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A New Encrypted Data Switching Protocol: Bridging IBE and ABE without Loss of Data Confidentiality

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ABSTRACT Encryption technologies have become one of the most prevalent solutions to safeguard data confidentiality in may real-world applications, e.g., cloud-based data storage systems. Encryption outputting a relatively "static" format of encrypted data, however, may hinder further data operations, for example, encrypted data may need to be "transformed" into other formats for either computation or other purposes. In order to enable an encryption to be used in another device equipped with a different encryption mechanism, the concept of encryption switching is first proposed in CRYPTO 2016 for conversion particularly between Paillier and ElGamal encryptions. This paper considers the conversion between conventional identity-based and attribute-based encryptions and further proposes a concrete construction via the technique of proxy re-encryption. The construction is proved to be CPA secure in the standard model under q-decisional parallel bilinear Diffie-Hellman exponent assumption. The performance comparisons highlight that our bridging mechanism reduces computation and communication cost on client side, especially when the data of client is encrypted and outsourced to remote cloud. The computational costs w.r.t. re-encryption (on server side) and decryption (on client side) are acceptable in practice.

INDEX TERMS Data Security, Encryption Switching, Identity-Based Encryption, Attribute-Based Encryption, CPA Security, Standard Model

I. INTRODUCTION

An interesting and useful primitive of public key cryptography, which is called encryption switching protocol (ESP), has been introduced in CRYPTO 2016 by Couteau et al. [1]. The basic idea behind ESP is to build a "bridge" between an ElGamal-like ciphertext and a Paillier encryption [2] in such a way that the two different encryptions can transfer from one to the other. For instance, give an encryption of Paillier, ESP can be used to convert the ciphertext to ElGamal-like encryption under the same plaintext and furthermore, it cannot leak the underlying plaintext in encryption conversion phase. The initial motivation of the design of ESP is to bring convenience and scalability in the transformation between homomorphic computations ($+$ and $\times$), so that even a garbled circuit with only $+$ (resp. $\times$) gates is able to take ElGamal-like (resp. Paillier) encryption as input.

Inspired by the seminal notion, this paper explores the concept of ESP into more general context of public key encryption (PKE). As the advanced versions of PKE, identity-based encryption (IBE) [3] and attribute-based encryption (ABE) [4] have been introduced in the literature to enhance fine-grained data sharing by allowing data encryptor to encrypt data under the "fuzzy" information of data receiver. Furthermore, ABE also supports one-to-many data sharing

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mode in the sense that data owner only needs to generate an encryption intended for a group of users specified by some descriptions, so that the users can leverage respective decryption keys to reveal the underlying plaintext. Both of the cryptographic primitives can be implemented in many real-world applications, such as Voltage[1], Secure Zones [5] and Andraben [6].

Motivation. Suppose a local tax authority may send an email to contact a tax payer, say Alice, to ask for necessary documents (e.g. bank details, income) to see if Alice commits some frauds in tax report. If there is a sender address in the email, Alice may encrypt an audit log of personal online bank transactions under the address for the authority. Upon the arrival of the encrypted message, the gateway of the tax authority may recognize it in order to send the encryption to the most appropriate officials. To do so, the gateway has to decrypt the ciphertext and further re-encrypt it under, say the email address of Bob (who is the official at tax auditing department). If Alice cannot see the address of sender in the email (note this is quite common in practice, known as "No-Reply" email), she may encrypt the file under the descriptions of the authority, for example, ("Tax Authority" AND "London Area" AND ("Auditing Dept." OR "Others")), and further upload the encryption to the authority online. The gateway of the tax authority may do nothing but broadcast the encryption within the inside network. To shorten the response time of handling each auditing case, the gateway may reform the ciphertext intended for specified officials by decrypting the message and re-encrypting under the officials' email addresses. However, both of the above approaches leak sensitive personal information to the gateway.

We may also consider a scenario where a communication channel can only support a special type of encrypted message, say IBE, due to the control of communication bandwidth. However, an ABE ciphertext requests to go through the channel to reach another network domain. Without a secure ciphertext convertor, the gateway of the channel has to decrypt the message to fulfil the transformation of encryption. How to allow one to securely convert the ciphertexts without gaining access to the underlying plaintext that motivates this work.

The conversion between encryptions with different domains may bring convenience in data analysis and communication. For instance, in the context of big data aggregation, a data collector may receive various formats of data from many sources. It is challenging for the collector to aggregate the data if they are encrypted in different domains. A naive way of data aggregation here is first to request all the data sources to provide decryption keys and further to fulfil expensive decryption. But this method requires share of secret keys that yields potential data security breach to the data sources. How to allow one to securely share data without sharing secret key that also motivates our work.

[1]https://www.voltage.com/technology/data-encryption/identity-based-encryption/

Under the umbrella of EPS, this paper considers the conversion between IBE and ABE.

Difficulty. It is challenging to achieve our goal - designing an encryption switching scheme to bridge IBE and ABE via proxy re-encryption (PRE) technique. In the literature, only Mizuno and Doi [7] have proposed an $ABE \rightarrow IBE$ type PRE construction that is able to convert a ciphertext in the format of ABE to an IBE encryption. The scheme, however, cannot achieve the conversion for the other way round, i.e. converting an IBE ciphertext to an ABE encryption. Besides, [7] only supports AND gates on positive and negative attributes w.r.t. ABE encryption, which is with low expressiveness. The construction proposed in this paper will not be limited to the above issues. But the main difficulty depends on how to construct re-encryption key to (i) enable bilateral conversion and (ii) minimize the effect expressiveness (in terms of ABE). In order to construct a re-encryption key we usually need to input the secret/private key of a delegator (i.e. original data owner) and the public key information (or ID, attributes) of a delegatee (i.e. the data receiver after conversion). We here give the re-encryption key construction in [7] as an example whereby g^{α_1} and g^{at} are parts of the private key of delegator and meanwhile ID is the public identity of delegatee. However, the part $g^{\alpha_1} g^{at} (g^{ID} h)^w$ is the hindrance to prevent the conversion from IBE to ABE. To bypass this hindrance, in our construction, we design a re-encryption key from the private key of delegator and a partial private key of delegatee. The re-encryption key actually contains the delegator's private key and an IBE ciphertext. When being used to convert an ABE ciphertext to an IBE one, the re-encryption algorithm runs the ABE decryption and further outputs the decryption results which is an IBE ciphertext. In this case, we must guarantee that, given a re-encryption key, proxy cannot obtain any information of the underling plaintext, even if it colludes with the corresponding delegatee (who is without knowledge of the delegator's private key). To achieve the guarantee, we randomize the private keys of both delegator and delegatee. Besides, we require that the hard assumptions of the underlying ABE and IBE should be the same or at least, have an inclusive relationship.

Identity-Based Encryption. Identity-based cryptography is a general extension of public-key cryptography where the public key of a user can be any arbitrary string uniquely representing the identity of the user (e.g. name or email address). In 1984, Shamir first proposed the concept of IBE [3]. Till 2001, the first construction of IBE was constructed by Boneh and Franklin [8] by using Weil pairing. However, the security proof is based on the random oracle model. In 2004, Boneh and Boyen presented an IBE scheme with IND-ID-CPA security in the standard model [9], and later Waters [10] proposed a more efficient IBE scheme. Since its introduction, IBE has been explored to support various features, e.g., anonymous IBE [11], [12], hierarchical IBE [13], identity-based broadcast encryption [14] and revocable IBE [15].

Attribute-Based Encryption. ABE is an extension of IBE. It allows private key and ciphertext to be labeled with de-

scriptions, so that a decryption is valid if and only if the description of a decryption key matches that of a ciphertext. It has been widely employed in fine-grained data access control. There are two important variants of ABE, one is key-policy ABE (KP-ABE) [16] relating access control policy to decryption key, and the other is ciphertext-policy ABE (CP-ABE) [17], [18] associating ciphertext with access control policy. Since its introduction, ABE has been extended to support various features, e.g., large universe ABE [19], [20], traceable ABE [21], [22] and outsourced ABE [23], [24].

