Pairing-based public-key encryption schemes with backward-and-forward security

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Identity-based cryptosystems utilize some arbitrary strings as the participants' public key in the underlying system. The encryptioner will not need to obtain the decryptioner's certificate. That will simplify the certificate management. Therefore, it is still interesting to propose some new identity-based encryption schemes. In this paper, we will propose two new different constructions, i.e. *receiptor-oriented encryption schemes*. They are both identity-based encryption schemes and also based on pairings. The proposed encryption schemes have a new advantage, i.e. backward-and-forward security. In addition, we provide the security analysis for the proposed schemes.

Keywords: Semantic Security, Public Key Encryption, Bilinear Pairings, Backward-and-forward Security.

1. INTRODUCTION

Public key cryptography has been widely involved in today's digital life, such as network communication, wireless communication, smart cards, etc. [13, 16, 26]. Public key encryption technique plays an important role in its utilization of public key cryptography. Very recently, some new semantically secure encryption schemes are attracting attention. Galindo et al proposed two schemes [6, 7]. However, most of the previous encryption schemes have not provided several properties; One of these properties is backward-and-forward security, i.e. some partial keys of participants can be changed with ongoing time. This property is necessary, since an attacker may given all the time catch up with a targeted communication channel and try to break the underlying private key. Therefore, it is potentially important to construct new semantiscaly secure public key encryption schemes which have the above backward-and-forward security property. In this paper, we will propose two such schemes.

Identity-based cryptosystems and cryptographic protocols have also been paid more attention over the years since Shamir proposed the first identity-based encryptions and signatures [18]. The benefits of identity-based cryptosystems and cryptographic protocols are that they use some arbitrary strings as the participant's public key in the underlying schemes. Thus it will not need the encryptioner to obtain the decryptioner's certificate. Therefore, that will simplify certificate management [16]. Some identity-based signatures, encryptions, key agreement, and signcryption were proposed in references [2, 11, 12]. In this paper, we will propose two identity-based semantically secure encryption schemes.

Recently, the bilinear pairings modified from Weil or Tate pairings [1, 11] are becoming one of the new active research topics in information security. Especially, the supersingular curves are the main object used by the bilinear pairings. However, prior to [2, 11], the supersingular curves were undesirable in cryptographic settings since Weil pairing can reduce the discrete logarithm problems in supersingular curves to that in an extension of the underlying finite field. Thanks to Joux [11] and Boneh et al [2], the pairings have become desirable and applied to various cryptographic schemes: identity-based signa-

tures [11, 23], encryptions [2, 19], confirmer/undeniable signatures [14, 24, 24], key agreement [11], committal deniable signature [14], signcryption [12], and blind signature with message recovery [4, 21, 25]. Bilinear pairs were also used to construct a knapsack diffie-hellman family [8, 9].

In our paper, we will propose two new public key encryption schemes different from [2, 19]. And the new constructions are motivated by some techniques from references [3, 6, 7, 11, 12, 19].

The organization of the rest of our paper is as follows: The definition of receptor-oriented encryption scheme is presented in section 2. Section 3 provides the new cryptosystems. The security and efficiency analysis is given in section 4 and section 5, respectively. The conclusion is in section 6.

2. DEFINITIONS OF RECEPTOR-ORIENTED ENCRYPTIONS

In this section, the definition of the receptor-oriented encryption system is presented as follows. This follows [19].

Definition 1 (Receptor-Oriented Encryptions) A *receptor-oriented encryption* (abbr. *ROE*) scheme is a public key cryptosystem comprised of the following three procedures, and in which two entities (encryptioner and decryptioner) are involved:

(1) **Key Generation:** On input a security parameter ℓ, this probabilistic algorithm returns the long-term public keys and private keys for the encriptioner (pk_2, sk_2) and the decryptioner (pk_1, sk_1) respectively. Simultaneously, this algorithm also outputs a pair of specified time-stage(t_i) public key pk_{t_i} and private key sk_{t_i} for the *oriented receptor*, i.e. the decryptioner. The initialized time-stage is t_0. Therefore, the initial time-stage public key and private key for the decryptioner are pk_{t_0} and sk_{t_0}, respectively. The relationship of the three main keypairs (pk_1, sk_1), (pk_2, sk_2) and (pk_{t_i}, sk_{t_i}) are as follows: (pk_1, sk_1) and (pk_2, sk_2) are long-term keys, while (pk_{t_i}, sk_{t_i}) are short-term (i.e. specified time-stage) keys; Suppose a message m is encrypted in time-stage t_i: for encryption, the keys including pk_1, (pk_2, sk_2) and pk_{t_i} will be involved in the generation of a ciphertext c_{t_i} of m; for decryption, the keys (pk_1, sk_1), pk_2 and (pk_{t_i}, sk_{t_i}) will be involved in the generation of the plaintext (i.e. m) from c_{t_i}.

