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Interplay of magnetization dynamics with a microwave waveguide at cryogenic temperatures

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In this work, magnetization dynamics is studied at low temperatures in a hybrid system that consists of a thin epitaxial magnetic film coupled with a superconducting planar microwave waveguide. The resonance spectrum was observed over a wide magnetic field range, including low fields below the saturation magnetization and both polarities. Analysis of the spectrum via a developed fitting routine allowed for the derivation of all magnetic parameters of the film at cryogenic temperatures, the detection of waveguide-induced uniaxial magnetic anisotropies of the first and the second order, and the uncovering of a minor misalignment of magnetic field. A substantial influence of the superconducting critical state on resonance spectrum is observed and discussed.

I. INTRODUCTION

The field of magnonics studies the application of magnetization oscillations and waves in ferromagnetic structures^{1–6}. The following benefits make magnonics promising for application in processing of microwave signals: tunability of the magnon dispersion with applied magnetic field and the geometry of the medium, low dissipation and power consumption, high operational frequencies, convenient micron and sub-micron scales of spin wavelength at microwave frequencies, and, finally, absence of parasitic coupling of spin waves with non-magnetic environments. Conventionally, magnonics is a room-temperature research discipline.

Currently a sub-discipline is emerging that deals with magnetization dynamics at cryogenic temperatures and can be referred to as “cryogenic magnonics”. Indeed, quantum magnonics is of high current interest^{7–11}. Microwave experiments in quantum magnonics are typically performed at milli-kelvin temperatures, often using setups equipped with superconducting quantum circuits. On the other hand, a development of various hybrid devices is taking place based on superconducting resonators^{7,12} and Josephson junctions^{13–15}. Also, it was shown that hybridization of a magnon medium with superconducting structures results in substantial modification of dispersion properties^{16–19}, as well as in the formation of magnonic band structures²⁰. Lastly, metamaterial properties have been reported for superconduc-

tor/ferromagnet superlattices²¹. More generally and beyond superconductor-induced phenomena, the magnetic properties at low temperatures are probed in absence or only with minor thermal excitations. Typical thermal effects for standard magnonics, such as reduced saturation magnetization or thermally activated domain wall motion, are lessened for cryo-magnonics, leading to new phenomena in ferromagnetic resonance (FMR).

In this regard, investigation of magnetic properties of ferromagnetic films at low temperature as well as of their interaction with superconducting circuits is imperative. This report addresses both problems. We focus on the ferromagnetic resonance in a thin Yttrium Iron Garnet (YIG) film coupled to a superconducting Nb planar waveguide in out-of-plane magnetic field. We obtain the FMR spectrum at low temperature in a wide field range. The spectrum shows linear magnetic resonance versus field dependence for high fields and a range of nonlinear dependence of FMR frequency at low magnetic fields where the Kittel formulas are inapplicable. Developing a fitting routine, we derive all magnetic parameters of the YIG film. Our analysis shows that the waveguide itself induces substantial uniaxial magnetic anisotropy. Next, we study the FMR spectrum at temperatures below the superconducting critical temperature of the waveguide and observe an influence of the superconducting critical state of Nb on the resonance spectrum.

We note that while YIG is probably the most popular magnetic material for magnonic applications, owing to

its low damping, the damping in YIG and its temperature dependence are not addressed in this paper and can be found elsewhere²²⁻²⁴. In this report, YIG is selected as a model magnetic single-crystalline thin film with distinct magnetocrystalline anisotropy and sufficiently low saturation magnetization, which is convenient for out-of-plane measurements.

II. EXPERIMENTAL DETAILS

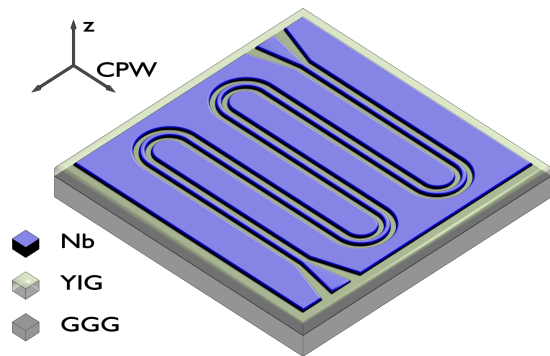


FIG. 1. Schematic illustration of the investigated system. YIG epitaxial film is grown on [111]-oriented single-crystal GGG substrate by means of LPE. A Nb CPW is fabricated directly on top of YIG film. The main direction of the CPW is indicated with the axis. Magnetic field H is applied out-of-plane, along [111] orientation of YIG/GGG (i.e., along z -direction).

The FMR absorption measurements were performed using the so-called VNA-FMR approach²⁵⁻²⁷ (VNA stands for the vector network analyzer). A schematic illustration of the investigated system is shown in Fig. 1. The single-crystalline epitaxial YIG film of thickness $d = 51$ nm was deposited on single-crystal [111]-oriented Gadolinium Gallium Garnet (GGG) substrate using the liquid phase epitaxy (LPE) technique. Details of LPE as well as room-temperature characteristics of LPE-grown ultra-thin YIG films can be found elsewhere^{23,28}. Measurement of the FMR response in YIG was enabled by fabrication of a co-planar waveguide (CPW) directly on top of YIG film. The CPW was patterned out of 150 nm thick magnetron-sputtered niobium (Nb) thin film with superconducting critical temperature $T_c \simeq 8.5$ K using photo-lithography and plasma-chemical etching. Deposition of Nb at room temperature was obstructed by poor adhesion of the metal film to the YIG surface, and therefore, was performed at 300°C. The 50 Ω impedance of the superconducting CPW was provided by its 27-40-27 μm gap-center-gap dimensions. Direct placement of the CPW on the probed magnetic film and its elongation via meandering enhance sensitivity to weak FMR absorptions²⁹. The experimental chip was installed in a copper sample holder and wire bonded to a PCB with RF

connectors. A thermometer and a heater were attached directly to the holder for precise temperature control. The holder was placed in a superconducting solenoid inside a closed-cycle cryostat (Oxford Instruments Triton, base temperature 1.2 K). The response of the system was studied by analyzing the transmitted microwave signal S_{21} with the VNA Rohde & Schwarz ZVB20.

