begin{array}{c}
0 \\
583 F_{t} \\
0
\end{array}\right]
\end{aligned}
$$

Based on the load on the interface for $\gamma=0$, the loading on the rods and screw has been simplified to:
$M_{\text {front rods }}=R \times F=(0.583+0.02445) F=0.60745 F$
$M_{\text {screw }}=R \times F=(0.583+0.0545) F=0.6375 F$
$M_{\text {back rods }}=R \times F=(0.583+0.08445) F=0.66745$
The loading scenario on the members is that of figure C.5.3


Figure C.5.2: Deflections Caused by Loading on Column Members

$$
\begin{gather*}
\delta_{y}=\frac{L_{1}}{L_{2}} \delta_{x}=\frac{L_{1}}{L_{2}} \frac{M_{o} a}{2 E I}(2 L-a)  \tag{C.5.7}\\
\delta_{y}=\frac{L_{1}}{L_{2}} \frac{R F a}{2 E I}(2 L-a)
\end{gather*}
$$

For individual members $\mathrm{L}_{1}=\mathrm{R}$ and $\mathrm{L}_{2}=\mathrm{L}$ :

$$
\begin{align*}
& K=\frac{F}{\delta_{y}}=\frac{2 L E I}{R^{2} a(2 L-a)}  \tag{C.5.8}\\
& K=\frac{F}{\delta_{y}}=\frac{2 L E I}{R^{2} a(2 L-a)} \tag{C.5.9}
\end{align*}
$$

Table C.5.3: Physical Specifications of Column Support Elements

|  | $\mathbf{d}(\mathbf{m m})$ | $\mathbf{E}(\mathbf{G P a})$ | $\mathbf{a}(\mathbf{m m})$ | $\mathbf{L}(\mathbf{m m})$ | $\mathbf{R}(\mathbf{m m})$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Front Rods | 15.00 | 207 | 600 | 700 | 607.45 |
| Screw | 24.00 | 207 | 600 | 700 | 637.50 |
| Back Rods | 15.00 | 207 | 600 | 700 | 667.45 |

$$
\begin{aligned}
& I_{\text {rod }}=\frac{\pi d^{4}}{64}+A r^{2}=\frac{\pi \times 0.015^{4}}{64}+\left(\frac{\pi 0.015^{2}}{4}\right) \times 0.0425^{2}=321.676 \times 10^{-9} \mathrm{~m}^{4} \\
& I_{\text {screw }}=\frac{\pi d^{4}}{64}=\frac{\pi \times 0.024^{4}}{64}=16.286 \times 10^{-9} \mathrm{~m}^{4} \\
& K_{1}=\frac{2 L E I}{R^{2} a(2 L-a)}=\frac{2 \times 0.7 \times 207 \times 10^{9} \times 321.676 \times 10^{-9}}{0.60745^{2} \times 0.6 \times(2 \times 0.7-0.6)}=5.26326 \times 10^{5} \mathrm{N.m}^{-1} \\
& K_{2}=\frac{2 L E I}{R^{2} a(2 L-a)}=\frac{2 \times 0.7 \times 207 \times 10^{9} \times 16.286 \times 10^{-9}}{0.63750^{2} \times 0.6 \times(2 \times 0.7-0.6)}=2.4194 \times 10^{4} \mathrm{~N} . \mathrm{m}^{-1} \\
& K_{3}=\frac{2 L E I}{R^{2} a(2 L-a)}=\frac{2 \times 0.7 \times 207 \times 10^{9} \times 321.676 \times 10^{-9}}{0.66745^{2} \times 0.6 \times(2 \times 0.7-0.6)}=4.35952 \times 10^{5} \mathrm{~N}^{2} \mathrm{~m}^{-1}
\end{aligned}
$$

The elements act as springs in parallel:
$K_{\text {total }}=2 \times 5.26326 \times 10^{5}+2.4194 \times 10^{4}+2 \times 4.35952 \times 10^{5}=1.94875 \times 10^{6} \mathrm{~N} . \mathrm{m}^{-1}$
$K_{V 3}=1.94875 \times 10^{6} \mathrm{~N} . \mathrm{m}^{-1}$

## Horizontal Orientation

For a horizontally orientated drilling head $\gamma=90^{\circ}$, therefore:

$$
\begin{aligned}
{ }^{i+1} f_{i+1} & =\left[\begin{array}{c}
0 \\
-F_{t} \\
0
\end{array}\right] \\
{ }^{i+1} n_{i+1} & =\left[\begin{array}{c}
0 \\
0 \\
583 F_{t}
\end{array}\right]
\end{aligned}
$$

Based on the load on the interface for $\gamma=90^{\circ}$, the total torque about the center of the module is:
$M_{o}=R \times F=0.6375 F_{t}$
The power screw is located at the center; however by nature it cannot resist this torque. The torque is balanced by the guide rods which provide a normal reaction force. The guide rods and the power screw resist the horizontal force $F_{t}$. This is illustrated in Figure C.5.3 (Red: Force due to torque about center; Green: Force due to $\mathrm{F}_{\mathrm{t}}$ )


Figure C.5.3: Schematic Diagram of Loading on Column Power Screw and Guide Rods

For simplicity the effect of the torque and the effect of the force $F_{t}$ shall be dealt with separately. The torque $M_{o}$ will have the effect of rotating the system about its center as illustrated in Figure C.5.4.a, while the force $F_{t}$ will have the effect of causing a deflection of the module in the horizontal plane as illustrated in Figure C.5.4.b. The total deflection of the cutting head, due to the loading on the column is illustrated in Figure C.5.4.c.


Figure C.5.4: Deflection and Rotation of Column Module
a. Rotation of column module due to torque $\mathrm{M}_{0}$ generated by thrust force on drill
b. Deflection of column module due to force thrust force $F_{t}$
c. Combined deflection of drilling head due to thrust force

## Rotation Due to Torque



Figure C.5.5: Deflection of Individual Guide Rods in Relation to Deflection of Drilling Head
The rotation of the column module about its center is a result of the deflections of individual guide rods under the forces generated by the torque $\mathrm{M}_{0}$. The force on an individual rod, causing this deflection is $\mathrm{F}^{\text {ce }}$, where:

$$
\begin{equation*}
F^{`}=\grave{K} \delta \tag{C.5.10}
\end{equation*}
$$

The torque $\mathrm{M}_{0}$ represented as the sum of the individual torques generated by $\mathrm{F}^{\mathrm{C}}$ :

$$
\begin{equation*}
M_{o}=F_{t} L_{t}=4 \grave{F} D \tag{C.5.11}
\end{equation*}
$$

Relating the deflection of the drilling head to the deflection of an individual guide rod:

$$
\begin{equation*}
\grave{\delta}=\frac{D}{L_{t}} \delta \tag{C.5.12}
\end{equation*}
$$

Substituting equation C.5.10 into equation C.5.11

$$
\begin{equation*}
F_{t} L_{t}=4 \grave{K} \grave{\delta} D \tag{C.5.13}
\end{equation*}
$$

Substituting equation C.5.12 into equation C.5.13

$$
\begin{gather*}
\mathrm{F}_{\mathrm{t}}=4 \grave{\mathrm{~K}} \delta \frac{\mathrm{D}^{2}}{\mathrm{~L}_{\mathrm{t}}^{2}} \\
K=\frac{F_{t}}{\delta}=\frac{4 \grave{K} D^{2}}{L_{t}^{2}} \tag{C.5.14}
\end{gather*}
$$

For an individual rod (See Figure C.4.2 and equation C.4.2):

$$
\begin{equation*}
\grave{K}=\frac{6 E I}{a^{2}\left(3 L_{\text {rod }}-a\right)} \tag{C.5.15}
\end{equation*}
$$

Therefore:

$$
\begin{equation*}
K=\frac{24 E I D^{2}}{a^{2} L_{t}^{2}\left(3 L_{\text {rod }}-a\right)} \tag{C.5.14}
\end{equation*}
$$

Table C.5.4: Physical Parameters Relating to Torque Applied on Column

| E (GPa) | $\mathbf{D}(\mathbf{m m})$ | $\mathbf{d}(\mathbf{m m})$ | $\mathbf{a}(\mathbf{m m})$ | $\mathbf{L}_{\text {rod }}(\mathbf{m m})$ | $\mathbf{L}_{\mathrm{t}}(\mathbf{m m})$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 207 | 42.5 | 15.00 | 600 | 700 | 637.5 |

$I_{\text {rod }}=\frac{\pi d^{4}}{64}+A r^{2}=\frac{\pi \times 0.015^{4}}{64}+\left(\frac{\pi 0.015^{2}}{4}\right) \times 0.0601^{2}=6.408 \times 10^{-7} \mathrm{~m}^{4}$
$K=\frac{24 E I D^{2}}{a^{2} L_{t}^{2}\left(3 L_{\text {rod }}-a\right)}=\frac{24 \times 207 \times 10^{9} \times 6.408 \times 10^{-7} \times 0.0425^{2}}{0.6^{2} \times 0.6375^{2}(3 \times 0.7-0.6)}=2.620 \times 10^{4} \mathrm{~N} . \mathrm{m}^{-1}$

## Deflection Due to Drilling Thrust Force

The loading on individual members is as per Figure C.4.2

Table C.5.5: Physical Parameters Relating to Drilling Thrust Force on Column

|  | $\mathbf{d}(\mathbf{m m})$ | E (GPa) | $\mathbf{a}(\mathbf{m m})$ | L (mm) |
| :---: | :---: | :---: | :---: | :---: |
| Front Rods | 15.00 | 207 | 600 | 700 |
| Screw | 24.00 | 207 | 600 | 700 |
| Back Rods | 15.00 | 207 | 600 | 700 |

$I_{\text {rod }}=\frac{\pi d^{4}}{64}+A r^{2}=\frac{\pi \times 0.015^{4}}{64}+\left(\frac{\pi 0.015^{2}}{4}\right) \times 0.0425^{2}=321.676 \times 10^{-9} \mathrm{~m}^{4}$
$I_{\text {screw }}=\frac{\pi d^{4}}{64}=\frac{\pi \times 0.024^{4}}{64}=16.286 \times 10^{-9} \mathrm{~m}^{4}$
$K_{1}=\frac{6 E I}{a^{2}\left(3 L_{\text {rod }}-a\right)}=\frac{6 \times 207 \times 10^{9} \times 321.676 \times 10^{-9}}{0.6^{2}(3 \times 0.7-0.6)}=739.855 \times 10^{3} \mathrm{~N} . \mathrm{m}^{-1}$
$K_{2}=\frac{6 E I}{a^{2}\left(3 L_{\text {screw }}-a\right)}=\frac{6 \times 207 \times 10^{9} \times 16.286 \times 10^{-9}}{0.6^{2}(3 \times 0.7-0.6)}=37.458 \times 10^{3} \mathrm{~N} . \mathrm{m}^{-1}$
The members act as springs in parallel
$K=4 \times 739.855 \times 10^{3}+37.458 \times 10^{3}=2.997 \times 10^{6} \mathrm{~N} . \mathrm{m}^{-1}$

## Total Horizontal Stiffness

The spring rates combine reciprocally:
$K_{H 3}=\left[\frac{1}{2.620 \times 10^{4}}+\frac{1}{2.997 \times 10^{6}}\right]^{-1}=2.5973 \times 10^{4} \mathrm{~N} . \mathrm{m}^{-1}$

## C. 6 Mechanical Vibration Analysis

Table C.6.1: Physical Parameters used in Vibration Analysis - Vertical Direction

| $\mathbf{F}_{\mathbf{0}}$ | $\mathbf{K}_{\mathrm{V}}\left(\mathbf{N} \cdot \mathrm{m}^{-1}\right)$ | $\mathrm{m}(\mathrm{kg})$ | $\mathbf{C}\left(\mathbf{N} \cdot \mathbf{S} \cdot \mathrm{m}^{-1}\right)$ | $\boldsymbol{x}_{\boldsymbol{o}}(\mathbf{m})$ | $\dot{x}_{o}\left(\mathrm{~m} \cdot \mathrm{~s}^{-1}\right)$ | $f(\mathrm{~Hz})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 50 N | $8.683 \times 10^{5}$ | 2.1 | 5 | $-2.373 \times 10^{-5}$ | 0 | 20 |

Table C.6.2: Physical Parameters used in Vibration Analysis - Horizontal Direction

| $\mathbf{F}_{\mathbf{o}}$ | $\mathbf{K}_{\mathrm{H}}\left(\mathbf{N} . \mathrm{m}^{-1}\right)$ | $\mathbf{m}(\mathrm{kg})$ | $\mathbf{C}\left(\mathbf{N} . S . \mathrm{m}^{-1}\right)$ | $x_{o}(\mathbf{m})$ | $\dot{x}_{o}\left(\mathrm{~m}_{\mathrm{o}}{ }^{-1}\right)$ | $f(\mathrm{~Hz})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 50 N | $2.552 \times 10^{4}$ | 2.1 | 5 | 0 | 0 | 20 |

The total response $\mathrm{x}(\mathrm{t})$ for a damped system under a harmonic force is calculated by equation C.6.1:

$$
\begin{equation*}
x(t)=X_{0} e^{-\zeta \omega_{n} t} \cos \left(\omega_{d} t-\phi_{0}\right)+X \cos (\omega t-\phi) \tag{C.6.1}
\end{equation*}
$$

For the initial conditions of the system:

$$
\begin{gather*}
x_{o}=X_{0} \cos \left(\phi_{0}\right)+X \cos (\phi)  \tag{C.6.2}\\
\dot{x}_{0}=-\zeta \omega_{n} X_{0} \cos \left(\phi_{0}\right)+\omega_{d} X_{0} \sin \left(\phi_{0}\right)+\omega X \sin (\phi) \tag{C.6.3}
\end{gather*}
$$

Refer to Section 5.12 for additional equations. Note that the stiffness"s presented in Tables C.6.12 correspond to the column slide being in a position of 600 mm above its base.

## Vertical Harmonic Force

Initial displacement based purely on weight of drill head:
$x_{o}=-\frac{\text { Weight }}{k}=\frac{2.1 \times 9.81}{8.683 \times 10^{5}}=-2.373 \times 10^{-5} \mathrm{~m}$
$\omega_{n}=\sqrt{\frac{k}{m}}=\sqrt{\frac{8.683 \times 10^{5}}{2.1}}=643.02 \mathrm{rad} . \mathrm{s}^{-1}$
$\delta_{s t}=\frac{F_{o}}{k}=\frac{50}{8.683 \times 10^{5}}=5.758 \times 10^{-5} \mathrm{~m}$
$\zeta=\frac{C}{2 \sqrt{k m}}=\frac{5}{2 \sqrt{8.683 \times 10^{5} \times 2.1}}=0.0019$
$\omega_{d}=\sqrt{1-\zeta^{2}} \omega_{n}=\sqrt{1-0.0019^{2}} \times 643.02=643.02 \mathrm{rad} . \mathrm{s}^{-1}$
$\omega=2 \pi f=2 \pi \times 20=125.66 \mathrm{rad} . \mathrm{s}^{-1}$
$r=\frac{\omega}{\omega_{n}}=\frac{125.66}{643.02}=0.1954$
$X=\frac{\delta_{s t}}{\sqrt{\left(1-r^{2}\right)^{2}+(2 \zeta r)^{2}}}=\frac{5.758 \times 10^{-5}}{\sqrt{\left(1-0.1954^{2}\right)^{2}+(2 \times 0.0019 \times 0.1954)^{2}}}=5.987 \times 10^{-5} \mathrm{~m}$
$\phi=\tan ^{-1}\left(\frac{2 \zeta r}{1-r^{2}}\right)=\tan ^{-1}\left(\frac{2 \times 0.0019 \times 0.1954}{1-0.1954^{2}}\right)=0.0442^{\circ}$

Using the initial conditions with equation C.6.2
$x_{o}=X_{0} \cos \left(\phi_{0}\right)+X \cos (\phi)=-2.373 \times 10^{-5} \mathrm{~m}$
$x_{o}=X_{0} \cos \left(\phi_{0}\right)+5.987 \times 10^{-5} \cos (0.0442)=-2.373 \times 10^{-5} \mathrm{~m}$
$X_{0} \cos \left(\phi_{0}\right)=-8.360 \times 10^{-5}$

Using the initial conditions with equation C.6.3
$\dot{x}_{0}=-\zeta \omega_{n} X_{0} \cos \left(\phi_{0}\right)+\omega_{d} X_{0} \sin \left(\phi_{0}\right)+\omega X \sin (\phi)=0$
$-0.0019 \times 643.02 \times-8.360 \times 10^{-5}+643.02 \times X_{0} \sin \left(\phi_{0}\right)+125.66 \times 5.987$
$\times 10^{-5} \sin (0.0442)=0$
$X_{0} \sin \left(\phi_{0}\right)=-1.679 \times 10^{-7}$
$X_{0}=\left[\left(X_{0} \sin \left(\phi_{0}\right)\right)^{2}+\left(X_{0} \cos \left(\phi_{0}\right)\right)^{2}\right]^{0.5}=\left[\left(-1.679 \times 10^{-7}\right)^{2}+\left(-8.360 \times 10^{-5}\right)^{2}\right]^{0.5}$
$X_{0}=8.360 \times 10^{-5} \mathrm{~m}$
$\tan \phi_{0}=\frac{X_{0} \sin \left(\phi_{0}\right)}{X_{0} \cos \left(\phi_{0}\right)}=\frac{=-1.679 \times 10^{-7}}{-8.360 \times 10^{-5}}=2.008 \times 10^{-3}$
$\phi_{0}=0.1151^{\circ}$

## Horizontal Harmonic Force

$$
\begin{aligned}
& \omega_{n}=\sqrt{\frac{k}{m}}=\sqrt{\frac{2.552 \times 10^{4}}{2.1}}=110.24 \mathrm{rad} . \mathrm{s}^{-1} \\
& \delta_{s t}=\frac{F_{o}}{k}=\frac{50}{2.552 \times 10^{4}}=1.959 \times 10^{-3} \mathrm{~m}
\end{aligned}
$$

$\zeta=\frac{C}{2 \sqrt{k m}}=\frac{5}{2 \sqrt{2.552 \times 10^{4} \times 2.1}}=0.0108$
$\omega_{d}=\sqrt{1-\zeta^{2}} \omega_{n}=\sqrt{1-0.0108^{2}} \times 110.24=110.23 \mathrm{rad} . \mathrm{s}^{-1}$
$\omega=2 \pi f=2 \pi \times 20=125.66 \mathrm{rad} . \mathrm{s}^{-1}$
$r=\frac{\omega}{\omega_{n}}=\frac{125.66}{110.14}=1.1409$
$X=\frac{\delta_{s t}}{\sqrt{\left(1-r^{2}\right)^{2}+(2 \zeta r)^{2}}}=\frac{1.959 \times 10^{-3}}{\sqrt{\left(1-1.1409^{2}\right)^{2}+(2 \times 0.0108 \times 1.1409)^{2}}}=6.473 \times 10^{-3} \mathrm{~m}$
$\phi=\tan ^{-1}\left(\frac{2 \zeta r}{1-r^{2}}\right)=\tan ^{-1}\left(\frac{2 \times 0.0108 \times 1.1409}{1-1.1409^{2}}\right)=-4.670^{\circ}$

The phase angle is in the second quadrant:
$\phi=175.33^{\circ}$

Using the initial conditions with equation C.6.2
$x_{o}=X_{0} \cos \left(\phi_{0}\right)+X \cos (\phi)=0 \mathrm{~m}$
$x_{o}=X_{0} \cos \left(\phi_{0}\right)+6.473 \times 10^{-3} \cos (175.33)=0 \mathrm{~m}$
$X_{0} \cos \left(\phi_{0}\right)=6.452 \times 10^{-3}$

Using the initial conditions with equation C.6.3
$\dot{x}_{0}=-\zeta \omega_{n} X_{0} \cos \left(\phi_{0}\right)+\omega_{d} X_{0} \sin \left(\phi_{0}\right)+\omega X \sin (\phi)=0$
$-0.0108 \times 110.24 \times 6.452 \times 10^{-3}+110.23 X_{0} \sin \left(\phi_{0}\right)+125.66 \times 6.473$

$$
\times 10^{-3} \sin (175.33)=0
$$

$X_{0} \sin \left(\phi_{0}\right)=-5.311 \times 10^{-4}$
$X_{0}=\left[\left(X_{0} \sin \left(\phi_{0}\right)\right)^{2}+\left(X_{0} \cos \left(\phi_{0}\right)\right)^{2}\right]^{0.5}=\left[\left(-5.311 \times 10^{-4}\right)^{2}+\left(6.452 \times 10^{-3}\right)^{2}\right]^{0.5}$
$X_{0}=6.474 \times 10^{-3} \mathrm{~m}$
$\tan \phi_{0}=\frac{X_{0} \sin \left(\phi_{0}\right)}{X_{0} \cos \left(\phi_{0}\right)}=\frac{-5.311 \times 10^{-4}}{6.452 \times 10^{-3}}=-8.232 \times 10^{-2}$
$\phi_{0}=-4.7060^{\circ}$
The phase angle is in the second quadrant:
$\phi_{0}=175.29^{\circ}$

## Appendix D

## D. 1 Three Axis Drilling Configuration

## Axes - X, Y and Z



Figure D.1: Three Axis Drilling Machine (X, Y and Z)

Table D.1: Bill of Modules for Three Axis Drilling Machine (X, Y, and Z)

| Bill of Modules | Module | Module Code <br> (MRM-Type-Range-Moving Interface-Static Interface) |
| :--- | :--- | :--- |
| Motion Modules | Base | MRM-B01-500-T1-T4/5 |
|  | Work Table Slide | MRM -WTS01-300-T3-T5 |
|  | Column | MRM-C01-562-T2A/2B-T1 |
| Process Module | Drilling Head | MRM-DH01-12-T0-T2A |
| Accessory Modules | Work Table | MRM-WT01-160-T0-T3 |
|  | Range Ext Arm | MRM-REA-370-T0-T2A |

$$
\underset{\text { Drill }}{\text { Worktable }} T=\left[\begin{array}{cccc}
1 & 0 & 0 & -344.5+x \\
0 & 1 & 0 & 2.5+y \\
0 & 0 & 1 & -2+z \\
0 & 0 & 0 & 1
\end{array}\right]
$$

## D. 2 Four Axis Drilling Configurations

## Axes - X, Y, Z and A



Figure D.2: Four Axis Drilling Machine (X, Y, Z and A)

Table D.2: Bill of Modules for Four Axis Drilling Machine (X, Y, Z and A)

| Bill of Modules | Module | Module Code <br> (MRM-Type-Range-Moving Interface-Static Interface) |
| :--- | :--- | :--- |
| Motion Modules | Base | MRM-B01-500-T1-T4/5 |
|  | Work Table Slide | MRM -WTS01-300-T3-T5 |
|  | Column | MRM-C01-562-T2A/2B-T1 |
|  | Cutting Head Rot | MRM-CHR01-360-T2A-T2B |
| Process Module | Drilling Head | MRM-DH01-12-T0-T2A |
| Accessory Modules | Work Table | MRM-WT01-160-T0-T3 |
|  | Range Ext Arm | MRM-REA-370-T0-T2A |

$$
\underset{\text { Drill }}{\text { Worktable }} T=\left[\begin{array}{cccc}
1 & 0 & 0 & -482.5+x \\
0 & c \gamma & -s \gamma & 2.5+81.5 s \gamma+y \\
0 & s \gamma & c \gamma & 79.5-81.5 c \gamma+z \\
0 & 0 & 0 & 1
\end{array}\right]
$$

## Axes - X, Y, Z and B



Figure D.3: Four Axis Drilling Machine (X, Y, Z and B)

Table D.3: Bill of Modules for Four Axis Drilling Machine (X, Y, Z and B)

| Bill of Modules | Module | Module Code <br> (MRM-Type-Range-Moving Interface-Static Interface) |
| :--- | :--- | :--- |
| Motion Modules | Base | MRM-B01-500-T1-T4/5 |
|  | Work Table Slide | MRM -WTS01-300-T3-T5 |
|  | Column | MRM-C01-562-T2A/2B-T1 |
|  | Tilt Table | MRM-TT01-90-T3-T3 |
| Process Module | Drilling Head | MRM-DH01-12-T0-T2A |
| Accessory Modules | Work Table | MRM-WT01-160-T0-T3 |
|  | Range Ext Arm | MRM-REA-370-T0-T2A |

$\underset{\text { Drill }}{\text { Worktable }} T=\left[\begin{array}{cccc}c \beta & 0 & s \beta & -344.5 c \beta-27.5 s \beta+z s \beta+x c \beta \\ 0 & 1 & 0 & 2.5+y \\ -s \beta & 0 & c \beta & 344.5 s \beta-119.5-27.5 c \beta+z c \beta-x s \beta \\ 0 & 0 & 0 & 1\end{array}\right]$

## Axes - $\mathrm{X}, \mathrm{Y}, \mathrm{Z}$ and C



Figure D.4: Four Axis Drilling Machine (X, Y, Z and C)

Table D.4: Bill of Modules for Four Axis Drilling Machine (X, Y, Z and C)

| Bill of Modules | Module | Module Code <br> (MRM-Type-Range-Moving Interface-Static Interface) |
| :--- | :--- | :--- |
| Motion Modules | Base | MRM-B01-500-T1-T4/5 |
|  | Work Table Slide | MRM -WTS01-300-T3-T5 |
|  | Column | MRM-C01-562-T2A/2B-T1 |
|  | Rotary Table | MRM-RT01-360-T3-T3 |
| Process Module | Drilling Head | MRM-DH01-12-T0-T2A |
| Accessory Modules | Work Table | MRM-WT01-160-T0-T3 |
|  | Range Ext Arm | MRM-REA-370-T0-T2A |

Worktable $T=\left[\begin{array}{cccc}c \alpha & -s \alpha & 0 & -344.5 c \alpha+x c \alpha-2.5 s \alpha-y s \alpha \\ s \alpha & c \alpha & 0 & -344.5 s \alpha+x s \alpha+2.5 c \alpha+y c \alpha \\ 0 & 0 & 1 & -154+z \\ 0 & 0 & 0 & 1\end{array}\right]$

## D. 3 Five Axis Drilling Configurations

Axes - X, Y, Z, A and B



Figure D.5: Five Axis Drilling Machine (X, Y, Z, A and B)

Table D.5: Bill of Modules for Five Axis Drilling Machine (X, Y, Z, A and B)

| Bill of Modules | Module | Module Code <br> (MRM-Type-Range-Moving Interface-Static Interface) |
| :--- | :--- | :--- |
| Motion Modules | Base | MRM-B01-500-T1-T4/5 |
|  | Work Table Slide | MRM -WTS01-300-T3-T5 |
|  | Column | MRM-C01-562-T2A/2B-T1 |
|  | Cutting Head Rot | MRM-CHR01-360-T2A-T2B |
|  | Tilt Table | MRM-TT01-90-T3-T3 |
| Process Module | Drilling Head | MRM-DH01-12-T0-T2A |
| Accessory Modules | Work Table | MRM-WT01-160-T0-T3 |
|  | Range Ext Arm | MRM-REA-370-T0-T2A |

$$
\underset{\text { Worktable }}{\text { Drill }} T=\left[\begin{array}{cccc}
c \beta & s \beta c \gamma & s \beta c \gamma & -482.5 c \beta-81.5 s \beta c \gamma+z s \beta+x c \beta+54 s \beta \beta \\
0 & c \gamma & -s \gamma & 2.5+81.5 s \gamma+y \\
-s \beta & c \beta s \gamma & c \beta c \gamma & 482.5 s \beta-119.5-81.5 c \beta c \gamma+z c \beta-x s \beta+54 c \beta \\
0 & 0 & 0 & 1
\end{array}\right]
$$

## Axes - X, Y, Z, A and C



Figure D.6: Five Axis Drilling Machine (X, Y, Z, A and C)

Table D.6: Bill of Modules for Five Axis Drilling Machine (X, Y, Z, A and C)

| Bill of Modules | Module | Module Code <br> (MRM-Type-Range-Moving Interface-Static Interface) |
| :--- | :--- | :--- |
| Motion Modules | Base | MRM-B01-500-T1-T4/5 |
|  | Work Table Slide | MRM -WTS01-300-T3-T5 |
|  | Column | MRM-C01-562-T2A/2B-T1 |
|  | Cutting Head Rot | MRM-CHR01-360-T2A-T2B |
|  | Rotary Table | MRM-RT01-360-T3-T3 |
| Process Module | Drilling Head | MRM-DH01-12-T0-T2A |
| Accessory Modules | Work Table | MRM-WT01-160-T0-T3 |
|  | Range Ext Arm | MRM-REA-370-T0-T2A |

$\underset{\text { Wrill }}{\text { Worktable }} T=\left[\begin{array}{cccc}c \alpha & -s \alpha c \gamma & s \alpha s \gamma & -482.5 c \alpha-81.5 s \alpha s \gamma+x c \alpha-2.5 s \alpha-y s \alpha \\ s \alpha & c \alpha c \gamma & -c \alpha s \gamma & -482.5 s \alpha+81.5 c \alpha s \gamma+x s \alpha+2.5 c \alpha+y c \alpha \\ 0 & s \gamma & c \gamma & -72.5-81.5 c \gamma+z \\ 0 & 0 & 0 & 1\end{array}\right]$

## Axes - X, Y, Z, B and C



Figure D.7: Five Axis Drilling Machine (X, Y, Z, B and C)

Table D.7: Bill of Modules for Five Axis Drilling Machine (X, Y, Z, B and C)

| Bill of Modules | Module | Module Code <br> (MRM-Type-Range-Moving Interface-Static Interface) |
| :--- | :--- | :--- |
| Motion Modules | Base | MRM-B01-500-T1-T4/5 |
|  | Work Table Slide | MRM -WTS01-300-T3-T5 |
|  | Column | MRM-C01-562-T2A/2B-T1 |
|  | Tilt Table | MRM-TT01-90-T3-T3 |
|  | Rotary Table | MRM-RT01-360-T3-T3 |
| Process Module | Drilling Head | MRM-DH01-12-T0-T2A |
| Accessory Modules | Work Table | MRM-WT01-160-T0-T3 |
|  | Range Ext Arm | MRM-REA-370-T0-T2A |

$$
\begin{aligned}
& \text { Worktable } \\
& \text { Drill } T= \\
& {\left[\begin{array}{cccc}
c \beta c \alpha & -c \beta s \alpha & s \beta & -344.5 c \beta c \alpha-179.5 s \beta+s \beta Z+x c \beta c \alpha-2.5 c \beta s \alpha-y c \beta s \alpha \\
s \alpha & c \alpha & 0 & -344.5 s \alpha+x s \alpha+2.5 c \alpha+y c \alpha \\
-s \beta c \alpha & s \beta s \alpha & c \beta & 344.5 s \beta c \alpha-119.5-179.5 c \beta+z c \beta-x s \beta c \alpha+2.5 s \beta s \alpha+y s \beta s \alpha \\
0 & 0 & 0 & 1
\end{array}\right]}
\end{aligned}
$$

## D. 4 Six Axis Drilling Configuration



Figure D.8: Six Axis Drilling Machine (X, Y, Z, A, B and C)

Table D.8: Bill of Modules for Six Axis Drilling Machine (X, Y, Z, A, B and C)

| Bill of Modules | Module | Module Code <br> (MRM-Type-Range-Moving Interface-Static Interface) |
| :--- | :--- | :--- |
| Motion Modules | Base | MRM-B01-500-T1-T4/5 |
|  | Work Table Slide | MRM -WTS01-300-T3-T5 |
|  | Column | MRM-C01-562-T2A/2B-T1 |
|  | Cutting Head Rot | MRM-CHR01-360-T2A-T2B |
|  | Tilt Table | MRM-TT01-90-T3-T3 |
|  | Rotary Table | MRM-RT01-360-T3-T3 |
|  | Process Module | Drilling Head |
| Accessory Modules | Work Table | MRM-DH01-12-T0-T2A |
|  | Range Ext Arm | MRM-REA-160-T0-T3 |

$$
\underset{\text { Worktable }}{\text { Drill }} T=\left[\begin{array}{cccc}
c \beta c \alpha & -c \beta s \alpha c \gamma+s \beta s \gamma & c \beta s \alpha s \gamma+s \beta c \gamma & K_{1} \\
s \alpha & c \alpha c \gamma & -c \alpha s \gamma & K_{2} \\
-s \beta c \alpha & s \beta s \alpha c \gamma+c \alpha s \gamma & -s \beta s \alpha s \gamma+c \beta c \gamma & K_{3} \\
0 & 0 & 0 & 1
\end{array}\right]
$$

$K_{1}=-482.5 c \beta c \alpha-81.5 c \beta s \alpha s \gamma-81.5 s \beta c \gamma+z s \beta+x c \beta c \alpha-2.5 c \beta s \alpha-98 s \beta-y c \beta s \alpha$
$K_{2}=-965 / 2 * s \alpha+163 / 2 * c \alpha s \gamma+x s \alpha+2.5 c \alpha+y c \alpha$
$K_{1}=482.5 s \beta c \alpha-119.5+81.5 s \beta s \alpha s \gamma-81.5 c \beta c \gamma+z c \beta-x s \beta c \alpha+2.5 s \beta s \alpha-98 c \beta+$ $y_{s} \beta s \alpha$

## D. 5 Turning Configuration

Axes - X, Y and C



Figure D.9: Three Axis Lathe (X, Y and C)

Table D.9: Bill of Modules for Three Axis Lathe (X, Y and C)

| Bill of Modules | Module | Module Code <br> (MRM-Type-Range-Moving Interface-Static <br> Interface) |
| :--- | :--- | :--- |
| Motion Modules | Base | MRM-B01-500-T1-T4/5 |

$$
\underset{\text { Tool Post }}{\text { Chuck }} T=\left[\begin{array}{cccc}
c \alpha & -s \alpha & 0 & x-192.5 \\
s \alpha & c \alpha & 0 & 2.5+y+v \\
0 & 0 & 1 & 0.5 \\
0 & 0 & 0 & 1
\end{array}\right]
$$

## Appendix E

## E. 1 Pin Configurations of Microcontrollers and IC's



Figure E.1.1: Pin Out of the ATmega 32L Microcontroller [38]

|  | $\checkmark$ |  |
| :---: | :---: | :---: |
| (RESET) PC6 1 | 28 | PPC5 (ADC5/SCL) |
| (RXD) PDO ${ }^{2}$ | 27 | PPC4 (ADC4/SDA) |
| (TXD) $\mathrm{PD1} \mathrm{l}^{3}$ | 26 | PPC3 (ADC3) |
| (INT0) PD2 ${ }^{4}$ | 25 | PPC2 (ADC2) |
| (INT1) PD3 ${ }^{5}$ | 24 | PPC1 (ADC1) |
| (XCKTT0) PD4 ${ }^{6}$ | 23 | PPCO (ADCO) |
| vcc- ${ }^{7}$ | 22 | IGND |
| GND-8 | 21 | AREF |
| (XTAL1/TOSC1) PB6 ${ }^{\text {a }} 9$ | 20 | avcc |
| (XTAL2TOSC2) PB7 10 | 19 | PB5 (SCK) |
| (T1) PD5-11 | 18 | Pr84 (MISO) |
| (AIN0) PD6 - 12 | 17 | PB3 (MOSI/OC2) |
| (AIN1) PD7 ${ }^{13}$ | 16 | PR2 (SS/OC13) |
| (ICP1) PB0 14 | 15 | PPB1 (OC1A) |

Figure E.1.2: Pin Out of the ATmega 8L Microcontroller [39]


Figure E.1.3: Pin Out of the FT232RL USB USART IC [66]

## E. 2 Layouts of Component Boards



Figure E.2.1: Layout of the H-Bridge Motor Driver Used in Servo Control Modules

Table E.2.1: Configuration of Terminals on H-Bridge Motor Driver

| Terminal | Function <br> 1 |
| :---: | :--- |
| 2 | PWM terminal, connected to microcontroller |
| $3 \& 4$ | Direction terminal, connected to microcontroller |
| $5 \& 6$ | 12 DC input, negative terminal |
| $7 \& 8$ | Output to motor, positive terminal |
| $9 \& 10$ | Output to motor, negative terminal |



Figure E.2.2: Layout of the ATmega 32L Microcontroller Board Used in Servo and Spindle Control Modules

Table E.2.2: Configuration of Terminals on the ATmega 32L Board Used in Servo and Spindle Control Modules

| Terminal | Function |  |
| :---: | :--- | :--- |
|  | Spindle Control | Servo Control |
| 1 | Unused | PWM output |
| 2 | Unused | PWM output (spare) |
| 3 | Unused | Limit switch interrupt terminal |
| 4 | Unused | Limit switch interrupt terminal |
| 5 | USART transmit | USART transmit |
| 6 | USART receive | USART receive |
| 7 | Ground | Ground |
| 8 | Vcc | Vcc |

Table E. 2.2 (Continued): Configuration of Terminals on the ATmega 32L...

| Terminal | Function |  |
| :---: | :--- | :--- |
|  | Spindle Control | Servo Control |
| $9-18$ | Unused | Unused |
| $19-26$ | ADC channels | ADC channels (optional use) |
| 27 | Ground | Ground |
| 28 | AVcc | AVcc |
| $29-32$ | Unused | Unused |
| $33-34$ | I/O terminals for relay switching | Unused |
| 35 | Unused | I2C data terminal |
| 36 | Unused | I2C clock terminal |
| $37-40$ | Unused | Unused |



Figure E.2.3: Layout of the ATmega 8L Microcontroller Board Used in Servo Control Modules

Table E.2.3: Configuration of Terminals on the ATmega 8L Board Used in Servo Control Modules

| Terminal | Function |
| :---: | :--- |
| $1-4$ | Unused |
| 5 | Vcc |
| 6 | Ground |
| 7 | Unused |
| $8-9$ | Encoder interrupt terminals |
| 10 | USART transmit |
| 11 | USART receive |
| 12 | Unused |
| $13-21$ | ADC channels (optional) |

Table E. 2.3 (Continued): Configuration of Terminals on the ATmega 8L Board...

| Terminal | Function |
| :---: | :--- |
| 22 | Ground |
| $23-34$ | Unused |



Figure E.2.4: Layout of the ATmega 32L + USB Microcontroller Board Used in Servo Communication Modules

Table E.2.4: Configuration of Terminals on the ATmega 32L + USB Microcontroller Board

| Terminal | Function |
| :---: | :--- |
| 1 | Ground |
| 2 | Vcc |
| $3-19$ | Unused |
| 20 | Ground |
| $21-27$ | Unused |
| 28 | I2C data terminal |
| 29 | I2C clock terminal |
| $30-37$ | Unused |



Figure E.2.5: Layout of the DC Relay Switch used in Spindle Control Modules

Table E.2.5: Configuration of Terminals on the DC Relay Switch used in Spindle Control Modules


Figure E.2.6: Layout of the AC Relay Switch used in the AC Power Box

Table E.2.6: Configuration of Terminals on the AC Relay Switch used in the AC Power Box

| Terminal | Function |
| :---: | :--- |
| 1 | AC line in |
| 2 | AC line out |
| 3 | Actuation Terminal |
| 4 | Ground |

## E. 3 General Feedback Byte

Table E.3.1: Hexadecimal Values of the General Feedback Bytes

| Spindle Control Modules |  |
| :---: | :---: |
| Instruction | General Feedback Byte Value (HDX) |
| Successful Execution of Instruction | $0 \times 01$ |
| Instruction Incomplete | $0 \times 02$ |
| Instruction | Servo Control Modules |
| General Feedback Byte Value (HIDX) |  |
| Successful Execution of Instruction | $0 \times 01$ |
| Collision at Lower Limit | $0 \times 02$ |
| Collision at Upper Limit | $0 \times 03$ |
| No Actuation | $0 \times 04$ |

## Appendix F

## F. 1 Interpolation: Linear Axes

## Base Module (- X Direction)

Linear interpolation performed for a distance of 100 mm at a feed rate of $100 \mathrm{~mm} / \mathrm{min}$.


