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Convective Heat Transfer In Airflow Through A Duct With

Wall Thermal Radiation

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Abstract. This paper presents a numerical investigation on airflow through a heated horizontal rectangular duct wherein the model considers the combined modes of natural and forced convection heat transfer and the thermal radiation from duct walls. The duct periphery is differentially heated with known temperature profiles imposed on the two opposite vertical sidewalls while the other two walls are treated as adiabatic. The air enters into the duct hydrodynamically fully developed and flows steadily under laminar conditions undergoing thermal development within the duct. Considering several temperature profiles on the two vertical sidewalls, the numerical simulation generates the heat transfer rates and associated fluid flow patterns in the duct for a range of airflow rates, duct aspect ratios and surface emissivity. The variation of local Nusselt number at duct walls and the fluid flow patterns are critically examined to identify thermal instabilities and the significance of wall thermal radiation effects on the overall heat transfer rates.

1. Introduction

Clear understanding of heat and fluid flow characteristics in heated ducts is essential for developing reliable design tools for a wide range of thermal energy conversion devices such as compact heat exchangers, electronic circuitry cooling systems and gas turbine blade cooling. Whilst the heat flow processes within ducts are fundamentally based on the combined mechanics of convection and thermal radiation, most research work on heated ducts ignores these multimode heat transfer behaviour to simplify complexities of analytical models. They often overlook the relevance of natural convection in flow through heated ducts and predominantly focus on forced convection mechanism with no account for wall thermal radiation. This reflects a major deficiency in the current state of the thermal design technology for heated ducts.

In heated ducts, the external heating induces a lateral fluid movement called secondary flow, which is essentially the buoyancy-driven natural convection current superimposed on the main axial flow. The orientation of wall heating is a primary factor affecting the characteristics of secondary flow. In view of this, the early studies have examined fluid flows in rectangular ducts heated only at the bottom wall. The experimental work on laminar airflow in a bottom-heated duct by Incropera and Maughan [1,2] showed a special flow condition called thermal instability, which is indicated by fluctuating Nusselt number. In a similar study by Nyce et al.[3], the secondary fluid movement was found to be independent of flow Reynolds number and the thermal instability was observed even at a low Reynolds number of 18.75. For a duct cooled at the top wall, Huang and Lin [4] observed a flow

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transition from steady laminar longitudinal vortex flow to unsteady chaotic flow, which did not occur in ducts heated from the bottom.

The literature reports only a limited number of studies with sidewall heating. Silekens et al.[5] examined rectangular ducts with symmetrical heating at the two opposite sidewalls and have illustrated that the thermally induced secondary flow would substantial increase heat transfer. Examining mixed convection in a rectangular duct heated from one side wall, Gau et al.[6] concluded that fluid stratification in the upper duct section would reduce the overall heat transfer rate to the fluid. A study by Corcione [7] has shown that the bottom wall heat transfer rates could be improved if the side vertical walls were cooled (or heated) instead of insulating them.

The published literature reports only a very few studies on heated ducts incorporating mixed mode analysis of convective heat transfer mechanisms and surface thermal radiation. This is because analytical models could be highly simplified by assuming negligible interaction between thermal radiation and convection in flow through ducts. While significance of radiation is customarily associated with high temperature situations, recent evidence strongly suggests that even at moderate surface temperatures, thermal radiation not only substantially contributes towards the mixed mode heat transfer, but also enhances natural convection process to promote overall heat dissipation rates in heated ducts [15,16,17,18]. One such limited study by Yang and Ebadian[8] concludes that the duct wall emissivity significantly influences the combined heat transfer rates wherein the total Nusselt number increases with higher surface radiation effects.

In a differentially heated duct, the thermal radiation from externally heated walls would alter the equilibrium surface temperature of unheated walls. This in turn will change not only the intensity of thermally induced convection currents, but also the overall heat dissipation from (heated and unheated) duct walls to the fluid. Thus, a careful examination of both radiative and convective heat transfer processes is necessary for a more realistic description of heat transfer characteristics in differentially heated ducts. The present numerical study performs a parametric investigation on the airflow through a horizontal duct with specified wall heating configurations to ascertain the significance of mixed convection and surface radiation towards the overall heat transfer rates.