(2) **Encryption:** This is a probabilistic algorithm carried by the encryptioner. Given a plaintext m, the encryptioner will encrypt m by use of its own long-term public key pk_2 and private key sk_2. During the encrypting, the encryptioner will also use the oriented receptor's (i.e. *decryptioner's*) specified time-stage public key pk_{t_i} and long-term public key pk_1. In addition, some random elements chosen by the encryptioner will be involved. In the end, the encryptioner publishes the ciphertext C (of plaintext m) on its homepage. Furthermore, its homepage will be renewed in time.

(3) **Decryption:** This is an algorithm done by the decryptioner. The algorithm inputs the ciphertext C, the decryptioner's

long-term public key pk_1 and private key sk_1, its specified time-stage public key pk_{t_i} and private key sk_{t_i}, as well as the encryptioner's public key pk_2. In the end, the plaintext m will be returned.

Definition 2 (Requirements of a Secure ROE System) A *secure receptor oriented public key encryption* system must satisfy at least the following three requirements.

(1) **Soundness**: For any plaintext $m \in M$ (M is the plaintext space), and for any given time stage t_i, there always holds that:

$$D_{pk_1, pk_2, sk_1, sk_{t_i}, pk_{t_i}}(E_{pk_1, pk_2, sk_2, pk_{t_i}}(m, r)) = m \quad (1)$$

where E and D are the encryption and the decryption algorithms respectively; r is a random element chosen by the encryptioner; pk_1, pk_{t_i}, and sk_1, sk_{t_i} are the decryptioner's public keys and private keys respectively; pk_2 and sk_2 are the encryptioner's public and private keys, respectively.

(2) **Semantic Security**: For any $m_0 \in M$(M is the plaintext space), for any polynomial time attacker **A**, who can input the public keys of the encryptioner and decryptioner, cannot distinguish the ciphertext c (of plaintext m) from a random element $\phi \in_R C$ (C is the ciphertext space) in polynomial time.

(3) **Backward-and-Forward Security**: This property is with respect to the oriented receptor while its specified time-stage private sk_{t_i} is compromised by an attcker **A**. Backward-and-forward security means that even though an attacker **A** obtains the time-stage private sk_{t_i} for the time stage t_i, **A** is still not able to do the followings:

- figure out the plaintext of any ciphertext c encrypted during time-stage t_i.
- derive the former time-stage t_{i-1}'s private key $sk_{t_{i-1}}$ from sk_{t_i}.
- calculate the latter time-stage t_{i+1}'s private key $sk_{t_{i+1}}$ from sk_{t_i}.

3. ID-BASED ENCRYPTION SCHEMES

In this section we will propose two identity-based receptor-oriented encryption schemes (ID-based ROE schemes). We develop the constructions motivated by some techniques from [3, 6, 7, 12]. The proposed identity-based encryption schemes are based on pairings over elliptic curves. We will first review some mathematical tools, that will be used in the proposed schemes.

3.1 Notations

In this paper, we choose ℓ as the security parameter for all the proposed receptor-oriented encryption schemes. Let q be a large prime, and Z_q^* be $Z_q\backslash\{0\}$. F_q denotes a finite field with q elements. $\bigoplus$ denotes the bit-wise *XOR* calculation. Let n be a positive integer with $n = \bigcirc(\ell)$. Let H and H_1 be two cryptographic

hash functions: $H : \{0, 1\}^* \rightarrow G_1$, and $H_1 : G_2 \rightarrow \{0, 1\}^n$; where H_1 is a universal one-way hash function [11, 16]. G_1 and G_2 will be given later.

Definition 3 Let $p > 3$ be a prime. An elliptic curve over the the finite field F_p, denoted by $E_p(a, b)$ or $E(a, b)/F_p$, where $a, b \in F_p$, and $gcd(4a^3 + 27, b^2) = 1$, is the set of points $P_{(x,y)}$ such that $y^2 = (x^3 + ax + b) \bmod p$, together with a point $\hat{O}$ [15], called the point at infinity.