Figure F.1.1: Graph of Measured Position vs Time: Base Module (-X Direction)


Figure F.1.2: Graph of Measured Speed vs Time: Base Module (-X Direction)


Figure F.1.3: Graph of Position Error vs Time: Base Module (-X Direction)

## Work Table Slide Module (+ Y Direction)

Linear interpolation performed for a distance of 100 mm at a feed rate of $100 \mathrm{~mm} / \mathrm{min}$.


Figure F.1.4: Graph of Measured Position vs Time: Work Table Slide Module (+Y Direction)


Figure F.1.5: Graph of Measured Speed vs Time: Work Table Slide Module (+Y Direction)


Figure F.1.6: Graph of Position Error vs Time: Work Table Slide Module (+Y Direction)

## Work Table Slide Module (- Y Direction)

Linear interpolation performed for a distance of 100 mm at a feed rate of $100 \mathrm{~mm} / \mathrm{min}$.


Figure F.1.7: Graph of Measured Position vs Time: Work Table Slide Module (-Y Direction)


Figure F.1.8: Graph of Measured Speed vs Time: Work Table Slide Module (-Y Direction)


Figure F.1.9: Graph of Position Error vs Time: Work Table Slide Module (-Y Direction)

## Column Module (+Z Direction)

Linear interpolation performed for a distance of 100 mm at a feed rate of $100 \mathrm{~mm} / \mathrm{min}$.


Figure F.1.10: Graph of Measured Position vs Time: Column Module (+Z Direction)


Figure F.1.11: Graph of Measured Speed vs Time: Column Module (+Z Direction)


Figure F.1.12: Graph of Position Error vs Time: Column Module (+Z Direction)

## Column Module (-Z Direction)

Linear interpolation performed for a distance of 100 mm at a feed rate of $100 \mathrm{~mm} / \mathrm{min}$.


Figure F.1.13: Graph of Measured Position vs Time: Column Module (-Z Direction)


Figure F.1.14: Graph of Measured Speed vs Time: Column Module (-Z Direction)


Figure F.1.15: Graph of Position Error vs Time: Column Module (-Z Direction)

## Cross Slide Module (+Y Direction)

Linear interpolation performed for a distance of 50 mm at a feed rate of $100 \mathrm{~mm} / \mathrm{min}$.


Figure F.1.16: Graph of Measured Position vs Time: Cross Slide Module (+Y Direction)


Figure F.1.17: Graph of Measured Speed vs Time: Cross Slide Module (+Y Direction)


Figure F.1.18: Graph of Position Error vs Time: Cross Slide Module (+Y Direction)

## Cross Slide Module (-Y Direction)

Linear interpolation performed for a distance of 50 mm at a feed rate of $100 \mathrm{~mm} / \mathrm{min}$.


Figure F.1.19: Graph of Measured Position vs Time: Cross Slide Module (-Y Direction)


Figure F.1.20: Graph of Measured Speed vs Time: Cross Slide Module (-Y Direction)


Figure F.1.21: Graph of Position Error vs Time: Cross Slide Module (-Y Direction)

## F. 2 Interpolation: Rotary Axes

## Cutting Head Rotary Module (+ A/ $\gamma$ Direction)

Interpolation performed for an angle of $360^{\circ}$ at a speed of $10 \mathrm{rev} / \mathrm{min}$.


Figure F.2.1: Graph of Angular Position vs Time: Cutting Head Rotary Module ( $+\mathbf{A} / \gamma$ Direction)


Figure F.2.2: Graph of Measured Speed vs Time: Cutting Head Rotary Module ( $+\mathbf{A} / \gamma$ Direction)


Figure F.2.3: Graph of Angular Position Error vs Time: Cutting Head Rotary Module ( $+\mathbf{A} / \gamma$ Direction)

## Cutting Head Rotary Module (- A/ $\gamma$ Direction)

Interpolation performed for an angle of $360^{\circ}$ at a speed of $10 \mathrm{rev} / \mathrm{min}$.


Figure F.2.4: Graph of Angular Position vs Time: Cutting Head Rotary Module (-A/ $\gamma$ Direction)


Figure F.2.5: Graph of Measured Speed vs Time: Cutting Head Rotary Module (-A/ $\gamma$ Direction)


Figure F.2.6: Graph of Angular Position Error vs Time: Cutting Head Rotary Module (-A/ $\gamma$ Direction)

## Tilt Table Module ( $+\mathrm{B} / \boldsymbol{\beta}$ Direction)

Interpolation performed for an angle of $90^{\circ}$ at a speed of $15 \mathrm{rev} / \mathrm{min}$.


Figure F.2.7: Graph of Angular Position vs Time: Tilt Table Module (+B/ $\boldsymbol{\beta}$ Direction)


Figure F.2.8: Graph of Measured Speed vs Time: Tilt Table Module (+B/ $\boldsymbol{\beta}$ Direction)


Figure F.2.9: Graph of Angular Position Error vs Time: Tilt Table Module (+B/ $\boldsymbol{\beta}$ Direction)

## Tilt Table Module (-B/ $\beta$ Direction)

Interpolation performed for an angle of $90^{\circ}$ at a speed of $15 \mathrm{rev} / \mathrm{min}$


Figure F.2.10: Graph of Angular Position vs Time: Tilt Table Module (-B/ $\boldsymbol{\beta}$ Direction)


Figure F.2.11: Graph of Measured Speed vs Time: Tilt Table Module (-B/ $\boldsymbol{\beta}$ Direction)


Figure F.2.12: Graph of Angular Position Error vs Time: Tilt Table Module (-B/ß Direction)

## Rotary Table Module (- C/ $\alpha$ Direction)

Interpolation performed for an angle of $360^{\circ}$ at a speed of $15 \mathrm{rev} / \mathrm{min}$.


Figure F.2.13: Graph of Angular Position vs Time: Rotary Table Module (-C/ $\alpha$ Direction)


Figure F.2.14: Graph of Measured Speed vs Time: Rotary Table Module (-C/ $\alpha$ Direction)


Figure F.2.15: Graph of Angular Position Error vs Time: Rotary Table Module (-C/ $\alpha$ Direction)

## F. 3 Point to Point Motion Control

Table F.3.1: Test Results, Point to Point Motion Control of Linear Axes

|  | Base Module | Work Table <br> Slide Module | Column Module | Cross Slide <br> Module |
| :---: | :---: | :---: | :---: | :---: |
| Target <br> Distance $(\mathrm{mm})$ | Overshoot <br> $(\mathrm{mm})$ | Overshoot <br> $(\mathrm{mm})$ | Overshoot <br> $(\mathrm{mm})$ | Overshoot <br> $(\mathrm{mm})$ |
| $\mathbf{2 5}$ | 0.029 | 0.001 | 0.001 | 0.000 |
| $\mathbf{- 2 5}$ | 0.020 | 0.001 | 0.007 | 0.004 |
| $\mathbf{5 0}$ | 0.000 | 0.026 | 0.026 | 0.000 |
| $\mathbf{- 5 0}$ | 0.034 | 0.015 | 0.059 | 0.000 |
| $\mathbf{7 5}$ | - | - | - | 0.000 |
| $\mathbf{- 7 5}$ | - | - | - | 0.004 |
| $\mathbf{1 0 0}$ | 0.010 | 0.023 | 0.000 | - |
| $\mathbf{- 1 0 0}$ | 0.015 | 0.018 | 0.018 | - |
| Average | $\mathbf{0 . 0 1 8}$ | $\mathbf{0 . 0 1 4}$ | $\mathbf{0 . 0 1 9}$ | $\mathbf{0 . 0 0 1}$ |
| Maximum | $\mathbf{0 . 0 3 4}$ | $\mathbf{0 . 0 2 6}$ | $\mathbf{0 . 0 5 9}$ | $\mathbf{0 . 0 0 4}$ |

Table F.3.2: Test Results, Point to Point Motion Control of Rotary Axes

| Target Angle <br> $($ Deg $)$ | Cutting Head Rotary <br> Module <br> Overshoot <br> $($ Deg) | Tilt Table Module | Rotary Table Module |
| :---: | :---: | :---: | :---: |
| $\mathbf{4 5}$ | 0.000 | Overshoot <br> $($ Deg $)$ | Overshoot <br> (Deg) |
| $\mathbf{- 4 5}$ | 0.703 | 0.000 | 0.013 |
| $\mathbf{9 0}$ | 0.000 | 0.000 | 0.025 |
| $\mathbf{- 9 0}$ | 0.000 | 0.703 | 0.113 |
| $\mathbf{1 8 0}$ | 0.703 | 0.703 | 0.100 |
| $\mathbf{- 1 8 0}$ | 0.000 | - | 0.113 |
| $\mathbf{3 6 0}$ | 0.703 | - | 0.088 |
| $\mathbf{- 3 6 0}$ | 1.406 | - | 0.100 |
| Average | $\mathbf{0 . 4 3 9}$ | - | 0.138 |
| Maximum | $\mathbf{1 . 4 0 6}$ | $\mathbf{0 . 3 5 2}$ | $\mathbf{0 . 0 8 6}$ |

## F. 4 Accuracy and Repeatability Test Data

Table F.4.1: Control Accuracy and Repeatability, Test Data for Linear Modules

|  | Base Module |  | Work Table <br> Slide Module |  | Column Module |  | Cross Slide <br> Module |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Conditions | $\mathbf{X}+$ | $\mathbf{X}-$ | $\mathbf{Y}+$ | $\mathbf{Y}-$ | $\mathbf{Z}+$ | $\mathbf{Z}-$ | $\mathbf{Y}+$ | $\mathbf{Y}-$ |
| Target (mm) | 100 | -100 | 100 | -100 | 100 | -100 | 50 | -50 |
| Speed (mm/s) | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 |
| Test No | Error (mm) |  | Error (mm) |  | Error (mm) |  | Error (mm) |  |
| Test 1 | 0.015 | 0.000 | 0.012 | 0.012 | 0.018 | 0.012 | 0.008 | 0.000 |
| Test 2 | 0.015 | 0.005 | 0.012 | 0.018 | 0.012 | 0.012 | 0.012 | 0.004 |
| Test 3 | 0.015 | 0.010 | 0.018 | 0.023 | 0.012 | 0.006 | 0.008 | 0.008 |
| Test 4 | 0.010 | 0.005 | 0.018 | 0.006 | 0.018 | 0.006 | 0.004 | 0.008 |
| Test 5 | 0.020 | 0.010 | 0.023 | 0.012 | 0.029 | 0.023 | 0.008 | 0.008 |
| Test 6 | 0.020 | 0.015 | 0.018 | 0.012 | 0.029 | 0.006 | 0.012 | 0.012 |
| Statistics |  |  |  |  |  |  |  |  |
| Mean Error | 0.015 | 0.007 | 0.017 | 0.014 | 0.020 | 0.011 | 0.008 | 0.007 |
| Std Dev | 0.004 | 0.005 | 0.004 | 0.006 | 0.008 | 0.007 | 0.003 | 0.004 |
| Max Error | 0.020 | 0.015 | 0.023 | 0.023 | 0.029 | 0.023 | 0.012 | 0.012 |

Table F.4.2: Control Accuracy and Repeatability, Test Data for Rotary Modules

|  | Cutting Head Rotary <br> Module |  | Tilt Table Module |  | Rotary Table Module |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Conditions | A+ | A- | B+ | B- | C+ | C- |
| Target (Deg) | 360 | -360 | 90 | -90 | 360 | -360 |
| Speed (rev/min) | 40 | 40 | 30 | 30 | 0.75 | 0.75 |
| Test No | Error (Deg) |  | Error (Deg) |  | Error (Deg) |  |
| Test 1 | 0.000 | 1.406 | 0.000 | 0.000 | 0.063 | 0.038 |
| Test 2 | 0.703 | 0.703 | 1.406 | 0.703 | 0.100 | 0.038 |
| Test 3 | 1.406 | 2.109 | 0.703 | 0.000 | 0.151 | 0.038 |
| Test 4 | 0.703 | 0.703 | 1.406 | 0.703 | 0.075 | 0.000 |
| Test 5 | 0.703 | 0.000 | 0.703 | 1.406 | 0.088 | 0.113 |
| Test 6 | 1.406 | 1.406 | 1.406 | 0.000 | 0.075 | 0.050 |
| Statistics |  |  |  |  |  |  |
| Mean Error | 0.820 | 1.055 | 0.938 | 0.469 | 0.092 | 0.046 |
| Std Dev | 0.529 | 0.737 | 0.574 | 0.574 | 0.031 | 0.037 |
| Max Error | 1.406 | 2.109 | 1.406 | 1.406 | 0.151 | 0.113 |

## F. 5 Sample Output from Accelerometer



Figure F.5.1: Mounting of ADXL 204 Accelerometer
a. Mounting of ADXL 204 accelerometer on drilling head
b. Axes of ADXL 204 accelerometer in relation to drilling head

Table F.5.1: Conditions for Sampling of Accelerometer Signal

| Test Conditions |  |
| :--- | :--- |
| Spindle Speed | approximately $580 \mathrm{rev} / \mathrm{min}$ |
| Spindle Loading | Unloaded |
| Spindle Orientation | Vertical |
| Test Axis | X-axis |
| Signal Sampling Rate | 100 Hz |



Figure F.5.2: Accelerometer Signal Sampled at 100 Hz for a Spindle Speed of $580 \mathrm{rev} / \mathrm{min}$

## F. 6 Test Data - Samples

Note: only a sample of the data collected during performance testing is presented in this appendix. This is due to the extensive number of readings that are generated in a position control performance test (100 lines of readings for every 10 seconds). The data used in the preparation of ALL performance tables and graphs is located on the supplementary DVD disk.

Performance Test on Base Module (Figures 9.1-3)
Linear interpolation performed on the base module for a distance of 100 mm at a feed rate of 100 $\mathrm{mm} / \mathrm{min}$. The following data was used in the preparation of Figures 9.1-3.

Table F.6.1: Test Data, Performance Test on Base Module

| Speed <br> (pulses/s) | Ref Position <br> (pulses) | Measured <br> Position <br> (pulses) | Speed <br> $(\mathbf{m m} / \mathbf{m i n})$ | Ref <br> Position <br> $(\mathbf{m m})$ | Measured <br> Position <br> $(\mathbf{m m})$ | Error <br> $(\mathbf{m m})$ | Time <br> $(\mathbf{s})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | 0.000 | 0.000 | 0.000 | 0.000 | 0.0 |
| 1 | 34 | 1 | 2.930 | 0.166 | 0.005 | 0.161 | 0.1 |
| 1 | 68 | 2 | 2.930 | 0.332 | 0.010 | 0.322 | 0.2 |
| 6 | 102 | 8 | 17.578 | 0.498 | 0.039 | 0.459 | 0.3 |
| 17 | 136 | 25 | 49.805 | 0.664 | 0.122 | 0.542 | 0.4 |
| 27 | 170 | 52 | 79.102 | 0.830 | 0.254 | 0.576 | 0.5 |
| 33 | 204 | 85 | 96.680 | 0.996 | 0.415 | 0.581 | 0.6 |
| 36 | 238 | 121 | 105.469 | 1.162 | 0.591 | 0.571 | 0.7 |
| 40 | 272 | 161 | 117.188 | 1.328 | 0.786 | 0.542 | 0.8 |
| 41 | 306 | 202 | 120.117 | 1.494 | 0.986 | 0.508 | 0.9 |
| 42 | 340 | 244 | 123.047 | 1.660 | 1.191 | 0.469 | 1.0 |
| 44 | 374 | 288 | 128.906 | 1.826 | 1.406 | 0.420 | 1.1 |
| 44 | 408 | 332 | 128.906 | 1.992 | 1.621 | 0.371 | 1.2 |
| 42 | 442 | 374 | 123.047 | 2.158 | 1.826 | 0.332 | 1.3 |
| 41 | 476 | 415 | 120.117 | 2.324 | 2.026 | 0.298 | 1.4 |
| 38 | 510 | 453 | 111.328 | 2.490 | 2.212 | 0.278 | 1.5 |
| 36 | 544 | 489 | 105.469 | 2.656 | 2.388 | 0.269 | 1.6 |
| 36 | 578 | 525 | 105.469 | 2.822 | 2.563 | 0.259 | 1.7 |
| 35 | 612 | 560 | 102.539 | 2.988 | 2.734 | 0.254 | 1.8 |
| 35 | 646 | 595 | 102.539 | 3.154 | 2.905 | 0.249 | 1.9 |
| 36 | 680 | 631 | 105.469 | 3.320 | 3.081 | 0.239 | 2.0 |
| 37 | 714 | 668 | 108.398 | 3.486 | 3.262 | 0.225 | 2.1 |
| 38 | 748 | 706 | 111.328 | 3.652 | 3.447 | 0.205 | 2.2 |
| 40 | 782 | 746 | 117.188 | 3.818 | 3.643 | 0.176 | 2.3 |
| 41 | 816 | 787 | 120.117 | 3.984 | 3.843 | 0.142 | 2.4 |
| 41 | 850 | 828 | 120.117 | 4.150 | 4.043 | 0.107 | 2.5 |
| 39 | 884 | 867 | 114.258 | 4.316 | 4.233 | 0.083 | 2.6 |
| 37 | 918 | 904 | 108.398 | 4.482 | 4.414 | 0.068 | 2.7 |
| 35 | 952 | 939 | 102.539 | 4.648 | 4.585 | 0.063 | 2.8 |
| 33 | 986 | 972 | 96.680 | 4.814 | 4.746 | 0.068 | 2.9 |
| 32 | 1020 | 1004 | 93.750 | 4.980 | 4.902 | 0.078 | 3.0 |
| 31 | 1054 | 1035 | 90.820 | 5.146 | 5.054 | 0.093 | 3.1 |
|  |  |  |  |  |  |  |  |


| 31 | 1088 | 1066 | 90.820 | 5.313 | 5.205 | 0.107 | 3.2 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 33 | 1122 | 1099 | 96.680 | 5.479 | 5.366 | 0.112 | 3.3 |
| 33 | 1156 | 1132 | 96.680 | 5.645 | 5.527 | 0.117 | 3.4 |
| 35 | 1190 | 1167 | 102.539 | 5.811 | 5.698 | 0.112 | 3.5 |
| 37 | 1224 | 1204 | 108.398 | 5.977 | 5.879 | 0.098 | 3.6 |
| 38 | 1258 | 1242 | 111.328 | 6.143 | 6.064 | 0.078 | 3.7 |
| 41 | 1292 | 1283 | 120.117 | 6.309 | 6.265 | 0.044 | 3.8 |
| 38 | 1326 | 1321 | 111.328 | 6.475 | 6.450 | 0.024 | 3.9 |
| 38 | 1360 | 1359 | 111.328 | 6.641 | 6.636 | 0.005 | 4.0 |
| 37 | 1394 | 1396 | 108.398 | 6.807 | 6.816 | -0.010 | 4.1 |
| 36 | 1428 | 1432 | 105.469 | 6.973 | 6.992 | -0.020 | 4.2 |
| 33 | 1462 | 1465 | 96.680 | 7.139 | 7.153 | -0.015 | 4.3 |
| 29 | 1496 | 1494 | 84.961 | 7.305 | 7.295 | 0.010 | 4.4 |
| 29 | 1530 | 1523 | 84.961 | 7.471 | 7.437 | 0.034 | 4.5 |
| 30 | 1564 | 1553 | 87.891 | 7.637 | 7.583 | 0.054 | 4.6 |
| 31 | 1598 | 1584 | 90.820 | 7.803 | 7.734 | 0.068 | 4.7 |
| 32 | 1632 | 1616 | 93.750 | 7.969 | 7.891 | 0.078 | 4.8 |
| 33 | 1666 | 1649 | 96.680 | 8.135 | 8.052 | 0.083 | 4.9 |
| 36 | 1700 | 1685 | 105.469 | 8.301 | 8.228 | 0.073 | 5.0 |
| 37 | 1734 | 1722 | 108.398 | 8.467 | 8.408 | 0.059 | 5.1 |
| 37 | 1768 | 1759 | 108.398 | 8.633 | 8.589 | 0.044 | 5.2 |
| 39 | 1802 | 1798 | 114.258 | 8.799 | 8.779 | 0.020 | 5.3 |
| 39 | 1836 | 1837 | 114.258 | 8.965 | 8.970 | -0.005 | 5.4 |
| 37 | 1870 | 1874 | 108.398 | 9.131 | 9.150 | -0.020 | 5.5 |
| 36 | 1904 | 1910 | 105.469 | 9.297 | 9.326 | -0.029 | 5.6 |
| 34 | 1938 | 1944 | 99.609 | 9.463 | 9.492 | -0.029 | 5.7 |
| 32 | 1972 | 1976 | 93.750 | 9.629 | 9.648 | -0.020 | 5.8 |
| 30 | 2006 | 2006 | 87.891 | 9.795 | 9.795 | 0.000 | 5.9 |
| 30 | 2040 | 2036 | 87.891 | 9.961 | 9.941 | 0.020 | 6.0 |
| 30 | 2074 | 2066 | 87.891 | 10.127 | 10.088 | 0.039 | 6.1 |
| 31 | 2108 | 2097 | 90.820 | 10.293 | 10.239 | 0.054 | 6.2 |
| 33 | 2142 | 2130 | 96.680 | 10.459 | 10.400 | 0.059 | 6.3 |
| 34 | 2176 | 2164 | 99.609 | 10.625 | 10.566 | 0.059 | 6.4 |
| 36 | 2210 | 2200 | 105.469 | 10.791 | 10.742 | 0.049 | 6.5 |
| 39 | 2244 | 2239 | 114.258 | 10.957 | 10.933 | 0.024 | 6.6 |
| 38 | 2278 | 2277 | 111.328 | 11.123 | 11.118 | 0.005 | 6.7 |
| 40 | 2312 | 2317 | 117.188 | 11.289 | 11.313 | -0.024 | 6.8 |
| 38 | 2346 | 2355 | 111.328 | 11.455 | 11.499 | -0.044 | 6.9 |
| 37 | 2380 | 2392 | 108.398 | 11.621 | 11.680 | -0.059 | 7.0 |
| 35 | 2414 | 2427 | 102.539 | 11.787 | 11.851 | -0.063 | 7.1 |
| 31 | 2448 | 2458 | 90.820 | 11.953 | 12.002 | -0.049 | 7.2 |
| 31 | 2482 | 2489 | 90.820 | 12.119 | 12.153 | -0.034 | 7.3 |
| 29 | 2516 | 2518 | 84.961 | 12.285 | 12.295 | -0.010 | 7.4 |
| 29 | 2550 | 2547 | 84.961 | 12.451 | 12.437 | 0.015 | 7.5 |
| 30 | 2584 | 2577 | 87.891 | 12.617 | 12.583 | 0.034 | 7.6 |
| 32 | 2618 | 2609 | 93.750 | 12.783 | 12.739 | 0.044 | 7.7 |
| 32 | 2652 | 2641 | 93.750 | 12.949 | 12.896 | 0.054 | 7.8 |
| 35 | 2686 | 2676 | 102.539 | 13.115 | 13.066 | 0.049 | 7.9 |
| 37 | 2720 | 2713 | 108.398 | 13.281 | 13.247 | 0.034 | 8.0 |
| 36 | 2754 | 2749 | 105.469 | 13.447 | 13.423 | 0.024 | 8.1 |
| 39 | 2788 | 2788 | 114.258 | 13.613 | 13.613 | 0.000 | 8.2 |
| 38 | 2822 | 2826 | 111.328 | 13.779 | 13.799 | -0.020 | 8.3 |
| 38 | 2856 | 2864 | 111.328 | 13.945 | 13.984 | -0.039 | 8.4 |


| 36 | 2890 | 2900 | 105.469 | 14.111 | 14.160 | -0.049 | 8.5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 34 | 2924 | 2934 | 99.609 | 14.277 | 14.326 | -0.049 | 8.6 |
| 33 | 2958 | 2967 | 96.680 | 14.443 | 14.487 | -0.044 | 8.7 |
| 32 | 2992 | 2999 | 93.750 | 14.609 | 14.644 | -0.034 | 8.8 |
| 30 | 3026 | 3029 | 87.891 | 14.775 | 14.790 | -0.015 | 8.9 |
| 30 | 3060 | 3059 | 87.891 | 14.941 | 14.937 | 0.005 | 9.0 |
| 30 | 3094 | 3089 | 87.891 | 15.107 | 15.083 | 0.024 | 9.1 |
| 31 | 3128 | 3120 | 90.820 | 15.273 | 15.234 | 0.039 | 9.2 |
| 33 | 3162 | 3153 | 96.680 | 15.439 | 15.396 | 0.044 | 9.3 |
| 36 | 3196 | 3189 | 105.469 | 15.605 | 15.571 | 0.034 | 9.4 |
| 38 | 3230 | 3227 | 111.328 | 15.771 | 15.757 | 0.015 | 9.5 |
| 37 | 3264 | 3264 | 108.398 | 15.938 | 15.938 | 0.000 | 9.6 |
| 37 | 3298 | 3301 | 108.398 | 16.104 | 16.118 | -0.015 | 9.7 |
| 38 | 3332 | 3339 | 111.328 | 16.270 | 16.304 | -0.034 | 9.8 |
| 39 | 3366 | 3378 | 114.258 | 16.436 | 16.494 | -0.059 | 9.9 |
| 36 | 3400 | 3414 | 105.469 | 16.602 | 16.670 | -0.068 | 10.0 |
| 35 | 3434 | 3449 | 102.539 | 16.768 | 16.841 | -0.073 | 10.1 |
| 30 | 3468 | 3479 | 87.891 | 16.934 | 16.987 | -0.054 | 10.2 |
| 28 | 3502 | 3507 | 82.031 | 17.100 | 17.124 | -0.024 | 10.3 |
| 29 | 3536 | 3536 | 84.961 | 17.266 | 17.266 | 0.000 | 10.4 |
| 30 | 3570 | 3566 | 87.891 | 17.432 | 17.412 | 0.020 | 10.5 |
| 31 | 3604 | 3597 | 90.820 | 17.598 | 17.563 | 0.034 | 10.6 |
| 34 | 3638 | 3631 | 99.609 | 17.764 | 17.729 | 0.034 | 10.7 |
| 34 | 3672 | 3665 | 99.609 | 17.930 | 17.896 | 0.034 | 10.8 |
| 36 | 3706 | 3701 | 105.469 | 18.096 | 18.071 | 0.024 | 10.9 |
| 37 | 3740 | 3738 | 108.398 | 18.262 | 18.252 | 0.010 | 11.0 |
| 37 | 3774 | 3775 | 108.398 | 18.428 | 18.433 | -0.005 | 11.1 |
| 37 | 3808 | 3812 | 108.398 | 18.594 | 18.613 | -0.020 | 11.2 |
| 36 | 3842 | 3848 | 105.469 | 18.760 | 18.789 | -0.029 | 11.3 |
| 36 | 3876 | 3884 | 105.469 | 18.926 | 18.965 | -0.039 | 11.4 |
| 38 | 3910 | 3922 | 111.328 | 19.092 | 19.150 | -0.059 | 11.5 |
| 33 | 3944 | 3955 | 96.680 | 19.258 | 19.312 | -0.054 | 11.6 |
| 30 | 3978 | 3985 | 87.891 | 19.424 | 19.458 | -0.034 | 11.7 |
| 29 | 4012 | 4014 | 84.961 | 19.590 | 19.600 | -0.010 | 11.8 |
| 29 | 4046 | 4043 | 84.961 | 19.756 | 19.741 | 0.015 | 11.9 |
| 30 | 4080 | 4073 | 87.891 | 19.922 | 19.888 | 0.034 | 12.0 |
| 32 | 4114 | 4105 | 93.750 | 20.088 | 20.044 | 0.044 | 12.1 |
| 33 | 4148 | 4138 | 96.680 | 20.254 | 20.205 | 0.049 | 12.2 |
| 35 | 4182 | 4173 | 102.539 | 20.420 | 20.376 | 0.044 | 12.3 |
| 38 | 4216 | 4211 | 111.328 | 20.586 | 20.562 | 0.024 | 12.4 |
| 37 | 4250 | 4248 | 108.398 | 20.752 | 20.742 | 0.010 | 12.5 |
| 37 | 4284 | 4285 | 108.398 | 20.918 | 20.923 | -0.005 | 12.6 |
| 37 | 4318 | 4322 | 108.398 | 21.084 | 21.104 | -0.020 | 12.7 |
| 38 | 4352 | 4360 | 111.328 | 21.250 | 21.289 | -0.039 | 12.8 |
| 35 | 4386 | 4395 | 102.539 | 21.416 | 21.460 | -0.044 | 12.9 |
| 36 | 4420 | 4431 | 105.469 | 21.582 | 21.636 | -0.054 | 13.0 |
| 32 | 4454 | 4463 | 93.750 | 21.748 | 21.792 | -0.044 | 13.1 |
| 31 | 4488 | 4494 | 90.820 | 21.914 | 21.943 | -0.029 | 13.2 |
| 28 | 4522 | 4522 | 82.031 | 22.080 | 22.080 | 0.000 | 13.3 |
| 29 | 4556 | 4551 | 84.961 | 22.246 | 22.222 | 0.024 | 13.4 |
| 30 | 4590 | 4581 | 87.891 | 22.412 | 22.368 | 0.044 | 13.5 |
| 31 | 4624 | 4612 | 90.820 | 22.578 | 22.520 | 0.059 | 13.6 |
| 34 | 4658 | 4646 | 99.609 | 22.744 | 22.686 | 0.059 | 13.7 |


