

Article

Multi-Points Cooperative Relay in NOMA System with $N-1$ DF Relaying Nodes in HD/FD Mode for N User Equipments with Energy Harvesting

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Abstract: Non-Orthogonal Multiple Access (NOMA) is the key technology promised to be applied in next-generation networks in the near future. In this study, we propose a multi-points cooperative relay (MPCR) NOMA model instead of just using a relay as in previous studies. Based on the channel state information (CSI), the base station (BS) selects a closest user equipment (UE) and sends a superposed signal to this UE as a first relay node. We have assumed that there are N UEs in the network and the N -th UE, which is farthest from BS, has the poorest quality signal transmitted from the BS compared the other UEs. The N -th UE received a forwarded signal from $N - 1$ relaying nodes that are the UEs with better signal quality. At the i -th relaying node, it detects its own symbol by using successive interference cancellation (SIC) and will forward the superimposed signal to the next closest user, namely the $(i + 1)$ -th UE, and include an excess power which will use for energy harvesting (EH) intention at the next UE. By these, the farthest UE in network can be significantly improved. In addition, closed-form expressions of outage probability for users over both the Rayleigh and Nakagami- m fading channels are also presented. Analysis and simulation results performed by Matlab software, which are presented accurately and clearly, show that the effectiveness of our proposed model and this model will be consistent with the multi-access wireless network in the future.

Keywords: cooperative NOMA; multi-points DF relaying nodes; half-duplex; full-duplex; Rayleigh fading channels; Nakagami- m fading channels; energy harvesting

1. Introduction

The next-generation network (5G) technology has the advantage of increasing system capacity by superior sharing-spectrum efficiency [1]. Therefore, multiple users in the network can be served in the same frequency band/time slot and various allocation power coefficients by the key technology is called Non-Orthogonal Multiple Access (NOMA). The is fundamentally different from previous orthogonal access methods, e.g., Orthogonal Multiple Access (OMA) [2]. In NOMA system, the users with better channel conditions are allocated less transmitting power coefficients. On the other hand, the users with worse channel conditions are allocated more transmitting power coefficients to guarantee the quality of service (QoS) for all users in the system. After receiving a superposed signal, successive interference cancellation (SIC) is done at the end users [3]. In [4], the authors investigated the impact of imperfect SIC on the analysis performance of NOMA system. Their analysis results showed that even though SIC is not perfect, the performance of the NOMA system is still better than the orthogonal system. A down-link NOMA wireless network was studied in [5] by considering using a relay for forwarding

signals to combat the fading effect of the transmission channel. Authors applied to dual-hop relaying systems with decode-and-forward (DF) or amplify-and-forward (AF) protocols [6]. Relay full-duplex (FD) model over the Rayleigh fading channels using the DF protocol investigated the performance by optimizing the transmit power factor [7]. The study impacts relay selection of cooperative NOMA on the performance system [8]. The authors in [9] proposed a novel best cooperative mechanism (BCM) for wireless EH and spectrum sharing in the 5G network. The [10–12] include AF and DF relaying. In [12], it showed that a dual-hop power line communication (PLC) system can improve the system capacity compared to direct-link (DL) transmission. And M. Rabie et al. [13] proposed using Multi-hop relay instead of using one hop relay or dual-hop relays. The authors investigated the energy efficiency over PLC channels with assuming log-normal fading. The studies [14,15] analyzed the system performance of multi-hop AF/DF relaying over PLC channels in terms of average bit error and ergodic capacity. These studies showed that the system performance can be improved by increasing the number of relaying. In addition, The authors in [8] studied the impact of relay selection (RS) on system performance. The compared results on two-stage versus max-min RS showed that cooperative NOMA system over Rayleigh fading channels with two-stage RS is better than the max-min one. We hypothesized that there are N users with the N -th user at the far end from BS with the worst channel condition. The QoS of the N -th user can be improved with the cooperation of $N - 1$ users instead of just receiving only a relay cooperation. At each node, one must perform the best neighbor selection to forward the signal next neighbor. The best selection of neighbors is repeated until the signal reaches the destination.

In addition, we also consider EH at UEs. The explosion of the number of wireless devices, radio frequency (RF) EH becomes a potential technology to convert the energy of receiving wireless signal into electricity. Therefore, the MPCR is not only transmitting information but also delivering energy to the users. In Ref. [16–18], only users located close to BS can collect energy. This is because signal reception and energy collection cannot be done simultaneously. Thus, the users need to divide the received signal for EH and information decoding (ID) by using power splitting (PS) or time switching (TS) which was called “received TS” [19,20]. Though the PS approach has been shown to mostly outperform the receive-TS approach, however, the PS is complicated and inefficient for practical implementation. The research results have shown that PS is better than TS, however, PS is more complex and difficult to practical application than TS. In our study, we consider compressing both information and energy in one transmission phase instead of splitting it into two transmission phases as in previous studies. Furthermore, a user faraway from BS can still receive information and collect energy from the nearest relay node. Researchers have made important contributions to the 5G wireless multi-access network. Specially, L. Dai et al. [21] presented the introduction, development process, and recent research trends on NOMA, comprehensively. Because of the potential application of NOMA in the future, there have been many important research contributions [22–29]. These positive research results are motivations for other researchers to continue to study NOMA improvement.

In this study, we focus on MPCR in NOMA network to improve the QoS for the user faraway from BS with poor channel. In terms of contributions in this research, the main contributions include:

- The first, this article proposes a down-link side NOMA network with random N UEs.
- The next, the MPCR model is proposed to improve QoS for the N th UE with farthest distance from BS among the others users by using $N - 1$ UEs as DF relaying nodes in HD/FD mode. Each UE_i relaying node receives and forwards a superposed signal to next hop, namely UE_{i+1} , which is nearest from UE_i . This work will loop until the superposed signal is sent to last UE, namely UE_N .
- A algorithm for selecting relay nodes in MPCR is also presented clearly in next section.
- At UE_i with $\forall i > 1$, the received signal has an excess power that is used for EH to charge the battery with assuming unlimited capacity of the battery.
- In additional, this study investigates and finds an outage probability and system throughput for each UE, which are written in closed-form expressions.

- Further, The analysis and simulation results are presented in a clear way by the Monte Carlo simulation (10^6 samples of channels) from the Matlab software to prove our propositions.

This article is presented as following. In the next section, namely Experimental Models, we propose system models and analyse two transmission scenarios which are called $N - 1$ relaying nodes in HD or FD mode. In the third section, we have analyzed the system performance on outage probability and system throughput. In Section 4, we use Matlab software to simulate and results will also be presented in this section. A summary of the results of this study will be presented in Section 5.

Notice: In this study, we use a few notations included as

- $h_{a,b}$ is a channel from source a to destination b .
- α_i is an allocation power coefficient for the i -th UE.
- y_i^Ω is the received signal at the i -th UE with Ω protocol where $\Omega = \{HD, FD\}$.
- $\gamma_{i \rightarrow x_j}^\Omega$ is a signal-to-interference-plus-noise-ratios (SINRs) at i -th UE while the i -th UE decodes x_j symbol.
- $\Pr \{.\}$ is a probability.
- $\mathfrak{R}\Theta_i^\Omega$ or $\mathfrak{N}\Theta_i^\Omega$ is an outage probability of the i -th UE with Ω protocol over Rayleigh or Nakagami- m fading channels, respectively.
- R_i^* is a bit rate threshold of the i -th UE.

2. Experimental Models

In previous studies about NOMA, a direct down-link scenario is considered to serve a number of users in the same time slot. However, in such studies, there are usually a fixed number of users. Therefore, they have not shown the generality of the model. In order to ensure the generality, we have upgraded the model to a random and unpredictable number of users.

2.1. Direct Link Scenario

The authors analyzed different NOMA techniques including power domain and code domain [22]. The role of the power domain is proven to be important in determining the performance of the system through the availability of CSI [23]. The BS send a superposed signal S to all UEs in the same power domain and same time slot as following

$$S = \sqrt{P_0} \sum_{j=1}^N \sqrt{\alpha_j} x_j. \tag{1}$$

Thus, the received signal at the i -th UE, $\forall i \in \{1, \dots, N\}$, would be expressed as following

$$y_i^{Dir} = h_{0,i} \sqrt{P_0} \sum_{j=1}^N \sqrt{\alpha_j} x_j + n_i, \tag{2}$$

where $h_{0,i}$ is denoted as the channels from BS to each the i -th UE over Rayleigh or Nakagami- m fading channel. Furthermore, N is a random number of UEs joined to network, α_j in rule with $\sum_{j=1}^N \alpha_j = 1$ is an allocation power coefficient for each UE and P_0 is the transmission power of BS. n_i is denoted as the additive white Gaussian noise (AWGN) of the i -th UE, where $n_i \sim CN(0, N_0)$ with zero mean, variance N_0 and $i \in \{1, \dots, N\}$.

It is important to notice that the channel coefficient from BS to each UE, in paired, is expressed as $h_{0,i}$ in our expressions.