In our paper, we choose elliptic curves $E(a, b)/F_p$ with $y^2 = (x^3 + ax + b) \bmod p$ such that:

- $a = 0$; b is some random integer with $gcd(27b^2, p) = 1$. For simplicity, b may be equal 1.

- $p \equiv 2 \bmod 3$. In this case, the order of $E(0, b)/F_p$(the number of it) is $|E(0, b)/F_p| = p + 1$, and thus avoiding the difficulty of computing $|E(a, b)/F_p|$.

- the bit length of p is ℓ; and ℓ may be 160 or larger than it for security reason.

3.2 Pairings over Elliptic Curves

Let p be a sufficiently large prime that satisfies: (a) $p \equiv 2 \bmod 3$; (b) $p = 6q - 1$, where q is also a large prime. Consider the elliptic curves E/F_p defined by the equation:

$$y^2 = x^3 + 1. \tag{2}$$

Let G_1 be an additive group of points of prime order q on the elliptic curve E/F_p and let G_2 be a multiplicative group of same order q of some finite field F_{p^2}. We are able to derive a bilinear pairing from the Weil pairing or Tate pairing [1, 4]:

$$e : G_1 \times G_1 \rightarrow G_2 \tag{3}$$

with respect to which the Elliptic Curve Discrete Logarithm (ECDL) problems are difficult in G_1 and the Computational Diffi-Hellman (CDH) problems and the Inversion of Weil pairing (IWP) problem are difficult in G_2.

The pairing $e : G_1 \times G_1 \rightarrow G_2$ has the following properties:

(1) Bilinearity: $e(aP, bQ) = e(P, Q)^{ab}$ for every pair $P, Q \in G_1$ and for any $a, b \in Z_p$.

(2) Non-degenerate: there exists at least one point $P \in G_1$ such that $e(P, P) \neq 1$.

(3) Efficient Computability: there are efficient algorithms to compute the bilinear pairings e.

3.3 ID-based ROE Scheme 1

By the definition of ROE system in section 2, the ROE system 1 has three algorithms:

(1) **Key Generation** The KGC first chooses an elliptic curve E/F_p as in section 3. And then it chooses G_1, G_2, P, $e(*, *)$ as above in the same section. It then chooses $s \in Z_q$

and computes domain public key $P_{KGC} = sP$. The encryptioner and the receiptor-oriented decryptioner's respective identities id_2 and id_1 as their prime public keys. Then, the decryptioner's long-term public key and private key are respectively $S_1 = sQ_1$ and Q_1; the encryptioner's long-term public key and private key are respectively $S_2 = sQ_2$ and Q_2; where $Q_1 = H(id_1)$ and $Q_2 = H(id_2)$. Since the decryptioner is a *receiptor-oriented entity*, so by the definition she will have a pair of specified time-stage private key sk_{t_i} and public key pk_{t_i}. The initialized time-stage is t_0. Therefore, the initial time-stage public key and private key for the decryptioner may take $pk_{t_0} = \upsilon P$ and $sk_{t_0} = \upsilon$, respectively. In addition, the plaintext space is $M = \{0, 1\}^n$.

(2) **Encryption** This is a probabilistic algorithm done by the encryptioner. For any plaintext $m \in M$,

- the encryptioner chooses uniformly and randomly an element $r \in Z_q^*$, and computes $c_1 = rP$.
- the encryptioner then computes $c_2 = e(rQ_1, P_{KGC}) \, e(S_2, \upsilon P)$, and $c_3 = H_1(c_2)$, respectively.
- At the last step, he computes $c_4 = c_3 \oplus m$.

Then, he publishes the ciphertext $\{c_1, c_4\}$.

(3) **Decryption** This is a deterministic algorithm done by the receiptor-oriented decryptioner. Given the ciphertext $\{c_1, c_4\}$,

- she first calculates $d_1 = e(\upsilon Q_2, P_{KGC}) \cdot e(S_1, c_1)$.
- she then calculates $d_2 = H_1(d_1)$.
- she recovers the plaintext by $m = d_2 \oplus c_4$. If the ciphertext is invalid one, then she recovers nothing ⊔.

In the above encryption algorithm, the computation of ciphertext of plaintext m combines the encryptioner's public and private keys with the decryptioner's public key and the specified time-stage public key. In addition, some random elements and a universal collision-free one-way hash function are also involved.

