Copyright is owned by the Author of the thesis. Permission is given for a copy to be downloaded by an individual for the purpose of research and private study only. The thesis may not be reproduced elsewhere without the permission of the Author.

# A SIMULATION OF SELECTED STATISTICAL PROCESS CONTROL METHODS

A thesis presented in partial fulfilment of the requirements for the degree of Master in Technology at Massey University

Siree Chanprasert

1989

#### ABSTRACT

A simulation program, SQC, was developed at the Production Technology Department, Massey University. The program was written in Vax Basic 3.0 which is structured programming language and is run on the Vax computer under the VAX/VMS operating system 4.5. SQC is a menu-driven program which was designed to simulate data from a variety production processes subject to inherent random variation and sample selection for predetermined changes; statistical quality purposes. Such decisions were made via the available feature to allow for user interactive control of the process parameters and sample selection methods while the chart of selected method was plotted on the terminal screen as well as optionally on the printer.

The exercise has been done to test and to observe how the program performed and produced the output on the screen and terminal-format files. Moreover, the program evaluation was carried out by comparing with a published article, which is satisfactorily acceptable.

The SQC can be utilized as a teaching tool for students in practising how each statistical process control method performs and how to make a right decision at a right time and as a research tool to observe and use the simulated results to predict and to improve the production process in the future.

#### ACKNOWLEDGEMENTS

I wish to express my heartfelt gratitude to Mr. G. E. Smith, my supervisor for his warm encouragement, understanding, constructive crititisms and patience in discussing my project.

My sincere thank is also extended to Mr. Bradley Bridges for his helpful suggestions concerning my study.

Finally, I would like to thank my parents for their love and encouragement and also my husband, Wanchai, for his companionship and moral support.

## TABLE OF CONTENTS

			page
		Abstract	1
		Acknowledgements	ii
		Table of Contents	iii
		List of Tables	iv
		List of Figures	V
		List of Appendices	vi
Chapter	1	Introduction	1
Chapter	2	Statistical Process Control	4
		2.1 Pre-control	5
		2.2 Shewhart Control Charts	8
		2.2.1 $\bar{X}$ -R Chart	9
		2.2.2 P Chart	10
		2.2.3 C Chart	11
		2.2.4 U Chart	12
		2.3 Cumulative Sum Chart	12
Chapter	3	Description of SQC Program	18
		3.1 Overview	18
		3.2 Program Specification	19
		3.3 Program Structure	21
		3.4 Data and File Descriptions	24
Chapter ·	4	Program Implementation	26
		How to Run the SQC Program	26
		Program Validation	45
		Exercise 1	46
		Exercise 2	55
Chapter	5	Conclusion and Suggestion for Further Study	62
References			67
Appendice	S		

## LIST OF TABLES

TABLE		page
4.1	Summary results of actual run lengths in	
	$\overline{X}$ chart of 5 different seeds runs compared	
	with theoretical average run length (ARLs)	49
4.2	Summary results of actual run length compared	
	between $\overline{\mathtt{X}}$ chart and CuSum chart applied to	
	$ar{\mathtt{X}}$ chart	50
4.3	Summary results of actual run lengths in	
	CuSum chart of 5 different seeds runs compared	
	with theoretical average run length (ARLs)	51
4.4	Summary results of actual run length compared	
	between P chart and CuSum chart applied to	
	P chart	52
4.5	Summary results of cumulatives percent	
	defectives produced from various sample sizes	54
4.6	Summary results of generated changes and	
	parameters reset in Bommer and Frazer (1976)'s	
	simulation	56
4.7	Comparison of the detected samples between	
	the Bommer and Frazer's and the SQC program	57
4.8	Comparison of the control limits from the	
	Bommer and Frazer's and the SOC program	58

## LIST OF FIGURES

FIGURE		page
2.1	The location of Pre-control limits	6
3.1	SQC model structure	20
4.1	Screen layout of Pre-control chart	29
4.2	Screen layout of $\overline{X}-R$ chart	30
4.3	Screen layout of P chart with fixed sample	
	size	31
4.4	Screen layout of P chart with variable sample	
	size	32
4.5	Screen layout of standardized P chart	33
4.6	Screen layout of CuSum applied to X chart	34
4.7	Screen layout of CuSum applied to P chart	35
4.8	Screen layout of CuSum applied to C chart	36
4.9	Screen layout of C chart	37
4.10	Screen layout of U chart	38
4.11	Screen layout of standardized U chart	39
4.12	The output of $\overline{X}$ -R chart plotted by SQC using	
	input process parameters from Bommer and	
	Frazer (1976)	59