In direct link scenario, the first user in the nearest distance from the BS with the strongest channel conditions was ordered first in the channel gain list. Furthermore, the list is in decreasing order as following

$$h_{0,1} > h_{0,2} > \dots > h_{0,i} > \dots > h_{0,N-1} > h_{0,N}. \tag{3}$$

According to the NOMA theory, users with the worst signal quality should be given priority to allocate the highest transmitting power factor. Another assumption in terms of the NOMA characteristics, we have assumed that the BS already owns the CSI of all UEs fully. In a previous study [30], the authors considered that CSI is available to the system and used to determine the decoding order of user’s data. The authors in [31] studied how NOMA performance depends on power allocation techniques to ensure fairness for users under instantaneous CSI and average CSI. The superimposed signals are sent to the UEs in the same power domain with different power coefficients, in the hope of ensuring system performance and ensuring service quality fairness for all users. Therefore, the list of allocation power factors is arranged in descending order for each UE in the network as

$$\alpha_1 < \alpha_2 < \dots < \alpha_i < \dots < \alpha_{N-1} < \alpha_N. \tag{4}$$

In Figure 1, the UE_N is farthest from the BS. Thus, the x_N symbol is allocated the strongest power factor. Therefore, x_N symbol will be first decoded at all UEs in the network by applying SIC [3]. Furthermore, the order of decoding is done sequentially according to the reversed list of power factor allocations presented in (4) expression. The Signal-to-interference-plus-noise ratios (SINRs) of all UEs have been expressed as

$$\gamma_{i \rightarrow x_j}^{Dir} = \frac{|h_{0,i}|^2 \rho_0 \alpha_j}{|h_{0,i}|^2 \rho_0 \sum_{k=1}^{j-1} \alpha_{k+1}}, \tag{5}$$

where $i \in \{1, \dots, N\}$ and $j \in \{N, \dots, i\}$.

In a special case at the UE_1 , after it decoded x_j symbols with $j \in \{N, \dots, 2\}$ by using (5), UE_1 decodes its own symbol x_1 with only AWGN n_1 as

$$\gamma_{1 \rightarrow x_1}^{Dir} = |h_{0,1}|^2 \rho_0 \alpha_1. \tag{6}$$

Furthermore, ρ_0 in (5) or (6) is signal-to-noise ratio (SNR) which can be calculated by

$$\rho_i = \frac{P_i}{N_0}, \tag{7}$$

where $i \in \{0, \dots, N - 1\}$, e.g., $\rho_0 = P_0/N_0$ with P_0 is the transmitting power of the BS.

The achievable instantaneous bit rate of the i -th UE when it decodes x_j symbol with $x_j \in \{x_N, \dots, x_i\}$ is shown by

$$R_{i \rightarrow x_j}^{Dir} = \frac{1}{2} \log_2 \left(1 + \gamma_{i \rightarrow x_j}^{Dir} \right), \tag{8}$$

where $i \in \{1, \dots, N\}$ and $j \in \{N, \dots, i\}$. If $i \neq j \neq 1$, and $\gamma_{i \rightarrow x_j}^{Dir}$ is given by (5) then. Else if $i = j = 1$, and $\gamma_{i \rightarrow x_j}^{Dir}$ is given by (6) then.

2.2. $N - 1$ DF Relaying Nodes Scenario

On the other hand, the system model in [13] has only one relaying to improve the QoS of UEs which are faraway from the BS. We propose a improved model with using a MPCR model instead of using only one user as a relay device. See in Figure 1, there are N users in the network with descending order channel conditions with the N -th UE has the poorest signal compared to the other UEs. The Figure 1a,b are $N - 1$ HD relaying nodes model and $N - 1$ FD relaying nodes models,

respectively. In FD mode, the relays are impacted by the loop interference channels, which themselves affected the system’s performance. This study investigates the system performance on MPCR in HD or FD mode for N users over Rayleigh or Nakagami- m fading channels. Previous studies on the NOMA system used a cooperative relay to improve system performance compared to a direct transmission system. The contributions of previous studies [30–32] are the motivation for this research to continue to improve system performance.

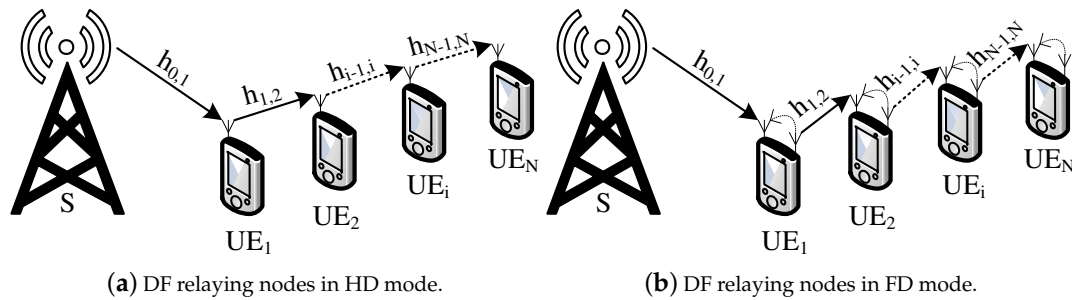


Figure 1. The NOMA system with $N - 1$ relaying nodes in HD/FD mode.

Z. Ding et al. [8] proposed the relay selection method to choose the best relay with the best channel condition by using two-stage relay selection protocol which outperforms versus max-min relay selection protocol. There is a difference compared model in [8] versus our model. The authors consider selection a best relay in N relays to serve for two other users [8]. In our proposed model, Figure 1, all of the $N - 1$ UEs can be selected for relaying node. A selected relay node set is initialized empty $\omega = \emptyset$, and a first relaying node can be selected by

$$\omega_1 = \max \left\{ R_{i \rightarrow x_1}^\Omega > R_1^* \right\}, \tag{9}$$

where $R_{i \rightarrow x_1}^\Omega$ is given by (22), and ω_1 has been added into $\omega = \omega \cup \omega_1$ then.

BS sends a superposed signal to the closest distance user with strongest channel condition, namely UE_1 in the Figure 1a,b, after BS selected UE_1 as a relay successfully. It is important to point out the difference. In this study, each relay node has a single or a twin antenna and works in HD or FD mode.

The received signals at the UE_1 in HD or FD mode are respectively the same like (2) or (10) as

$$y_1^{FD} = h_{0,1} \sqrt{P_0} \sum_{j=1}^N \sqrt{\alpha_j} x_j + h_{LL,1} \sqrt{P_0} \tilde{x}_1 + n_1, \tag{10}$$

where $h_{LL,1}$ is the loop interference channel generated by the itself transmitter antenna, and n_1 is the AWGN noise of the device UE_1 .

In case the UE_1 is working in HD relaying mode, UE_1 decodes its own symbol by applying (5) and (6), respectively. On the other hand, the UE_1 is working in FD relaying mode, UE_1 decodes x_j symbol with $j \in \{N, \dots, 2\}$ or $j = 1$ by applying SINRs in (11a) or (11b), respectively,

$$\gamma_{1 \rightarrow x_j}^{FD} \triangleq \frac{|h_{0,1}|^2 \rho_0 \alpha_j}{|h_{0,1}|^2 \rho_0 \sum_{k=1}^{j-1} \alpha_k + |h_{LL,1}|^2 \rho_1 + 1} \tag{11a}$$

$$\triangleq \frac{|h_{0,1}|^2 \rho_0 \alpha_1}{|h_{LL,1}|^2 \rho_1 + 1}. \tag{11b}$$

Then, the UE_1 sends a mixed signal, namely S_1 in (13), to the next UE which is next nearest relay node, namely UE_2 . The second relay node can be selected by applying (9) as

$$\omega_2 = \max \left\{ R_{i \rightarrow x_2}^\Omega > R_2^*, i = \{1, \dots, N\}, i \notin \omega \right\}, \tag{12}$$

where R_i^Ω is also given by (22) and not being contained in ω set which is a selected relay nodes set. We removed UE_i with $i \in \omega$ from the relays selection because the signal could be sent back to the previous relay node and the superposed signal is unable to send to the UE_N . Furthermore, the ω_2 is also added into ω then. Note that the nearest neighbor represented in [33,34] are neighbors closest to the BS. However, the authors in [35] have extended the definition of nearest neighbor as the device can set up the transmission channel in the best condition compared to the other devices.

A mixed signal is sent to the next relay node as expressed

$$S_1 = \sqrt{P_1} \left(\sqrt{\alpha_1} x_\emptyset + \sum_{j=2}^N \sqrt{\alpha_j} x_j \right), \tag{13}$$

where x_\emptyset is an empty information symbol which was also namely x_1 decoded at the UE_1 .