3.4 ID-based ROE Scheme 2

By the definition of ROE system in section 2, the ROE system 2 has three algorithms:

(1) **Key Generation** The KGC first chooses an elliptic curve E/F_p as in section 3. And then it chooses G_1, G_2, P, $e(*, *)$ as above in the same section. It then chooses $s \in Z_q$ and computes domain public key $P_{KGC} = sP$. The encryptioner and the receiptor-oriented decryptioner's respective identities id_2 and id_1 as their prime public keys. Then, the decryptioner's long-term public key and private key are respectively $S_1 = sQ_1$ and Q_1; the encryptioner's long-term public key and private key are respectively $S_2 = sQ_2$ and Q_2; where $Q_1 = H(id_1)$ and $Q_2 = H(id_2)$. Since the decryptioner is a receiptor-oriented entity, so by the definition she will have a pair of specified time-stage private key sk_{t_i} and public key pk_{t_i}. The initialized time-stage is t_0. Therefore, the initial time-stage public key and private key for the decryptioner may (without loss of generality) take $pk_{t_0} = \alpha Q_1$ and $sk_{t_0} = \alpha$, respectively.

(2) **Encryption** This is a polynomially probabilistic algorithm done by the encryptioner. For any plaintext $m \in M$,

- the encryptioner chooses uniformly and randomly an element $r \in Z_q^*$, and computes $c_1 = rQ_2$.

- the encryptioner then computes $c_2 = e(\alpha Q_1 + rQ_1, S_2)$, and $c_3 = H_1(c_2)$, respectively.

- At the last step, he computes $c_4 = c_3 \oplus m$.

Then, he publishes the ciphertext $\{c_1, c_4\}$.

(3) **Decryption** This is a deterministic algorithm done by the receiptor-oriented decryptioner. Given the ciphertext $\{c_1, c_4\}$,

- she first calculates $d_1 = e(c_1 + \alpha Q_2, S_1)$.

- she then calculates $d_2 = H_1(d_1)$.

- she recovers the plaintext by $m = d_2 \oplus c_4$. If the ciphertext is invalid one, then she recovers nothing $\sqcup$.

It is easy to see the difference between the above two ROE schemes is that the former has two pairing evaluations on both encryption and decryption; and the latter has only one such evaluation. Probably, the second one is more efficient than the first. Fortunately, in identity-based ROE system 1, one of the two pairing evaluations could be preprocessed.

4. SECURITY ANALYSIS

In this section, we will prove that both of the two identity-based ROE schemes have the soundness, semantic security, and backward-and-forward security.

4.1 Soundness

The soundness of the receiptor-oriented encryption schemes is that: if the encryptioner correctly calculates the ciphertexts according to the descriptions of encryption algorithm, and if the decryptioner correctly carries on the decryption algorithm, then the latter will surely recovers the corresponding plaintexts.

Theorem 1 The two identity-based receiptor-oriented encryption schemes in section 4 both have the soundness. In other words, if $\{c_1, c_4\}$ is a legal ciphertext returned by the encryptioner on plaintext $m \in \{0, 1\}^n$, then the decryptioner will surely recovers the plaintext $m \in \{0, 1\}^n$ such that

$$D_{Q_1, Q_2, S_1, sk_{t_0}, pk_{t_0}}(E_{Q_2, Q_1, S_2, pk_{t_0}}(m, r)) = m \quad (4)$$

where E and D are the encryption and the decryption algorithms, respectively; r is a random element chosen by the encryptioner; and other data are the same to what are in the two identity-based ROE schemes in section 4.

Proof. Because of the similar proofs on the two ROE schemes, the authors only present the theorem proof for the identity-based ROE system 1.

By the encryption algorithm of the identity-based ROE system 1, we can write

$c_1 = rP$;
$c_2 = e(rQ_1, P_{KGC})e(S_2, \upsilon P)(\text{mod } q)$;
$c_3 = H(c_2)$;
$c_4 = c_3 \oplus m$.
where $r \in Z_q^*$ is a random element.