| 37 | 4692 | 4683 | 108.398 | 22.910 | 22.866 | 0.044 | 13.8 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 38 | 4726 | 4721 | 111.328 | 23.076 | 23.052 | 0.024 | 13.9 |
| 39 | 4760 | 4760 | 114.258 | 23.242 | 23.242 | 0.000 | 14.0 |
| 37 | 4794 | 4797 | 108.398 | 23.408 | 23.423 | -0.015 | 14.1 |
| 37 | 4828 | 4834 | 108.398 | 23.574 | 23.604 | -0.029 | 14.2 |
| 37 | 4862 | 4871 | 108.398 | 23.740 | 23.784 | -0.044 | 14.3 |
| 36 | 4896 | 4907 | 105.469 | 23.906 | 23.960 | -0.054 | 14.4 |
| 34 | 4930 | 4941 | 99.609 | 24.072 | 24.126 | -0.054 | 14.5 |
| 33 | 4964 | 4974 | 96.680 | 24.238 | 24.287 | -0.049 | 14.6 |
| 29 | 4998 | 5003 | 84.961 | 24.404 | 24.429 | -0.024 | 14.7 |
| 29 | 5032 | 5032 | 84.961 | 24.570 | 24.570 | 0.000 | 14.8 |
| 29 | 5066 | 5061 | 84.961 | 24.736 | 24.712 | 0.024 | 14.9 |
| 30 | 5100 | 5091 | 87.891 | 24.902 | 24.858 | 0.044 | 15.0 |
| 31 | 5134 | 5122 | 90.820 | 25.068 | 25.010 | 0.059 | 15.1 |
| 34 | 5168 | 5156 | 99.609 | 25.234 | 25.176 | 0.059 | 15.2 |
| 35 | 5202 | 5191 | 102.539 | 25.400 | 25.347 | 0.054 | 15.3 |
| 39 | 5236 | 5230 | 114.258 | 25.566 | 25.537 | 0.029 | 15.4 |
| 38 | 5270 | 5268 | 111.328 | 25.732 | 25.723 | 0.010 | 15.5 |
| 37 | 5304 | 5305 | 108.398 | 25.898 | 25.903 | -0.005 | 15.6 |
| 38 | 5338 | 5343 | 111.328 | 26.064 | 26.089 | -0.024 | 15.7 |
| 37 | 5372 | 5380 | 108.398 | 26.230 | 26.270 | -0.039 | 15.8 |
| 35 | 5406 | 5415 | 102.539 | 26.396 | 26.440 | -0.044 | 15.9 |
| 35 | 5440 | 5450 | 102.539 | 26.563 | 26.611 | -0.049 | 16.0 |
| 32 | 5474 | 5482 | 93.750 | 26.729 | 26.768 | -0.039 | 16.1 |
| 30 | 5508 | 5512 | 87.891 | 26.895 | 26.914 | -0.020 | 16.2 |
| 28 | 5542 | 5540 | 82.031 | 27.061 | 27.051 | 0.010 | 16.3 |
| 30 | 5576 | 5570 | 87.891 | 27.227 | 27.197 | 0.029 | 16.4 |
| 31 | 5610 | 5601 | 90.820 | 27.393 | 27.349 | 0.044 | 16.5 |
| 32 | 5644 | 5633 | 93.750 | 27.559 | 27.505 | 0.054 | 16.6 |
| 34 | 5678 | 5667 | 99.609 | 27.725 | 27.671 | 0.054 | 16.7 |
| 36 | 5712 | 5703 | 105.469 | 27.891 | 27.847 | 0.044 | 16.8 |
| 37 | 5746 | 5740 | 108.398 | 28.057 | 28.027 | 0.029 | 16.9 |
| 38 | 5780 | 5778 | 111.328 | 28.223 | 28.213 | 0.010 | 17.0 |
| 38 | 5814 | 5816 | 111.328 | 28.389 | 28.398 | -0.010 | 17.1 |
| 38 | 5848 | 5854 | 111.328 | 28.555 | 28.584 | -0.029 | 17.2 |
| 37 | 5882 | 5891 | 108.398 | 28.721 | 28.765 | -0.044 | 17.3 |
| 36 | 5916 | 5927 | 105.469 | 28.887 | 28.940 | -0.054 | 17.4 |
| 34 | 5950 | 5961 | 99.609 | 29.053 | 29.106 | -0.054 | 17.5 |
| 31 | 5984 | 5992 | 90.820 | 29.219 | 29.258 | -0.039 | 17.6 |
| 29 | 6018 | 6021 | 84.961 | 29.385 | 29.399 | -0.015 | 17.7 |
| 29 | 6052 | 6050 | 84.961 | 29.551 | 29.541 | 0.010 | 17.8 |
| 29 | 6086 | 6079 | 84.961 | 29.717 | 29.683 | 0.034 | 17.9 |
| 30 | 6120 | 6109 | 87.891 | 29.883 | 29.829 | 0.054 | 18.0 |
| 32 | 6154 | 6141 | 93.750 | 30.049 | 29.985 | 0.063 | 18.1 |
| 34 | 6188 | 6175 | 99.609 | 30.215 | 30.151 | 0.063 | 18.2 |
| 37 | 6222 | 6212 | 108.398 | 30.381 | 30.332 | 0.049 | 18.3 |
| 37 | 6256 | 6249 | 108.398 | 30.547 | 30.513 | 0.034 | 18.4 |
| 37 | 6290 | 6286 | 108.398 | 30.713 | 30.693 | 0.020 | 18.5 |
| 38 | 6324 | 6324 | 111.328 | 30.879 | 30.879 | 0.000 | 18.6 |
| 38 | 6358 | 6362 | 111.328 | 31.045 | 31.064 | -0.020 | 18.7 |
| 38 | 6392 | 6400 | 111.328 | 31.211 | 31.250 | -0.039 | 18.8 |
| 36 | 6426 | 6436 | 105.469 | 31.377 | 31.426 | -0.049 | 18.9 |
| 33 | 6460 | 6469 | 96.680 | 31.543 | 31.587 | -0.044 | 19.0 |


| 32 | 6494 | 6501 | 93.750 | 31.709 | 31.743 | -0.034 | 19.1 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 29 | 6528 | 6530 | 84.961 | 31.875 | 31.885 | -0.010 | 19.2 |
| 28 | 6562 | 6558 | 82.031 | 32.041 | 32.021 | 0.020 | 19.3 |
| 30 | 6596 | 6588 | 87.891 | 32.207 | 32.168 | 0.039 | 19.4 |
| 31 | 6630 | 6619 | 90.820 | 32.373 | 32.319 | 0.054 | 19.5 |
| 33 | 6664 | 6652 | 96.680 | 32.539 | 32.480 | 0.059 | 19.6 |
| 34 | 6698 | 6686 | 99.609 | 32.705 | 32.646 | 0.059 | 19.7 |
| 37 | 6732 | 6723 | 108.398 | 32.871 | 32.827 | 0.044 | 19.8 |
| 37 | 6766 | 6760 | 108.398 | 33.037 | 33.008 | 0.029 | 19.9 |
| 38 | 6800 | 6798 | 111.328 | 33.203 | 33.193 | 0.010 | 20.0 |
| 38 | 6834 | 6836 | 111.328 | 33.369 | 33.379 | -0.010 | 20.1 |
| 38 | 6868 | 6874 | 111.328 | 33.535 | 33.564 | -0.029 | 20.2 |
| 37 | 6902 | 6911 | 108.398 | 33.701 | 33.745 | -0.044 | 20.3 |
| 35 | 6936 | 6946 | 102.539 | 33.867 | 33.916 | -0.049 | 20.4 |
| 35 | 6970 | 6981 | 102.539 | 34.033 | 34.087 | -0.054 | 20.5 |
| 30 | 7004 | 7011 | 87.891 | 34.199 | 34.233 | -0.034 | 20.6 |
| 29 | 7038 | 7040 | 84.961 | 34.365 | 34.375 | -0.010 | 20.7 |
| 28 | 7072 | 7068 | 82.031 | 34.531 | 34.512 | 0.020 | 20.8 |
| 30 | 7106 | 7098 | 87.891 | 34.697 | 34.658 | 0.039 | 20.9 |
| 32 | 7140 | 7130 | 93.750 | 34.863 | 34.814 | 0.049 | 21.0 |
| 34 | 7174 | 7164 | 99.609 | 35.029 | 34.980 | 0.049 | 21.1 |
| 35 | 7208 | 7199 | 102.539 | 35.195 | 35.151 | 0.044 | 21.2 |
| 38 | 7242 | 7237 | 111.328 | 35.361 | 35.337 | 0.024 | 21.3 |
| 37 | 7276 | 7274 | 108.398 | 35.527 | 35.518 | 0.010 | 21.4 |
| 38 | 7310 | 7312 | 111.328 | 35.693 | 35.703 | -0.010 | 21.5 |
| 37 | 7344 | 7349 | 108.398 | 35.859 | 35.884 | -0.024 | 21.6 |
| 38 | 7378 | 7387 | 111.328 | 36.025 | 36.069 | -0.044 | 21.7 |
| 36 | 7412 | 7423 | 105.469 | 36.191 | 36.245 | -0.054 | 21.8 |
| 35 | 7446 | 7458 | 102.539 | 36.357 | 36.416 | -0.059 | 21.9 |
| 32 | 7480 | 7490 | 93.750 | 36.523 | 36.572 | -0.049 | 22.0 |
| 30 | 7514 | 7520 | 87.891 | 36.689 | 36.719 | -0.029 | 22.1 |
| 28 | 7548 | 7548 | 82.031 | 36.855 | 36.855 | 0.000 | 22.2 |
| 30 | 7582 | 7578 | 87.891 | 37.021 | 37.002 | 0.020 | 22.3 |
| 31 | 7616 | 7609 | 90.820 | 37.188 | 37.153 | 0.034 | 22.4 |
| 32 | 7650 | 7641 | 93.750 | 37.354 | 37.310 | 0.044 | 22.5 |
| 34 | 7684 | 7675 | 99.609 | 37.520 | 37.476 | 0.044 | 22.6 |
| 35 | 7718 | 7710 | 102.539 | 37.686 | 37.646 | 0.039 | 22.7 |
| 38 | 7752 | 7748 | 111.328 | 37.852 | 37.832 | 0.020 | 22.8 |
| 37 | 7786 | 7785 | 108.398 | 38.018 | 38.013 | 0.005 | 22.9 |
| 38 | 7820 | 7823 | 111.328 | 38.184 | 38.198 | -0.015 | 23.0 |
| 37 | 7854 | 7860 | 108.398 | 38.350 | 38.379 | -0.029 | 23.1 |
| 38 | 7888 | 7898 | 111.328 | 38.516 | 38.564 | -0.049 | 23.2 |
| 36 | 7922 | 7934 | 105.469 | 38.682 | 38.740 | -0.059 | 23.3 |
| 34 | 7956 | 7968 | 99.609 | 38.848 | 38.906 | -0.059 | 23.4 |
| 31 | 7990 | 7999 | 90.820 | 39.014 | 39.058 | -0.044 | 23.5 |
| 29 | 8024 | 8028 | 84.961 | 39.180 | 39.199 | -0.020 | 23.6 |
| 29 | 8058 | 8057 | 84.961 | 39.346 | 39.341 | 0.005 | 23.7 |
| 29 | 8092 | 8086 | 84.961 | 39.512 | 39.482 | 0.029 | 23.8 |
| 31 | 8126 | 8117 | 90.820 | 39.678 | 39.634 | 0.044 | 23.9 |
| 32 | 8160 | 8149 | 93.750 | 39.844 | 39.790 | 0.054 | 24.0 |
| 35 | 8194 | 8184 | 102.539 | 40.010 | 39.961 | 0.049 | 24.1 |
| 37 | 8228 | 8221 | 108.398 | 40.176 | 40.142 | 0.034 | 24.2 |
| 38 | 8262 | 8259 | 111.328 | 40.342 | 40.327 | 0.015 | 24.3 |


| 37 | 8296 | 8296 | 108.398 | 40.508 | 40.508 | 0.000 | 24.4 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 38 | 8330 | 8334 | 111.328 | 40.674 | 40.693 | -0.020 | 24.5 |
| 37 | 8364 | 8371 | 108.398 | 40.840 | 40.874 | -0.034 | 24.6 |
| 37 | 8398 | 8408 | 108.398 | 41.006 | 41.055 | -0.049 | 24.7 |
| 35 | 8432 | 8443 | 102.539 | 41.172 | 41.226 | -0.054 | 24.8 |
| 33 | 8466 | 8476 | 96.680 | 41.338 | 41.387 | -0.049 | 24.9 |
| 31 | 8500 | 8507 | 90.820 | 41.504 | 41.538 | -0.034 | 25.0 |
| 29 | 8534 | 8536 | 84.961 | 41.670 | 41.680 | -0.010 | 25.1 |
| 28 | 8568 | 8564 | 82.031 | 41.836 | 41.816 | 0.020 | 25.2 |
| 30 | 8602 | 8594 | 87.891 | 42.002 | 41.963 | 0.039 | 25.3 |
| 31 | 8636 | 8625 | 90.820 | 42.168 | 42.114 | 0.054 | 25.4 |
| 34 | 8670 | 8659 | 99.609 | 42.334 | 42.280 | 0.054 | 25.5 |
| 35 | 8704 | 8694 | 102.539 | 42.500 | 42.451 | 0.049 | 25.6 |
| 37 | 8738 | 8731 | 108.398 | 42.666 | 42.632 | 0.034 | 25.7 |
| 38 | 8772 | 8769 | 111.328 | 42.832 | 42.817 | 0.015 | 25.8 |
| 38 | 8806 | 8807 | 111.328 | 42.998 | 43.003 | -0.005 | 25.9 |
| 37 | 8840 | 8844 | 108.398 | 43.164 | 43.184 | -0.020 | 26.0 |
| 37 | 8874 | 8881 | 108.398 | 43.330 | 43.364 | -0.034 | 26.1 |
| 37 | 8908 | 8918 | 108.398 | 43.496 | 43.545 | -0.049 | 26.2 |
| 34 | 8942 | 8952 | 99.609 | 43.662 | 43.711 | -0.049 | 26.3 |
| 33 | 8976 | 8985 | 96.680 | 43.828 | 43.872 | -0.044 | 26.4 |
| 31 | 9010 | 9016 | 90.820 | 43.994 | 44.023 | -0.029 | 26.5 |
| 28 | 9044 | 9044 | 82.031 | 44.160 | 44.160 | 0.000 | 26.6 |
| 29 | 9078 | 9073 | 84.961 | 44.326 | 44.302 | 0.024 | 26.7 |
| 30 | 9112 | 9103 | 87.891 | 44.492 | 44.448 | 0.044 | 26.8 |
| 33 | 9146 | 9136 | 96.680 | 44.658 | 44.609 | 0.049 | 26.9 |
| 33 | 9180 | 9169 | 96.680 | 44.824 | 44.771 | 0.054 | 27.0 |
| 37 | 9214 | 9206 | 108.398 | 44.990 | 44.951 | 0.039 | 27.1 |
| 37 | 9248 | 9243 | 108.398 | 45.156 | 45.132 | 0.024 | 27.2 |
| 37 | 9282 | 9280 | 108.398 | 45.322 | 45.313 | 0.010 | 27.3 |
| 40 | 9316 | 9320 | 117.188 | 45.488 | 45.508 | -0.020 | 27.4 |
| 37 | 9350 | 9357 | 108.398 | 45.654 | 45.688 | -0.034 | 27.5 |
| 37 | 9384 | 9394 | 108.398 | 45.820 | 45.869 | -0.049 | 27.6 |
| 37 | 9418 | 9431 | 108.398 | 45.986 | 46.050 | -0.063 | 27.7 |
| 33 | 9452 | 9464 | 96.680 | 46.152 | 46.211 | -0.059 | 27.8 |
| 32 | 9486 | 9496 | 93.750 | 46.318 | 46.367 | -0.049 | 27.9 |
| 29 | 9520 | 9525 | 84.961 | 46.484 | 46.509 | -0.024 | 28.0 |
| 28 | 9554 | 9553 | 82.031 | 46.650 | 46.646 | 0.005 | 28.1 |
| 29 | 9588 | 9582 | 84.961 | 46.816 | 46.787 | 0.029 | 28.2 |
| 30 | 9622 | 9612 | 87.891 | 46.982 | 46.934 | 0.049 | 28.3 |
| 33 | 9656 | 9645 | 96.680 | 47.148 | 47.095 | 0.054 | 28.4 |
| 34 | 9690 | 9679 | 99.609 | 47.314 | 47.261 | 0.054 | 28.5 |
| 37 | 9724 | 9716 | 108.398 | 47.480 | 47.441 | 0.039 | 28.6 |
| 38 | 9758 | 9754 | 111.328 | 47.646 | 47.627 | 0.020 | 28.7 |
| 39 | 9792 | 9793 | 114.258 | 47.813 | 47.817 | -0.005 | 28.8 |
| 38 | 9826 | 9831 | 111.328 | 47.979 | 48.003 | -0.024 | 28.9 |
| 37 | 9860 | 9868 | 108.398 | 48.145 | 48.184 | -0.039 | 29.0 |
| 37 | 9894 | 9905 | 108.398 | 48.311 | 48.364 | -0.054 | 29.1 |
| 34 | 9928 | 9939 | 99.609 | 48.477 | 48.530 | -0.054 | 29.2 |
| 34 | 9962 | 9973 | 99.609 | 48.643 | 48.696 | -0.054 | 29.3 |
| 31 | 9996 | 10004 | 90.820 | 48.809 | 48.848 | -0.039 | 29.4 |
| 28 | 10030 | 10032 | 82.031 | 48.975 | 48.984 | -0.010 | 29.5 |
| 29 | 10064 | 10061 | 84.961 | 49.141 | 49.126 | 0.015 | 29.6 |


| 29 | 10098 | 10090 | 84.961 | 49.307 | 49.268 | 0.039 | 29.7 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 31 | 10132 | 10121 | 90.820 | 49.473 | 49.419 | 0.054 | 29.8 |
| 32 | 10166 | 10153 | 93.750 | 49.639 | 49.575 | 0.063 | 29.9 |
| 36 | 10200 | 10189 | 105.469 | 49.805 | 49.751 | 0.054 | 30.0 |
| 37 | 10234 | 10226 | 108.398 | 49.971 | 49.932 | 0.039 | 30.1 |
| 37 | 10268 | 10263 | 108.398 | 50.137 | 50.112 | 0.024 | 30.2 |
| 38 | 10302 | 10301 | 111.328 | 50.303 | 50.298 | 0.005 | 30.3 |
| 39 | 10336 | 10340 | 114.258 | 50.469 | 50.488 | -0.020 | 30.4 |
| 38 | 10370 | 10378 | 111.328 | 50.635 | 50.674 | -0.039 | 30.5 |
| 36 | 10404 | 10414 | 105.469 | 50.801 | 50.850 | -0.049 | 30.6 |
| 35 | 10438 | 10449 | 102.539 | 50.967 | 51.021 | -0.054 | 30.7 |
| 33 | 10472 | 10482 | 96.680 | 51.133 | 51.182 | -0.049 | 30.8 |
| 30 | 10506 | 10512 | 87.891 | 51.299 | 51.328 | -0.029 | 30.9 |
| 29 | 10540 | 10541 | 84.961 | 51.465 | 51.470 | -0.005 | 31.0 |
| 28 | 10574 | 10569 | 82.031 | 51.631 | 51.606 | 0.024 | 31.1 |
| 30 | 10608 | 10599 | 87.891 | 51.797 | 51.753 | 0.044 | 31.2 |
| 33 | 10642 | 10632 | 96.680 | 51.963 | 51.914 | 0.049 | 31.3 |
| 34 | 10676 | 10666 | 99.609 | 52.129 | 52.080 | 0.049 | 31.4 |
| 36 | 10710 | 10702 | 105.469 | 52.295 | 52.256 | 0.039 | 31.5 |
| 37 | 10744 | 10739 | 108.398 | 52.461 | 52.437 | 0.024 | 31.6 |
| 37 | 10778 | 10776 | 108.398 | 52.627 | 52.617 | 0.010 | 31.7 |
| 37 | 10812 | 10813 | 108.398 | 52.793 | 52.798 | -0.005 | 31.8 |
| 38 | 10846 | 10851 | 111.328 | 52.959 | 52.983 | -0.024 | 31.9 |
| 37 | 10880 | 10888 | 108.398 | 53.125 | 53.164 | -0.039 | 32.0 |
| 36 | 10914 | 10924 | 105.469 | 53.291 | 53.340 | -0.049 | 32.1 |
| 35 | 10948 | 10959 | 102.539 | 53.457 | 53.511 | -0.054 | 32.2 |
| 33 | 10982 | 10992 | 96.680 | 53.623 | 53.672 | -0.049 | 32.3 |
| 30 | 11016 | 11022 | 87.891 | 53.789 | 53.818 | -0.029 | 32.4 |
| 28 | 11050 | 11050 | 82.031 | 53.955 | 53.955 | 0.000 | 32.5 |
| 29 | 11084 | 11079 | 84.961 | 54.121 | 54.097 | 0.024 | 32.6 |
| 29 | 11118 | 11108 | 84.961 | 54.287 | 54.238 | 0.049 | 32.7 |
| 32 | 11152 | 11140 | 93.750 | 54.453 | 54.395 | 0.059 | 32.8 |
| 34 | 11186 | 11174 | 99.609 | 54.619 | 54.561 | 0.059 | 32.9 |
| 36 | 11220 | 11210 | 105.469 | 54.785 | 54.736 | 0.049 | 33.0 |
| 38 | 11254 | 11248 | 111.328 | 54.951 | 54.922 | 0.029 | 33.1 |
| 37 | 11288 | 11285 | 108.398 | 55.117 | 55.103 | 0.015 | 33.2 |
| 38 | 11322 | 11323 | 111.328 | 55.283 | 55.288 | -0.005 | 33.3 |
| 38 | 11356 | 11361 | 111.328 | 55.449 | 55.474 | -0.024 | 33.4 |
| 36 | 11390 | 11397 | 105.469 | 55.615 | 55.649 | -0.034 | 33.5 |
| 36 | 11424 | 11433 | 105.469 | 55.781 | 55.825 | -0.044 | 33.6 |
| 35 | 11458 | 11468 | 102.539 | 55.947 | 55.996 | -0.049 | 33.7 |
| 32 | 11492 | 11500 | 93.750 | 56.113 | 56.152 | -0.039 | 33.8 |
| 30 | 11526 | 11530 | 87.891 | 56.279 | 56.299 | -0.020 | 33.9 |
| 28 | 11560 | 11558 | 82.031 | 56.445 | 56.436 | 0.010 | 34.0 |
| 30 | 11594 | 11588 | 87.891 | 56.611 | 56.582 | 0.029 | 34.1 |
| 30 | 11628 | 11618 | 87.891 | 56.777 | 56.729 | 0.049 | 34.2 |
| 32 | 11662 | 11650 | 93.750 | 56.943 | 56.885 | 0.059 | 34.3 |
| 34 | 11696 | 11684 | 99.609 | 57.109 | 57.051 | 0.059 | 34.4 |
| 37 | 11730 | 11721 | 108.398 | 57.275 | 57.231 | 0.044 | 34.5 |
| 37 | 11764 | 11758 | 108.398 | 57.441 | 57.412 | 0.029 | 34.6 |
| 39 | 11798 | 11797 | 114.258 | 57.607 | 57.603 | 0.005 | 34.7 |
| 37 | 11832 | 11834 | 108.398 | 57.773 | 57.783 | -0.010 | 34.8 |
| 37 | 11866 | 11871 | 108.398 | 57.939 | 57.964 | -0.024 | 34.9 |


| 37 | 11900 | 11908 | 108.398 | 58.105 | 58.145 | -0.039 | 35.0 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 35 | 11934 | 11943 | 102.539 | 58.271 | 58.315 | -0.044 | 35.1 |
| 34 | 11968 | 11977 | 99.609 | 58.438 | 58.481 | -0.044 | 35.2 |
| 32 | 12002 | 12009 | 93.750 | 58.604 | 58.638 | -0.034 | 35.3 |
| 29 | 12036 | 12038 | 84.961 | 58.770 | 58.779 | -0.010 | 35.4 |
| 29 | 12070 | 12067 | 84.961 | 58.936 | 58.921 | 0.015 | 35.5 |
| 30 | 12104 | 12097 | 87.891 | 59.102 | 59.067 | 0.034 | 35.6 |
| 31 | 12138 | 12128 | 90.820 | 59.268 | 59.219 | 0.049 | 35.7 |
| 32 | 12172 | 12160 | 93.750 | 59.434 | 59.375 | 0.059 | 35.8 |
| 35 | 12206 | 12195 | 102.539 | 59.600 | 59.546 | 0.054 | 35.9 |
| 37 | 12240 | 12232 | 108.398 | 59.766 | 59.727 | 0.039 | 36.0 |
| 38 | 12274 | 12270 | 111.328 | 59.932 | 59.912 | 0.020 | 36.1 |
| 38 | 12308 | 12308 | 111.328 | 60.098 | 60.098 | 0.000 | 36.2 |
| 39 | 12342 | 12347 | 114.258 | 60.264 | 60.288 | -0.024 | 36.3 |
| 37 | 12376 | 12384 | 108.398 | 60.430 | 60.469 | -0.039 | 36.4 |
| 36 | 12410 | 12420 | 105.469 | 60.596 | 60.645 | -0.049 | 36.5 |
| 35 | 12444 | 12455 | 102.539 | 60.762 | 60.815 | -0.054 | 36.6 |
| 34 | 12478 | 12489 | 99.609 | 60.928 | 60.981 | -0.054 | 36.7 |
| 31 | 12512 | 12520 | 90.820 | 61.094 | 61.133 | -0.039 | 36.8 |
| 28 | 12546 | 12548 | 82.031 | 61.260 | 61.270 | -0.010 | 36.9 |
| 29 | 12580 | 12577 | 84.961 | 61.426 | 61.411 | 0.015 | 37.0 |
| 30 | 12614 | 12607 | 87.891 | 61.592 | 61.558 | 0.034 | 37.1 |
| 31 | 12648 | 12638 | 90.820 | 61.758 | 61.709 | 0.049 | 37.2 |
| 33 | 12682 | 12671 | 96.680 | 61.924 | 61.870 | 0.054 | 37.3 |
| 35 | 12716 | 12706 | 102.539 | 62.090 | 62.041 | 0.049 | 37.4 |
| 38 | 12750 | 12744 | 111.328 | 62.256 | 62.227 | 0.029 | 37.5 |
| 37 | 12784 | 12781 | 108.398 | 62.422 | 62.407 | 0.015 | 37.6 |
| 38 | 12818 | 12819 | 111.328 | 62.588 | 62.593 | -0.005 | 37.7 |
| 38 | 12852 | 12857 | 111.328 | 62.754 | 62.778 | -0.024 | 37.8 |
| 37 | 12886 | 12894 | 108.398 | 62.920 | 62.959 | -0.039 | 37.9 |
| 36 | 12920 | 12930 | 105.469 | 63.086 | 63.135 | -0.049 | 38.0 |
| 35 | 12954 | 12965 | 102.539 | 63.252 | 63.306 | -0.054 | 38.1 |
| 33 | 12988 | 12998 | 96.680 | 63.418 | 63.467 | -0.049 | 38.2 |
| 30 | 13022 | 13028 | 87.891 | 63.584 | 63.613 | -0.029 | 38.3 |
| 29 | 13056 | 13057 | 84.961 | 63.750 | 63.755 | -0.005 | 38.4 |
| 29 | 13090 | 13086 | 84.961 | 63.916 | 63.896 | 0.020 | 38.5 |
| 30 | 13124 | 13116 | 87.891 | 64.082 | 64.043 | 0.039 | 38.6 |
| 32 | 13158 | 13148 | 93.750 | 64.248 | 64.199 | 0.049 | 38.7 |
| 34 | 13192 | 13182 | 99.609 | 64.414 | 64.365 | 0.049 | 38.8 |
| 36 | 13226 | 13218 | 105.469 | 64.580 | 64.541 | 0.039 | 38.9 |
| 37 | 13260 | 13255 | 108.398 | 64.746 | 64.722 | 0.024 | 39.0 |
| 37 | 13294 | 13292 | 108.398 | 64.912 | 64.902 | 0.010 | 39.1 |
| 38 | 13328 | 13330 | 111.328 | 65.078 | 65.088 | -0.010 | 39.2 |
| 38 | 13362 | 13368 | 111.328 | 65.244 | 65.273 | -0.029 | 39.3 |
| 36 | 13396 | 13404 | 105.469 | 65.410 | 65.449 | -0.039 | 39.4 |
| 36 | 13430 | 13440 | 105.469 | 65.576 | 65.625 | -0.049 | 39.5 |
| 34 | 13464 | 13474 | 99.609 | 65.742 | 65.791 | -0.049 | 39.6 |
| 32 | 13498 | 13506 | 93.750 | 65.908 | 65.947 | -0.039 | 39.7 |
| 30 | 13532 | 13536 | 87.891 | 66.074 | 66.094 | -0.020 | 39.8 |
| 29 | 13566 | 13565 | 84.961 | 66.240 | 66.235 | 0.005 | 39.9 |
| 29 | 13600 | 13594 | 84.961 | 66.406 | 66.377 | 0.029 | 40.0 |
| 30 | 13634 | 13624 | 87.891 | 66.572 | 66.523 | 0.049 | 40.1 |
| 32 | 13668 | 13656 | 93.750 | 66.738 | 66.680 | 0.059 | 40.2 |


| 35 | 13702 | 13691 | 102.539 | 66.904 | 66.851 | 0.054 | 40.3 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 37 | 13736 | 13728 | 108.398 | 67.070 | 67.031 | 0.039 | 40.4 |
| 38 | 13770 | 13766 | 111.328 | 67.236 | 67.217 | 0.020 | 40.5 |
| 37 | 13804 | 13803 | 108.398 | 67.402 | 67.397 | 0.005 | 40.6 |
| 38 | 13838 | 13841 | 111.328 | 67.568 | 67.583 | -0.015 | 40.7 |
| 38 | 13872 | 13879 | 111.328 | 67.734 | 67.769 | -0.034 | 40.8 |
| 37 | 13906 | 13916 | 108.398 | 67.900 | 67.949 | -0.049 | 40.9 |
| 36 | 13940 | 13952 | 105.469 | 68.066 | 68.125 | -0.059 | 41.0 |
| 33 | 13974 | 13985 | 96.680 | 68.232 | 68.286 | -0.054 | 41.1 |
| 32 | 14008 | 14017 | 93.750 | 68.398 | 68.442 | -0.044 | 41.2 |
| 29 | 14042 | 14046 | 84.961 | 68.564 | 68.584 | -0.020 | 41.3 |
| 28 | 14076 | 14074 | 82.031 | 68.730 | 68.721 | 0.010 | 41.4 |
| 31 | 14110 | 14105 | 90.820 | 68.896 | 68.872 | 0.024 | 41.5 |
| 31 | 14144 | 14136 | 90.820 | 69.063 | 69.023 | 0.039 | 41.6 |
| 33 | 14178 | 14169 | 96.680 | 69.229 | 69.185 | 0.044 | 41.7 |
| 35 | 14212 | 14204 | 102.539 | 69.395 | 69.355 | 0.039 | 41.8 |
| 37 | 14246 | 14241 | 108.398 | 69.561 | 69.536 | 0.024 | 41.9 |
| 38 | 14280 | 14279 | 111.328 | 69.727 | 69.722 | 0.005 | 42.0 |
| 37 | 14314 | 14316 | 108.398 | 69.893 | 69.902 | -0.010 | 42.1 |
| 37 | 14348 | 14353 | 108.398 | 70.059 | 70.083 | -0.024 | 42.2 |
| 37 | 14382 | 14390 | 108.398 | 70.225 | 70.264 | -0.039 | 42.3 |
| 35 | 14416 | 14425 | 102.539 | 70.391 | 70.435 | -0.044 | 42.4 |
| 35 | 14450 | 14460 | 102.539 | 70.557 | 70.605 | -0.049 | 42.5 |
| 33 | 14484 | 14493 | 96.680 | 70.723 | 70.767 | -0.044 | 42.6 |
| 30 | 14518 | 14523 | 87.891 | 70.889 | 70.913 | -0.024 | 42.7 |
| 29 | 14552 | 14552 | 84.961 | 71.055 | 71.055 | 0.000 | 42.8 |
| 29 | 14586 | 14581 | 84.961 | 71.221 | 71.196 | 0.024 | 42.9 |
| 30 | 14620 | 14611 | 87.891 | 71.387 | 71.343 | 0.044 | 43.0 |
| 31 | 14654 | 14642 | 90.820 | 71.553 | 71.494 | 0.059 | 43.1 |
| 34 | 14688 | 14676 | 99.609 | 71.719 | 71.660 | 0.059 | 43.2 |
| 36 | 14722 | 14712 | 105.469 | 71.885 | 71.836 | 0.049 | 43.3 |
| 37 | 14756 | 14749 | 108.398 | 72.051 | 72.017 | 0.034 | 43.4 |
| 38 | 14790 | 14787 | 111.328 | 72.217 | 72.202 | 0.015 | 43.5 |
| 38 | 14824 | 14825 | 111.328 | 72.383 | 72.388 | -0.005 | 43.6 |
| 38 | 14858 | 14863 | 111.328 | 72.549 | 72.573 | -0.024 | 43.7 |
| 37 | 14892 | 14900 | 108.398 | 72.715 | 72.754 | -0.039 | 43.8 |
| 36 | 14926 | 14936 | 105.469 | 72.881 | 72.930 | -0.049 | 43.9 |
| 37 | 14960 | 14973 | 108.398 | 73.047 | 73.110 | -0.063 | 44.0 |
| 32 | 14994 | 15005 | 93.750 | 73.213 | 73.267 | -0.054 | 44.1 |
| 29 | 15028 | 15034 | 84.961 | 73.379 | 73.408 | -0.029 | 44.2 |
| 29 | 15062 | 15063 | 84.961 | 73.545 | 73.550 | -0.005 | 44.3 |
| 28 | 15096 | 15091 | 82.031 | 73.711 | 73.687 | 0.024 | 44.4 |
| 30 | 15130 | 15121 | 87.891 | 73.877 | 73.833 | 0.044 | 44.5 |
| 32 | 15164 | 15153 | 93.750 | 74.043 | 73.989 | 0.054 | 44.6 |
| 34 | 15198 | 15187 | 99.609 | 74.209 | 74.155 | 0.054 | 44.7 |
| 37 | 15232 | 15224 | 108.398 | 74.375 | 74.336 | 0.039 | 44.8 |
| 38 | 15266 | 15262 | 111.328 | 74.541 | 74.521 | 0.020 | 44.9 |
| 37 | 15300 | 15299 | 108.398 | 74.707 | 74.702 | 0.005 | 45.0 |
| 38 | 15334 | 15337 | 111.328 | 74.873 | 74.888 | -0.015 | 45.1 |
| 37 | 15368 | 15374 | 108.398 | 75.039 | 75.068 | -0.029 | 45.2 |
| 37 | 15402 | 15411 | 108.398 | 75.205 | 75.249 | -0.044 | 45.3 |
| 36 | 15436 | 15447 | 105.469 | 75.371 | 75.425 | -0.054 | 45.4 |
| 34 | 15470 | 15481 | 99.609 | 75.537 | 75.591 | -0.054 | 45.5 |


| 31 | 15504 | 15512 | 90.820 | 75.703 | 75.742 | -0.039 | 45.6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 30 | 15538 | 15542 | 87.891 | 75.869 | 75.889 | -0.020 | 45.7 |
| 28 | 15572 | 15570 | 82.031 | 76.035 | 76.025 | 0.010 | 45.8 |
| 29 | 15606 | 15599 | 84.961 | 76.201 | 76.167 | 0.034 | 45.9 |
| 31 | 15640 | 15630 | 90.820 | 76.367 | 76.318 | 0.049 | 46.0 |
| 32 | 15674 | 15662 | 93.750 | 76.533 | 76.475 | 0.059 | 46.1 |
| 36 | 15708 | 15698 | 105.469 | 76.699 | 76.650 | 0.049 | 46.2 |
| 37 | 15742 | 15735 | 108.398 | 76.865 | 76.831 | 0.034 | 46.3 |
| 38 | 15776 | 15773 | 111.328 | 77.031 | 77.017 | 0.015 | 46.4 |
| 38 | 15810 | 15811 | 111.328 | 77.197 | 77.202 | -0.005 | 46.5 |
| 39 | 15844 | 15850 | 114.258 | 77.363 | 77.393 | -0.029 | 46.6 |
| 37 | 15878 | 15887 | 108.398 | 77.529 | 77.573 | -0.044 | 46.7 |
| 37 | 15912 | 15924 | 108.398 | 77.695 | 77.754 | -0.059 | 46.8 |
| 35 | 15946 | 15959 | 102.539 | 77.861 | 77.925 | -0.063 | 46.9 |
| 33 | 15980 | 15992 | 96.680 | 78.027 | 78.086 | -0.059 | 47.0 |
| 30 | 16014 | 16022 | 87.891 | 78.193 | 78.232 | -0.039 | 47.1 |
| 29 | 16048 | 16051 | 84.961 | 78.359 | 78.374 | -0.015 | 47.2 |
| 28 | 16082 | 16079 | 82.031 | 78.525 | 78.511 | 0.015 | 47.3 |
| 29 | 16116 | 16108 | 84.961 | 78.691 | 78.652 | 0.039 | 47.4 |
| 32 | 16150 | 16140 | 93.750 | 78.857 | 78.809 | 0.049 | 47.5 |
| 33 | 16184 | 16173 | 96.680 | 79.023 | 78.970 | 0.054 | 47.6 |
| 35 | 16218 | 16208 | 102.539 | 79.189 | 79.141 | 0.049 | 47.7 |
| 38 | 16252 | 16246 | 111.328 | 79.355 | 79.326 | 0.029 | 47.8 |
| 38 | 16286 | 16284 | 111.328 | 79.521 | 79.512 | 0.010 | 47.9 |
| 37 | 16320 | 16321 | 108.398 | 79.688 | 79.692 | -0.005 | 48.0 |
| 38 | 16354 | 16359 | 111.328 | 79.854 | 79.878 | -0.024 | 48.1 |
| 37 | 16388 | 16396 | 108.398 | 80.020 | 80.059 | -0.039 | 48.2 |
| 36 | 16422 | 16432 | 105.469 | 80.186 | 80.234 | -0.049 | 48.3 |
| 35 | 16456 | 16467 | 102.539 | 80.352 | 80.405 | -0.054 | 48.4 |
| 33 | 16490 | 16500 | 96.680 | 80.518 | 80.566 | -0.049 | 48.5 |
| 30 | 16524 | 16530 | 87.891 | 80.684 | 80.713 | -0.029 | 48.6 |
| 29 | 16558 | 16559 | 84.961 | 80.850 | 80.854 | -0.005 | 48.7 |
| 28 | 16592 | 16587 | 82.031 | 81.016 | 80.991 | 0.024 | 48.8 |
| 30 | 16626 | 16617 | 87.891 | 81.182 | 81.138 | 0.044 | 48.9 |
| 31 | 16660 | 16648 | 90.820 | 81.348 | 81.289 | 0.059 | 49.0 |
| 34 | 16694 | 16682 | 99.609 | 81.514 | 81.455 | 0.059 | 49.1 |
| 36 | 16728 | 16718 | 105.469 | 81.680 | 81.631 | 0.049 | 49.2 |
| 37 | 16762 | 16755 | 108.398 | 81.846 | 81.812 | 0.034 | 49.3 |
| 38 | 16796 | 16793 | 111.328 | 82.012 | 81.997 | 0.015 | 49.4 |
| 38 | 16830 | 16831 | 111.328 | 82.178 | 82.183 | -0.005 | 49.5 |
| 38 | 16864 | 16869 | 111.328 | 82.344 | 82.368 | -0.024 | 49.6 |
| 37 | 16898 | 16906 | 108.398 | 82.510 | 82.549 | -0.039 | 49.7 |
| 36 | 16932 | 16942 | 105.469 | 82.676 | 82.725 | -0.049 | 49.8 |
| 35 | 16966 | 16977 | 102.539 | 82.842 | 82.896 | -0.054 | 49.9 |
| 32 | 17000 | 17009 | 93.750 | 83.008 | 83.052 | -0.044 | 50.0 |
| 30 | 17034 | 17039 | 87.891 | 83.174 | 83.198 | -0.024 | 50.1 |
| 28 | 17068 | 17067 | 82.031 | 83.340 | 83.335 | 0.005 | 50.2 |
| 29 | 17102 | 17096 | 84.961 | 83.506 | 83.477 | 0.029 | 50.3 |
| 31 | 17136 | 17127 | 90.820 | 83.672 | 83.628 | 0.044 | 50.4 |
| 32 | 17170 | 17159 | 93.750 | 83.838 | 83.784 | 0.054 | 50.5 |
| 35 | 17204 | 17194 | 102.539 | 84.004 | 83.955 | 0.049 | 50.6 |
| 37 | 17238 | 17231 | 108.398 | 84.170 | 84.136 | 0.034 | 50.7 |
| 38 | 17272 | 17269 | 111.328 | 84.336 | 84.321 | 0.015 | 50.8 |