The received signals at the UE_2 in both HD and FD relaying modes are expressed as, respectively,

$$y_2^{HD} = h_{1,2} \sqrt{P_1} \left(\sqrt{\alpha_1} x_\emptyset + \sum_{j=2}^N \sqrt{\alpha_j} x_j \right) + n_2, \tag{14}$$

and

$$y_2^{FD} = h_{1,2} \sqrt{P_1} \left(\sqrt{\alpha_1} x_\emptyset + \sum_{j=2}^N \sqrt{\alpha_j} x_j \right) + h_{LI,2} \sqrt{P_2} \tilde{x}_2 + n_2, \tag{15}$$

where $h_{1,2}$ is the channel from UE_1 to UE_2 , P_1 is denoted as transmitting power at UE_1 , and $h_{LI,2}$ is loop interference channel from transmitting antenna to receiving one at UE_2 . Specially, the x_1 symbol existed in (2) and (10) but it was replaced by x_\emptyset symbol in (14) and (15). Because x_1 was previously decoded and removed from the mixed signal by UE_1 . Therefore, the x_\emptyset symbol does not contain information and becomes a redundancy in the mixed signal. This paper will use excess power of x_\emptyset symbol for EH purposes as is described in the next section.

The SINRs for decoding x_j symbol and its own x_2 symbol at UE_2 in both HD and FD relaying modes can be expressed, respectively, as following

$$\gamma_{2 \rightarrow x_j}^{HD} \triangleq \frac{|h_{1,2}|^2 \rho_1 \alpha_j}{|h_{1,2}|^2 \rho_1 \sum_{k=2}^{j-1} \alpha_k + 1} \tag{16a}$$

$$\triangleq |h_{1,2}|^2 \rho_1 \alpha_2, \tag{16b}$$

and

$$\gamma_{2 \rightarrow x_j}^{FD} \triangleq \frac{|h_{1,2}|^2 \rho_1 \alpha_j}{|h_{1,2}|^2 \rho_1 \sum_{k=2}^{j-1} \alpha_k + |h_{LI,2}|^2 \rho_2 + 1} \tag{17a}$$

$$\triangleq \frac{|h_{1,2}|^2 \rho_1 \alpha_2}{|h_{LI,2}|^2 \rho_2 + 1}, \tag{17b}$$

where (16a) and (17a) with $j \in \{N, \dots, 3\}$, or (16b) and (17b) with $j = 2$.

After UE_2 decoded its own symbol, it selects a next relay node and sends a new superposed signal to next nearest UE, namely UE_3 . This work will loop until a superposed signal is sent to the farthest UE, namely UE_N in Figure 1.

Proposition 1. *In this study, we propose a EH model to use excess power in the mixed signals for purposing EH as Figure 2. As expressing in (18) and (19), the received signals at the i -th UE, where $i \in \{2, \dots, N\}$, have an empty x_\emptyset symbol with no information. Thus, the transmit power coefficients of each empty symbol can be harvested. In previous studies, the power for EH was transmitted to users on different time slots or on different antennas on the receivers. However, in this study, we use only one antenna for receiving both signals and energy from the transmitter.*

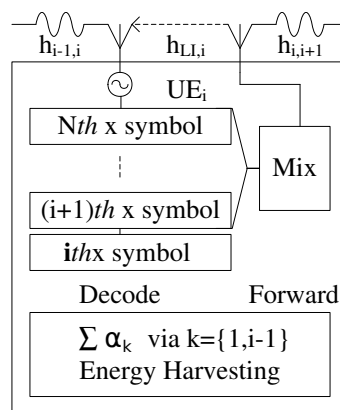


Figure 2. DF protocol and EH protocol at the i -th UE node.

In general, the received signals at the UE_i in both HD and FD relaying nodes can be rewritten by, respectively

$$y_i^{HD} = h_{i-1,i} \sqrt{P_{i-1}} \left(\sum_{l=1}^{i-1} \sqrt{\alpha_l} x_\emptyset + \sum_{k=i}^N \sqrt{\alpha_k} x_k \right) + n_i, \tag{18}$$

and

$$y_i^{FD} = h_{i-1,i} \sqrt{P_{i-1}} \left(\sum_{l=1}^{i-1} \sqrt{\alpha_l} x_\emptyset + \sum_{k=i}^N \sqrt{\alpha_k} x_k \right) + h_{LI,i} \sqrt{P_i} \tilde{x}_i + n_i, \tag{19}$$

where y_i^{HD} and y_i^{FD} are denoted as receiving signals at the UE_i node, $h_{i-1,i}$ is the channel from previous node to current node, P_{i-1} and P_i are transmitting power of previous UE and current UE, respectively.

It is important to notice that $\sum_{l=1}^{i-1} \alpha_l + \sum_{k=i}^N \alpha_k = 1$.

The SINRs of each the i -th UE relaying node for detecting x_j symbol in HD and FD modes are expressed as, respectively

$$\gamma_{i \rightarrow x_j}^{HD} \triangleq \frac{|h_{i-1,i}|^2 \rho_{i-1} \alpha_j}{|h_{i-1,i}|^2 \rho_{i-1} \sum_{k=i}^{j-1} \alpha_k + 1}, \tag{20a}$$

$$\triangleq |h_{i-1,i}|^2 \rho_{i-1} \alpha_i, \tag{20b}$$

and

$$\gamma_{i \rightarrow x_j}^{FD} \triangleq \frac{|h_{i-1,i}|^2 \rho_{i-1} \alpha_j}{|h_{i-1,i}|^2 \rho_{i-1} \sum_{k=i}^{j-1} \alpha_k + |h_{LL,i}|^2 \rho_i + 1}, \tag{21a}$$

$$\triangleq \frac{|h_{i-1,i}|^2 \rho_{i-1} \alpha_i}{|h_{LL,i}|^2 \rho_i + 1}, \tag{21b}$$

where both (20a) and (21a) are with $i \in \{1, \dots, N\}$ and $j \in \{N, \dots, i + 1\}$. Furthermore, both (20b) and (21b) are with $i = j$.

In NOMA theory, reachable instantaneous bit rate can be calculated by

$$R_{i \rightarrow x_j}^\Omega = \frac{1}{2} \log_2 \left(1 + \gamma_{i \rightarrow x_j}^\Omega \right), \tag{22}$$

where $\Omega = \{HD, FD\}$, $i \in \{1, \dots, N\}$, and $j \in \{N, \dots, i\}$. If $i \neq j$, and $\gamma_{i \rightarrow x_j}^\Omega$ is given by (20a) or (21a) then. Else if $i = j$, and $\gamma_{i \rightarrow x_j}^\Omega$ is given by (20b) or (21b) then.

A selected relay node can be performed by

$$\omega_i = \max \left\{ R_{i \rightarrow x_j}^\Omega > R_j^*, i \in \{1, \dots, N\}, i \notin \omega \right\}. \tag{23}$$

Furthermore, a selected relay nodes set ω after the signal has been sent to the UE_N included

$$\omega = \omega_1 \cup \omega_2 \cup \dots \cup \omega_{N-1}. \tag{24}$$

3. The System Performance Analysis

In this section, we evaluate the performance of the system that we have proposed based on outage probability and system throughput, in order.

3.1. Outage Probability

In terms of investigating outage probability, the outage probability is defined as the occurrence of the stop transmitting event if any instantaneous bit rate in (8) or (22) cannot reach minimum bit rate thresholds.

The probability density function (PDF) and cumulative distribution function (CDF) of Rayleigh distribution are shown by, respectively,

$$f_{|h_{a,b}|^2}(x) = \frac{1}{\sigma_{a,b}^2} e^{-\frac{x}{\sigma_{a,b}^2}} dx, \tag{25}$$

and

$$F_{|h_{a,b}|^2}(x) = 1 - e^{-\frac{x}{\sigma_{a,b}^2}}, \tag{26}$$

where $|h_{a,b}|^2$ are random independent variables namely x in PDF and CDF, respectively, with a and b are source and destination of channels, and $\sigma_{a,b}^2$ is mean of channel with $\sigma_{a,b}^2 = E \left[|h_{a,b}|^2 \right]$.

In general, the PDF and CDF over nakagami- m fading channels can be expressed, respectively,

$$f_{|h_{a,b}|^2}(x) = \left(\frac{m}{\sigma_{a,b}^2} \right)^m \frac{x^{m-1}}{\Gamma(m)} e^{-\frac{mx}{\sigma_{a,b}^2}}, \tag{27}$$

and

$$\begin{aligned}
 F_{|h_{a,b}|^2}(x) &= \frac{\gamma\left(m, \frac{mx}{\sigma_{a,b}^2}\right)}{\Gamma(m)} \\
 &= 1 - e^{-\frac{mx}{\sigma_{a,b}^2}} \sum_{j=0}^{m-1} \left(\frac{mx}{\sigma_{a,b}^2}\right)^j \frac{1}{j!}.
 \end{aligned}
 \tag{28}$$

In direct link scenario, outage event occurs if UE_i , where $i \in \{1, \dots, N\}$, cannot decode x_j symbol, where $j \in \{N, \dots, i\}$. The outage probability for each of the joining UE in NOMA system is expressed as

$$\Theta_i^{Dir} = 1 - \prod_{j=N}^i \Pr\left(R_{i \rightarrow x_j}^{Dir} > R_j^*\right).
 \tag{29}$$

where $R_{i \rightarrow x_j}^{Dir}$ is given by (8) and R_j^* is bit rate threshold of UE_j .