Proxy re-encryption. Blaze et al. [25] introduced the notion of PRE in the context of PKE. In a PRE system, a delegator, say Alice, can request a semi-trusted proxy to transform a ciphertext under her public key to another ciphertext under the public key of a delegatee, say Bob, without leaking the underlying information of the plaintext to the proxy. Some variants of traditional PRE have been proposed in the literature (e.g. [26]–[28]). In 2007, Green and Ateniese [29] explored PRE in the context of IBE and further introduced the notion of the identity-based PRE (IBPRE). To implement PRE in the attribute-based cryptographic setting, Liang et al. [30] defined CP-ABPRE, and proposed a concrete construction on top of [31]. Following the seminal work, ABPRE have been proposed to achieve better security and more expressiveness in data sharing [32].

However, all the aforementioned schemes cannot support encryption switching. A hybrid proxy PRE was first proposed by Matsuo [33] in 2007 to enable a PKE ciphertext to be converted to an IBE one. Later, Mizuno et al. [7] proposed a PRE conversion from ABE to IBE while maintaining the confidentiality of plaintext. Rencently, Couteau, Peters and Pointcheval [1] introduce an encryption switching between Paillier and ElGamal based on homomorphic encryption. We compare our construction with [1], [7], [9], [18], [33] in terms of functionality, security and feature in Table 1. We state that the details of efficiency analysis will be given in Section 5. We state that our scheme is the first of its type to achieve bidirectional conversion between ABE and IBE with CPA security in the standard model.

A. ORGANIZATION

The rest of this paper is organized as follows. In Section 2, we briefly review complexity assumption, definitions and security notion used in this paper. In Section 3 we present the construction. In Section 4, we give the security proof. In Section 5, we compare our work with other related works in terms of efficiency. In Section 6, we present the conclusion.

II. PRELIMINARIES

A. BILINEAR GROUPS AND COMPLEXITY ASSUMPTION

Two multiplicative cyclic groups $\mathbb{G}$ and $\mathbb{G}_T$ whose orders are prime p and a bilinear map $e : \mathbb{G} \times \mathbb{G} \to \mathbb{G}_T$ has following three properties:

- **Bilinearity:** $e(g^a, h^b) = e(g, h)^{ab}$ for all $g, h \in \mathbb{G}$ and $a, b \in \mathbb{Z}_p$.
- **Non-degeneracy:** There exist $g, h \in \mathbb{G}$ such that $e(g, h) \neq 1_{\mathbb{G}}$.
- **Computability:** There exists an efficient algorithm to compute $e(g, h)$ for all $g, h \in \mathbb{G}$.

Decisional Parallel Bilinear Diffie-Hellman Exponent Assumption [18]. Given a group $\mathbb{G}$ of prime order p, let $a, s, b_1, \cdots, b_q \in_R \mathbb{Z}_p$ and g be a generator of $\mathbb{G}$. If an algorithm is given $\overrightarrow{y} = g, g^s, g^a, \cdots, g^{a^q}, , g^{a^{q+2}}, \cdots, g^{a^{2q}}$

$$\forall 1 \leq j \leq q \quad g^{s \cdot b_j}, g^{a/b_j}, \cdots, g^{a^q/b_j}, , g^{a^{q+2}/b_j}, \cdots, g^{a^{2q}/b_j}$$

$$\forall 1 \leq j, k \leq q, k \neq j \quad g^{a \cdot s \cdot b_k/b_j}, \cdots, g^{a^q \cdot s \cdot b_k/b_j}$$

It is hard to distinguish $e(g, g)^{a^{q+1}s} \in \mathbb{G}_T$ from a random element in $\mathbb{G}_T$.

The advantage ε of an adversary $\mathcal{A}$ to solve decisional q-parallel BDHE if

$$|Pr[\mathcal{A}(\overrightarrow{y}, T = e(g, g)^{a^{q+1}s}) = 0] - Pr[\mathcal{A}(\overrightarrow{y}, T = R) = 0]| \geq \varepsilon$$

B. DEFINITION OF ATTRIBUTE-BASED ENCRYPTION

Definition 1. *An attribute-based encryption (ABE) usually consists of four algorithms.*

ABE.Setup(λ, U): intake a security parameter λ and description universe, output the public parameters PK and a master key MSK. We assume that PK is implicitly seen as input for the following algorithms.

ABE.KeyGen($MSK, \mathbb{A}$): intake the master key MSK and a description $\mathbb{A}$, output a private key SK.

ABE.Encrypt($\mathcal{M}, \mathbb{B}$): intake a message $\mathcal{M}$, and a description $\mathbb{B}$, output a ciphertext CT.

ABE.Decrypt(CT, SK): intake a ciphertext CT which contains a description $\mathbb{A}$, and a private key SK corresponding to another description $\mathbb{B}$. If $\mathbb{B}$ matches $\mathbb{A}$ the algorithm decrypts the ciphertext and returns a message $\mathcal{M}$; otherwise, return $\perp$.

While $\mathbb{A}$ is a set of attributes over U and $\mathbb{B}$ is an access policy, the definition is for KP-ABE; if the case is the other way round, that is for CP-ABE.

C. DEFINITION OF IDENTITY-BASED ENCRYPTION

Definition 2. *Following Definition 1, if we set $\mathbb{A} = \mathbb{B}$ as an identity of a system user, we have the definition for IBE.*

D. DEFINITION OF ENCRYPTION SWITCHING

We here define a general ciphertext conversion framework between ABE and IBE.

Definition 3. *Following Definition 1 and 2, we have the definition of encryption switching (ES):*

ES.Setup(λ, U): $(ABE.PK, ABE.MSK) \leftarrow$ ABE.Setup(λ, U) and $(IBE.PK, IBE.MSK) \leftarrow$ IBE.Setup(λ, U). Set $PK = (ABE.PK, IBE.PK)$ and $MSK = (ABE.MSK, IBE.MSK)$. We note that λ is the same security parameter and the $ABE.PK, IBE.PK$ could be held by two distinct trusted parties, respectively.

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TABLE 1. Comparison with Related Works

Scheme	Type	Complexity Assumption	Security	Standard Model
[9]	IBE	decisional bilinear Diffie-Hellman (DBDH)	CPA	√
[18]	ABE	decisional q-parallel BDHE	CPA	√
[33]	PKE→IBE	DBDH	CPA	√
[7]	ABE→IBE	DBDH	CPA	√
[1]	Paillier↔ElGammal	decisional composite residuosity, decisional Diffie-Hellman, quadratic residuosity assumptions	CPA	√ √
Ours	IBE↔ABE	decisional q-parallel BDHE	CPA	√

ES.KeyGen$(MSK, \mathbb{A})$: $SK_{\mathbb{A}} \leftarrow \delta.KeyGen(MSK, \mathbb{A})$, where $\delta \in \{ABE, IBE\}$ and $\mathbb{A} \in \{an\ attribute\ set, anaccess\ policy, an\ identity\}$.

ES.ReKeyGen$(\mathbb{A}, \mathbb{B}, SK_{\mathbb{A}}, SK_{\mathbb{B}})$: intake the descriptions $\mathbb{A}$, $\mathbb{B}$ and private keys $SK_{\mathbb{A}}$, $SK_{\mathbb{B}}$, output a re-encryption key $RK_{\mathbb{A}\to\mathbb{B}}$, where $\mathbb{A}$ and $\mathbb{B}$ are from distinct encryption mechanisms, e.g., $\mathbb{A} \in \{an\ attribute\ set,\ an\ access\ policy\}$ and $\mathbb{B}$ is an identity.