| 38 | 17306 | 17307 | 111.328 | 84.502 | 84.507 | -0.005 | 50.9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 38 | 17340 | 17345 | 111.328 | 84.668 | 84.692 | -0.024 | 51.0 |
| 37 | 17374 | 17382 | 108.398 | 84.834 | 84.873 | -0.039 | 51.1 |
| 37 | 17408 | 17419 | 108.398 | 85.000 | 85.054 | -0.054 | 51.2 |
| 35 | 17442 | 17454 | 102.539 | 85.166 | 85.225 | -0.059 | 51.3 |
| 34 | 17476 | 17488 | 99.609 | 85.332 | 85.391 | -0.059 | 51.4 |
| 31 | 17510 | 17519 | 90.820 | 85.498 | 85.542 | -0.044 | 51.5 |
| 28 | 17544 | 17547 | 82.031 | 85.664 | 85.679 | -0.015 | 51.6 |
| 27 | 17578 | 17574 | 79.102 | 85.830 | 85.811 | 0.020 | 51.7 |
| 29 | 17612 | 17603 | 84.961 | 85.996 | 85.952 | 0.044 | 51.8 |
| 30 | 17646 | 17633 | 87.891 | 86.162 | 86.099 | 0.063 | 51.9 |
| 33 | 17680 | 17666 | 96.680 | 86.328 | 86.260 | 0.068 | 52.0 |
| 35 | 17714 | 17701 | 102.539 | 86.494 | 86.431 | 0.063 | 52.1 |
| 38 | 17748 | 17739 | 111.328 | 86.660 | 86.616 | 0.044 | 52.2 |
| 38 | 17782 | 17777 | 111.328 | 86.826 | 86.802 | 0.024 | 52.3 |
| 38 | 17816 | 17815 | 111.328 | 86.992 | 86.987 | 0.005 | 52.4 |
| 38 | 17850 | 17853 | 111.328 | 87.158 | 87.173 | -0.015 | 52.5 |
| 38 | 17884 | 17891 | 111.328 | 87.324 | 87.358 | -0.034 | 52.6 |
| 36 | 17918 | 17927 | 105.469 | 87.490 | 87.534 | -0.044 | 52.7 |
| 36 | 17952 | 17963 | 105.469 | 87.656 | 87.710 | -0.054 | 52.8 |
| 33 | 17986 | 17996 | 96.680 | 87.822 | 87.871 | -0.049 | 52.9 |
| 31 | 18020 | 18027 | 90.820 | 87.988 | 88.022 | -0.034 | 53.0 |
| 29 | 18054 | 18056 | 84.961 | 88.154 | 88.164 | -0.010 | 53.1 |
| 28 | 18088 | 18084 | 82.031 | 88.320 | 88.301 | 0.020 | 53.2 |
| 29 | 18122 | 18113 | 84.961 | 88.486 | 88.442 | 0.044 | 53.3 |
| 31 | 18156 | 18144 | 90.820 | 88.652 | 88.594 | 0.059 | 53.4 |
| 34 | 18190 | 18178 | 99.609 | 88.818 | 88.760 | 0.059 | 53.5 |
| 36 | 18224 | 18214 | 105.469 | 88.984 | 88.936 | 0.049 | 53.6 |
| 37 | 18258 | 18251 | 108.398 | 89.150 | 89.116 | 0.034 | 53.7 |
| 38 | 18292 | 18289 | 111.328 | 89.316 | 89.302 | 0.015 | 53.8 |
| 38 | 18326 | 18327 | 111.328 | 89.482 | 89.487 | -0.005 | 53.9 |
| 38 | 18360 | 18365 | 111.328 | 89.648 | 89.673 | -0.024 | 54.0 |
| 37 | 18394 | 18402 | 108.398 | 89.814 | 89.854 | -0.039 | 54.1 |
| 36 | 18428 | 18438 | 105.469 | 89.980 | 90.029 | -0.049 | 54.2 |
| 36 | 18462 | 18474 | 105.469 | 90.146 | 90.205 | -0.059 | 54.3 |
| 32 | 18496 | 18506 | 93.750 | 90.313 | 90.361 | -0.049 | 54.4 |
| 29 | 18530 | 18535 | 84.961 | 90.479 | 90.503 | -0.024 | 54.5 |
| 28 | 18564 | 18563 | 82.031 | 90.645 | 90.640 | 0.005 | 54.6 |
| 29 | 18598 | 18592 | 84.961 | 90.811 | 90.781 | 0.029 | 54.7 |
| 30 | 18632 | 18622 | 87.891 | 90.977 | 90.928 | 0.049 | 54.8 |
| 33 | 18666 | 18655 | 96.680 | 91.143 | 91.089 | 0.054 | 54.9 |
| 34 | 18700 | 18689 | 99.609 | 91.309 | 91.255 | 0.054 | 55.0 |
| 37 | 18734 | 18726 | 108.398 | 91.475 | 91.436 | 0.039 | 55.1 |
| 38 | 18768 | 18764 | 111.328 | 91.641 | 91.621 | 0.020 | 55.2 |
| 37 | 18802 | 18801 | 108.398 | 91.807 | 91.802 | 0.005 | 55.3 |
| 38 | 18836 | 18839 | 111.328 | 91.973 | 91.987 | -0.015 | 55.4 |
| 38 | 18870 | 18877 | 111.328 | 92.139 | 92.173 | -0.034 | 55.5 |
| 37 | 18904 | 18914 | 108.398 | 92.305 | 92.354 | -0.049 | 55.6 |
| 36 | 18938 | 18950 | 105.469 | 92.471 | 92.529 | -0.059 | 55.7 |
| 34 | 18972 | 18984 | 99.609 | 92.637 | 92.695 | -0.059 | 55.8 |
| 31 | 19006 | 19015 | 90.820 | 92.803 | 92.847 | -0.044 | 55.9 |
| 28 | 19040 | 19043 | 82.031 | 92.969 | 92.983 | -0.015 | 56.0 |
| 27 | 19074 | 19070 | 79.102 | 93.135 | 93.115 | 0.020 | 56.1 |


| 29 | 19108 | 19099 | 84.961 | 93.301 | 93.257 | 0.044 | 56.2 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 30 | 19142 | 19129 | 87.891 | 93.467 | 93.403 | 0.063 | 56.3 |
| 33 | 19176 | 19162 | 96.680 | 93.633 | 93.564 | 0.068 | 56.4 |
| 35 | 19210 | 19197 | 102.539 | 93.799 | 93.735 | 0.063 | 56.5 |
| 38 | 19244 | 19235 | 111.328 | 93.965 | 93.921 | 0.044 | 56.6 |
| 38 | 19278 | 19273 | 111.328 | 94.131 | 94.106 | 0.024 | 56.7 |
| 38 | 19312 | 19311 | 111.328 | 94.297 | 94.292 | 0.005 | 56.8 |
| 38 | 19346 | 19349 | 111.328 | 94.463 | 94.478 | -0.015 | 56.9 |
| 37 | 19380 | 19386 | 108.398 | 94.629 | 94.658 | -0.029 | 57.0 |
| 37 | 19414 | 19423 | 108.398 | 94.795 | 94.839 | -0.044 | 57.1 |
| 35 | 19448 | 19458 | 102.539 | 94.961 | 95.010 | -0.049 | 57.2 |
| 34 | 19482 | 19492 | 99.609 | 95.127 | 95.176 | -0.049 | 57.3 |
| 31 | 19516 | 19523 | 90.820 | 95.293 | 95.327 | -0.034 | 57.4 |
| 28 | 19550 | 19551 | 82.031 | 95.459 | 95.464 | -0.005 | 57.5 |
| 28 | 19584 | 19579 | 82.031 | 95.625 | 95.601 | 0.024 | 57.6 |
| 30 | 19618 | 19609 | 87.891 | 95.791 | 95.747 | 0.044 | 57.7 |
| 31 | 19652 | 19640 | 90.820 | 95.957 | 95.898 | 0.059 | 57.8 |
| 33 | 19686 | 19673 | 96.680 | 96.123 | 96.060 | 0.063 | 57.9 |
| 36 | 19720 | 19709 | 105.469 | 96.289 | 96.235 | 0.054 | 58.0 |
| 37 | 19754 | 19746 | 108.398 | 96.455 | 96.416 | 0.039 | 58.1 |
| 38 | 19788 | 19784 | 111.328 | 96.621 | 96.602 | 0.020 | 58.2 |
| 38 | 19822 | 19822 | 111.328 | 96.787 | 96.787 | 0.000 | 58.3 |
| 39 | 19856 | 19861 | 114.258 | 96.953 | 96.978 | -0.024 | 58.4 |
| 37 | 19890 | 19898 | 108.398 | 97.119 | 97.158 | -0.039 | 58.5 |
| 37 | 19924 | 19935 | 108.398 | 97.285 | 97.339 | -0.054 | 58.6 |
| 35 | 19958 | 19970 | 102.539 | 97.451 | 97.510 | -0.059 | 58.7 |
| 33 | 19992 | 20003 | 96.680 | 97.617 | 97.671 | -0.054 | 58.8 |
| 30 | 20026 | 20033 | 87.891 | 97.783 | 97.817 | -0.034 | 58.9 |
| 28 | 20060 | 20061 | 82.031 | 97.949 | 97.954 | -0.005 | 59.0 |
| 29 | 20094 | 20090 | 84.961 | 98.115 | 98.096 | 0.020 | 59.1 |
| 30 | 20128 | 20120 | 87.891 | 98.281 | 98.242 | 0.039 | 59.2 |
| 31 | 20162 | 20151 | 90.820 | 98.447 | 98.394 | 0.054 | 59.3 |
| 35 | 20196 | 20186 | 102.539 | 98.613 | 98.564 | 0.049 | 59.4 |
| 36 | 20230 | 20222 | 105.469 | 98.779 | 98.740 | 0.039 | 59.5 |
| 38 | 20264 | 20260 | 111.328 | 98.945 | 98.926 | 0.020 | 59.6 |
| 37 | 20298 | 20297 | 108.398 | 99.111 | 99.106 | 0.005 | 59.7 |
| 39 | 20332 | 20336 | 114.258 | 99.277 | 99.297 | -0.020 | 59.8 |
| 36 | 20340 | 20372 | 105.469 | 99.316 | 99.473 | -0.156 | 59.9 |
| 33 | 20348 | 20405 | 96.680 | 99.355 | 99.634 | -0.278 | 60.0 |
| 24 | 20356 | 20429 | 70.313 | 99.395 | 99.751 | -0.356 | 60.1 |
| 17 | 20364 | 20446 | 49.805 | 99.434 | 99.834 | -0.400 | 60.2 |
| 11 | 20372 | 20457 | 32.227 | 99.473 | 99.888 | -0.415 | 60.3 |
| 5 | 20380 | 20462 | 14.648 | 99.512 | 99.912 | -0.400 | 60.4 |
| 0 | 20388 | 20462 | 0.000 | 99.551 | 99.912 | -0.361 | 60.5 |
| 0 | 20396 | 20462 | 0.000 | 99.590 | 99.912 | -0.322 | 60.6 |
| 1 | 20404 | 20463 | 2.930 | 99.629 | 99.917 | -0.288 | 60.7 |
| 0 | 20412 | 20463 | 0.000 | 99.668 | 99.917 | -0.249 | 60.8 |
| 0 | 20420 | 20463 | 0.000 | 99.707 | 99.917 | -0.210 | 60.9 |
| 1 | 20428 | 20464 | 2.930 | 99.746 | 99.922 | -0.176 | 61.0 |
| 1 | 20436 | 20465 | 2.930 | 99.785 | 99.927 | -0.142 | 61.1 |
| 1 | 20444 | 20466 | 2.930 | 99.824 | 99.932 | -0.107 | 61.2 |
| 1 | 20452 | 20467 | 2.930 | 99.863 | 99.937 | -0.073 | 61.3 |
| 3 | 20460 | 20470 | 8.789 | 99.902 | 99.951 | -0.049 | 61.4 |


| 2 | 20468 | 20472 | 5.859 | 99.941 | 99.961 | -0.020 | 61.5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 4 | 20476 | 20476 | 11.719 | 99.980 | 99.980 | 0.000 | 61.6 |
| 4 | 20480 | 20480 | 11.719 | 100.000 | 100.000 | 0.000 | 61.7 |
| 3 | 20480 | 20483 | 8.789 | 100.000 | 100.015 | -0.015 | 61.8 |
| 0 | 20480 | 20483 | 0.000 | 100.000 | 100.015 | -0.015 | 61.9 |

## Performance Test on Rotary Table Module (Figures 9.4-6)

Interpolation performed on the rotary table module for a $360^{\circ}$ rotation at a speed of $0.75 \mathrm{rev} / \mathrm{min}$. The following data was used in the preparation of Figures 9.4-6.

Table F.6.2: Test Data, Performance Test on Rotary Table Module

| Speed (pulses/s) | Ref Position (pulses) | Measured Position (pulses) | $\begin{gathered} \text { Speed } \\ (\mathrm{rev} / \mathrm{min}) \end{gathered}$ |  | Measured Position (deg) | Error (deg) | Time <br> (s) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | 0.000 | 0.000 | 0.000 | 0.000 | 0.0 |
| 3 | 34 | 3 | 0.063 | 0.427 | 0.038 | 0.389 | 0.1 |
| 14 | 68 | 17 | 0.293 | 0.854 | 0.213 | 0.640 | 0.2 |
| 27 | 102 | 44 | 0.565 | 1.281 | 0.552 | 0.728 | 0.3 |
| 35 | 136 | 79 | 0.732 | 1.708 | 0.992 | 0.716 | 0.4 |
| 39 | 170 | 118 | 0.816 | 2.134 | 1.482 | 0.653 | 0.5 |
| 42 | 204 | 160 | 0.879 | 2.561 | 2.009 | 0.552 | 0.6 |
| 41 | 238 | 201 | 0.858 | 2.988 | 2.524 | 0.465 | 0.7 |
| 41 | 272 | 242 | 0.858 | 3.415 | 3.039 | 0.377 | 0.8 |
| 41 | 306 | 283 | 0.858 | 3.842 | 3.553 | 0.289 | 0.9 |
| 39 | 340 | 322 | 0.816 | 4.269 | 4.043 | 0.226 | 1.0 |
| 39 | 374 | 361 | 0.816 | 4.696 | 4.533 | 0.163 | 1.1 |
| 35 | 408 | 396 | 0.732 | 5.123 | 4.972 | 0.151 | 1.2 |
| 35 | 442 | 431 | 0.732 | 5.550 | 5.412 | 0.138 | 1.3 |
| 32 | 476 | 463 | 0.670 | 5.977 | 5.813 | 0.163 | 1.4 |
| 31 | 510 | 494 | 0.649 | 6.403 | 6.203 | 0.201 | 1.5 |
| 31 | 544 | 525 | 0.649 | 6.830 | 6.592 | 0.239 | 1.6 |
| 33 | 578 | 558 | 0.691 | 7.257 | 7.006 | 0.251 | 1.7 |
| 33 | 612 | 591 | 0.691 | 7.684 | 7.420 | 0.264 | 1.8 |
| 34 | 646 | 625 | 0.711 | 8.111 | 7.847 | 0.264 | 1.9 |
| 36 | 680 | 661 | 0.753 | 8.538 | 8.299 | 0.239 | 2.0 |
| 35 | 714 | 696 | 0.732 | 8.965 | 8.739 | 0.226 | 2.1 |
| 36 | 748 | 732 | 0.753 | 9.392 | 9.191 | 0.201 | 2.2 |
| 36 | 782 | 768 | 0.753 | 9.819 | 9.643 | 0.176 | 2.3 |
| 37 | 816 | 805 | 0.774 | 10.246 | 10.107 | 0.138 | 2.4 |
| 37 | 850 | 842 | 0.774 | 10.672 | 10.572 | 0.100 | 2.5 |
| 36 | 884 | 878 | 0.753 | 11.099 | 11.024 | 0.075 | 2.6 |
| 34 | 918 | 912 | 0.711 | 11.526 | 11.451 | 0.075 | 2.7 |
| 34 | 952 | 946 | 0.711 | 11.953 | 11.878 | 0.075 | 2.8 |
| 32 | 986 | 978 | 0.670 | 12.380 | 12.280 | 0.100 | 2.9 |
| 33 | 1020 | 1011 | 0.691 | 12.807 | 12.694 | 0.113 | 3.0 |
| 32 | 1054 | 1043 | 0.670 | 13.234 | 13.096 | 0.138 | 3.1 |
| 33 | 1088 | 1076 | 0.691 | 13.661 | 13.510 | 0.151 | 3.2 |
| 34 | 1122 | 1110 | 0.711 | 14.088 | 13.937 | 0.151 | 3.3 |
| 34 | 1156 | 1144 | 0.711 | 14.515 | 14.364 | 0.151 | 3.4 |
| 35 | 1190 | 1179 | 0.732 | 14.941 | 14.803 | 0.138 | 3.5 |
| 35 | 1224 | 1214 | 0.732 | 15.368 | 15.243 | 0.126 | 3.6 |
| 35 | 1258 | 1249 | 0.732 | 15.795 | 15.682 | 0.113 | 3.7 |
| 37 | 1292 | 1286 | 0.774 | 16.222 | 16.147 | 0.075 | 3.8 |
| 36 | 1326 | 1322 | 0.753 | 16.649 | 16.599 | 0.050 | 3.9 |
| 36 | 1360 | 1358 | 0.753 | 17.076 | 17.051 | 0.025 | 4.0 |
| 35 | 1394 | 1393 | 0.732 | 17.503 | 17.490 | 0.013 | 4.1 |
| 33 | 1428 | 1426 | 0.691 | 17.930 | 17.905 | 0.025 | 4.2 |


| 33 | 1462 | 1459 | 0.691 | 18.357 | 18.319 | 0.038 | 4.3 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 32 | 1496 | 1491 | 0.670 | 18.783 | 18.721 | 0.063 | 4.4 |
| 33 | 1530 | 1524 | 0.691 | 19.210 | 19.135 | 0.075 | 4.5 |
| 33 | 1564 | 1557 | 0.691 | 19.637 | 19.549 | 0.088 | 4.6 |
| 32 | 1598 | 1589 | 0.670 | 20.064 | 19.951 | 0.113 | 4.7 |
| 35 | 1632 | 1624 | 0.732 | 20.491 | 20.391 | 0.100 | 4.8 |
| 34 | 1666 | 1658 | 0.711 | 20.918 | 20.818 | 0.100 | 4.9 |
| 35 | 1700 | 1693 | 0.732 | 21.345 | 21.257 | 0.088 | 5.0 |
| 35 | 1734 | 1728 | 0.732 | 21.772 | 21.696 | 0.075 | 5.1 |
| 37 | 1768 | 1765 | 0.774 | 22.199 | 22.161 | 0.038 | 5.2 |
| 36 | 1802 | 1801 | 0.753 | 22.626 | 22.613 | 0.013 | 5.3 |
| 37 | 1836 | 1838 | 0.774 | 23.052 | 23.078 | -0.025 | 5.4 |
| 37 | 1870 | 1875 | 0.774 | 23.479 | 23.542 | -0.063 | 5.5 |
| 34 | 1904 | 1909 | 0.711 | 23.906 | 23.969 | -0.063 | 5.6 |
| 32 | 1938 | 1941 | 0.670 | 24.333 | 24.371 | -0.038 | 5.7 |
| 30 | 1972 | 1971 | 0.628 | 24.760 | 24.747 | 0.013 | 5.8 |
| 31 | 2006 | 2002 | 0.649 | 25.187 | 25.137 | 0.050 | 5.9 |
| 31 | 2040 | 2033 | 0.649 | 25.614 | 25.526 | 0.088 | 6.0 |
| 33 | 2074 | 2066 | 0.691 | 26.041 | 25.940 | 0.100 | 6.1 |
| 33 | 2108 | 2099 | 0.691 | 26.468 | 26.355 | 0.113 | 6.2 |
| 35 | 2142 | 2134 | 0.732 | 26.895 | 26.794 | 0.100 | 6.3 |
| 35 | 2176 | 2169 | 0.732 | 27.321 | 27.234 | 0.088 | 6.4 |
| 36 | 2210 | 2205 | 0.753 | 27.748 | 27.686 | 0.063 | 6.5 |
| 36 | 2244 | 2241 | 0.753 | 28.175 | 28.138 | 0.038 | 6.6 |
| 36 | 2278 | 2277 | 0.753 | 28.602 | 28.590 | 0.013 | 6.7 |
| 36 | 2312 | 2313 | 0.753 | 29.029 | 29.042 | -0.013 | 6.8 |
| 37 | 2346 | 2350 | 0.774 | 29.456 | 29.506 | -0.050 | 6.9 |
| 35 | 2380 | 2385 | 0.732 | 29.883 | 29.946 | -0.063 | 7.0 |
| 34 | 2414 | 2419 | 0.711 | 30.310 | 30.372 | -0.063 | 7.1 |
| 32 | 2448 | 2451 | 0.670 | 30.737 | 30.774 | -0.038 | 7.2 |
| 31 | 2482 | 2482 | 0.649 | 31.164 | 31.164 | 0.000 | 7.3 |
| 32 | 2516 | 2514 | 0.670 | 31.590 | 31.565 | 0.025 | 7.4 |
| 32 | 2550 | 2546 | 0.670 | 32.017 | 31.967 | 0.050 | 7.5 |
| 33 | 2584 | 2579 | 0.691 | 32.444 | 32.381 | 0.063 | 7.6 |
| 34 | 2618 | 2613 | 0.711 | 32.871 | 32.808 | 0.063 | 7.7 |
| 34 | 2652 | 2647 | 0.711 | 33.298 | 33.235 | 0.063 | 7.8 |
| 35 | 2686 | 2682 | 0.732 | 33.725 | 33.675 | 0.050 | 7.9 |
| 35 | 2720 | 2717 | 0.732 | 34.152 | 34.114 | 0.038 | 8.0 |
| 36 | 2754 | 2753 | 0.753 | 34.579 | 34.566 | 0.013 | 8.1 |
| 36 | 2788 | 2789 | 0.753 | 35.006 | 35.018 | -0.013 | 8.2 |
| 35 | 2822 | 2824 | 0.732 | 35.432 | 35.458 | -0.025 | 8.3 |
| 36 | 2856 | 2860 | 0.753 | 35.859 | 35.910 | -0.050 | 8.4 |
| 34 | 2890 | 2894 | 0.711 | 36.286 | 36.336 | -0.050 | 8.5 |
| 33 | 2924 | 2927 | 0.691 | 36.713 | 36.751 | -0.038 | 8.6 |
| 33 | 2958 | 2960 | 0.691 | 37.140 | 37.165 | -0.025 | 8.7 |
| 32 | 2992 | 2992 | 0.670 | 37.567 | 37.567 | 0.000 | 8.8 |
| 33 | 3026 | 3025 | 0.691 | 37.994 | 37.981 | 0.013 | 8.9 |
| 32 | 3060 | 3057 | 0.670 | 38.421 | 38.383 | 0.038 | 9.0 |
| 33 | 3094 | 3090 | 0.691 | 38.848 | 38.797 | 0.050 | 9.1 |
| 34 | 3128 | 3124 | 0.711 | 39.275 | 39.224 | 0.050 | 9.2 |
| 34 | 3162 | 3158 | 0.711 | 39.701 | 39.651 | 0.050 | 9.3 |
| 35 | 3196 | 3193 | 0.732 | 40.128 | 40.091 | 0.038 | 9.4 |
| 35 | 3230 | 3228 | 0.732 | 40.555 | 40.530 | 0.025 | 9.5 |


| 35 | 3264 | 3263 | 0.732 | 40.982 | 40.970 | 0.013 | 9.6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 36 | 3298 | 3299 | 0.753 | 41.409 | 41.422 | -0.013 | 9.7 |
| 36 | 3332 | 3335 | 0.753 | 41.836 | 41.874 | -0.038 | 9.8 |
| 35 | 3366 | 3370 | 0.732 | 42.263 | 42.313 | -0.050 | 9.9 |
| 35 | 3400 | 3405 | 0.732 | 42.690 | 42.753 | -0.063 | 10.0 |
| 33 | 3434 | 3438 | 0.691 | 43.117 | 43.167 | -0.050 | 10.1 |
| 32 | 3468 | 3470 | 0.670 | 43.544 | 43.569 | -0.025 | 10.2 |
| 32 | 3502 | 3502 | 0.670 | 43.970 | 43.970 | 0.000 | 10.3 |
| 32 | 3536 | 3534 | 0.670 | 44.397 | 44.372 | 0.025 | 10.4 |
| 32 | 3570 | 3566 | 0.670 | 44.824 | 44.774 | 0.050 | 10.5 |
| 34 | 3604 | 3600 | 0.711 | 45.251 | 45.201 | 0.050 | 10.6 |
| 34 | 3638 | 3634 | 0.711 | 45.678 | 45.628 | 0.050 | 10.7 |
| 35 | 3672 | 3669 | 0.732 | 46.105 | 46.067 | 0.038 | 10.8 |
| 34 | 3706 | 3703 | 0.711 | 46.532 | 46.494 | 0.038 | 10.9 |
| 35 | 3740 | 3738 | 0.732 | 46.959 | 46.934 | 0.025 | 11.0 |
| 36 | 3774 | 3774 | 0.753 | 47.386 | 47.386 | 0.000 | 11.1 |
| 35 | 3808 | 3809 | 0.732 | 47.813 | 47.825 | -0.013 | 11.2 |
| 36 | 3842 | 3845 | 0.753 | 48.239 | 48.277 | -0.038 | 11.3 |
| 36 | 3876 | 3881 | 0.753 | 48.666 | 48.729 | -0.063 | 11.4 |
| 34 | 3910 | 3915 | 0.711 | 49.093 | 49.156 | -0.063 | 11.5 |
| 33 | 3944 | 3948 | 0.691 | 49.520 | 49.570 | -0.050 | 11.6 |
| 32 | 3978 | 3980 | 0.670 | 49.947 | 49.972 | -0.025 | 11.7 |
| 32 | 4012 | 4012 | 0.670 | 50.374 | 50.374 | 0.000 | 11.8 |
| 32 | 4046 | 4044 | 0.670 | 50.801 | 50.776 | 0.025 | 11.9 |
| 32 | 4080 | 4076 | 0.670 | 51.228 | 51.177 | 0.050 | 12.0 |
| 34 | 4114 | 4110 | 0.711 | 51.655 | 51.604 | 0.050 | 12.1 |
| 34 | 4148 | 4144 | 0.711 | 52.081 | 52.031 | 0.050 | 12.2 |
| 35 | 4182 | 4179 | 0.732 | 52.508 | 52.471 | 0.038 | 12.3 |
| 35 | 4216 | 4214 | 0.732 | 52.935 | 52.910 | 0.025 | 12.4 |
| 35 | 4250 | 4249 | 0.732 | 53.362 | 53.350 | 0.013 | 12.5 |
| 36 | 4284 | 4285 | 0.753 | 53.789 | 53.802 | -0.013 | 12.6 |
| 36 | 4318 | 4321 | 0.753 | 54.216 | 54.254 | -0.038 | 12.7 |
| 36 | 4352 | 4357 | 0.753 | 54.643 | 54.706 | -0.063 | 12.8 |
| 34 | 4386 | 4391 | 0.711 | 55.070 | 55.133 | -0.063 | 12.9 |
| 34 | 4420 | 4425 | 0.711 | 55.497 | 55.559 | -0.063 | 13.0 |
| 33 | 4454 | 4458 | 0.691 | 55.924 | 55.974 | -0.050 | 13.1 |
| 31 | 4488 | 4489 | 0.649 | 56.350 | 56.363 | -0.013 | 13.2 |
| 32 | 4522 | 4521 | 0.670 | 56.777 | 56.765 | 0.013 | 13.3 |
| 33 | 4556 | 4554 | 0.691 | 57.204 | 57.179 | 0.025 | 13.4 |
| 32 | 4590 | 4586 | 0.670 | 57.631 | 57.581 | 0.050 | 13.5 |
| 33 | 4624 | 4619 | 0.691 | 58.058 | 57.995 | 0.063 | 13.6 |
| 35 | 4658 | 4654 | 0.732 | 58.485 | 58.435 | 0.050 | 13.7 |
| 35 | 4692 | 4689 | 0.732 | 58.912 | 58.874 | 0.038 | 13.8 |
| 35 | 4726 | 4724 | 0.732 | 59.339 | 59.314 | 0.025 | 13.9 |
| 35 | 4760 | 4759 | 0.732 | 59.766 | 59.753 | 0.013 | 14.0 |
| 36 | 4794 | 4795 | 0.753 | 60.193 | 60.205 | -0.013 | 14.1 |
| 36 | 4828 | 4831 | 0.753 | 60.619 | 60.657 | -0.038 | 14.2 |
| 36 | 4862 | 4867 | 0.753 | 61.046 | 61.109 | -0.063 | 14.3 |
| 34 | 4896 | 4901 | 0.711 | 61.473 | 61.536 | -0.063 | 14.4 |
| 33 | 4930 | 4934 | 0.691 | 61.900 | 61.950 | -0.050 | 14.5 |
| 33 | 4964 | 4967 | 0.691 | 62.327 | 62.365 | -0.038 | 14.6 |
| 32 | 4998 | 4999 | 0.670 | 62.754 | 62.766 | -0.013 | 14.7 |
| 32 | 5032 | 5031 | 0.670 | 63.181 | 63.168 | 0.013 | 14.8 |


| 32 | 5066 | 5063 | 0.670 | 63.608 | 63.570 | 0.038 | 14.9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 33 | 5100 | 5096 | 0.691 | 64.035 | 63.984 | 0.050 | 15.0 |
| 34 | 5134 | 5130 | 0.711 | 64.461 | 64.411 | 0.050 | 15.1 |
| 35 | 5168 | 5165 | 0.732 | 64.888 | 64.851 | 0.038 | 15.2 |
| 34 | 5202 | 5199 | 0.711 | 65.315 | 65.278 | 0.038 | 15.3 |
| 35 | 5236 | 5234 | 0.732 | 65.742 | 65.717 | 0.025 | 15.4 |
| 35 | 5270 | 5269 | 0.732 | 66.169 | 66.157 | 0.013 | 15.5 |
| 36 | 5304 | 5305 | 0.753 | 66.596 | 66.609 | -0.013 | 15.6 |
| 36 | 5338 | 5341 | 0.753 | 67.023 | 67.061 | -0.038 | 15.7 |
| 36 | 5372 | 5377 | 0.753 | 67.450 | 67.513 | -0.063 | 15.8 |
| 35 | 5406 | 5412 | 0.732 | 67.877 | 67.952 | -0.075 | 15.9 |
| 33 | 5440 | 5445 | 0.691 | 68.304 | 68.366 | -0.063 | 16.0 |
| 32 | 5474 | 5477 | 0.670 | 68.730 | 68.768 | -0.038 | 16.1 |
| 32 | 5508 | 5509 | 0.670 | 69.157 | 69.170 | -0.013 | 16.2 |
| 32 | 5542 | 5541 | 0.670 | 69.584 | 69.572 | 0.013 | 16.3 |
| 32 | 5576 | 5573 | 0.670 | 70.011 | 69.973 | 0.038 | 16.4 |
| 33 | 5610 | 5606 | 0.691 | 70.438 | 70.388 | 0.050 | 16.5 |
| 34 | 5644 | 5640 | 0.711 | 70.865 | 70.815 | 0.050 | 16.6 |
| 35 | 5678 | 5675 | 0.732 | 71.292 | 71.254 | 0.038 | 16.7 |
| 34 | 5712 | 5709 | 0.711 | 71.719 | 71.681 | 0.038 | 16.8 |
| 35 | 5746 | 5744 | 0.732 | 72.146 | 72.121 | 0.025 | 16.9 |
| 37 | 5780 | 5781 | 0.774 | 72.573 | 72.585 | -0.013 | 17.0 |
| 36 | 5814 | 5817 | 0.753 | 72.999 | 73.037 | -0.038 | 17.1 |
| 35 | 5848 | 5852 | 0.732 | 73.426 | 73.477 | -0.050 | 17.2 |
| 35 | 5882 | 5887 | 0.732 | 73.853 | 73.916 | -0.063 | 17.3 |
| 34 | 5916 | 5921 | 0.711 | 74.280 | 74.343 | -0.063 | 17.4 |
| 33 | 5950 | 5954 | 0.691 | 74.707 | 74.757 | -0.050 | 17.5 |
| 33 | 5984 | 5987 | 0.691 | 75.134 | 75.172 | -0.038 | 17.6 |
| 32 | 6018 | 6019 | 0.670 | 75.561 | 75.573 | -0.013 | 17.7 |
| 32 | 6052 | 6051 | 0.670 | 75.988 | 75.975 | 0.013 | 17.8 |
| 32 | 6086 | 6083 | 0.670 | 76.415 | 76.377 | 0.038 | 17.9 |
| 33 | 6120 | 6116 | 0.691 | 76.842 | 76.791 | 0.050 | 18.0 |
| 35 | 6154 | 6151 | 0.732 | 77.268 | 77.231 | 0.038 | 18.1 |
| 35 | 6188 | 6186 | 0.732 | 77.695 | 77.670 | 0.025 | 18.2 |
| 34 | 6222 | 6220 | 0.711 | 78.122 | 78.097 | 0.025 | 18.3 |
| 34 | 6256 | 6254 | 0.711 | 78.549 | 78.524 | 0.025 | 18.4 |
| 36 | 6290 | 6290 | 0.753 | 78.976 | 78.976 | 0.000 | 18.5 |
| 36 | 6324 | 6326 | 0.753 | 79.403 | 79.428 | -0.025 | 18.6 |
| 36 | 6358 | 6362 | 0.753 | 79.830 | 79.880 | -0.050 | 18.7 |
| 34 | 6392 | 6396 | 0.711 | 80.257 | 80.307 | -0.050 | 18.8 |
| 35 | 6426 | 6431 | 0.732 | 80.684 | 80.746 | -0.063 | 18.9 |
| 33 | 6460 | 6464 | 0.691 | 81.110 | 81.161 | -0.050 | 19.0 |
| 32 | 6494 | 6496 | 0.670 | 81.537 | 81.563 | -0.025 | 19.1 |
| 32 | 6528 | 6528 | 0.670 | 81.964 | 81.964 | 0.000 | 19.2 |
| 32 | 6562 | 6560 | 0.670 | 82.391 | 82.366 | 0.025 | 19.3 |
| 32 | 6596 | 6592 | 0.670 | 82.818 | 82.768 | 0.050 | 19.4 |
| 34 | 6630 | 6626 | 0.711 | 83.245 | 83.195 | 0.050 | 19.5 |
| 35 | 6664 | 6661 | 0.732 | 83.672 | 83.634 | 0.038 | 19.6 |
| 34 | 6698 | 6695 | 0.711 | 84.099 | 84.061 | 0.038 | 19.7 |
| 34 | 6732 | 6729 | 0.711 | 84.526 | 84.488 | 0.038 | 19.8 |
| 36 | 6766 | 6765 | 0.753 | 84.953 | 84.940 | 0.013 | 19.9 |
| 36 | 6800 | 6801 | 0.753 | 85.379 | 85.392 | -0.013 | 20.0 |
| 36 | 6834 | 6837 | 0.753 | 85.806 | 85.844 | -0.038 | 20.1 |