By applying the CDF in (25) and (27), the (29) is solved and it can be rewritten in closed-form as

$$\Re\Theta_i^{Dir} = 1 - \prod_{j=N}^i e^{-\frac{R_j^{**}}{\chi_j \rho_0 \sigma_{0,i}^2}},
 \tag{30}$$

and

$$\Re\Theta_i^{Dir} = 1 - \prod_{j=N}^i \left[\frac{\left(\frac{m}{\sigma_{0,i}^2}\right)^m \left(\frac{m}{\sigma_{0,i}^2}\right)^{-m} \Gamma(m) + \left(\frac{R_j^{**}}{\chi_j \rho_0}\right)^m \left(\frac{m R_j^{**}}{\chi_j \rho_0 \sigma_{0,i}^2}\right)^{-m} \left(\Gamma\left(m, \frac{m R_j^{**}}{\chi_j \rho_0 \sigma_{0,i}^2}\right) - \Gamma(m)\right)}{\Gamma(m)} \right],
 \tag{31}$$

where $\Gamma(\cdot)$ and $\Gamma(\cdot, \cdot)$ are gamma function and gamma incomplete function, respectively. Furthermore, $R_j^{**} = 2^{2R_j^*} - 1$. It is important to notice that (30) and (31) are with the users over Rayleigh and Nakagami- m fading channels, respectively. In addition, χ_j in both (30) and (31) is given by

$$\chi_j \triangleq \alpha_j - R_j^{**} \sum_{k=1}^{j-1} \alpha_k
 \tag{32a}$$

$$\chi_j \triangleq \alpha_1,
 \tag{32b}$$

where (32a) is with $\forall i$, and $j \in \{N, \dots, 2\}$ then. Furthermore, Equation (32b) is with $i = j = 1$ then.

Remark 1. Base on the proposed model with $N - 1$ relaying nodes as in Figure 1, this study investigates the outage probabilities of N UE nodes in both HD and FD modes as

$$\Theta_i^\Omega = \left(1 - \underbrace{\prod_{l=1}^{i-1} \Pr\left(R_{l \rightarrow x_i}^\Omega > R_i^*\right)}_{\eta} \right) \text{ and } \left(1 - \underbrace{\prod_{j=N}^i \Pr\left(R_{i \rightarrow x_j}^\Omega > R_j^*\right)}_{\mu} \right),
 \tag{33}$$

where η is the successful probability to detect x_i symbol at previous UEs and μ is the successful probability to detect x_j symbol at the i -th UE. In a special case of the i -th UE with $i = 1$, It is important to notice that η in (33) is equal with zero and the (33) becomes the same with (29). In (33), η and μ are also solved by applying the CDF and gotten closed-form outage probability of each UE node over Rayleigh fading channel on both HD and FD modes as, respectively,

$$\mathfrak{R}\Theta_i^{HD} = \underbrace{\left(1 - \underbrace{\prod_{l=1}^{i-1} e^{-\frac{R_l^{**}}{\psi_l \rho_{l-1} \sigma_{l-1,l}^2}}}_{\eta} \right)}_{A_1} \underbrace{\left(1 - \underbrace{\prod_{j=N}^i e^{-\frac{R_j^{**}}{\chi_j \rho_{j-1} \sigma_{j-1,i}^2}}}_{\mu} \right)}_{A_2}, \tag{34}$$

and

$$\mathfrak{R}\Theta_i^{FD} = \underbrace{\left(1 - \underbrace{\prod_{l=1}^{i-1} \left(e^{-\frac{R_l^{**}}{\psi_l \rho_{l-1} \sigma_{l-1,l}^2}} \frac{\psi_l \rho_{l-1} \sigma_{l-1,l}^2}{\psi_l \rho_{l-1} \sigma_{l-1,l}^2 + R_l^{**} \rho_l \sigma_{LL,l}^2} \right)}_{\eta} \right)}_{B_1} \underbrace{\left(1 - \underbrace{\prod_{j=N}^i \left(e^{-\frac{R_j^{**}}{\chi_j \rho_{j-1} \sigma_{j-1,i}^2}} \frac{\chi_j \rho_{j-1} \sigma_{j-1,i}^2}{\chi_j \rho_{j-1} \sigma_{j-1,i}^2 + R_j^{**} \rho_j \sigma_{LL,i}^2} \right)}_{\mu} \right)}_{B_2}. \tag{35}$$

To be clearer, here is some information that should be clearly explained. We denoted $\mathfrak{R}\Theta_i^\Omega$, where $i \in \{1, \dots, N\}$ and $\Omega = \{HD, FD\}$, is the outage probability of UE_i over Rayleigh fading channels. The η symbol in both (34) and (35) is the successful detected x_i symbol at UE_l probability with $l \in \{1, \dots, i - 1\}$. Similarly, the μ symbol in both (34) and (35) is the successful detected x_j symbol with $j \in \{N, \dots, i\}$ at the UE_i . Here are two cases such as:

- First case with $i = 1, \eta = 0$ in both (34) and (35) then. Furthermore, the outage probability of the UE_1 in HD/FD mode is $\mathfrak{R}\Theta_i^\Omega = \{A_2, B_2\}$.
- In addition, second case with $\forall i > 1$, the (34) and (35) are with $\mathfrak{R}\Theta_i^\Omega = \{A_1.B_1, A_2.B_2\}$.

In only the second case: ψ_i in both (34) and (35) is given by

$$\Psi_i = \left(\alpha_i - R_i^{**} \sum_{k=l}^{i-1} \alpha_k \right). \tag{36}$$

In both cases: χ_j is given by (32a) or (32b) after it has been rewritten as following, respectively,

$$\begin{cases} \chi_j \stackrel{\Delta}{=} \alpha_j - R_j^{**} \sum_{k=i}^{j-1} \alpha_k \\ \chi_j \stackrel{\Delta}{=} \alpha_i \end{cases} \tag{37}$$

Remark 2. The presented results of the studies [8,36] have firmly contributed to the role of NOMA system over the Rayleigh fading channels. However, studies on the NOMA system over the Nakagami- m fading channels have received little attention because of its complexity. Therefore, we investigate the outage probability of each UE over Nakagami- m fading channels with $m = 2$ on both $N - 1$ HD/FD relaying nodes. Furthermore, the (33) can be solved by applying the PDF in (27) which is expressed in closed-form, respectively, as this research contributes.

$$\mathbb{N}\Theta_i^{HD,m=2} = \left(\underbrace{1 - \prod_{l=1}^{i-1} \left[e^{-\frac{2R_i^{**}}{\psi_i \rho_{l-1} \sigma_{l-1,l}^2} \frac{2R_i^{**} + \psi_i \rho_{l-1} \sigma_{l-1,l}^2}{\psi_i \rho_{l-1} \sigma_{l-1,l}^2}} \right]}_{\eta} \right)_{C_1} \left(\underbrace{1 - \prod_{j=N}^i \left[e^{-\frac{2R_j^{**}}{\chi_j \rho_{i-1} \sigma_{i-1,i}^2} \frac{2R_j^{**} + \chi_j \rho_{i-1} \sigma_{i-1,i}^2}{\chi_j \rho_{i-1} \sigma_{i-1,i}^2}} \right]}_{\mu} \right)_{C_2}, \tag{38}$$

and

$$\mathbb{N}\Theta_i^{FD,m=2} = \left(\underbrace{1 - \prod_{l=1}^{i-1} \left[e^{-\frac{2R_i^{**}}{\psi_i \rho_{l-1} \sigma_{l-1,l}^2} \frac{\psi_i \rho_{l-1} \sigma_{l-1,l}^2 (\psi_i \rho_{l-1} \sigma_{l-1,l}^2 (\psi_i \rho_{l-1} \sigma_{l-1,l}^2 + 2R_i^{**}) + \rho_l \sigma_{L,l}^2 R_i^{**} (3\psi_i \rho_{l-1} \sigma_{l-1,l}^2 + 2R_i^{**}))}{(\psi_i \rho_{l-1} \sigma_{l-1,l}^2 + \rho_l \sigma_{L,l}^2 R_i^{**})^3}} \right]}_{\eta} \right)_{D_1} \left(\underbrace{1 - \prod_{j=N}^i \left[e^{-\frac{2R_j^{**}}{\chi_j \rho_{i-1} \sigma_{i-1,i}^2} \frac{\chi_j \rho_{i-1} \sigma_{i-1,i}^2 (\chi_j \rho_{i-1} \sigma_{i-1,i}^2 (\chi_j \rho_{i-1} \sigma_{i-1,i}^2 + 2R_j^{**}) + \rho_i \sigma_{L,i}^2 R_j^{**} (3\chi_j \rho_{i-1} \sigma_{i-1,i}^2 + 2R_j^{**}))}{(\chi_j \rho_{i-1} \sigma_{i-1,i}^2 + \rho_i \sigma_{L,i}^2 R_j^{**})^3}} \right]}_{\mu} \right)_{D_2}. \tag{39}$$

There have been two cases described above. It is not necessary to represent these cases. The analysis results will be presented in the next section. See Appendix A for proofing of remarks.