ES.Encrypt$(\mathcal{M}, \mathbb{A})$: $CT_{\mathbb{A}} \leftarrow \delta.Encryption(\mathcal{M}, \mathbb{A})$. We assume that ABE and IBE share the same message domain in the definition.

ES.ReEncrypt$(CT_{\mathbb{A}}, RK_{\mathbb{A}\to\mathbb{B}})$: intake a ciphertext $CT_{\mathbb{A}}$ under the description $\mathbb{A}$ and a re-encryption key $RK_{\mathbb{A}\to\mathbb{B}}$, output a re-encrypted ciphertext $CT_{\mathbb{B}}$.

ES.Decrypt(CT, SK): $\mathcal{M}/\perp \leftarrow \delta.Decrypt(CT, SK)$.

Note that we assume the above conversion definition between ABE and IBE should share the same message domain $\mathcal{M}$ (so that the conversion can be executed smoothly).

E. SECURITY MODEL OF ENCRYPTION SWITCHING ABE↔IBE IN GAME-BASED FRAMEWORK

The selectively chosen plaintext security against ABE→IBE type ES is defined as the following game between an attacker $\mathcal{A}$ and a challenger $\mathcal{C}$. The game describes the security of underlying ABE and IBE scheme even if $\mathcal{A}$ achieves re-encryption keys which can transform the ciphertext of ABE to the one of IBE.

Init. $\mathcal{A}$ chooses a target access structure $\mathbb{A}^*$ and a target IBE identity ID^*, and sends them to $\mathcal{C}$.

Setup. $\mathcal{C}$ runs $Setup_A(1^\kappa)$ and $Setup_I(1^\kappa)$, and returns ABE public parameters and IBE public parameters to the $\mathcal{A}$.

Phase 1. $\mathcal{A}$ is allowed to adaptively issue ABE private key queries, IBE private key queries and re-encryption key queries as follows:

- $Extract_A(S)$: $\mathcal{A}$ can adaptively and repeatedly request an ABE private key for a set S where $S \not\models \mathbb{A}^*$.
- $Extract_I(ID, params)$: $\mathcal{A}$ can adaptively and repeatedly issue an IBE private key corresponding to an identity ID of his choice.
- $Extract_{A\to I}(S, ID)$: $\mathcal{A}$ can adaptively and repeatedly request re-encryption key which can transform ABE ciphertexts encrypted for set S to IBE ciphertexts corresponding to an identity ID. (It is only with the security of [ABE-IBE] type proxy re-encryption scheme)

Challenge. $\mathcal{A}$ submits two equal length messages M_0 and M_1 and selects which scheme to attack (ABE or IBE). $\mathcal{C}$ randomly chooses $\beta \in \{0, 1\}$ and returns the encrypted result of M_β encrypted by the selected scheme.

Phase 2. Same as Phase 1.

Guess. $\mathcal{A}$ submits a guess $\beta' \in \{0, 1\}$. If $\beta' = \beta$, $\mathcal{A}$ wins.

During Phase 1 and 2, $\mathcal{A}$ is restricted the following queries:

- $Extract_A(S)$, where $S \models \mathbb{A}^*$.
- $Extract_I(ID^*)$.
- $Extract_{A\to I}(S^*, ID)$ and $Extract_I(ID, param)$ queries, where $S \models \mathbb{A}^*$ and ID is an arbitrary IBE user's identity.

Remark. The selectively chosen plaintext security against IBE→ABE type ES is similar to the above security game except the queries of re-encryption key $Extract_{I\to A}(ID, S)$ where the re-encryption key transforms IBE under an identity ID to ABE under a description S.

Definition 4. *We define $\mathcal{A}$'s advantage in the above game as $Adv_A(1^\kappa) = 2Pr[\beta' = \beta] - 1$. We state that an ABE→IBE (resp. IBE→ABE) type ES is indistinguishable under selectively chosen-plaintext attacks, if for any probabilistic polynomial time (*PPT*) adversary $\mathcal{A}$, the advantage in the security game is negligible.*

III. CONSTRUCTIONS

A. BUILDING BLOCKS REVIEW

Our ES between ABE and IBE is built on top of Waters-ABE scheme [18] and the first construction of BB-IBE [9]. We are going to review them as follows.

Waters-ABE Construction. Waters-ABE consists of the following four algorithms [18].

Setup(λ, U). Let U be the maximum number of system attributes. Let $\mathbb{G}, \mathbb{G}_T$ be a bilinear group of prime order p. Let $e : \mathbb{G} \times \mathbb{G} \to \mathbb{G}_T$. Then it chooses a generator g as well as random group elements $h_1, \cdots, h_U \in \mathbb{G}$ that are associated with the U attributes in the system. In addition, it chooses random exponents $\alpha_1, a \in \mathbb{Z}_p$. The public key is

$$PK_1 = g, e(g, g)^{\alpha_1}, g^a, h_1, \cdots, h_U.$$

The master private key is $MSK_1 = g^{\alpha_1}$.

Encrypt$(PK_1, \mathcal{M}, (M, \rho))$. It takes as input the public parameters PK_1, a message $\mathcal{M}$ as well as an LSSS access structure (M, ρ), where M be an $\ell \times n$ matrix and ρ associates rows of M to attributes. It first chooses a vector

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$\vec{v}$=$(s, y_2, \cdots, y_n) \in_R \mathbb{Z}_p^n$. These values will be used to share the encryption exponent s. For $i = 1$ to ℓ, it calculates $\lambda_i = \vec{v} \cdot M_i$, where M_i is the vector corresponding to the ith row of M. Then it chooses $r_1, \cdots, r_\ell \in_R \mathbb{Z}_p$ and computes the ciphertext as follows:

$$C = \mathcal{M} \cdot e(g,g)^{\alpha_1 s},$$

$$C' = g^s, \quad \{C_i = g^{a\lambda_i} h_{\rho(i)}^{-r_i}, \ D_i = g^{r_i}\}_{i \in \{1,\cdots,\ell\}}$$

The ciphertext is $CT_S = (C, C', \{C_i, D_i\}_{\rho(i) \in M})$ along with a description of (M, ρ).

KeyGen(MSK_1, S). It takes as input the master private key MSK_1 and a set S of attributes. It chooses $t \in_R \mathbb{Z}_p$ and creates the private key $SK_S = (K, L, \{K_x\}_{x \in S})$ as

$$K = g^{\alpha_1} g^{at}, \quad L = g^t, \quad \forall x \in S: \ K_x = h_x^t$$

Decrypt(CT, SK_S). It takes as input a ciphertext CT for a linear access structure (M, ρ) and a private key SK_S. Suppose that S satisfies the access structure and let $I \subset \{1, 2, \cdots, \ell\}$ be defined as $I = \{i : \rho(i) \in S\}$. Then, let $\{w_i \in \mathbb{Z}_p\}_{i \in I}$ be a set of constants such that if $\{\lambda_i\}$ are valid shares of any secret s according to M, then $\sum_{i \in I} w_i \lambda_i = s$. It computes

$$\mathcal{M} = \frac{C \cdot \prod_{i \in I} \left(e(C_i, L) e(D_i, K_{\rho(i)})\right)^{w_i}}{e(C', K)}$$

$$= \frac{\mathcal{M} \cdot e(g,g)^{\alpha_1 s} \cdot \prod_{i \in I} e(g,g)^{a\lambda_i w_i t}}{e(g,g)^{\alpha_1 s} e(g,g)^{ast}}$$

BB-IBE. We review BB-IBE [9] construction as follows.