| 36 | 6868 | 6873 | 0.753 | 86.233 | 86.296 | -0.063 | 20.2 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 34 | 6902 | 6907 | 0.711 | 86.660 | 86.723 | -0.063 | 20.3 |
| 33 | 6936 | 6940 | 0.691 | 87.087 | 87.137 | -0.050 | 20.4 |
| 33 | 6970 | 6973 | 0.691 | 87.514 | 87.552 | -0.038 | 20.5 |
| 32 | 7004 | 7005 | 0.670 | 87.941 | 87.953 | -0.013 | 20.6 |
| 32 | 7038 | 7037 | 0.670 | 88.368 | 88.355 | 0.013 | 20.7 |
| 32 | 7072 | 7069 | 0.670 | 88.795 | 88.757 | 0.038 | 20.8 |
| 33 | 7106 | 7102 | 0.691 | 89.222 | 89.171 | 0.050 | 20.9 |
| 34 | 7140 | 7136 | 0.711 | 89.648 | 89.598 | 0.050 | 21.0 |
| 34 | 7174 | 7170 | 0.711 | 90.075 | 90.025 | 0.050 | 21.1 |
| 35 | 7208 | 7205 | 0.732 | 90.502 | 90.465 | 0.038 | 21.2 |
| 34 | 7242 | 7239 | 0.711 | 90.929 | 90.891 | 0.038 | 21.3 |
| 36 | 7276 | 7275 | 0.753 | 91.356 | 91.343 | 0.013 | 21.4 |
| 36 | 7310 | 7311 | 0.753 | 91.783 | 91.795 | -0.013 | 21.5 |
| 37 | 7344 | 7348 | 0.774 | 92.210 | 92.260 | -0.050 | 21.6 |
| 35 | 7378 | 7383 | 0.732 | 92.637 | 92.699 | -0.063 | 21.7 |
| 34 | 7412 | 7417 | 0.711 | 93.064 | 93.126 | -0.063 | 21.8 |
| 34 | 7446 | 7451 | 0.711 | 93.491 | 93.553 | -0.063 | 21.9 |
| 32 | 7480 | 7483 | 0.670 | 93.917 | 93.955 | -0.038 | 22.0 |
| 32 | 7514 | 7515 | 0.670 | 94.344 | 94.357 | -0.013 | 22.1 |
| 32 | 7548 | 7547 | 0.670 | 94.771 | 94.759 | 0.013 | 22.2 |
| 31 | 7582 | 7578 | 0.649 | 95.198 | 95.148 | 0.050 | 22.3 |
| 33 | 7616 | 7611 | 0.691 | 95.625 | 95.562 | 0.063 | 22.4 |
| 34 | 7650 | 7645 | 0.711 | 96.052 | 95.989 | 0.063 | 22.5 |
| 35 | 7684 | 7680 | 0.732 | 96.479 | 96.429 | 0.050 | 22.6 |
| 35 | 7718 | 7715 | 0.732 | 96.906 | 96.868 | 0.038 | 22.7 |
| 35 | 7752 | 7750 | 0.732 | 97.333 | 97.307 | 0.025 | 22.8 |
| 35 | 7786 | 7785 | 0.732 | 97.759 | 97.747 | 0.013 | 22.9 |
| 36 | 7820 | 7821 | 0.753 | 98.186 | 98.199 | -0.013 | 23.0 |
| 36 | 7854 | 7857 | 0.753 | 98.613 | 98.651 | -0.038 | 23.1 |
| 36 | 7888 | 7893 | 0.753 | 99.040 | 99.103 | -0.063 | 23.2 |
| 34 | 7922 | 7927 | 0.711 | 99.467 | 99.530 | -0.063 | 23.3 |
| 33 | 7956 | 7960 | 0.691 | 99.894 | 99.944 | -0.050 | 23.4 |
| 32 | 7990 | 7992 | 0.670 | 100.321 | 100.346 | -0.025 | 23.5 |
| 32 | 8024 | 8024 | 0.670 | 100.748 | 100.748 | 0.000 | 23.6 |
| 32 | 8058 | 8056 | 0.670 | 101.175 | 101.150 | 0.025 | 23.7 |
| 32 | 8092 | 8088 | 0.670 | 101.602 | 101.551 | 0.050 | 23.8 |
| 33 | 8126 | 8121 | 0.691 | 102.028 | 101.966 | 0.063 | 23.9 |
| 34 | 8160 | 8155 | 0.711 | 102.455 | 102.393 | 0.063 | 24.0 |
| 36 | 8194 | 8191 | 0.753 | 102.882 | 102.845 | 0.038 | 24.1 |
| 35 | 8228 | 8226 | 0.732 | 103.309 | 103.284 | 0.025 | 24.2 |
| 35 | 8262 | 8261 | 0.732 | 103.736 | 103.723 | 0.013 | 24.3 |
| 36 | 8296 | 8297 | 0.753 | 104.163 | 104.176 | -0.013 | 24.4 |
| 36 | 8330 | 8333 | 0.753 | 104.590 | 104.628 | -0.038 | 24.5 |
| 36 | 8364 | 8369 | 0.753 | 105.017 | 105.080 | -0.063 | 24.6 |
| 35 | 8398 | 8404 | 0.732 | 105.444 | 105.519 | -0.075 | 24.7 |
| 33 | 8432 | 8437 | 0.691 | 105.871 | 105.933 | -0.063 | 24.8 |
| 32 | 8466 | 8469 | 0.670 | 106.297 | 106.335 | -0.038 | 24.9 |
| 32 | 8500 | 8501 | 0.670 | 106.724 | 106.737 | -0.013 | 25.0 |
| 31 | 8534 | 8532 | 0.649 | 107.151 | 107.126 | 0.025 | 25.1 |
| 33 | 8568 | 8565 | 0.691 | 107.578 | 107.540 | 0.038 | 25.2 |
| 32 | 8602 | 8597 | 0.670 | 108.005 | 107.942 | 0.063 | 25.3 |
| 34 | 8636 | 8631 | 0.711 | 108.432 | 108.369 | 0.063 | 25.4 |


| 35 | 8670 | 8666 | 0.732 | 108.859 | 108.809 | 0.050 | 25.5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 34 | 8704 | 8700 | 0.711 | 109.286 | 109.235 | 0.050 | 25.6 |
| 35 | 8738 | 8735 | 0.732 | 109.713 | 109.675 | 0.038 | 25.7 |
| 37 | 8772 | 8772 | 0.774 | 110.140 | 110.140 | 0.000 | 25.8 |
| 36 | 8806 | 8808 | 0.753 | 110.566 | 110.592 | -0.025 | 25.9 |
| 36 | 8840 | 8844 | 0.753 | 110.993 | 111.044 | -0.050 | 26.0 |
| 35 | 8874 | 8879 | 0.732 | 111.420 | 111.483 | -0.063 | 26.1 |
| 34 | 8908 | 8913 | 0.711 | 111.847 | 111.910 | -0.063 | 26.2 |
| 34 | 8942 | 8947 | 0.711 | 112.274 | 112.337 | -0.063 | 26.3 |
| 33 | 8976 | 8980 | 0.691 | 112.701 | 112.751 | -0.050 | 26.4 |
| 31 | 9010 | 9011 | 0.649 | 113.128 | 113.140 | -0.013 | 26.5 |
| 31 | 9044 | 9042 | 0.649 | 113.555 | 113.530 | 0.025 | 26.6 |
| 32 | 9078 | 9074 | 0.670 | 113.982 | 113.931 | 0.050 | 26.7 |
| 33 | 9112 | 9107 | 0.691 | 114.408 | 114.346 | 0.063 | 26.8 |
| 34 | 9146 | 9141 | 0.711 | 114.835 | 114.773 | 0.063 | 26.9 |
| 34 | 9180 | 9175 | 0.711 | 115.262 | 115.199 | 0.063 | 27.0 |
| 35 | 9214 | 9210 | 0.732 | 115.689 | 115.639 | 0.050 | 27.1 |
| 35 | 9248 | 9245 | 0.732 | 116.116 | 116.078 | 0.038 | 27.2 |
| 36 | 9282 | 9281 | 0.753 | 116.543 | 116.530 | 0.013 | 27.3 |
| 36 | 9316 | 9317 | 0.753 | 116.970 | 116.982 | -0.013 | 27.4 |
| 36 | 9350 | 9353 | 0.753 | 117.397 | 117.434 | -0.038 | 27.5 |
| 35 | 9384 | 9388 | 0.732 | 117.824 | 117.874 | -0.050 | 27.6 |
| 34 | 9418 | 9422 | 0.711 | 118.251 | 118.301 | -0.050 | 27.7 |
| 34 | 9452 | 9456 | 0.711 | 118.677 | 118.728 | -0.050 | 27.8 |
| 32 | 9486 | 9488 | 0.670 | 119.104 | 119.129 | -0.025 | 27.9 |
| 33 | 9520 | 9521 | 0.691 | 119.531 | 119.544 | -0.013 | 28.0 |
| 32 | 9554 | 9553 | 0.670 | 119.958 | 119.946 | 0.013 | 28.1 |
| 32 | 9588 | 9585 | 0.670 | 120.385 | 120.347 | 0.038 | 28.2 |
| 34 | 9622 | 9619 | 0.711 | 120.812 | 120.774 | 0.038 | 28.3 |
| 33 | 9656 | 9652 | 0.691 | 121.239 | 121.189 | 0.050 | 28.4 |
| 34 | 9690 | 9686 | 0.711 | 121.666 | 121.616 | 0.050 | 28.5 |
| 35 | 9724 | 9721 | 0.732 | 122.093 | 122.055 | 0.038 | 28.6 |
| 34 | 9758 | 9755 | 0.711 | 122.520 | 122.482 | 0.038 | 28.7 |
| 36 | 9792 | 9791 | 0.753 | 122.946 | 122.934 | 0.013 | 28.8 |
| 36 | 9826 | 9827 | 0.753 | 123.373 | 123.386 | -0.013 | 28.9 |
| 38 | 9860 | 9865 | 0.795 | 123.800 | 123.863 | -0.063 | 29.0 |
| 39 | 9894 | 9904 | 0.816 | 124.227 | 124.353 | -0.126 | 29.1 |
| 32 | 9928 | 9936 | 0.670 | 124.654 | 124.754 | -0.100 | 29.2 |
| 31 | 9962 | 9967 | 0.649 | 125.081 | 125.144 | -0.063 | 29.3 |
| 30 | 9996 | 9997 | 0.628 | 125.508 | 125.520 | -0.013 | 29.4 |
| 30 | 10030 | 10027 | 0.628 | 125.935 | 125.897 | 0.038 | 29.5 |
| 31 | 10064 | 10058 | 0.649 | 126.362 | 126.286 | 0.075 | 29.6 |
| 33 | 10098 | 10091 | 0.691 | 126.789 | 126.701 | 0.088 | 29.7 |
| 34 | 10132 | 10125 | 0.711 | 127.215 | 127.128 | 0.088 | 29.8 |
| 35 | 10166 | 10160 | 0.732 | 127.642 | 127.567 | 0.075 | 29.9 |
| 35 | 10200 | 10195 | 0.732 | 128.069 | 128.006 | 0.063 | 30.0 |
| 35 | 10234 | 10230 | 0.732 | 128.496 | 128.446 | 0.050 | 30.1 |
| 36 | 10268 | 10266 | 0.753 | 128.923 | 128.898 | 0.025 | 30.2 |
| 36 | 10302 | 10302 | 0.753 | 129.350 | 129.350 | 0.000 | 30.3 |
| 36 | 10336 | 10338 | 0.753 | 129.777 | 129.802 | -0.025 | 30.4 |
| 36 | 10370 | 10374 | 0.753 | 130.204 | 130.254 | -0.050 | 30.5 |
| 34 | 10404 | 10408 | 0.711 | 130.631 | 130.681 | -0.050 | 30.6 |
| 35 | 10438 | 10443 | 0.732 | 131.057 | 131.120 | -0.063 | 30.7 |


| 32 | 10472 | 10475 | 0.670 | 131.484 | 131.522 | -0.038 | 30.8 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 32 | 10506 | 10507 | 0.670 | 131.911 | 131.924 | -0.013 | 30.9 |
| 32 | 10540 | 10539 | 0.670 | 132.338 | 132.326 | 0.013 | 31.0 |
| 32 | 10574 | 10571 | 0.670 | 132.765 | 132.727 | 0.038 | 31.1 |
| 32 | 10608 | 10603 | 0.670 | 133.192 | 133.129 | 0.063 | 31.2 |
| 33 | 10642 | 10636 | 0.691 | 133.619 | 133.544 | 0.075 | 31.3 |
| 34 | 10676 | 10670 | 0.711 | 134.046 | 133.970 | 0.075 | 31.4 |
| 35 | 10710 | 10705 | 0.732 | 134.473 | 134.410 | 0.063 | 31.5 |
| 36 | 10744 | 10741 | 0.753 | 134.900 | 134.862 | 0.038 | 31.6 |
| 35 | 10778 | 10776 | 0.732 | 135.326 | 135.301 | 0.025 | 31.7 |
| 36 | 10812 | 10812 | 0.753 | 135.753 | 135.753 | 0.000 | 31.8 |
| 36 | 10846 | 10848 | 0.753 | 136.180 | 136.205 | -0.025 | 31.9 |
| 36 | 10880 | 10884 | 0.753 | 136.607 | 136.657 | -0.050 | 32.0 |
| 36 | 10914 | 10920 | 0.753 | 137.034 | 137.109 | -0.075 | 32.1 |
| 33 | 10948 | 10953 | 0.691 | 137.461 | 137.524 | -0.063 | 32.2 |
| 32 | 10982 | 10985 | 0.670 | 137.888 | 137.926 | -0.038 | 32.3 |
| 32 | 11016 | 11017 | 0.670 | 138.315 | 138.327 | -0.013 | 32.4 |
| 32 | 11050 | 11049 | 0.670 | 138.742 | 138.729 | 0.013 | 32.5 |
| 32 | 11084 | 11081 | 0.670 | 139.169 | 139.131 | 0.038 | 32.6 |
| 32 | 11118 | 11113 | 0.670 | 139.595 | 139.533 | 0.063 | 32.7 |
| 33 | 11152 | 11146 | 0.691 | 140.022 | 139.947 | 0.075 | 32.8 |
| 35 | 11186 | 11181 | 0.732 | 140.449 | 140.386 | 0.063 | 32.9 |
| 34 | 11220 | 11215 | 0.711 | 140.876 | 140.813 | 0.063 | 33.0 |
| 36 | 11254 | 11251 | 0.753 | 141.303 | 141.265 | 0.038 | 33.1 |
| 36 | 11288 | 11287 | 0.753 | 141.730 | 141.717 | 0.013 | 33.2 |
| 37 | 11322 | 11324 | 0.774 | 142.157 | 142.182 | -0.025 | 33.3 |
| 36 | 11356 | 11360 | 0.753 | 142.584 | 142.634 | -0.050 | 33.4 |
| 35 | 11390 | 11395 | 0.732 | 143.011 | 143.073 | -0.063 | 33.5 |
| 33 | 11424 | 11428 | 0.691 | 143.438 | 143.488 | -0.050 | 33.6 |
| 34 | 11458 | 11462 | 0.711 | 143.864 | 143.915 | -0.050 | 33.7 |
| 32 | 11492 | 11494 | 0.670 | 144.291 | 144.316 | -0.025 | 33.8 |
| 32 | 11526 | 11526 | 0.670 | 144.718 | 144.718 | 0.000 | 33.9 |
| 33 | 11560 | 11559 | 0.691 | 145.145 | 145.133 | 0.013 | 34.0 |
| 32 | 11594 | 11591 | 0.670 | 145.572 | 145.534 | 0.038 | 34.1 |
| 33 | 11628 | 11624 | 0.691 | 145.999 | 145.949 | 0.050 | 34.2 |
| 33 | 11662 | 11657 | 0.691 | 146.426 | 146.363 | 0.063 | 34.3 |
| 35 | 11696 | 11692 | 0.732 | 146.853 | 146.802 | 0.050 | 34.4 |
| 34 | 11730 | 11726 | 0.711 | 147.280 | 147.229 | 0.050 | 34.5 |
| 35 | 11764 | 11761 | 0.732 | 147.706 | 147.669 | 0.038 | 34.6 |
| 37 | 11798 | 11798 | 0.774 | 148.133 | 148.133 | 0.000 | 34.7 |
| 35 | 11832 | 11833 | 0.732 | 148.560 | 148.573 | -0.013 | 34.8 |
| 36 | 11866 | 11869 | 0.753 | 148.987 | 149.025 | -0.038 | 34.9 |
| 35 | 11900 | 11904 | 0.732 | 149.414 | 149.464 | -0.050 | 35.0 |
| 34 | 11934 | 11938 | 0.711 | 149.841 | 149.891 | -0.050 | 35.1 |
| 33 | 11968 | 11971 | 0.691 | 150.268 | 150.306 | -0.038 | 35.2 |
| 32 | 12002 | 12003 | 0.670 | 150.695 | 150.707 | -0.013 | 35.3 |
| 35 | 12036 | 12038 | 0.732 | 151.122 | 151.147 | -0.025 | 35.4 |
| 31 | 12070 | 12069 | 0.649 | 151.549 | 151.536 | 0.013 | 35.5 |
| 31 | 12104 | 12100 | 0.649 | 151.975 | 151.925 | 0.050 | 35.6 |
| 33 | 12138 | 12133 | 0.691 | 152.402 | 152.340 | 0.063 | 35.7 |
| 34 | 12172 | 12167 | 0.711 | 152.829 | 152.766 | 0.063 | 35.8 |
| 34 | 12206 | 12201 | 0.711 | 153.256 | 153.193 | 0.063 | 35.9 |
| 36 | 12240 | 12237 | 0.753 | 153.683 | 153.645 | 0.038 | 36.0 |


| 36 | 12274 | 12273 | 0.753 | 154.110 | 154.097 | 0.013 | 36.1 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 36 | 12308 | 12309 | 0.753 | 154.537 | 154.549 | -0.013 | 36.2 |
| 36 | 12342 | 12345 | 0.753 | 154.964 | 155.001 | -0.038 | 36.3 |
| 35 | 12376 | 12380 | 0.732 | 155.391 | 155.441 | -0.050 | 36.4 |
| 35 | 12410 | 12415 | 0.732 | 155.818 | 155.880 | -0.063 | 36.5 |
| 33 | 12444 | 12448 | 0.691 | 156.244 | 156.295 | -0.050 | 36.6 |
| 33 | 12478 | 12481 | 0.691 | 156.671 | 156.709 | -0.038 | 36.7 |
| 32 | 12512 | 12513 | 0.670 | 157.098 | 157.111 | -0.013 | 36.8 |
| 31 | 12546 | 12544 | 0.649 | 157.525 | 157.500 | 0.025 | 36.9 |
| 32 | 12580 | 12576 | 0.670 | 157.952 | 157.902 | 0.050 | 37.0 |
| 33 | 12614 | 12609 | 0.691 | 158.379 | 158.316 | 0.063 | 37.1 |
| 33 | 12648 | 12642 | 0.691 | 158.806 | 158.730 | 0.075 | 37.2 |
| 34 | 12682 | 12676 | 0.711 | 159.233 | 159.157 | 0.075 | 37.3 |
| 35 | 12716 | 12711 | 0.732 | 159.660 | 159.597 | 0.063 | 37.4 |
| 36 | 12750 | 12747 | 0.753 | 160.086 | 160.049 | 0.038 | 37.5 |
| 35 | 12784 | 12782 | 0.732 | 160.513 | 160.488 | 0.025 | 37.6 |
| 37 | 12818 | 12819 | 0.774 | 160.940 | 160.953 | -0.013 | 37.7 |
| 36 | 12852 | 12855 | 0.753 | 161.367 | 161.405 | -0.038 | 37.8 |
| 35 | 12886 | 12890 | 0.732 | 161.794 | 161.844 | -0.050 | 37.9 |
| 36 | 12920 | 12926 | 0.753 | 162.221 | 162.296 | -0.075 | 38.0 |
| 33 | 12954 | 12959 | 0.691 | 162.648 | 162.711 | -0.063 | 38.1 |
| 32 | 12988 | 12991 | 0.670 | 163.075 | 163.112 | -0.038 | 38.2 |
| 32 | 13022 | 13023 | 0.670 | 163.502 | 163.514 | -0.013 | 38.3 |
| 32 | 13056 | 13055 | 0.670 | 163.929 | 163.916 | 0.013 | 38.4 |
| 32 | 13090 | 13087 | 0.670 | 164.355 | 164.318 | 0.038 | 38.5 |
| 32 | 13124 | 13119 | 0.670 | 164.782 | 164.720 | 0.063 | 38.6 |
| 33 | 13158 | 13152 | 0.691 | 165.209 | 165.134 | 0.075 | 38.7 |
| 36 | 13192 | 13188 | 0.753 | 165.636 | 165.586 | 0.050 | 38.8 |
| 35 | 13226 | 13223 | 0.732 | 166.063 | 166.025 | 0.038 | 38.9 |
| 34 | 13260 | 13257 | 0.711 | 166.490 | 166.452 | 0.038 | 39.0 |
| 37 | 13294 | 13294 | 0.774 | 166.917 | 166.917 | 0.000 | 39.1 |
| 38 | 13328 | 13332 | 0.795 | 167.344 | 167.394 | -0.050 | 39.2 |
| 35 | 13362 | 13367 | 0.732 | 167.771 | 167.833 | -0.063 | 39.3 |
| 34 | 13396 | 13401 | 0.711 | 168.198 | 168.260 | -0.063 | 39.4 |
| 35 | 13430 | 13436 | 0.732 | 168.624 | 168.700 | -0.075 | 39.5 |
| 32 | 13464 | 13468 | 0.670 | 169.051 | 169.102 | -0.050 | 39.6 |
| 32 | 13498 | 13500 | 0.670 | 169.478 | 169.503 | -0.025 | 39.7 |
| 33 | 13532 | 13533 | 0.691 | 169.905 | 169.918 | -0.013 | 39.8 |
| 32 | 13566 | 13565 | 0.670 | 170.332 | 170.319 | 0.013 | 39.9 |
| 32 | 13600 | 13597 | 0.670 | 170.759 | 170.721 | 0.038 | 40.0 |
| 32 | 13634 | 13629 | 0.670 | 171.186 | 171.123 | 0.063 | 40.1 |
| 33 | 13668 | 13662 | 0.691 | 171.613 | 171.537 | 0.075 | 40.2 |
| 35 | 13702 | 13697 | 0.732 | 172.040 | 171.977 | 0.063 | 40.3 |
| 35 | 13736 | 13732 | 0.732 | 172.467 | 172.416 | 0.050 | 40.4 |
| 36 | 13770 | 13768 | 0.753 | 172.893 | 172.868 | 0.025 | 40.5 |
| 37 | 13804 | 13805 | 0.774 | 173.320 | 173.333 | -0.013 | 40.6 |
| 36 | 13838 | 13841 | 0.753 | 173.747 | 173.785 | -0.038 | 40.7 |
| 36 | 13872 | 13877 | 0.753 | 174.174 | 174.237 | -0.063 | 40.8 |
| 35 | 13906 | 13912 | 0.732 | 174.601 | 174.676 | -0.075 | 40.9 |
| 33 | 13940 | 13945 | 0.691 | 175.028 | 175.091 | -0.063 | 41.0 |
| 33 | 13974 | 13978 | 0.691 | 175.455 | 175.505 | -0.050 | 41.1 |
| 33 | 14008 | 14011 | 0.691 | 175.882 | 175.919 | -0.038 | 41.2 |
| 31 | 14042 | 14042 | 0.649 | 176.309 | 176.309 | 0.000 | 41.3 |


| 33 | 14076 | 14075 | 0.691 | 176.735 | 176.723 | 0.013 | 41.4 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 32 | 14110 | 14107 | 0.670 | 177.162 | 177.125 | 0.038 | 41.5 |
| 33 | 14144 | 14140 | 0.691 | 177.589 | 177.539 | 0.050 | 41.6 |
| 34 | 14178 | 14174 | 0.711 | 178.016 | 177.966 | 0.050 | 41.7 |
| 35 | 14212 | 14209 | 0.732 | 178.443 | 178.405 | 0.038 | 41.8 |
| 35 | 14246 | 14244 | 0.732 | 178.870 | 178.845 | 0.025 | 41.9 |
| 35 | 14280 | 14279 | 0.732 | 179.297 | 179.284 | 0.013 | 42.0 |
| 35 | 14314 | 14314 | 0.732 | 179.724 | 179.724 | 0.000 | 42.1 |
| 36 | 14348 | 14350 | 0.753 | 180.151 | 180.176 | -0.025 | 42.2 |
| 37 | 14382 | 14387 | 0.774 | 180.578 | 180.640 | -0.063 | 42.3 |
| 35 | 14416 | 14422 | 0.732 | 181.004 | 181.080 | -0.075 | 42.4 |
| 34 | 14450 | 14456 | 0.711 | 181.431 | 181.507 | -0.075 | 42.5 |
| 33 | 14484 | 14489 | 0.691 | 181.858 | 181.921 | -0.063 | 42.6 |
| 33 | 14518 | 14522 | 0.691 | 182.285 | 182.335 | -0.050 | 42.7 |
| 31 | 14552 | 14553 | 0.649 | 182.712 | 182.725 | -0.013 | 42.8 |
| 32 | 14586 | 14585 | 0.670 | 183.139 | 183.126 | 0.013 | 42.9 |
| 32 | 14620 | 14617 | 0.670 | 183.566 | 183.528 | 0.038 | 43.0 |
| 34 | 14654 | 14651 | 0.711 | 183.993 | 183.955 | 0.038 | 43.1 |
| 34 | 14688 | 14685 | 0.711 | 184.420 | 184.382 | 0.038 | 43.2 |
| 35 | 14722 | 14720 | 0.732 | 184.847 | 184.821 | 0.025 | 43.3 |
| 34 | 14756 | 14754 | 0.711 | 185.273 | 185.248 | 0.025 | 43.4 |
| 35 | 14790 | 14789 | 0.732 | 185.700 | 185.688 | 0.013 | 43.5 |
| 37 | 14824 | 14826 | 0.774 | 186.127 | 186.152 | -0.025 | 43.6 |
| 36 | 14858 | 14862 | 0.753 | 186.554 | 186.604 | -0.050 | 43.7 |
| 36 | 14892 | 14898 | 0.753 | 186.981 | 187.056 | -0.075 | 43.8 |
| 35 | 14926 | 14933 | 0.732 | 187.408 | 187.496 | -0.088 | 43.9 |
| 33 | 14960 | 14966 | 0.691 | 187.835 | 187.910 | -0.075 | 44.0 |
| 33 | 14994 | 14999 | 0.691 | 188.262 | 188.324 | -0.063 | 44.1 |
| 32 | 15028 | 15031 | 0.670 | 188.689 | 188.726 | -0.038 | 44.2 |
| 31 | 15062 | 15062 | 0.649 | 189.116 | 189.116 | 0.000 | 44.3 |
| 32 | 15096 | 15094 | 0.670 | 189.542 | 189.517 | 0.025 | 44.4 |
| 33 | 15130 | 15127 | 0.691 | 189.969 | 189.932 | 0.038 | 44.5 |
| 34 | 15164 | 15161 | 0.711 | 190.396 | 190.359 | 0.038 | 44.6 |
| 34 | 15198 | 15195 | 0.711 | 190.823 | 190.785 | 0.038 | 44.7 |
| 35 | 15232 | 15230 | 0.732 | 191.250 | 191.225 | 0.025 | 44.8 |
| 35 | 15266 | 15265 | 0.732 | 191.677 | 191.664 | 0.013 | 44.9 |
| 35 | 15300 | 15300 | 0.732 | 192.104 | 192.104 | 0.000 | 45.0 |
| 37 | 15334 | 15337 | 0.774 | 192.531 | 192.568 | -0.038 | 45.1 |
| 38 | 15368 | 15375 | 0.795 | 192.958 | 193.045 | -0.088 | 45.2 |
| 35 | 15402 | 15410 | 0.732 | 193.384 | 193.485 | -0.100 | 45.3 |
| 34 | 15436 | 15444 | 0.711 | 193.811 | 193.912 | -0.100 | 45.4 |
| 32 | 15470 | 15476 | 0.670 | 194.238 | 194.314 | -0.075 | 45.5 |
| 32 | 15504 | 15508 | 0.670 | 194.665 | 194.715 | -0.050 | 45.6 |
| 32 | 15538 | 15540 | 0.670 | 195.092 | 195.117 | -0.025 | 45.7 |
| 32 | 15572 | 15572 | 0.670 | 195.519 | 195.519 | 0.000 | 45.8 |
| 33 | 15606 | 15605 | 0.691 | 195.946 | 195.933 | 0.013 | 45.9 |
| 32 | 15640 | 15637 | 0.670 | 196.373 | 196.335 | 0.038 | 46.0 |
| 34 | 15674 | 15671 | 0.711 | 196.800 | 196.762 | 0.038 | 46.1 |
| 35 | 15708 | 15706 | 0.732 | 197.227 | 197.201 | 0.025 | 46.2 |
| 34 | 15742 | 15740 | 0.711 | 197.653 | 197.628 | 0.025 | 46.3 |
| 35 | 15776 | 15775 | 0.732 | 198.080 | 198.068 | 0.013 | 46.4 |
| 35 | 15810 | 15810 | 0.732 | 198.507 | 198.507 | 0.000 | 46.5 |
| 36 | 15844 | 15846 | 0.753 | 198.934 | 198.959 | -0.025 | 46.6 |


| 37 | 15878 | 15883 | 0.774 | 199.361 | 199.424 | -0.063 | 46.7 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 36 | 15912 | 15919 | 0.753 | 199.788 | 199.876 | -0.088 | 46.8 |
| 34 | 15946 | 15953 | 0.711 | 200.215 | 200.303 | -0.088 | 46.9 |
| 34 | 15980 | 15987 | 0.711 | 200.642 | 200.730 | -0.088 | 47.0 |
| 32 | 16014 | 16019 | 0.670 | 201.069 | 201.131 | -0.063 | 47.1 |
| 31 | 16048 | 16050 | 0.649 | 201.496 | 201.521 | -0.025 | 47.2 |
| 32 | 16082 | 16082 | 0.670 | 201.922 | 201.922 | 0.000 | 47.3 |
| 32 | 16116 | 16114 | 0.670 | 202.349 | 202.324 | 0.025 | 47.4 |
| 34 | 16150 | 16148 | 0.711 | 202.776 | 202.751 | 0.025 | 47.5 |
| 33 | 16184 | 16181 | 0.691 | 203.203 | 203.165 | 0.038 | 47.6 |
| 35 | 16218 | 16216 | 0.732 | 203.630 | 203.605 | 0.025 | 47.7 |
| 35 | 16252 | 16251 | 0.732 | 204.057 | 204.044 | 0.013 | 47.8 |
| 34 | 16286 | 16285 | 0.711 | 204.484 | 204.471 | 0.013 | 47.9 |
| 37 | 16320 | 16322 | 0.774 | 204.911 | 204.936 | -0.025 | 48.0 |
| 36 | 16354 | 16358 | 0.753 | 205.338 | 205.388 | -0.050 | 48.1 |
| 36 | 16388 | 16394 | 0.753 | 205.765 | 205.840 | -0.075 | 48.2 |
| 35 | 16422 | 16429 | 0.732 | 206.191 | 206.279 | -0.088 | 48.3 |
| 34 | 16456 | 16463 | 0.711 | 206.618 | 206.706 | -0.088 | 48.4 |
| 32 | 16490 | 16495 | 0.670 | 207.045 | 207.108 | -0.063 | 48.5 |
| 33 | 16524 | 16528 | 0.691 | 207.472 | 207.522 | -0.050 | 48.6 |
| 32 | 16558 | 16560 | 0.670 | 207.899 | 207.924 | -0.025 | 48.7 |
| 31 | 16592 | 16591 | 0.649 | 208.326 | 208.313 | 0.013 | 48.8 |
| 33 | 16626 | 16624 | 0.691 | 208.753 | 208.728 | 0.025 | 48.9 |
| 33 | 16660 | 16657 | 0.691 | 209.180 | 209.142 | 0.038 | 49.0 |
| 34 | 16694 | 16691 | 0.711 | 209.607 | 209.569 | 0.038 | 49.1 |
| 34 | 16728 | 16725 | 0.711 | 210.033 | 209.996 | 0.038 | 49.2 |
| 35 | 16762 | 16760 | 0.732 | 210.460 | 210.435 | 0.025 | 49.3 |
| 35 | 16796 | 16795 | 0.732 | 210.887 | 210.875 | 0.013 | 49.4 |
| 36 | 16830 | 16831 | 0.753 | 211.314 | 211.327 | -0.013 | 49.5 |
| 37 | 16864 | 16868 | 0.774 | 211.741 | 211.791 | -0.050 | 49.6 |
| 36 | 16898 | 16904 | 0.753 | 212.168 | 212.243 | -0.075 | 49.7 |
| 36 | 16932 | 16940 | 0.753 | 212.595 | 212.695 | -0.100 | 49.8 |
| 35 | 16966 | 16975 | 0.732 | 213.022 | 213.135 | -0.113 | 49.9 |
| 31 | 17000 | 17006 | 0.649 | 213.449 | 213.524 | -0.075 | 50.0 |
| 31 | 17034 | 17037 | 0.649 | 213.876 | 213.913 | -0.038 | 50.1 |
| 32 | 17068 | 17069 | 0.670 | 214.302 | 214.315 | -0.013 | 50.2 |
| 32 | 17102 | 17101 | 0.670 | 214.729 | 214.717 | 0.013 | 50.3 |
| 32 | 17136 | 17133 | 0.670 | 215.156 | 215.119 | 0.038 | 50.4 |
| 33 | 17170 | 17166 | 0.691 | 215.583 | 215.533 | 0.050 | 50.5 |
| 34 | 17204 | 17200 | 0.711 | 216.010 | 215.960 | 0.050 | 50.6 |
| 35 | 17238 | 17235 | 0.732 | 216.437 | 216.399 | 0.038 | 50.7 |
| 37 | 17272 | 17272 | 0.774 | 216.864 | 216.864 | 0.000 | 50.8 |
| 35 | 17306 | 17307 | 0.732 | 217.291 | 217.303 | -0.013 | 50.9 |
| 36 | 17340 | 17343 | 0.753 | 217.718 | 217.755 | -0.038 | 51.0 |
| 36 | 17374 | 17379 | 0.753 | 218.145 | 218.207 | -0.063 | 51.1 |
| 36 | 17408 | 17415 | 0.753 | 218.571 | 218.659 | -0.088 | 51.2 |
| 35 | 17442 | 17450 | 0.732 | 218.998 | 219.099 | -0.100 | 51.3 |
| 32 | 17476 | 17482 | 0.670 | 219.425 | 219.501 | -0.075 | 51.4 |
| 31 | 17510 | 17513 | 0.649 | 219.852 | 219.890 | -0.038 | 51.5 |
| 31 | 17544 | 17544 | 0.649 | 220.279 | 220.279 | 0.000 | 51.6 |
| 31 | 17578 | 17575 | 0.649 | 220.706 | 220.668 | 0.038 | 51.7 |
| 33 | 17612 | 17608 | 0.691 | 221.133 | 221.083 | 0.050 | 51.8 |
| 33 | 17646 | 17641 | 0.691 | 221.560 | 221.497 | 0.063 | 51.9 |