3.2. System Throughput

The total achievable received data rate at UE_i , which is denoted as system throughput P_{sum}^Ω , is the sum of throughput results of all UEs in system shown by

$$P_{sum}^\Omega = \sum_{i=1}^N P_i^\Omega = \sum_{i=1}^N (1 - \Theta_i^\Omega) R_i^*. \tag{40}$$

3.3. A Proposal for Energy Harvesting

Proposition 2. In (18) and (19), the received signals at UE_i , with $\forall i > 1$, include two parts which are x_k data symbol and x_\emptyset empty symbol where $k \in \{i, \dots, N\}$ and $l \in \{1, \dots, i - 1\}$. The x_\emptyset does not contain information. Therefore, we proposed collecting the energy of allocating power coefficient of the x_\emptyset symbol for charging the battery. Another assumption is that the battery is not limited by capacity. Thus, the EH for each UE in both HD and FD scenarios are expressed by, respectively

$$EH_i = \xi \sqrt{\sum_{l=1}^{i-1} \alpha_l \rho_{i-1} |h_{i-1,i}|^2}, \quad (41)$$

where $i \in \{2, \dots, N\}$ and ξ is collection coefficient.

3.4. A Proposed Algorithm for $N - 1$ Relaying Nodes

Proposition 3. In this section, an algorithm for processing with $N - 1$ relaying nodes as shown in Figure 1 is proposed. The treatment flow is done in the waterfall pattern in the order shown in Figure 2.

1. Generate a random N UEs in the network with N channels from BS to UEs.
2. Creating a list of channels in descending order with the element at the top of the list is the best channel. Upon completion of the arrangement, BS will know which user is best chosen to use for first hop relaying node.
3. Through the results of the analysis [30], the authors have found that the performance of the NOMA system depends on the efficiency of the power allocation and the selection of the bit rate threshold, accordingly. Lack of CSI may affect the performance of the NOMA system. We have assumed that at BS and at each UE, there is full CSI of the UEs. Based on ordering of SCI as shown in (3), allocate the power coefficients and select the bit rate threshold for the UEs as, respectively

$$\alpha_i = \frac{\min(\sigma_{0,j}^2)}{\sum_{k=i}^N \sigma_{0,k}^2}, \quad (42)$$

and

$$R_i^* = \frac{\max(\sigma_{0,i}^2)}{\sum_{k=i}^N \sigma_{0,k}^2}, \quad (43)$$

where in ordering and paring $i \in \{1, \dots, N\}$ and $j \in \{N, \dots, 1\}$. After the BS allocates the transmit power factor to the UEs, logically, a superposed signal will be sent to the nearest UE which is selected as the first hop relaying node, namely UE_1 .

4. The UE_1 receives and decodes x_j symbol with $j \in \{N, \dots, i\}$ by (20a)–(21b), and excess power is collected by the UE for recharging. The UE_1 will select a next relay node by (23) and send a superposed signal as (18) or (19) to next hop relaying node after UE_1 detects its own symbol, namely x_1 , successfully. This work (step 4) will be repeated until the superposed signal will be transmitted to the last UE, namely UE_N in model. The outage probability will occur when x_j , where $j \in \{N, \dots, i\}$, cannot be detected successfully at UE_i with $i \in \{1, \dots, N\}$.

4. Numerical Results and Discussion

It is important to announce that all of our analysis results are simulated by the Matlab software and are presented accurately and clearly. We undertake no reproduction of any prior research results. Furthermore, this study does not use any given data set, channels were generated randomly during the simulation of a rule. e.g., if there are random N users, the random channels are arranged according to the rule $h_{0,1} > h_{0,2} > \dots > h_{0,i} > \dots > h_{0,N-1} > h_{0,N}$ and the corresponding channel coefficients $1/1 > 1/2 > \dots > 1/i > \dots > 1/(N-1) > 1/N$.

For the results to be clear and accurate, we have performed the Monte Carlo simulation with 10^6 random samples of each $h_{a,b}$ channel.

4.1. Numerical Results and Discussion for Outage Probability

It is important to note that the outage probability results of Dir, HD and FD scenarios are presented by black dashed lines, red dash-dot lines, and blue solid lines, respectively, as shown in Figure 3a,b.

In the first case, we assume that there are only three users connected in the network at t -th time slot. We analyzed the performance of the system based on the outage probability of each user in three different scenarios such as Dir, HD and FD schemes. There are some simulation parameters, e.g., the channel coefficients $h_{0,1} = 1$, $h_{0,2} = 1/2$, and $h_{0,3} = 1/3$ are in accordance with the earlier presented assumptions. Based on the transmission channel coefficients of the users, we can allocate power factors for the users UE_1 , UE_2 , and UE_3 with $\alpha_1 = 0.1818$, $\alpha_2 = 0.2727$, $\alpha_3 = 0.5455$, respectively, with $\sum_{i=1}^3 \alpha_i = 1$ by applying (42). Because the third user, namely UE_3 , has the poorest signal quality, it is prioritized to allocate the biggest power factor among the users. Our analysis results showed that users who are far from BS with poor signal quality have better results, e.g., the outage probability results of the UE_2 and the UE_3 are better than the UE_1 , although their signal qualities are weaker than the first one. In addition, Figure 3a showed that UE_3 has the outage probability results which were marked with diamond marker, which are the best results compared to the other ones, although UE_3 has the weakest signal quality $h_{0,3} = 1/3$. Because UE_3 receives cooperation from the other UEs, the UE_3 's QoS has been improved and is better than the other ones. These results demonstrate the effectiveness of the proposed MPCR model. In addition, the outage probability results of the first user, namely UE_1 , has worse results than the other UEs, and U_1 's outage probability results approximate to each other in all three scenarios, namely Dir, HD and FD relaying scenarios. The UE_1 with the strongest channel coefficient $h_{0,1} = 1$ has been allocated the worst power coefficient $\alpha_1 = 0.1818$ compared to the others. A previous study of FD relay [37,38] and the results of comparison between FD and HD [27] showed that the outage probability results of the relaying in FD mode was worse than the HD one. There is a similarity in these research results. The system performance efficiency of the MPCR model with $N - 1$ FD relaying nodes has resulted in approximation with $N - 1$ HD relaying nodes in the low dB SNRs. However, as ascending the SNRs, the performance of the MPCR system with $N - 1$ HD relaying nodes becomes better demonstrated by the red dash-dot lines in Figure 3a. Specifically, the first user's outage probability results in the FD scenario are the worst. However, there is not much difference compared to the other scenarios, such as Dir and HD scenarios. The reason is that the first relaying node in FD mode is affected by its own antenna channel noise, whereas in the direct and HD transmission scenarios with one antenna there are no loop interference channels.

To be more clear, we increased the number of users in the network to $N = 4$ users with the channel coefficient of UE_4 was $h_{0,4} = 1/4$ at $(t+1)$ -th time slot. In addition, the outage probability of the users are presented in Figure 3b. This is because the system has a new joined user, namely UE_4 , involved in the network with very weak signal quality. Therefore, we reused (42) to reallocate the transmit power factors to the users with $\alpha_1 = 0.12$, $\alpha_2 = 0.16$, $\alpha_3 = 0.24$, $\alpha_4 = 0.48$ as showing in Table 2. This is also because the power distribution coefficients have been changed. As a result, the instantaneous bit rate thresholds of users have been changed accordingly. The instantaneous bit rate thresholds of the user are $R_i^* = \{0.48, 0.24, 0.16, 0.12\}$ bps/Hz with $i \in \{1, \dots, 4\}$. In this case, to ensure the QoS to the fourth user with the poorest signal quality, we have allocated to this user the biggest power factor, namely $\alpha_4 = 0.48$, and the lowest threshold, namely $R_4^* = 0.12$ bps/Hz, compared with the other users in the network. In addition, the other users must share power coefficient to UE_4 in the same power domain. The compared row contents in Tables 1 and 2 correspondingly, both α_i and R_i^* with $i = \{1, 2, 3\}$ are reduced for sharing power and bit rate to UE_4 . As showing in Figure 3b, although the UE_4 has the poorest signal quality, it has the best outage probability results. This demonstrates that the MPCR combines with allocating power factor and instantaneous bit rate threshold selection are effective. In particular, the outage probability results in both HD and FD scenarios using $N - 1$ relaying nodes always outperform the scheme with no relaying.

Table 1. 3 UEs in NOMA system at t -th time slot.

UEs	Channels	Allocation Power Coefficients	Bit Rate Thresholds
UE_1	$h_{0,1} = 1$	$\alpha_1 = 0.1818$	$R_1^* = 0.5455$
UE_2	$h_{0,2} = 0.5$	$\alpha_2 = 0.2727$	$R_2^* = 0.2727$
UE_3	$h_{0,3} = 0.3333$	$\alpha_3 = 0.5455$	$R_3^* = 0.1818$

Table 2. 4 UEs in NOMA system at $(t+1)$ th time slot.