Setup(λ). Let $\mathbb{G}, \mathbb{G}_T$ be a bilinear group of prime order p, and $e : \mathbb{G} \times \mathbb{G} \to G_T$ be the bilinear map. Given a security parameter λ as input, the algorithm selects a generator $g_0 \in_R \mathbb{G}$ and $h, g_2 \in_R \mathbb{G}$. It picks $\alpha_2 \in_R \mathbb{Z}_p$ and sets $g_1 = g_0^{\alpha_2}$. The public parameters are $PK_2 = (g_0, g_1, g_2, h)$ and the master private key is $MSK_2 = \alpha_2$.

Encrypt$(ID, PK_2, \mathcal{M})$. Given an identity ID, public parameter PK_2 and plaintext $\mathcal{M} \in \mathbb{G}_T$ as input, the algorithm selects $w \in_R \mathbb{Z}_p$ and outputs an IBE ciphertext CT_{ID}.

$$CT_{ID} = (C_1, C_2, C_3) = (g_0^w, (g_1^{ID} h)^w, \mathcal{M} e(g_1, g_2)^w)$$

KeyGen(MSK_2, PK_2, ID). Given master private key MSK_2, public parameters PK_2 and an identity ID as input, the algorithm picks $u \in_R \mathbb{Z}_p$ and outputs an IBE private key as

$$SK_{ID} = (SK_{ID}^1, SK_{ID}^2) = (g_2^{\alpha_2} (g_1^{ID} h)^u, g_0^u).$$

Decrypt(SK_{ID}, CT_{ID}). Given an IBE private key SK_{ID} and an IBE ciphertext CT_{ID} as input, the algorithm outputs a plaintext $\mathcal{M}$.

$$\mathcal{M} = \frac{C_3 \cdot e(SK_{ID}^2, C_2)}{e(SK_{ID}^1, C_1)}$$

B. CONSTRUCTION: ABE→IBE TYPE ES

Based on the above ABE and IBE schemes, we design an ES via PRE technique which converts the encryption of ABE to that of IBE scheme. We define that $ES.Setup$ =[Setup(λ, U), Setup(λ)], $ES.KeyGen$ = [KeyGen(MSK_1, S), KeyGen(MSK_2, PK_2, ID)], and $ES.Encrypt$ = [Encrypt$(PK_1, \mathcal{M}, (M, \rho))$, Encrypt$(ID, PK_2, \mathcal{M})$]. The main technique we introduce here is to build a plug-in to convert two types of encryption, so that we only focus on the algorithms related to the conversion, namely ES.ReKenGen, ES.ReEncrypt and ES.Decrypt. For the setup, key generation and encryption, one may use respective algorithm depending on which encryption domain he/she is currently in, for example, one may use the algorithm Encrypt$(ID, PK_2, \mathcal{M})$ to encrypt data if he/she is in the context of IBE.

ES.ReKenGen$_{A \to I}(PK_1, PK_2, S, ID, SK_S, SK_{ID}^2)$: Given the ABE and IBE public parameter PK_1 and PK_2, attribute set S and a delegator B's ABE private key SK_S, a delegatee A's IBE identity ID and its 2nd component of private key SK_{ID}^2 as input, the algorithm outputs a re-encryption key $RK_{A \to I} = (R_a, R_b, R_c, R_d, rk_1, \{rk_x\}_{x \in S})$ as follows:

- Client A chooses $u' \in_R \mathbb{Z}_p$ and computes $SK_{ID}^2{}' = SK_{ID}^2 \cdot g_0^{u'} = g_0^{u''}$, where $u + u' = u''$. Then client A returns $SK_{ID}^2{}'$ to client B and keeps secret u' which is needed in the decryption algorithm.
- Client B selects $t' \in_R \mathbb{Z}_p$ and sets

$$R_a = K \cdot g^{at'} \cdot SK_{ID}^2{}' = g^{\alpha_1} g^{at''} g_0^{u''}.$$

Client B selects $\tau \in_R \mathbb{Z}_p$ and sets

$$R_b = g_0^\tau, \ \ R_c = (g_1^{ID} h)^\tau, \ \ R_d = e(g_1, g_2)^\tau.$$

Client B computes $rk_1 = L \cdot g^{t'} = g^{t''}$.
For each attribute $x \in S$: $rk_x = K_x \cdot h_x^{t'} = h_x^{t''}$, where $t + t' = t''$.

ES.ReEncrypt$_{A \to I}(RK_{A \to I}, CT_S)$: Given attribute set S, identity ID, a re-encryption key $RK_{A \to I}$ and an ABE ciphertext $CT_S = (C, C', \{C_i, D_i\}_{\rho(i) \in M})$ along with a description of (M,ρ) as input, output an IBE ciphertext $CT_{ID} = (\overline{C_1}, \overline{C_2}, \overline{C_3})$ as follows:
Suppose S satisfies the access structure (M, ρ) and let $I \subset \{1, 2, \cdots, \ell\}$ be defined as $I = \{i : \rho(i) \in S\}$. Then, let $\{w_i \in \mathbb{Z}_p\}_{i \in I}$ be a set of constants such that if $\{\lambda_i\}$ are valid shares of any secret s according to M, then $\sum_{i \in I} w_i \lambda_i = s$.
Compute $C_i' = e(C_i, rk_1) e(rk_i, D_i) = e(g,g)^{a\lambda_i t''}$.
Select $y \in_R \mathbb{Z}_p$ and compute:

$$\overline{C_1} = R_b^y = g_0^{\tau y}$$

$$\overline{C_2} = R_c^y \cdot C' = (g_1^{ID} h)^{\tau y} \cdot g^s$$

$$\overline{C_3} = \frac{C \cdot R_d^y \cdot \prod_{i \in I} C_i'^{w_i}}{e(C', R_a)} = \mathcal{M} \cdot \frac{e(g_1, g_2)^{\tau y}}{e(g^s, g_0^{u''})}$$

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ES.Decrypt(PK_2, CT_{ID}, SK_{ID}): Given IBE public parameters PK_2, ciphertext CT_{ID} and private key SK_{ID} of identity ID, client A uses u' and computes

$$\mathcal{M} = \frac{\overline{C_3} \cdot e(SK_{ID}^2 \cdot g_0^{u'}, \overline{C_2})}{e\left(SK_{ID}^1 \cdot (g_1^{ID}h)^{u'}, \overline{C_1}\right)}$$
$$= \frac{\mathcal{M} \cdot e(g_1, g_2)^{\tau y} e(g_0^{u''}, (g_1^{ID}h)^{\tau y} \cdot g^s)}{e(g^s, g_0^{u''}) e\left(g_2^{\alpha}(g_1^{ID}h)^{u}(g_1^{ID}h)^{u'}, g_0^{\tau y}\right)}$$

C. IBE→ABE TYPE ES

We further design IBE→ABE Type ES which converts ciphertexts of IBE to ABE format as follows. Similarly, we focus on the algorithms supporting ciphertext conversion.