| 34 | 17680 | 17675 | 0.711 | 221.987 | 221.924 | 0.063 | 52.0 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 36 | 17714 | 17711 | 0.753 | 222.414 | 222.376 | 0.038 | 52.1 |
| 35 | 17748 | 17746 | 0.732 | 222.840 | 222.815 | 0.025 | 52.2 |
| 35 | 17782 | 17781 | 0.732 | 223.267 | 223.255 | 0.013 | 52.3 |
| 35 | 17816 | 17816 | 0.732 | 223.694 | 223.694 | 0.000 | 52.4 |
| 35 | 17850 | 17851 | 0.732 | 224.121 | 224.134 | -0.013 | 52.5 |
| 36 | 17884 | 17887 | 0.753 | 224.548 | 224.586 | -0.038 | 52.6 |
| 36 | 17918 | 17923 | 0.753 | 224.975 | 225.038 | -0.063 | 52.7 |
| 34 | 17952 | 17957 | 0.711 | 225.402 | 225.465 | -0.063 | 52.8 |
| 33 | 17986 | 17990 | 0.691 | 225.829 | 225.879 | -0.050 | 52.9 |
| 33 | 18020 | 18023 | 0.691 | 226.256 | 226.293 | -0.038 | 53.0 |
| 32 | 18054 | 18055 | 0.670 | 226.682 | 226.695 | -0.013 | 53.1 |
| 32 | 18088 | 18087 | 0.670 | 227.109 | 227.097 | 0.013 | 53.2 |
| 33 | 18122 | 18120 | 0.691 | 227.536 | 227.511 | 0.025 | 53.3 |
| 33 | 18156 | 18153 | 0.691 | 227.963 | 227.926 | 0.038 | 53.4 |
| 34 | 18190 | 18187 | 0.711 | 228.390 | 228.352 | 0.038 | 53.5 |
| 34 | 18224 | 18221 | 0.711 | 228.817 | 228.779 | 0.038 | 53.6 |
| 34 | 18258 | 18255 | 0.711 | 229.244 | 229.206 | 0.038 | 53.7 |
| 35 | 18292 | 18290 | 0.732 | 229.671 | 229.646 | 0.025 | 53.8 |
| 35 | 18326 | 18325 | 0.732 | 230.098 | 230.085 | 0.013 | 53.9 |
| 36 | 18360 | 18361 | 0.753 | 230.525 | 230.537 | -0.013 | 54.0 |
| 36 | 18394 | 18397 | 0.753 | 230.951 | 230.989 | -0.038 | 54.1 |
| 35 | 18428 | 18432 | 0.732 | 231.378 | 231.429 | -0.050 | 54.2 |
| 35 | 18462 | 18467 | 0.732 | 231.805 | 231.868 | -0.063 | 54.3 |
| 33 | 18496 | 18500 | 0.691 | 232.232 | 232.282 | -0.050 | 54.4 |
| 33 | 18530 | 18533 | 0.691 | 232.659 | 232.697 | -0.038 | 54.5 |
| 32 | 18564 | 18565 | 0.670 | 233.086 | 233.098 | -0.013 | 54.6 |
| 32 | 18598 | 18597 | 0.670 | 233.513 | 233.500 | 0.013 | 54.7 |
| 33 | 18632 | 18630 | 0.691 | 233.940 | 233.915 | 0.025 | 54.8 |
| 33 | 18666 | 18663 | 0.691 | 234.367 | 234.329 | 0.038 | 54.9 |
| 33 | 18700 | 18696 | 0.691 | 234.794 | 234.743 | 0.050 | 55.0 |
| 35 | 18734 | 18731 | 0.732 | 235.220 | 235.183 | 0.038 | 55.1 |
| 34 | 18768 | 18765 | 0.711 | 235.647 | 235.610 | 0.038 | 55.2 |
| 35 | 18802 | 18800 | 0.732 | 236.074 | 236.049 | 0.025 | 55.3 |
| 36 | 18836 | 18836 | 0.753 | 236.501 | 236.501 | 0.000 | 55.4 |
| 36 | 18870 | 18872 | 0.753 | 236.928 | 236.953 | -0.025 | 55.5 |
| 36 | 18904 | 18908 | 0.753 | 237.355 | 237.405 | -0.050 | 55.6 |
| 35 | 18938 | 18943 | 0.732 | 237.782 | 237.845 | -0.063 | 55.7 |
| 34 | 18972 | 18977 | 0.711 | 238.209 | 238.271 | -0.063 | 55.8 |
| 33 | 19006 | 19010 | 0.691 | 238.636 | 238.686 | -0.050 | 55.9 |
| 32 | 19040 | 19042 | 0.670 | 239.063 | 239.088 | -0.025 | 56.0 |
| 32 | 19074 | 19074 | 0.670 | 239.489 | 239.489 | 0.000 | 56.1 |
| 32 | 19108 | 19106 | 0.670 | 239.916 | 239.891 | 0.025 | 56.2 |
| 33 | 19142 | 19139 | 0.691 | 240.343 | 240.306 | 0.038 | 56.3 |
| 33 | 19176 | 19172 | 0.691 | 240.770 | 240.720 | 0.050 | 56.4 |
| 34 | 19210 | 19206 | 0.711 | 241.197 | 241.147 | 0.050 | 56.5 |
| 35 | 19244 | 19241 | 0.732 | 241.624 | 241.586 | 0.038 | 56.6 |
| 35 | 19278 | 19276 | 0.732 | 242.051 | 242.026 | 0.025 | 56.7 |
| 35 | 19312 | 19311 | 0.732 | 242.478 | 242.465 | 0.013 | 56.8 |
| 35 | 19346 | 19346 | 0.732 | 242.905 | 242.905 | 0.000 | 56.9 |
| 36 | 19380 | 19382 | 0.753 | 243.331 | 243.357 | -0.025 | 57.0 |
| 36 | 19414 | 19418 | 0.753 | 243.758 | 243.809 | -0.050 | 57.1 |
| 35 | 19448 | 19453 | 0.732 | 244.185 | 244.248 | -0.063 | 57.2 |


| 34 | 19482 | 19487 | 0.711 | 244.612 | 244.675 | -0.063 | 57.3 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 33 | 19516 | 19520 | 0.691 | 245.039 | 245.089 | -0.050 | 57.4 |
| 31 | 19550 | 19551 | 0.649 | 245.466 | 245.479 | -0.013 | 57.5 |
| 32 | 19584 | 19583 | 0.670 | 245.893 | 245.880 | 0.013 | 57.6 |
| 33 | 19618 | 19616 | 0.691 | 246.320 | 246.295 | 0.025 | 57.7 |
| 32 | 19652 | 19648 | 0.670 | 246.747 | 246.696 | 0.050 | 57.8 |
| 34 | 19686 | 19682 | 0.711 | 247.174 | 247.123 | 0.050 | 57.9 |
| 34 | 19720 | 19716 | 0.711 | 247.600 | 247.550 | 0.050 | 58.0 |
| 35 | 19754 | 19751 | 0.732 | 248.027 | 247.990 | 0.038 | 58.1 |
| 35 | 19788 | 19786 | 0.732 | 248.454 | 248.429 | 0.025 | 58.2 |
| 35 | 19822 | 19821 | 0.732 | 248.881 | 248.869 | 0.013 | 58.3 |
| 36 | 19856 | 19857 | 0.753 | 249.308 | 249.321 | -0.013 | 58.4 |
| 35 | 19890 | 19892 | 0.732 | 249.735 | 249.760 | -0.025 | 58.5 |
| 36 | 19924 | 19928 | 0.753 | 250.162 | 250.212 | -0.050 | 58.6 |
| 36 | 19958 | 19964 | 0.753 | 250.589 | 250.664 | -0.075 | 58.7 |
| 33 | 19992 | 19997 | 0.691 | 251.016 | 251.078 | -0.063 | 58.8 |
| 33 | 20026 | 20030 | 0.691 | 251.443 | 251.493 | -0.050 | 58.9 |
| 31 | 20060 | 20061 | 0.649 | 251.869 | 251.882 | -0.013 | 59.0 |
| 31 | 20094 | 20092 | 0.649 | 252.296 | 252.271 | 0.025 | 59.1 |
| 32 | 20128 | 20124 | 0.670 | 252.723 | 252.673 | 0.050 | 59.2 |
| 33 | 20162 | 20157 | 0.691 | 253.150 | 253.087 | 0.063 | 59.3 |
| 34 | 20196 | 20191 | 0.711 | 253.577 | 253.514 | 0.063 | 59.4 |
| 35 | 20230 | 20226 | 0.732 | 254.004 | 253.954 | 0.050 | 59.5 |
| 35 | 20264 | 20261 | 0.732 | 254.431 | 254.393 | 0.038 | 59.6 |
| 34 | 20298 | 20295 | 0.711 | 254.858 | 254.820 | 0.038 | 59.7 |
| 36 | 20332 | 20331 | 0.753 | 255.285 | 255.272 | 0.013 | 59.8 |
| 36 | 20366 | 20367 | 0.753 | 255.711 | 255.724 | -0.013 | 59.9 |
| 36 | 20400 | 20403 | 0.753 | 256.138 | 256.176 | -0.038 | 60.0 |
| 37 | 20434 | 20440 | 0.774 | 256.565 | 256.641 | -0.075 | 60.1 |
| 35 | 20468 | 20475 | 0.732 | 256.992 | 257.080 | -0.088 | 60.2 |
| 33 | 20502 | 20508 | 0.691 | 257.419 | 257.494 | -0.075 | 60.3 |
| 31 | 20536 | 20539 | 0.649 | 257.846 | 257.884 | -0.038 | 60.4 |
| 31 | 20570 | 20570 | 0.649 | 258.273 | 258.273 | 0.000 | 60.5 |
| 31 | 20604 | 20601 | 0.649 | 258.700 | 258.662 | 0.038 | 60.6 |
| 32 | 20638 | 20633 | 0.670 | 259.127 | 259.064 | 0.063 | 60.7 |
| 33 | 20672 | 20666 | 0.691 | 259.554 | 259.478 | 0.075 | 60.8 |
| 34 | 20706 | 20700 | 0.711 | 259.980 | 259.905 | 0.075 | 60.9 |
| 35 | 20740 | 20735 | 0.732 | 260.407 | 260.345 | 0.063 | 61.0 |
| 36 | 20774 | 20771 | 0.753 | 260.834 | 260.797 | 0.038 | 61.1 |
| 36 | 20808 | 20807 | 0.753 | 261.261 | 261.249 | 0.013 | 61.2 |
| 35 | 20842 | 20842 | 0.732 | 261.688 | 261.688 | 0.000 | 61.3 |
| 36 | 20876 | 20878 | 0.753 | 262.115 | 262.140 | -0.025 | 61.4 |
| 35 | 20910 | 20913 | 0.732 | 262.542 | 262.580 | -0.038 | 61.5 |
| 35 | 20944 | 20948 | 0.732 | 262.969 | 263.019 | -0.050 | 61.6 |
| 35 | 20978 | 20983 | 0.732 | 263.396 | 263.458 | -0.063 | 61.7 |
| 32 | 21012 | 21015 | 0.670 | 263.823 | 263.860 | -0.038 | 61.8 |
| 33 | 21046 | 21048 | 0.691 | 264.249 | 264.275 | -0.025 | 61.9 |
| 32 | 21080 | 21080 | 0.670 | 264.676 | 264.676 | 0.000 | 62.0 |
| 32 | 21114 | 21112 | 0.670 | 265.103 | 265.078 | 0.025 | 62.1 |
| 32 | 21148 | 21144 | 0.670 | 265.530 | 265.480 | 0.050 | 62.2 |
| 33 | 21182 | 21177 | 0.691 | 265.957 | 265.894 | 0.063 | 62.3 |
| 35 | 21216 | 21212 | 0.732 | 266.384 | 266.334 | 0.050 | 62.4 |
| 35 | 21250 | 21247 | 0.732 | 266.811 | 266.773 | 0.038 | 62.5 |


| 34 | 21284 | 21281 | 0.711 | 267.238 | 267.200 | 0.038 | 62.6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 35 | 21318 | 21316 | 0.732 | 267.665 | 267.640 | 0.025 | 62.7 |
| 36 | 21352 | 21352 | 0.753 | 268.092 | 268.092 | 0.000 | 62.8 |
| 36 | 21386 | 21388 | 0.753 | 268.518 | 268.544 | -0.025 | 62.9 |
| 36 | 21420 | 21424 | 0.753 | 268.945 | 268.996 | -0.050 | 63.0 |
| 34 | 21454 | 21458 | 0.711 | 269.372 | 269.422 | -0.050 | 63.1 |
| 34 | 21488 | 21492 | 0.711 | 269.799 | 269.849 | -0.050 | 63.2 |
| 33 | 21522 | 21525 | 0.691 | 270.226 | 270.264 | -0.038 | 63.3 |
| 32 | 21556 | 21557 | 0.670 | 270.653 | 270.665 | -0.013 | 63.4 |
| 32 | 21590 | 21589 | 0.670 | 271.080 | 271.067 | 0.013 | 63.5 |
| 33 | 21624 | 21622 | 0.691 | 271.507 | 271.482 | 0.025 | 63.6 |
| 32 | 21658 | 21654 | 0.670 | 271.934 | 271.883 | 0.050 | 63.7 |
| 34 | 21692 | 21688 | 0.711 | 272.360 | 272.310 | 0.050 | 63.8 |
| 34 | 21726 | 21722 | 0.711 | 272.787 | 272.737 | 0.050 | 63.9 |
| 34 | 21760 | 21756 | 0.711 | 273.214 | 273.164 | 0.050 | 64.0 |
| 35 | 21794 | 21791 | 0.732 | 273.641 | 273.604 | 0.038 | 64.1 |
| 35 | 21828 | 21826 | 0.732 | 274.068 | 274.043 | 0.025 | 64.2 |
| 38 | 21862 | 21864 | 0.795 | 274.495 | 274.520 | -0.025 | 64.3 |
| 36 | 21896 | 21900 | 0.753 | 274.922 | 274.972 | -0.050 | 64.4 |
| 36 | 21930 | 21936 | 0.753 | 275.349 | 275.424 | -0.075 | 64.5 |
| 33 | 21964 | 21969 | 0.691 | 275.776 | 275.838 | -0.063 | 64.6 |
| 33 | 21998 | 22002 | 0.691 | 276.203 | 276.253 | -0.050 | 64.7 |
| 33 | 22032 | 22035 | 0.691 | 276.629 | 276.667 | -0.038 | 64.8 |
| 32 | 22066 | 22067 | 0.670 | 277.056 | 277.069 | -0.013 | 64.9 |
| 31 | 22100 | 22098 | 0.649 | 277.483 | 277.458 | 0.025 | 65.0 |
| 33 | 22134 | 22131 | 0.691 | 277.910 | 277.872 | 0.038 | 65.1 |
| 33 | 22168 | 22164 | 0.691 | 278.337 | 278.287 | 0.050 | 65.2 |
| 34 | 22202 | 22198 | 0.711 | 278.764 | 278.714 | 0.050 | 65.3 |
| 35 | 22236 | 22233 | 0.732 | 279.191 | 279.153 | 0.038 | 65.4 |
| 35 | 22270 | 22268 | 0.732 | 279.618 | 279.593 | 0.025 | 65.5 |
| 34 | 22304 | 22302 | 0.711 | 280.045 | 280.020 | 0.025 | 65.6 |
| 35 | 22338 | 22337 | 0.732 | 280.472 | 280.459 | 0.013 | 65.7 |
| 35 | 22372 | 22372 | 0.732 | 280.898 | 280.898 | 0.000 | 65.8 |
| 37 | 22406 | 22409 | 0.774 | 281.325 | 281.363 | -0.038 | 65.9 |
| 36 | 22440 | 22445 | 0.753 | 281.752 | 281.815 | -0.063 | 66.0 |
| 35 | 22474 | 22480 | 0.732 | 282.179 | 282.254 | -0.075 | 66.1 |
| 33 | 22508 | 22513 | 0.691 | 282.606 | 282.669 | -0.063 | 66.2 |
| 32 | 22542 | 22545 | 0.670 | 283.033 | 283.071 | -0.038 | 66.3 |
| 32 | 22576 | 22577 | 0.670 | 283.460 | 283.472 | -0.013 | 66.4 |
| 31 | 22610 | 22608 | 0.649 | 283.887 | 283.862 | 0.025 | 66.5 |
| 32 | 22644 | 22640 | 0.670 | 284.314 | 284.263 | 0.050 | 66.6 |
| 33 | 22678 | 22673 | 0.691 | 284.741 | 284.678 | 0.063 | 66.7 |
| 34 | 22712 | 22707 | 0.711 | 285.167 | 285.105 | 0.063 | 66.8 |
| 35 | 22746 | 22742 | 0.732 | 285.594 | 285.544 | 0.050 | 66.9 |
| 35 | 22780 | 22777 | 0.732 | 286.021 | 285.984 | 0.038 | 67.0 |
| 35 | 22814 | 22812 | 0.732 | 286.448 | 286.423 | 0.025 | 67.1 |
| 35 | 22848 | 22847 | 0.732 | 286.875 | 286.862 | 0.013 | 67.2 |
| 36 | 22882 | 22883 | 0.753 | 287.302 | 287.314 | -0.013 | 67.3 |
| 37 | 22916 | 22920 | 0.774 | 287.729 | 287.779 | -0.050 | 67.4 |
| 39 | 22950 | 22959 | 0.816 | 288.156 | 288.269 | -0.113 | 67.5 |
| 34 | 22984 | 22993 | 0.711 | 288.583 | 288.696 | -0.113 | 67.6 |
| 30 | 23018 | 23023 | 0.628 | 289.009 | 289.072 | -0.063 | 67.7 |
| 31 | 23052 | 23054 | 0.649 | 289.436 | 289.461 | -0.025 | 67.8 |


| 31 | 23086 | 23085 | 0.649 | 289.863 | 289.851 | 0.013 | 67.9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 31 | 23120 | 23116 | 0.649 | 290.290 | 290.240 | 0.050 | 68.0 |
| 32 | 23154 | 23148 | 0.670 | 290.717 | 290.642 | 0.075 | 68.1 |
| 34 | 23188 | 23182 | 0.711 | 291.144 | 291.069 | 0.075 | 68.2 |
| 35 | 23222 | 23217 | 0.732 | 291.571 | 291.508 | 0.063 | 68.3 |
| 35 | 23256 | 23252 | 0.732 | 291.998 | 291.948 | 0.050 | 68.4 |
| 35 | 23290 | 23287 | 0.732 | 292.425 | 292.387 | 0.038 | 68.5 |
| 36 | 23324 | 23323 | 0.753 | 292.852 | 292.839 | 0.013 | 68.6 |
| 36 | 23358 | 23359 | 0.753 | 293.278 | 293.291 | -0.013 | 68.7 |
| 35 | 23392 | 23394 | 0.732 | 293.705 | 293.730 | -0.025 | 68.8 |
| 36 | 23426 | 23430 | 0.753 | 294.132 | 294.182 | -0.050 | 68.9 |
| 35 | 23460 | 23465 | 0.732 | 294.559 | 294.622 | -0.063 | 69.0 |
| 34 | 23494 | 23499 | 0.711 | 294.986 | 295.049 | -0.063 | 69.1 |
| 34 | 23528 | 23533 | 0.711 | 295.413 | 295.476 | -0.063 | 69.2 |
| 32 | 23562 | 23565 | 0.670 | 295.840 | 295.878 | -0.038 | 69.3 |
| 31 | 23596 | 23596 | 0.649 | 296.267 | 296.267 | 0.000 | 69.4 |
| 32 | 23630 | 23628 | 0.670 | 296.694 | 296.669 | 0.025 | 69.5 |
| 32 | 23664 | 23660 | 0.670 | 297.121 | 297.070 | 0.050 | 69.6 |
| 33 | 23698 | 23693 | 0.691 | 297.547 | 297.485 | 0.063 | 69.7 |
| 34 | 23732 | 23727 | 0.711 | 297.974 | 297.912 | 0.063 | 69.8 |
| 34 | 23766 | 23761 | 0.711 | 298.401 | 298.338 | 0.063 | 69.9 |
| 36 | 23800 | 23797 | 0.753 | 298.828 | 298.790 | 0.038 | 70.0 |
| 35 | 23834 | 23832 | 0.732 | 299.255 | 299.230 | 0.025 | 70.1 |
| 36 | 23868 | 23868 | 0.753 | 299.682 | 299.682 | 0.000 | 70.2 |
| 36 | 23902 | 23904 | 0.753 | 300.109 | 300.134 | -0.025 | 70.3 |
| 37 | 23936 | 23941 | 0.774 | 300.536 | 300.598 | -0.063 | 70.4 |
| 35 | 23970 | 23976 | 0.732 | 300.963 | 301.038 | -0.075 | 70.5 |
| 33 | 24004 | 24009 | 0.691 | 301.390 | 301.452 | -0.063 | 70.6 |
| 33 | 24038 | 24042 | 0.691 | 301.816 | 301.867 | -0.050 | 70.7 |
| 32 | 24072 | 24074 | 0.670 | 302.243 | 302.268 | -0.025 | 70.8 |
| 32 | 24106 | 24106 | 0.670 | 302.670 | 302.670 | 0.000 | 70.9 |
| 31 | 24140 | 24137 | 0.649 | 303.097 | 303.059 | 0.038 | 71.0 |
| 32 | 24174 | 24169 | 0.670 | 303.524 | 303.461 | 0.063 | 71.1 |
| 35 | 24208 | 24204 | 0.732 | 303.951 | 303.901 | 0.050 | 71.2 |
| 34 | 24242 | 24238 | 0.711 | 304.378 | 304.328 | 0.050 | 71.3 |
| 35 | 24276 | 24273 | 0.732 | 304.805 | 304.767 | 0.038 | 71.4 |
| 36 | 24310 | 24309 | 0.753 | 305.232 | 305.219 | 0.013 | 71.5 |
| 36 | 24344 | 24345 | 0.753 | 305.658 | 305.671 | -0.013 | 71.6 |
| 36 | 24378 | 24381 | 0.753 | 306.085 | 306.123 | -0.038 | 71.7 |
| 35 | 24412 | 24416 | 0.732 | 306.512 | 306.563 | -0.050 | 71.8 |
| 36 | 24446 | 24452 | 0.753 | 306.939 | 307.015 | -0.075 | 71.9 |
| 35 | 24480 | 24487 | 0.732 | 307.366 | 307.454 | -0.088 | 72.0 |
| 32 | 24514 | 24519 | 0.670 | 307.793 | 307.856 | -0.063 | 72.1 |
| 31 | 24548 | 24550 | 0.649 | 308.220 | 308.245 | -0.025 | 72.2 |
| 32 | 24582 | 24582 | 0.670 | 308.647 | 308.647 | 0.000 | 72.3 |
| 31 | 24616 | 24613 | 0.649 | 309.074 | 309.036 | 0.038 | 72.4 |
| 33 | 24650 | 24646 | 0.691 | 309.501 | 309.450 | 0.050 | 72.5 |
| 33 | 24684 | 24679 | 0.691 | 309.927 | 309.865 | 0.063 | 72.6 |
| 34 | 24718 | 24713 | 0.711 | 310.354 | 310.292 | 0.063 | 72.7 |
| 35 | 24752 | 24748 | 0.732 | 310.781 | 310.731 | 0.050 | 72.8 |
| 35 | 24786 | 24783 | 0.732 | 311.208 | 311.170 | 0.038 | 72.9 |
| 34 | 24820 | 24817 | 0.711 | 311.635 | 311.597 | 0.038 | 73.0 |
| 36 | 24854 | 24853 | 0.753 | 312.062 | 312.049 | 0.013 | 73.1 |


| 35 | 24888 | 24888 | 0.732 | 312.489 | 312.489 | 0.000 | 73.2 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 36 | 24922 | 24924 | 0.753 | 312.916 | 312.941 | -0.025 | 73.3 |
| 37 | 24956 | 24961 | 0.774 | 313.343 | 313.405 | -0.063 | 73.4 |
| 34 | 24990 | 24995 | 0.711 | 313.770 | 313.832 | -0.063 | 73.5 |
| 33 | 25024 | 25028 | 0.691 | 314.196 | 314.247 | -0.050 | 73.6 |
| 33 | 25058 | 25061 | 0.691 | 314.623 | 314.661 | -0.038 | 73.7 |
| 33 | 25092 | 25094 | 0.691 | 315.050 | 315.075 | -0.025 | 73.8 |
| 32 | 25126 | 25126 | 0.670 | 315.477 | 315.477 | 0.000 | 73.9 |
| 32 | 25160 | 25158 | 0.670 | 315.904 | 315.879 | 0.025 | 74.0 |
| 32 | 25194 | 25190 | 0.670 | 316.331 | 316.281 | 0.050 | 74.1 |
| 35 | 25228 | 25225 | 0.732 | 316.758 | 316.720 | 0.038 | 74.2 |
| 34 | 25262 | 25259 | 0.711 | 317.185 | 317.147 | 0.038 | 74.3 |
| 33 | 25296 | 25292 | 0.691 | 317.612 | 317.561 | 0.050 | 74.4 |
| 35 | 25330 | 25327 | 0.732 | 318.039 | 318.001 | 0.038 | 74.5 |
| 37 | 25364 | 25364 | 0.774 | 318.465 | 318.465 | 0.000 | 74.6 |
| 36 | 25398 | 25400 | 0.753 | 318.892 | 318.917 | -0.025 | 74.7 |
| 35 | 25432 | 25435 | 0.732 | 319.319 | 319.357 | -0.038 | 74.8 |
| 36 | 25466 | 25471 | 0.753 | 319.746 | 319.809 | -0.063 | 74.9 |
| 34 | 25500 | 25505 | 0.711 | 320.173 | 320.236 | -0.063 | 75.0 |
| 33 | 25534 | 25538 | 0.691 | 320.600 | 320.650 | -0.050 | 75.1 |
| 32 | 25568 | 25570 | 0.670 | 321.027 | 321.052 | -0.025 | 75.2 |
| 32 | 25602 | 25602 | 0.670 | 321.454 | 321.454 | 0.000 | 75.3 |
| 32 | 25636 | 25634 | 0.670 | 321.881 | 321.855 | 0.025 | 75.4 |
| 32 | 25670 | 25666 | 0.670 | 322.307 | 322.257 | 0.050 | 75.5 |
| 33 | 25704 | 25699 | 0.691 | 322.734 | 322.672 | 0.063 | 75.6 |
| 34 | 25738 | 25733 | 0.711 | 323.161 | 323.098 | 0.063 | 75.7 |
| 35 | 25772 | 25768 | 0.732 | 323.588 | 323.538 | 0.050 | 75.8 |
| 35 | 25806 | 25803 | 0.732 | 324.015 | 323.977 | 0.038 | 75.9 |
| 36 | 25840 | 25839 | 0.753 | 324.442 | 324.429 | 0.013 | 76.0 |
| 36 | 25874 | 25875 | 0.753 | 324.869 | 324.881 | -0.013 | 76.1 |
| 36 | 25908 | 25911 | 0.753 | 325.296 | 325.333 | -0.038 | 76.2 |
| 35 | 25942 | 25946 | 0.732 | 325.723 | 325.773 | -0.050 | 76.3 |
| 35 | 25976 | 25981 | 0.732 | 326.150 | 326.212 | -0.063 | 76.4 |
| 34 | 26010 | 26015 | 0.711 | 326.576 | 326.639 | -0.063 | 76.5 |
| 33 | 26044 | 26048 | 0.691 | 327.003 | 327.054 | -0.050 | 76.6 |
| 32 | 26078 | 26080 | 0.670 | 327.430 | 327.455 | -0.025 | 76.7 |
| 31 | 26112 | 26111 | 0.649 | 327.857 | 327.845 | 0.013 | 76.8 |
| 32 | 26146 | 26143 | 0.670 | 328.284 | 328.246 | 0.038 | 76.9 |
| 33 | 26180 | 26176 | 0.691 | 328.711 | 328.661 | 0.050 | 77.0 |
| 33 | 26214 | 26209 | 0.691 | 329.138 | 329.075 | 0.063 | 77.1 |
| 35 | 26248 | 26244 | 0.732 | 329.565 | 329.515 | 0.050 | 77.2 |
| 34 | 26282 | 26278 | 0.711 | 329.992 | 329.941 | 0.050 | 77.3 |
| 36 | 26316 | 26314 | 0.753 | 330.419 | 330.393 | 0.025 | 77.4 |
| 36 | 26350 | 26350 | 0.753 | 330.845 | 330.845 | 0.000 | 77.5 |
| 37 | 26384 | 26387 | 0.774 | 331.272 | 331.310 | -0.038 | 77.6 |
| 37 | 26418 | 26424 | 0.774 | 331.699 | 331.775 | -0.075 | 77.7 |
| 35 | 26452 | 26459 | 0.732 | 332.126 | 332.214 | -0.088 | 77.8 |
| 33 | 26486 | 26492 | 0.691 | 332.553 | 332.628 | -0.075 | 77.9 |
| 33 | 26520 | 26525 | 0.691 | 332.980 | 333.043 | -0.063 | 78.0 |
| 32 | 26554 | 26557 | 0.670 | 333.407 | 333.444 | -0.038 | 78.1 |
| 31 | 26588 | 26588 | 0.649 | 333.834 | 333.834 | 0.000 | 78.2 |
| 31 | 26622 | 26619 | 0.649 | 334.261 | 334.223 | 0.038 | 78.3 |
| 33 | 26656 | 26652 | 0.691 | 334.688 | 334.637 | 0.050 | 78.4 |


| 32 | 26690 | 26684 | 0.670 | 335.114 | 335.039 | 0.075 | 78.5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 34 | 26724 | 26718 | 0.711 | 335.541 | 335.466 | 0.075 | 78.6 |
| 35 | 26758 | 26753 | 0.732 | 335.968 | 335.905 | 0.063 | 78.7 |
| 36 | 26792 | 26789 | 0.753 | 336.395 | 336.357 | 0.038 | 78.8 |
| 34 | 26826 | 26823 | 0.711 | 336.822 | 336.784 | 0.038 | 78.9 |
| 36 | 26860 | 26859 | 0.753 | 337.249 | 337.236 | 0.013 | 79.0 |
| 39 | 26894 | 26898 | 0.816 | 337.676 | 337.726 | -0.050 | 79.1 |
| 35 | 26928 | 26933 | 0.732 | 338.103 | 338.165 | -0.063 | 79.2 |
| 34 | 26962 | 26967 | 0.711 | 338.530 | 338.592 | -0.063 | 79.3 |
| 34 | 26996 | 27001 | 0.711 | 338.956 | 339.019 | -0.063 | 79.4 |
| 34 | 27030 | 27035 | 0.711 | 339.383 | 339.446 | -0.063 | 79.5 |
| 32 | 27064 | 27067 | 0.670 | 339.810 | 339.848 | -0.038 | 79.6 |
| 31 | 27098 | 27098 | 0.649 | 340.237 | 340.237 | 0.000 | 79.7 |
| 32 | 27132 | 27130 | 0.670 | 340.664 | 340.639 | 0.025 | 79.8 |
| 32 | 27166 | 27162 | 0.670 | 341.091 | 341.041 | 0.050 | 79.9 |
| 32 | 27200 | 27194 | 0.670 | 341.518 | 341.443 | 0.075 | 80.0 |
| 34 | 27234 | 27228 | 0.711 | 341.945 | 341.869 | 0.075 | 80.1 |
| 35 | 27268 | 27263 | 0.732 | 342.372 | 342.309 | 0.063 | 80.2 |
| 36 | 27302 | 27299 | 0.753 | 342.799 | 342.761 | 0.038 | 80.3 |
| 34 | 27336 | 27333 | 0.711 | 343.225 | 343.188 | 0.038 | 80.4 |
| 36 | 27370 | 27369 | 0.753 | 343.652 | 343.640 | 0.013 | 80.5 |
| 36 | 27404 | 27405 | 0.753 | 344.079 | 344.092 | -0.013 | 80.6 |
| 36 | 27438 | 27441 | 0.753 | 344.506 | 344.544 | -0.038 | 80.7 |
| 37 | 27472 | 27478 | 0.774 | 344.933 | 345.008 | -0.075 | 80.8 |
| 34 | 27506 | 27512 | 0.711 | 345.360 | 345.435 | -0.075 | 80.9 |
| 33 | 27540 | 27545 | 0.691 | 345.787 | 345.850 | -0.063 | 81.0 |
| 32 | 27574 | 27577 | 0.670 | 346.214 | 346.251 | -0.038 | 81.1 |
| 31 | 27608 | 27608 | 0.649 | 346.641 | 346.641 | 0.000 | 81.2 |
| 32 | 27642 | 27640 | 0.670 | 347.068 | 347.042 | 0.025 | 81.3 |
| 31 | 27676 | 27671 | 0.649 | 347.494 | 347.432 | 0.063 | 81.4 |
| 33 | 27710 | 27704 | 0.691 | 347.921 | 347.846 | 0.075 | 81.5 |
| 34 | 27744 | 27738 | 0.711 | 348.348 | 348.273 | 0.075 | 81.6 |
| 35 | 27778 | 27773 | 0.732 | 348.775 | 348.712 | 0.063 | 81.7 |
| 35 | 27812 | 27808 | 0.732 | 349.202 | 349.152 | 0.050 | 81.8 |
| 35 | 27846 | 27843 | 0.732 | 349.629 | 349.591 | 0.038 | 81.9 |
| 36 | 27880 | 27879 | 0.753 | 350.056 | 350.043 | 0.013 | 82.0 |
| 35 | 27914 | 27914 | 0.732 | 350.483 | 350.483 | 0.000 | 82.1 |
| 37 | 27948 | 27951 | 0.774 | 350.910 | 350.947 | -0.038 | 82.2 |
| 36 | 27982 | 27987 | 0.753 | 351.336 | 351.399 | -0.063 | 82.3 |
| 34 | 28016 | 28021 | 0.711 | 351.763 | 351.826 | -0.063 | 82.4 |
| 33 | 28050 | 28054 | 0.691 | 352.190 | 352.241 | -0.050 | 82.5 |
| 34 | 28084 | 28088 | 0.711 | 352.617 | 352.667 | -0.050 | 82.6 |
| 31 | 28118 | 28119 | 0.649 | 353.044 | 353.057 | -0.013 | 82.7 |
| 31 | 28152 | 28150 | 0.649 | 353.471 | 353.446 | 0.025 | 82.8 |
| 34 | 28186 | 28184 | 0.711 | 353.898 | 353.873 | 0.025 | 82.9 |
| 32 | 28220 | 28216 | 0.670 | 354.325 | 354.275 | 0.050 | 83.0 |
| 33 | 28254 | 28249 | 0.691 | 354.752 | 354.689 | 0.063 | 83.1 |
| 33 | 28288 | 28282 | 0.691 | 355.179 | 355.103 | 0.075 | 83.2 |
| 35 | 28322 | 28317 | 0.732 | 355.605 | 355.543 | 0.063 | 83.3 |
| 35 | 28356 | 28352 | 0.732 | 356.032 | 355.982 | 0.050 | 83.4 |
| 38 | 28390 | 28390 | 0.795 | 356.459 | 356.459 | 0.000 | 83.5 |
| 37 | 28424 | 28427 | 0.774 | 356.886 | 356.924 | -0.038 | 83.6 |
| 36 | 28458 | 28463 | 0.753 | 357.313 | 357.376 | -0.063 | 83.7 |


| 35 | 28492 | 28498 | 0.732 | 357.740 | 357.815 | -0.075 | 83.8 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 33 | 28526 | 28531 | 0.691 | 358.167 | 358.230 | -0.063 | 83.9 |
| 32 | 28534 | 28563 | 0.670 | 358.267 | 358.631 | -0.364 | 84.0 |
| 28 | 28542 | 28591 | 0.586 | 358.368 | 358.983 | -0.615 | 84.1 |
| 23 | 28550 | 28614 | 0.481 | 358.468 | 359.272 | -0.804 | 84.2 |
| 16 | 28558 | 28630 | 0.335 | 358.569 | 359.473 | -0.904 | 84.3 |
| 11 | 28566 | 28641 | 0.230 | 358.669 | 359.611 | -0.942 | 84.4 |
| 6 | 28574 | 28647 | 0.126 | 358.770 | 359.686 | -0.917 | 84.5 |
| 1 | 28582 | 28648 | 0.021 | 358.870 | 359.699 | -0.829 | 84.6 |
| 4 | 28590 | 28652 | 0.084 | 358.970 | 359.749 | -0.778 | 84.7 |
| 5 | 28598 | 28657 | 0.105 | 359.071 | 359.812 | -0.741 | 84.8 |
| 6 | 28606 | 28663 | 0.126 | 359.171 | 359.887 | -0.716 | 84.9 |
| 6 | 28614 | 28669 | 0.126 | 359.272 | 359.962 | -0.691 | 85.0 |
| 5 | 28622 | 28674 | 0.105 | 359.372 | 360.025 | -0.653 | 85.1 |
| 1 | 28630 | 28675 | 0.021 | 359.473 | 360.038 | -0.565 | 85.2 |
| 0 | 28638 | 28675 | 0.000 | 359.573 | 360.038 | -0.465 | 85.3 |
| 0 | 28646 | 28675 | 0.000 | 359.674 | 360.038 | -0.364 | 85.4 |
| 0 | 28654 | 28675 | 0.000 | 359.774 | 360.038 | -0.264 | 85.5 |
| 0 | 28662 | 28675 | 0.000 | 359.874 | 360.038 | -0.163 | 85.6 |
| 0 | 28670 | 28675 | 0.000 | 359.975 | 360.038 | -0.063 | 85.7 |
| 0 | 28672 | 28675 | 0.000 | 360.000 | 360.038 | -0.038 | 85.8 |

## Appendix G

Note: only a sample of the engineering drawings created during this research are located in this appendix. This is due to the extensive number of drawings that were necessary for the fabrication of the library of modules ( +80 drawings). The drawings used in the manufacturing of ALL MRM modules are located on the supplementary DVD disk.