UEs	Channels	Allocation Power Coefficients	Bit Rate Thresholds
UE_1	$h_{0,1} = 1$	$\alpha_1 = 0.1200$	$R_1^* = 0.4800$
UE_2	$h_{0,2} = 0.5$	$\alpha_2 = 0.1600$	$R_2^* = 0.2400$
UE_3	$h_{0,3} = 0.3333$	$\alpha_3 = 0.2400$	$R_3^* = 0.1600$
UE_4	$h_{0,4} = 0.2500$	$\alpha_4 = 0.4800$	$R_4^* = 0.1200$

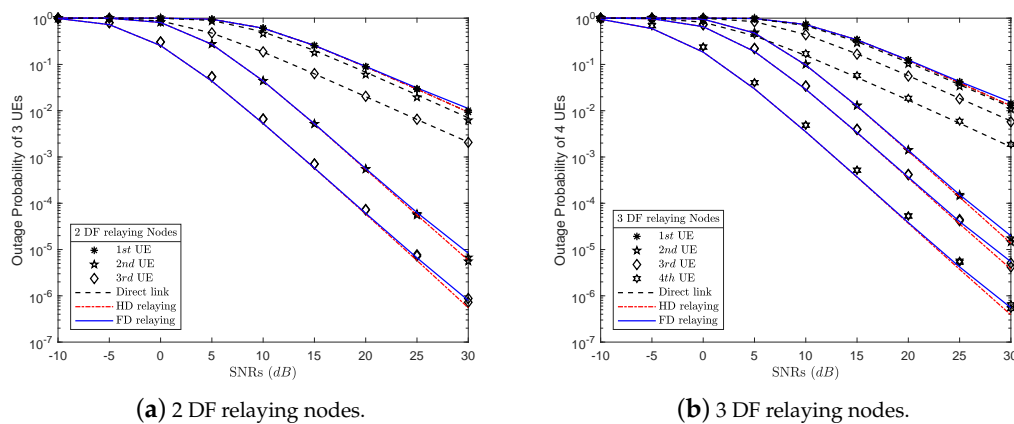


Figure 3. The outage probability results of $N = \{3, 4\}$ UEs over Rayleigh fading channels.

Furthermore, this study investigates the impact of both allocation power coefficient and SNRs affecting user’s service quality, especially weak users. In Figure 3b, the weakest user, namely UE_4 , has been assigned a fixed power factor $\alpha_4 = 0.48$. This study considers if the power allocation coefficient for UE_4 increases or decreases, the quality of service of UE_4 is varied over the corresponding SNRs. For simplicity, we assume that user UE_4 and the other users are over the Rayleigh fading channel. On the other hand, the UE_4 and the other users that are over Nakagami- m fading channels will be analyzed later. This study has assumed that the fourth user can be allocated a variable power factor $\alpha_4 \in \{0.1, \dots, 0.9\}$. The Figure 4 shows the outage probability of the UE_4 with the allocation power factor which can be variable by one-by-one submitting each variable value α_4 into (34), (35), (38), and (39). It is important to notice that the outage probability results of UE_4 in direct, HD relaying, FD relaying scenario are presented by solid grid, dashed grid, and dash-dot grid, respectively. The Figure 4 showed that the outage probability results of UE_4 with the cooperation of 3 HD relaying nodes and 3 FD relaying nodes in MPCR scenarios are better than the UE_4 ’s results in direct scenario. Specially, the outage probability results of UE_4 in MPCR system with $N - 1$ HD/FD relaying nodes are also approximations in all SNRs. These results are consistent with the UE_4 ’s results presented earlier in Figure 3b.

In addition, this study investigates the outage probability of the users over Nakagami- m fading channels scenario versus the ones over Rayleigh fading channels scenario as shown in Figure 5. To ensure that this comparison is fair, the simulation parameters in the Nakagami- m fading channels scenario are the same as the simulation parameters shown in Table 1. Therefore, it is not necessary to represent these simulation parameters. In low SNRs, the outage probability results of the users over Rayleigh fading channels and Nakagami- m fading channels are approximated. However, when the

SNRs are increased, the outage probability results of the users over the Nakagami-m scenario are greatly improved.

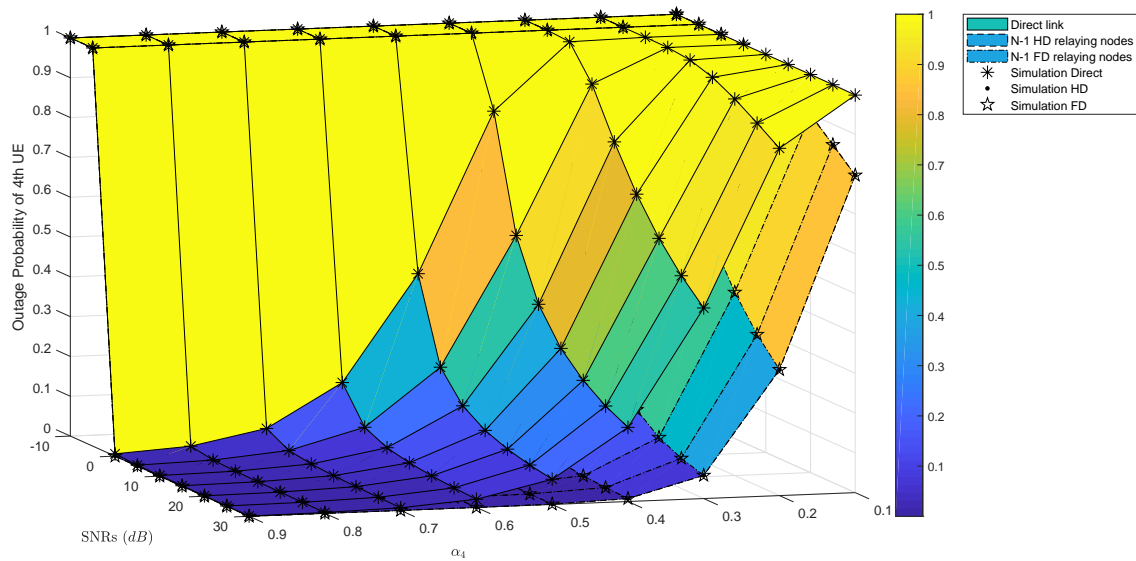


Figure 4. The outage probability results of 4th UE with $\alpha_4 = \{0.1, \dots, 0.9\}$ and SNRs = $\{-10, \dots, 30\}$.

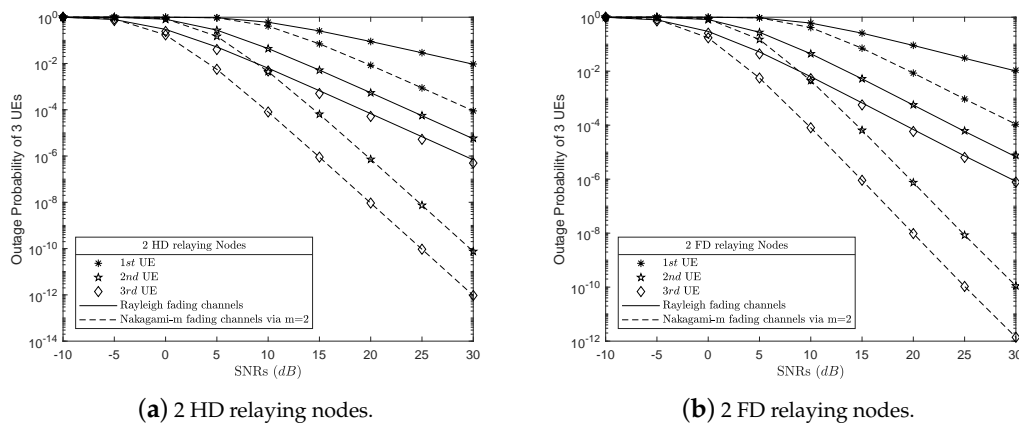


Figure 5. The outage probability results of three UEs over Rayleigh fading channels versus Nakagami- m fading channels via $m = 2$.

4.2. Numerical Results and Discussion for System Throughput

In system performance evaluation, system throughput is an important criterion that is known as the sum of instantaneous achievable bit rate of each user in the system. We reuse the simulation parameters as described in the evaluation of the outage probability shown in Tables 1 and 2. Therefore, we do not restate these parameters. The system throughput of each user with $N = 3$ UEs and $N = 4$ ones are presented in Figure 6a,b, respectively. It is important to notice that the solid lines, dash-dot lines and dashed lines are the system throughput of the users in Dir, HD and FD scenarios, respectively. This is because the outage probability results of the users in HD and FD scenarios are approximately equal. As a result, the throughput results of these users are also approximately equal. Thus, the dash-dot lines and dashed ones are overlapped in both Figure 6a,b. The analysis results showed that the system throughput of users in the $N - 1$ HD/FD relaying nodes scenarios are always better than the system throughput of the ones in the non-relay scenario. Specifically, the first UE's system throughput is approximate in all three scenarios. At SNR in 30 dB, all users in three scenarios reach their bit rate thresholds R_i^* .