ES.ReKenGen$_{I\to A}$($PK_1, PK_2, S, ID, SK_{ID}, SK_S$): Given ABE and IBE public parameter PK_1 and PK_2, attribute set S and a delegator B's ABE private key SK_S, a delegatee's IBE identity ID and an IBE user A's private key SK_{ID} as input, output a re-encryption key $RK_{I\to A} = (R_a, R_b, \{R_{ci}\}_{\rho(i)\in M'}, R_d, rk_1, rk_2)$ as follows:

- Client B chooses $t' \in_R \mathbb{Z}_p$ and computes $K' = K \cdot g^{at'} = g^{\alpha_1} g^{at''}$, where $t + t' = t''$. Client B sends K' to client A and keeps secret t' which is needed in the decryption algorithm.
- Client A selects $u' \in_R \mathbb{Z}_p$ and sets

  $$R_a = SK_{ID}^1 \cdot (g_1^{ID}h)^{u'} \cdot K' = g_2^{\alpha_2}(g_1^{ID}h)^{u''} g^{\alpha_1} g^{at''}$$

  Client A selects $\tau \in_R \mathbb{Z}_p$ and sets $R_b = g^{\tau}$.
  Let M' be an $\ell \times n$ matrix. The algorithm chooses a random vector $\vec{v'} = (\tau, y_2', \cdots, y_n') \in \mathbb{Z}_p^n$, which will be used to share the encryption exponent τ.
  For $i = 1$ to ℓ, it calculates $\lambda_i' = \vec{v'} \cdot M_i'$, where M_i' is the vector corresponding to the ith row of M'. In addition, it chooses random $r_i' \in \mathbb{Z}_p$ and computes

  $$R_{ci} = \{C_i = g^{a\lambda_i'} h_{\rho(i)}^{-r_i'}, \quad D_i = g^{r_i'}\}, \quad R_d = e(g,g)^{\alpha_1 \tau}$$

  Client A chooses $\delta \in \mathbb{Z}_p$ and computes

  $$rk_1 = sk_{ID}^2 \cdot g_0^{u'} \cdot g_0^{\delta} = g_0^{u''+\delta}, \qquad rk_2 = (g_1^{ID}h)^{\delta}$$

ES.ReEncrypt$_{I\to A}$($RK_{I\to A}, CT_{ID}$): Given a re-encryption key $RK_{I\to A} = (R_a, R_b, \{R_{ci}\}_{\rho(i)\in M'}, R_d, rk_1, rk_2\})$ and an IBE ciphertext $CT_{ID} = (C_1, C_2, C_3)$ as input, output an ABE ciphertext $CT_S = (\{\overline{C_{1i}}\}_{\rho(i)\in M'}, \overline{C_2}, \overline{C_3}, \overline{C_4})$ as follows:

$$\overline{C} = \frac{e(C_2, rk_1)}{e(C_1, rk_2)}$$
$$= \frac{e\left((g_1^{ID}h)^w, g_0^{u''+\delta}\right)}{e\left(g_0^w, (g_1^{ID}h)^{\delta}\right)} = e\left((g_1^{ID}h)^w, g_0^{u''}\right)$$

Chooses $y \in \mathbb{Z}_p$, for $\rho(i) \in M_i'$, compute

$$\overline{C_{1i}} = R_{ci}^y$$
$$= \{\overline{C_i} = C_i{}^y = (g^{a\lambda_i'} h_{\rho(i)}^{-r_i'})^y, \overline{D_i} = D_i^y = (g^{r_i'})^y\}$$
$$\overline{C_2} = R_b^y \cdot C_1 = g^{\tau y} \cdot g_0^w$$
$$\overline{C_3} = R_d^y = e(g,g)^{\alpha_1 \tau y}$$
$$\overline{C_4} = \frac{C_3 \cdot \overline{C}}{e(R_a, C_1)} = \frac{\mathcal{M} \cdot e(g_1, g_2)^w \cdot e\left((g_1^{ID}h)^w, g_0^{u''}\right)}{e\left(g_2^{\alpha_2}(g_1^{ID}h)^{u''} \cdot g^{\alpha_1} g^{at''}, g_0^w\right)}$$
$$= \frac{\mathcal{M}}{e(g^{\alpha_1} g^{at''}, g_0^w)}$$

ES.Decrypt(CT_S, SK_S): Given ciphertext CT_S and private key SK_S, let $I \subset \{1, 2, \cdots, \ell\}$ be defined as $I = \{i : \rho(i) \in S\}$. Then, let $\{w_i \in \mathbb{Z}_p\}_{i\in I}$ be a set of constants such that if $\{\lambda_i'\}$ are valid shares of any secret τ according to M, then $\sum_{i\in I} w_i \lambda_i' = \tau$.

The decryption algorithm uses t' and computes

$$\mathcal{M} = \frac{\overline{C_4} \cdot e\left(\overline{C_2}, K \cdot g^{at'}\right)}{\prod_{i\in I}\left(e(\overline{C_i}, L \cdot g^{t'}) \cdot e(\overline{D_i}, K_{\rho(i)} \cdot h_{\rho(i)}^{t'})\right)^{w_i} \cdot \overline{C_3}}$$
$$= \frac{\mathcal{M} \cdot e\left(g^{\tau y} g_0^w, g^{\alpha_1} g^{at''}\right)}{e(g^{\alpha_1} g^{at''}, g_0^w) \cdot \left(\prod_{i\in I} e(g,g)^{t'' a y \lambda_i' w_i}\right) \cdot e(g,g)^{\alpha_1 \tau y}}$$

IV. SECURITY ANALYSIS

We first prove that our ABE→IBE type ES is indistinguishable under selectively chosen-plaintext attacks (IND-sCPA), if the decisional q-parallel BDHE assumption holds.

Theorem 1. *Suppose the decisional q-parallel BDHE assumption holds, our ABE→IBE type ES is IND-sCPA secure with a challenge matrix of size $\ell^* \times n^*$, where $\ell^*, n^* \leq q$.*

Proof: Suppose we have an adversary $\mathcal{A}$ with non-negligible advantage against the ABE→IBE type ES. We construct an algorithm $\mathcal{B}$ which can solve the decisional q-parallel BDHE problem by using $\mathcal{A}$.

Init. $\mathcal{A}$ chooses a target access structure $\mathbb{A}^*$ and a target identity ID^*, and sends them to $\mathcal{B}$.

Setup. $\mathcal{B}$ Setup simulation as follows:

ABE Setup. $\mathcal{B}$ chooses $\alpha' \in_R \mathbb{Z}_p$ and implicitly sets $\alpha = \alpha' + a^{q+1}$ by letting

$$e(g,g)^{\alpha_1} = e(g^a, g^{a^q}) e(g,g)^{\alpha'}.$$

For each attribute $x \in U$, $\mathcal{B}$ chooses a values $z_x \in_R \mathbb{Z}_p$. Let X denote the set of indices i, such that $\rho^*(i) = x$, $\mathcal{B}$ sets

$$h_x = g^{z_x} \prod_{i\in X} g^{aM_{i,1}^*/b_i} \cdot g^{a^2 M_{i,2}^*/b_i} \cdots g^{a^{n^*} M_{i,n^*}^*/b_i}.$$

Note that if $X = \Phi$ then sets $h_x = g^{z_x}$. $\mathcal{B}$ sends the public parameters $g, e(g,g)^{\alpha_1}, g^a, \{h_x\}_{\rho^*(i)\in U}$ to $\mathcal{A}$.

IBE-Setup. $\mathcal{B}$ chooses $z_1, z_2, z_3 \in_R \mathbb{Z}_p^*$ and sets $g_0 = g$, $g_1 = g^{az_1}, g_2 = g^{a^q z_2}, h = g_1^{-ID^*} g^{z_3}$. $\mathcal{B}$ sets the master private key $MSK = az_1$. $\mathcal{B}$ sends the public parameters g_0, g_1, g_2, h to $\mathcal{A}$.

Phase 1. $\mathcal{A}$ adaptively interacts with $\mathcal{B}$ as follows:

- $Extract_A(S)$. $\mathcal{A}$ queries the ABE private key SK_S with a set S, where $S \not\models \mathbb{A}^*$.