III. RESULTS AND DISCUSSION

Figures 2a,b show transmission spectra of the studied sample at $T = 10$ K $> T_c$ of Nb and at 2 K $< T_c$. Spectra have been normalized with $S_{21}(f)$ at $\mu_0 H = 0.5$ T. Figures 2c,d show a set of normalized absorption curves $S_{21}(f)$ of the sample at the same temperatures and several magnetic fields. Field dependent spectral lines in Figs. 2a,b with the minimum transmission correspond to FMR curves $f_r(\mu_0 H)$. Both spectra show linear FMR response at $|\mu_0 H| > 0.2$ T, which is typical for the Kittel-FMR mode of a thin film in out-of-plane magnetic field. The resonance frequency with out-of-plane field is $f_r \propto (\mu_0 H - 4\pi M_{\text{eff}})$, which indicates the value of the effective saturation magnetization $4\pi M_{\text{eff}} \sim 2000$ Oe at $f_r \rightarrow 0$. Upon decreasing $|\mu_0 H|$, the linear resonance line is terminated with a kink at $|\mu_0 H| \sim 4\pi M_{\text{eff}}$ and transforms into two FMR branches with nonlinear dependence of resonance frequency versus field for $|\mu_0 H| < 4\pi M_{\text{eff}}$. We refer to the higher-frequency FMR branch with stronger absorption as C-line and to the lower-frequency FMR branch with weaker absorption as G-line. Note that in general, observation of FMR in thin films with out-of-plane geometry at $|\mu_0 H| < 4\pi M_{\text{eff}}$ might be challenging due to formation of nonuniform magnetization configurations. With out-of-plane field $|\mu_0 H| < 4\pi M_{\text{eff}}$, ferromagnetic films are not magnetized to saturation, and Kittel formulas for FMR are not applicable. Splitting of the FMR response into several spectral lines at $|\mu_0 H| < 4\pi M_{\text{eff}}$ can be caused by various factors, including standing spin wave resonances^{18,30-32}, FMR response of magnetic domain structure³³⁻³⁵, or magnetic phase separation.

After transition of the Nb CPW into the superconducting state, the transmission spectrum changes (compare Figs. 2a and b, Figs. 2c and d). While the spectrum at $T < T_c$ consists of the same resonance lines as at $T > T_c$, superconductivity manifests itself in hysteresis of FMR peak absorption at $|\mu_0 H| < 0.2$ T, which is best visible for the C-line (compare $S_{21}(f)$ at $\mu_0 H = 0.1$ T and $\mu_0 H = -0.1$ T in Fig. 2d): FMR absorption at negatively swept magnetic field (positive H in Figs. 2b,d) is substantially stronger than at positively swept magnetic field (negative H in Figs. 2b,d). In addition, at $T < T_c$ a suppression of FMR response is observed at the low field region $|\mu_0 H| < 0.02$ T. Below we will discuss the FMR response of YIG in absence of superconductivity, establish causes for the split of FMR at $|\mu_0 H| < 4\pi M_{\text{eff}}$, and define the contribution of superconductivity to the FMR