2. Nomenclature

А	[m ²]	Duct cross sectional area
AR	[-]	Duct aspect ratio W/H
D _h	[m]	Hydraulic diameter 2WH/(W+H)
g	$[m/s^2]$	Gravitational acceleration
Gr	[-]	Grashof number Gr=g $(T_h-T_c) H^3/^2$
Gr*	[-]	Modified Grashof number $Gr=g q''H^4/k^2$
h	$[W/m^2 \cdot K]$	Heat transfer coefficient
Н	[m]	Duct height
k	[W/m·K]	Thermal conductivity
L	[m]	Duct length
Nu	[-]	Nusselt number Nu=h D_{h}/k
Pr	[-]	Prandtl number
Pl	[-]	Planck number
q‴	$[W/m^2]$	Heat flux - convective or radiative
Ra	[-]	Rayleigh number GrPr
Re	[-]	Reynolds number $U_{in}D_{b}$
Т	[K]	Temperature
T*	[-]	Dimensionless temperature $(T-T_c)/(T_b-T_c)$
U	[m/s]	Average fluid velocity
u	[m/s]	Fluid velocity
W	[m]	Duct width
х	[m]	x-coordinate
у	[m]	y-coordinate
Ζ	[-]	Dimensionless z-coordinate

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Z	[m]	Coordinate z along duct axis
Spec	cial characters	
-	[1/K]	Thermal expansion coefficient
	[-]	Emissivity
	$[m^2/s]$	Kinematic viscosity
Subs	scripts	-
avg		Average
b		Bulk mean temperature
c		Cooled wall
con		Convection
h		Heated wall
in		Inlet
1		Local
rad		Radiation
tran		Transverse

3. Numerical model and solution

The geometrical model of the analysis is illustrated in Figure 1 and consists of a horizontal rectangular duct whose aspect ratio W/H is chosen to be 0.5, 1, and 2. A sufficient duct length is considered to ensure thermally fully developed conditions at the duct outlet. The duct circumference is differentially heated where known temperature profiles are applied to the two vertical walls while the two horizontal walls are assumed to be adiabatic. Three wall heating configurations used in the analysis are illustrated in Figure 2. In these, the cold wall is kept at a constant temperature of 300 K while a maximum temperature of 350 K is considered for the hot wall. The airflow through the duct is taken to be laminar and hydrodynamically fully developed. The physical properties of air are assumed to vary linearly with temperature and are evaluated for conditions at duct inlet [10].



Figure 1. Geometrical model of duct

Based on the geometrical model, the solution domain with a grid structure is prepared and solved using the computational fluid dynamics solver FLUENT [14]. The Body Force Weight scheme is used for pressure discretisation to capture the effects of natural convection. It is assumed that, the walls are diffuse reflectors and emitters, while the working fluid is a radiatively non-participating medium. The Discrete Ordinates Method (DOM) is chosen to model the surface radiation heat transfer among internal duct walls, as it provides a better compatibility with the finite volume method used for the analysis. The SIMPLE algorithm is applied to the pressure-velocity coupling. Momentum and energy equations are discretised under the second order upwind scheme.

The operating parameters for the present study are selected to obtain Grashof number in the range of $2x10^3 \cdot \text{Gr} \cdot 1x10^6$ at a fixed Reynolds number of 100. Two emissivity values of 0.05 and 0.85 are considered for the simulation to obtain extreme conditions for surface thermal radiation.

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Figure 2. Duct wall heating configurations

The numerical solution is assumed to have converged when the net residual of the total heat transfer rates for successive iteration cycles is less than one percent. This convergence criterion ensured that the scaled residuals of mass and momentum fluxes were also less than 10^{-4} and 10^{-5} , respectively. The grid sensitivity analysis was also performed for a range of grid sizes. A grid of 50x50x400 provided less than 0.2 percent deviation in Nusselt number and was chosen as the suitable grid size for the simulation.

From the converged solution, the individual heat transfer rates due to mixed convection and surface thermal radiation are separately evaluated. Using these values, the convective Nusselt number Nu_{con} and the radiative Nusselt number Nu_{rad} are computed from the definition of the local Nusselt number,

$$Nu_{l} = \frac{q^{\prime\prime}D_{h}}{k(T_{w} - T_{h})}$$
(1)

where $q^{"}$ is the convective or radiative heat flux depending on the quantity to be evaluated. In Equation (1), the bulk mean fluid temperature T_{h} at duct cross section is given by,

$$T_{b}(z) = \frac{1}{U(z)A} \int u(x, y, z) T(x, y, z) dA$$
⁽²⁾

where U(z) is the average fluid velocity for each cross section. The average Nu for each cross section (transverse average) along the heated wall is then evaluated from,

$$Nu_{tran,avg,h} = \frac{\sum_{Y=0}^{Y=1} Nu_1}{N}$$
(3)

where N is the number of Nu_i nodal values on the heated wall. The total Nusselt number Nu_{total} is computed from,

$$Nu_{total} = Nu_{con} + Nu_{rad}$$
(4)

4. Results and Discussion

4.1. Mixed forced and natural convection effects

For all duct aspect ratios, the transverse average convective Nusselt number at any duct cross section rapidly increases with Grashof number, as typically illustrated in Figure 3 for Case (1) wall heating configuration. This clearly indicates the favourable contribution from natural convection to the overall heat transfer process in heated ducts.