## Mechanical Drawings for Base Module



Figure G.1: Assembly of Base Module (View One)


Figure G.2: Assembly of Base Module (View Two)


Figure G.3: Bed Carriage - Part One


Figure G.4: Brass Collar

Quantity: 2
Material: Steel Supplied


| University of Kwa-Zulu Natal School of Mechanical Engineering | Orrogreptic Recieation | Sche 2:1 |  | Tme | Coupling-Base Shared Components |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\square$ OR ¢ $¢$ | unts: $=$ m |  |  |  |  |  |
|  |  | Oite | Cheobs | moiect RMS Project |  |  |  |
|  |  |  |  | Stucent name Jared Padayachee$1227$ |  |  |  |
|  | Tolnical Nasoger |  |  |  |  |  |  |  |  |  |

Figure G.5: Motor Coupling


Figure G.6: Lead Screw


Figure G.7: Supporting Plate for Slide/Carriage Mechanism


Figure G.8: Motor Spacer


Figure G.9: Bed Carriage - Part Two


Figure G.10: Bearing Housing


Figure G.11: Bearing Housing Cap

## Appendix H

## Final Specifications for MRM Modules and Assemblies

Table H.1: Specifications for MRM Modules and Assemblies

| Specifications | Prescribed | Final |
| :---: | :---: | :---: |
| General |  |  |
| Processing functions | Drilling and Turning | Drilling and Turning |
| Machinable Materials | Wax and Plastic | Wax and Plastic |
| Drilling - degrees of freedom | 3-6 | 3-6 |
| Turning - degrees of freedom | 2-3 | 2-3 |
| Motion Modules (Modular Axes) |  |  |
| Linear Axes |  |  |
| Maximum speed of at least | $100 \mathrm{~mm} / \mathrm{min}$ | $116 \mathrm{~mm} / \mathrm{min}$ |
| Worst Accuracy | 1 mm | 0.038 mm |
| Worst Repeatability | 0.5 mm | 0.035 mm |
| Rotary Axes |  |  |
| Maximum speed of at least | $1 \mathrm{rev} / \mathrm{min}$ | $1 \mathrm{rev} / \mathrm{min}$ |
| Worst Accuracy | $1.5{ }^{\circ}$ | $3.164^{\circ}$ |
| Worst Repeatability | $1^{\circ}$ | $2.812^{\circ}$ |
| Process Modules (Modular Cutting Heads) |  |  |
| Drilling capacity | $1 \mathrm{~mm}-10 \mathrm{~mm}$ | $0.5 \mathrm{~mm}-12 \mathrm{~mm}$ |
| Drilling speeds | Not Specified | $700 \mathrm{rev} / \mathrm{min}$ (unloaded) |
| Drilling Motor Power | Not Specified | 80 watts |
| Turning Capacity | 100 mm | 120 mm |
| Turning Spindle Hole | Not Specified | 24 mm |
| Turning Speeds | Not Specified | 315 to $1054 \mathrm{rev} / \mathrm{min}$ |
| Turning Motor Power | Not Specified | 550 watts |
| Drilling Assemblies |  |  |
| Work table size | 100 mm by 100 mm | 100 mm by 100 mm |
| Maximum part size | $\begin{aligned} & 100 \mathrm{~mm} \times 100 \mathrm{~mm} \\ & \times 100 \mathrm{~mm} \end{aligned}$ | $\begin{aligned} & 10 \mathrm{~mm} \times 100 \mathrm{~mm} \mathrm{x} \\ & 100 \mathrm{~mm} \end{aligned}$ |
| Turning Assemblies |  |  |
| Maximum part length of at least | 400 mm | 500 mm |
| Maximum swing over bed of at least | 300 mm | 420 mm |
| Electrical Specifications |  |  |
| Operating voltage | 220 volts, AC current | 220 volts, AC current |
| Digital electronics power supply | 12 volts, DC current | 12 volts, DC current |
| Software Specifications |  |  |
| Software programming languages | C/C++ | C/C++ |
| Machine operating system | Linux | Linux |
| Machine programming language | Simplified G-Code | Simplified G-Code |

## Appendix I

## Sample C++ Code for Host PC

Note: only a seventeen page sample of the C++ code that was written for the host PC has been included in this appendix (not the entire host PC code). This is due to the lengthy amount of code that was written for the host PC, the servo communication module, servo control modules and spindle control modules. The C and C++ code that was written for the entire control system is located on the supplementary DVD disk.

## //main. cpp (initializes machine GUI)

```
#include <qapplication.h>
#include "MRMmain.h"
int main( int argc, char ** argv )
{
    QApplication a( argc, argv );
    MRMmain w;
    w.show();
    a.connect( &a, SIGNAL( lastWindowClosed() ), &a, SLOT( quit() ) );
    return a.exec();
}
#include "codemanip.h"
#include "execute.h"
#include "Transmission_Control.h"
#include "mrm_error.h"
```

//MRMmain.ui(initializes functions that are called through GUI)

```
void MRMmain::sortAndSave()
{
    int lineNumber=0;
    int lines= codeEdit->lines();
    int error;
    int linear;
    int angular;
    int second;
//create code storgae data object
    codeManip code;
    code.PWarninglineEdit=WarninglineEdit;
    code.PStatuslineEdit=StatuslineEdit;
    code.PcodeEdit=codeEdit;
    code.PprogressBar=progressBar;
//initialize progress ber
    progressBar->setTotalSteps(lines);
//Store the MRMs current configuration
    linear=linear_axis_combo->currentItem();
    angular=angular_axis_combo->currentItem();
    second=second_a\overline{xis_cōmbo->currentItem();}
    code.storeConfiguration(linear,angular,second);
```

```
// check and store lines of code one at a time
    while(lineNumber<lines)
    { error=code.codeGet(lineNumber);
        if(error>0) //N.B error reporting handled by other functions
        {break;}
        else{ progressBar->setProgress(lineNumber+1);
            ++lineNumber;}
    }
//report sucessful storage once all lines are done
    if(lineNumber==lines)
    {StatuslineEdit->setText("Code Storage Successful");
        WarninglineEdit->setText("No Warnings");
    }
}
void MRMmain::codeExecute()
{
LineExecute Line;
int SerialSpeed;
int box=0;
Line.PWarninglineEdit=WarninglineEdit;// grant access to warning line
Line.PStatuslineEdit=StatuslineEdit;//grant access to status line
Line.PSpindlePortlineEdit=USB1lineEdit;
Line.PServoPortlineEdit=USB2lineEdit;
Line.PTIPOlineEdit=TIPOlineEdit;
Line.PcodeEdit=codeEdit;// grant access to code editting box
Line.PprogressBar=progressBar;// grant access to progress bar
box=SpeedcomboBox->currentItem();
switch(box)
{
case 0:
    SerialSpeed=2400;
    break;
case 1:
    SerialSpeed=4800;
    break;
case 2:
    SerialSpeed=9600;
    break;
case 3:
    SerialSpeed=19200;
    break;
case 4:
    SerialSpeed=38400;
    break;
default:
        SerialSpeed=9600;
        break;
}
Line.Start(SerialSpeed);
}
```

```
void MRMmain::vibrationMonitor( bool state )
{
TransmissionControl readPort;
char sensorReading[2];
const char *PortName;
int SerialSpeed;
int acceleration=0;
int box=0;
int error=0;
PortName= new char[strlen(USB1lineEdit->text())];
PortName=USB1lineEdit->text();
vibrationBar->setTotalSteps(20);
switch(box)
{
case 0:
    SerialSpeed=2400;
    break;
case 1:
    SerialSpeed=4800;
    break;
case 2:
    SerialSpeed=9600;
    break;
case 3:
    SerialSpeed=19200;
    break;
case 4:
    SerialSpeed=38400;
    break;
default:
    SerialSpeed=9600;
    break;
}
box=SpeedcomboBox->currentItem();
if(state==TRUE)
    {
    //while(1)
    {
        error=readPort.serialReceive(PortName,SerialSpeed, sensorReading,
2);
        switch(error)
        {
        case PORT_OPEN_FAIL:
            WarninglineEdit->setText("Failed To Open Serial Port");
            break;
        case PORT_READ_FAIL:
            WarninglineEdit->setText("Failed To Read Serial Port");
            break;
        case PORT_CLOSE_FAIL:
            WarninglineEdit->setText("Failed To Close Serial Port");
            break;
        default:
    break;
        }
```

```
        vibrationBar->setProgress(10);
        vibration_LCD->display(9);
        //break;
    }
}
}
```


## //Codemanip.h (text interpreter, error checking and code storage)

```
#ifndef CODEMANIP H
#define CODEMANIP H
#include <qlineedit.h>
#include <qtextedit.h>
#include <qprogressbar.h>
#include <qcombobox.h>
class codeManip{
public:
    codeManip();
    ~codeManip();
    void resetVariables();
    int codeGet(int);
    int codeSyntaxFilter();
    void storeConfiguration(int, int, int);
    int codeSort();
    int codeInterpret(int, const char*);// reads values into variables
    int check_G();
    int check_M();
    int check_R();
    int check_Arc();
    int codeSave();//writes to file
    QLineEdit *PWarninglineEdit; //pointer to warning line
    QLineEdit *PStatuslineEdit;//pointer to status line
    QTextEdit *PcodeEdit;//pointer to code edit box
    QProgressBar *PprogressBar;//pointer to progress bar
private:
    const char *codeLineHold;
    int N;//line number
    int M;// miscellanoues functions
    int G;// function
    float A; // rotation about x
    float B; // rotation about y
    float C;//rotation about z
    float X;
    float Y;
    float Z;
    float U;
    float V;
    float W;
    float S;// spindle speed
    float F;// feed rate
    float I;// arc about X
    float J;//are about Y
    float K;//arc about Z
    float R; // radius
    //Axis Activation Code
```

```
    unsigned char a;
    unsigned char b;
    unsigned char c;
    unsigned char x;
    unsigned char y;
    unsigned char z;
    unsigned char u;
    unsigned char v;
    unsigned char w;
};
#endif
```


## //Codemanip.cpp (text interpreter, error checking and code storage

```
#include <string.h>
```

\#include <string.h>
\#include <stdlib.h>
\#include <stdlib.h>
\#include <stdio.h>
\#include <stdio.h>
\#include "codemanip.h"
\#include "codemanip.h"
\#include "mrm_error.h"
\#include "mrm_error.h"
codeManip::codeManip()
codeManip::codeManip()
{
{
// clear code.dat file
// clear code.dat file
FILE *fp;
FILE *fp;
fp=fopen("code.dat","w");
fp=fopen("code.dat","w");
fclose(fp);
fclose(fp);
// reset kinematic configuration variables
// reset kinematic configuration variables
a=0;
a=0;
b=0;
b=0;
C=0;
C=0;
x=0;
x=0;
y=0;
y=0;
z=0;
z=0;
u=0;
u=0;
v=0;
v=0;
w=0;
w=0;
//reset
//reset
resetVariables();
resetVariables();
}
}
codeManip::~codeManip()
{;}
void codeManip::resetVariables()
{
N=0;//line number
M=100;// miscellanoues functions N.B 100 is the default value if it
is not overwritten in code
G=100;// function
A=0; // rotation about x
B=0; // rotation about y
C=0;//rotation about z
X=0;// linear x
Y=0;// inear Y
Z=0;// linear z
U=0;// 2nd x
V=0;// 2nd Y
W=0;//2nd z
S=0;// spindle speed
F=0;// feed rate

```
```

    I=0;// arc about X
    J=0;//are about Y
    K=0;// arc about Z
    R=0;// radius
    }
void codeManip::storeConfiguration(int linear_box, int angular_box ,int
second_box)
{
// store linear kinematic config
switch(linear_box)
{
case 0:
x=y=z=0;
break;
case 1:
x=1;
break;
case 2:
y=1;
break;
case 3:
z=1;
break;
case 4:
x=y=1;
break;
case 5:
x=z=1;
break;
case 6:
y=z=1;
break;
case 7:
x=y=z=1;
break;
}
//store angular kinematic config
switch(angular_box)
{
case 0:
a=b=c=0;
break;
case 1:
a=1;
break;
case 2:
b=1;
break;
case 3:
c=1;
break;
case 4:
a=b=1;
case 5:
a=c=1;
break;
case 6:
b=c=1;
break;

```
```

    case 7:
        a=b=c=1;
        break;
    }
    // store secondry axis config
switch(second box)
{
case 0:
u}=\textrm{v}=\textrm{w}=0\mathrm{ ;
break;
case 1:
u=1;
break;
case 2:
v=1;
break;
case 3:
w=1;
break;
case 4:
u=v=1;
case 5:
u=w=1;
break;
case 6:
v=W=1;
break;
case 7:
u=v=w=1;
break;
}
}
int codeManip::codeGet(int lineCounter)
{
int error;
//return 1 = syntax error; return 2 = inactive axis
//return 3 = not supported by current configuration; return 4 = not
available on this machine
//Obtain a line of code for processinf
codeLineHold= new char[strlen(PcodeEdit->text(lineCounter))];
if(codeLineHold==NULL)
{PWarninglineEdit->setText("ERROR: Dynamic Memory Allocation
Failed");
return 1;
}
codeLineHold=PcodeEdit->text(lineCounter);
//Filter line of code for syntax errors
error=codeSyntaxFilter();
if(error==1)
{PWarninglineEdit->setText("ERROR: Code Syntax");
PStatuslineEdit-
>setText(QString::number(lineCounter+1,'f',0));
return 1;
}

```
```

//sort text code and convert to numerical values
error=codeSort();
switch(error)
{
case CODE_SYNTAX_ERROR:
PWarninglineEdit->setText("ERROR: Code Syntax Error");
PStatuslineEdit->setText(QString::number(lineCounter+1,'f',0));
return 1;
case AXIS INACTIVE:
PWarninglineEdit->setText("ERROR: Axis Inactive In Current
Configuration");
PStatuslineEdit->setText(QString::number(lineCounter+1,'f',0));
return 1;
case INVALID_IN_CONFIGURATION:
PWarninglineEdit->setText("ERROR: Command Invalid In Current
Configuration");
PStatuslineEdit->setText(QString::number(lineCounter+1,'f',0));
return 1;
case FUNCTION_NOT_AVAILABLE:
PWarninglīneE\overline{d}it->setText("ERROR: Function Not Available On
Platform");
PStatuslineEdit->setText(QString::number(lineCounter+1,'f',0));
return 1;
}
//store the line of processed code in code.dat file
error=codeSave();
if(error==1)
{ PWarninglineEdit->setText("ERROR: Code Storage Failed");
PStatuslineEdit-
>setText(QString::number(lineCounter+1,'f',0));
}
//reset g-code variables for next stage of sort and store
resetVariables();
return 0;
}
int codeManip::codeSyntaxFilter()
{
int length=strlen(codeLineHold);
int counter;
for(counter=0; counter<length; counter++)
{
switch(codeLineHold[counter])
{
case 'N':
break;
case 'M':
break;
case 'G':
break;
// axis word addresses
case 'A':
break;
case 'B':
break;
case 'C':
break;

```
```

    case 'X':
        break;
        case 'Y':
        break;
        case 'Z':
        break;
    case 'U':
        break;
        case 'V':
        break;
    case 'W':
        break;
    // other word addresses
case 'S':
break;
case 'F':
break;
case 'I':
break;
case 'J':
break;
case 'K':
break;
case 'R':
break;
// numerical characters etc
case ' ':
break;
case '-':
break;
case '.':
break;
case '0':
break;
case '1':
break;
case '2':
break;
case '3':
break;
case '4':
break;
case '5':
break;
case '6':
break;
case '7':
break;
case '8':
break;
case '9':
break;
default:
return CODE_SYNTAX_ERROR;
}// end of switch
}//end of for check loop
return 0;
}
int codeManip::codeSort()
{
int length=strlen(codeLineHold);

```
```

    int counter;
    int error=0;
    char holder[7];
    int variableNumber=0;
    int holderPlace=0;
    const char reset[]="xxxxxxx";
    strcpy(holder,reset);
    for(counter=0; counter<length; counter++)
{
switch(codeLineHold[counter])
{
case 'N':
if(variableNumber>0)
{error=codeInterpret(variableNumber, holder);
if(error>0)
{return error;}
holderPlace=0;
strcpy(holder,reset);
}
variableNumber=1;
break;
case 'M':
if(variableNumber>0)
{error=codeInterpret(variableNumber, holder);
if(error>0)
{return error;}
holderPlace=0;
strcpy(holder,reset);
}
variableNumber=2;
break;
case 'G':
if(variableNumber>0)
{error=codeInterpret(variableNumber, holder);
if(error>0)
{return error;}
holderPlace=0;
strcpy(holder,reset);
}
variableNumber=3;
break;
case 'A':
if(variableNumber>0) // call store on previous string item
{error=codeInterpret(variableNumber, holder);
if(error>0)
{return error;}
holderPlace=0;
strcpy(holder,reset);
}
variableNumber=4;
break;
case 'B':
if(variableNumber>0)
{error=codeInterpret(variableNumber, holder);
if(error>0)
{return error;}
holderPlace=0;
strcpy(holder,reset);
}
variableNumber=5;

```
```

    break;
    case 'C':
if(variableNumber>0)
{error=codeInterpret(variableNumber, holder);
if(error>0)
{return error;}
holderPlace=0;
strcpy(holder,reset);
}
variableNumber=6;
break;
case 'X':
if(variableNumber>0)
{error=codeInterpret(variableNumber, holder);
if(error>0)
{return error;}
holderPlace=0;
strcpy(holder,reset);
}
variableNumber=7;
break;
case 'Y':
if(variableNumber>0)
{error=codeInterpret(variableNumber, holder);
if(error>0)
{return error;}
holderPlace=0;
strcpy(holder,reset);
}
variableNumber=8;
break;
case 'Z':
if(variableNumber>0)
{error=codeInterpret(variableNumber, holder);
if(error>0)
{return error;}
holderPlace=0;
strcpy(holder,reset);
}
variableNumber=9;
break;
case 'U':
if(variableNumber>0)
{error=codeInterpret(variableNumber, holder);
if(error>0)
{return error;}
holderPlace=0;
strcpy(holder,reset);
}
variableNumber=10;
break;
case 'V':
if(variableNumber>0)
{error=codeInterpret(variableNumber, holder);
if(error>0)
{return error;}
holderPlace=0;
strcpy(holder,reset);
}
variableNumber=11;
break;
case 'W':
if(variableNumber>0)

```
```

    {error=codeInterpret(variableNumber, holder);
        if(error>0)
            {return error;}
    holderPlace=0;
    strcpy(holder,reset);
        }
    variableNumber=12;
    break;
    case 'S':
if(variableNumber>0)
{error=codeInterpret(variableNumber, holder);
if(error>0)
{return error;}
holderPlace=0;
strcpy(holder,reset);
}
variableNumber=13;
break;
case 'F':
if(variableNumber>0)
{error=codeInterpret(variableNumber, holder);
if(error>0)
{return error;}
holderPlace=0;
strcpy(holder,reset);
}
variableNumber=14;
break;
case 'I':
if(variableNumber>0)
{error=codeInterpret(variableNumber, holder);
if(error>0)
{return error;}
holderPlace=0;
strcpy(holder,reset);
}
variableNumber=15;
break;
case 'J':
if(variableNumber>0)
{error=codeInterpret(variableNumber, holder);
if(error>0)
{return error;}
holderPlace=0;
strcpy(holder,reset);
}
variableNumber=16;
break;
case 'K':
if(variableNumber>0)
{error=codeInterpret(variableNumber, holder);
if(error>0)
{return error;}
holderPlace=0;
strcpy(holder,reset);
}
variableNumber=17;
break;
case 'R':
if(variableNumber>0)
{error=codeInterpret(variableNumber, holder);
if(error>0)

```
```

                    {return error;}
            holderPlace=0;
            strcpy(holder,reset);
                        }
            variableNumber=18;
            break;
    case ' ':
break;
default:
holder[holderPlace]=codeLineHold[counter];
++holderPlace;
break;
} // end of switch
}// end of for
if (codeLineHold[counter]=='\0') //save last string item
{
if (variableNumber>0)
{error=codeInterpret(variableNumber, holder);
if(error>0)
{return error;}
holderPlace=0;}
}// end of final save
return 0;
}//end function
int codeManip::codeInterpret(int variable, const char *string)
{
int error=0;
switch(variable)
{
case 1:
N=atoi(string);
break;
case 2:
M=atof(string);
error=check_M();
if(error>0)
{M=0;
return error;}
break;
case 3:
G=atof(string);
error=check G();
if(error>0)
{G=0;
return error;}
break;
case 4:
if(a==0)
{return AXIS_INACTIVE;}
else A=atof(string);
break;
case 5:
if(b==0)
{return AXIS_INACTIVE;}
else B=atof(string);
break;
case 6:

```
```

            if(c==0)
            {return AXIS_INACTIVE;}
            else C=atof(string);
        break;
    case 7:
if(x==0)
{return AXIS INACTIVE;}
else X=ato\overline{f}(string);
break;
case 8:
if(y==0)
{return AXIS_INACTIVE;}
else Y=atof(string);
break;
case 9:
if(z==0)
{return AXIS_INACTIVE;
else Z=ato\overline{f}(string);
break;
case 10:
if(u==0)
{return AXIS INACTIVE;}
else U=ato\overline{f}(string);
break;
case 11:
if(v==0)
{return AXIS_INACTIVE;}
else V=atof(string);
break;
case 12:
if(w==0)
{return AXIS_INACTIVE;}
else W=atof(\overline{string);}
break;
case 13:
S=atof(string);
break;
case 14:
F=atof(string);
break;
case 15:
if(x==0)
{return INVALID_IN_CONFIGURATION;}
else I=atof(strīng);
break;
case 16:
if(y==0)
{return INVALID_IN_CONFIGURATION;}
else J=atof(string);
break;
case 17:
if(z==0)
{return INVALID_IN_CONFIGURATION; }
else K=atof(string);
break;
case 18:
error=check_Arc();
if(error>0)
{return error;}
else R=atof(string);
break;
default:
return 1;

```
```

}//end switch
return 0;
}
int codeManip::codeSave()
{
FILE *fp;
fp=fopen("code.dat","a+");
if(fp==NULL)
{return 1;}
else {
fprintf(fp,"%7d%7d%7d%7.2f%7.2f%7.2f%7.2f%7.2f%7.2f",N,M,G,A,B,C,X,Y,Z);
fprintf(fp,"%7.2f%7.2f%7.2f%7.2f%7.2f%7.2f%7.2f%7.2f%7.2f\n",U,V,W,S,F,I
,J,K,R);
}
fclose(fp);
return 0;
}
int codeManip::check_G()
{
int error=0;
switch(G)
{
case 0:
break;
case 1:
break;
case 2:
error=check_Arc();
break;
case 3:
error=check_Arc();
break;
case 10:
break;
case 90:
break;
case 91:
break;
default:
return FUNCTION_NOT_AVAILABLE;
}
return error;}
int codeManip::check_M()
{
switch(M)
{
case 0:
break;
case 2:
break;
case 3:
break;
case 4:
break;

```
```

    case 5:
        break;
    default:
    return FUNCTION_NOT_AVAILABLE;
    }
    return 0;}
    int codeManip::check_Arc()
{
if(x*y)
{return 0;}
else if(x*z)
{return 0;}
else if(y*z)
{return 0;}
return INVALID_IN_CONFIGURATION; //return error code if none of the
pairs of axes are active
}

```
//Execute.h (header file for functions associated with the execution of user instructions)
```

\#ifndef EXECUTE H
\#define EXECUTE _
\#include <qlineedit.h>
\#include <qtextedit.h>
\#include <qprogressbar.h>
class LineExecute{
public:
LineExecute();
~LineExecute();
void resetVariables();
int Start(int SerialPortSpeed);
int NumberOfLines();
int loadFunction(int SerialPortSpeed);
void DistanceCalculator();
void setGlobal Position();
void getGlobal_Position();
void ProgramStop();
void ProgramEnd();
void goToOrigin(int TIPO);
QLineEdit *PWarninglineEdit; //pointer to warning line
QLineEdit *PStatuslineEdit;//pointer to status line
QLineEdit *PServoPortlineEdit;
QLineEdit *PSpindlePortlineEdit;
QLineEdit *PTIPOlineEdit;
QTextEdit *PcodeEdit;//pointer to code edit box
QProgressBar *PprogressBar;//pointer to progress bar
const char *ServoPortName;
const char *SpindlePortName;
const char *InterpolationCycleTime;
private:
int N;
int M;
int G;
float A;

```
```