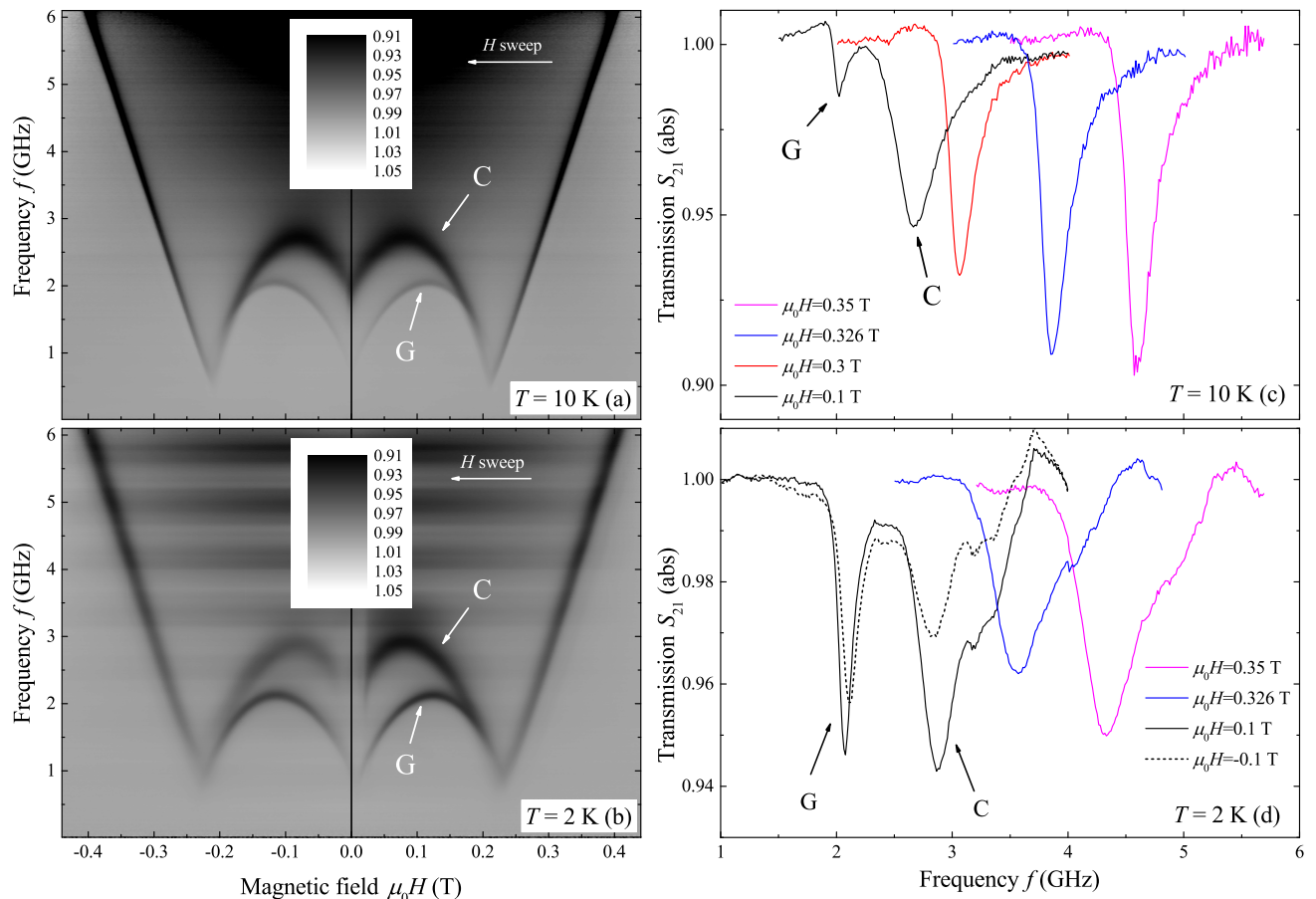


FIG. 2. a) and b) Gray-scale-coded transmission spectra $|S_{21}(\mu_0 H, f)/S_{21}(\mu_0 H = 0.5 \text{ T}, f)|$ measured at $T = 10 \text{ K}$ above T_c (a) and $T = 2 \text{ K}$ below T_c (b). c) and d) Corresponding frequency dependencies of the normalized transmission $|S_{21}(f)|$ at several magnetic fields at $T = 10 \text{ K}$ (c) and $T = 2 \text{ K}$ (d). For curves in (c) and (d) the background was subtracted. At $T < T_c$ the spectrum shows hysteresis of absorption. Magnetic field was swept negatively from $+0.5$ to -0.5 T (indicated with arrows), and, therefore, the part of spectra in (b) at positive fields provides the “down-field-sweep” data while the part of the spectrum at negative fields provides the “up-field-sweep” data. Labels C and G indicate higher- and lower-frequency spectral lines, respectively.

spectrum.

A. FMR at $T > T_c$. Magnetic properties of YIG film at cryogenic temperatures.

Having analysed possible origins for the split of the FMR into the C-line and G-line in Fig. 2 we can state that neither domain structure nor spin waves can contribute to the FMR spectrum for our particular study. For instance, nucleation of magnetic domains upon demagnetization at $\mu_0 H < 4\pi M_{\text{eff}}$ occurs for thin films with strong perpendicular anisotropy in comparison with the demagnetizing energy^{36,37}, i.e. when the magnetic quality parameter $Q = K_u/2\pi M_s^2 > 1$, where K_u is the out-of-plane uniaxial anisotropy, and M_s is the saturation magnetization. However, a typical field of uniaxial anisotropy $\mu_0 H_{K_u} = 2K_u/M_s$ in LPE-grown YIG thin

films ranges up to $\sim 200 \text{ Oe}$ ^{23,28,32,38} ensuring $Q \ll 1$. The highest values of uniaxial anisotropy in YIG films $\mu_0 H_{K_u} \sim 10^3 \text{ Oe}$ that can be obtained in pulsed-laser-deposited films³⁹ still ensure $Q < 1$. As an additional test, we have performed a magnetic force microscopy study of magnetic flux structure at the surface of the YIG film at 4 K using attocube attoDRY 1000 closed-cycle cryogenic microscope, supplied with a superconducting solenoid, and found no traces of domains or any field-dependent magnetic structure. Therefore, we confirm that formation of the domain structure does not occur. The magnetic state of the YIG film is single-domain, and variation of the out-of-plane component of magnetization at $\mu_0 H < 4\pi M_{\text{eff}}$ occurs via rotation of the magnetization vector from out-of-plane orientation to in-plane.

The absence of contribution of standing spin-wave resonances to the FMR spectrum can be illustrated in the following way. At $H = 0$ the magnetization vector of