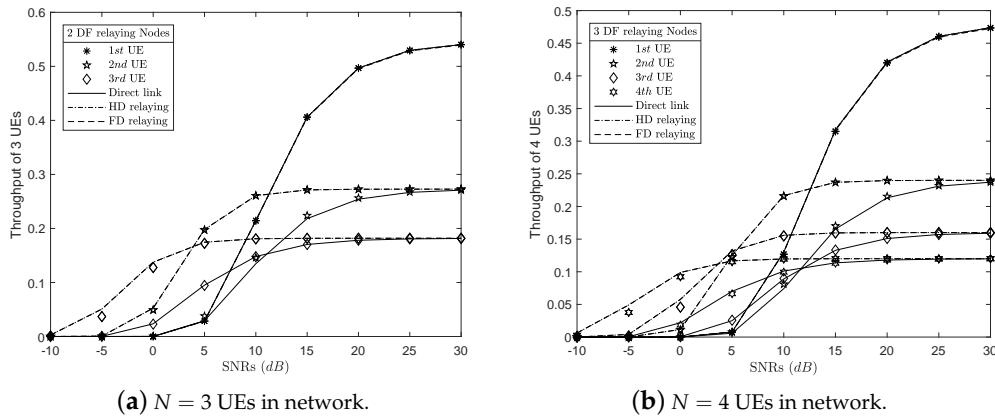


Figure 6. The system throughput results of the users over Rayleigh fading channels.

On the other hand, this study analyzes the impact of the allocation power factor α_4 on the fourth user’s throughput with variable $\alpha_4 \in \{0.1, \dots, 0.9\}$ values instead fixing $\alpha_4 = 0.48$. As shown in Figure 7, higher grid lines are better results than the other ones. In this case, the instantaneous bit rate threshold of UE_4 is $R_4^* = 0.12$ bps/Hz. In low SNRs, e.g., $SNR = 0$ db, the system throughput results in all scenarios being approximately zero. On the other hand, although the SNRs have been increased, e.g., $SNR = 10$ dB, the system throughput results are still approximately zero if the power factor, namely α_4 , is still in low, e.g., $\alpha_4 = 0.1$. However, with $\alpha_4 = 0.4$ and SNR is still held in 10 dB, the system throughput results of UE_4 in both three HD relaying nodes and three FD relaying nodes in MPCR scenarios are improved and reach their bit rate threshold. The Figure 6b showed that at SNR in 10 dB and $\alpha_4 = 0.48$, the UE_4 reach its bit rate threshold, approximately. Another e.g., in paired $\alpha_4 = 0.5$ and $SNR = 0$ dB, UE_4 also reach its bit rate threshold in Figure 7. By this analysis, we can find pairs of values α_4 and SNR where UE_4 can reach the threshold $R_4^* = 0.12$ bps/Hz.

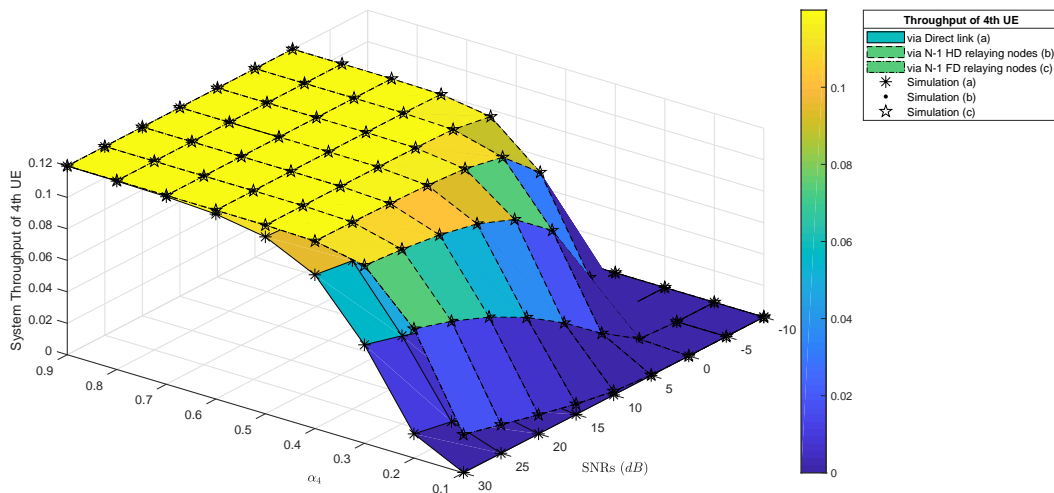


Figure 7. The throughput of the 4th UE over Rayleigh fading channels with $\alpha_4 = \{0.1, \dots, 0.9\}$ and $SNRs = \{-10, \dots, 30\}$ dB.

The system throughput of the users in $N - 1$ HD relaying nodes over both Rayleigh and Nakagami- m scenarios were analyzed, compared and presented in Figure 8a. In Figure 8a, there are $N = 3$ UEs over Rayleigh fading channels and Nakagami- m fading channels with solid lines and dashed ones, respectively. This is because of the results of $\Theta_1^{HD} > \Theta_2^{HD} > \Theta_3^{HD}$ as shown in Figure 5a. By applying (40), we get $P_1^{HD} < P_2^{HD} < P_3^{HD}$ with low SNRs. With increasing SNRs, the system throughput of each UE changes, e.g., $SNR = 30$ dB, $P_1^{HD} > P_2^{HD} > P_3^{HD}$ and reach their bit rate thresholds R_i^* .

The similarly results also happen in $N - 1$ FD relaying nodes scheme as shown in Figure 8b. Specifically, because the users over Nakagami- m fading channels have better outage probability results than the ones over the Rayleigh fading channels as shown in Figure 5b, in some SNRs, e.g., $\text{SNR} = 10$ dB then $\mathfrak{N}\Theta_i^{FD} < \mathfrak{R}\Theta_i^{FD}$. Therefore, $\mathfrak{N}P_i^{FD} > \mathfrak{R}P_i^{FD}$ where \mathfrak{N} and \mathfrak{R} were denoted as Nakagami- m and Rayleigh fading channels, respectively, after applying (40). These results proved that the Nakagami- m channel is better than the Rayleigh channel. However, when SNRs are increasing, the users have the throughput results approximately and close to the thresholds $\mathfrak{N}P_i^{HD} \approx \mathfrak{R}P_i^{HD} \approx R_i^*$.

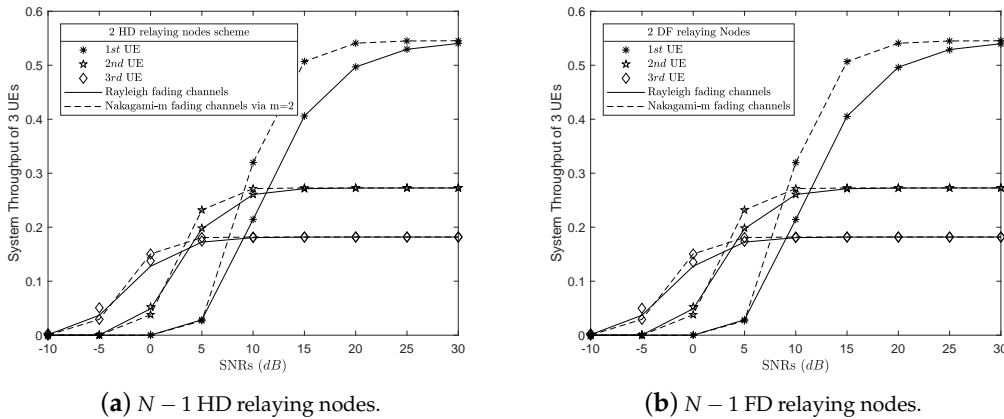


Figure 8. Comparison of the system throughput results of Rayleigh versus Nakagami- m via $m = 2$.

4.3. N UEs with $N - 1$ HD/FD Relaying Nodes

As modeling Figure 1a,b, the proposed Proposition 3 can investigate the system performance with N UEs where N is a random and big number. Because of the limited power of our personal computers, this study only investigates and presents cases where there are only three or four users, $N = \{3, 4\}$, in the system. However, the results presented do not show all the advantages of proposing algorithm. Thus, we are increasing the limit the number user with bigger number N . As shown in Figure 9a,b, there are 9 UEs in the network. By applying Proposition 3, we investigated the outage probability of the UEs in the network over both Rayleigh and Nakagami- m fading channels. For e.g., in $N - 1$ HD relaying nodes scenario, the outage probability of the first UE, namely UE_1 , can be calculated by (34) or (28) over Rayleigh or Nakagami- m fading channels with $m = 2$, respectively, where $\eta = 0$. Another e.g., in FD scenario, the outage probability of last UEs, namely UE_9 , over Rayleigh or Nakagami- m fading channels can be computed by (35) or (39), respectively. With the number of users is greater than nine UEs, $N > 9$, the results of the analysis are difficult to observe in the figure and it needs more time for the simulation. Therefore, we end the investigation with up to nine users in network.