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$\mathcal{B}$ first finds a vector $\overrightarrow{w} = (w_1, \cdots, w_{n^*}) \in \mathbb{Z}_p$ such that $w_1 = -1$ and for all i where $\rho^*(i) \in S$ we have that $\overrightarrow{w} \cdot M_i^* = 0$. Then $\mathcal{B}$ chooses $r \in_R \mathbb{Z}_p$.
$\mathcal{B}$ defines $t = r + w_1 a^q + w_2 a^{q-1} + \cdots + w_{n^*} a^{q-n^*+1}$. It lets

$$L = g^r \prod_{i=1,\cdots,n^*} \left(g^{a^{q+1-i}}\right)^{w_i} = g^t.$$

$\mathcal{B}$ computes $K = g^{\alpha'} g^{ar} \prod_{i=2,\cdots,n^*} \left(g^{a^{q+2-i}}\right)^{w_i}$. For $x \in S$ and there is no i such that $\rho^*(i) = x$, $\mathcal{B}$ defines $K_x = L^{z_x}$.
For $x \in S$ and let X be the set of all i such that $\rho^*(i) = x$, $\mathcal{B}$ defines

$$K_x = L^{z_x} \prod_{i \in X} \prod_{j=(1,n^*)} \left(g^{\frac{a^j \cdot r}{b_i}} \prod_{\substack{k=(1,n^*) \\ k \neq j}} \left(g^{a^{q+1+j-k/b_i}}\right)^{w_k} \right)^{M^*_{i,j}}$$

$\mathcal{B}$ returns SK_S to $\mathcal{A}$ and records the tuple (S, SK_S) in an ABE private key List (ASKL).

- $Extract_I(ID)$. $\mathcal{A}$ queries the IBE user's private key SK_{ID} with an identity ID.
  - If $ID = ID^*$, $\mathcal{B}$ rejects.
  - If $ID \neq ID^*$, $\mathcal{B}$ checks the list of $REKL$, and if there exits the re-encryption key to ID and $S \models W$, $\mathcal{B}$ rejects. Otherwise, $\mathcal{B}$ chooses $u \in_R \mathbb{Z}_p$ and computes

$$SK^1_{ID} = g^{\frac{-a^q z_2 z_3}{(ID-ID^*)}} \left(g^{az_1(ID-ID^*)} g^{z_3}\right)^u,$$

$$SK^2_{ID} = g^{\frac{-a^q z_2}{(ID-ID^*)}} g^u$$

  $\mathcal{B}$ returns $SK_{ID} = (SK^1_{ID}, SK^2_{ID})$ to $\mathcal{A}$ and records the tuple (ID, SK_{ID}) in an IBE private key list (ISKL).
- $Extract_{A \to I}(S, ID)$. $\mathcal{A}$ queries the re-encryption key from attribute set S to identity ID as follows:
  If $S \not\models M^*$: $\mathcal{B}$ runs $Extract_A(S)$ and obtains an ABE private key $SK_S = (K, L, \{K_x\}_{x \in S})$.
  - When $ID \neq ID^*$, $\mathcal{B}$ sets the re-encryption key $RK_{I \to A} = (R_a, R_b, \{R_{ci}\}_{\rho(i) \in M'}, R_d, rk_1, rk_2\})$ as follows:
    Select $t', u' \in_R \mathbb{Z}_p$ and set

$$R_a = K \cdot g^{at'} \cdot SK^2_{ID} \cdot g^{u'} = K \cdot g^{at'} g^{\frac{-a^q z_2}{(ID-ID^*)}} \cdot g^{u'}.$$

    Select $\tau \in_R \mathbb{Z}_p$ and set

$$R_b = g^\tau,$$

$$R_c = (g^{az_1(ID-ID^*)} g^{z_3})^\tau,$$

$$R_d = e(g^a, g^{a^q})^\tau.$$

    Compute $rk_1 = L \cdot g^{t'}$ and for each $x \in S$,

$$rk_x = K_x \cdot h_x^{t'}.$$

  - When $ID = ID^*$, $\mathcal{B}$ chooses $t', u'' \in_R \mathbb{Z}_p$ and computes

$$R_a = K \cdot g^{at'} \cdot g^{u''} = K \cdot g^{at'} \cdot g^{u''}.$$

    Select $\tau \in_R \mathbb{Z}_p$ and set

$$R_b = g^\tau, \quad R_c = g^{z_3 \tau}, \quad R_d = e(g^a, g^{a^q})^\tau.$$

    Compute $rk_1 = L \cdot g^{t'}$ and for each $x \in S$,

$$rk_x = K_x \cdot h_x^{t'}.$$

Otherwise $S \models M^*$: If $\mathcal{B}$ already answers IBE private key for ID, $\mathcal{B}$ rejects. Otherwise, does as follows:

- When $ID \neq ID^*$, $\mathcal{B}$ chooses $t'', u \in \mathbb{Z}_p$ and computes

$$R_a = g^{\alpha'} g^{at} g^{\frac{-a^q z_2}{(ID-ID^*)}} g^u.$$

  Select $\tau \in_R \mathbb{Z}_p$ and set

$$R_b = g^\tau,$$

$$R_c = \left(g^{az_1(ID-ID^*)} g^{z_3}\right)^\tau,$$

$$R_d = e\left(g^a, g^{a^q}\right)^\tau.$$

  Compute $rk_1 = g^{t''}$, $\{rk_x = h_x^{t''}\}_{x \in S}$.
  Remark.

$$\begin{aligned} R_a &= g^{\alpha'} g^{at''} g^{\frac{-a^q z_2}{(ID-ID^*)}} g^u \\ &= g^{\alpha' + a^{q+1}} g^{at''} g^{\frac{-a^q z_2}{(ID-ID^*)}} g^{u - a^{q+1}} \\ &= g^\alpha g^{at} g^{at'} g^{\frac{-a^q z_2}{(ID-ID^*)}} g^{u_1} g^{u'} \\ &= K \cdot g^{at'} \cdot SK^2_{ID} \cdot g^{u'} \end{aligned}$$

  where $t + t' = t''$, $u = \frac{-a^q z_2}{(ID-ID^*)} + u_1$, $u_1 + u' = u - a^{q+1}$.
- When $ID = ID^*$, $\mathcal{B}$ chooses $t, u \in \mathbb{Z}_p$ and computes $R_a = g^{\alpha'} g^{at} g^u$.
  Select $\tau \in_R \mathbb{Z}_p$ and set

$$R_b = (g^{z_3})^\tau, \quad R_c = g^\tau, \quad R_d = e(g^a, g^{a^q})^\tau.$$

  Compute $rk_1 = g^t$ and for each $x \in S$, $rk_x = h_x^t$.
  $\mathcal{B}$ returns $RK_{A \to I}$ to $\mathcal{A}$ and records the tuple $(S, ID, RK_{A \to I})$ in re-encryption key list (REKL).

Challenge. $\mathcal{A}$ submits two equal length plaintexts $\mathcal{M}_0, \mathcal{M}_1 \in \mathbb{G}_T$ and chooses which scheme to attack. $\mathcal{B}$ flips a coins β.
If $\mathcal{A}$ selects ABE scheme to attack, $\mathcal{B}$ builds the challenge ciphertext $CT^*_A = (C^*, C'^*, \{C^*_x, D^*_x\}_{\rho(x)^* \in M^*})$

$$C^* = \mathcal{M}_\beta \cdot T \cdot e(g^s, g^{\alpha'}), \qquad C' = g^s$$

$\mathcal{B}$ chooses $y'_2, \cdots, y'_{n^*}$ and the share the secret using the vector

$$\overrightarrow{v} = (s, sa + y'_2, sa^2 + y'_3, \cdots, sa^{n-1} + y'_{n^*}) \in \mathbb{Z}_p^{n^*}$$

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$\mathcal{B}$ chooses $r'_1, \cdots, r'_\ell \in \mathbb{Z}_p$. For $i = 1, \cdots, n^*$, let R_i as the set of all $k \neq i$ such that $\rho^*(i) = \rho^*(k)$ meaning the same attributes as row i.
$\mathcal{B}$ computes

$$D_i = g^{-r'_i} g^{-sb_i}$$

$$C_i = h_{\rho^*(i)}^{r'_i} \left(\prod_{j=2,\cdots,n^*} (g^a)^{M^*_{i,j} y'_j} \right) (g^{b_i \cdot s})^{-z_{\rho^*(i)}}$$

$$\cdot \left(\prod_{k \in R_i} \prod_{j=1,\cdots,n^*} (g^{a^j \cdot s \cdot (b_i/b_k)})^{M^*_{k,j}} \right)$$

If $\mathcal{A}$ selects IBE scheme to attack, $\mathcal{B}$ outputs an IBE challenge ciphertext $CT^* = (C_1^*, C_2^*, C_3^*)$ corresponding to a target identity ID^* as follows:

$$C_1^* = M_\beta \cdot T, \qquad C_2^* = g^s, \qquad C_3^* = g^{sz_3}$$

Phase 2. Same as in Phase 1.
Guess. $\mathcal{A}$ outputs a guess $\beta' \in \{0, 1\}$. If $\beta' = \beta$ then $\mathcal{B}$ outputs 1 meaning $T = e(g, g)^{a^{q+1} s}$; otherwise, it outputs 0 to indicate T is a random group element in $\mathbb{G}_T$.