a single-domain film is aligned in-plane. Therefore, the Kittel formula for FMR and dispersion relations for any spin-wave mode at $H = 0$ become applicable. When several resonances are observed, a contributing spin-wave mode can be identified by estimating a resonance frequency difference Δf_r between the Kittel mode and any standing spin-wave mode. The latter appears due to quantization of the wavelength with geometrical parameters of a sample. The difference Δf_r is then compared with the experimentally observed one ~ 1.3 GHz at $H = 0$ (Fig. 2). If an in-plane magnetostatic standing spin-wave mode^{40,41} is assumed, e.g., the backward volume mode or the magnetostatic surface mode, its wavelength $\lambda/2$ for the standing mode should be quantized with dimensions of the CPW, i.e., $\lambda/2 \sim 20 - 40 \mu\text{m}$. Such a standing spin-wave mode provides only marginal difference $\Delta f_r \lesssim 10$ MHz due to a small ratio $d/\lambda \sim 10^{-3}$. Alternatively, if exchange-dominated perpendicular standing spin-wave resonance^{42,43} is assumed the typical exchange constant in YIG films³² $\sim 4 \times 10^{-12}$ J/m provides $\Delta f_r \sim 2.5$ GHz for $d = \lambda/4$ and $\Delta f_r \sim 7.5$ GHz for $d = \lambda/2$. Thus, none of the possible standing spin-wave modes can provide $\Delta f_r \sim 1.3$ GHz. Overall, when a standing spin-wave resonance is excited multiple consequential spectral lines are expected. FMR absorption for each line should decrease progressively with the mode number (see, for instance Ref.⁴⁴). Such a picture is not observed in our experiment. Therefore, we confirm that several spectral lines in Fig. 2 at $|\mu_0 H| < 4\pi M_s$ are not caused by standing spin-wave resonances.

The remaining explanation for two FMR lines requires the existence of two resonating areas with different magnetic properties in the vicinity of the CPW. The magnetic structure is essentially single-domain in each area. The resonating areas can be identified by the coupling strength of microwaves to precessing magnetization that is proportional to the FMR amplitude and correlates directly with the amplitude of excitation AC magnetic fields. In CPW geometry, AC magnetic fields are mainly focused in the vicinity of the central transmission line^{12,25}. Therefore, geometry of the experiment (Fig. 1) suggests that the lower-frequency, weaker G-line originates from YIG at gap areas of CPW where the coupling is weaker, while higher-frequency, stronger C-line appears due to FMR response of YIG area under the central conducting line of the CPW. The accuracy of that explanation is strengthened by additional features, as discussed below.

For the case of the single-domain single-crystalline YIG film, the analytical resonance curve $f_r(\mu_0 H)$ can be obtained in the entire H -range following Refs.^{38,45-47} (we keep the notations given in Ref.³⁸). The orientation of magnetization of a single-domain film at arbitrarily oriented magnetic field is defined by the minimum of free magnetostatic energy $g = g(M_s, h, k_1, k_2, k_u, \theta, \psi, \phi_h, \phi_m)$, where k_1 , k_2 and k_u are unitless parameters of cubic magnetocrystalline anisotropy and out-of-plane uniaxial anisotropy, respec-

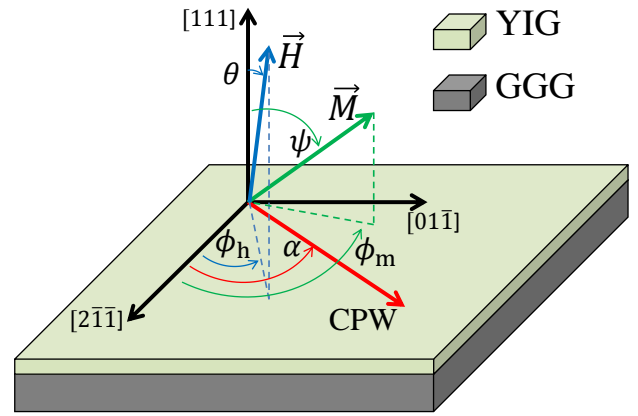


FIG. 3. Spherical coordinate system for the studied YIG film sample. Adopted from Ref.³⁸. Direction of the CPW transmission line (see Fig. 1) is indicated with the red axis, which specifies additional in-plane uniaxial anisotropy due to CPW directionality .

tively, $h = \mu_0 H / 4\pi M_s$ is the normalized external magnetic field, and $\theta, \psi, \phi_h, \phi_m$ define the orientations of H and M_s with respect to principle crystallographic axes of YIG in spherical coordinates (see Fig. 3). In addition, the system in Fig. 1 has a distinct directionality along the orientation of the CPW. This directionality may contribute to the orientation of magnetization. We account for its possible contribution by an additional energy term g_a added to the free magnetostatic energy g that provides a phenomenological in-plane uniaxial anisotropy of the first order. The term of the in-plane uniaxial anisotropy of the first order in the coordinates of Fig. 3 is

$$g_a = -k_{a1} \sin(\psi)^2 \cos(\phi_h - \alpha)^2. \quad (1)$$

FMR frequency is defined by derivatives at position of minimum of free energy⁴⁵⁻⁴⁷ as

$$f_r \sim \gamma (g_{\psi\psi} g_{\phi_m\phi_m} - g_{\psi\phi_m}^2)^{1/2} / \sin(\psi), \quad (2)$$

where γ is the gyromagnetic ratio. See Refs.^{38,45-47} for details.

Dotted data in Fig. 4a show the experimental $f_r(\mu_0 H)$ resonance curves extracted from Fig. 2a. First, we focus on the G-line of the FMR spectrum. In order to fit the data, we have developed the following routine, which allowed us to obtain all magnetic parameters of g and f_r , despite a large number of parameters and their partial interdependency. First, we note that when misalignment θ of orientation of magnetic field with the z -axis is small, and in-plane CPW uniaxial anisotropy k_{a1} is negligible, the linear part at $\mu_0 H \gg 4\pi M_{\text{eff}}$ can be fitted with the simplified expression³⁸

$$f_r = 2\gamma M_s (h - (1 - k_u + 2k_1/3 + 2k_2/9)). \quad (3)$$

Fitting the data in the field range from 0.3 T to 0.4 T with Eq. 3, we obtain the gyromagnetic ratio $\gamma/2\pi =$