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Figure 3. Variation of transverse average convective Nusselt number for AR=1 and = 0.05

When Gr is low (Gr = 2000 and 5000), the flow is dominated by forced convection. The Nu follows the conventional behaviour where it steadily declines with the thermally development of the flow due to the growth of thermal boundary layer. This trend changes when Gr is about 100,000 where the natural convection effects are manifested in the flow and mixed convection becomes significant. Then, Nu shows a marginal reduction at first near duct inlet and reaches a near-constant value over the rest of the duct. For Gr above 100,000, Nu does not show a reduction at duct inlet as for lower Gr and increases towards a steady value. A physical explanation is given below for the behaviour with Gr > 100,000.

For $Gr \ge 100,000$, the differentially heated sidewalls induce convection currents that are comparable in strength to the axial flow through the duct. This buoyancy-driven secondary fluid circulation interacts and shifts the axial flow towards the hot wall creating steeper velocity gradients there, as illustrated in Figure 4. Consequently, both natural and forced convection mechanisms at the hot wall are enhanced along with overall heat transfer rates to fluid. Similarly, the downward-directed buoyancy promotes the convective heat transfer at the cold wall.



Figure 4. Axial velocity contours and vectors in duct

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4.2. Effects of Radiation heat transfer

The most visible effects of thermal radiation are illustrated in Figure 5, which shows the temperature contours of the top and bottom adiabatic duct walls for cases of high and low wall surface emissivity.



Figure 5. Dimensionless temperature contours at the top and bottom duct walls along duct length

For $\varepsilon = 0.05$, the temperature contours are highly localised near the heated (or cooled) side of the duct while for $\varepsilon = 0.85$, the contours are more spread out over the wall surface. This indicates that the thermal radiation heat exchange among walls in fact acts to increase the average top wall temperature and decrease the bottom wall temperature. The impact of this temperature redistribution is seen from the comparison between Figures 3 and 6.



Figure 6 Variation of transverse average convective Nusselt number for AR=1 and = 0.85

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It is noted from Figure 6 that for high wall emissivity of 0.85, the convective Nusselt number shows a wavy appearance when Gr exceeds 100,000. Such behaviour is not present for identical cases with low wall emissivity of 0.05 shown in Figure 3. The wall surface radiation effects are therefore deduced to be the cause of these Nu fluctuations, which are referred to as thermal instability of the flow. Incropera and Maughan[1,2] have observed similar behaviour for Nusselt number in bottomheated ducts without attributing that to radiation effects. The current work is the first reported instance of thermal instability in ducts arising from thermal radiation effects and sidewall heating.

The thermal instability essentially originates from the interaction between natural convection currents at the sidewalls and the thermal boundary layers at the adiabatic walls. As observed previously in relation to Figure 5, the adiabatic duct walls are heated or cooled by the thermal radiation exchange among duct walls. This leads to the development of thicker thermal boundary layers at these walls. In flows dominated by natural convection (Gr > 100,000), the convection currents at sidewalls are stronger and interact vigorously with thermal boundary layers at top and bottom walls. Unstable flow regimes are then created at the top and bottom walls along with variable heat transfer characteristics, which are recognised as thermal instability. An exact mechanistic explanation for thermal instability has yet to be developed.

In flows with weak natural convection (Gr < 100,000), a poor interaction will occur between the convection currents at sidewalls and the thermal boundary layers at top and bottom walls. Therefore, the flow will not experience any significant fluid or thermal instability at the top and bottom walls due to thermal radiation effects.

Figure 7 considers the ratio of Nu_{total} for surface emissivities of 0.85 and 0.05, which illustrates the thermal radiation effects on the total heat transfer. A value greater than one for this ratio indicates the degree of overall heat transfer enhancement arising from the duct wall thermal radiation. In Figure 7, the ratio varies between 1.5 and 1.7, and indicates significant heat transfer enhancement vindicating that the thermal radiation is indeed an important consideration in heated ducts even at low wall temperatures.



Figure 7. Variation of the total Nusselt number ratio at high ($\varepsilon = 0.85$) and low ($\varepsilon = 0.05$) emissivities for Gr =1000,000

5. Conclusions

Considering the mechanisms of mixed convection and thermal radiation, a model has been successfully developed and used to examine the heat transfer characteristics of steady thermally developing laminar flow through a differentially heated horizontal rectangular duct. This novel investigation demonstrates the occurrence of thermal instability with duct sidewall heating and vindicates the significance of thermal radiation in heated ducts. The analysis clearly shows that mixed convection heat transfer rates are well above those achievable from forced convection-dominated

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flow. The surface radiation significantly alters the wall equilibrium temperature and generates thermal instability under certain conditions while enhancing the overall heat transfer rates. Even with low operating temperatures, the wall surface radiation in heated ducts makes a major contribution towards the total heat transfer rates.

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