Since $d_1 = e(\upsilon Q_2, P_{KGC}) \cdot e(S_1, c_1)$, and by the key generation algorithm, therefore $d_1 = e(\upsilon Q_2, P_{KGC}) \cdot e(S_1, c_1)$
$= e(\upsilon Q_2, sP)e(sQ_1, c_1)$
$= e(Q_2, P)^{s\upsilon}e(Q_1, P)^{sr}(\text{mod } q)$
$= e(sQ_2, \upsilon P) \cdot e(rQ_1, sP)$
$= e(S_2, \upsilon P) \cdot e(rQ_1, P_{KGC})$
$= c_2(\text{mod } q)$
Hence,

$$d_2 = c_3.$$

Thus, the recovered plaintext is

$$m = c_3 \oplus c_4 = d_2 \oplus c_4.$$

Therefore, the soundness is satisfied in this system.

4.2 Semantic Security

The semantic security of the receiptor-oriented encryption schemes is that: if for any plaintext $m_0 \in \{0, 1\}^n$(the plaintext space), for any polynomial time attacker **A**, who can input the public keys of the encryptioner and decryptioner, cannot distinguish the ciphertext c(of plaintext m) from a random element $\phi \in_R C$ (C is the ciphertext space) in polynomial time.

Theorem 2 The two identity-based receiptor-oriented encryption schemes in section 4 both have the semantic security. In other words, if $\{c_1, c_4\}$ is any legal ciphertext returned by the encryptioner on plaintext $m \in \{0, 1\}^n$, then any probabilistic polynomial time attacker A will distinguish between $\{c_1, c_4\}$ and $\{\Phi, \Psi\}$ with negligible probability; where Φ and Ψ are two random elements belonging to G_1 and G_2, respectively.

Proof. Notice that, by the descriptions on encryption algorithms of the identity-based receiptor-oriented encryption system 1 in section 4, and without of generality, we may let $c_1 = \zeta P$
$c_2 = e(\zeta Q_1, P_{KGC})e(S_2, pk_{t_i})(\text{mod } q)$
$c_3 = H_1(c_2)$
$c_4 = c_3 \oplus m$.
where $\zeta \in Z_q^*$ is an unknown (with respect to A) random element; pk_{t_i} and Q_1 are the decryptioner's specified time-stage public key and long-term public key, respectively. m is any plaintext in $\{0, 1\}^n$. P_{KGC} is the domain public parameter.

Since ζ is a random element in Z_q^*, $c_1 = \zeta P$ is a random element in G_1. In addition, c_2 is also random in G_2 since $e(*, *)$ is a bilinear map from $G_1 \times G_1$ to G_2. Therefore, by the definition of universal collision-free one-way hash function [11], we know that $c_4 = c_3 \oplus m$ is a random element in G_2. What's more, the attacker A does not know the value of $\zeta \in Z_q^*$ and $S_2 \in G_1$. Hence, from the point of view of the attacker A, $\{c_1, c_4\}$ is a random pair in $G_1 \times G_2$. Therefore, the probability of attacker A tells $\{c_1, c_4\}$ from $\{\Phi, \Psi\}$ is approximately $1/q^2$.

According to the above analysis, any probabilistic polynomial time attacker A will distinguish between $\{c_1, c_4\}$ and $\{\Phi, \Psi\}$ only with negligible probability.

4.3 Backward-and-Forward Security

The backward-and-forward security is formalized with respect to the *oriented receiptor* while its specified time-stage private sk_{t_i} is compromised by a probabilistic polynomial time attcker **A**. Backward-and-future security means that even though attacker **A** obtains the time-stage private sk_{t_i} for the time stage t_i, **A** is still not able to: (1) figure out the corresponding plaintext of any ciphertext c encrypted during time-stage t_i; (2) derive the former time-stage t_{i-1}'s private key $sk_{t_{i-1}}$ from sk_{t_i}; (3) calculate the latter time-stage t_{i+1}'s private key $sk_{t_{i+1}}$ based on sk_{t_i}.

Theorem 3 The two identity based receiptor-oriented encryption schemes in section 4 both have the backward-and-forward security defined in section 2.

Proof. Due to the similar construction of the two identity based ROE schemes, we will prove this theorem with identity based ROE system 1.

Without of generality, we may assume there is a probabilistic polynomial time attacker **A**, who already (because of some special reason) compromised the time-stage private key sk_{t_i} of the decryptioner during the course of t_i. In addition, suppose $\{c_1, c_4\}$ is any legal ciphertext on an arbitrary plaintext m enciphered by the encryptioner. To complete the proof, we may by the encryption algorithm assume that $c_1 = \eta P$;

$c_2 = e(\eta Q_1, sP)e(sQ_2, vP)$;

$c_3 = H_1(c_2)$;

$c_4 = c_3 \oplus m$.

where η is a random element; and the compromised private key by attacker **A** is $sk_{t_i} = v$.