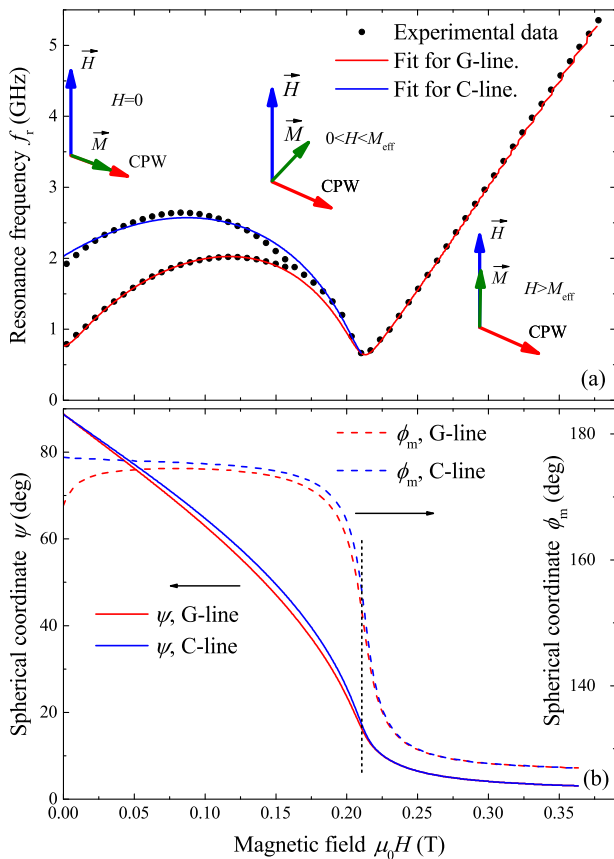


FIG. 4. Fitting experimental $f_r(\mu_0 H)$. (a) The dependence of the FMR frequencies on magnetic field. The CPW induces the uniaxial anisotropy of the 1st (G-line) and the 2nd order (C-line). Pictograms in (a) illustrate orientation of magnetization relative to orientations of magnetic field and CPW axis at different magnetic fields. (b) The dependence of free-energy-minimum orientations of magnetization on magnetic field. The black dotted line indicates position of the kink in FMR curves.

2.985 GHz/kOe, which is close to the ratio for a free electron 2.803 GHz/kOe, and also the value of saturation magnetization in relation with anisotropy parameters $4\pi M_{\text{eff}} = 4\pi M_s \times (1 - k_u + 2k_1/3 + 2k_2/9) = 1975$ Oe. Next we note that (i) the position of the kink at $\mu_0 H \simeq 0.22$ T in the $(f_r, \mu_0 H)$ plot is mostly determined by misalignment of the magnetic field with z -axis, i.e., by θ and ϕ_h ; (ii) the position of the maximum of FMR frequency at $\mu_0 H \simeq 0.12$ T in the $(f_r, \mu_0 H)$ plot is mostly determined by the magnetocrystalline anisotropy parameters k_1 and k_2 ; (iii) the slope of the resonance curve $f_r(\mu_0 H)$ at $H \rightarrow 0$ and the value $f_r(H = 0)$ are defined by the CPW-induced uniaxial anisotropy, i.e., by k_{a1} and α in Eq. 1. Using the least-squares method for optimization through steps (i) to (iii) and back, after several runs, (iv) the fit is further optimized by adjusting parameter k_u . Following routines (i)-(iv) we have obtained an optimum fit of the G-line (see the red curve in Fig. 4a) with

the following parameters: $4\pi M_s = 1876$ Oe, $k_1 = -0.16$, $k_2 = 0.18$, $k_u = -0.12$, $\theta = 1.4$, $\phi_h = 126$, $k_{a1} = 0.025$, and $\alpha = 177$. Importantly, parameters of the cubic magnetocrystalline anisotropy k_1 and k_2 are by a factor of 2-3 higher than typical values at room temperature^{23,38}. This trend correlates well with the temperature dependence of the cubic magnetocrystalline anisotropy in YIG bulk single crystals⁴⁸.

After fitting the G-line, which corresponds to the FMR response of YIG areas at the CPW gaps, the only option to fit the C-line, which corresponds to the FMR response of YIG areas under the central CPW line, is to introduce an additional term into the energy g that represents the second order uniaxial anisotropy induced by the CPW. The term of the in-plane uniaxial anisotropy of the second order in the coordinates of Fig. 3 is

$$g_a = -(k_{a1} + 2k_{a2}) \sin(\psi)^2 \cos(\phi_h - \alpha)^2 + k_{a2} \sin(\psi)^4 \cos(\phi_h - \alpha)^4 \quad (4)$$

Using magnetic parameters obtained for the G-line, the fitting procedure for the C-line with the anisotropy given by Eq. 4 provides $k_{a1} = 0.121$ and $k_{a2} = -0.048$. This fit is shown in Fig. 4a with the blue curve.

Possible origins of the CPW-induced anisotropy include a distinct directionality of microwave currents. Also, directionality of the surface stress can be considered that appears from differences in thermal expansion of narrow central transmission line of metal CPW and YIG/GGG oxides. The surface stress may appear either due to deposition of Nb film at elevated temperature or due to performance of experiments at cryogenic temperatures. For instance, the difference in thermal expansions between Nb and garnets can enable a strain in YIG at 2 K of up to $\epsilon \approx +6 \times 10^{-4}$ along the CPW in case of absence of mechanical relaxation in Nb. In contrast, if a complete relaxation of tensions occurs in Nb at room temperature, the difference in thermal expansions enables the opposite-sign strain in YIG of $\epsilon \approx -4 \times 10^{-4}$. Both values of the strain are well comparable with the growth induced tensions provided by the lattice misfit between the GGG substrate and YIG film that induces the uniaxial anisotropy in LPE-grown²⁸ and PLD-grown films^{49,50}. See the Appendix section for details. Importantly, presence of both first- and second-order anisotropies suggests different mechanisms for their induction.