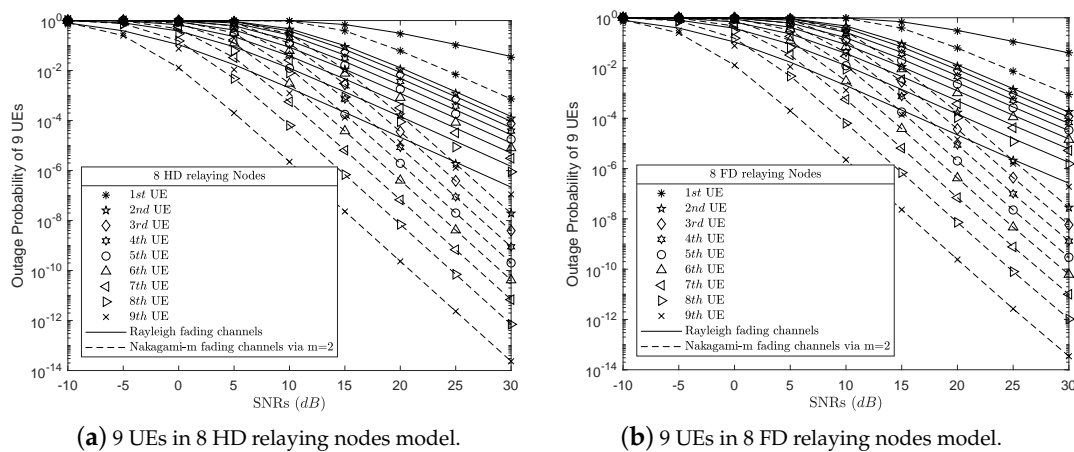


Figure 9. Comparison of the outage probability results of Rayleigh versus Nakagami- m fading channels.

5. Conclusions

In this study, we proposed a novel NOMA network model with $N - 1$ relaying nodes instead of using only one relay as in previous studies. A superposed signal would be sent through $N - 1$ relaying nodes before it reaches the farthest UE which is denoted by UE_N . The closed-form expressions of $N - 1$ HD/FD relaying nodes scenarios over Rayleigh/Nakagami- m fading channels are also presented along with an explanation for the corresponding processing. By presenting results in the figures, our proposed models with $N - 1$ HD/FD relaying nodes are effective for applying to the cooperated NOMA network in the next generation of wireless telecommunications.

Author Contributions: T.-N.T. is the first author who proposed the main idea, analyzed and simulated the system, and presented the writing—original draft preparation, writing—review and editing, visualization. M.V. is the second author who has experience in wireless communication research. He has made a supervision, review, and given the first author some useful comments and funding acquisition for this research. All authors read and approved the final manuscript.

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Abbreviations

The following abbreviations are used in this manuscript:

No.	Abbreviations	Full description
1	AWGNs	Additive white Gaussian noises
2	BS	Base station
3	CDF	Cumulative distribution function
4	CSI	Channel state information
5	FD	Full-duplex
6	Fig.	Figure
7	HD	Half-duplex
8	MPCR	Multi-Point Cooperative Relay
9	NOMA	non-orthogonal multiple access
10	PDF	Probability density function
11	QoS	Quality of service
12	S	Source
13	SIC	Successive interference cancellation
14	SINR	Signal-to-interference-plus-noise ratio
15	SNR	Signal-to-noise ratio
16	UEs	User Equipments

Appendix A

Proof of $N - 1$ HD relaying nodes scenario: The condition for occurrence of the outage events has been presented in (33). By substituting (22), where $\Omega = HD$, into (33), we can get an expression for computing the outage probability of each UE in $N - 1$ HD relaying nodes scenario as following

$$\Theta_i^{HD} = \left(1 - \prod_{l=1}^{i-1} \Pr \left(|h_{l-1,l}|^2 > \frac{R_l^{**}}{\chi_l \rho_{l-1}} \right) \right) \text{ and } \left(1 - \prod_{j=N}^i \Pr \left(|h_{i-1,i}|^2 > \frac{R_j^{**}}{\chi_j \rho_{i-1}} \right) \right). \quad (\text{A1})$$

The (A1) can be rewritten in experimental integral by applying the PDF (25) of Rayleigh distributions as

$$\Re\Theta_i^{HD} = \left(1 - \prod_{l=1}^{i-1} \int_{\frac{R_l^{**}}{\chi_i \rho_{l-1}}}^{\infty} \frac{1}{\sigma_{l-1,l}^2} e^{-\frac{x}{\sigma_{l-1,l}^2}} dx \right) \text{ and } \left(1 - \prod_{j=N}^i \int_{\frac{R_j^{**}}{\chi_j \rho_{i-1}}}^{\infty} \frac{1}{\sigma_{i-1,i}^2} e^{-\frac{x}{\sigma_{i-1,i}^2}} dx \right). \tag{A2}$$

The (A2) can be solved and expressed as (34).

On the other hand, the (A2) can be written with the PDF (27) of Nakagami- m fading channels as following

$$\Re\Theta_i^{HD} = \left(1 - \prod_{l=1}^{i-1} \int_{\frac{R_l^{**}}{\chi_i \rho_{l-1}}}^{\infty} \left(\frac{m}{\sigma_{l-1,l}^2} \right)^m \frac{x^{m-1}}{\Gamma(m)} e^{-\frac{mx}{\sigma_{l-1,l}^2}} dx \right) \text{ and } \left(1 - \prod_{j=N}^i \int_{\frac{R_j^{**}}{\chi_j \rho_{i-1}}}^{\infty} \left(\frac{1}{\sigma_{i-1,i}^2} \right)^m \frac{x^{m-1}}{\Gamma(m)} e^{-\frac{mx}{\sigma_{i-1,i}^2}} dx \right). \tag{A3}$$

and after the (A3) was solved, it can be expressed as (38). □

Proof of $N - 1$ FD relaying nodes scenario: Similarly, by submitting (22) with $\Omega = FD$ into (33), we can get an expression for computing the outage probability of each UE in $N - 1$ FD relaying nodes scenario

$$\Theta_i^{FD} = \left(1 - \prod_{l=1}^{i-1} \Pr \left(|h_{l-1,l}|^2 > \frac{R_l^{**} (|h_{L,l}|^2 \rho_l + 1)}{\chi_i \rho_{l-1}}, |h_{L,l}|^2 > 0 \right) \right) \left(1 - \prod_{j=N}^i \Pr \left(|h_{i-1,i}|^2 > \frac{R_j^{**} (|h_{L,i}|^2 \rho_i + 1)}{\chi_j \rho_{i-1}}, |h_{L,i}|^2 > 0 \right) \right). \tag{A4}$$

The (A4) is also rewritten in experimental integral by applying the PDF of Rayleigh or Nakagami- m fading which are respectively (25) or (27), respectively, as

$$\Re\Theta_i^{HD} = \left(1 - \prod_{l=1}^{i-1} \int_0^{\infty} \int_0^{\infty} \frac{1}{\sigma_{l-1,l}^2 \sigma_{L,l}^2} e^{-\left(\frac{x}{\sigma_{l-1,l}^2} + \frac{y}{\sigma_{L,l}^2}\right)} dx dy \right) \left(1 - \prod_{j=N}^i \int_0^{\infty} \int_0^{\infty} \frac{1}{\sigma_{i-1,i}^2 \sigma_{L,i}^2} e^{-\left(\frac{x}{\sigma_{i-1,i}^2} + \frac{y}{\sigma_{L,i}^2}\right)} dx dy \right), \tag{A5}$$

and

$$\Re\Theta_i^{FD} = \left(1 - \prod_{l=1}^{i-1} \int_{\frac{R_l^{**} (y \rho_l + 1)}{\chi_i \rho_{l-1}}}^{\infty} \int_0^{\infty} \left(\frac{m^2}{\sigma_{l-1,l}^2 \sigma_{L,l}^2} \right)^m \frac{(xy)^{m-1}}{(\Gamma(m))^2} e^{-m \left(\frac{x}{\sigma_{l-1,l}^2} + \frac{y}{\sigma_{L,l}^2} \right)} dx dy \right) \left(1 - \prod_{j=N}^i \int_{\frac{R_j^{**} (y \rho_i + 1)}{\chi_j \rho_{i-1}}}^{\infty} \int_0^{\infty} \left(\frac{m^2}{\sigma_{i-1,i}^2 \sigma_{L,i}^2} \right)^m \frac{(xy)^{m-1}}{(\Gamma(m))^2} e^{-m \left(\frac{x}{\sigma_{i-1,i}^2} + \frac{y}{\sigma_{L,i}^2} \right)} dx dy \right). \tag{A6}$$

For e.g., $m = 2$, the (A5) and (A6) are solved and expressed as (38) and (39), respectively. End of proof. □

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