Now we will prove the probabilistic polynomial time attacker **A** will not be able to:

(1) figure out the corresponding plaintext m of $\{c_1, c_4\}$;

(2) derive the former time-stage private key $sk_{t_{i-1}}$ (of the decrytioner) from $sk_{t_i} = vP$;

(3) calculate the latter time-stage private key $sk_{t_{i+1}}$ (of the decryptioner) based on $sk_{t_i} = vP$.

Notice that η and s are both hidden i.e. unknown by the attacker **A** from the information theoretical view. Therefore,

(1) By the assumption of ECDL, **A** is not able to inverse η from $c_1 = \eta P$. At the same time,

$$c_2 = e(\eta Q_1, sP)e(sQ_2, vP)$$
$$= e(\eta Q_1, P)^s e(sQ_2, P)^v$$
$$= e(s\eta Q_1, P)e(vsQ_2, P)$$
$$= e(s\eta Q_1 + vsQ_2, P)$$

By the IWP assumption, **A** is not able to compute d_1. Consequently, **A** is not able to figure $d_2 = H_1(d_1)$. Therefore, she is not able to figure out the plaintext $m = d_3 = d_2 \oplus d_4$.

(2) By the construction of the identity based ROE system 1, both the decryptioner's time-stage private key sk_{t_i} and $sk_{t_{i-1}}$ are randomly and uniformly chosen by the decrypitoner from Z_q^*. Therefore, from the point of view of attacker **A**,

sk_{t_i} and $sk_{t_{i-1}}$ have no relationship useful to attacker **A**. Thus, she will be not able to derive the former time-stage private key $sk_{t_{i-1}}$ from sk_{t_i}.

(3) Due to the similar reason as above (2), attacker **A** is not able to calculate the latter time-stage private key $sk_{t_{i+1}}$ (of the decryptioner) based on $sk_{t_i} = vP$.

5. PERFORMANCE COMPARISON

When all the new proposed semantically secure encryption schemes are implemented, the performance of them is dominated by the *encryption* algorithm and the *decryption* algorithm respectively.

We first investigate the *expansion factor*, i.e. the ratio between the lengths of the cipher text and the plaintext. The expansion factor of the proposed new schemes is the same as that of [2]. By this definition, we can use some compression technique applying to the cipher text $\{c_1, c_4\}$ (of message m) to get its length equal to c_4 [19]. Therefore, the expansion factor of all our new schemes is 1, and at most 2. In terms of encryption algorithms, the dominated computation is the bilinear pairing evaluation. The encryption for identity-based ROE system 1 needs two bilinear pairing evaluations, and one of them can be precomputed. While id-based ROE system 2 only needs one pairing evaluation. Because of the symmetric construction of the encryption and decryption algorithms, so they have the same computation workloads. On the other hand, our schemes are identity-based encryption schemes, while those in [6, 7, 19] are not identity-based ones. Therefore, our encryption schemes are better than those of [6, 7, 19], from the certificate management point of view [16]. In addition, the scheme in [19] involves two pairing evaluations, while the proposed scheme only needs one evaluation.

The following table presents the complexity comparison of the encryption algorithm between the Scheme in [2] and the new ROE scheme 2 in our paper. Please refer to the appendix.

Table 1 Comparison between Encryption algorithm in reference [2] and the ROE scheme 2

Complexity comparison	ROE scheme 2	Scheme in reference [2]
Pairing evaluation	1	1
Map-to-point has operation in G_1	0	1
Scalar multiplication in G_1	2	1
Group exponent in G_2	0	1
XOR operation	1	1
Hash operation in G_2	1	1
Backward-and-forward security	available	not available

6.   CONCLUSION

This paper proposed two identity-based receptor-oriented encryption schemes: id-based ROE scheme 1 and id-based ROE scheme 2. Both of the proposed encryption schemes have a new security characteristic, namely backward-and-forward security. This means that if an attacker were able to obtain the private key for a particular time stage, be it not able to obtain the former and later time stage private keys not is it able to figure out the plaintext corresponding to ciphertext encrypted at that time stage. In addition, We proved that both of the new schemes possess soundness, semantic security, and backward-and-forward security. A complexity comparison was presented. From the complexity comparison, the id-based ROE scheme 2 is more efficient and reliable in terms of backward-and-forward security.

Acknowledgements

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