Figure 4b shows dependencies of orientations of magnetization $\psi(\mu_0 H)$ and $\phi_m(\mu_0 H)$ for C- and G-FMR lines on magnetic field. A marginal difference between C- and G-curves in the entire field range indicates co-alignment of magnetization orientations at both gap and center areas of the CPW, implying that the entire volume of YIG that is subjected to the FMR remains in the single-domain state throughout the experiment.

Our experimental setup does not allow us to study microwave transmission at higher temperatures $T \gtrsim 15$ K. Therefore, temperature dependence of magnetic parameters of YIG is not addressed in this report and can be found elsewhere^{22,23,51}.

B. FMR at $T < T_c$. Impact of the superconducting critical state.

At $T < T_c$ of Nb, in presence of superconductivity, the FMR absorption spectrum changes (see Fig. 2b). Since the Nb CPW is placed directly on top of the YIG film, all changes in absorptions in the C-branch can be attributed to the magnetization state under the Nb line. Therefore, the effect of superconductivity on the FMR can be tracked by analyzing the superconducting critical state of Nb film and its variation with applied magnetic field.

Figure 5a shows the zero-field-cooled (ZFC) transmission spectra that is acquired when the sample is cooled down to 2 K at zero magnetic field, and afterward S_{21} measurements were performed while sweeping magnetic field from 0 to 0.11 T. Figure 5b shows the field-cooled (FC) transmission spectra that is acquired when the sample was cooled down to 2 K at $\mu_0 H = 0.25$ T, and afterward S_{21} measurements were performed while sweeping magnetic field back from 0.11 T down to 0. The hysteresis in peak absorption can be tracked by fitting $S_{21}(f)$ curves at each value of H and plotting dependencies of FMR amplitude I on magnetic field H (Fig. 5c). $I(\mu_0 H)$ dependency is caused by variation of the CPW-FMR coupling strength with magnetic field, i.e., by variation of magnetization and magnetic flux inhomogeneity in the YIG induced by the Nb superconducting critical state. Note that no hysteresis in peak absorption is observed at $T > T_c$ (Figs. 2a and 5c), where the transmission spectra is fully reversible and independent of the ZFC/FC initial state.

First we discuss the ZFC curve in Fig. 5c, where three intervals in $I(\mu_0 H)$ can be distinguished. At low fields, the strongest FMR absorption is observed with $I \sim 0.1$ at $\mu_0 H$ up to 2×10^{-3} T (highlighted with the red circle in Fig. 5a). This corresponds to the Meissner state of the Nb line when the Meissner screening currents circulate at the edges of the Nb film and exclude magnetic flux from its cross-section. In the Meissner state, DC magnetic flux remains homogeneous across the Nb line and ensures a strong coupling of the CPW to the YIG at FMR. At intermediate fields $2 \times 10^{-3} < \mu_0 H < 10^{-2}$ T, the FMR absorption drops rapidly from $I \sim 0.1$ to the minimum $I \sim 0.02$, caused by the partially penetrated superconducting critical state where superconducting vortices start to penetrate Nb film. The magnetic flux profile in partially penetrated superconducting films is the most inhomogeneous^{52–54}, which causes a weak coupling of the FMR to the CPW and low absorption intensity. The partially penetrated state commences at the flux-focus enhanced first critical field of the superconducting film $\mu_0 H_{c1} \sim 2 \times 10^{-3}$ T, where the first Abrikosov vortices start to penetrate into the film, and terminates at the magnetic field of full penetration 10^{-2} T. At high fields $\mu_0 H > 0.01$ T, after full penetration is reached, magnetic flux in the superconducting film forms a constant gradient that can be depicted by the Bean critical