Theorem 2. *Suppose the decisional q-parallel BDHE assumption holds, the IBE→ABE type ES is IND-sCPA secure with a challenge matrix of size $\ell^* \times n^*$, where $\ell^*, n^* \leq q$.*

Proof: The security of IBE→ABE type ES is similar to that of ABE→IBE type ES except the re-encryption key queries $Extract_{I \to A}(ID, S)$. Therefore, we just present the re-encryption key queries as follows.
$Extract_{I \to A}(S, ID)$ $\mathcal{A}$ queries the re-encryption key from identity ID to attribute set S as follows:
If $ID \neq ID^*$: $\mathcal{B}$ runs $Extract_I(ID)$ and obtains an IBE private key $SK_{ID} = (SK_{ID}^1, SK_{ID}^2)$.

- $S \not\models M^*$: $\mathcal{B}$ runs $Extract_A(S)$ and obtains an ABE private key SK_S=$(K, L, \{K_x\}_{x \in S})$. $\mathcal{B}$ uses SK_{ID} and SK_S to generate $RK_{I \to A}$=$(R_a$,R_b, $\{R_{ci}\}_{\rho(i) \in M'}$, $R_d, rk_1, rk_2\})$.
- $S \models M^*$: $\mathcal{B}$ chooses $t, t'', u' \in_R \mathbb{Z}_p$ and computes

$$R_a = SK_{ID}^1 \cdot (g^{az_1(ID - ID^*)} g^{z_3})^{u'} \cdot g^{\alpha'} g^{at} g^{at''}$$

Remark.

$$\begin{aligned} R_a &= SK_{ID}^1 \cdot (g^{az_1(ID-ID^*)} g^{z_3})^{u'} \cdot g^{\alpha'} g^{at} g^{at''} \\ &= SK_{ID}^1 \cdot (g^{az_1(ID-ID^*)} g^{z_3})^{u'} \cdot g^{\alpha' + a^{q+1}} g^{at} g^{a(t''-a^q)} \\ &= SK_{ID}^1 \cdot (g^{az_1(ID-ID^*)} g^{z_3})^{u'} \cdot g^{\alpha_1} g^{at} g^{a(t''-a^q)} \\ &= SK_{ID}^1 \cdot (g_1^{ID} h)^{u'} \cdot K \cdot g^{at'} \end{aligned}$$

$\mathcal{B}$ selects $\tau \in_R \mathbb{Z}_p$ and sets $R_b = g^\tau$.
Let M^* be an $\ell \times n$ matrix. The algorithm first chooses a random vector $\vec{v^*} = (\tau, y_2^*, \cdots, y_n^*) \in \mathbb{Z}_p^n$. These values will be used to share the encryption exponent τ.

For $i = 1$ to ℓ, it calculates $\lambda_i^* = \vec{v^*} \cdot M_i^*$, where M_i^* is the vector corresponding to the ith row of M^*. In addition, the algorithm chooses random $r_i^* \in \mathbb{Z}_p$ and computes

$$R_{ci} = \{C_i = g^{a\lambda_i^*} h_{\rho(i)}^{-r_i^*}, \quad D_i = g^{r_i^*}$$

$$R_d = \left(e(g^a, g^{a^q}) \cdot e(g, g)^{\alpha'} \right)^\tau$$

$\mathcal{B}$ chooses $\delta \in_R \mathbb{Z}_p$ and computes $rk_1 = sk_{ID}^2 \cdot g^{u'} \cdot g^\delta$, $rk_2 = (g^{az_1(ID-ID^*)} g^{z_3})^\delta$. $\mathcal{B}$ returns $RK_{I \to A}$ to $\mathcal{A}$.
If $ID = ID^*$:

- $S \not\models M^*$: If $\mathcal{B}$ already answers ABE private key for S, $\mathcal{B}$ rejects. Otherwise, does as follows:
  $\mathcal{B}$ runs $Extract_A(S)$ to generate K, then it chooses $t'', u'' \in \mathbb{Z}_p$ and computes $R_a = g^{z_3(u'')} \cdot K \cdot g^{at''}$.
  Remark.

$$\begin{aligned} R_a &= g^{z_3 u''} \cdot K \cdot g^{at''} \\ &= g^{a^{q+1} z_1 z_2} g^{z_3(u+u')} \cdot K \cdot g^{a(t''-a^q z_1 z_2)} \\ &= g_2^{\alpha_2} (g_1^{ID^*} g_1^{-ID^*} g^{z_3})^{(u+u')} \cdot K \cdot g^{at'} \\ &= g_2^{\alpha_2} (g_1^{ID^*} h)^u (g_1^{ID^*} h)^{u'} \cdot K \cdot g^{at'} \end{aligned}$$

  where $t' = t'' - a^q z_1 z_2$.
  $\mathcal{B}$ generates $\{R_{ci}\}_{\rho(i) \in M^*}$ and R_d as the case when $S \models M^*$ and $ID \neq ID^*$. $\mathcal{B}$ chooses $\delta \in \mathbb{Z}_p$ and computes $rk_1 = g^{u''+\delta}, rk_2 = g^{z_3 \delta}$. $\mathcal{B}$ returns $RK_{I \to A}$ to $\mathcal{A}$.
- $S \models M^*$: $\mathcal{B}$ chooses $t'', u'' \in \mathbb{Z}_p$ and computes $R_a = g^{z_3(u'')} \cdot g^{\alpha'} g^{at} \cdot g^{at''}$.
  Remark.

$$\begin{aligned} R_a &= g^{z_3 u''} \cdot g^{\alpha'} g^{at} \cdot g^{at''} \\ &= g^{a^{q+1} z_1 z_2} g^{z_3(u+u')} \cdot g^{\alpha' + a^{q+1}} g^{at} \cdot g^{a(t''-a^q z_1 z_2 - a^q)} \\ &= g_2^{\alpha_2} (g_1^{ID^*} g_1^{-ID^*} g^{z_3})^{(u+u')} \cdot K \cdot g^{at'} \\ &= g_2^{\alpha_2} (g_1^{ID^*} h)^u (g_1^{ID^*} h)^{u'} \cdot K \cdot g^{at'} \end{aligned}$$

  where $t' = t'' - a^q z_1 z_2 - a^q$.
  $\mathcal{B}$ generates $\{R_{ci}\}_{\rho(i) \in M^*}$ and R_d as the case when $S \models M^*$ and $ID \neq ID^*$. $\mathcal{B}$ chooses $\delta \in \mathbb{Z}_p$ and computes $rk_1 = g^{u''+\delta}$, $rk_2 = g^{z_3 \delta}$. $\mathcal{B}$ returns $RK_{I \to A}$ to $\mathcal{A}$.

V. EFFICIENCY ANALYSIS

A. THEORETICAL ANALYSIS

In this subsection, we present the theoretical analysis of our construction in terms of computation, communication and storage complexity. In the analysis, we consider the following operations: E_p denotes the computation in bilinear pairings, E_e denotes the exponentiation computation, $|G_T|$ is the size of group $\mathbb{G}_T$, $|G_1|$ is the size of group $\mathbb{G}$, and s is the number of user's attributes, respectively.