    float B;
    float C;
    float X;
    float Y;
    float Z;
    float U;
    float V;
    float W;
    float S;
    float F;
    float I;
    float J;
    float K;
    float R;
    //Variables for transmission in float
    int Mp;
    int Gp;
    int Sp;
    float Ap;
    float Bp;
    float Cp;
    float Xp;
    float Yp;
    float Zp;
    float Up;
    float Vp;
    float Wp;
    float Fp;
    float Ip;
    float Jp;
    float Kp;
    float Rp;
    //absoute Programming
    int ABS; //Absolute Programming Flag
    float absA;
    float absB;
    float absC
    float absX;
    float absY;
    float absZ;
    float absU;
    float absV
    float absW
    };
\#endif

```
\begin{tabular}{|c|c|l|}
\hline \multicolumn{3}{|c|}{ Parts List } \\
\hline ITEM & QTY & \multicolumn{1}{|c|}{ PART NUMBER } \\
\hline 1 & 1 & Bearing housing for bed \\
\hline 2 & 1 & Bearing housing cap \\
\hline 3 & 1 & Bed Carrige \\
\hline 4 & 1 & motor plate \\
\hline 5 & 1 & Wiper Motor \\
\hline 6 & 3 & Motor spacer \\
\hline 7 & 1 & Carriage Part 2 \\
\hline 8 & 1 & Lead screw \\
\hline 9 & 1 & Coupling \\
\hline 20 & 2 & Coordinate System \\
\hline
\end{tabular}

\begin{tabular}{|c|c|c|c|c|c|c|}
\hline \multirow[t]{6}{*}{University of Kwa-Zulu Natal School of Mechanical Engineering} & Orthographic Projection & \multicolumn{2}{|c|}{SCALE 1:6} & \multirow[t]{2}{*}{TITLE} & \multicolumn{2}{|l|}{\multirow[t]{2}{*}{New Base Assembly 1}} \\
\hline & \multirow[t]{2}{*}{Q@ OR ¢} & \multicolumn{2}{|c|}{UNITS : mm} & & & \\
\hline & & Date & Checked & \multicolumn{3}{|l|}{\multirow[t]{2}{*}{PROJECT RMS Project}} \\
\hline & \multicolumn{3}{|l|}{Project Supervisor} & & & \\
\hline & \multicolumn{3}{|l|}{Workshop Technician} & \multicolumn{3}{|l|}{STUDENT NAME Jared Padayachee} \\
\hline & Technical Manager & & & \[
\text { TEL No. } 1227
\] & & 20350539 \\
\hline
\end{tabular}

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\begin{tabular}{|c|c|l|}
\hline \multicolumn{3}{|c|}{ Parts List } \\
\hline ITEM & QTY & \multicolumn{1}{|c|}{ PART NUMBER } \\
\hline 1 & 1 & Bed Carrige \\
\hline 2 & 1 & Bed Carriage Part 2 \\
\hline 3 & 1 & Lead screw \\
\hline 4 & 1 & Brass sleeve \\
\hline 20 & 2 & Coordinate System \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|c|c|c|c|}
\hline \multirow[t]{2}{*}{University of Kwa-Zulu Natal} & Orthographic Projection & \multicolumn{2}{|c|}{SCALE 1:2} & \multirow[t]{2}{*}{TITLE} & \multicolumn{2}{|l|}{\multirow[b]{2}{*}{Bed Carriage Assembly}} \\
\hline & \multirow[t]{2}{*}{* OR ¢} & \multicolumn{2}{|c|}{UNITS : mm} & & & \\
\hline  & & Date & Checked & \multirow[t]{2}{*}{PROJECT} & \multicolumn{2}{|l|}{\multirow[t]{2}{*}{RMS Project}} \\
\hline School & Project Supervisor & & & & & \\
\hline \multirow{2}{*}{Engineering} & Workshop Technician & & & \multicolumn{3}{|l|}{\multirow[t]{2}{*}{\(\qquad\)}} \\
\hline & Technical Manager & & & & & \\
\hline
\end{tabular}


Quantity: 2
Material: Steel Supplied

\begin{tabular}{|c|c|c|c|c|c|c|c|}
\hline \multirow[t]{6}{*}{University of Kwa-Zulu Natal School of Mechanical Engineering} & Orthographic Projection & \multicolumn{2}{|c|}{SCALE 1:2} & \multirow[t]{2}{*}{TitLe} & \multicolumn{3}{|l|}{\multirow[b]{2}{*}{Bed Carriage - Part 1}} \\
\hline & \multirow[t]{2}{*}{¢} & \multicolumn{2}{|c|}{UNITS : mm} & & & & \\
\hline & & Date & Checked & \multirow[t]{2}{*}{PROJECT} & \multicolumn{3}{|c|}{\multirow[t]{2}{*}{RMS Project}} \\
\hline & Project Supervisor & & & & & & \\
\hline & Workshop Technician & & & \multicolumn{4}{|l|}{\multirow[t]{2}{*}{Student name \(\quad\) Jared Padayachee
tel no. 1227 email \(203505399 @ u k z n . a c . z a ~\)}} \\
\hline & Technical Manager & & & & & & \\
\hline
\end{tabular}


Quantity:2
Material: Threaded Bar Supplied



Quantity: 2
Material: Steel Supplied
\(\square \rightarrow\)
\begin{tabular}{|c|c|c|c|c|c|c|c|}
\hline \multirow[t]{6}{*}{University of Kwa-Zulu Natal School of Mechanical Engineering} & Orthographic Projection & \multicolumn{2}{|c|}{SCALE 1:2} & \multirow[t]{2}{*}{TITLE} & \multicolumn{3}{|l|}{\multirow[t]{2}{*}{Bed Carriage - Part 2}} \\
\hline & \multirow[t]{2}{*}{*} & \multicolumn{2}{|c|}{UNITS : mm} & & & & \\
\hline & & Date & Checked & \multirow[t]{2}{*}{PROJECT} & \multicolumn{3}{|l|}{\multirow[t]{2}{*}{RMS Project}} \\
\hline & Project Supervisor & & & & & & \\
\hline & Workshop Technician & & & \multicolumn{4}{|l|}{student name Jared Padayachee} \\
\hline & Technical Manager & & & tel no. & 1227 & & 20350539 \\
\hline
\end{tabular}

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Quantity: 2
Material: Steel Supplied

\begin{tabular}{|c|c|c|c|c|c|c|}
\hline \multirow[t]{6}{*}{University of Kwa-Zulu Natal School of Mechanical Engineering} & Orthographic Projection & \multicolumn{2}{|c|}{SCALE \(1: 1\)} & \multirow[t]{2}{*}{TITLE} & \multicolumn{2}{|l|}{\multirow[t]{2}{*}{Bearing Housing Cap}} \\
\hline & \multirow[t]{2}{*}{¢} & \multicolumn{2}{|c|}{UNITS : mm} & & & \\
\hline & & Date & Checked & \multicolumn{3}{|l|}{\multirow[t]{2}{*}{PROJECT RMS Project}} \\
\hline & Project Supervisor & & & & & \\
\hline & Workshop Technician & & & \multicolumn{3}{|l|}{Student name Jared Padayachee} \\
\hline & Technical Manager & & & TEL No. 1227 & & 203505399 \\
\hline
\end{tabular}

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Quantity: 2
Material: Steel Supplied

\begin{tabular}{|c|c|c|c|c|c|c|c|}
\hline \multirow[t]{4}{*}{University of Kwa-Zulu Natal School of Mechanical Engineering} & Orthographic Projection & \multicolumn{2}{|c|}{\[
\begin{array}{ll}
\hline \text { SCALE } & 1: 1.5 \\
\hline
\end{array}
\]} & \multicolumn{4}{|l|}{\multirow[t]{2}{*}{\({ }^{\text {TTTLE }} \quad\) Bearing Housing For Bed}} \\
\hline & \(\dagger\) OR ¢ ¢ \(\dagger\) & \multicolumn{2}{|c|}{UNITS : mm} & & & & \\
\hline & Project Supenisor & & & \multicolumn{4}{|l|}{PROJECT RMS Project} \\
\hline & Workshop Technician & & & \multicolumn{4}{|l|}{\multirow[t]{2}{*}{STUDENT NAME Jared Padayachee
1227 20350539}} \\
\hline & Technical Manager & & & & & & \\
\hline
\end{tabular}


Quantity: 6
Material: Steel Supplied




Quantity: 2
Material: Steel Supplied

\begin{tabular}{|c|c|c|c|c|c|c|}
\hline \multirow[t]{2}{*}{University of Kwa-Zulu Natal} & Orthographic Projection & \multicolumn{2}{|c|}{SCALE 2:1} & TITLE & \multicolumn{2}{|l|}{\multirow[b]{2}{*}{Coupling-Base Shared Components}} \\
\hline & \multirow[t]{2}{*}{¢} & \multicolumn{2}{|c|}{UNITS : mm} & & & \\
\hline & & Date & Checked & \multicolumn{3}{|l|}{\multirow[t]{2}{*}{Project RMS Project}} \\
\hline Schoo & Project Supervisor & & & & & \\
\hline \multirow[t]{2}{*}{Engineering} & Workshop Technician & & & \multicolumn{3}{|l|}{student name Jared Padayachee} \\
\hline & Technical Manager & & & \[
\text { tel no. } 1227
\] & EMAIL & 203505399@ukzn.ac.za \\
\hline
\end{tabular}


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2
Front


Left View
\begin{tabular}{|c|c|l|}
\hline \multicolumn{3}{|c|}{ Parts List } \\
\hline ITEM & QTY & \multicolumn{1}{|c|}{ PART NUMBER } \\
\hline 1 & 1 & Column Cap \\
\hline 2 & 1 & Column Base \\
\hline 3 & 1 & Lead screw \\
\hline 4 & 4 & Guide Rod \\
\hline 5 & 1 & Carriage \\
\hline 6 & 1 & Carriage adaptor plate \\
\hline 7 & 1 & Wiper Motor \\
\hline 8 & 3 & Motor spacer \\
\hline 9 & 1 & Coupling \\
\hline
\end{tabular}

\begin{tabular}{|c|c|c|c|c|c|c|c|}
\hline \multirow[t]{5}{*}{University of Kwa-Zulu Natal School of Mechanical Engineering} & Orthographic Projection & \multicolumn{2}{|c|}{SCALE 1:8} & \multicolumn{4}{|l|}{\multirow[t]{2}{*}{TTTLE \(\quad\) Column Assembly 1}} \\
\hline & \(\checkmark\) OR ¢ \(\dagger\) & \multicolumn{2}{|c|}{UNITS : mm} & & & & \\
\hline & Projets Supenisor & Date & Checked & \multicolumn{4}{|l|}{PROJECT RMS Project} \\
\hline & Workshop Technician & & & \multicolumn{4}{|l|}{\multirow[t]{2}{*}{\[
\begin{aligned}
& \text { STUDENT NAME } \quad \text { Jared Padayachee } \\
& \text { TEL no. } 1227 \quad \text { EMAIL } \quad 203505399 @ u k z n . a c . z a
\end{aligned}
\]}} \\
\hline & Techical Manager & & & & & & \\
\hline
\end{tabular}

All Holes on PCD 85 mm are identical


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Quantity:2 Material: Aluminium Supplied
\begin{tabular}{|c|c|c|c|c|c|c|}
\hline \multirow[t]{6}{*}{University of Kwa-Zulu Natal School of Mechanical Engineering} & Orthographic Projection & \multicolumn{2}{|c|}{SCALE 1:2} & TITLE & & \\
\hline & \multirow[t]{2}{*}{\(\otimes\) OR ¢} & \multicolumn{2}{|c|}{UNITS : mm} & \multicolumn{3}{|r|}{Carriage - Column} \\
\hline & & Date & Checked & \multirow[t]{2}{*}{PROJECT R} & \multicolumn{2}{|l|}{\multirow[t]{2}{*}{RMS Project}} \\
\hline & Project Supervisor & & & & & \\
\hline & Workshop Technician & & & \multicolumn{3}{|l|}{Student name Jared Padayachee} \\
\hline & Technical Manager & & & \[
\text { TEL No. } 1227
\] & & 203 \\
\hline
\end{tabular}


Quantity: 2
Material: Steel Supplied



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Quantity: 2
Material: Brass Supplied

\begin{tabular}{|c|c|c|c|c|c|c|c|}
\hline \multirow[t]{6}{*}{University of Kwa-Zulu Natal School of Mechanical Engineering} & Orthographic Projection & \multicolumn{2}{|r|}{\multirow[t]{2}{*}{\[
\begin{array}{|l|}
\hline \text { SCALE } 1.5: 1 \\
\hline \text { UNITS: mm }
\end{array}
\]}} & \multicolumn{4}{|l|}{\multirow[t]{2}{*}{TTTLE collar for column}} \\
\hline & \multirow[t]{2}{*}{\(\checkmark\) OR ¢ \(\dagger\)} & & & & & & \\
\hline & & Date & Checked & Project & \multicolumn{3}{|l|}{RMS Project} \\
\hline & Project Superisor & & & \multicolumn{4}{|l|}{\multirow[t]{2}{*}{student name Jared Padayachee}} \\
\hline & Workshop Technician & & & & & & \\
\hline & Technical Manager & & & \multicolumn{4}{|l|}{tel no. 1227 emall 203505399} \\
\hline
\end{tabular}



Quantity: 6
Material: Steel Supplied

\begin{tabular}{|c|c|c|c|c|c|c|c|}
\hline \multirow[t]{6}{*}{University of Kwa-Zulu Natal School of Mechanical Engineering} & Orthographic Projection & \multicolumn{2}{|r|}{\multirow[t]{2}{*}{\[
\begin{aligned}
& \hline \text { SCALE } \quad 2: 1 \\
& \hline \text { UNITS: mm }
\end{aligned}
\]}} & \multirow[t]{2}{*}{TTTLE} & \multicolumn{3}{|l|}{\multirow[b]{2}{*}{Motor Spacer}} \\
\hline & ¢¢ OR ¢ \(\dagger\) & & & & & & \\
\hline & Project Superisor & Date & Checked & PROJECT & \multicolumn{3}{|l|}{RMS Project} \\
\hline & \multirow[b]{2}{*}{Workshop Technician} & & & \multicolumn{4}{|l|}{\multirow[t]{2}{*}{Student name Jared Padayachee}} \\
\hline & & & & & & & \\
\hline & Technical Manager & & & \multicolumn{4}{|l|}{tel no. 1227 email 203505399} \\
\hline
\end{tabular}



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Quantity: 8
Material: Rod Supplied

\begin{tabular}{|c|c|c|c|c|c|c|}
\hline \multirow[t]{5}{*}{University of Kwa-Zulu Natal School of Mechanical Engineering} & Orthographic Projection & \multicolumn{2}{|l|}{} & \multicolumn{3}{|l|}{\multirow[t]{2}{*}{TTTLE Guide rod - Column}} \\
\hline & ¢¢ OR ¢ \(\dagger\) & \multicolumn{2}{|c|}{UNITS : mm} & & & \\
\hline & Project Superisor & Date & Checked & \multicolumn{3}{|l|}{PROJECT RMS Project} \\
\hline & Workshop Techician & & & \multicolumn{3}{|l|}{\multirow[t]{2}{*}{student name Jared Padayachee
1227}} \\
\hline & Technical Manager & & & & & \\
\hline
\end{tabular}

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Quantity: 1

Material : Steel supplied



Parts List
\begin{tabular}{|c|c|l|}
\hline \multicolumn{3}{|c|}{ Parts List } \\
\hline ITEM & QTY & \multicolumn{1}{|c|}{ PART NUMBER } \\
\hline 1 & 1 & Rotary lower plate \\
\hline 2 & 4 & ISO 4762 - M6 \(\times 12\) \\
\hline 3 & 2 & Rotary-Side plates \\
\hline 4 & 4 & ISO 4762 - M6 \(\times 16\) \\
\hline 5 & 8 & ISO 4762 - M4 x 8 \\
\hline 6 & 2 & Cover \\
\hline 7 & 1 & Small motor \\
\hline 8 & 3 & Motor spacer \\
\hline 9 & 3 & ISO 4762 - M6 \(\times 20\) \\
\hline \multicolumn{3}{|c|}{10} \\
\hline \multicolumn{3}{|c|}{ Rotary Assembly 1 } \\
\hline \multicolumn{3}{|c|}{ RMS Project } \\
\hline
\end{tabular}

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Quantity: 3
Material: Steel Supplied

\begin{tabular}{|c|c|c|c|c|c|c|c|}
\hline \multirow[t]{6}{*}{University of Kwa-Zulu Natal School of Mechanical Engineering} & Orthographic Projection & \multicolumn{2}{|c|}{SCALE 5:1} & \multirow[t]{2}{*}{TITLE} & \multicolumn{3}{|l|}{\multirow[b]{2}{*}{Motor Spacer}} \\
\hline & \multirow[t]{2}{*}{¢@ OR ¢} & \multicolumn{2}{|c|}{UNITS : mm} & & & & \\
\hline & & Date & Checked & \multirow[t]{2}{*}{PROJECT} & \multicolumn{3}{|c|}{\multirow[t]{2}{*}{RMS Project}} \\
\hline & \multicolumn{3}{|l|}{Project Supervisor} & & & & \\
\hline & Workshop Technician & & & \multicolumn{4}{|l|}{student name Jared Padayachee} \\
\hline & Technical Manager & & & tel no. & 1227 & email & 203505399 \\
\hline
\end{tabular}


Quantity:1
Material: Aluminium Supplied





Plate Thickness: 2mm
Quantity: 2
Material: Stainless Steel Sheet Supplied

\begin{tabular}{|c|c|c|c|c|c|c|}
\hline \multirow[t]{6}{*}{University of Kwa-Zulu Natal School of Mechanical Engineering} & Orthographic Projection & \multicolumn{2}{|c|}{SCALE \(1: 1\)} & \multirow[t]{2}{*}{TITLE} & \multicolumn{2}{|l|}{\multirow[t]{2}{*}{Cover - Rotary Unit}} \\
\hline & \multirow[t]{2}{*}{\(\checkmark\) OR ¢} & \multicolumn{2}{|c|}{UNITS : mm} & & & \\
\hline & & Date & Checked & \multirow[t]{2}{*}{PROJECT} & \multicolumn{2}{|l|}{\multirow[t]{2}{*}{RMS Project}} \\
\hline & Project Supervisor & & & & & \\
\hline & Workshop Technician & & & \multicolumn{3}{|l|}{\multirow[t]{2}{*}{STUDENT NAME
TEL No.
1227
Emared Padayachee
203505399@ukzn.ac.za}} \\
\hline & Technical Manager & & & & & \\
\hline
\end{tabular}

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Quantity:1
Material: Aluminium Supplied
 UNLESS OTHERWISE STATED

8 identical tapped holes equi spaced on PCD 108mm



Quantity: 1
Material: Aluminium Supplied



Quantity: 2
Material: Aluminium supplied

\begin{tabular}{|c|c|c|c|c|c|c|}
\hline \multirow[t]{6}{*}{University of Kwa-Zulu Natal School of Mechanical Engineering} & Orthographic Projection & \multicolumn{2}{|c|}{SCALE 1:2} & \multirow[t]{2}{*}{TITLE S} & \multicolumn{2}{|l|}{\multirow[t]{2}{*}{Side Plate : Rotary unit}} \\
\hline & \multirow[t]{2}{*}{\(\otimes\) OR ¢} & \multicolumn{2}{|c|}{UNITS : mm} & & & \\
\hline & & Date & Checked & \multirow[t]{2}{*}{PROJECT R} & \multicolumn{2}{|l|}{\multirow[t]{2}{*}{RMS Project}} \\
\hline & Project Supervisor & & & & & \\
\hline & Workshop Technician & & & \multicolumn{3}{|l|}{\multirow[t]{2}{*}{}} \\
\hline & Technical Manager & & & & & \\
\hline
\end{tabular}


Quantity: 1
\begin{tabular}{|c|c|c|c|c|c|c|c|}
\hline \multirow[t]{4}{*}{University of Kwa-Zulu Natal School of Mechanical Engineering} & Orthographic Projection & \multicolumn{2}{|c|}{SCALE \(1: 3\)} & \multirow[t]{2}{*}{TTTLE} & \multicolumn{3}{|l|}{\multirow[t]{2}{*}{Work Table}} \\
\hline & \(\downarrow\) OR © \(\dagger\) & \multicolumn{2}{|c|}{Ts : m} & & & & \\
\hline & Project Superisor & Date & Checked & \multicolumn{4}{|l|}{PROJECT RMS Project} \\
\hline & Workshop Technician & & & \multicolumn{4}{|l|}{\multirow[t]{2}{*}{STUDENT NAME Jared Padayachee
1227}} \\
\hline & Technical Manager & & & & & & \\
\hline
\end{tabular}





Quantity:2
Material: Aluminium

\begin{tabular}{|c|c|c|c|c|c|}
\hline \multirow[t]{6}{*}{University of Kwa-Zulu Natal School of Mechanical Engineering} & Orthographic Projection & \multicolumn{2}{|r|}{\multirow[t]{2}{*}{\[
\text { SCALE } 1: 2
\]}} & \multicolumn{2}{|l|}{\multirow[t]{2}{*}{\({ }^{\text {TTTLE }}\) Arch two - work table - pivot}} \\
\hline & \multirow[t]{2}{*}{¢¢ OR ¢ \(\dagger\)} & & & & \\
\hline & & Date & Checked & Project & \multirow[t]{2}{*}{RMS Project} \\
\hline & Project Supervisor & & & & \\
\hline & Workshop Technician & & & \multicolumn{2}{|l|}{\multirow[t]{2}{*}{Student name Jared Padayachee
tel no. \(1227 \quad\) emall 203505399}} \\
\hline & Techrical Manager & & & & \\
\hline
\end{tabular}



Quantity: 1


Material: aluminium supplied
\begin{tabular}{|c|c|c|c|c|c|c|}
\hline \multirow[t]{2}{*}{University of Kwa-Zulu Natal} & Orthographic Projection & \multicolumn{2}{|c|}{SCALE} & TITLE & & \\
\hline & \multirow[t]{2}{*}{¢} & \multicolumn{2}{|c|}{UNITS : mm} & \multicolumn{3}{|r|}{Arch side one - work table - pivot} \\
\hline  & & Date & Checked & \multicolumn{3}{|l|}{\multirow[t]{2}{*}{PROJECT RMS Project}} \\
\hline School Of & Project Supervisor & & & & & \\
\hline \multirow{2}{*}{Engineering} & Workshop Technician & & & \multicolumn{3}{|l|}{\multirow[t]{2}{*}{Student name
tel no. \(1227 \quad\) emared Padayachee
203505399@ukzn.ac.za}} \\
\hline & Technical Manager & & & & & \\
\hline
\end{tabular}


Quantity: 2
Material: aluminium supplied
\begin{tabular}{|c|c|c|c|c|c|c|}
\hline \multirow[t]{2}{*}{University of Kwa-Zulu Natal} & Orthographic Projection & \multicolumn{2}{|c|}{SCALE \(1: 2\)} & TITLE A & \multicolumn{2}{|l|}{\multirow[b]{2}{*}{Arch one - work table - pivot}} \\
\hline & \multirow[t]{2}{*}{¢} & \multicolumn{2}{|c|}{UNITS : mm} & & & \\
\hline & & Date & Checked & \multirow[t]{2}{*}{PROJECT R} & \multicolumn{2}{|l|}{\multirow[t]{2}{*}{RMS Project}} \\
\hline School of & Project Supervisor & & & & & \\
\hline  & Workshop Technician & & & \multicolumn{3}{|l|}{student name Jared Padayachee} \\
\hline & Technical Manager & & & tel no. 1227 & & 203505399@ukzn.ac.za \\
\hline
\end{tabular}

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Quantity: 1
Material: Aluminium

\begin{tabular}{|c|c|c|c|c|c|c|c|}
\hline \multirow[t]{6}{*}{University of Kwa-Zulu Natal School of Mechanical Engineering} & Orthographic Projection & \multicolumn{2}{|c|}{SCALE 1:2} & \multirow[t]{2}{*}{TITLE} & \multicolumn{3}{|r|}{\multirow[t]{2}{*}{Connecting Rod - Work Table - pivot}} \\
\hline & \multirow[t]{2}{*}{¢¢ OR ¢} & \multicolumn{2}{|c|}{UNITS : mm} & & & & \\
\hline & & Date & Checked & \multirow[t]{2}{*}{PROJECT} & \multicolumn{3}{|c|}{\multirow[t]{2}{*}{RMS Project}} \\
\hline & Project Supervisor & & & & & & \\
\hline & Workshop Technician & & & \multicolumn{4}{|l|}{Student name Jared Padayachee} \\
\hline & Technical Manager & & & tel no. & 1227 & & 20350539 \\
\hline
\end{tabular}

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Material: Steel rod supplied
\begin{tabular}{|c|c|c|c|c|c|c|}
\hline \multirow[t]{6}{*}{University of Kwa-Zulu Natal School of Mechanical Engineering} & Orthographic Projection & \multicolumn{2}{|c|}{SCALE \(1: 1\)} & \multirow[t]{2}{*}{TITLE} & \multicolumn{2}{|l|}{\multirow[b]{2}{*}{Shaft - work table - pivot}} \\
\hline & \multirow[t]{2}{*}{Q OR ¢} & \multicolumn{2}{|c|}{UNITS : mm} & & & \\
\hline & & Date & Checked & \multicolumn{3}{|l|}{\multirow[t]{2}{*}{Project RMS Project}} \\
\hline & Project Supervisor & & & & & \\
\hline & Workshop Technician & & & \multicolumn{3}{|l|}{\multirow[t]{2}{*}{student name Jared Padayachee
\[
1227
\]}} \\
\hline & Technical Manager & & & & & \\
\hline
\end{tabular}

PRODUCED BY AN AUTODESK EDUCATIONAL PRODUCT





Quantity:1
Material: Aluminium

\begin{tabular}{|c|c|c|c|c|c|c|c|}
\hline \multirow[t]{6}{*}{University of Kwa-Zulu Natal School of Mechanical Engineering} & Orthographic Projection & \multicolumn{2}{|r|}{\multirow[t]{2}{*}{\[
\begin{aligned}
& \hline \text { SCALE } 1: 2 \\
& \hline \text { UNITS: mm }
\end{aligned}
\]}} & \multicolumn{4}{|l|}{\multirow[t]{2}{*}{\({ }^{\text {TTTLE }}\) Interface - wort table - rotary}} \\
\hline & \multirow[t]{2}{*}{\(\checkmark\) OR ¢ \(\dagger\)} & & & & & & \\
\hline & & Date & Checked & \multirow[t]{2}{*}{Project} & \multicolumn{3}{|l|}{\multirow[t]{2}{*}{RMS Project}} \\
\hline & \multirow[b]{2}{*}{Workshop Technician} & & & & & & \\
\hline & & & & \multicolumn{4}{|l|}{\multirow[t]{2}{*}{\begin{tabular}{l}
Student name Jared Padayachee \\
tel no. 1227 email 203505399
\end{tabular}}} \\
\hline & Technical Manager & & & & & & \\
\hline
\end{tabular}


Quantity: 1
Material: Supplied




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Quantity: 1
Material: Aluminium



PRODUCED BY AN AUTODESK EDUCATIONAL PRODUCT


University of Kwa-Zulu Natal School of Mechanical Engineering




Quantity: 3
Material: Steel Supplied

\begin{tabular}{|c|c|c|c|c|c|c|c|}
\hline \multirow[t]{6}{*}{University of Kwa-Zulu Natal School of Mechanical Engineering} & Orthographic Projection & & 3:1 & \multicolumn{4}{|l|}{\multirow[t]{2}{*}{TTTLE Motor Spacer - long -work table -rotary}} \\
\hline & \multirow[t]{2}{*}{¢里 OR ¢ \(\dagger\)} & \multicolumn{2}{|r|}{Units : mm} & & & & \\
\hline & & Date & Checked & \multicolumn{4}{|l|}{\multirow[t]{2}{*}{PROJECT RMS Project}} \\
\hline & Project Superisor & & & & & & \\
\hline & Workshop Technician & & & \multicolumn{4}{|l|}{Student name Jared Padayachee} \\
\hline & Technical Manager & & & \multicolumn{4}{|l|}{tel no. 1227 email 203505399} \\
\hline
\end{tabular}


Quantity: 1
Material: aluminium

\begin{tabular}{|c|c|c|c|c|c|c|}
\hline \multirow[t]{2}{*}{University of Kwa-Zulu Natal} & Orthographic Projection & \multicolumn{2}{|c|}{SCALE 1:2} & \multicolumn{3}{|l|}{TITLE Side Plate 2-work table - rotary} \\
\hline & \multirow[t]{2}{*}{\(\forall\) OR ¢} & \multicolumn{2}{|c|}{UNITS : mm} & \multicolumn{3}{|l|}{Side Plate 2 - work table - rotary} \\
\hline \multirow[t]{4}{*}{School of Mechanical Engineering} & & Date & Checked & \multirow[t]{2}{*}{PROJECT R} & \multicolumn{2}{|l|}{\multirow[t]{2}{*}{RMS Project}} \\
\hline & Project Supervisor & & & & & \\
\hline & Workshop Technician & & & \multicolumn{3}{|l|}{\multirow[t]{2}{*}{STUDENT NAME
TEL No.
1227}} \\
\hline & Technical Manager & & & & & \\
\hline
\end{tabular}


Quantity: 3
Material: Steel rod

\begin{tabular}{|c|c|c|c|c|c|c|c|}
\hline \multirow[t]{6}{*}{University of Kwa-Zulu Natal School of Mechanical Engineering} & Orthographic Projection & \multicolumn{2}{|r|}{\multirow[t]{2}{*}{\[
\begin{aligned}
& \hline \text { SCALE 3:1 } \\
& \text { UNITS: mm }
\end{aligned}
\]}} & \multicolumn{4}{|l|}{\multirow[t]{2}{*}{\[
f_{\text {Motor Spacer - work table - rotary }}^{\text {TiTLE }}
\]}} \\
\hline & \multirow[t]{2}{*}{\(\dagger\) OR ¢ \(\dagger\)} & & & & & & \\
\hline & & Date & Checked & \multicolumn{4}{|l|}{\multirow[t]{2}{*}{PROJECT RMS Project}} \\
\hline & Project Superisor & & & & & & \\
\hline & Workshop Technician & & & \multicolumn{4}{|l|}{\multirow[t]{2}{*}{Student name Jared Padayachee
tel no. 1227 email 203505399}} \\
\hline & Technical Manager & & & & & & \\
\hline
\end{tabular}
Quantity: 1

\begin{tabular}{|c|c|c|c|c|c|c|}
\hline \multirow[t]{5}{*}{University of Kwa-Zulu Natal School of Mechanical Engineering} & Orthographic Projection & \multicolumn{2}{|c|}{SCALE \(1: 2\)} & \multirow[t]{2}{*}{TTTLE} & \multicolumn{2}{|l|}{\multirow[t]{2}{*}{Top plate - work table - rotary}} \\
\hline & ¢¢ OR ¢ \(¢\) & \multicolumn{2}{|c|}{UNITS : mm} & & & \\
\hline & Project Supenisor & Date & Checked & \multicolumn{3}{|l|}{PROJECT RMS Project} \\
\hline & Workshop Technician & & & \multicolumn{3}{|l|}{\multirow[t]{2}{*}{student name Jared Padayachee}} \\
\hline & Techical Manager & & & & & \\
\hline
\end{tabular}


Quantity: 2


Material: Aluminium
\begin{tabular}{|c|c|c|c|c|c|c|}
\hline \multirow[t]{2}{*}{University of Kwa-Zulu Natal} & Orthographic Projection & \multicolumn{2}{|c|}{SCALE 1:2} & TITLE S & \multicolumn{2}{|l|}{\multirow[b]{2}{*}{Side plate 3 - work table - rotary}} \\
\hline & \multirow[t]{2}{*}{* OR ¢} & \multicolumn{2}{|c|}{UNITS : mm} & Sid & & \\
\hline & & Date & Checked & \multirow[t]{2}{*}{PROJECT R} & \multicolumn{2}{|l|}{\multirow[t]{2}{*}{RMS Project}} \\
\hline School & Project Supervisor & & & & & \\
\hline \multirow[t]{2}{*}{Engineering} & Workshop Technician & & & \multicolumn{3}{|l|}{student name Jared Padayachee} \\
\hline & Technical Manager & & & tel no. 1227 & EMAIL & 203505399@ukzn.ac.za \\
\hline
\end{tabular}

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Quantity: 1
Material: Steel Supplied




Quantity:1
Material: Brass Supplied

\begin{tabular}{|c|c|c|c|c|c|}
\hline \multirow[t]{6}{*}{University of Kwa-Zulu Natal School of Mechanical Engineering} & Orthographic Projection & \multicolumn{2}{|l|}{\multirow[t]{2}{*}{\[
\begin{array}{l|}
\hline \text { SCALE } \quad 1: 1 \\
\hline \text { UNITS: mm }
\end{array}
\]}} & \multirow[t]{2}{*}{TTTLE} & \multirow[b]{2}{*}{Collar - Work Table} \\
\hline & \multirow[t]{2}{*}{\(\checkmark\) OR ¢ \(\dagger\)} & & & & \\
\hline & & Date & Checked & PROJECT & RMS Project \\
\hline & & & & & \\
\hline & Workshop Technician & & & \multicolumn{2}{|l|}{Student name Jared Padayachee} \\
\hline & Technical Manager & & & tel no. & 1227 emall 203505399 \\
\hline
\end{tabular}
Quantity: 1
Material: Steel Supplied
\begin{tabular}{|c|c|c|c|c|c|c|}
\hline \multirow[t]{2}{*}{University of Kwa-Zulu Natal} & Orthographic Projection & \multicolumn{2}{|r|}{SCALE \(1: 2\)} & TITLE Ca & & \\
\hline & \multirow[t]{2}{*}{-} & \multicolumn{2}{|c|}{UNITS : mm} & \multicolumn{3}{|c|}{Carriage - work table} \\
\hline \multirow[t]{2}{*}{School of} & & Date & Checked & \multicolumn{3}{|l|}{\multirow[t]{2}{*}{PRoject RMS Project}} \\
\hline & Project Supervisor & & & & & \\
\hline \multirow[t]{2}{*}{Engineering} & Workshop Technician & & & \multicolumn{3}{|l|}{student name Jared Padayachee} \\
\hline & Technical Manager & & & \[
\text { tel no. } 1227
\] & & 203505399@ukzn.ac.za \\
\hline
\end{tabular}
Quantity: 4
Material: Steel Supplied




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Quantity: 1


Material: steel plate supplied




\begin{tabular}{|c|c|c|c|c|c|c|}
\hline \multirow[t]{6}{*}{University of Kwa-Zulu Natal School of Mechanical Engineering} & Orthographic Projection & \multicolumn{2}{|c|}{SCALE \(1: 8\)} & \multirow[t]{2}{*}{TITLE} & \multicolumn{2}{|l|}{\multirow[b]{2}{*}{Base - welding diagram}} \\
\hline & \multirow[t]{2}{*}{\(\square\) OR ¢} & \multicolumn{2}{|c|}{UNITS : mm} & & & \\
\hline & & Date & Checked & \multicolumn{3}{|l|}{\multirow[t]{2}{*}{PROJECT RMS Project}} \\
\hline & \multicolumn{3}{|l|}{Project Supervisor} & & & \\
\hline & Workshop Technician & & & \multicolumn{3}{|l|}{Student name Jared Padayachee} \\
\hline & Technical Manager & & & tel no. 1227 & & 20350539 \\
\hline
\end{tabular}


Quantity: 1
Material: Steel Supplied

\begin{tabular}{|c|c|c|c|c|c|c|}
\hline \multirow[t]{2}{*}{University of Kwa-Zulu Natal} & Orthographic Projection & \multicolumn{2}{|c|}{SCALE} & \multicolumn{3}{|l|}{TITLE} \\
\hline & \multirow[t]{2}{*}{\#} & \multicolumn{2}{|c|}{UNITS : mm} & \multicolumn{3}{|r|}{Interface Plate - work table} \\
\hline \multirow[t]{2}{*}{School of} & & Date & Checked & \multicolumn{3}{|l|}{\multirow[t]{2}{*}{Project RMS Project}} \\
\hline & Project Supervisor & & & & & \\
\hline \multirow{2}{*}{Engineering} & Workshop Technician & & & \multicolumn{3}{|l|}{Student name Jared Padayachee} \\
\hline & Technical Manager & & & \[
\text { TEL No. } 1227
\] & & 203505399@ukzn.ac.za \\
\hline
\end{tabular}


Quntity: 2


Material: Steel Supplied

Quantity: 1
Material: Steel Supplied

University of Kwa-Zulu Natal School of Mechanical Engineering
\begin{tabular}{|c|c|c|c|c|c|}
\hline Orthographic Projection & \multicolumn{2}{|c|}{SCALE \(1: 2\)} & \multirow[t]{2}{*}{TITLE} & \multicolumn{2}{|l|}{\multirow[b]{2}{*}{Rear Plate - work table base}} \\
\hline ¢ OR ¢ & \multicolumn{2}{|c|}{UNITS : mm} & & & \\
\hline & Date & Checked & \multicolumn{3}{|l|}{\multirow[t]{2}{*}{PROJECT RMS Project}} \\
\hline Project Supervisor & & & & & \\
\hline Workshop Technician & & & \multicolumn{3}{|l|}{Student name Jared Padayachee} \\
\hline Technical Manager & & & \[
\text { TEL No. } 1227
\] & & 203505399@ukzn.ac.za \\
\hline
\end{tabular}


Quantity: 3
Material: Steel supplied

\begin{tabular}{|c|c|c|c|c|c|}
\hline \multirow[t]{2}{*}{University of Kwa-Zulu Natal} & Oftrograpic Prijection & \multicolumn{2}{|r|}{SCale 3:1} & \({ }^{\text {TTLE }}\) & \multirow[t]{2}{*}{Motor Spacer - work table} \\
\hline & ¢¢ OR ¢ \(\dagger\) & \multicolumn{2}{|r|}{UNTIT: mm} & \multicolumn{2}{|l|}{\multirow[b]{2}{*}{Rolect RMS Project}} \\
\hline chool of & Projet Supenisor & & & & \\
\hline Mechanical & Worksop Peemicic & & & \multicolumn{2}{|l|}{\multirow[t]{2}{*}{Stuobent Name Jared Padayachee}} \\
\hline & Technical Manager & & & & \\
\hline
\end{tabular}


Quantity: 1
Material: Threaded bar supplied
\begin{tabular}{|c|c|c|c|c|c|c|c|}
\hline \multirow[t]{5}{*}{University of Kwa-Zulu Natal School of Mechanical Engineering} & Orthographic Projection & \multicolumn{2}{|c|}{SCALE \(1: 1\)} & \multirow[t]{2}{*}{\({ }^{\text {TTTLE }}\)} & \multicolumn{3}{|l|}{\multirow[t]{2}{*}{Lead Screw - work table}} \\
\hline & \multirow[t]{2}{*}{\(Ч\) OR ¢ \(¢\)} & \multicolumn{2}{|c|}{UNITS : mm} & & & & \\
\hline & & Date & Checked & PROECT & \multicolumn{3}{|l|}{RMS Project} \\
\hline & Workstop Technician & & & \multicolumn{4}{|l|}{\multirow[t]{2}{*}{STUDent Name \(\quad\) Jared Padayachee
TEL no. \(1227 \quad\) Emall \(\quad 203505399 @ u k z n . a c . z a ~\)}} \\
\hline & Technical Manager & & & & & & \\
\hline
\end{tabular}


Quantity: 2


Material: Steel rod supplied
\begin{tabular}{|c|c|c|c|c|c|c|}
\hline \multirow[t]{5}{*}{University of Kwa-Zulu Natal School of Mechanical Engineering} & Orthographic Projection & \multicolumn{2}{|c|}{SCALE \(1: 1\)} & \multirow[t]{2}{*}{TTTLE} & \multicolumn{2}{|l|}{\multirow[t]{2}{*}{Guide Rod - work table}} \\
\hline & ¢¢ OR ¢ \(\dagger\) & \multicolumn{2}{|c|}{UNITS : mm} & & & \\
\hline & Project Supenisor & Date & Checked & \({ }^{\text {PROJECT }}\) & \multicolumn{2}{|l|}{RMS Project} \\
\hline & Workshop Technician & & & \multicolumn{3}{|l|}{\multirow[t]{2}{*}{STUDENT NAME Jared Padayachee 1227 20350539}} \\
\hline & Technical Manager & & & & & \\
\hline
\end{tabular}



Quantity: 1
Material: Steel



Quantity: 2
Material: Steel

\begin{tabular}{|c|c|c|c|c|c|}
\hline \multirow[t]{3}{*}{University of Kwa-Zulu Natal} & Orthographic Projection & \multicolumn{2}{|r|}{SCALE 1:4} & \multirow[t]{2}{*}{TITLE} & \multirow[b]{2}{*}{Transmission Box Side Plate} \\
\hline & \multirow[t]{2}{*}{*や OR ¢} & & mm & & \\
\hline & & Date & Checked & \multirow[t]{2}{*}{PROJECT} & \multirow[t]{2}{*}{RMS Project} \\
\hline & Project Supervisor & & & & \\
\hline echanical & Workshop Technician & & & \multicolumn{2}{|l|}{Student name Jared Padayachee} \\
\hline & Technical Manager & & & tel no. & 1227 email 203505399 \\
\hline
\end{tabular}


Quantity: 1
Material: Steel
\begin{tabular}{|c|c|c|c|c|c|c|c|}
\hline \multirow[t]{6}{*}{University of Kwa-Zulu Natal School of Mechanical Engineering} & Orthographic Projection & \multicolumn{2}{|r|}{SCALE 1:5} & TTTLE & \multicolumn{3}{|l|}{\multirow[t]{2}{*}{Transmission Box - Front Plate}} \\
\hline & \multirow[t]{2}{*}{\(\downarrow\) OR ¢ \(\square^{\text {¢ }}\)} & \multicolumn{2}{|r|}{Units : mm} & & & & \\
\hline & & Date & Checked & \multirow[t]{2}{*}{PROJECT} & \multicolumn{3}{|l|}{\multirow[t]{2}{*}{RMS Project}} \\
\hline & Project Supervisor & & & & & & \\
\hline & Workshop Technician & & & \multicolumn{4}{|l|}{\multirow[t]{2}{*}{Student name Jared Padayachee}} \\
\hline & Technical Manager & & & & & & \\
\hline
\end{tabular}


Quantity: 1
Material: Steel
\begin{tabular}{|c|c|c|c|c|c|}
\hline University of & Orthographic Projection & \multicolumn{2}{|r|}{SCALE 1:4} & \({ }^{\text {TTTLE }}\) & \multirow[t]{2}{*}{Transmission Box Back Plate} \\
\hline \multirow[t]{5}{*}{\begin{tabular}{l}
Kwa-Zulu Natal \\
School of Mechanical Engineering
\end{tabular}} & \multirow[t]{2}{*}{\(\checkmark\) OR ¢ \(\dagger\)} & & : mm & & \\
\hline & & Date & Checked & PROJEC & RMS Project \\
\hline & Project Supervisor & & & & RMS Project \\
\hline & Workshop Technician & & & STUD & NaME Jared Padayachee \\
\hline & Technical Manager & & & tel no. & 1227 email 203505399 \\
\hline
\end{tabular}
Quantity: 1
Material: Steel




Quantity: 1


Material: Steel
\begin{tabular}{|c|c|c|c|c|c|c|}
\hline \multirow[t]{6}{*}{\begin{tabular}{l}
University of Kwa-Zulu Natal \\
School of Mechanical Engineering
\end{tabular}} & Orthographic Projection & \multicolumn{2}{|c|}{SCALE \(1: 4\)} & TITLE Moter & Bra & \\
\hline & \multirow[t]{2}{*}{O¢ OR ¢} & \multicolumn{2}{|c|}{UNITS : mm} & \multicolumn{3}{|r|}{Motor Bracket} \\
\hline & & Date & Checked & \multirow[t]{2}{*}{PROJECT R} & \multicolumn{2}{|l|}{\multirow[t]{2}{*}{RMS Project}} \\
\hline & Project Supervisor & & & & & \\
\hline & Workshop Technician & & & \multicolumn{3}{|l|}{student name Jared Padayachee} \\
\hline & Technical Manager & & & \[
\text { tel no. } 1227
\] & EMAIL & \\
\hline
\end{tabular}```