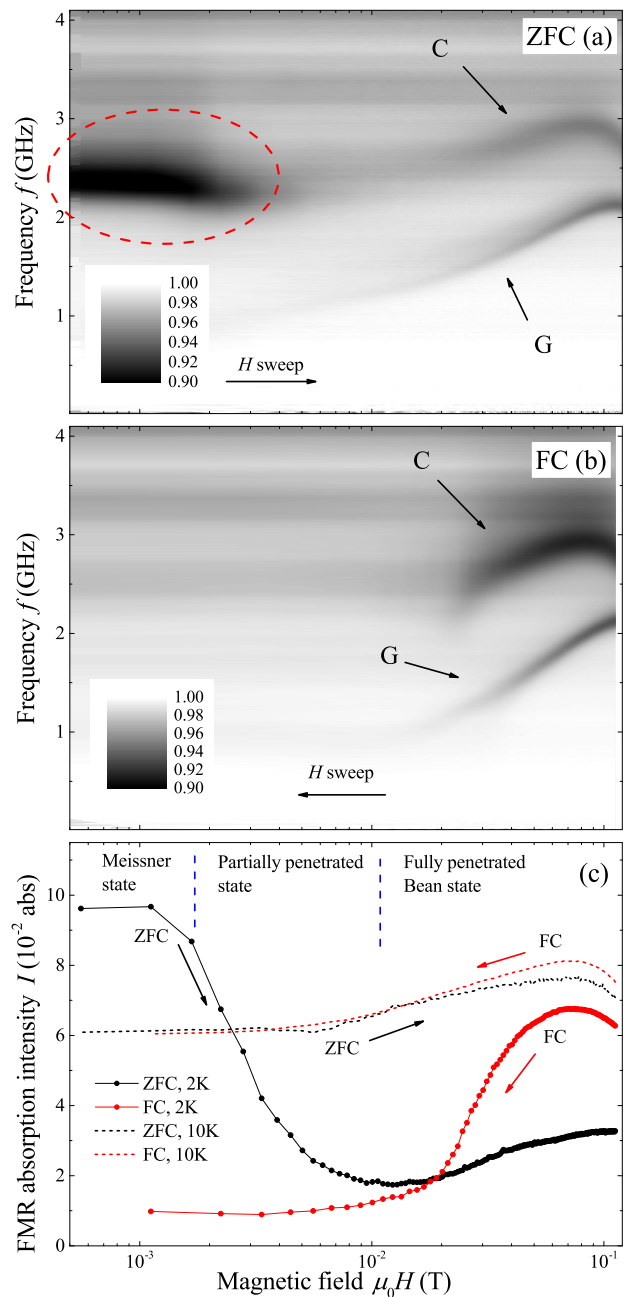


FIG. 5. Gray-scale-coded transmission spectra $|S_{21}(\mu_0 H, f)/S_{21}(\mu_0 H = 0.5 \text{ T}, f)|$ measured at 2 K starting from ZFC state (a) and FC state (b). C and G spectral lines are indicated. Red circle in (a) highlights FMR absorption in the Meissner state of the CPW. c) Dependencies of resonance peak absorption for C-lines on magnetic field $I(\mu_0 H)$ obtained at 2 K and 10 K. Direction of magnetic field sweep is indicated with arrows. The $\mu_0 H$ axis is given on a log scale. Field regions for three superconducting states of Nb at ZFC curve in (c) are separated with blue dashed lines.

state model^{55–58}. The gradient is formed due to pinning of vortices and induces a homogeneous circulating

critical currents. Upon increasing magnetic field, both the pinning of vortices and the slope of magnetic flux reduce^{57,58} making magnetic flux in YIG more homogeneous. A smaller gradient of the magnetic flux in the superconductor increases the coupling that we observe in gradual increase of the FMR peak absorption upon increasing magnetic field from 0.01 T to higher fields. Note that such nonmonotonic behavior of $I(\mu_0 H)$ is not observed for the G-line (Fig. 5a), which indicates additionally that the absorption at G-line is caused by the FMR at the gap areas of the CPW, where the influence of the superconducting state of Nb is marginal.

Increasing magnetic field further beyond the field range in Fig. 5, the ZFC curve should coincide with the FC curve at the so-called irreversibility field^{58–60}, where pinning of vortices becomes negligible. The FC curve in Fig. 5 consists of two parts. For $\mu_0 H > 0.03$ T the coupling remains by a factor of ~ 2 higher than one for the ZFC curve. This difference is attributed to the fact that upon decreasing magnetic field, the Bean critical currents counter-act the Meissner currents, diamagnetic response of the superconducting film is reduced as compared to the ZFC measurement⁶⁰, and the influence on YIG at the FMR decreases. Below 0.03 T, I drops rapidly, which can be explained by a gradual formation of a complex remanent critical state at $H = 0$ with highly nonuniformly distributed frozen magnetic flux. Also at low magnetic fields, magnetization of individual Abrikosov vortices may contribute to YIG inhomogeneity by inducing substantial local magnetic fields of up to $\mu_0 H_v \sim \Phi_0/\pi\lambda_L^2 \sim 0.06$ T, where Φ_0 is the magnetic flux quantum and $\lambda_L \sim 10^{-7}$ m is the typical London penetration depth in Nb films.

Overall, the influence of the superconducting critical state in our geometry on the FMR appears to be destructive. The FMR intensity for both ZFC and FC curves remains below values of I at $T > T_c$ (Fig. 5c). However, magnetic hysteresis often is employed in magnetic logic devices. Also, in vicinity to $H = 0$, FMR is substantially stronger when superconductor is in the Meissner state than for normal metal CPW. This effect may be a result of interaction of magnetic moments in YIG with Meissner screening currents in the ideal diamagnet.

IV. CONCLUSION

In conclusion, ferromagnetic resonance of YIG film is studied in out-of-plane magnetic fields and cryogenic temperatures using a superconducting coplanar waveguide that is fabricated directly on top of the magnetic film (see Fig. 1). FMR absorption spectra are obtained in a wide field range. Nonlinear dependence of the FMR frequency on magnetic field at low field values, below the field of saturation magnetization, showed a split of resonance into two spectral lines, which were identified as the FMR response of YIG at gap areas of the CPW and of YIG located directly under the central conducting line

of the CPW.

A routine was developed for fitting the FMR lines. This routine allowed us to obtain all magnetic parameters of YIG, i.e., the saturation magnetization, the gyromagnetic ratio, and parameters of magnetocrystalline and out-of-plane uniaxial anisotropies. In addition, the fitting routine has issued the misalignment angle of 1.4° between magnetic field and the out-of-plane orientation, as well as parameters of in-plane magnetic anisotropy of the first and the second order, which are induced by the CPW.

The FMR spectrum at temperatures below the superconducting critical temperature of the waveguide showed a hysteresis in FMR peak absorption. The hysteresis is explained by influence of magnetization of the Nb transmission line in the superconducting critical state. Tracking the dependence of the intensity of the FMR on magnetic field allowed us to identify all fundamental states of a superconducting film in out-of-plane magnetic field, i.e., the Meissner state, the partially penetrated state, and the fully penetrated Bean critical state. Also, it allowed explanation the hysteresis in the FMR absorption by the pinning of magnetic vortices, which induces the gradient of magnetic flux in superconducting films. The gradient is controlled by direction of the magnetic field sweep.