#### LIST OF APPENDICES

## APPENDIX

- 1 SQC program maintenance
- 2 Diagram of SQC program structure
- 3 Data description
- 4 Table of common block files called by subprograms
- 5 Table of parameters required by each chart method
- 6 Map block for record buffer
- 7 List of program module
- 8 Examples of information reports
- 9 Random variates generation

#### CHAPTER 1

#### INTRODUCTION

Blum and Bingham (1979) said that computer simulation is the method used to determine 'what would happen if' in the system. definition, 'simulation is the process of designing a computerized model of a system (or process) and conducting experiments with this model for the purpose either of understanding the behaviour of the system or of evaluating various strategies for the operation of the system' (Shannon, 1975). It is an appropriate method of system study where an analytical approach is not practical. Nowadays, computer simulation is widely used in many applications, because computers provide the capability of testing the model repeatedly with a variety of different conditions suitable to the questions to be answered (Blum 1979). The results from the simulation enable and Bingham, researchers to understand the performance of the present system and predict the performance in the future under various conditions.

The use of simulation applied to industrial area has been increasing rapidly in recent years. It has became an effective tool in problem solving and decision making for management because it can help imitate the production operation by varying the physical conditions to see what would happen under many different management strategies (Rao and Smith, 1974). Cousins et al. (1975) also described how simulation can be applied in quality control with a case study in manufacturing. They concluded that simulation offers an excellent method for decision making without interfering with day-to-day operations.

There are many statistical quality control researches that have been done by using simulation approach both on quality control techniques and management as Hahn (1985) suggested that statistics can help improve the quality of manufactured product. The quality simulation can clarify the techniques used to achieve a given quality goal in

advance in various stages of product development (Osamu, 1983).

However, sometimes, statistics is hard to understand by supervisors or operators without being trained. Therefore, education and training are an essential part of quality improvement (Juran, 1979). Gupta et al. (1987) said that education and training of entire workforce become a top priority in statistical process control scheme.

Computer laboratory in quality control using simulation method can be a good tool in training with many benefits (Bommer and Frazer, 1976).

- o It provides decision making experience in constructing and applying decision rules to actual data.
- o The experience provides the trainee with opportunity to experiment with alternative decision strategies.
- o The process identifies faulty decision strategy allowing the trainee to analyze and benefit from errors.
- o The trainee's confidence in utilizing quality control concepts is reinforced when he succeeds in developing an effective decision strategy.

Furthermore, Juran (1979) added that although the preparation of the simulation program for training is costly because of requiring considerable time by skilled analysts and programmers, once it is prepared it permits a good deal of flexibility in training and helps minimize total costs since it does not disturb the actual operation. Also the program provides the capability of testing and demonstrating the trials repeatedly with various questioned conditions.

### The objectives of the study

- 1. To build a programming package that adequately simulates :-
  - data from a variety of production processes subject to inherent random variation and predetermined or random parameter changes.
  - sample selection for SQC purposes
- 2. To compare the performance of each control methods resulted from the simulation.
- 3. To utilize the package as a study tool both in research and laboratory practice for statistical quality control students.

Chapter 2 describes the statistical process control method only those provided in the established program and discussed the advantages and disvantages of each control method.

Chapter 3 explains the design and description of the program which is called  ${\tt SQC}$  while Appendix 2 and 3 provide the diagram of program structure input specifications.

Chapter 4 provides the guidelines of how to run SQC and also demonstrated some examples to help users understand the use of SQC with both arbitrary data and data taken from some previous researches. In addition, Appendix 1, and 4 to 8 provide some useful informations of program maintenance for those users who are interested in program modification and development (see DEC, 1986a, 1986b and 1986c for more detail informations).

Chapter 5 concludes with the results of the study and suggests some interesting ideas for further study and program development.