Table 2 presents the comparison of efficiency between two approaches, one is the naive decrypt-and-Re-Encrypt method, and the other is our ABE→IBE type ES. The naive solution is the one that a client first downloads the encrypted data in the format of ABE from cloud server, decrypts the

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TABLE 2. Comparison between Naive Decrypt-and-Re-Encrypt with our ABE→IBE Type ES

	Naive Decrypt-and-Re-Encrypt	ABE→IBE Type ES
Computation	ABE.Dec+IBE.Enc: $(2+2s)E_p + 6E_e$	ES.ReKey (client side): $E_p + (3+s)E_e$ ES.ReEnc (cloud side): $2sE_p + 3E_e$
Communication	(ABE.CT+IBE.CT).Size $2\|G_T\| + (3+2s)\|G_1\|$	(ES.ReKey).Size (from client to cloud) $\|G_T\| + (4+s)\|G_1\|$
Storage	ABE.CT+IBE.CT $2\|G_T\| + (3+2s)\|G_1\|$	ES.ReEnc.CT: $\|G_T\| + 2\|G_1\|$

TABLE 3. Comparison between Naive Decrypt-and-Re-Encrypt with our IBE→ABE Type ES

	Naive Decrypt-and-Re-Encrypt	IBE→ABE Type ES
Computation	IBE.Dec+ABE.Enc: $3E_p + (3s+1)E_e$	ES.ReKey (client side): $E_p + (5+3s)E_e$ ES.ReEnc (cloud side): $3E_p + 3E_e$
Communication	(ABE.CT+IBE.CT).Size: $2\|G_T\| + (3+2s)\|G_1\|$	(ES.ReKey).Size (from client to cloud) $\|G_T\| + (4+2s)\|G_1\|$
Storage	IBE.CT+ABE.CT: $2\|G_T\| + (3+2s)\|G_1\|$	ES.ReEnc.CT: $2\|G_T\| + (2+s)\|G_1\|$

data using ABE secret key, further re-encrypts the data under IBE format, and eventually uploads the resulting encryption to cloud. In the computational complexity, it can be seen from the table that the naive solution requires client to consume linear cost in pairings, while ABE→IBE type ES only costs an E_p on client side (note the linear complexity is off-loaded to cloud). Although the communication complexity of the two approaches is nearly identical, the storage cost incurred by ABE→IBE type ES gets rid of linear requirement in $|G_1|$. Therefore, we can state that the new primitive designed in this paper outperforms the naive solution. We state that the complexity is reduced in our ES that makes sense because the ES converts a complex encryption, ABE, into a much simpler one, IBE. For the conversion from IBE to ABE, however, it may be another case. From Table 3, we can see that the complexity of the two solutions is quite close; a few pairings are reduced in our IBE→ABE Type ES in the communication and computation costs. Therefore, we may state that the performance of our solution is still a bit better than that of the naive solution w.r.t. the conversion from IBE to ABE.

B. EXPERIMENTAL ANALYSIS

We make use of bilinear pairings $e : G_1 \times G_1 \rightarrow G_2$ to achieve the security level of 80 bits. To simulate the worst case, we generate ciphertext policies in the form of (S_1 and S_2 ... and S_l) increasing from 10 to 100, where S_i is an attribute. We repeat each instance 20 times and eventually take the average. The time at figures is given in the unit of milliseconds. In the simulation, we use the famous and widely studied cryptographic library MIRACL[2]. We run the simulation on an Intel I7-4770 processor with 3.40 GHz clock frequency and 4 GB RAM running Windows 7 operating system.

[2]https://libraries.docs.miracl.com/miracl-user-manual/installation.

The simulation results (w.r.t. the time spent in computation) are shown in Fig 1(a), 1(b) and 1(c). In the figures, we let "ABE-IBE" denote the ABE→IBE Type ES (in Section III-B), "IBE-ABE" denote the IBE→ABE Type ES (in Section III-C), "BB-IBE" is the first construction in [9], respectively. The figure 1(a) shows the time spent in re-encryption key (w.r.t. ABE-IBE and IBE-ABE) and decryption key (w.r.t. Waters-ABE and BB-IBE) generation. IBE→ABE Type ES requires the longest time in the key preparation (nearly 0.52 s), while Waters-ABE and ABE→IBE Type ES share similar time complexity (around 0.18 s). The cost of time for BB-IBE is constant (approximately 0.01 s) because there is only one attribute, i.e. identity, embedded into the key. The figure 1(b) is about the complexity of re-encryption in our ESs. It can be seen that IBE-ABE (nearly 0.4 s) outperforms ABE-IBE (around 0.88 s). This is so because the re-encryption in the conversion from ABE to IBE requires the cost of pairings which is linear with the size of row matching set I (while the re-encryption of IBE-ABE is in the cost of constant pairings). It is worth of mentioning that the re-encryption burden in our ESs can be off-loaded to cloud server. The decryption complexity comparison is shown in the figure 1(c). The cost of ABE-IBE and BB-IBE is constant (only using constant number of pairings), nearly 0.1s, while IBE-ABE suffers from the worst performance, 2.5 s (due to a fact that two linear groups of pairings are required in decryption). In general, from the simulation results shown among the Figures, we can state that the cost incurred by our ESs is acceptable in practice (with best performance $<$1 s and the worst case 2.5 s).

VI. CONCLUSIONS

In this paper we have introduced encryption switching between IBE and ABE which is the first of its type in the literature. The security notion has been defined in the game-based framework. We have presented a concrete construction and meanwhile proved it to be CPA secure in the standard

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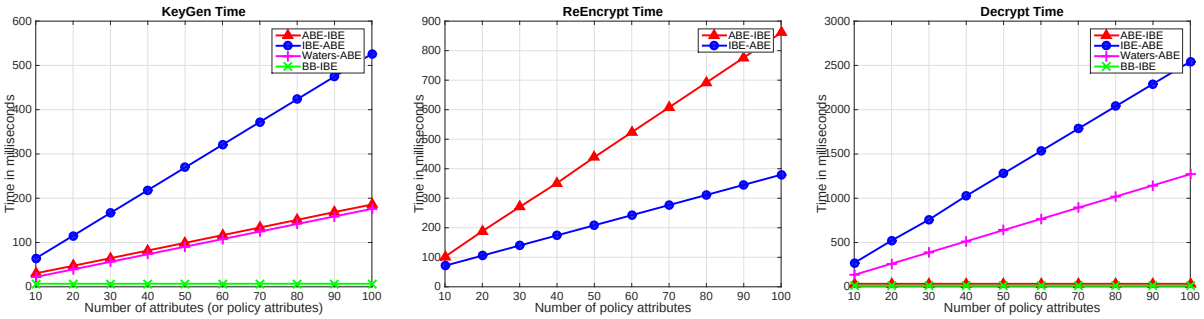

(a) keygen time (b) reencrypt time (c) decryption time

model under the decisional q-parallel BDHE assumption. The efficiency analysis has highlighted that our solution outperforms the download-and-re-encrypt conversion mode w.r.t. computation and communication cost. At last, the simulation results have shown that the computational complexity in terms of re-encryption and decryption (in our construction) are in the acceptable range, e.g., around 0.9 s and 2.5 s for ABE→IBE re-encryption and decryption, respectively. Some interesting open problems have been incurred from this work as well, for example, how to shorten the re-encrypt and decrypt time at the case of ABE→IBE, and seek an approach to achieve simulation-based security.

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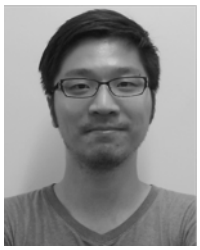

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