In general, this report suggests that development of magnonics at cryogenic temperatures may be beneficial due to: (i) substantially different properties of magnetic materials, including magneto-crystalline anisotropy, (ii) the possibility to engineer additional anisotropies with metal structures, and (iii) the potential to affect the spectra by hybridization of a magnonic media with superconductors. As a final remark we would like to point out a related work by Jeon et al. on the effect of the superconducting critical state on magnetization dynamics in thick superconductor/ferromagnet/superconductor trilayers⁶¹.

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VI. APPENDIX: STRESS INDUCED IN YIG BY NB CPW

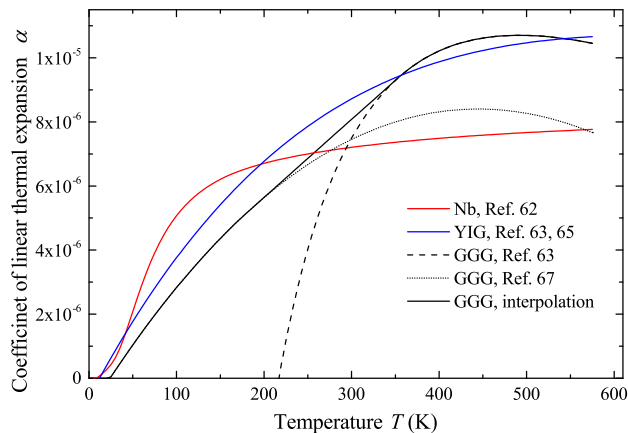


FIG. 6. Dependencies of the thermal expansion coefficient on temperature $\alpha(T)$ for Nb, YIG and GGG.

One possible cause of the CPW induced anisotropy that is derived in Sec. IIIA is the stress in YIG that is forced by differences in thermal expansion of the narrow extended central transmission line of the metal CPW and YIG/GGG oxides. Assuming that an unstressed continuous interface is formed between Nb and YIG during deposition of Nb at the deposition temperature $T_d \approx 600$ K, the stress at the interface at the measurement temperature $T_m = 2$ K can be estimated with the following expression

$$\sigma \approx \frac{E}{1-\nu} \epsilon = \frac{E}{1-\nu} \int_{T_d}^{T_m} [\alpha_G(T) - \alpha_{Nb}(T)] dT, \quad (5)$$

where σ is the stress in YIG, $E = 2 \times 10^{12}$ dyne/cm² is the Young's modulus of YIG at the temperature range from 0 to 300 K⁶², $\nu = 0.29$ is the Poisson's ratio, ϵ is

the strain at the interface at T_m due to the difference in thermal expansion, $\alpha_G(T)$ and $\alpha_{Nb}(T)$ are temperature dependencies of the linear thermal expansion of the garnet and Nb, respectively. Importantly, the stress in Eq. 5 implies absence of mechanical relaxation.

However, estimation of the stress at the Nb/YIG interface using Eq. 5 is impeded. While thermo-mechanical properties of Nb are well studied in a wide temperature range⁶³ from ≈ 0 K up to about the melting point, a consistent study of thermo-mechanical properties of YIG is not available for the required temperature range. The coefficient $\alpha_G(T)$ for YIG is available piecewise and can be obtained by interpolation of $\alpha_G(T)$ at temperatures above^{64,65} and below⁶⁶ the room temperature. On the other side, the coefficient $\alpha_G(T)$ for YIG can be substituted with one for GGG since their thermo-mechanical properties are almost identical^{64,65}. The coefficient $\alpha_G(T)$ for GGG is reported for several temperature ranges separately: room temperature and higher temperature data is available in Refs. ^{64,65}, $\alpha_G(T)$ at low temperatures is reported in Ref. ⁶⁷ for the range from 6 K to 300 K and in Ref. ⁶⁸ for the range from 80 K to 330 K.

Figure 6 shows dependencies of the thermal expansion on temperature $\alpha(T)$. The red curve shows $\alpha_{Nb}(T)$ for Nb that is calculated using Ref. ⁶³. The blue curve shows $\alpha_G(T)$ for YIG that is calculated using Refs. ^{64,66}. Black dashed and dotted curves show $\alpha_G(T)$ for GGG that are calculated using Ref. ⁶⁴ and Ref. ⁶⁸, respectively. Solid black curve shows linear interpolation between lower-temperature and higher-temperature curves $\alpha_G(T)$ for GGG at the range from 180 K up to 330 K. The interpolated dependence for $\alpha_G(T)$ is used for calculations.

Calculations with Eq. 5 and coefficients $\alpha(T)$ in Fig. 6 provide the strain at YIG/Nb interface $\epsilon \approx +6.4 \times 10^{-4}$ that produces a compressive stress $\sigma \sim 10^9$ dyne/cm². Note however, that if the room-temperature deposition of Nb takes place, or the strain in Nb relaxes at room temperature, according to Eq. 5 and Fig. 6 an opposite-sign strain $\epsilon \approx -4 \times 10^{-5}$ emerges at cryogenic temperature T_m . If the data for GGG is used instead of YIG, the integral in Eq. 5 provides approximately the same strain $\epsilon \approx +5.6 \times 10^{-4}$ at the interface with unrelaxed Nb, and a larger opposite-sign strain $\epsilon \approx -4 \times 10^{-4}$ at the interface with the room- T deposited or relaxed Nb. These values are well comparable with the growth induced tensions provided by the lattice misfit between the GGG substrate and the YIG film that induces the uniaxial anisotropy in LPE-grown²⁸ and PLD-grown^{49,50} films.

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